

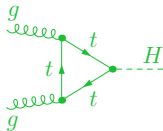
# MSSM Higgs Boson Production via Gluon Fusion

Heidi Rzehak

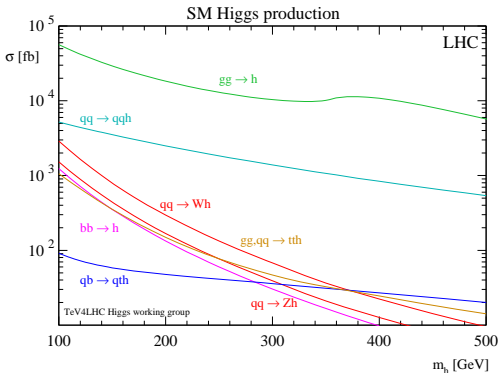
in coll. with M. Mühlleitner and M. Spira

- Higgs boson production via gluon fusion
- Decoupling of gluinos
- Genuine SUSY QCD contributions

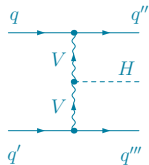
Gluon fusion:



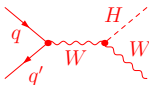
Largest cross section!



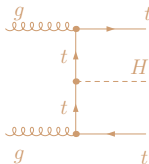
Weak boson fusion:



Higgs-strahlung:



Heavy quark fusion:

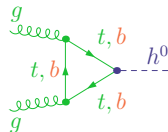


- Higgs production via gluon fusion with subsequent decay

- ▷ into photons:  $gg \rightarrow h^0 \rightarrow \gamma\gamma$

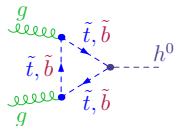
Possible discovery channel for

Higgs boson masses  $M_{h^0} \sim 120 \text{ GeV}$  [CMS 06, ATLAS 09]

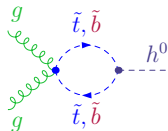


- ▷ into photons or other particles:  
Useful for coupling measurements

⇒ Need to know the cross section of  $gg \rightarrow h^0$

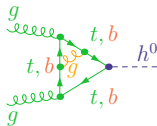


- Coupling of gluons,  $g$ , to the Higgs bosons is mediated via **quarks** and their superpartners **squarks**.  
(here:  $h^0$ , lightest MSSM Higgs boson)



- **Pure QCD (only gluons) corrections** to **quark** and **squark** loops with full mass dependence  
⇒ increase of the cross section of 100%.

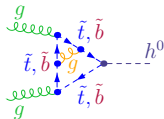
[Spira, Djouadi, Graudenz, Zerwas 92, 95; Graudenz, Spira, Zerwas 93;  
Anastasiou, Beerli, Bucherer, Daleo, Kunszt 07; Aglietti, Bonciani, Degrassi, Vicini 07;  
Bonciani, Degrassi, Vicini 07; Mühlleitner, Spira 08]



- **Pure QCD corrections** can be approximated by very heavy top quarks and squarks with 20 – 30 % accuracy for small  $\tan \beta$  (large  $\tan \beta$ : **bottom quark** and **squark** contributions are important).

$\tan \beta =$  ratio of Higgs vacuum expectation values

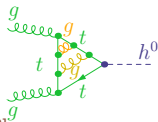
[Djouadi, Spira, Zerwas 91; Dawson 91; Kauffman, Schaffer 94; Dawson, Kauffman 94;  
Dawson, Djouadi, Spira 96; Krämer, Laenen, Spira 98]



- **NNLO QCD corrections** in the heavy top quark limit  
(no squarks included)

⇒ increase of the cross section by 20 – 30 %.

[Harlander, Kilgore 02, 02; Anastasiou, Melnikov 02, 03; Ravindran, Smith, van Neerven 03]



- Finite top quark mass effects at NNLO (no squarks)

⇒ below the scale uncertainty.

[Harlander, Ozeren 09, 09; Pak, Rogal, Steinhauser 09, 09; Harlander, Mantler, Marzani, Ozeren 09]

- Estimates of  $N^3$ LO corrections (no squarks)

⇒ improved convergence

[Catani, de Florian, Grazzini, Nason 07; Moch, Vogt 05; Ravindran 06, 06]

- Soft gluon resummation:  $\sim 10\%$  effects

[Catani, de Florian, Grazzini, Nason 07]

- Electroweak contributions:  $\sim 5\%$  effects

[Degrassi, Maltoni 04, Aglietti, Bonciani, Degrassi, Vicini 06,  
Actis, Passarino, Sturm, Uccirati 08, Anastasiou, Boughezal, Petriello 09]

- (SUSY) QCD (gluons and gluinos) contributions in the heavy top quark/squark and gluino limit:

Next term in the mass expansion indicates:

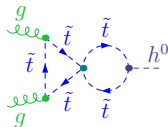
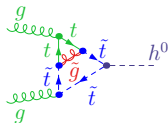
Approximation: Good for the lightest MSSM Higgs boson and small and moderate  $\tan \beta$  values.

[Harlander, Steinhauser 03,03, 04, Harlander, Hoffmann 06, Degrassi, Slavich 08]

- (SUSY) QCD contribution including the mass dependence of all particles (bottom quark/squark contributions included):

- ▷ The heavy mass limit approximation:  
Good for small and moderate  $\tan \beta$ .
- ▷ Contributions from squark quartic couplings and gluinos can be sizeable.

[Anastasiou, Beerli, Daleo 08]



On the one hand: Keeping supersymmetric relations between parameters intact

⇒ **gluinos** do not decouple

(For heavy gluinos: Result depends logarithmically on the **gluino mass**  $M_{\tilde{g}}$ .)

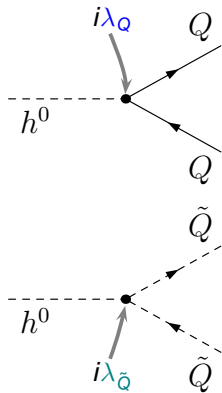
On the other hand: Decoupling theorem: [Appelquist, Carrazzone 75]

Heavy fields decouple at low momenta  
(except for renormalization effects).



# Decoupling of the Gluinos

Simplified scenario: no mixing, degenerate squark masses:



$$\lambda_Q = g \frac{m_Q}{v}$$

$$\lambda_{\tilde{Q}} = 2g \frac{m_Q^2}{v} = 2\frac{v}{g} \lambda_Q^2$$

SUSY relation

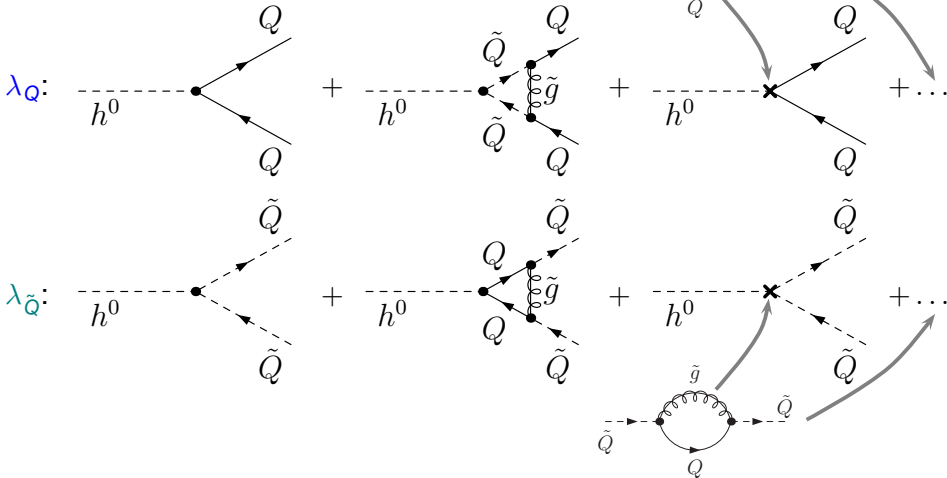
$m_Q$  = quark mass;

$v = (v_1^2 + v_2^2)^{\frac{1}{2}} \approx 246$  GeV,  $v_i$  = Higgs vacuum expectation value;

$g$  = norm. factor of the Higgs coupling to a quark pair with respect to the SM

# Decoupling of the Gluinos

In higher orders (1-loop):



Scales **above**  $M_{\tilde{g}}$ :  $\mu_R > M_{\tilde{g}}$

- Renormalization scheme:  
 **$\overline{MS}$**   
(only divergent parts in counterterms)
- RGE: (Renormalization group equations)  
**same** for  $\lambda_{\tilde{Q}}$  and  $2\frac{v}{g}\lambda_Q^2$
- Symmetry relation between  $\lambda_Q$  and  $\lambda_{\tilde{Q}}$  **intact**

Scales **below**  $M_{\tilde{g}}$ :  $\mu_R < M_{\tilde{g}}$

- Renormalization scheme:  
**momentum subtraction (MO)**  
(for decoupling of the gluino)
- RGE:  
**differ** for  $\lambda_{\tilde{Q}}$  and  $2\frac{v}{g}\lambda_Q^2$
- Symmetry relation between  $\lambda_Q$  and  $\lambda_{\tilde{Q}}$  **broken**

Matching **at** scale  $M_{\tilde{g}}$ :  $\mu_R = M_{\tilde{g}}$ :

- Threshold contributions

Taking into account the **mismatch** of the couplings  $\lambda_Q$  and  $\lambda_{\tilde{Q}}$  for  $\mu_R < M_{\tilde{g}}$ :

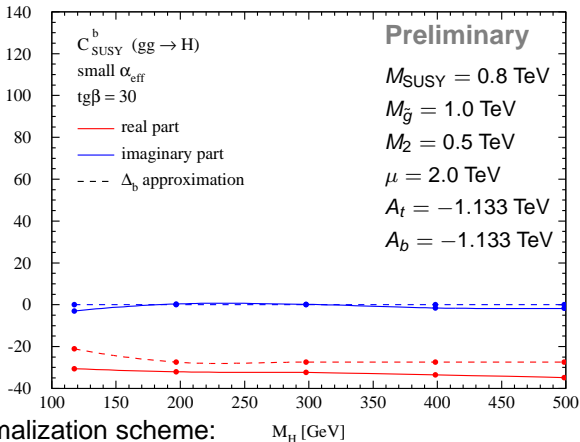
⇒ Gluino decouples from the theory [Mühlleitner, HR, Spira 08]

to the bottom quark/squark amplitude (with full mass dependence):

As form factor  $C_{\text{SUSY}}^b$ :

$$F_b^{\text{Higgs}} \left( 1 + C_{\text{SUSY}}^b \frac{\alpha_s}{\pi} \right)$$

$F_b^{\text{Higgs}}$ : bottom quark  
form factor



- Careful choice of renormalization scheme:

Here:  $A_b$  in  $\overline{\text{MS}}$  scheme [Mühlleitner, HR, Spira]

Other:  $A_b$  defined via vertex [Degrassi, Slavich 10]

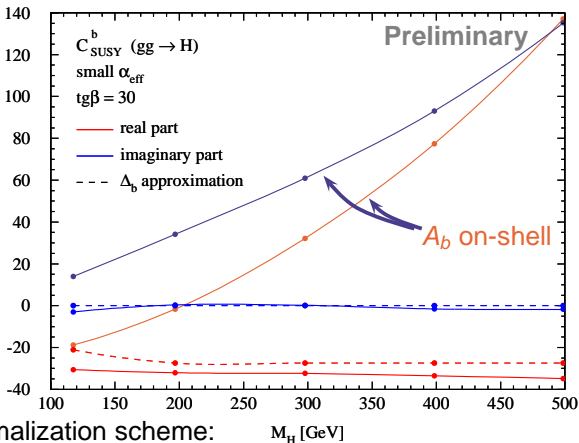
- $\Delta_b$  approximation (corrected bottom Yukawa coupling): Rough approx.

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$F_b^{\text{Higgs}}$ : bottom quark form factor



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- $\Delta_b$  approximation (corrected bottom Yukawa coupling): Rough approx.

- Gluon fusion:
  - ▷ A loop-induced Higgs boson production mechanism
  - ▷ Large cross section
- Cross section in the MSSM:
  - ▷ Pure QCD corrections: Large
  - ▷ SUSY QCD corrections: Sizeable
- For scales **below** the gluino mass:
  - ▷ **Symmetry relation** between Higgs couplings to quarks and to squarks: **Broken**
  - ▷ **Gluino decouples**
- **Genuine SUSY QCD contributions:**
  - ▷ **Sizeable**
  - ▷  $\Delta_b$  approximation works roughly.