Stop and Sbottom Sector Renormalization in the Complex MSSM

Sven Heinemeyer, IFCA (CSIC, Santander)

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based on collaboration with
Heidi Rzehak, Christian Schappacher

1. Introduction & The bigger picture
2. Renormalization schemes
3. Analysis of the renormalization schemes
4. Numerical results in the favored scheme
5. Conclusions & Outlook

1. Introduction

$\tilde{t}/\tilde{b}$ sector of the MSSM: (scalar partner of the top/bottom quark)

Stop, sbottom mass matrices ($X_t = A_t - \mu^*/\tan\beta$, $X_b = A_b - \mu^*\tan\beta$):

$$\mathbf{M}^2_{\tilde{t}} = \begin{pmatrix} M^2_{\tilde{t}_L} + m_t^2 + DT_{t_1} & m_t X_t^* \\ m_t X_t & M^2_{\tilde{t}_R} + m_t^2 + DT_{t_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{t}}} \begin{pmatrix} m^2_{\tilde{t}_1} & 0 \\ 0 & m^2_{\tilde{t}_2} \end{pmatrix}$$

$$\mathbf{M}^2_{\tilde{b}} = \begin{pmatrix} M^2_{\tilde{b}_L} + m_b^2 + DT_{b_1} & m_b X_b^* \\ m_b X_b & M^2_{\tilde{b}_R} + m_b^2 + DT_{b_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{b}}} \begin{pmatrix} m^2_{\tilde{b}_1} & 0 \\ 0 & m^2_{\tilde{b}_2} \end{pmatrix}$$

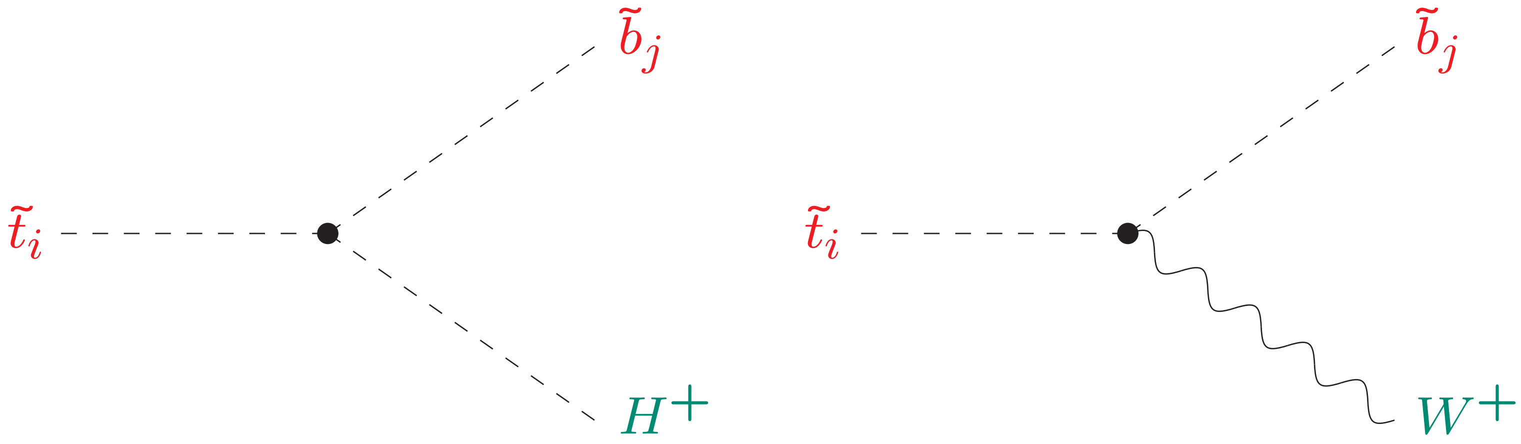
mixing important in stop sector (also in sbottom sector for large $\tan\beta$)

soft SUSY-breaking parameters A_t, A_b also appear in ϕ-$\tilde{t}/\tilde{b}$ couplings

$SU(2)$ relation $\Rightarrow M_{\tilde{t}_L} = M_{\tilde{b}_L}$

$\Rightarrow$ relation between $m_{\tilde{t}_1}, m_{\tilde{t}_2}, \theta_{\tilde{t}}, m_{\tilde{b}_1}, m_{\tilde{b}_2}, \theta_{\tilde{b}}$

Examples for processes with (external) stops and sbottoms:



- important decay modes of stops
- A_t and A_b directly enter the vertex
- possible source of charged Higgs bosons at the LHC
- ...

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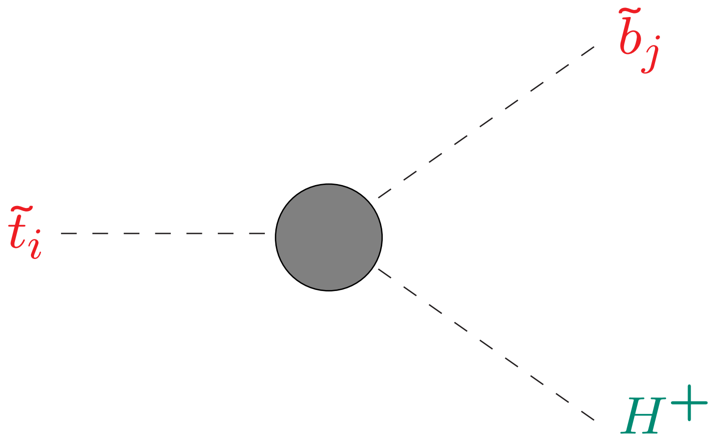

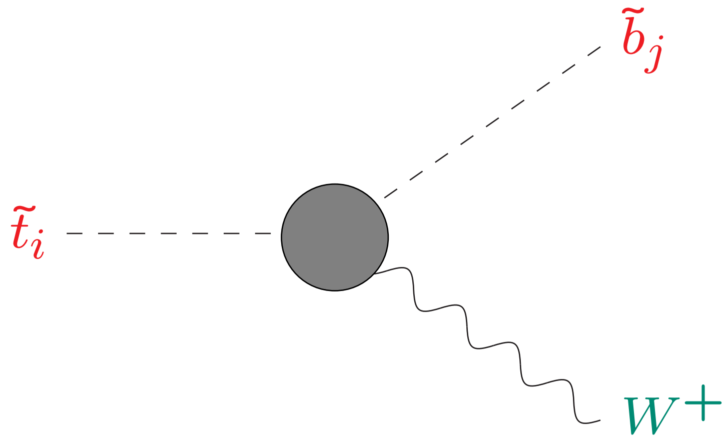

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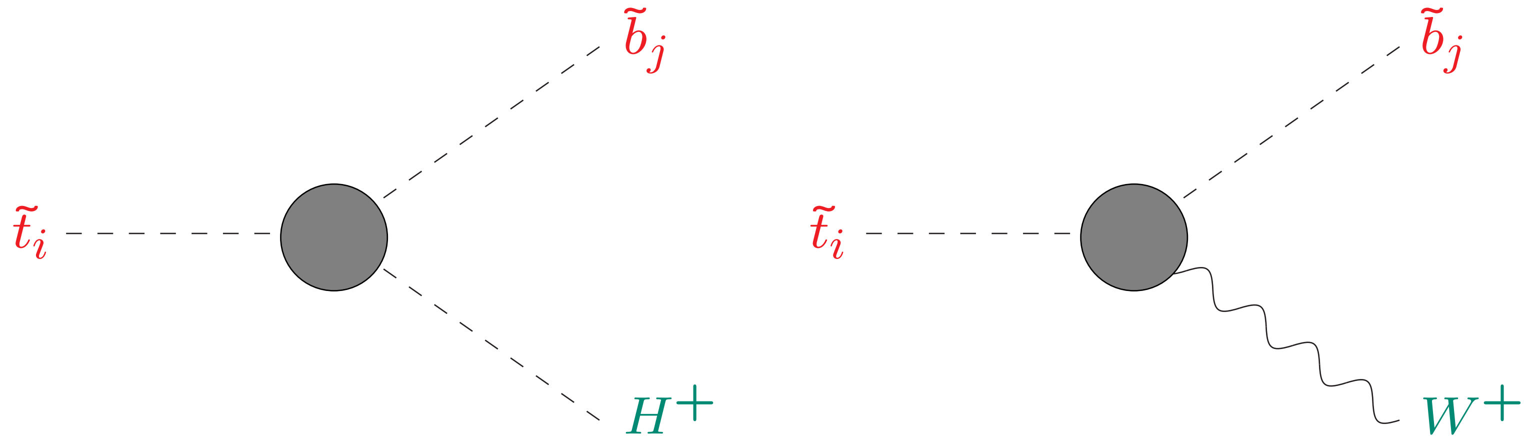

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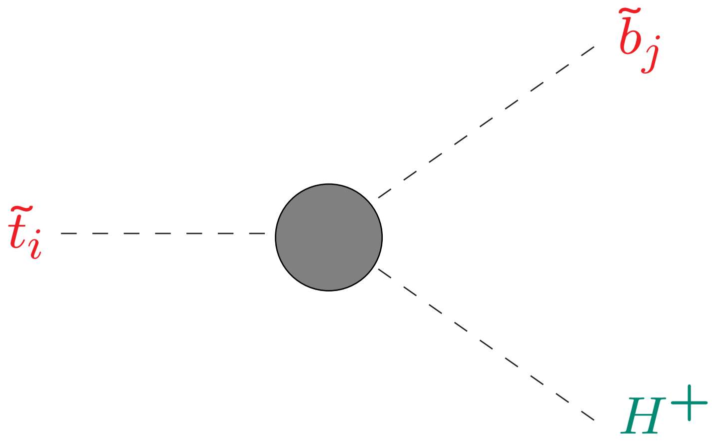

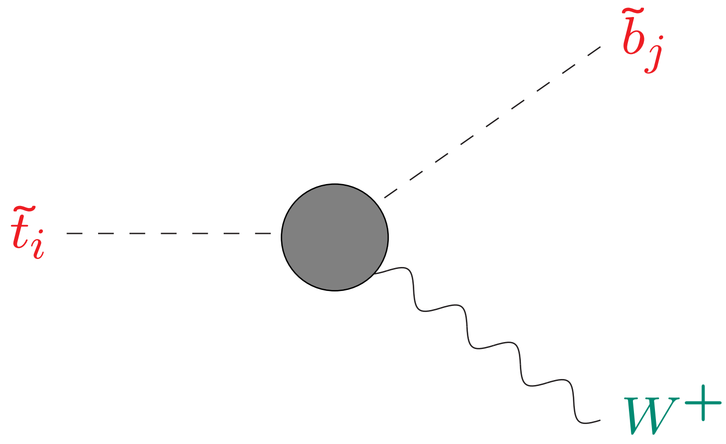

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– A_t and A_b directly enter the vertex
– possible source of charged Higgs bosons at the LHC
– . . .

⇒ higher-order corrections important!

⇒ simultaneous renormalization of stop and sbottom sector required!
⇒ with on-shell properties for external particles!

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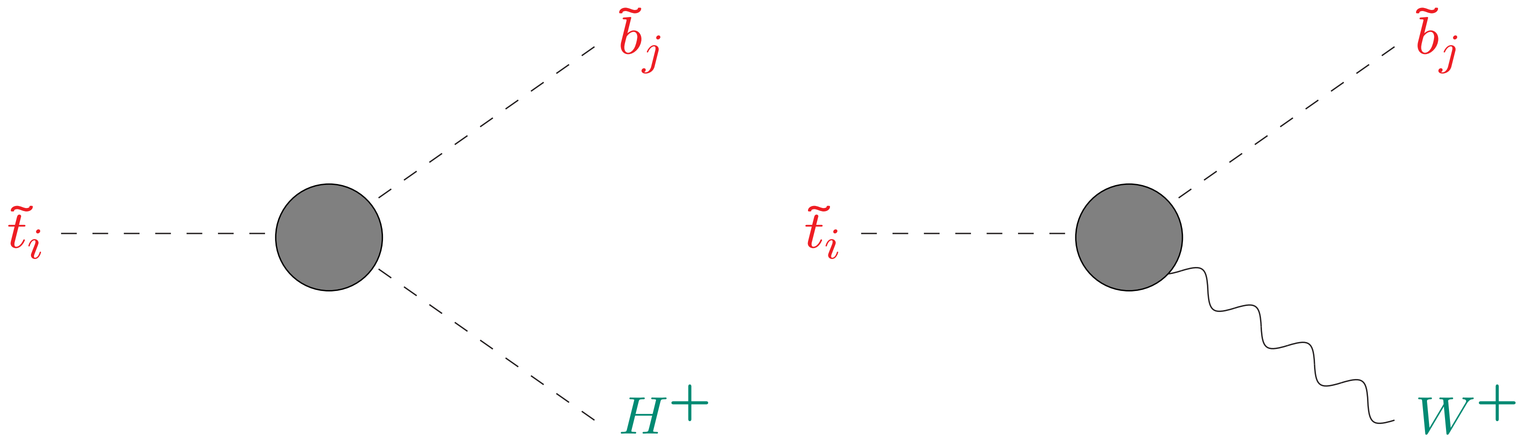


– important decay modes of stops

– A_t and A_b directly enter the vertex incl. complex phases!

– possible source of charged Higgs bosons at the LHC

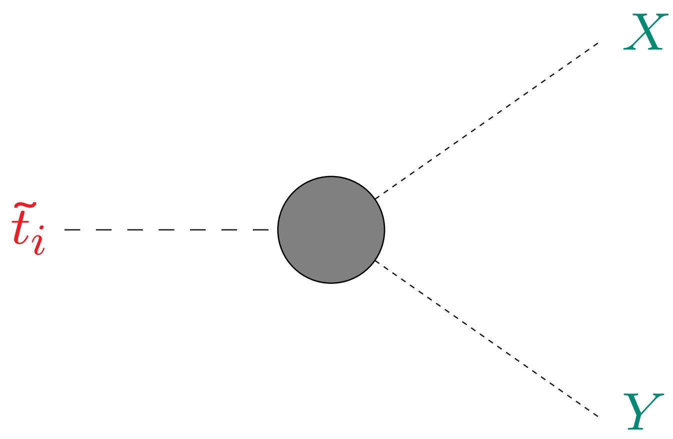
– . . .

⇒ higher-order corrections important!

⇒ simultaneous renormalization of stop and sbottom sector required!

⇒ including complex phases!

The bigger picture: stop decays in the cMSSM



– important for cascade decays at the LHC
– source of uncolored particles at the LHC
. . . especially for Higgs bosons

⇒ (nearly) all sectors of the cMSSM enter as external particles

⇒ (nearly) all sectors of the cMSSM have to be renormalized simultaneously

2. Renormalization schemes

Generic parameter and field renormalization for scalar quarks:

$$\mathbf{D}_{\tilde{q}} = \mathbf{U}_{\tilde{q}} \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger \quad (\tilde{q} = \tilde{t}, \tilde{b})$$

$$\mathbf{U}_{\tilde{q}} \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger \to \mathbf{U}_{\tilde{q}} \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger + \mathbf{U}_{\tilde{q}} \delta\mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger = \begin{pmatrix} m_{\tilde{q}_1}^2 & Y_q \\ Y_q^* & m_{\tilde{q}_2}^2 \end{pmatrix} + \begin{pmatrix} \delta m_{\tilde{q}_1}^2 & \delta Y_q \\ \delta Y_q^* & \delta m_{\tilde{q}_2}^2 \end{pmatrix}$$

$$\delta\mathbf{M}_{\tilde{q}12} = U_{\tilde{q}11}^* U_{\tilde{q}12} (\delta m_{\tilde{q}_1}^2 - \delta m_{\tilde{q}_2}^2) + U_{\tilde{q}11}^* U_{\tilde{q}22} \delta Y_q + U_{\tilde{q}12} U_{\tilde{q}21}^* \delta Y_q^*$$

$$\begin{pmatrix} \tilde{q}_1 \\ \tilde{q}_2 \end{pmatrix} \to \left(\mathbb{1} + \frac{1}{2}\delta\mathbf{Z}_{\tilde{q}}\right) \begin{pmatrix} \tilde{q}_1 \\ \tilde{q}_2 \end{pmatrix} \quad \text{with} \quad \delta\mathbf{Z}_{\tilde{q}} = \begin{pmatrix} \delta Z_{\tilde{q}_{11}} & \delta Z_{\tilde{q}_{12}} \\ \delta Z_{\tilde{q}_{21}} & \delta Z_{\tilde{q}_{22}} \end{pmatrix}$$

Renormalization of the $t/\tilde{t}$ sector

$\rightarrow$ employ the widely used on-shell renormalization

$$\delta m_t = \frac{1}{2}\widetilde{\mathrm{Re}}\left\{m_t\left[\Sigma_t^L(m_t^2) + \Sigma_t^R(m_t^2)\right] + \left[\Sigma_t^{SL}(m_t^2) + \Sigma_t^{SR}(m_t^2)\right]\right\}$$

$$\delta m_{\tilde{t}_i}^2 = \widetilde{\mathrm{Re}}\Sigma_{\tilde{t}_{ii}}(m_{\tilde{t}_i}^2) \qquad (i = 1, 2)$$

$$\delta Y_t = \frac{1}{2}\widetilde{\mathrm{Re}}\left\{\Sigma_{\tilde{t}_{12}}(m_{\tilde{t}_1}^2) + \Sigma_{\tilde{t}_{12}}(m_{\tilde{t}_2}^2)\right\}$$

[W. Hollik, H. Rzehak '03]

This defines the counter term for A_t:

$$\delta A_t = \frac{1}{m_t}\Big[U_{\tilde{t}_{11}}U_{\tilde{t}_{12}}^*(\delta m_{\tilde{t}_1}^2 - \delta m_{\tilde{t}_2}^2) + U_{\tilde{t}_{11}}U_{\tilde{t}_{22}}^*\delta Y_t^* + U_{\tilde{t}_{12}}^*U_{\tilde{t}_{21}}\delta Y_t - (A_t - \mu^*\cot\beta)\,\delta m_t\Big] + (\delta\mu^*\cot\beta - \mu^*\cot^2\beta\,\delta\tan\beta)$$

(with $\delta\mu$ from chargino/neutralino sector, $\delta\tan\beta$ from Higgs sector)

Field renormalization for on-shell squarks ($\tilde{t}$, $\tilde{b}$, ...):

Diagonal Z factors:

the real part of the residua of propagators is set to unity:

$$\widetilde{\text{Re}} \frac{\partial \hat{\Sigma}_{\tilde{q}_{ii}}(k^2)}{\partial k^2}\Big|_{k^2=m^2_{\tilde{q}_i}} = 0 \qquad (i = 1, 2)$$

yielding

$$\text{Re}\,\delta Z_{\tilde{q}_{ii}} = -\widetilde{\text{Re}} \frac{\partial \Sigma_{\tilde{q}_{ii}}(k^2)}{\partial k^2}\Big|_{k^2=m^2_{\tilde{q}_i}} \qquad \text{Im}\,\delta Z_{\tilde{q}_{ii}} = 0 \qquad (i = 1, 2)$$

Offdiagonal Z factors:

no transition from one squark to the other occurs:

$$\widetilde{\text{Re}}\hat{\Sigma}_{\tilde{q}_{12}}(m^2_{\tilde{q}_1}) = 0 \qquad \widetilde{\text{Re}}\hat{\Sigma}_{\tilde{q}_{12}}(m^2_{\tilde{q}_2}) = 0$$

yielding

$$\delta Z_{\tilde{q}_{12}} = +2 \frac{\widetilde{\text{Re}}\Sigma_{\tilde{q}_{12}}(m^2_{\tilde{q}_2}) - \delta Y_q}{(m^2_{\tilde{q}_1} - m^2_{\tilde{q}_2})} \qquad \delta Z_{\tilde{q}_{21}} = -2 \frac{\widetilde{\text{Re}}\Sigma_{\tilde{q}_{21}}(m^2_{\tilde{q}_1}) - \delta Y_q^*}{(m^2_{\tilde{q}_1} - m^2_{\tilde{q}_2})}$$

$SU(2)$ relation $\Rightarrow M_{\tilde{t}_L} = M_{\tilde{b}_L}$

"LL" soft SUSY-breaking term for $\tilde{q} = \{\tilde{t}, \tilde{b}\}$:

$$M^2_{\tilde{Q}_L}(\tilde{q}) = |U_{\tilde{q}11}|^2 m^2_{\tilde{q}_1} + |U_{\tilde{q}12}|^2 m^2_{\tilde{q}_2} - M_Z^2 c_{2\beta}(T_q^3 - Q_q s_W^2) - m_q^2$$

Keeping $SU(2)$ relation at the one-loop level leads to a shift in the soft SUSY-breaking parameters

[A. Bartl, H. Eberl, K. Hidaka, S. Kraml, W. Majerotto, W. Porod, Y. Yamada '97, '98]

[A. Djouadi, P. Gambino, S.H., W. Hollik, C. Jünger, G. Weiglein '98]

$$M^2_{\tilde{Q}_L}(\tilde{b}) = M^2_{\tilde{Q}_L}(\tilde{t}) + \delta M^2_{\tilde{Q}_L}(\tilde{t}) - \delta M^2_{\tilde{Q}_L}(\tilde{b})$$

with

$$\delta M^2_{\tilde{Q}_L}(\tilde{q}) = |U_{\tilde{q}11}|^2 \delta m^2_{\tilde{q}_1} + |U_{\tilde{q}12}|^2 \delta m^2_{\tilde{q}_2} - U_{\tilde{q}22} U^*_{\tilde{q}12} \delta Y_q - U_{\tilde{q}12} U^*_{\tilde{q}22} \delta Y_q^* - 2 m_q \delta m_q + M_Z^2\, c_{2\beta}\, Q_q\, \delta s_W^2 - (T_q^3 - Q_q s_W^2)(c_{2\beta}\, \delta M_Z^2 + M_Z^2\, \delta c_{2\beta})$$

$\longrightarrow$ under control

Renormalizations of the $b/\tilde{b}$ sector in the complex MSSM:

scheme	$m_{\tilde{b}_{1,2}}$	m_b	A_b	Y_b	name
analogous to the $t/\tilde{t}$ sector: "OS"	OS	OS	—	OS	RS1
"m_b, A_b $\overline{\text{DR}}$"	OS	$\overline{\text{DR}}$	$\overline{\text{DR}}$	—	RS2
"m_b, Y_b $\overline{\text{DR}}$"	OS	$\overline{\text{DR}}$	—	$\overline{\text{DR}}$	RS3
"m_b $\overline{\text{DR}}$, Y_b OS"	OS	$\overline{\text{DR}}$	—	OS	RS4
"A_b $\overline{\text{DR}}$, ReY_b OS"	OS	—	$\overline{\text{DR}}$	ReY_b: OS	RS5
"A_b vertex, ReY_b OS"	OS	—	vertex	ReY_b: OS	RS6

"— " = dependent parameter

$\Rightarrow$ often very involved analytical dependences

$\to$ more combinations possible

. . . also tested

. . . upcoming results remain unchanged

Renormalization of the sbottom masses:

OS renormalization:

$$\delta m^2_{\tilde{b}_i} = \widetilde{\text{Re}}\Sigma_{\tilde{b}_{ii}}(m^2_{\tilde{b}_i}) \qquad (i = 1, 2)$$

Renormalization of the bottom mass:

OS renormalization:

$$\delta m_b = \frac{1}{2}\widetilde{\text{Re}}\left\{m_b\left[\Sigma^L_b(m_b^2) + \Sigma^R_b(m_b^2)\right] + \left[\Sigma^{SL}_b(m_b^2) + \Sigma^{SL}_b(m_b^2)\right]\right\}$$

$\overline{\text{DR}}$ renormalization:

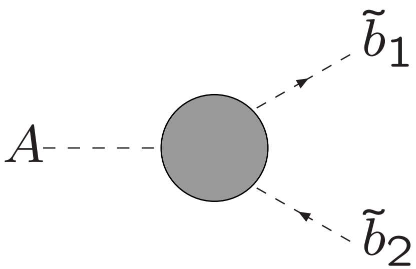
$$\delta m_b = \frac{1}{2}\widetilde{\text{Re}}\left\{m_b\left[\Sigma^L_b(m_b^2) + \Sigma^R_b(m_b^2)\right]_{\text{div}} + \left[\Sigma^{SL}_b(m_b^2) + \Sigma^{SL}_b(m_b^2)\right]_{\text{div}}\right\}$$

Renormalization of A_b:

DR renormalization: analogous to A_t:

$$\delta A_b = \frac{1}{m_b}\Big[U_{\tilde{b}_{11}} U^*_{\tilde{b}_{12}} \left(\widetilde{\mathrm{Re}}\Sigma_{\tilde{b}_{11}}(m^2_{\tilde{b}_1})|_{\mathrm{div}} - \widetilde{\mathrm{Re}}\Sigma_{\tilde{b}_{22}}(m^2_{\tilde{b}_2})|_{\mathrm{div}}\right)$$
$$+ \frac{1}{2} U^*_{\tilde{b}_{12}} U_{\tilde{b}_{21}} \left(\widetilde{\mathrm{Re}}\Sigma_{\tilde{b}_{12}}(m^2_{\tilde{b}_1})|_{\mathrm{div}} + \widetilde{\mathrm{Re}}\Sigma_{\tilde{b}_{12}}(m^2_{\tilde{b}_2})|_{\mathrm{div}}\right)$$
$$+ \frac{1}{2} U_{\tilde{b}_{11}} U^*_{\tilde{b}_{22}} \left(\widetilde{\mathrm{Re}}\Sigma_{\tilde{b}_{12}}(m^2_{\tilde{b}_1})|_{\mathrm{div}} + \widetilde{\mathrm{Re}}\Sigma_{\tilde{b}_{12}}(m^2_{\tilde{b}_2})|_{\mathrm{div}}\right)^*$$
$$- \frac{1}{2}(A_b - \mu^* \tan\beta)\, \widetilde{\mathrm{Re}}\Big\{m_b \left[\Sigma^L_b(m^2_b) + \Sigma^R_b(m^2_b)\right]_{\mathrm{div}}$$
$$+ \left[\Sigma^{SL}_b(m^2_b) + \Sigma^{SR}_b(m^2_b)\right]_{\mathrm{div}}\Big\}\Big] + \delta\mu^*|_{\mathrm{div}} \tan\beta + \mu^*\,\delta\tan\beta$$

Vertex renormalization:



$$\hat{=} \quad i\,\hat{\Lambda}(p^2_A, p^2_{\tilde{b}_1}, p^2_{\tilde{b}_2})$$

via $\quad \widetilde{\mathrm{Re}}\hat{\Lambda}(0, m^2_{\tilde{b}_1}, m^2_{\tilde{b}_1}) + \widetilde{\mathrm{Re}}\hat{\Lambda}(0, m^2_{\tilde{b}_2}, m^2_{\tilde{b}_2}) \stackrel{!}{=} 0$

Renormalization of Y_b:

OS renormalization:

$$\delta Y_b = \frac{1}{2}\widetilde{\text{Re}}\left\{\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2) + \Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2)\right\}$$

$\overline{\text{DR}}$ renormalization:

$$\delta Y_b = \frac{1}{2}\widetilde{\text{Re}}\left\{\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2)|_{\text{div}} + \Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2)|_{\text{div}}\right\}$$

ReY_b OS renormalization

$$\text{Re}\delta Y_b = \frac{1}{2}\text{Re}\left\{\widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2) + \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2)\right\}$$

Existing analyses all in the real MSSM:

- [A. Bartl et al. '98] [L. Jin, C. Li '01]
  "OS" used for stop and sbottom decays
  ($\rightarrow$ implemented into SDecay)

- [C. Weber, K. Kovarik, H. Eberl, W. Majerotto '07]
  similar to "m_b, A_b $\overline{\text{DR}}$" used for Higgs decays to sfermions

- [A. Arhrib, R. Benbrik '04]
  an "OS" scheme used for $\tilde{f} \rightarrow \tilde{f}'V$

- [Q. Li, L. Jin, C. Li '02]
  an "OS" scheme with running m_t, m_b, A_t, A_b used for $\tilde{t}_2 \rightarrow \tilde{t}_1\phi$

- [H. Eberl et al. '10]
  pure $\overline{\text{DR}}$ scheme used for stop decays

- [A. Brignole, G. Degrassi, P. Slavich and F. Zwirner '02]
  [S.H., W. Hollik, H. Rzehak, G. Weiglein '04]
  real "A_b vertex, ReY_b OS" used for two-loop Higgs self-energies

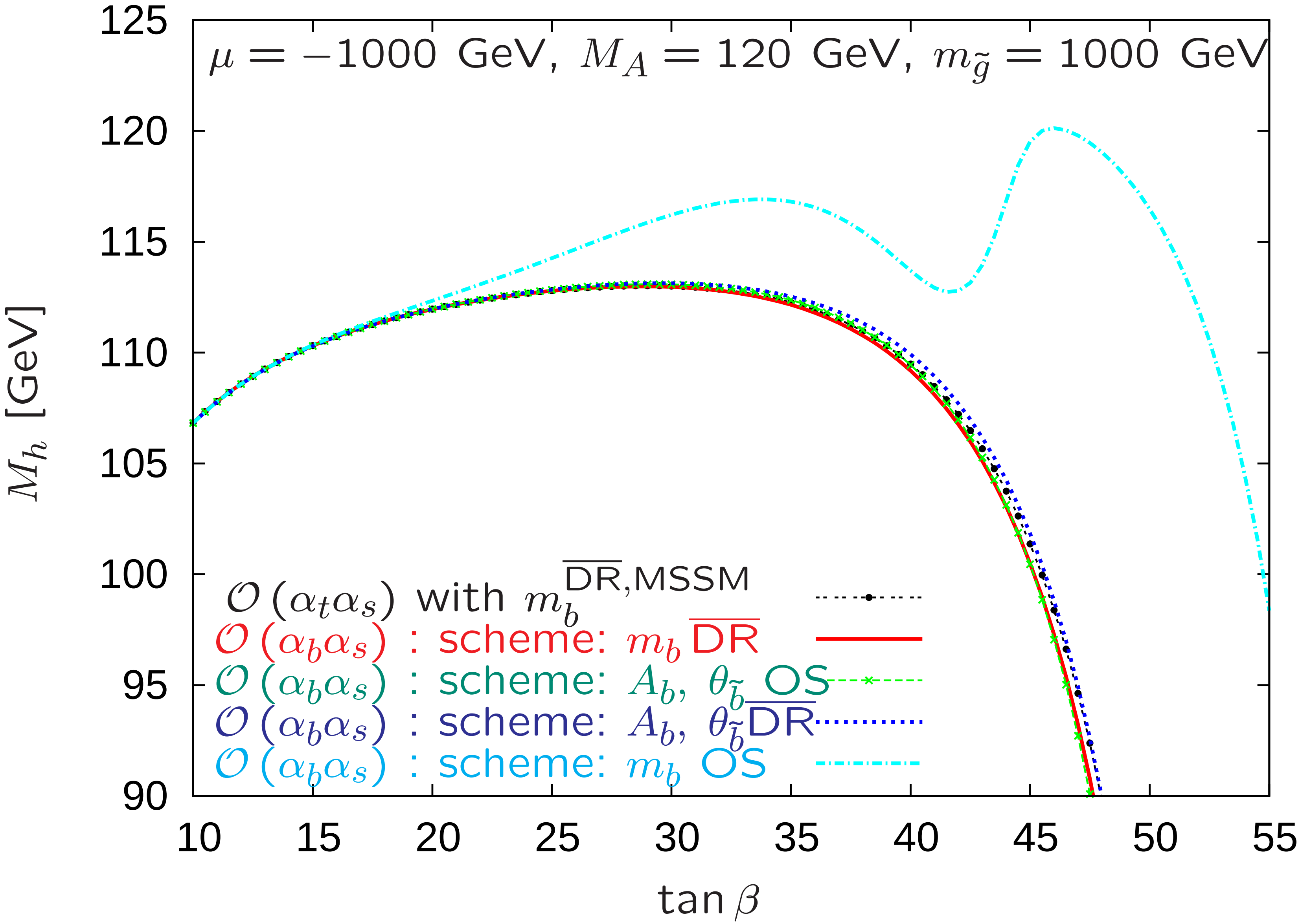
3. Analysis of the renormalization schemes

Numerical scenarios:

Scen.	$M_{H^\pm}$	$m_{\tilde{t}_2}$	μ	A_t	A_b	M_1	M_2	M_3
S1	150	600	200	900	400	200	300	800
S2	180	900	300	1800	1600	150	200	400

Scen.	$\tan\beta$	$m_{\tilde{t}_1}$	$m_{\tilde{t}_2}$	$m_{\tilde{b}_1}$	$m_{\tilde{b}_2}$
S1	2	293.391	600.000	441.987	447.168
	20	235.073	600.000	418.824	439.226
	50	230.662	600.000	400.815	449.638
S2	2	495.014	900.000	702.522	707.598
	20	445.885	900.000	678.531	695.180
	50	442.416	900.000	628.615	697.202

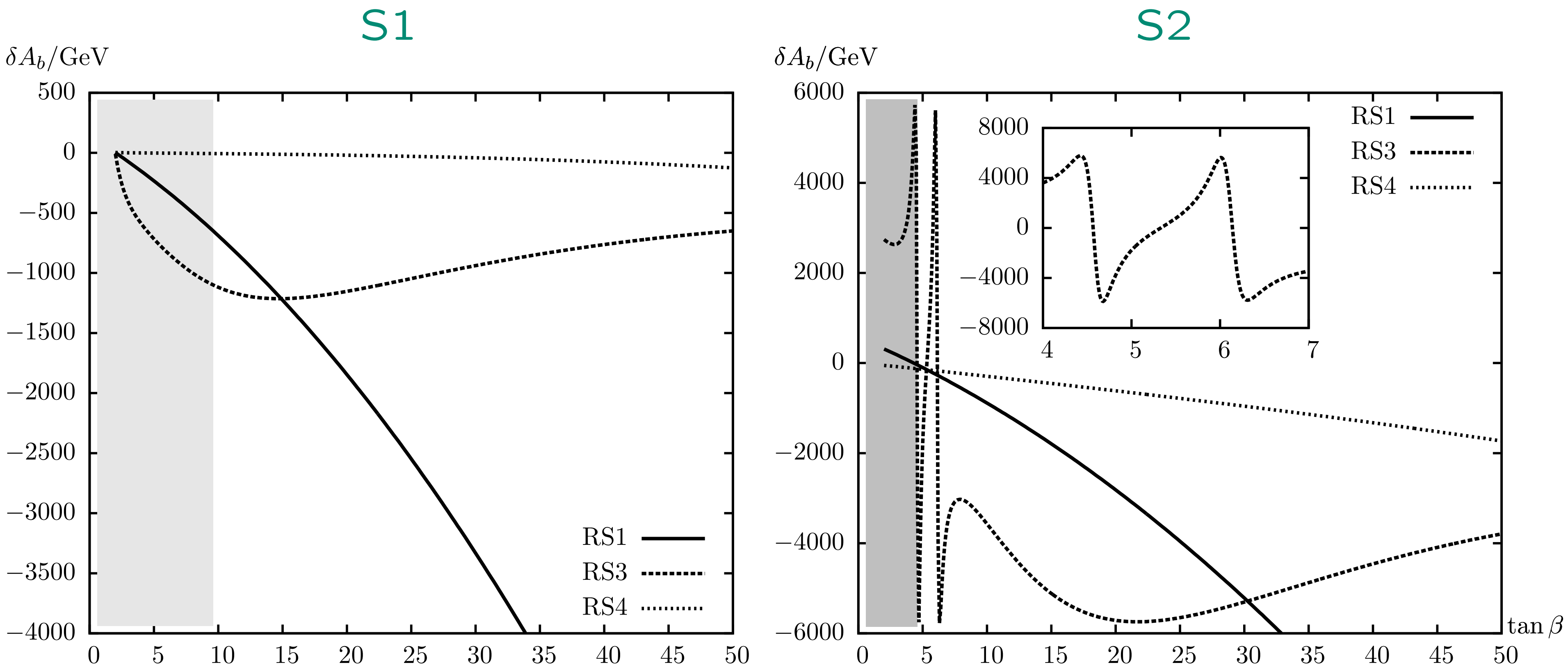
"OS" scheme: $\delta A_b = \frac{1}{m_b}\left[-(A_b - \mu^* \tan\beta)\,\delta m_b + \ldots\right]$



$\Rightarrow$ fails already for Higgs boson self-energies

Problems of non-A_b renormalizations:

$$\delta A_b|_{\text{fin}} = \frac{1}{m_b}\left[U_{\tilde{b}_{11}} U^*_{\tilde{b}_{12}} \left(\delta m^2_{\tilde{b}_1} - \delta m^2_{\tilde{b}_2}\right)\right]_{\text{fin}} + \ldots$$

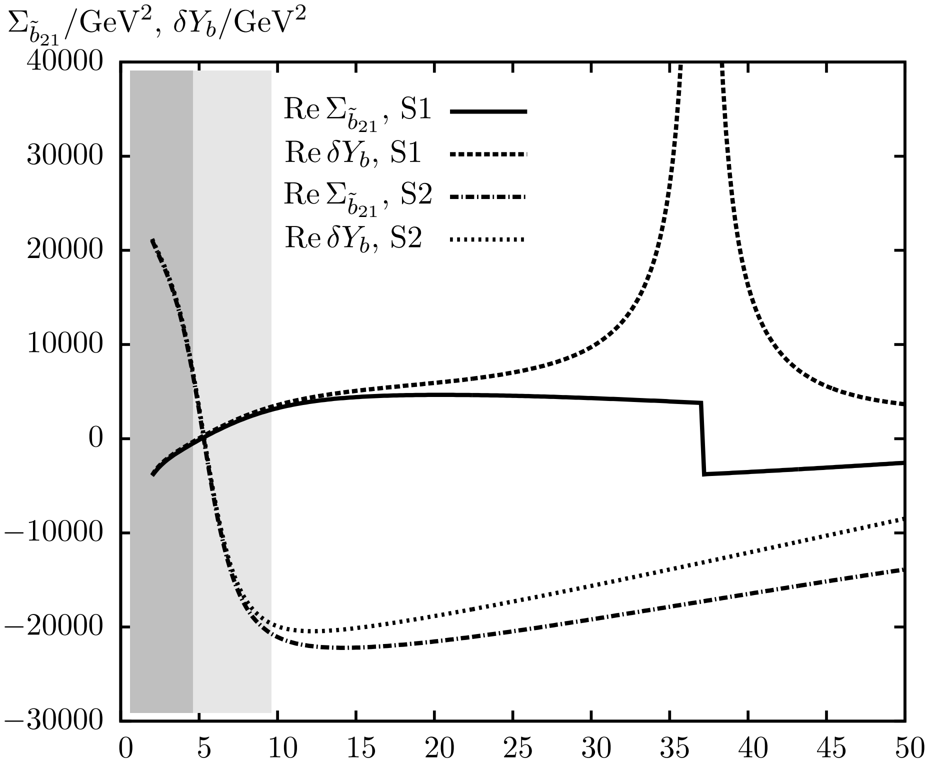


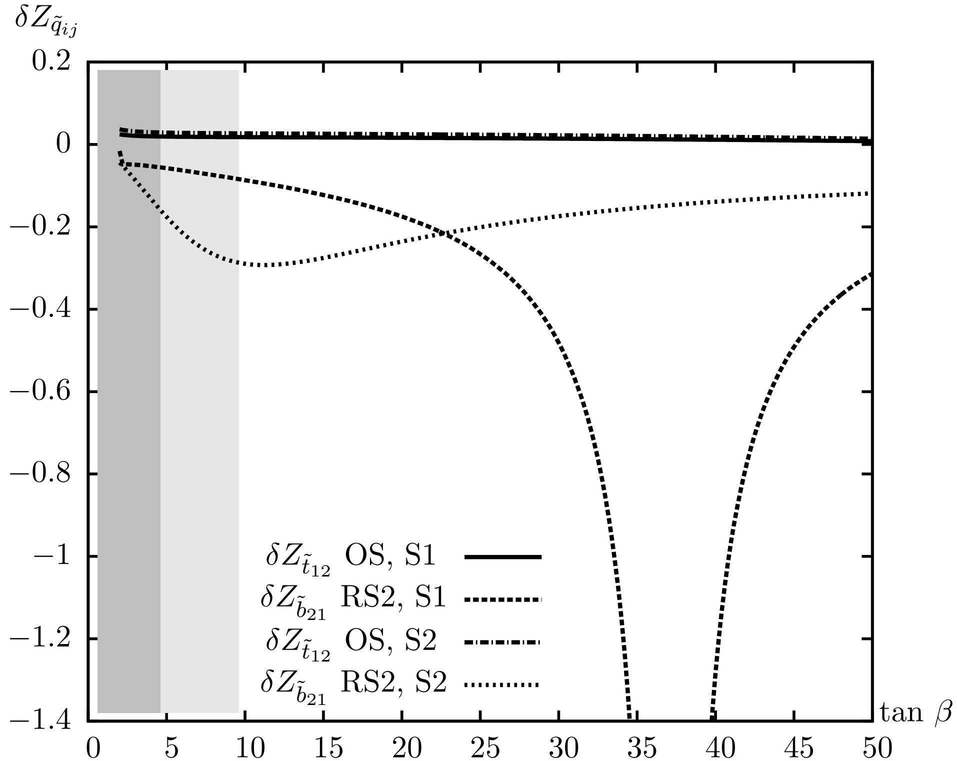
⇒ too large contributions to A_b are induced

Problems of m_b–A_b renormalizations:

$$\delta Y_b = \frac{U_{\tilde{b}_{11}} U_{\tilde{b}_{21}}}{|U_{\tilde{b}_{11}}|^2 - |U_{\tilde{b}_{12}}|^2} \left(\delta m^2_{\tilde{b}_1} - \delta m^2_{\tilde{b}_2} \right) + \ldots , \qquad \delta Z_{\tilde{b}_{21}} = -2 \, \frac{\mathrm{Re}\Sigma_{\tilde{b}_{21}}(m^2_{\tilde{b}_2}) - \delta Y_b}{m^2_{\tilde{b}_1} - m^2_{\tilde{b}_2}}$$

$\Rightarrow$ divergence for $|U_{\tilde{b}_{11}}| = |U_{\tilde{b}_{12}}|$ reached for $\tan\beta \approx 37$ in S1:





Problems of non-m_b renormalizations:

"A_b $\overline{\mathrm{DR}}$, ReY_b OS" (RS5): (rMSSM)

$$\delta m_b = -\frac{m_b\,\delta A_b + \delta S}{(A_b - \mu \tan\beta)}$$

$\Rightarrow$ divergent for $A_b = \mu \tan\beta$

"A_b vertex, ReY_b OS" (RS6): (rMSSM)

$$\delta m_b = \frac{\delta S + F}{\mu\,(\tan\beta + 1/\tan\beta)}$$

$\Rightarrow$ no problem in the rMSSM!

"A_b vertex, ReY_b OS" (RS6): (cMSSM: $U_- = U_{\tilde{b}_{11}} U^*_{\tilde{b}_{22}} - U_{\tilde{b}_{12}} U^*_{\tilde{b}_{21}}$)

$$\frac{1}{\delta m_b} \sim 4\,\mu\,\tan^3\beta \left[\mathrm{Re} U_- \left(|U_{\tilde{b}_{11}}|^2 - |U_{\tilde{b}_{12}}|^2 \right) + \mathrm{Im}\, U_- \frac{4\,m_b}{m^2_{\tilde{b}_1} - m^2_{\tilde{b}_2}} \mathrm{Im} \left(U^*_{\tilde{b}_{11}} U_{\tilde{b}_{12}} A_b \right) \right]$$

$\Rightarrow$ divergences appear depending on ϕ_{A_b}!

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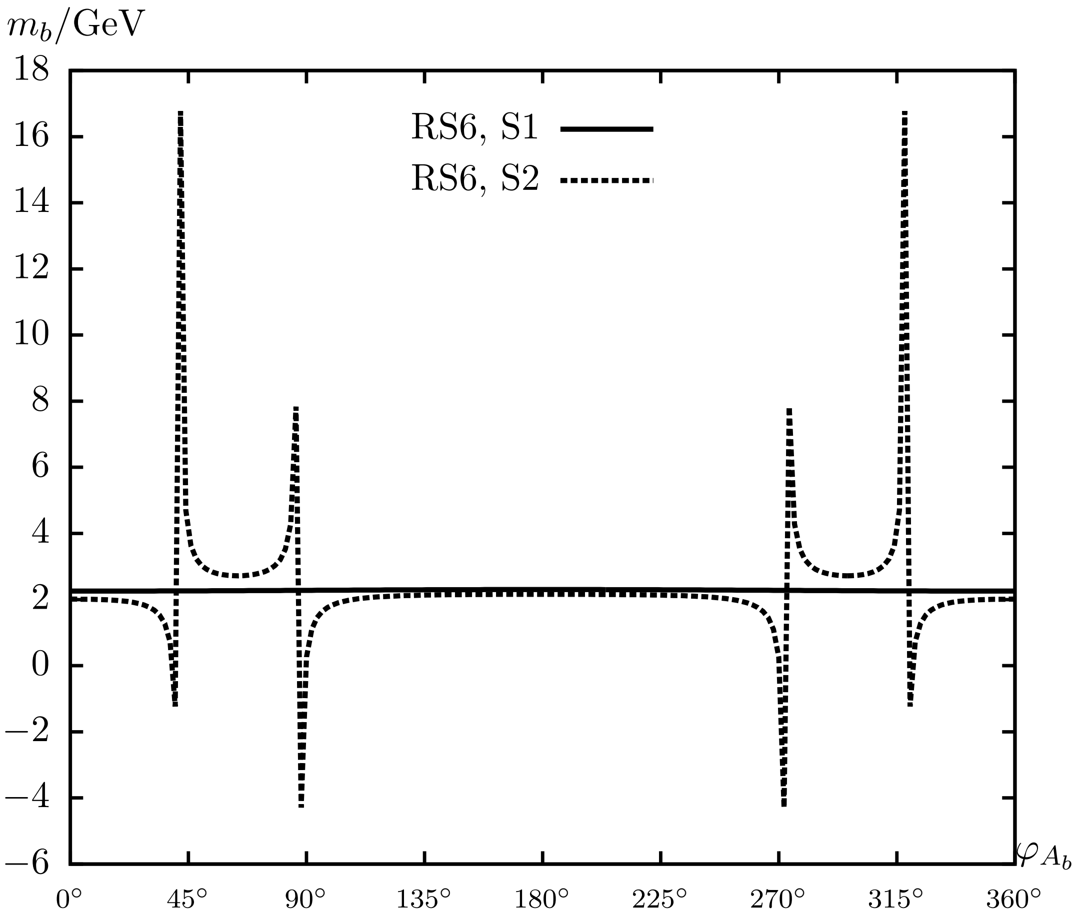

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Most "robust" behavior:

– RS2: "m_b, A_b $\overline{\text{DR}}$"
  ⇒ problems only for maximal sbottom mixing
– RS6: "A_b vertex, ReY_b OS"
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All problems could be avoided in a pure $\overline{\text{DR}}$ scheme
$\Rightarrow$ not suited for external stops and sbottoms

$\Rightarrow$ we choose RS2: "m_b, A_b $\overline{\text{DR}}$" as our "preferred" scheme

4. Numerical results in the favored scheme: "m_b, A_b $\overline{\mathrm{DR}}$"

Calculation of partial widths:

– all diagrams created with FeynArts → TT

→ model file with all counterterms in the cMSSM

– including all soft/hard QED/QCD diagrams

– further evaluation with FormCalc

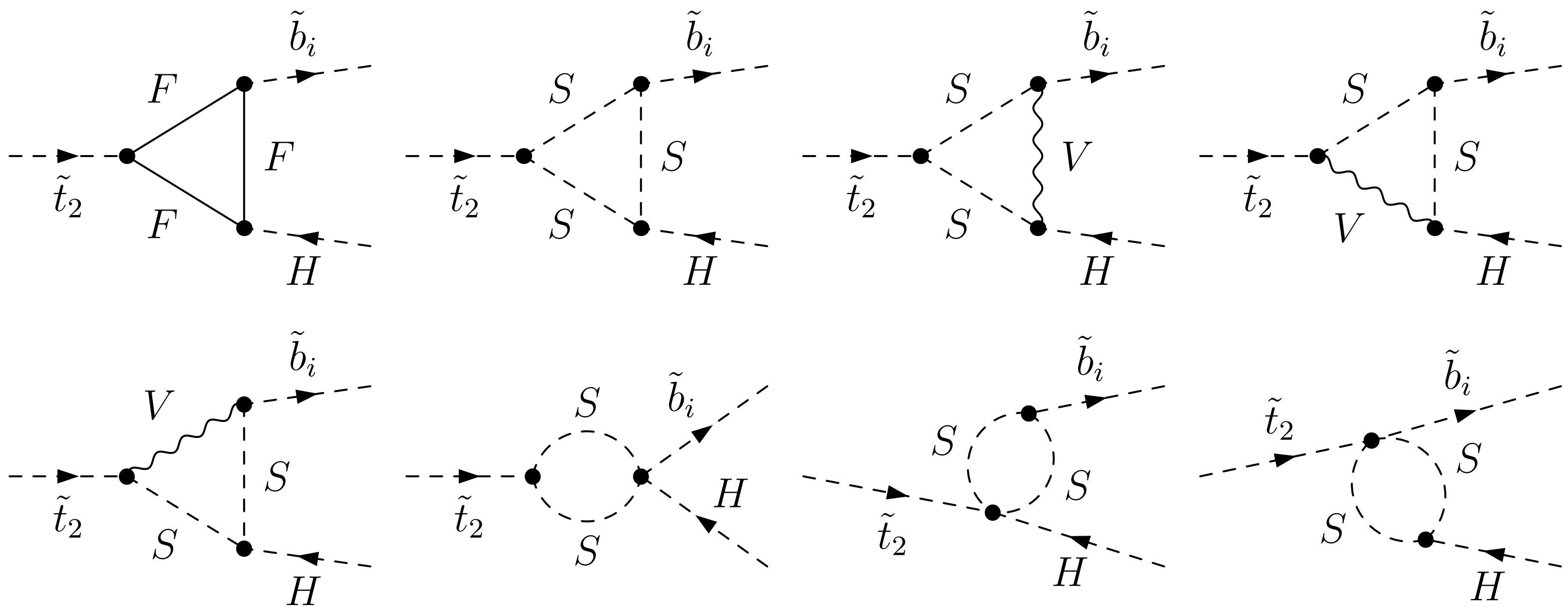
– Dimensional REDuction

– all UV and IR divergences cancel

– results will be included into FeynHiggs (www.feynhiggs.de)

→ example plots will focus on $\Gamma(\tilde{t}_2 \to \tilde{b}_1 H^+)$

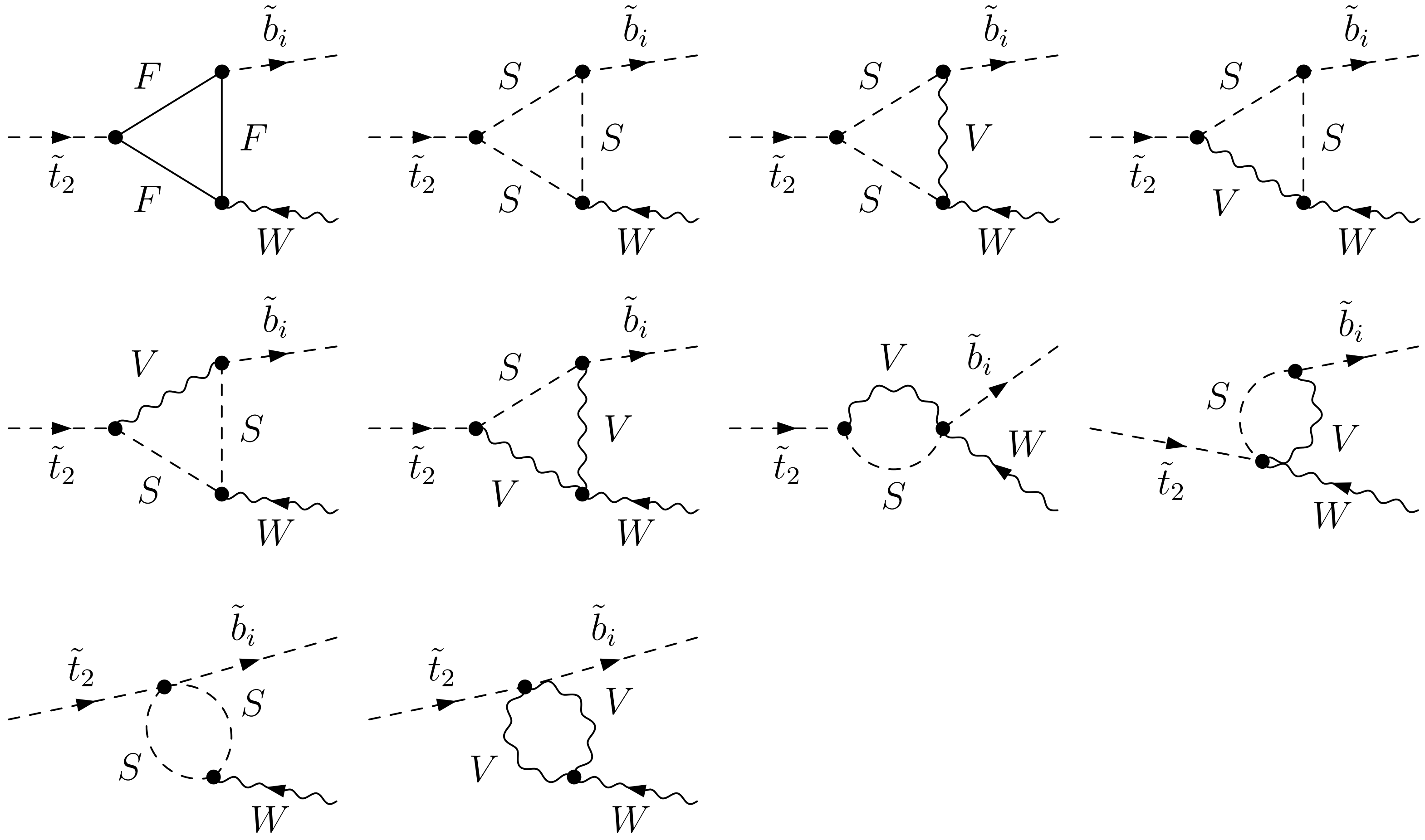
Feynman diagrams for $\tilde{t}_2 \to \tilde{b}_i H^+$



– including W^+–H^+ or G^+–H^+ transition contribution on the external Higgs boson leg

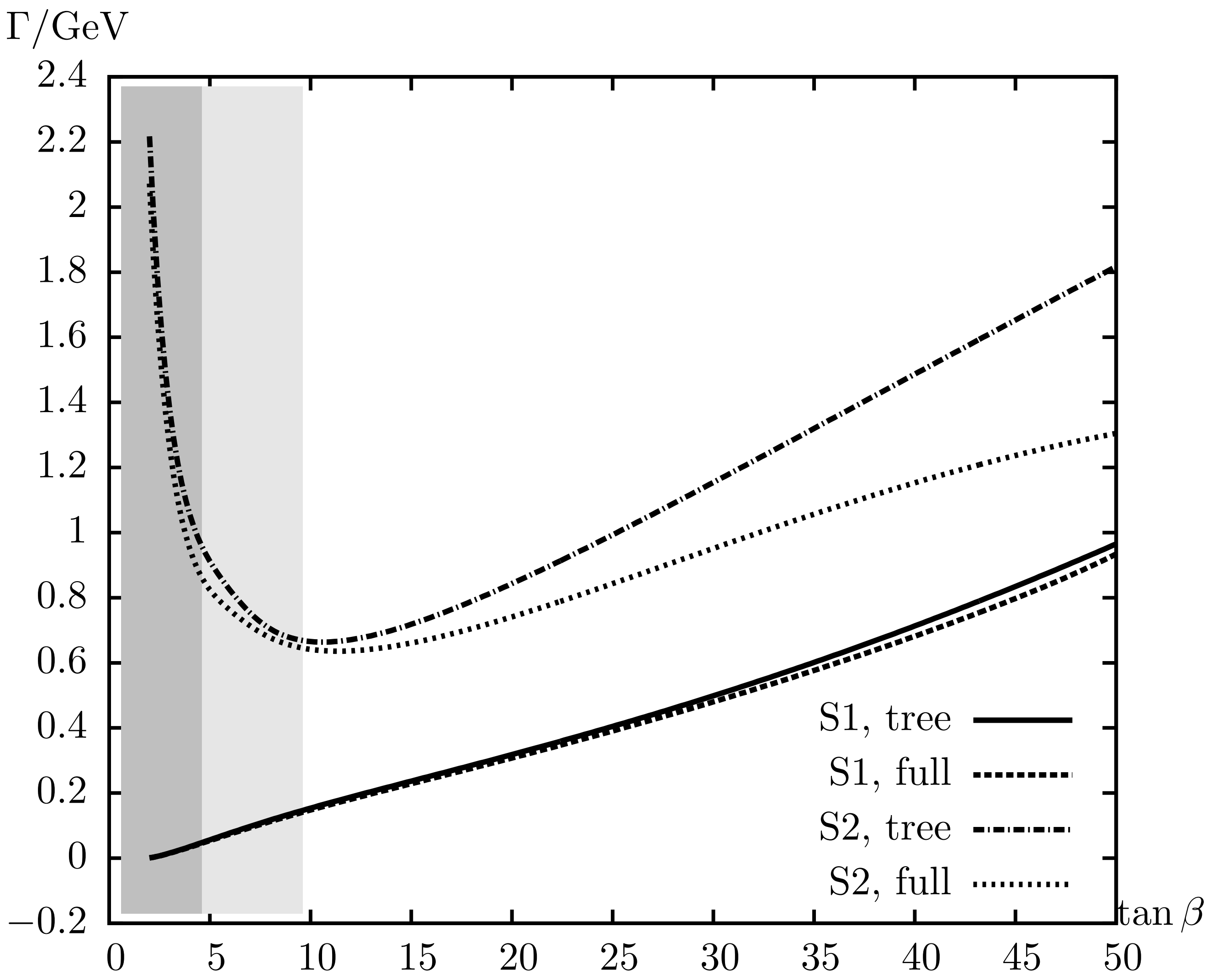
– including all soft/hard QED/QCD diagrams

Feynman diagrams for $\tilde{t}_2 \to \tilde{b}_i W^+$



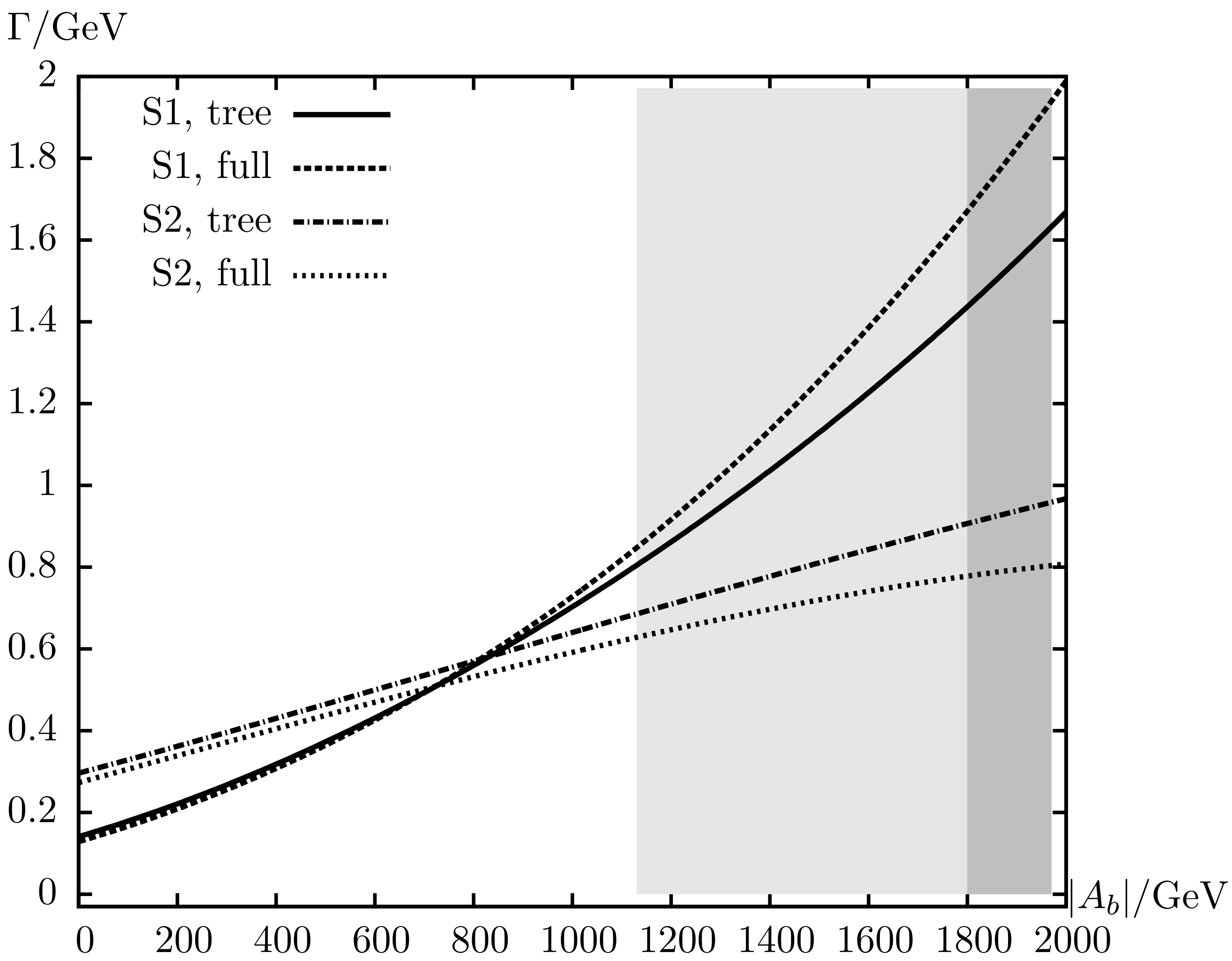
– including all soft/hard QED/QCD diagrams

$\Gamma(\tilde{t}_2 \to \tilde{b}_1 H^+)$: dependence on $\tan\beta$



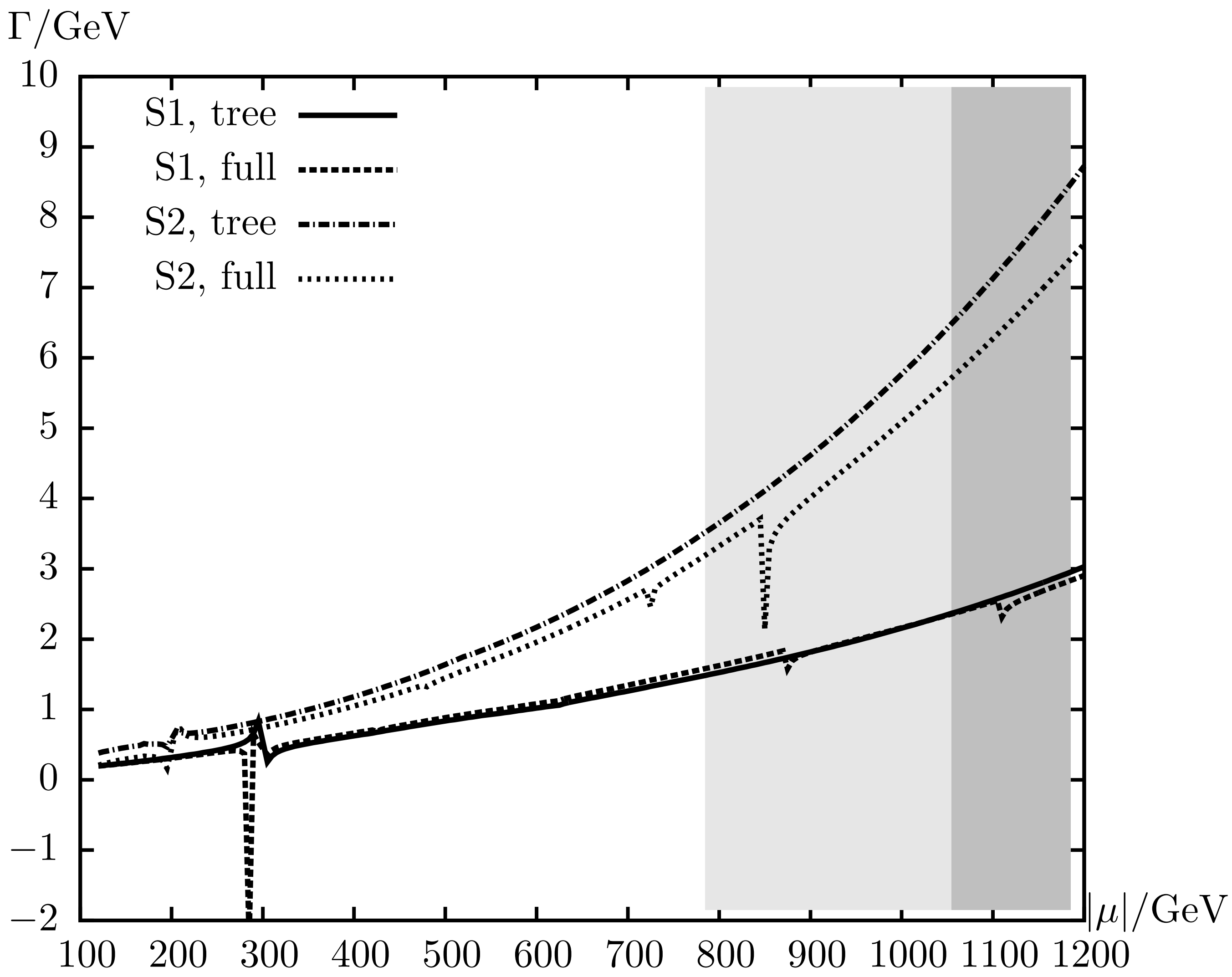
$\Rightarrow$ one-loop corrections under control for all $\tan\beta$ values

$\Gamma(\tilde{t}_2 \to \tilde{b}_1 H^+)$: dependence on A_b ($\tan\beta = 20$)



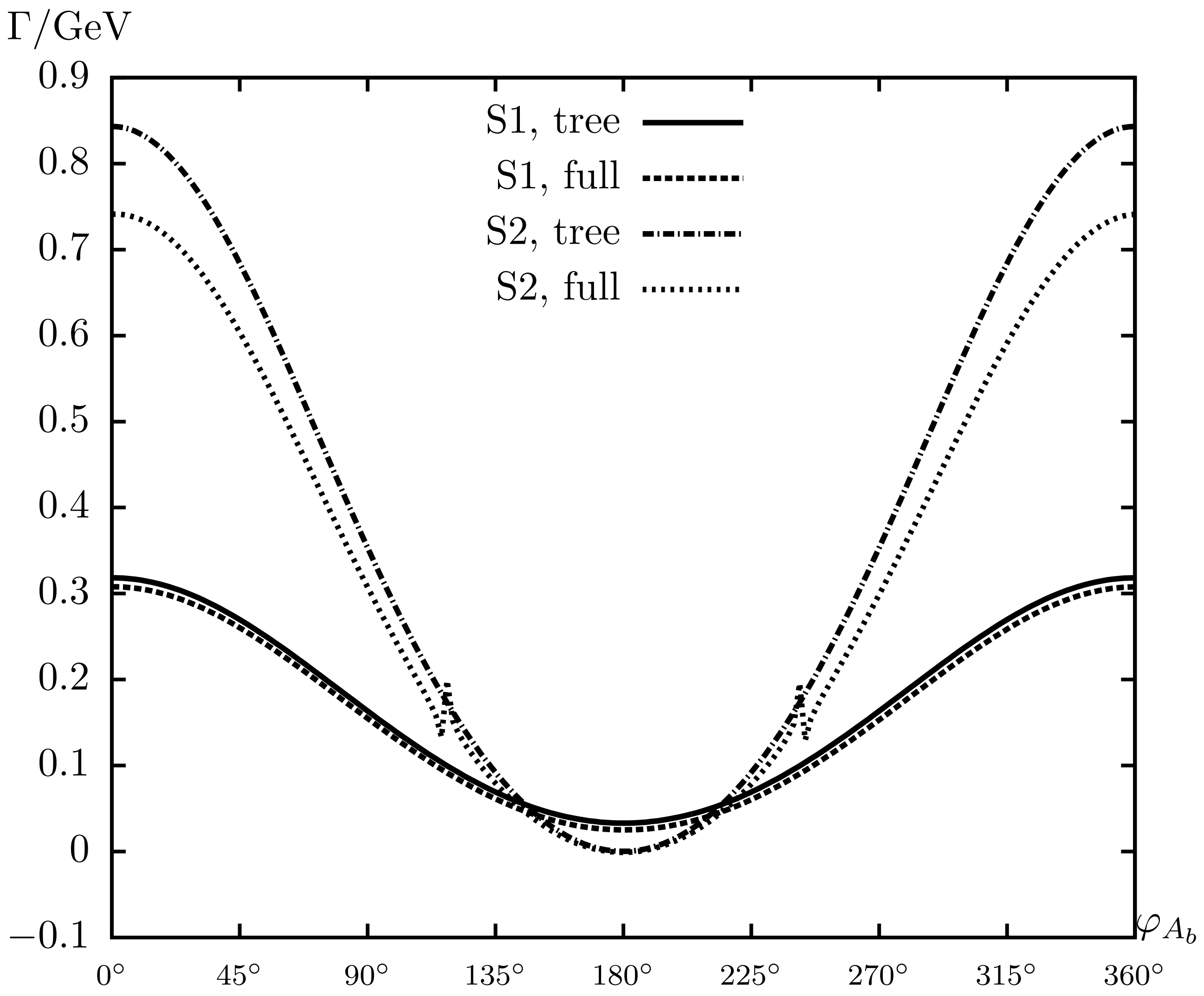
⇒ one-loop corrections under control for all A_b values

$\Gamma(\tilde{t}_2 \to \tilde{b}_1 H^+)$: dependence on μ ($\tan\beta = 20$)



⇒ one-loop corrections under control (but many thresholds)

$\Gamma(\tilde{t}_2 \to \tilde{b}_1 H^+)$: dependence on ϕ_{A_b} ($\tan\beta = 20$)



$\Rightarrow$ one-loop corrections under control except of sharp peaks at $|U_{\tilde{b}_{11}}| \approx |U_{\tilde{b}_{12}}|$

5. Conclusions & Outlook

- $\tilde{t}$ and $\tilde{b}$ sector important for collider phenomenology
- Simultaneous renormalization of both sectors crucial for higher-order corrections – on-shell properties for external squarks!

  $\Rightarrow$ $\tilde{t}/\tilde{b}$ renormalization in the cMSSM

- Stop sector: widely used on-shell renormalization
- $SU(2)$ $(M_{\tilde{t}_L} = M_{\tilde{b}_L})$ $\Rightarrow$ shift in $M^2_{\tilde{Q}_L}(\tilde{b})$
- Sbottom sector: six (+X) schemes defined and tested
  analytical deficiencies found in all schemes
  most "robust": RS2: "m_b, A_b $\overline{\text{DR}}$" ← preferred scheme
  RS6: "A_b vertex, ReY_b OS"
- Numerical analysis: RS2: "m_b, A_b $\overline{\text{DR}}$" shows very robust and stable behavior over nearly all (tested) cMSSM parameter space
- Outlook:
  full cMSSM renormalization and all $\Gamma(\tilde{t}_i \to XY)$ calculation ready soon


Higgs Days at Santander 2010
Theory meets Experiment
13.-16. October
HEPTOOLS
IFCA
Instituto de Física de Cantabria
CSIC
UC
UNIVERSIDAD DE CANTABRIA
contact: Sven.Heinemeyer@cern.ch
http://www.ifca.es/HDays10
Photo: Philip Bechtle HDays09

Back-up

Parameter definition: m_b

$$m_b^{\overline{\text{MS}}}(m_b) = 4.2\text{ GeV}$$
$$m_b^{\overline{\text{MS}}}(\mu_R) = \Phi^{\text{SM},3-\text{loop}}(m_b^{\overline{\text{MS}}}(m_b))$$

An "on-shell" mass is derived from the $\overline{\text{MS}}$ mass via

$$m_b^{\text{OS}} = m_b^{\overline{\text{MS}}}(\mu_R)\ \left[1 + \frac{\alpha_s^{\overline{\text{MS}}}(\mu_R)}{\pi}\left(\frac{4}{3} + 2\ \ln\frac{\mu_R}{m_b^{\overline{\text{MS}}}(\mu_R)}\right)\right]$$

The $\overline{\text{DR}}$ bottom quark mass is calculated iteratively

$$m_b^{\overline{\text{DR}}} = \frac{m_b^{\text{OS}}(1+\Delta_b) + \delta m_b^{\text{OS}} - \delta m_b^{\overline{\text{DR}}}}{1+\Delta_b}$$
$$\Delta_b = \frac{2\alpha_s(m_t)}{3\pi}\tan\beta\, M_3^*\,\mu^*\, I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, m_{\tilde{g}}^2)\ + \ldots$$

The bottom quark mass of a special renormalization scheme:

$$m_b = m_b^{\overline{\text{DR}}} + \delta m_b^{\overline{\text{DR}}} - \delta m_b$$