

Lepton flavour observables in the MSSM

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net



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Motivation: Lepton Flavour Violation

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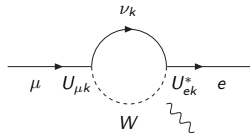
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- **Mixing** completely different from Quark-Sector:

$$U_{\text{PMNS}} = \begin{pmatrix} \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \end{pmatrix}, \quad V_{\text{CKM}} = \begin{pmatrix} \bullet & \bullet & \cdot \\ \cdot & \bullet & \cdot \\ \cdot & \cdot & \bullet \end{pmatrix}$$

Clear signal for physics beyond SM

SM+ ν_R : mixing of charged leptons, but **unobservable**:

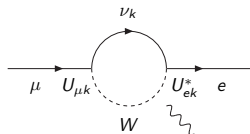
$$BR(\mu \rightarrow e\gamma) \approx \frac{3\alpha}{128\pi} \left(\frac{\Delta m_{21}^2}{M_W^2} \right)^2 \sin^2 2\theta_{12} \approx 10^{-54}$$



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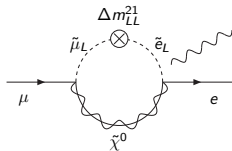
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- **SUSY**: LFV can be induced by **off-diagonal elements of the slepton mass matrix** (soft breaking terms)

$$\delta_{XY}^{ij} = \frac{\Delta m_{XY}^{ij}}{\sqrt{m_{iX}^2 m_{jY}^2}}, \quad X, Y = L, R, \quad i, j = e, \mu, \tau$$

Constraints from $\ell_j \rightarrow \ell_i \gamma$ (mainly $\delta_{LL}^{ij}, \delta_{LR}^{ij}$)



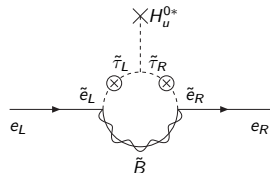
Lepton flavour violating effects
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LFV corrections to y_e : Constraints from a_e and m_e

tan β -enhanced corrections: $y_{d,\ell} = \frac{m_{d,\ell}}{v_d(1+\epsilon \tan \beta)}$, [Hall, Rattazzi, Sarid, 94]

- Inclusion of LFV: $y_e = \frac{m_e + \Sigma_e^{\text{FV}}}{v_d(1+\epsilon_e \tan \beta)}$
- $\Sigma_e^{\text{FV}} \propto \frac{\alpha_1}{4\pi} \frac{m_\tau \tan \beta}{1+\epsilon_\tau \tan \beta} \delta_{LL}^{13} \delta_{RR}^{13} \Rightarrow \delta y_e = y_e \frac{\delta m_e}{m_e} \propto \frac{m_\tau}{m_e}$

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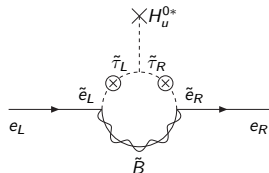
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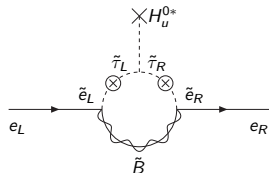
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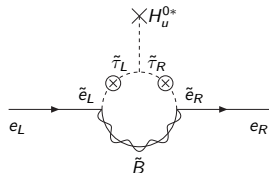


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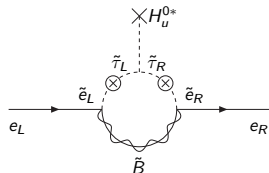
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- ▶ most stringent bound: $|\delta_{LL}^{13} \delta_{RR}^{13}| < 0.1$.
- ▶ since a_e decouples, bounds very loose for $M_{\text{SUSY}} \gtrsim 500$ GeV.

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Experiment	$R_K [10^{-5}]$	error $\delta R_K/R_K$
PDG 2006	2.45 ± 0.11	4.5%
NA48/2 '03	$2.416 \pm 0.043 \pm 0.024$	2.8%
NA48/2 '04	$2.455 \pm 0.045 \pm 0.041$	3.5%
KLOE	$2.55 \pm 0.05 \pm 0.05$	3.9%
Kaon 2007	2.457 ± 0.032	1.3%
KLOE '09	$2.493 \pm 0.025 \pm 0.019$	2.2%
NA62 '09	2.486 ± 0.013	0.5%

Probing LFV SUSY effects in NA62 experiment

- In MSSM: additional **charged-Higgs** contribution to $K \rightarrow \ell \nu$:
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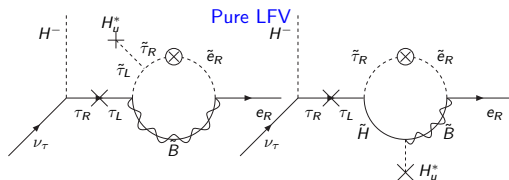
- ★ **model independent** analysis within a THDM-II: $\delta y_e = y_e \frac{\delta m_e}{m_e} \approx y_e \frac{\Sigma_e^{FV}}{m_e}$

$$\Delta r_{\text{min,LFC}}^{\mu-e} = -4 \frac{m_K^2 \tan^2 \beta}{M_H^2 (1 + \epsilon_s \tan \beta)}$$

For $\tan \beta = 50$, $\epsilon_s \tan \beta = 0.3$ and charged-Higgs mass $M_H = 300$ GeV:
 $\Delta r_{\text{min,LFC}}^{\mu-e} = -5 \cdot 10^{-3} \rightarrow$ **not measurable**

- ★ measurement $\Delta r^{\mu-e} < \Delta r_{\text{min,LFC}}^{\mu-e}$ needs more exotic NP explanation than charged-Higgs exchange

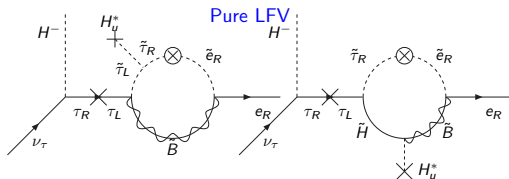
LFV contributions to R_K



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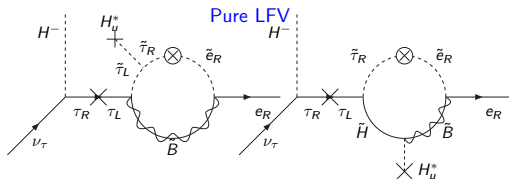


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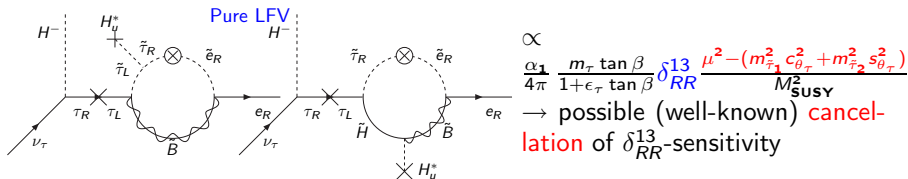
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- $$\Delta r_{\text{LFV}}^{\mu-e} = \frac{m_K^4 \tan^4 \beta}{M_H^4 (1 + \epsilon_e \tan \beta)^2 (1 + \epsilon_\tau \tan \beta)^2} \frac{m_\tau^2}{m_e^2} \left[\frac{\Sigma_{\tau_L-e_R}}{m_\tau} \right]^2$$

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- scenario: input lightest stau $m_{\tilde{\tau}_\ell} = 120$ GeV, 500 GeV $\leq \mu \leq 900$ GeV \rightarrow maximal effects for $\theta_\tau \approx 26^\circ$ [J.G., U. Nierste, in prep. 10]:

$$\Delta r_K^{\mu-e} \approx 0.006 \left(\frac{500 \text{ GeV}}{M_H} \right)^4 \left(\frac{\tan \beta}{50} \right)^6 \left(\frac{\delta_{RR}^{13}}{0.5} \right)^2 \left(\frac{\mu}{800 \text{ GeV}} \right)^2$$

- maximal LFV effects in $\Delta r_K^{\mu-e}$ ($\theta_\tau \neq 0 \neq \delta_{RR}^{13}$, large μ , light $\tilde{\tau}$) can reach future NA62 sensitivity of 0.2%

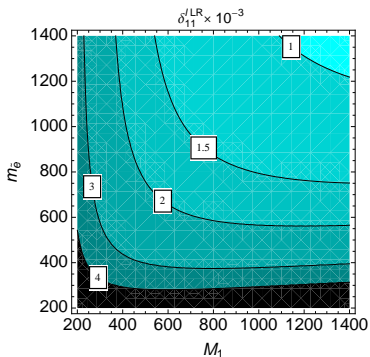
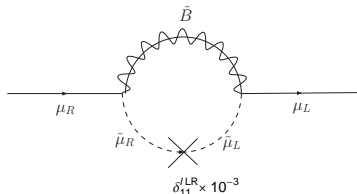
Chirally enhanced corrections
to light lepton masses
and interplay between a_μ and y_μ

Chiral corrections to light lepton masses: LO

- possible to generate light fermion masses radiatively via **A-terms** in $\sum_{f_L-f_R} \tilde{\chi}, \tilde{g}$ [Wyler, Nilles, 82; Banks 88; Borzumati, Farrar, Polonsky, Thomas, 99; Ferrandis, Haba, 04; Crivellin, Nierste, 09]

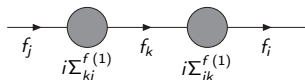
- Upper bound of fine tuning argument $|\sum_{f_L-f_R} \tilde{\chi}, \tilde{g}| \leq m_f$ corresponds to radiative mass generation [A. Crivellin, J.G, 09]

$$|\delta_{LR}^{\ell 11}| \lesssim 0.0025 \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right),$$
$$|\delta_{LR}^{\ell 22}| \lesssim 0.5 \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right).$$



Chirally enhanced corrections to light lepton masses: NLO

- A-terms with generic flavour structure \Rightarrow also **two-loop corrections** can contribute: constraints $\delta_{LR}^{ik} \delta_{LR}^{ki}$ (latter unconstrained for $k > i$)


$$|\delta_{LR}^{\ell 13} \delta_{LR}^{\ell 31}| \lesssim \frac{64\pi^2 m_e m_\tau}{(\alpha_1 M_{\text{SUSY}})^2} \approx 0.021 \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

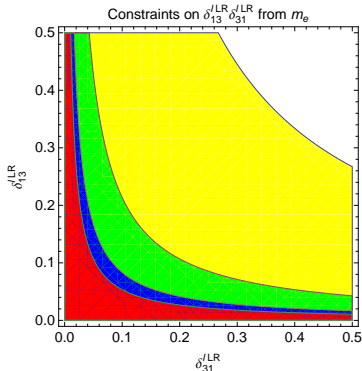


Figure: Naturalness bound $M_{\text{SUSY}} = 200 \text{ GeV}$ (yellow), 500 GeV (green), 800 GeV (blue), 1000 GeV (red)

Correlating a_μ and y_μ

- 3.2σ discrepancy: $a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.5 \pm 8.0) \times 10^{-10}$ [Jegerlehner, Nyffeler, 09; Passera, Marciano, Sirlin, 01; Prades 10; Teubner, Hagiwara, Liao, Martin, Nomura, 01]

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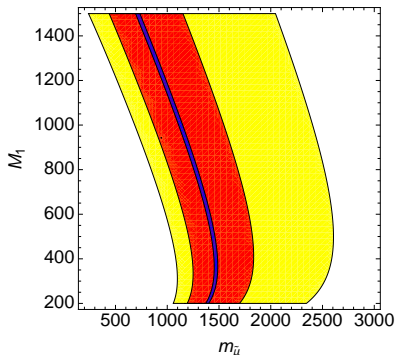
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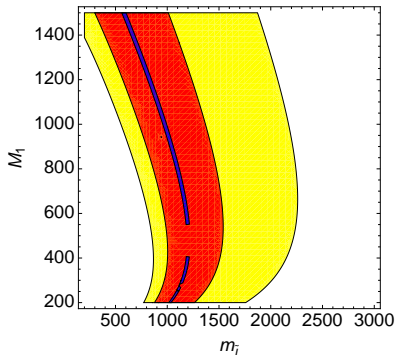
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- Left: Allowed region in the M_1 - $m_{\tilde{\mu}}$ plane ($m_{\tilde{\mu}}$ is the lighter smuon mass). Yellow: $a_\mu \pm 2\sigma$, red: $a_\mu \pm 1\sigma$, blue: $a_\mu \Rightarrow 750 \text{ GeV} \leq m_{\tilde{\mu}} \leq 2700 \text{ GeV}$
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 - ▶ LHC: detection of lighter smuon \Rightarrow proof of non-vanishing y_μ in MSSM superpotential

Thank's for your attention