



Hidden two-Higgs doublet model

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Two Higgs doublet models (2HDM)

Work together with Rikard Enberg and Glenn Wouda (Uppsala)

Why 2HDM?

- Simplest non-trivial extension of the SM Higgs sector
- Realized in the MSSM (type II)
- Interesting phenomenology

Here: Hidden 2HDM where

- softly broken Z_2 symmetry imposed in Higgs basis
(cf. Inert Doublet Model (IDM) by Barbieri, Hall and Rychkov)
- A and H^\pm have
 - no tree-level couplings to fermions
 - usual couplings to h , H and γ , Z , W
- Interesting phenomenology:
 - electroweak precision tests can be fulfilled also with heavy h
 - non-std decays of A/H^\pm such as $H^+ \rightarrow W^+ \gamma$ can dominate
 - essentially no limits on A , H^\pm from low-energy flavour experiments (B -decays etc)



General two Higgs doublet model potential

- Two complex $SU(2)_L$ doublets with hypercharge $Y=1$: Φ_1, Φ_2
- Invariance under global $SU(2)$: $\Phi_a \rightarrow U_{ab}\Phi_b$

General potential

$$\begin{aligned} \mathcal{V} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] + \frac{1}{2} \lambda_1 \left(\Phi_1^\dagger \Phi_1 \right)^2 \\ & + \frac{1}{2} \lambda_2 \left(\Phi_2^\dagger \Phi_2 \right)^2 + \lambda_3 \left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_2^\dagger \Phi_2 \right) + \lambda_4 \left(\Phi_1^\dagger \Phi_2 \right) \left(\Phi_2^\dagger \Phi_1 \right) \\ & + \left\{ \frac{1}{2} \lambda_5 \left(\Phi_1^\dagger \Phi_2 \right)^2 + \left[\lambda_6 \left(\Phi_1^\dagger \Phi_1 \right) + \lambda_7 \left(\Phi_2^\dagger \Phi_2 \right) \right] \left(\Phi_1^\dagger \Phi_2 \right) + \text{h.c.} \right\} \end{aligned}$$

- Potential real $\Rightarrow \{m_{11}^2, m_{22}^2, \lambda_{1-4}\}$ real, $\{m_{12}^2, \lambda_{5-7}\}$ complex
- No explicit CP-violation $\Rightarrow \{m_{12}^2, \lambda_{5-7}\}$ real

Exact Z_2 symmetry (as in IDM)

Demanding that the potential is symmetric under $\Phi_1 \rightarrow \Phi_1$,
 $\Phi_2 \rightarrow -\Phi_2 \Rightarrow m_{12}^2 = 0, \lambda_{6-7} = 0$ in general basis



Electroweak symmetry breaking

- Higgs basis \Rightarrow EW symmetry broken by non-zero vev of Φ_1

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}G^+ \\ v - h \sin \alpha + H \cos \alpha + iG^0 \end{pmatrix}$$

$$\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}H^+ \\ h \cos \alpha + H \sin \alpha + iA \end{pmatrix}$$

- Minimization $\Rightarrow \begin{cases} m_{11}^2 = -\frac{1}{2}v^2\lambda_1 \\ m_{12}^2 = \frac{1}{2}v^2\lambda_6 \end{cases} \quad (v \approx 246 \text{ GeV})$
- Three Goldstone bosons: $G^\pm, G^0 \Rightarrow$ masses to W and Z
- Five “Higgs” boson states: two CP-even, h, H with mixing angle α , one CP-odd A , and two charged H^\pm
- $\sin \alpha \propto m_{12}^2$ ($m_{12}^2 = 0$ restores Z_2 symmetry)
- Higgs-gauge couplings from $s_\alpha \equiv \sin \alpha$ ($\tan \beta = 0$)
- No hard breaking of Z_2 symmetry $\Rightarrow \lambda_2, \lambda_7$ fixed
- Parameterisation of potential: $\{ m_{22}^2, m_h, m_H, m_A, m_{H^\pm}, s_\alpha \}$



Yukawa sector

- In order for fermions to get mass they have to couple to Φ_1
- To avoid non-MFV CC and FCNC at tree-level, each fermion type can only couple to one Higgs doublet (Glashow & Weinberg)
- \Rightarrow fermions cannot couple to Φ_2

Yukawa couplings for SM fermions with mass eigenstates

$D = \{d, s, b\}$, $U = \{u, c, t\}$, $L = \{e, \mu, \tau\}$ and massless neutrinos

$$\mathcal{L}_Y = \frac{1}{v} \left(\sum_D \bar{D} m_D D + \sum_U \bar{U} m_U U + \sum_L \bar{L} m_L L \right) (\sin \alpha h - \cos \alpha H)$$



Theoretical constraints

Positivity of potential

Demanding that the potential is bounded from below \Rightarrow

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 > -\sqrt{\lambda_1 \lambda_2}, \quad \lambda_3 + \lambda_4 - \lambda_5 > -\sqrt{\lambda_1 \lambda_2}$$

plus more complicated expressions

Perturbativity

Cross-section for $2 \rightarrow 2$ Higgs scattering processes $\propto \frac{\lambda_{HHHH}^2}{16\pi^2}$
 \Rightarrow the quartic Higgs couplings λ_{HHHH} cannot be too large for the perturbative series to make sense

Tree-level unitarity

requiring tree-level unitarity for HH and HV_L scattering \Rightarrow limits on eigenvalues of the corresponding scattering matrices



Improved naturalness

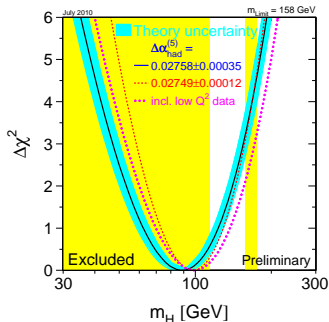
Naturalness (Barbieri, Hall, Rychkov)

The physics that cancels the quadratic corrections to m_h^2 must enter at a scale obtained from

$$(\delta m_h^2)_{\text{top}} = \frac{3m_t^2}{2\pi^2 v^2} \Lambda_t^2 < m_h^2 \quad \Rightarrow \quad \Lambda_t \lesssim \sqrt{4\pi} m_h$$

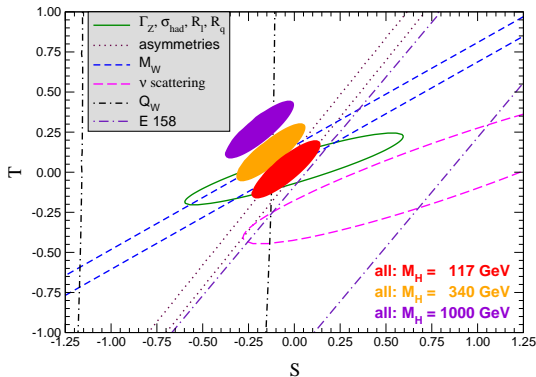
SM more natural (less fine-tuned) if m_h larger

But EW precision measurements restrict m_h severely in SM





- Oblique parameters S , T , U sensitive to new physics
- Fixing the SM Higgs mass and $U = 0$ gives region of allowed (90% CL) points in the $S - T$ plane

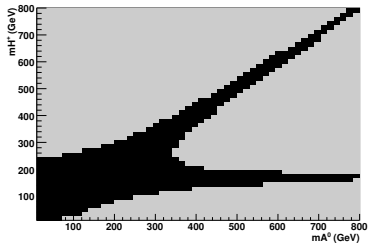


- If new physics increase T and/or decrease $S \Rightarrow$ lightest CP-even Higgs can be much heavier
- possible with an additional Higgs doublet (also in IDM and λ SUSY)

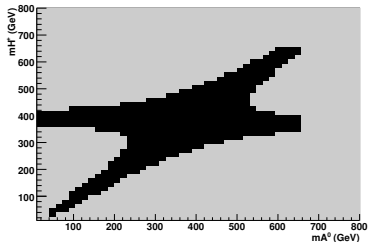


Examples of allowed regions from S, T as well as positivity, perturbativity and tree-level unitarity in m_A - m_{H^\pm} plane

$$\begin{aligned}m_h &= 150 \text{ GeV} \\m_H &= 200 \text{ GeV} \\ \sin \alpha &= 1/\sqrt{2} \\m_{22} &= 50 \text{ GeV}\end{aligned}$$



$$\begin{aligned}m_h &= 400 \text{ GeV} \\m_H &= 200 \text{ GeV} \\ \sin \alpha &= 0.3 \\m_{22} &= 100 \text{ GeV}\end{aligned}$$

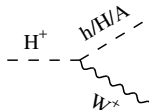


\Rightarrow points with an custodial global $SU(2)$ symmetry allowed
 $m_{H^\pm} \approx m_A$ or $m_{H^\pm}^2 \approx m_H^2 \sin^2 \alpha + m_h^2 \cos^2 \alpha$



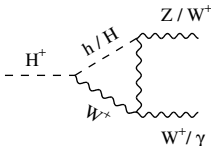
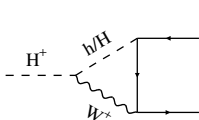
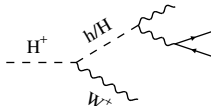
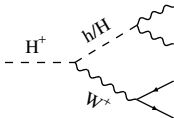
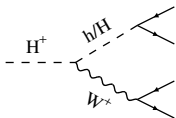
Non-standard H^+ decays

Basic decay vertex



$\cos\alpha / \sin\alpha / 1$

Decays into fermions and SM gauge bosons ($m_{H^\pm} < m_A$)



Note: all diagrams proportional to $\sin(2\alpha) \Rightarrow$ vanish in no-mixing limit $\sin\alpha \rightarrow 0$ or $\cos\alpha \rightarrow 0$



Example:

$$m_{H^\pm} = 300 \text{ GeV}$$

$$m_H = 600 \text{ GeV}$$

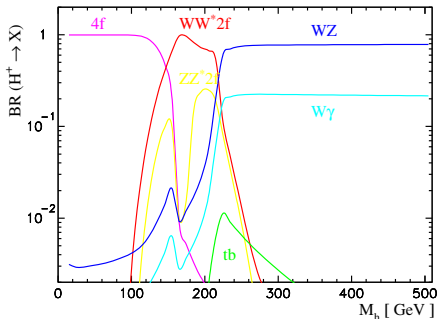
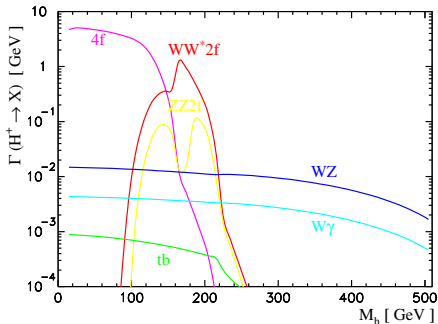
$$m_A = 400 \text{ GeV}$$

$$\sin \alpha = 0.3$$

$$m_{22} = 0$$

- $H^+ \rightarrow 4f$ dominates for $m_h \lesssim 2m_V$ GeV
- $H^+ \rightarrow VV^{(*)}2f$ dominates for $2m_V \lesssim m_h \lesssim m_{H^\pm} - m_V$
- $H^+ \rightarrow WZ$ dominates for $m_h > m_{H^\pm} - m_V$

For smaller m_{H^\pm} (~ 100 GeV)
 $H^+ \rightarrow W\gamma$ dominate for all m_h





Conclusions

Hidden two Higgs Doublet model

- softly broken Z_2 symmetry in Higgs basis
- no Yukawa couplings for A and H^\pm

Phenomenological consequences

- offers improved naturalness (m_h larger)
- non-standard decay modes of A and H^\pm can dominate

Next step

- look at lighter A and H^\pm and see possible effects on LEP searches