

***Flavor symmetry
combined with
spontaneous CP breaking
to suppress FCNCs and CP violations***

Jisuke Kubo (kanazawa Univ.)
at SUSY 2010

based on:

Babu and JK, PRD71, 056006 (2005);

Itou, Kajiyama and JK, NPB743, 74 (2006);

Kifune, JK and Lenz, PRD77, 076010 (2008);

Araki and JK, IJMod.A24, 5831 (2009);

Kawashima, JK and Lenz, PLB681,60 (2009);

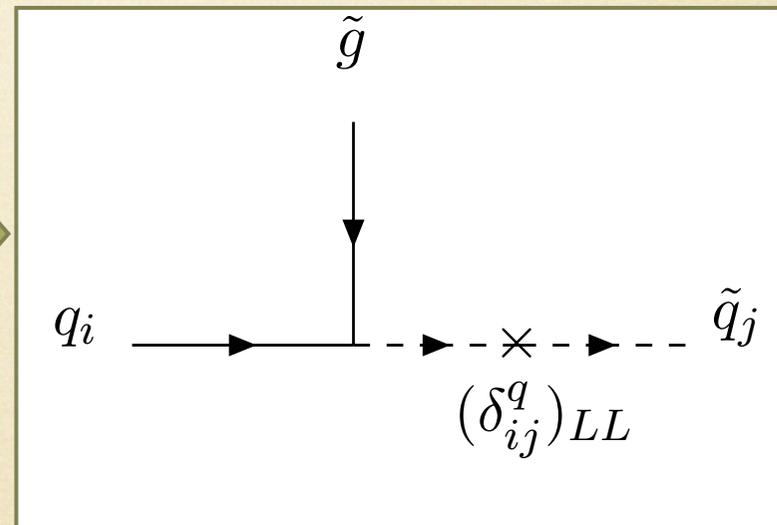
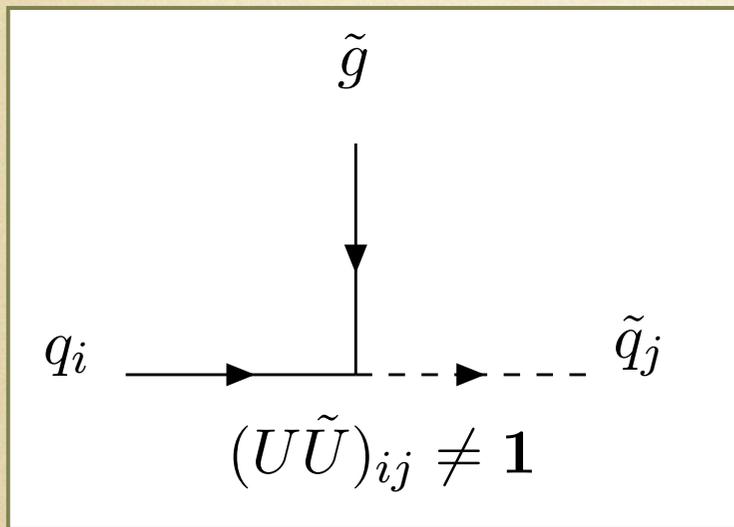
JK and Lenz, arXiv:1007.0680;

Babu and JK, to appear

The minimality of the Higgs sector does not help to suppress FCNCs and ~~CP~~.

Mismatch between flavors

Soft mass insertions



$$\Delta m_K = 3.5 \times 10^{-15} \text{ GeV} \longrightarrow$$

$$|(\delta_{12}^d)_{LR}| < 10^{-3}$$

$$d_e < 10^{-27} \text{ e cm} \longrightarrow$$

$$\text{Im}(\delta_{11}^l)_{LR} < 10^{-7}$$

We use:
 a flavor symmetry to suppress FCNCs,
 and break CP spontaneously to suppress CP

A SUSY model based on $Q_6 \times Z_4$

Babu and JK, PRD71, 056006 (2005); and to appear.

SM non-singlet

SM singlet

	Q, L	Q_3, L_3	U^c, D^c, N^c, E^c	$U_3^c, D_3^c, N_3^c, E_3^c$	$H^{u,d}$	$H_3^{u,d}$	S	S_3	T	T_3	U
Q_6	$\mathbf{2}_1$	$\mathbf{1}_{+2}$	$\mathbf{2}_2$	$\mathbf{1}_{-,1}$	$\mathbf{2}_2$	$\mathbf{1}_{-1}$	$\mathbf{2}_1$	$\mathbf{1}_{+,0}$	$\mathbf{2}_2$	$\mathbf{1}_{+2}$	$\mathbf{1}_{+,0}$
Z_4	$-i$	$-i$	$+$	$+$	i	i	$-$	$-$	$+$	$+$	$+$

$2+I=3$ structure except U

Each sector, except U , forms a family
 with parents + one child

Accidental permutation symmetries of V_{Higgs}

Vacuum I: $\langle H_1^{u,d} \rangle = \langle H_2^{u,d} \rangle \dots\dots$

Vacuum II: $\langle H_1^{u,d} \rangle = \langle H_2^{u,d} \rangle^* \dots\dots$

Two minima are physically different.

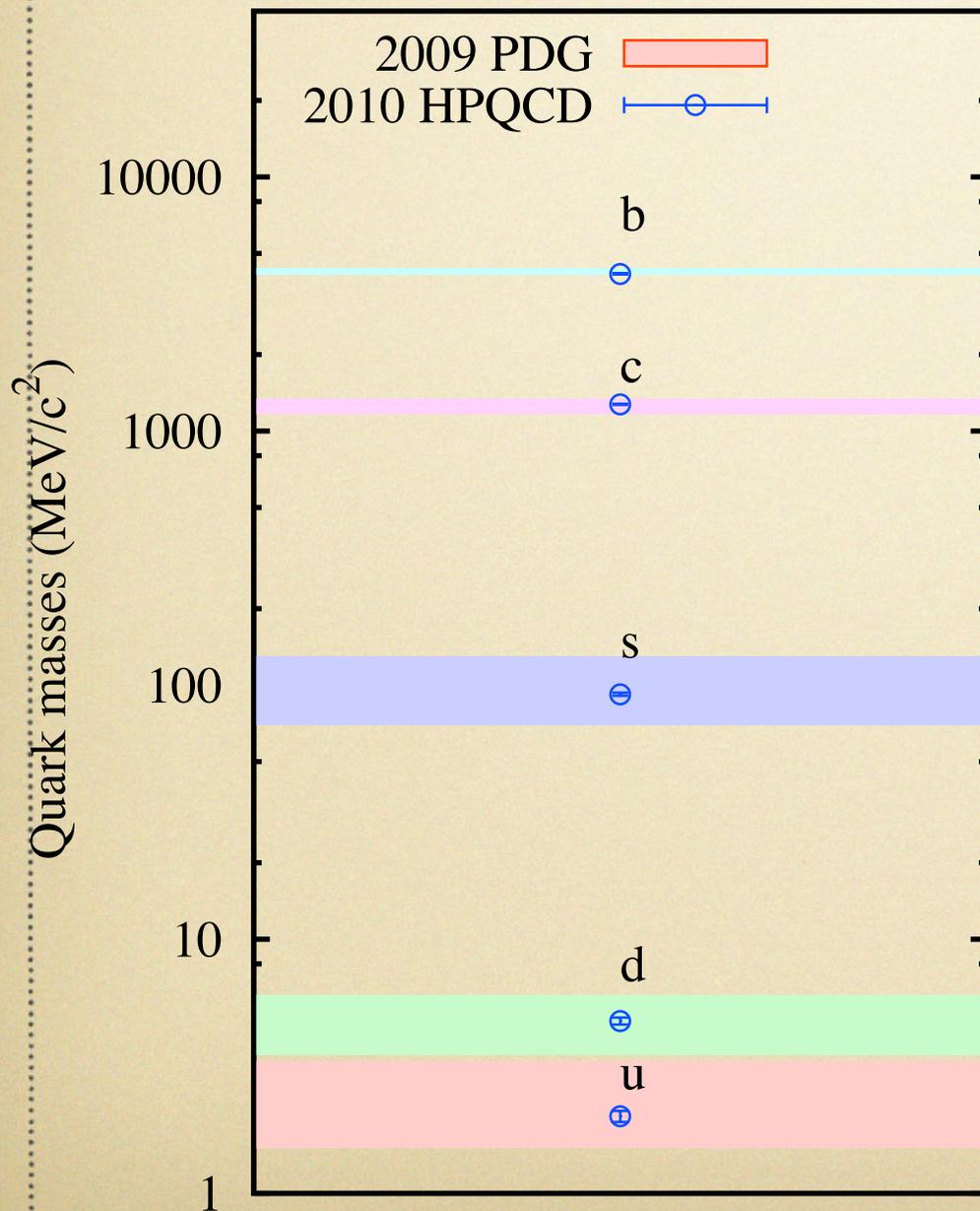
9 theory parameters for
6 quark masses and 4 CKM parameters.



One sum rule among them

Precise quark masses

HPQCD, arXiv:1004.4285 [hep-lat]
and P.R.L.104: 132003, 2010.



$$\Delta m_b : 4\% \rightarrow 0.7\%$$

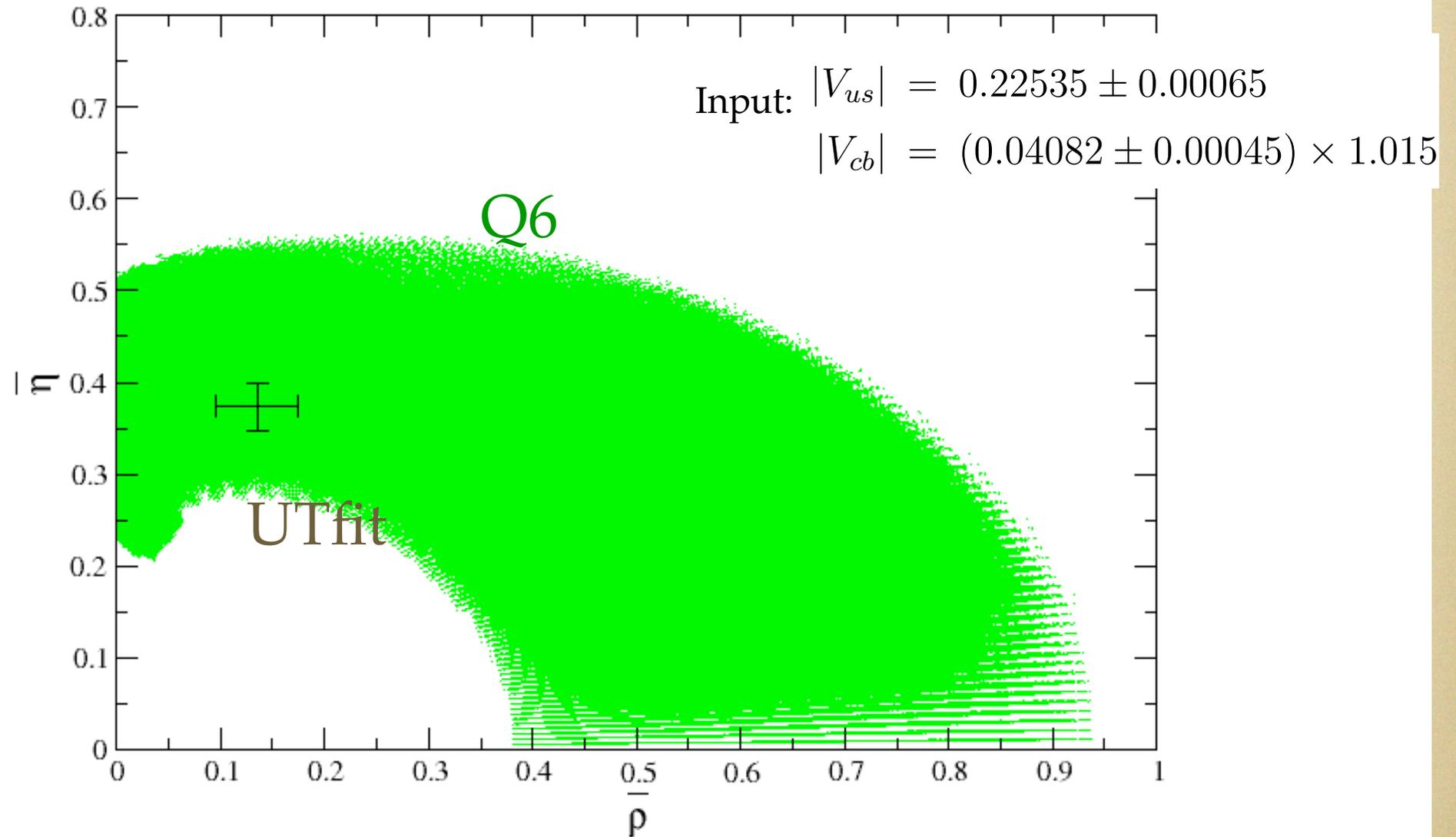
$$\Delta m_c : 9\% \rightarrow 1.3\%$$

$$\Delta m_s : 33\% \rightarrow 1.4\%$$

$$\Delta m_u : 38\% \rightarrow 5\%$$

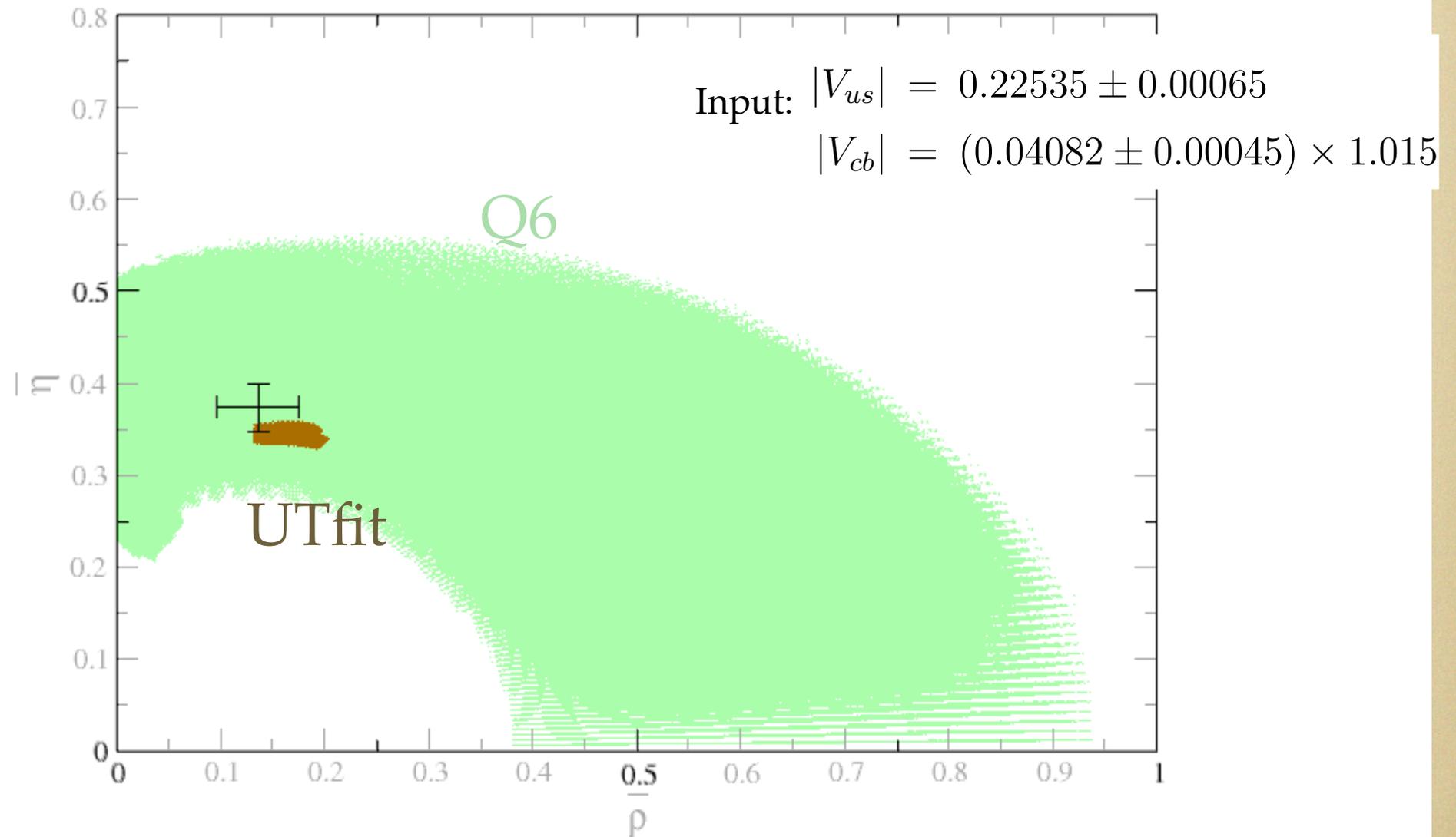
$$\Delta m_d : 27\% \rightarrow 3\%$$

Q6 sum rule (Vacuum I)



using mq of PDG

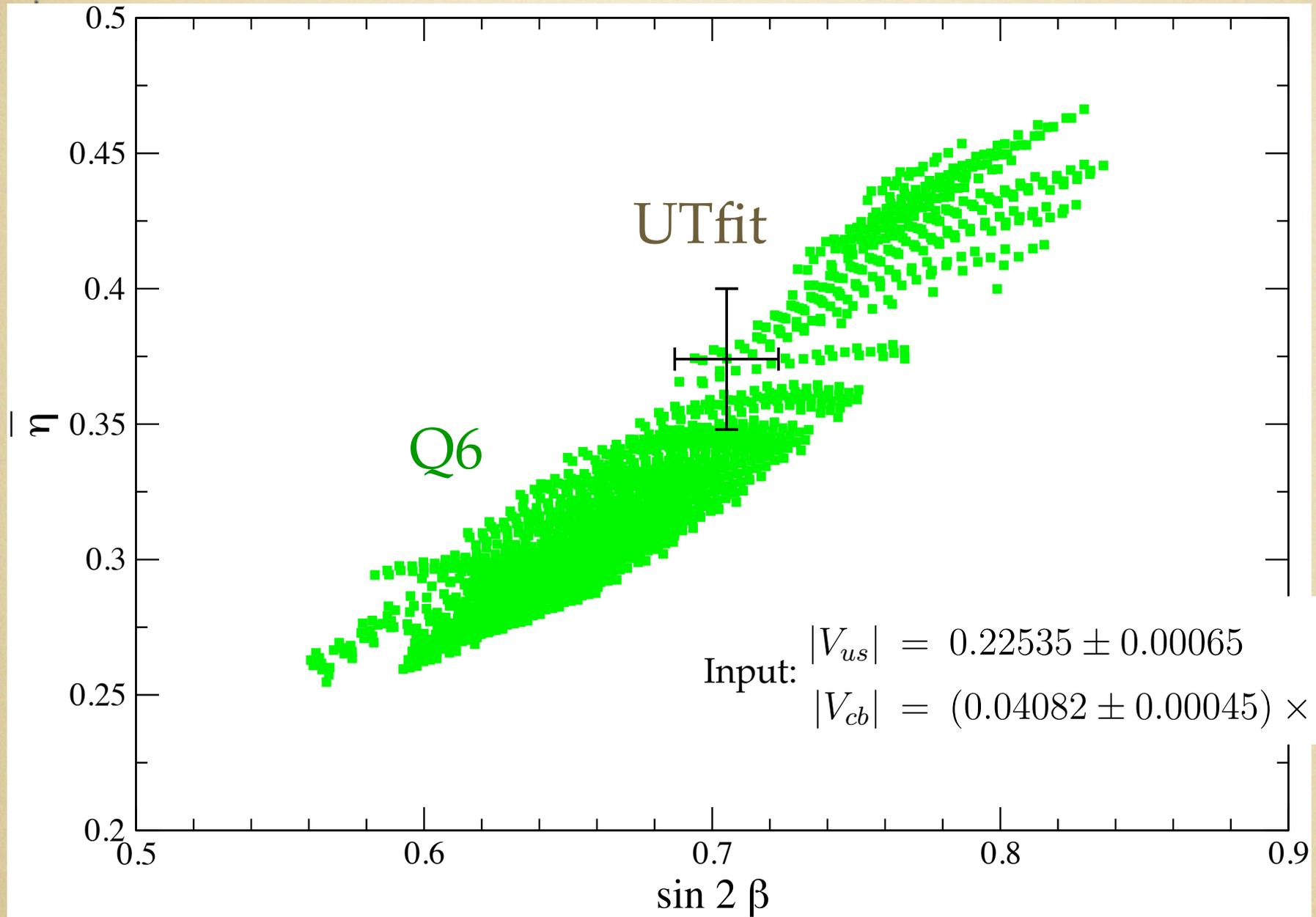
Q6 sum rule (Vacuum I)



using HPQCD mq with 2 sigma

Q6 sum rule

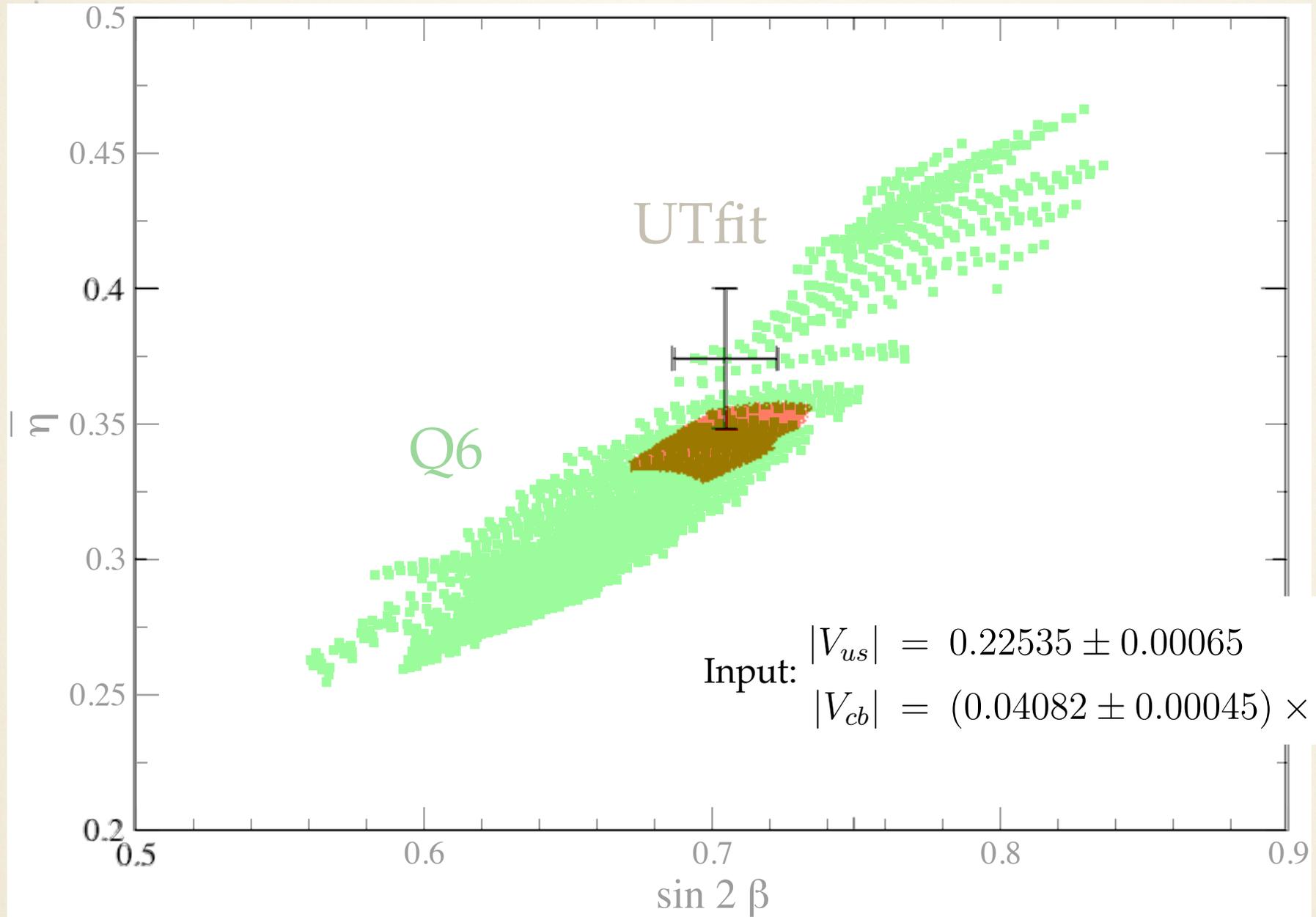
(Vacuum I)



using mq of PDG

Q6 sum rule

(Vacuum I)



using HPQCD mq with 2 sigma

Prediction in

$$i \frac{d}{dt} \begin{pmatrix} |B_q^0(t)\rangle \\ |\bar{B}_q^0(t)\rangle \end{pmatrix} = (\mathbf{M} - i\mathbf{\Gamma}) \begin{pmatrix} |B_q^0(t)\rangle \\ |\bar{B}_q^0(t)\rangle \end{pmatrix} \quad q = d, s$$

Lenz-Nierste parameterization

$$M_{12}^q = M_{12}^{SM,q} \cdot \Delta_q \quad \Delta_q = |\Delta_q| e^{i\phi_q^\Delta}$$
$$\Gamma_{12}^q = \Gamma_{12}^{SM,q} \quad \phi_q = \arg(-M_{12}^q / \Gamma_{12}^q)$$

Master equations for observables

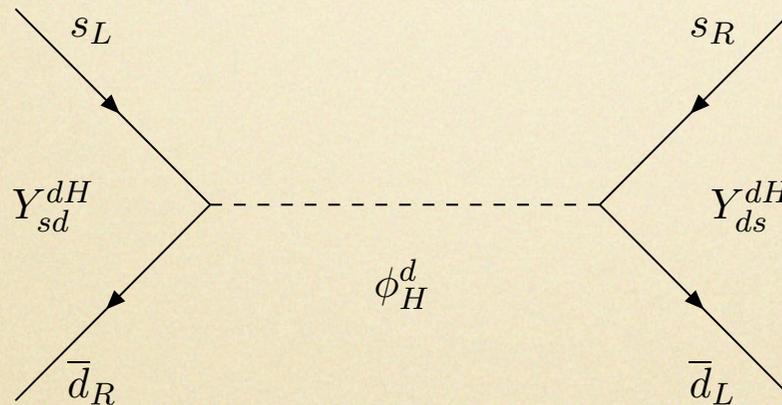
$$\Delta M_q = 2|M_{12}^{SM,q}| \cdot |\Delta_q|, \quad \Delta \Gamma_q = 2|\Gamma_{12}^q| \cos(\phi_q^{SM} + \phi_q^\Delta)$$
$$a_{sl}^q = \frac{|\Gamma_{12}^q|}{|M_{12}^{SM,q}|} \cdot \frac{\sin(\phi_q^{SM} + \phi_q^\Delta)}{|\Delta_q|}$$

In the Q6 model:

I. Extra Higgs sector

Tree-level contributions with real Yukawas

phase alignment



only real contribution to M_{12}^q

$$\Delta M_q \sim M_H^{-2} \quad \text{but small} \quad \phi_q^\Delta$$

II. SUSY breaking (at tree-level)

$$(\delta_{ij})_{LL,RR} = U_{L,R}^{q\dagger} \begin{pmatrix} a_{L,R} & 0 & 0 \\ 0 & a_{L,R} & 0 \\ 0 & 0 & b_{L,R} \end{pmatrix} U_{L,R}^q \quad \blacktriangleleft \text{2+1 family structure}$$

real

phase alignment

$$(\delta_{ij})_{LR} \sim A \text{ terms} + \mu \text{ terms}$$

EDMs

small μ s

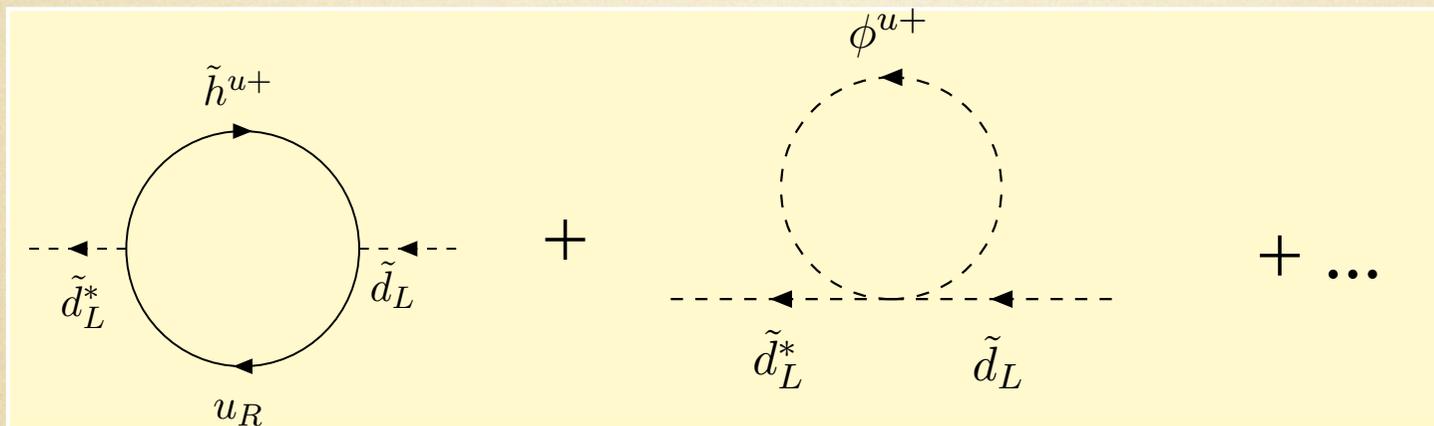
little contribution to $\text{Im } M_{12}^q$

$$I + II \quad \longrightarrow \quad -0.023 \lesssim \phi_s^\Delta \lesssim 0.009$$

Kawashima, JK and Lenz, PLB681,60 (2009)

III. Loop effects to (δ_{ij})

JK and Lenz, arXiv:1007.0680



quadratic and logarithmic ∞ cancel.

softness

flavor symmetry

However, large finite terms.

large susy breaking

small μ

and large M_H

EDM

FCNC

Mass of extra Higgions

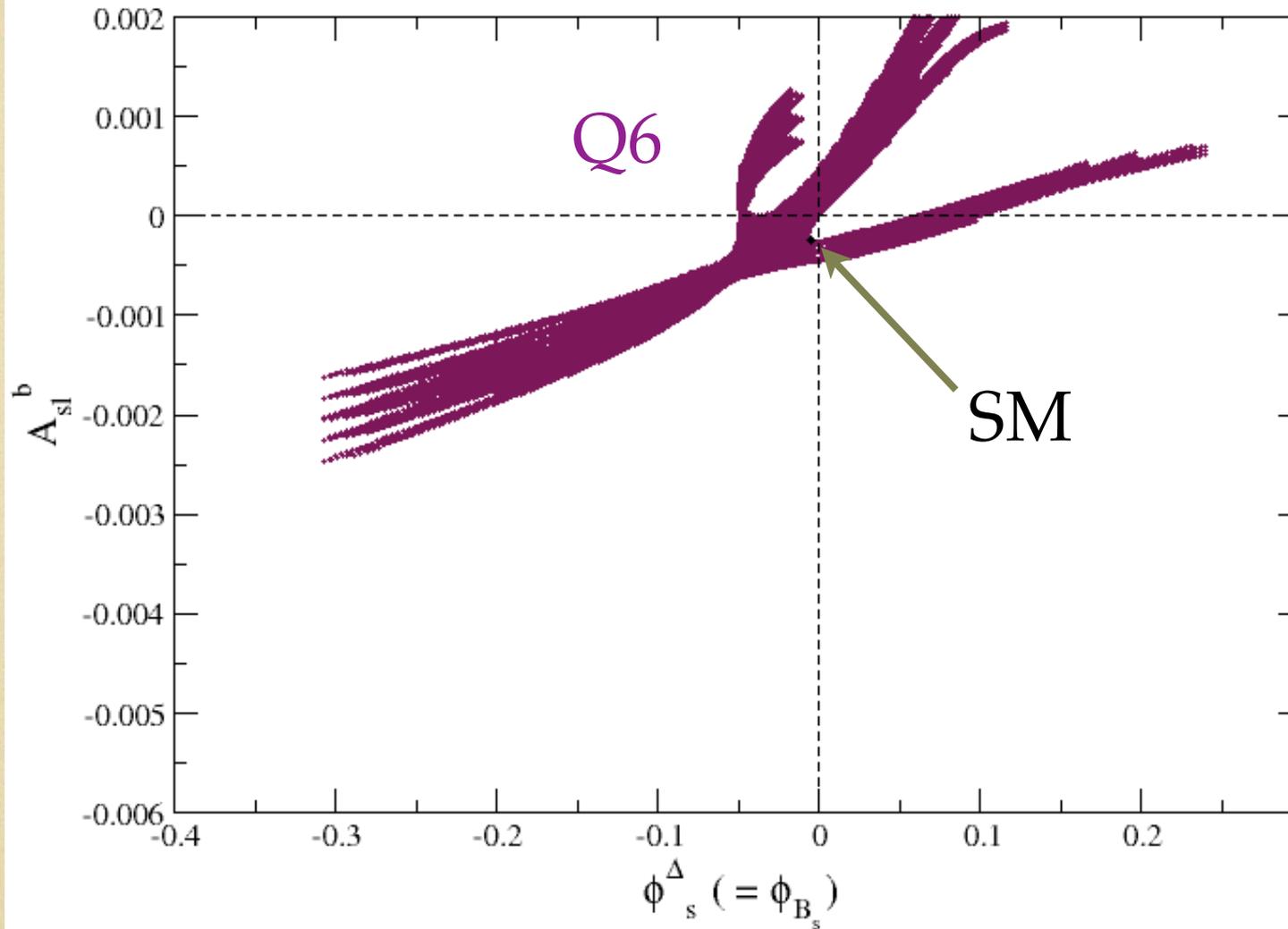
extra Higgbosons

$$(\delta_{23}^d)_{LL} \simeq -3.0 \times 10^{-2} \Delta a_L^q$$

tree

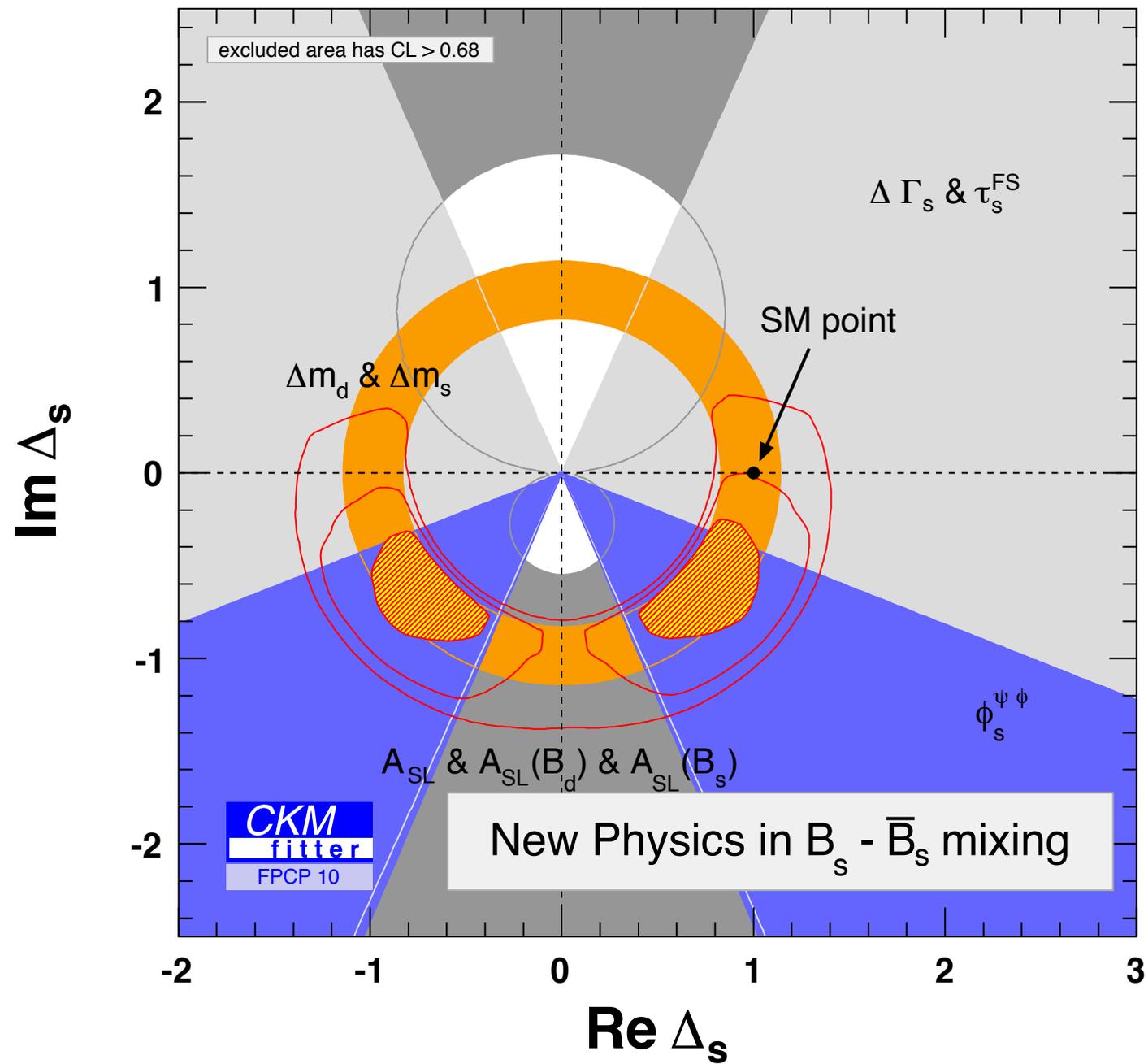
$$+ (0.05 - i 8.6) \times 10^{-2} \left[\frac{0.5 \text{ TeV}}{m_{\tilde{d}}} \right]^2$$

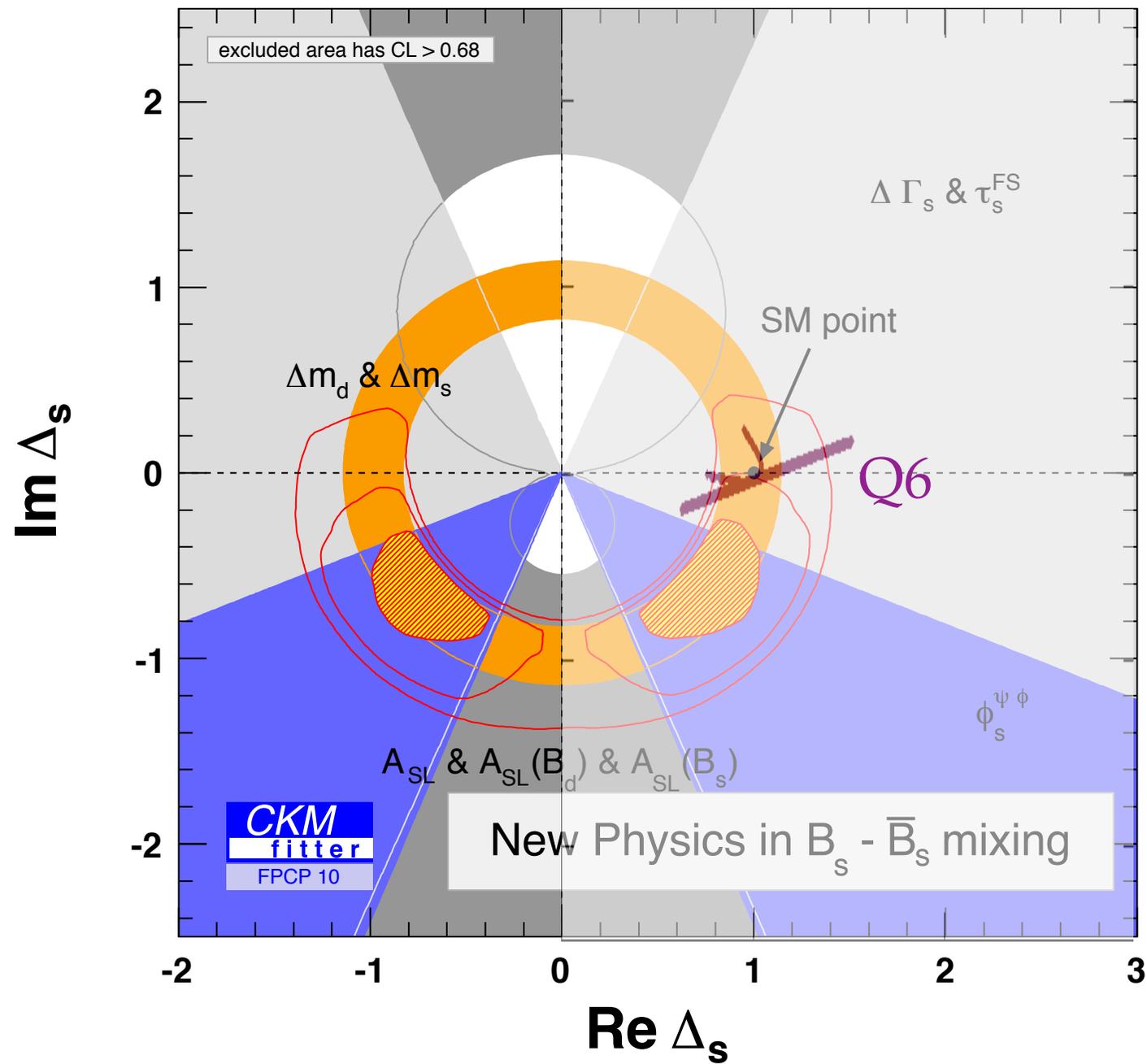
one-loop

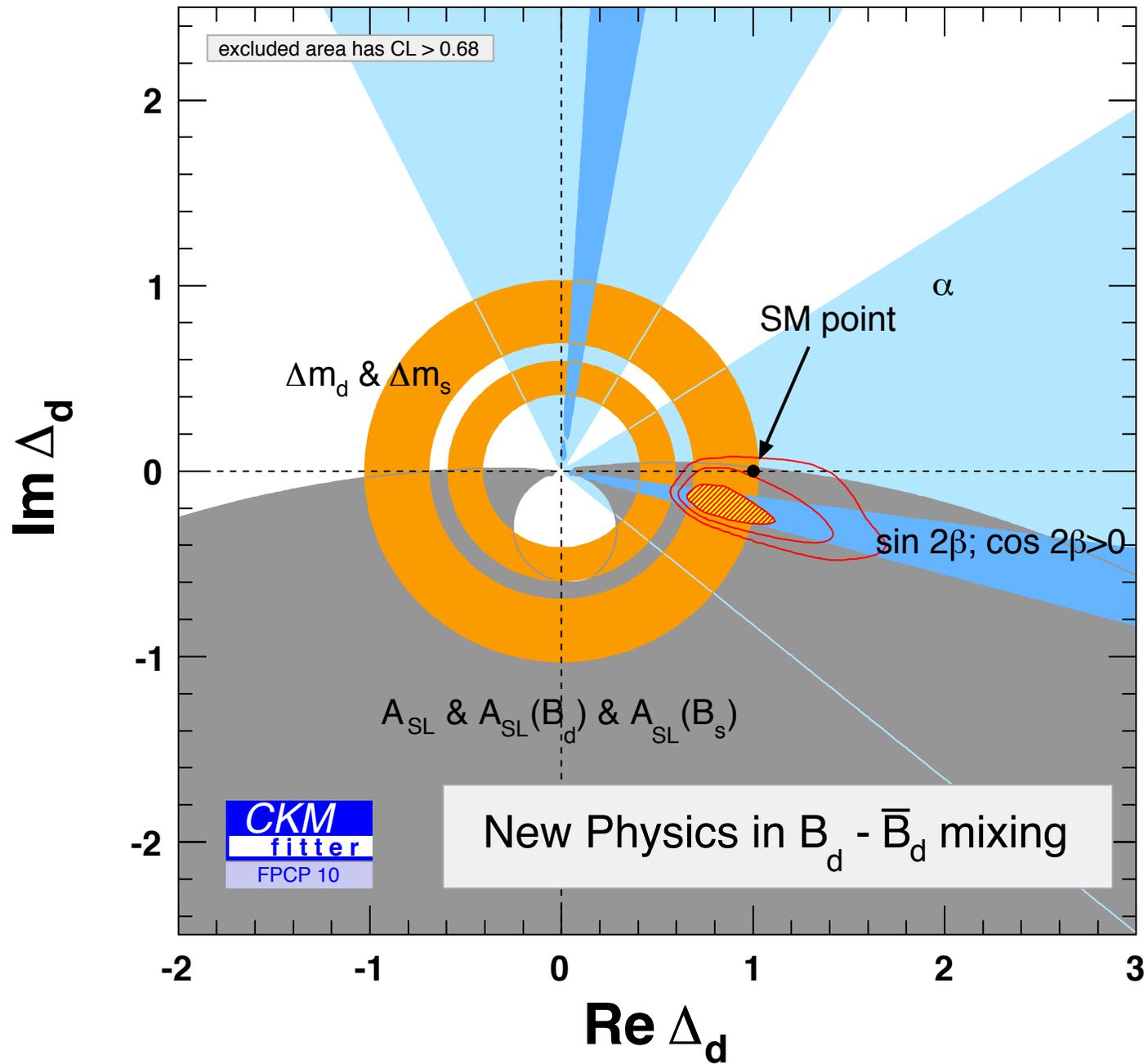


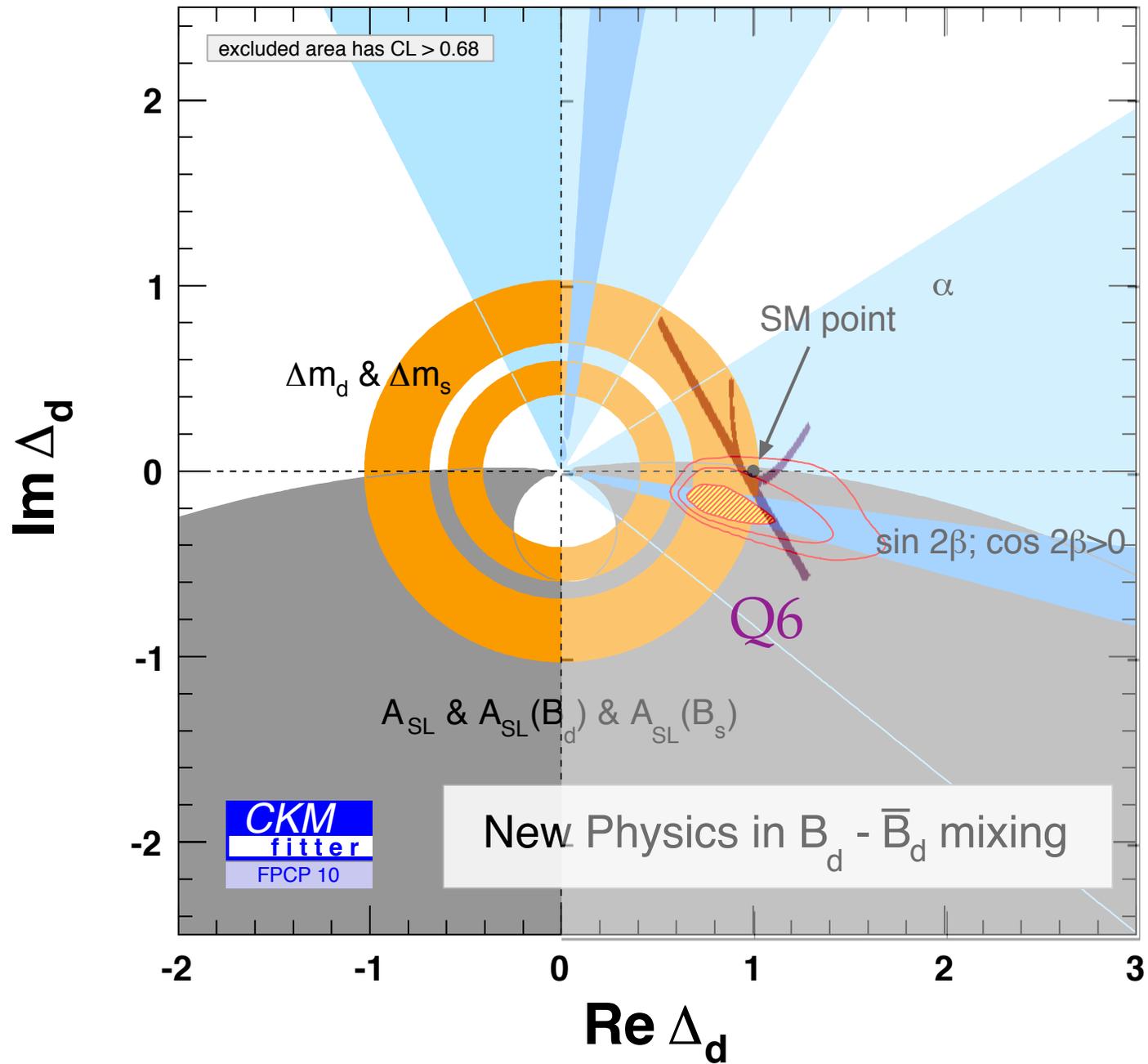
D0: $A_{sl}^b = -(9.57 \pm 2.51 \pm 1.46) \cdot 10^{-3}$

CDF: $\phi_s^\Delta \in [0, -1]$









Conclusion

*Flavor symmetry with spontaneous CP can nicely suppress FCNCs and CP in SUSY models.

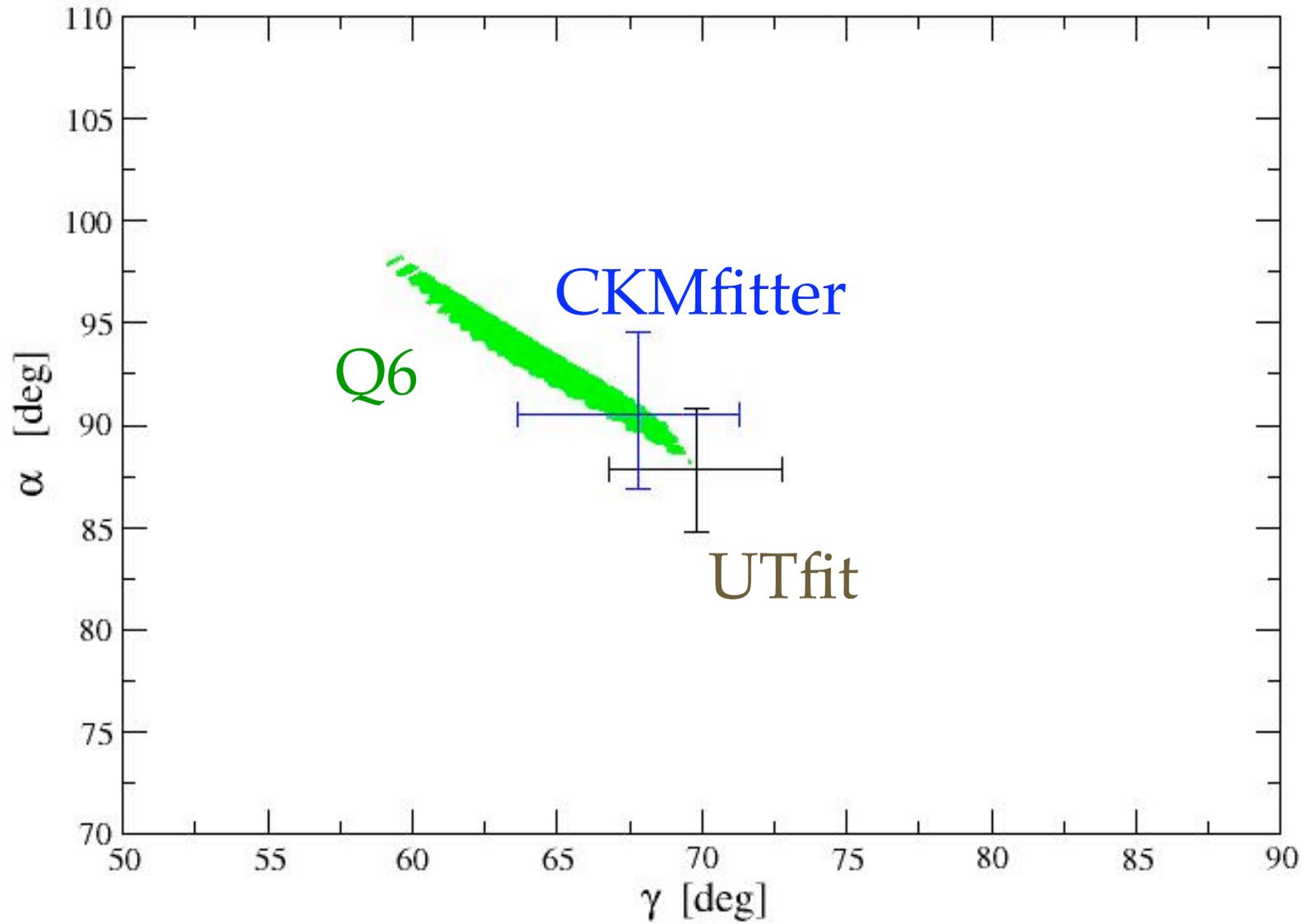
μ : small to suppress EDMs
 M_H : large to suppress FCNC

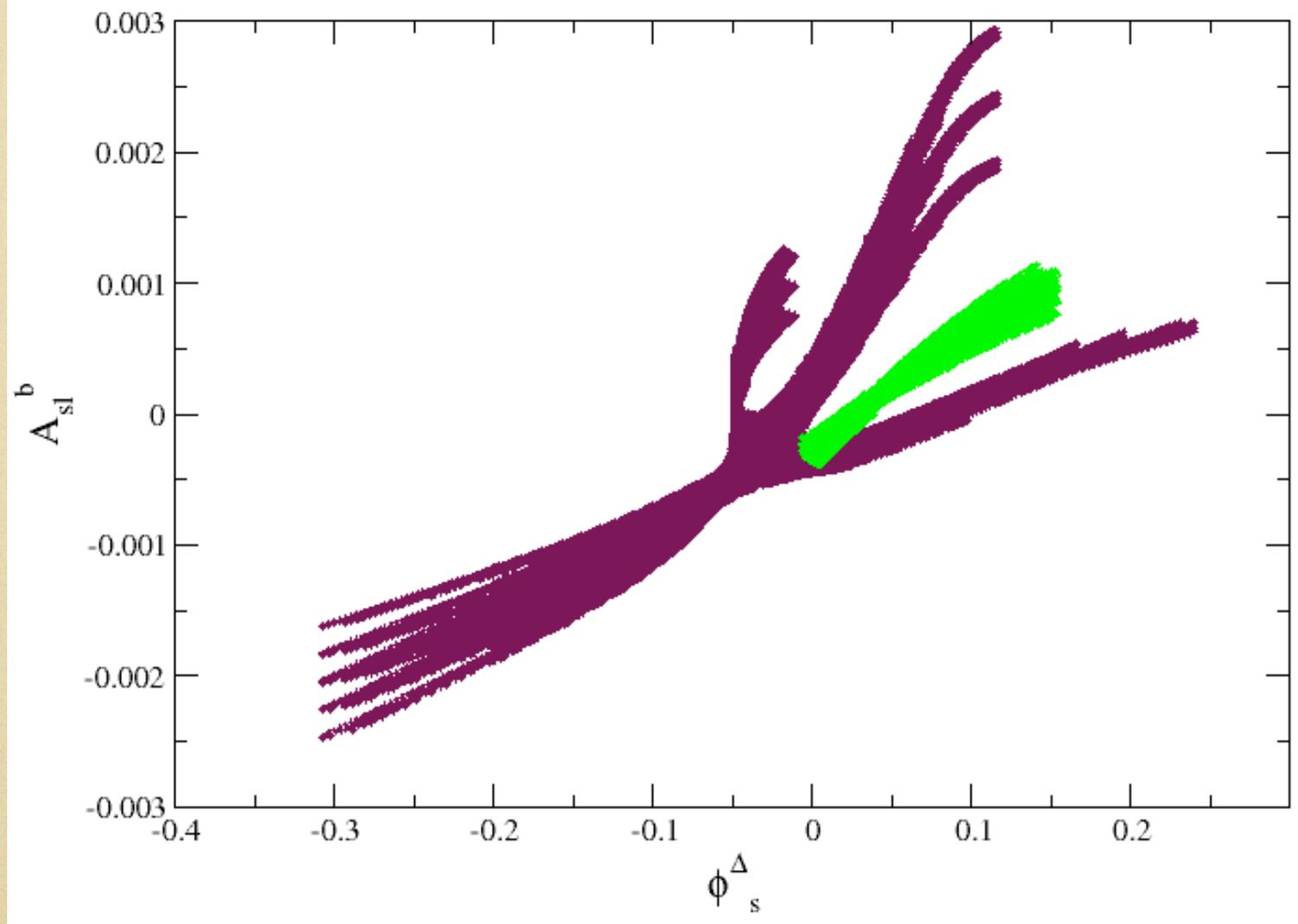
Large SUSY breaking in the extra Higgs sector

* Large loop effects to large CP in the B mixing

Danke Schön

Q6 sum rules (Vacuum I)





$$\begin{cases} \text{Im}(\delta_{11}^d)_{LR} = 3.7 \\ \text{Im}(\delta_{11}^u)_{LR} = 1.3 \end{cases} \times 10^{-6} \times \left[\frac{0.5 \text{ TeV}}{m_{\tilde{d}}} \right]^2$$

$$\left. \begin{array}{l} 0.6 \\ 0.8 \end{array} \right\} < \frac{\Delta M_{d,s}}{\Delta M_{d,s}^{\text{exp}}} < \begin{cases} 1.4 \\ 1.2 \end{cases}, \quad \frac{2|M_{12}^{\text{SUSY},K}|}{\Delta M_K^{\text{exp}}} < \begin{cases} 2 & I \\ 1 & II \end{cases}$$

$$\frac{\text{Im} M_{12}^{\text{SUSY},K}}{\sqrt{2} \Delta M_K^{\text{exp}}} < \epsilon_K = 2.2 \times 10^{-3},$$

Neutrino sector:

1. Inverted neutrino mass spectrum, i.e., $m_{\nu_3} < m_{\nu_1}, m_{\nu_2}$

$$2. m_{\nu_2}^2 / \Delta m_{23}^2 = \frac{(1+2t_{12}^2+t_{12}^4-rt_{12}^4)^2}{4t_{12}^2(1+t_{12}^2)(1+t_{12}^2-rt_{12}^2)} \cos^2 \phi_\nu - \tan^2 \phi_\nu$$

$$(r = \Delta m_{21}^2 / \Delta m_{23}^2, t_{12} = \tan \theta_{12})$$

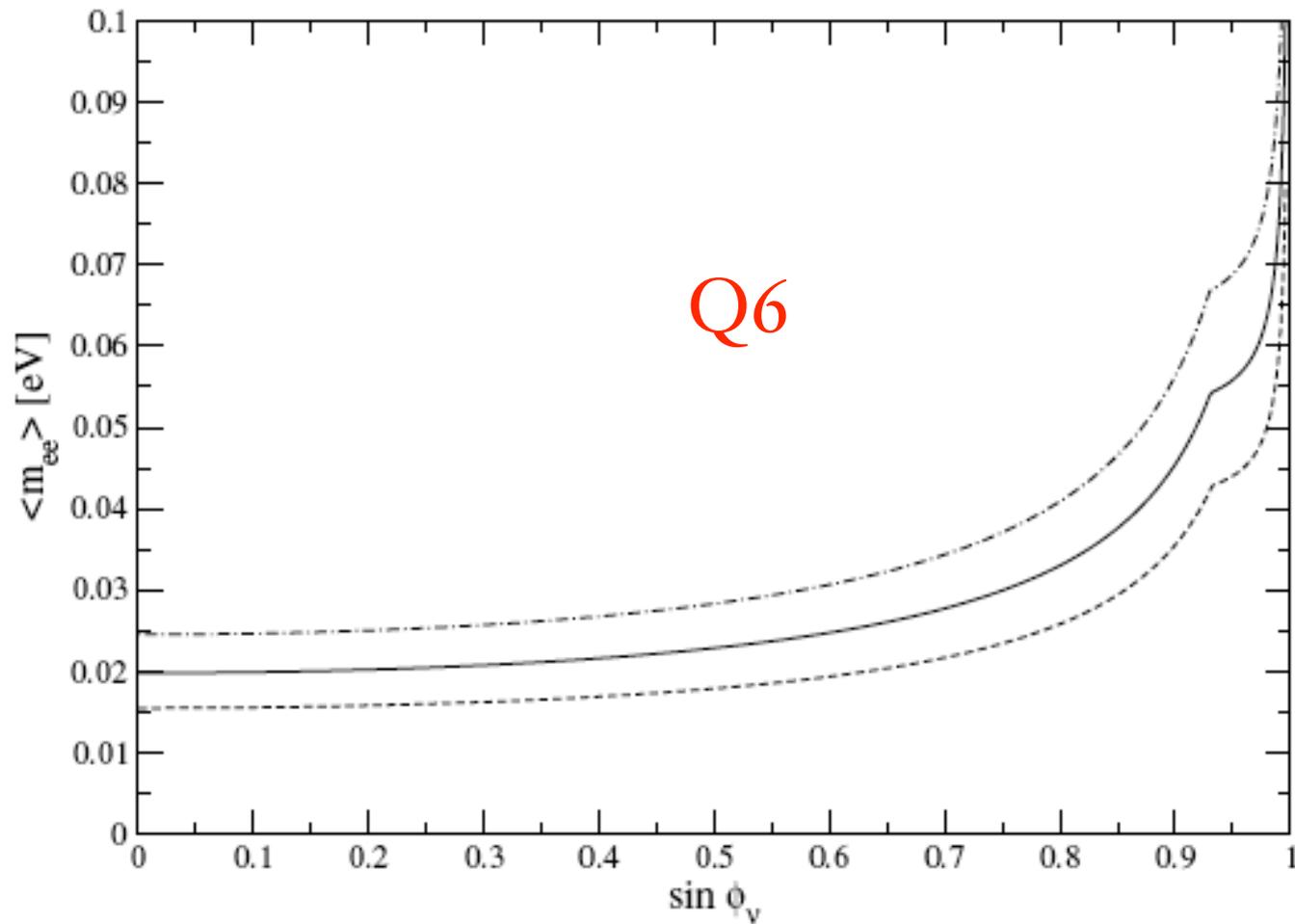
Dirac phase

$$3. \sin^2 \theta_{13} = \frac{1}{2} (m_e / m_\mu)^2 \simeq 10^{-6}$$

$$\sin^2 \theta_{23} = \frac{1}{2} + O((m_e / m_\mu)^2)$$

Violation of
 $\mu - \tau$ symmetry

*Almost maximal mixing
of the atm. neutrinos*



(*WMAP* : $\lesssim 0.17$ eV)

Input:

$$\sin^2 \theta_{12} = 0.3 \text{ and } \Delta m_{21}^2 = 6.9 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{23}^2 = 1.4, 2.3 \text{ and } 3.0 \times 10^{-3} \text{ eV}^2$$