

# "Anomalous" discrete symmetries

Michael Ratz



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Based on:

- M. Blaszczyk, S. Groot Nibbelink, F. Ruehle, M.R., M. Trapletti & P. Vaudrevange, Phys. Lett. B 683, 340-348 (2010)
- F. Brümmer, R. Kappl, M.R. & K. Schmidt-Hoberg, JHEP 1004:006 (2010)
- R. Kappl, B. Petersen, M.R., R. Schieren & P. Vaudrevange, to appear
- H.M. Lee, S. Raby, G. Ross, M.R., R. Schieren & P. Vaudrevange, to appear

# MSSM: good features and open questions

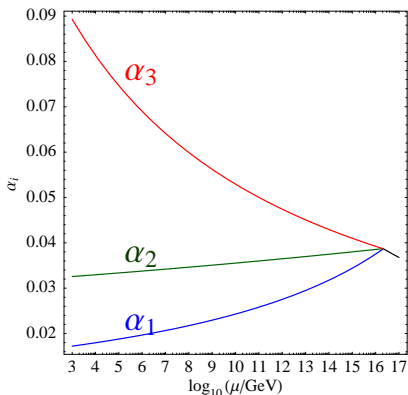
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- 😞 CP and flavor problems

➞ Supersymmetry alone seems not to be enough

# Outline

- ① Introduction & Motivation ✓
- ② A simple  $\mathbb{Z}_4^R$  symmetry can explain
  - suppressed  $\mu$  term
  - proton stability
- ③ String theory realization
- ④ Summary

# Proton decay operators

☞ Gauge invariant superpotential terms up to order 4 include

$$\begin{aligned}
 \mathcal{W} = & \mu H_d H_u + \kappa_i L_i H_u \\
 & + Y_e^{ij} L_i H_d \bar{E}_j + Y_d^{ij} Q_i H_d \bar{D}_j + Y_u^{ij} Q_i H_u \bar{U}_j \\
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forbidden by matter parity

Farrar & Fayet (1978); Dimopoulos, Raby & Wilczek (1981)

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Dreiner, Luhn & Thormeier (2006)

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☞ Proton hexality  $P_6 =$  matter parity  $\mathbb{Z}_2^M \times$  baryon triality  $B_3$

|                  | $Q$ | $\bar{U}$ | $\bar{D}$ | $L$ | $\bar{E}$ | $H_u$ | $H_d$ | $\bar{\nu}$ |
|------------------|-----|-----------|-----------|-----|-----------|-------|-------|-------------|
| $\mathbb{Z}_2^M$ | 1   | 1         | 1         | 1   | 1         | 0     | 0     | 1           |
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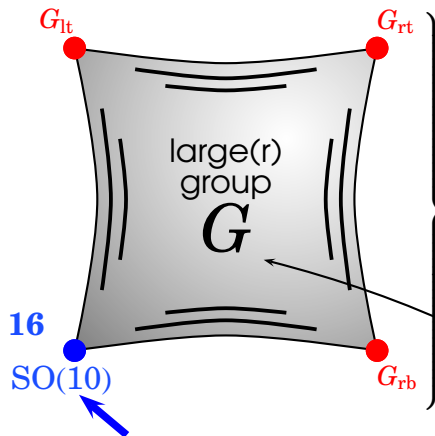
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# Local grand unification (using **small** extra dimensions)



Buchmüller, Hamaguchi, Lebedev, M.R. (2004-2006)  
 Lebedev, Nilles, Raby, Ramos-Sánchez,  
 M.R., Vaudrevange, Wingerter (2006)

'low-energy'  
 effective theory

standard  
 model  
 as an  
 intersection  
 of  $G_{rb}$ ,  $G_{rt}$ ,  $G_{lt}$   
 &  $SO(10)$   
 in  $G$

## SM generation(s):

localized in region with  
 $SO(10)$  symmetry

## Higgs doublets:

live in the 'bulk'

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need to be strongly suppressed

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  - **MSSM models with Local Grand Unification**
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- ➡ Two prejudices from string model building:
  - ① **Local Grand Unification**
  - ② **'anomalous' discrete symmetries** whose anomalies are canceled the **Green-Schwarz mechanism**

# From anomaly freedom to anomaly universality

Dine & Graesser (2004); Araki, Kobayashi, Kubo, Ramos-Sánchez, M.R. & Vaudrevange (2008)

☞ Important lesson from explicit string-derived (MSSM) models

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sum over all  
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sum over all fermions

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Dynkin index

discrete charges

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$$A_{G^2-\mathbb{Z}_N} = \sum_f \ell^{(f)} \cdot q^{(f)} \stackrel{!}{=} \gamma \mod N(2)$$

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## anomaly universality:

all  $A$  coefficients equal

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☞ Want to prove:

There is a unique  $\mathbb{Z}_4^R$  symmetry in the MSSM with these features

# Claim 1: it has to be an $R$ symmetry

☞ Anomaly coefficients for non- $R$  symmetry with  $SU(5)$  relations for matter charges

$$A_{SU(3)^2-\mathbb{Z}_N} = \frac{9}{2}q_{\mathbf{10}} + \frac{3}{2}q_{\overline{\mathbf{5}}}$$

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$$\leadsto \frac{1}{2}(q_{H_u} + q_{H_d}) = 0 \pmod{\begin{cases} N & \text{for } N \text{ odd} \\ N/2 & \text{for } N \text{ even} \end{cases}}$$

# Claim 1: it has to be an $R$ symmetry

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**bottom-line:**

non- $R$   $\mathbb{Z}_N$  symmetry cannot forbid  $\mu$  term

## Claim 2: Higgs discrete charges have to vanish

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# Claim 3: The order has to be 4 (or 2)

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$$A_{\text{SU}(2)^2 - \mathbb{Z}_N^R} - 4$$

however: there is no meaningful  $\mathbb{Z}_2^R$  symmetry

cf. e.g. Dine & Kehayias (2009)

$$r_{H_u} + r_{H_d} = 1 \pmod{N} \quad \left\{ \begin{array}{l} N \text{ odd} \\ N \text{ even} \end{array} \right.$$

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**bottom-line:**

$N = 4$  unique

# Unique $\mathbb{Z}_4^R$ symmetry

☞ We know:

- it is a  $\mathbb{Z}_4^R$  symmetry
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☞ Anomaly-free version of this  $\mathbb{Z}_4^R$  with extra matter has been discussed previously

# Implications of $\mathbb{Z}_4^R$

☞ Gauge invariant superpotential terms up to order 4

$$\begin{aligned}
 \mathcal{W} = & \mu H_d H_u + \kappa_i L_i H_u \\
 & + Y_e^{ij} L_i H_d \bar{E}_j + Y_d^{ij} Q_i H_d \bar{D}_j + Y_u^{ij} Q_i H_u \bar{U}_j \\
 & + \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k \\
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forbidden at the perturbative level

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appear at non-perturbative level

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also forbidden at  
non-perturbative level by  
non-anomalous  $\mathbb{Z}_2$  subgroup  
which is equivalent  
to matter parity

# Implications of $\mathbb{Z}_4^R$

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non-perturbative generation of  $\mu$  solves the  $\mu$  problem

# Implications of $\mathbb{Z}_4^R$

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non-perturbatively generated terms harmless

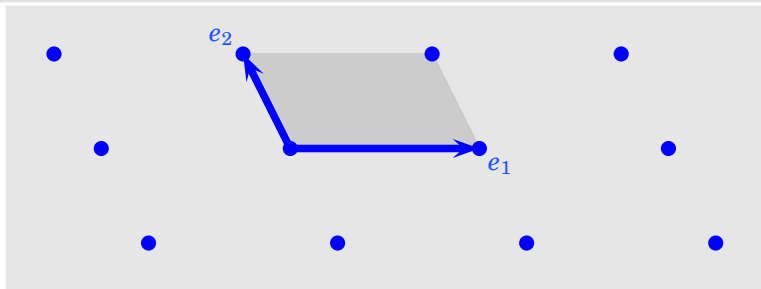
# **An explicit string-derived example**

...string theory allows us to understand the non-perturbative  
'violation' of 'anomalous' discrete symmetries

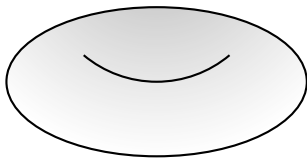
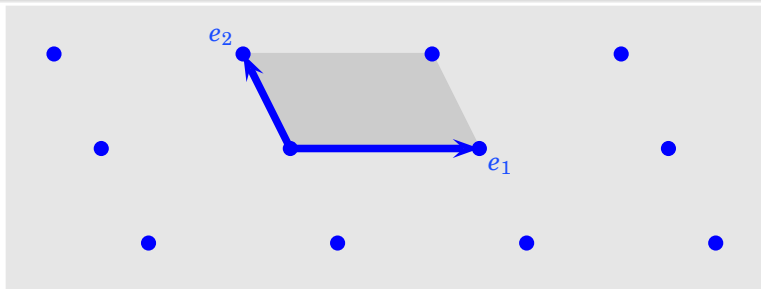
# The $\mathbb{Z}_2$ orbifold plane

2D space with  $SO(2)$  rotational symmetry

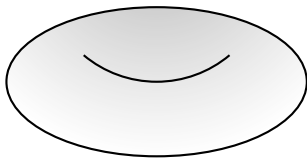
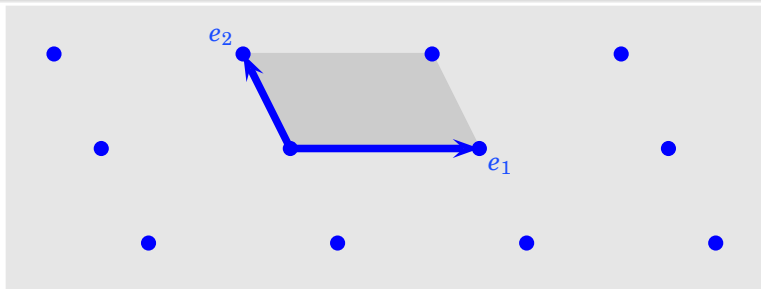
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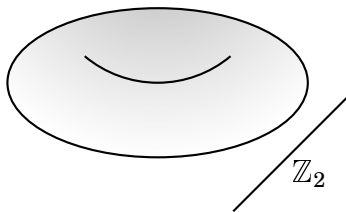
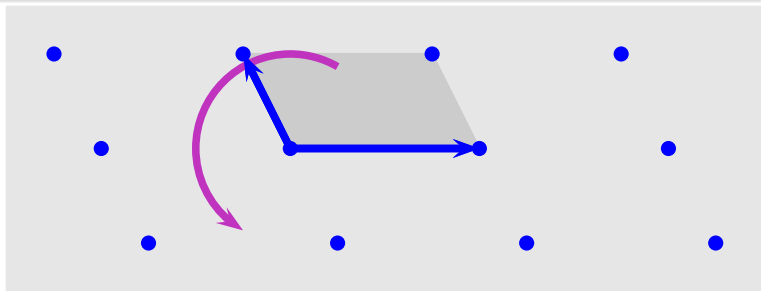
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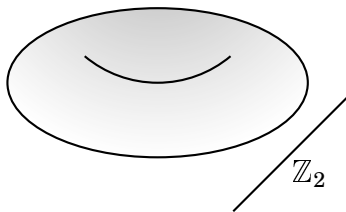
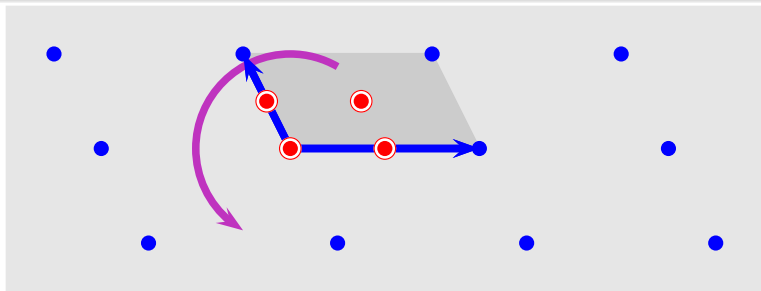
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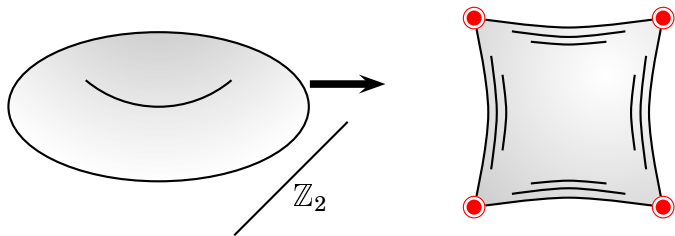
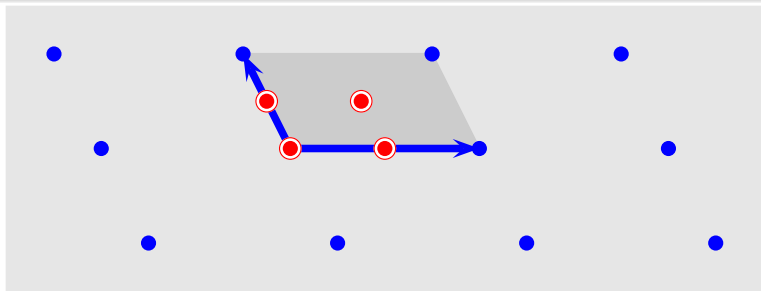
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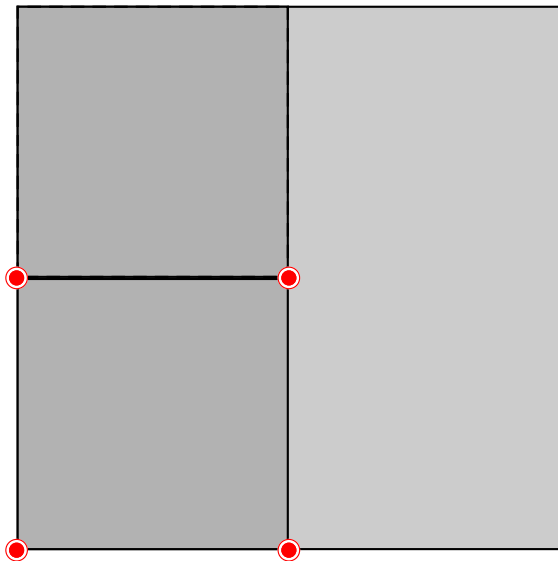
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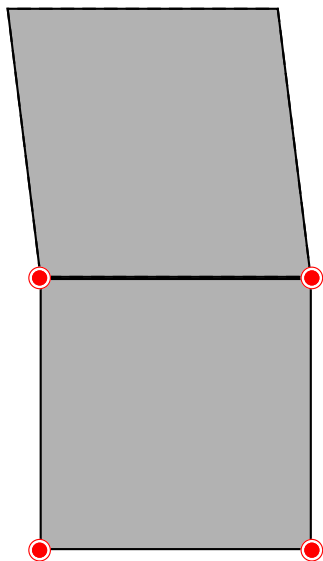
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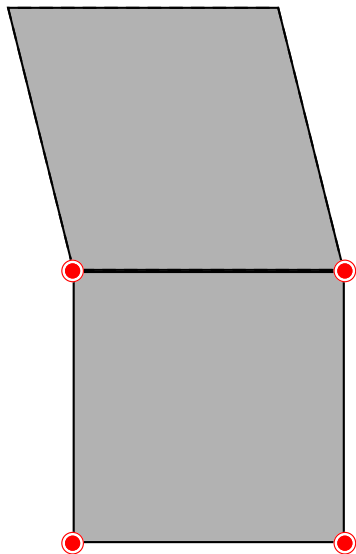
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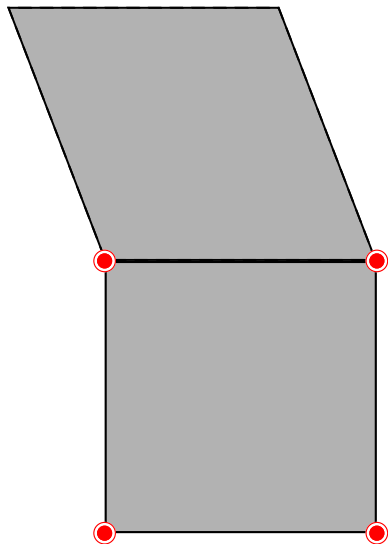
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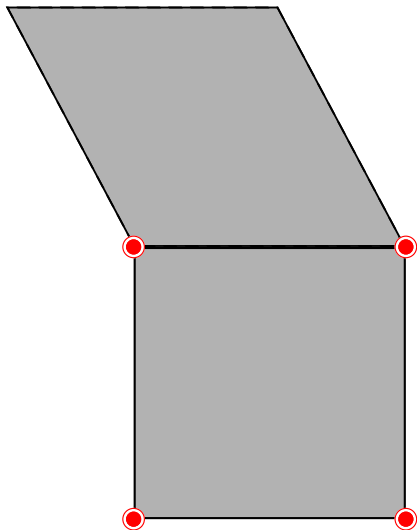
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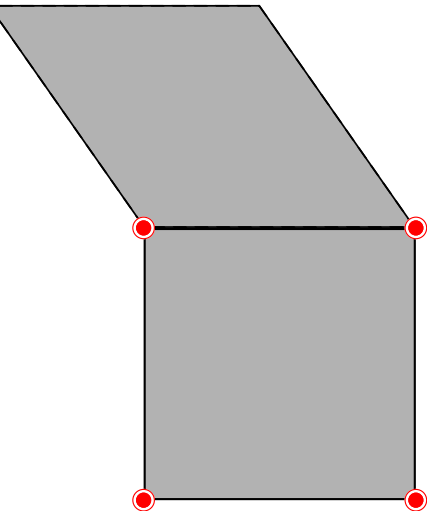
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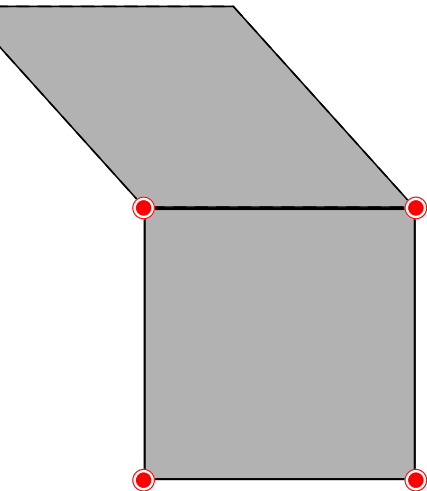
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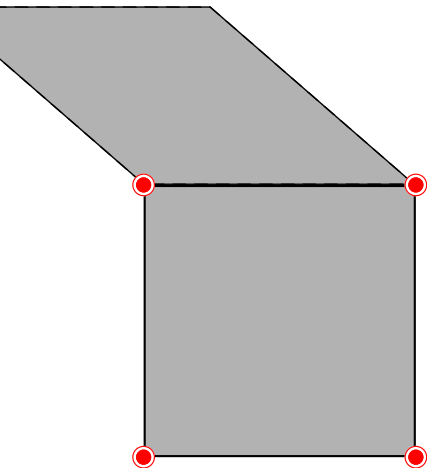
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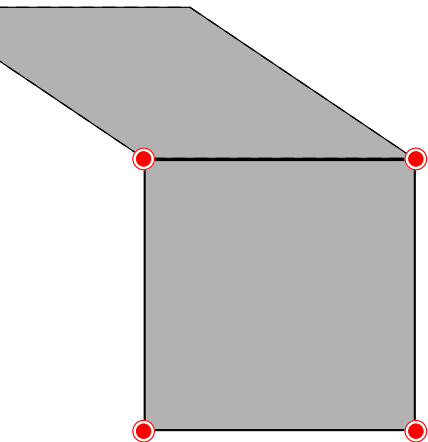
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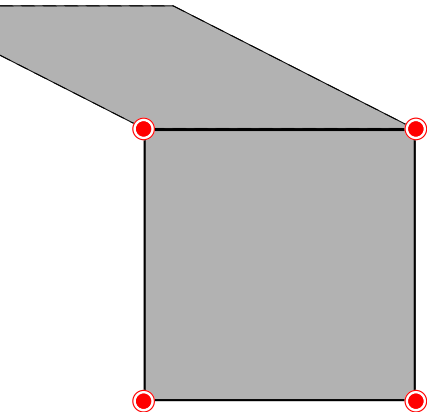
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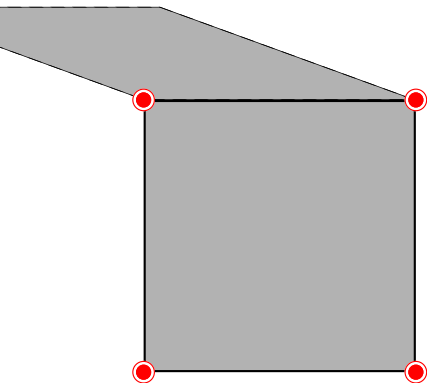
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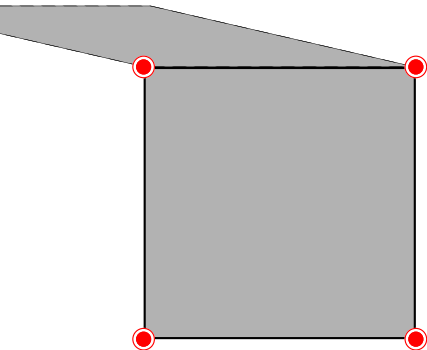
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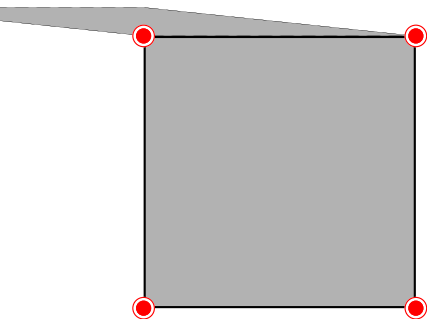
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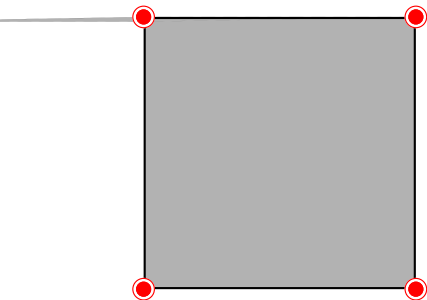
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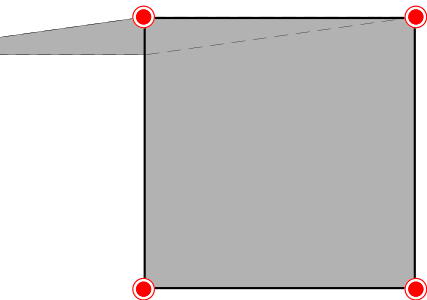
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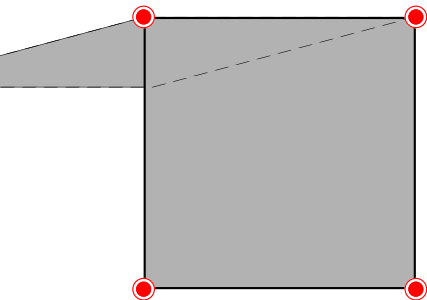
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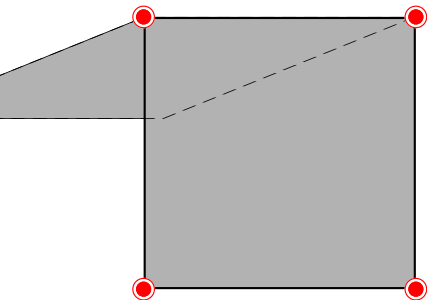
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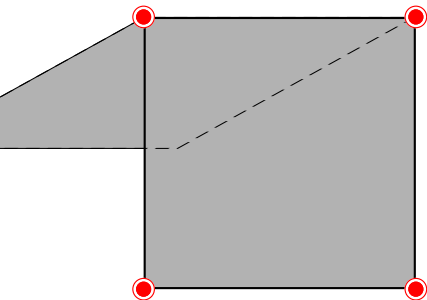
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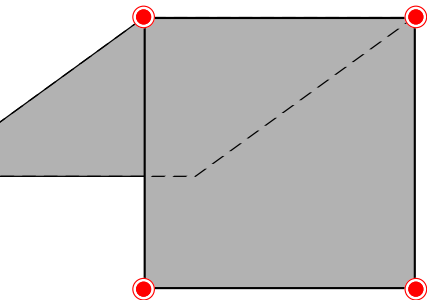
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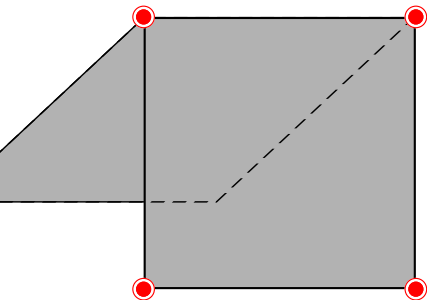
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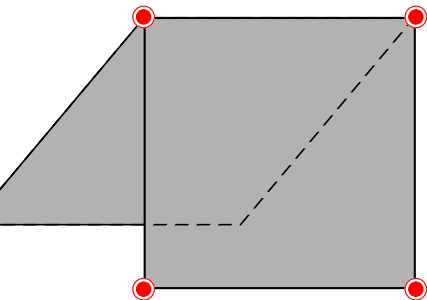
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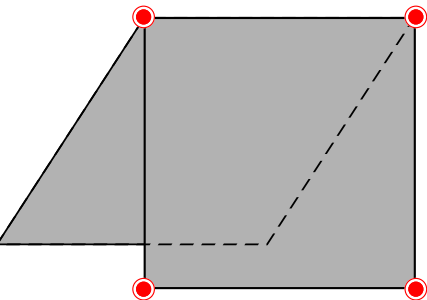
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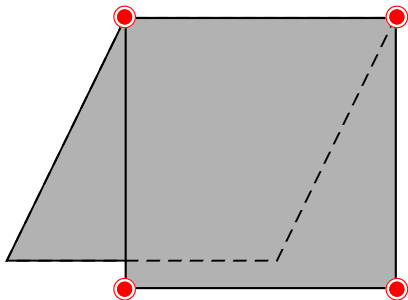
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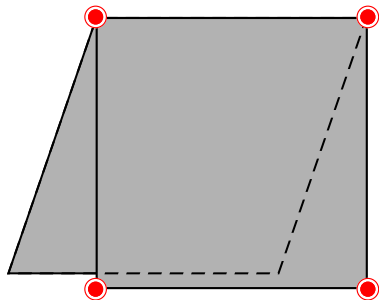
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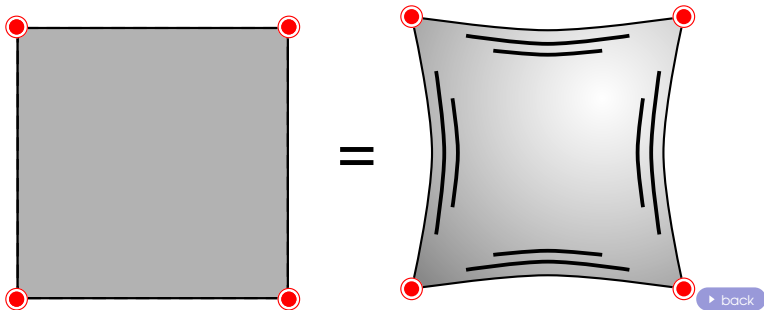
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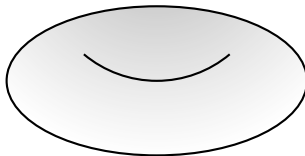
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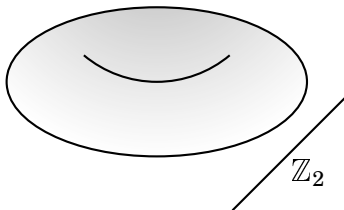
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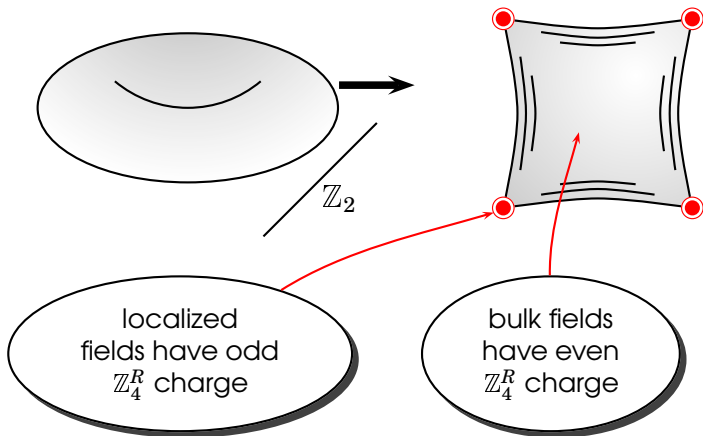
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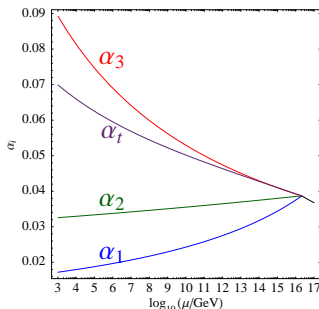


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P Hosteins, R. Kappl, M.R., K. Schmidt-Hoberg (2009)



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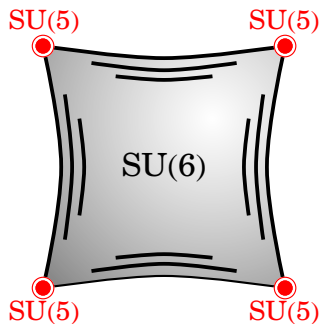
P. Hosteins, R. Kappl, M.R., K. Schmidt-Hoberg (2009)

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➡ Rest of this talk: discuss globally consistent string model with these features

# $\mathbb{Z}_2 \times \mathbb{Z}_2$ orbifold example

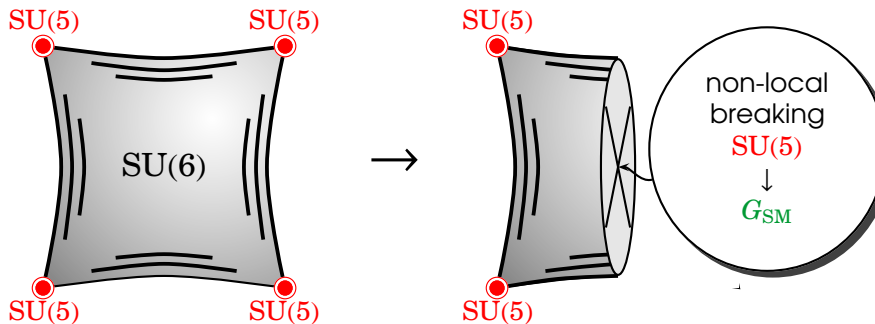
M. Blaszczyk, S. Groot Nibbelink, M.R., F. Ruehle, M. Trapletti, P. Vaudrevange (2009)



- ① step: 6 generation  $\mathbb{Z}_2 \times \mathbb{Z}_2$  model with  $SU(5)$  symmetry

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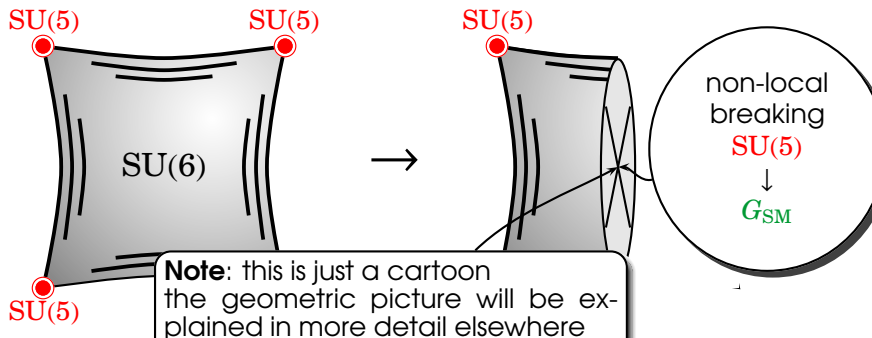
- ① step: 6 generation  $\mathbb{Z}_2 \times \mathbb{Z}_2$  model with  $SU(5)$  symmetry
- ② step: mod out a freely acting  $\mathbb{Z}_2$  symmetry which:
  - breaks  $SU(5) \rightarrow SU(3)_C \times SU(2)_L \times U(1)_Y$
  - reduces the number of generations to 3

analogous mechanism in CY MSSMs Bouchard & Donagi (2005)

Braun, He, Ovrut, Pantev (2005)

# $\mathbb{Z}_2 \times \mathbb{Z}_2$ orbifold example

M. Blaszczyk, S. Groot Nibbelink, M.R., F. Ruehle, M. Trapletti, P. Vaudrevange (2009)



① step: 6 generations

M. Fischer, M.R., P. Vaudrevange (to appear)

symmetry

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for further discussion of this model see talks by M. Blaszczyk & S. Groot Nibbelink

# Main features

- 1 GUT symmetry breaking **non-local**  
↪ no 'logarithmic running above the GUT scale'

Hebecker, Trappetti (2004)

- ↪ **precision gauge unification**  
with **distinctive pattern of soft masses**

Raby, M.R., Schmidt-Hoberg (2009)

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- 1 GUT symmetry breaking **non-local**
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     $\leadsto$  complete blow-up without breaking SM gauge symmetry in principle possible

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$$\text{spectrum} = 3 \times \text{generation} + \text{vector-like}$$

- 5 Various appealing features:
  - vacua where **exotics** decouple at the linear level in SM singlets
  - non-trivial Yukawa couplings
  - gauge-top unification
  - SU(5) relation  $y_\tau \simeq y_b$  (but also for light generations)

P. Hosteins, R. Kappl, M.R., K. Schmidt-Hoberg (2009)

for further discussion of this model see talks by M. Blaszczyk & S. Groot Nibbelink

# 'Anomalous' $\mathbb{Z}_4^R$ from the Blaszczyk et al. model

☞ We succeeded in finding vacua with the 'anomalous'  $\mathbb{Z}_4^R$   
... e.g. by switching on the fields

$$\{\phi_i\} = \{X_3, X_4, X_5, \overline{X}_4, \overline{X}_5, Y_1, Y_2, Z_1, Z_2, N_1, N_2, N_6, \\ N_{11}, N_{17}, N_{25}, N_{26}, N_{28}, N_{35}, N_{37}, N_{45}, N_{47}, N_{49}, N_{51}, N_{53}, N_{55}\}$$

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☞ Two conditions:

- vanishing  $F$  terms (no time to discuss)
- vanishing  $D$  terms

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dilaton

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**bottom-line:**

FI monomials consistent with t'Hooft instantons

# Non-perturbative violation of $\mathbb{Z}_4^R$

R. Kappl, B. Petersen, M.R., R. Schieren & P. Vaudrevange (to appear)

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$$\mathcal{W}_{\text{ADS}} = \left( \frac{\Lambda^{3N_c - N_f}}{\det M} \right)^{\frac{1}{N_c - N_f}}$$

is also  $\mathbb{Z}_4^R$  covariant

$$\Lambda \simeq \mu \exp \left( -8\pi^2 \frac{1}{3N_c - N_f} \frac{1}{g^2(\mu)} \right)$$

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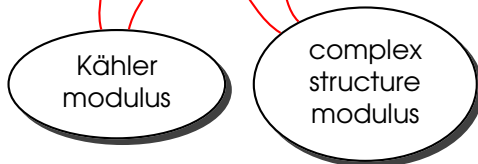
# $\mu$ from $\mathcal{W}$

F. Brümmer, R. Kappl, M.R., K. Schmidt-Hoberg (2009)

☞ Higher-dimensional gauge invariance  $\leadsto$  Kähler potential

Antoniadis, Gava, Narain & Taylor (1994); Choi et al. (2003)

$$K = -\ln \left[ \left( \overline{T}_3 + T_3 \right) \left( \overline{Z} + Z \right) - \left( \overline{H}_u + H_d \right) \left( \overline{H}_d + H_u \right) \right]$$




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Higgs fields  
= extra components  
of gauge fields

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normalized  
Higgs  
fields



$\mu$  from  $\mathcal{W}$ 

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➡ Consider now superpotential

$\mathcal{W} = \Omega =$  independent of the monomial  $\hat{H}_u \hat{H}_d$

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☞  $K$  &  $\mathcal{W}$  in leading order in  $\hat{H}_u \hat{H}_d$  equivalent to

$$K' = -\ln \left[ \left( T_3 + \overline{T}_3 \right) \left( Z + \overline{Z} \right) \right] + \left[ |\hat{H}_u|^2 + |\hat{H}_d|^2 \right]$$

$$\mathcal{W}' = \exp(\hat{H}_u \hat{H}_d) \Omega = \Omega \hat{H}_u \hat{H}_d + \dots$$

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**bottom-line:**

$\mu$  term proportional to  $\langle \Omega \rangle$

# Non-perturbative violation of $\mathbb{Z}_4^R$ (cont'd)

☞ Since  $H_u H_d$  is proportional to  $\langle \mathcal{W} \rangle$  we will get a holomorphic contribution to the  $\mu$  term of the right order

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... for instance, one may replace/describe hidden sector superpotential by gaugino condensate

Nilles (1982)

$$\langle \mathcal{W} \rangle \simeq \langle \lambda\lambda \rangle \simeq \Lambda^3$$

- this is consistent with a non-perturbative breaking of  $\mathbb{Z}_4^R$
- this assumes that the dilaton is fixed somehow (Kähler stabilization ...)

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- ☞ Dimension 5 proton decay operators will have highly suppressed coefficients

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- ☞ No  $R$  parity violation because  $\mathbb{Z}_4^R$  has a non-anomalous subgroup which is equivalent to matter parity

**Summary**

**&**

**outlook**

# Summary – bottom-up



A simple 'anomalous'  $\mathbb{Z}_4^R$  symmetry can

- provide a solution to the  $\mu$  problem
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universal anomaly coefficients  
universal charges for matter  
forbid  $\mu$  @ tree-level  
allow Yukawa couplings  
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$\mathbb{Z}_4^R \leadsto$ 
 {
   
 dim. 4 proton decay operators completely forbidden
   
 dim. 5 proton decay operators highly suppressed
   
 $\mu$  appears non-perturbatively

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# Summary – top-down

- ✎ Embedding into string theory allows us to understand where the  $\mathbb{Z}_4^R$  symmetry comes from: it may arise as a discrete remnant of Lorentz symmetry in extra dimensions
- ✎ Such symmetries are on the same footing as the fundamental symmetries  $C, P$  and  $T$
- ✎ Guided by the (unique)  $\mathbb{Z}_4^R$  symmetry we have constructed a globally consistent string model with:
  - exact MSSM spectrum
  - non-trivial Yukawa couplings
  - exact matter parity
  - $\mu \sim m_{3/2}$
  - dimension five proton decay operators sufficiently suppressed

**Vielen  
Dank!**