

Application of XCCA for nanoparticle self-assembly and colloidal phase transitions

Felix Lehmkuhler

Fluctuation X-Ray Scattering Workshop
June 2021

Correlation studies with coherent X-ray scattering

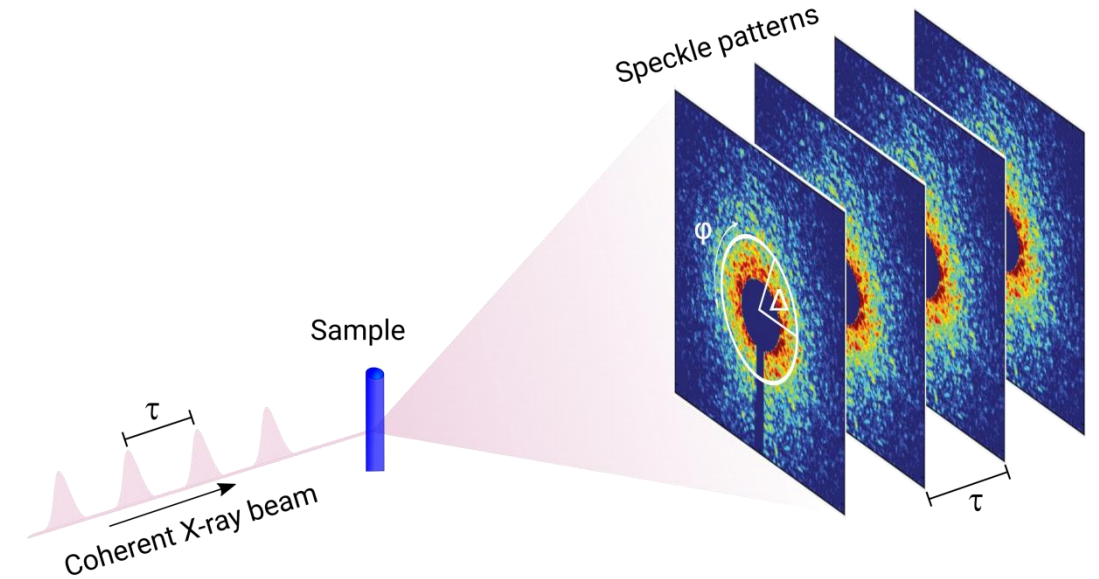
Spatial correlations: X-ray Cross Correlation Analysis (XCCA)

- Orientational structure beyond pair correlation functions
- Angular correlations $C(\Delta) = \langle I(\varphi)I(\varphi + \Delta) \rangle_\varphi$

Time correlations: X-ray photon correlation spectroscopy (XPCS)

- Analogue to dynamic light scattering (DLS)
- Temporal correlations $C(\tau) = \langle I(t)I(t + \tau) \rangle_t$

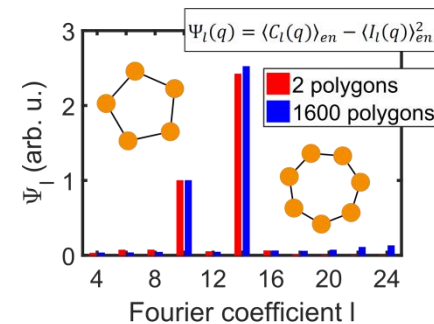
Nanoscale: SAXS



XCCA

Cross-correlation function

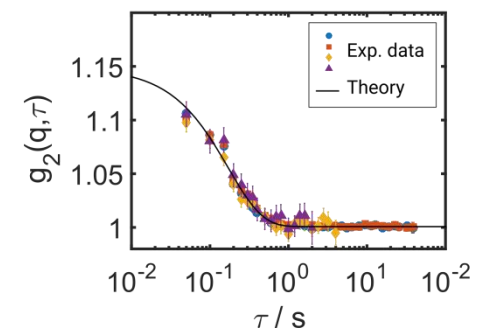
$$C(q, \Delta) = \frac{\langle I(q, \varphi)I(q, \varphi + \Delta) \rangle_\varphi - \langle I(q, \varphi) \rangle_\varphi^2}{\langle I(q, \varphi) \rangle_\varphi^2}$$



XPCS

Intensity-intensity time autocorrelation function

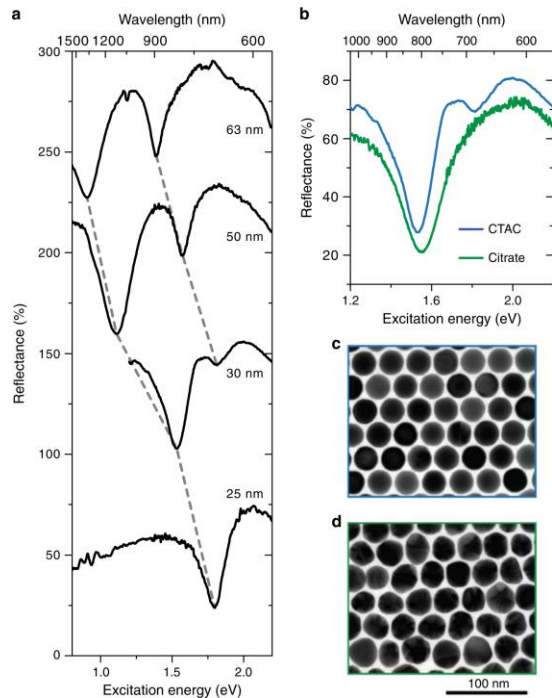
$$g_2(q, \tau) = \frac{\langle I(q, t)I(q, t + \tau) \rangle_t}{\langle I(q, t) \rangle_t^2}$$



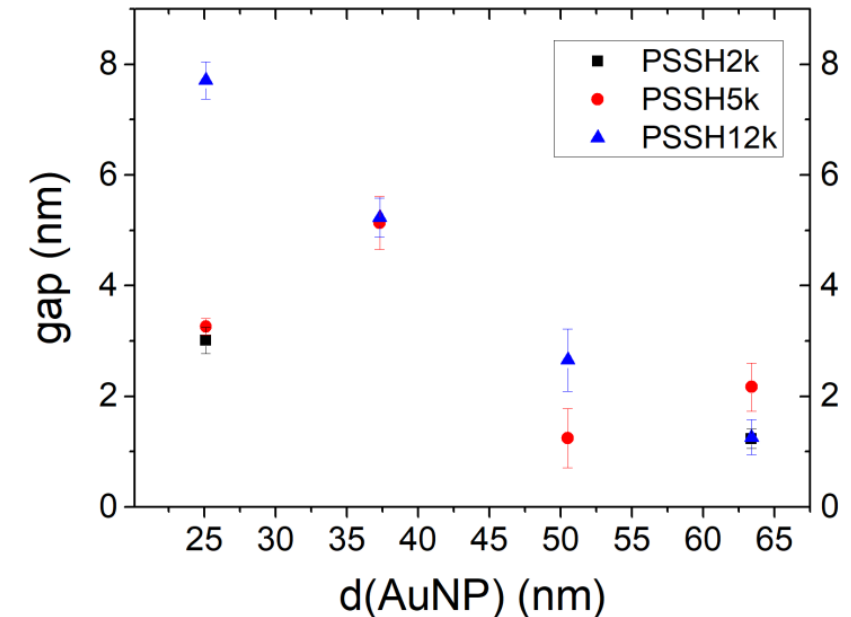
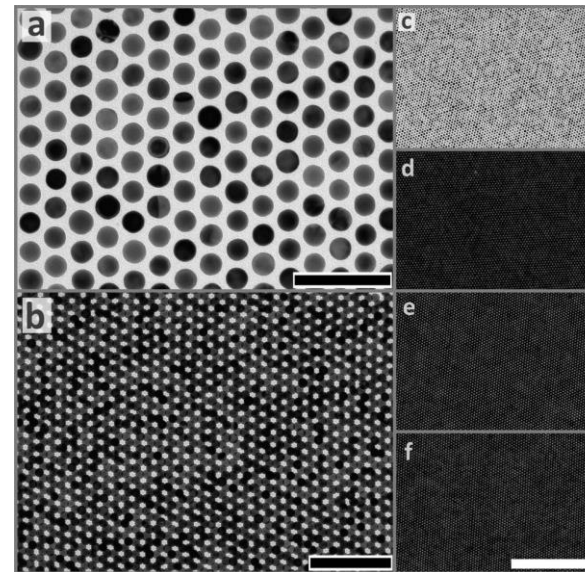
Example 1: Structure of self-assembled films

- Plasmonic NP: structure of assemblies correlates with emergence of coupled plasmon modes
- Deep strong coupling under ambient conditions

- Particles dried on TEM grids
- Polystyrene-coated Au particles
 - Gold core of 12 nm radius
 - Tune distance by ligand length

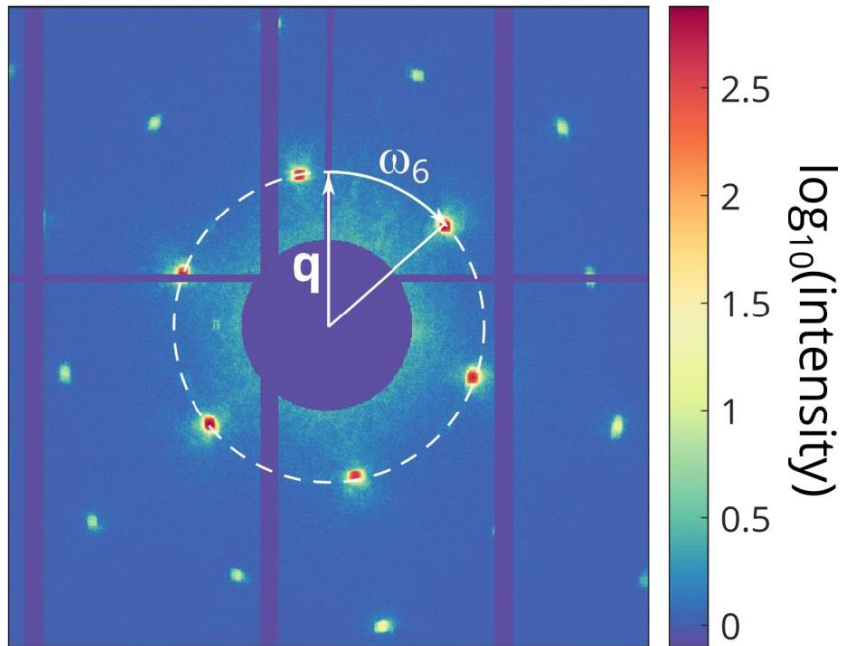


- Reflectance and polaritonic modes



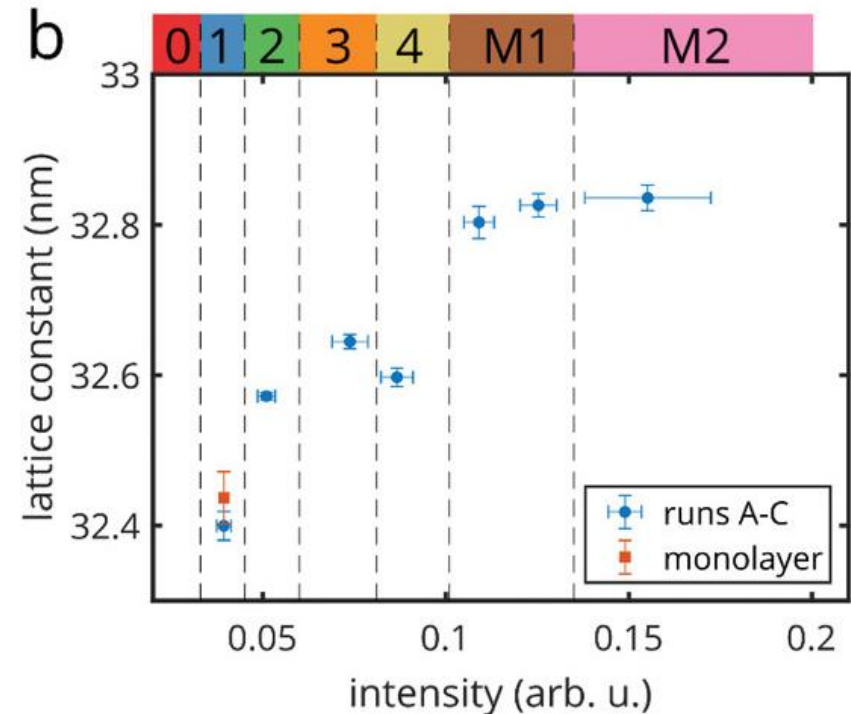
Example 1: Structure of self-assembled films

- Scanning SAXS approach at P10 (PETRA III)
- Beamsizes about $1\ \mu\text{m}$ = scan step size
- Intensity + order maps
- Fourier coefficients $I_\ell(q) = |I_\ell(q)| \exp(i\Omega_\ell(q))$

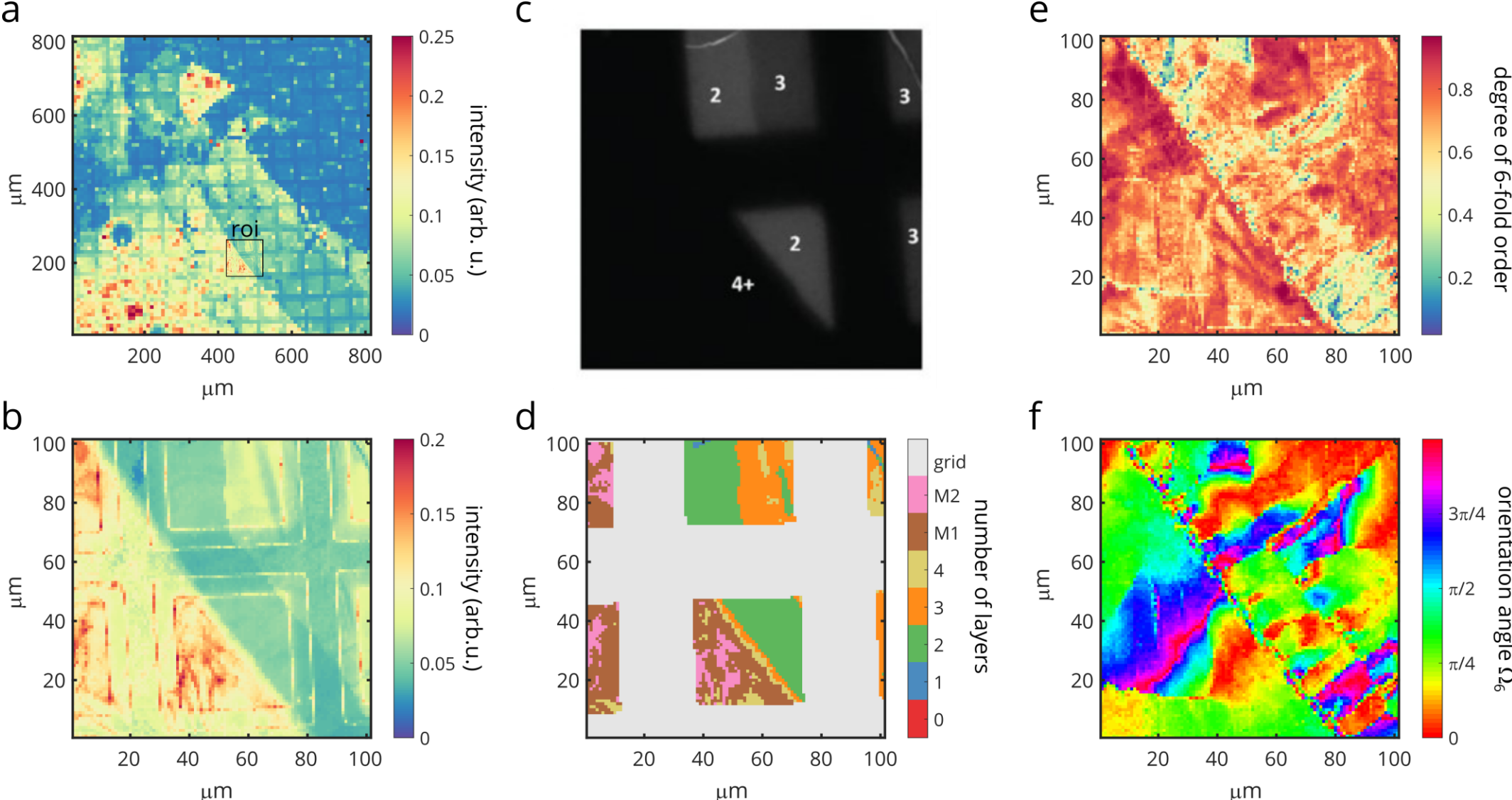


Conventional SAXS analysis

- Identify number of layers by scattering intensity
- Lattice constant

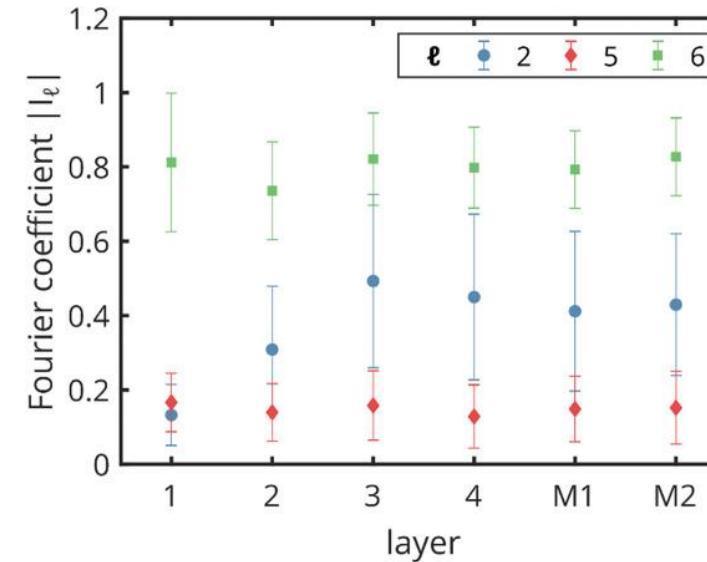
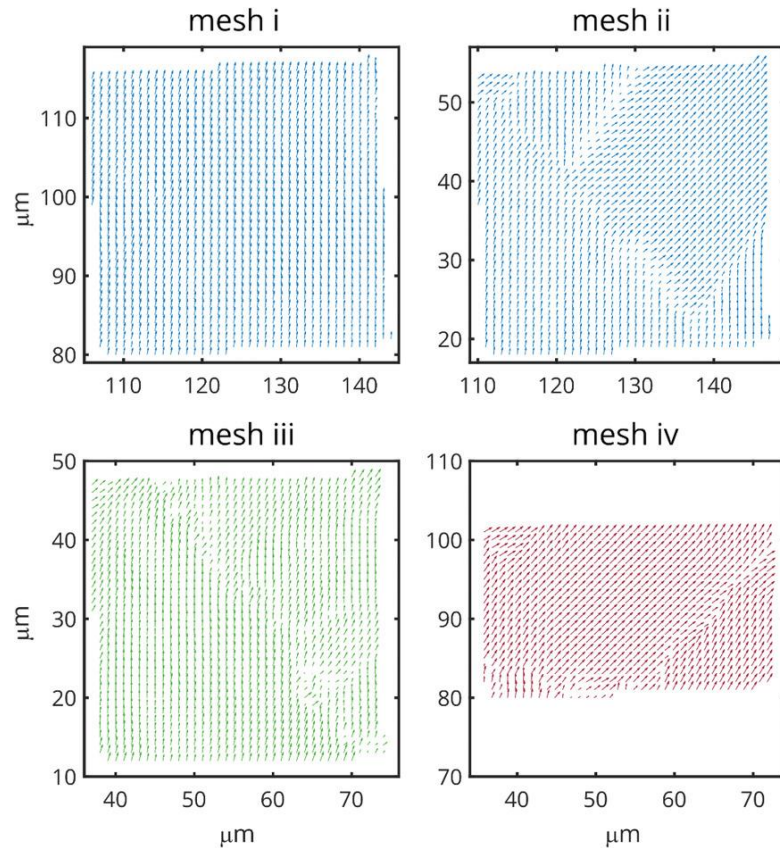


Example 1: Structure of self-assembled films



Example 1: Structure of self-assembled films

- Domain sizes from phase Ω_ℓ
- Exceeding mesh sizes of $40 \mu\text{m} \times 40 \mu\text{m}$



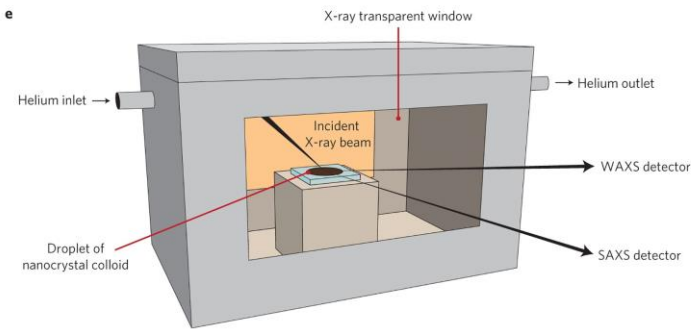
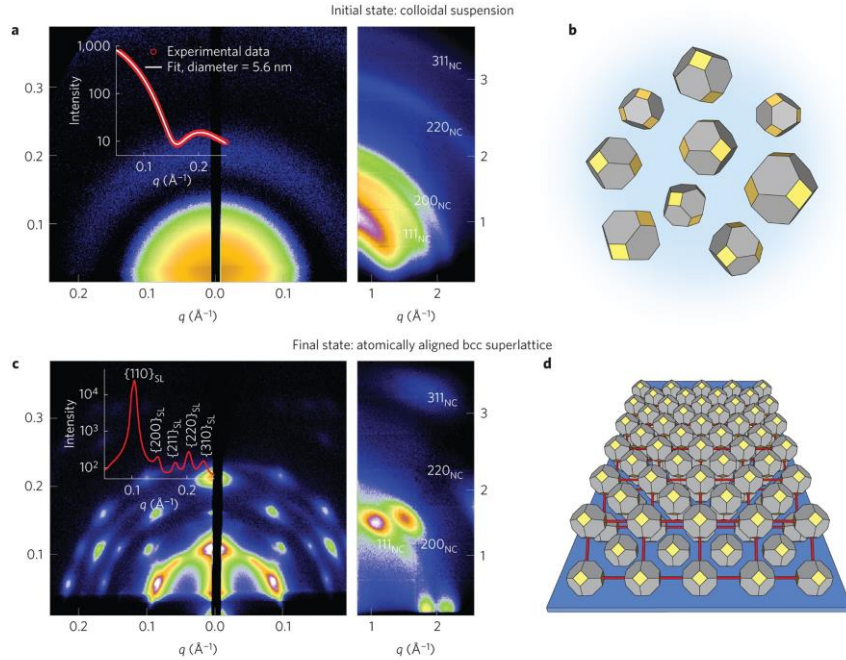
- Degree of six-fold symmetry does not depend on number of layers
- Two-fold symmetry: Friedel's law
- Five-fold: measure of background

Adv. Mater. Inferf. 7, 2000919 (2020)

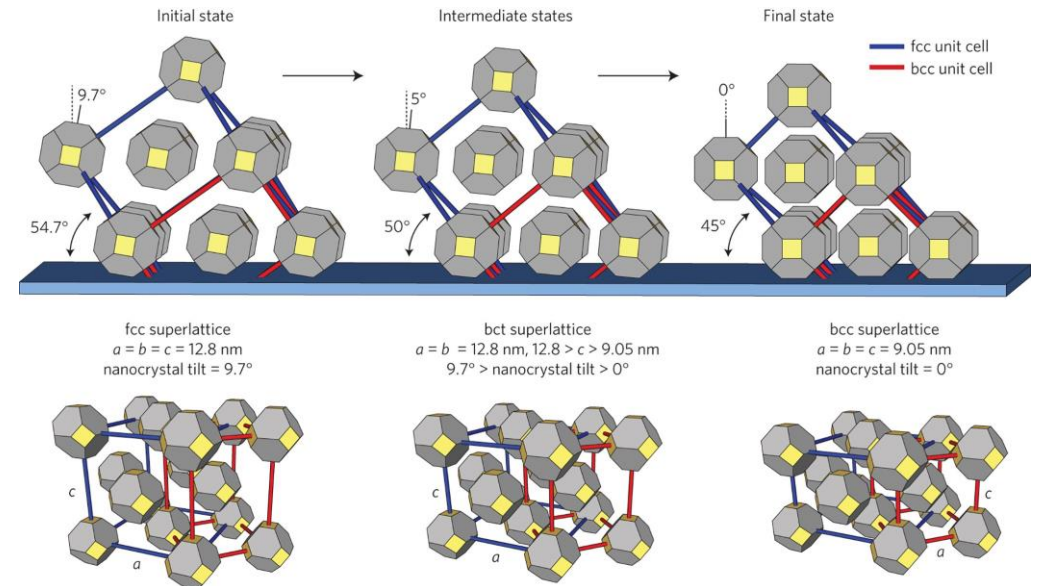
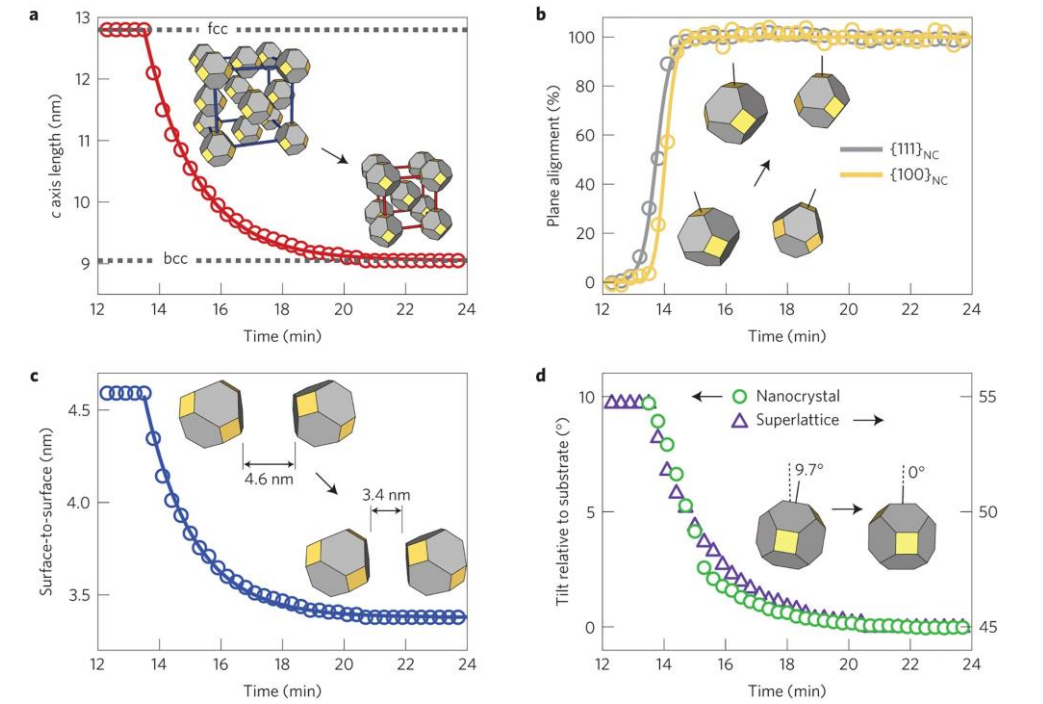
Soft matter 11, 5465 (2015); J. Appl. Cryst. 49, 2046 (2016); IUCrJ 5, 354 (2018); J. Appl. Cryst. 52, 777 (2019)

Example 2: In-situ self-assembly

GISAXS studies

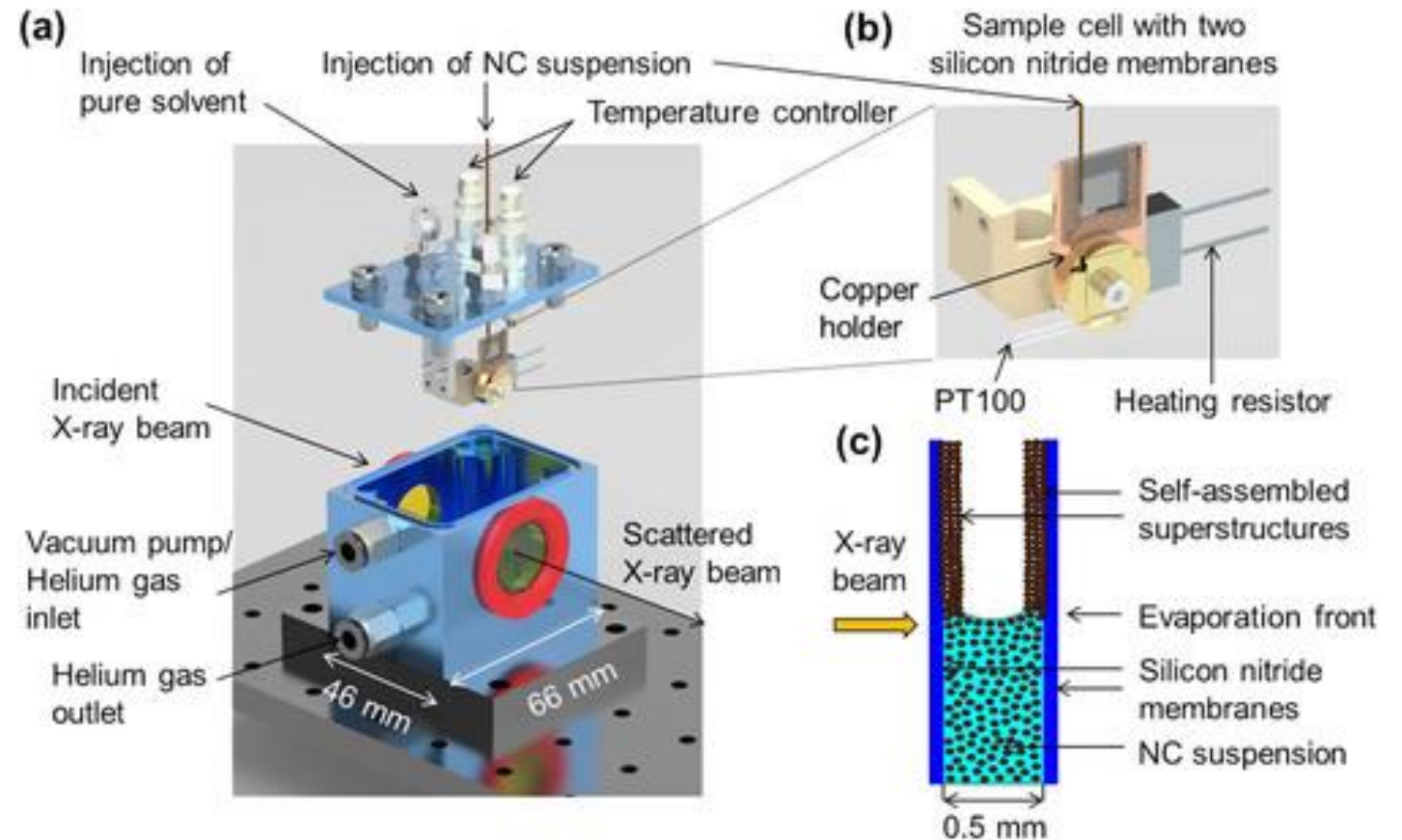


Weidman et al. Nat. Mater. 15, 775 (2016)

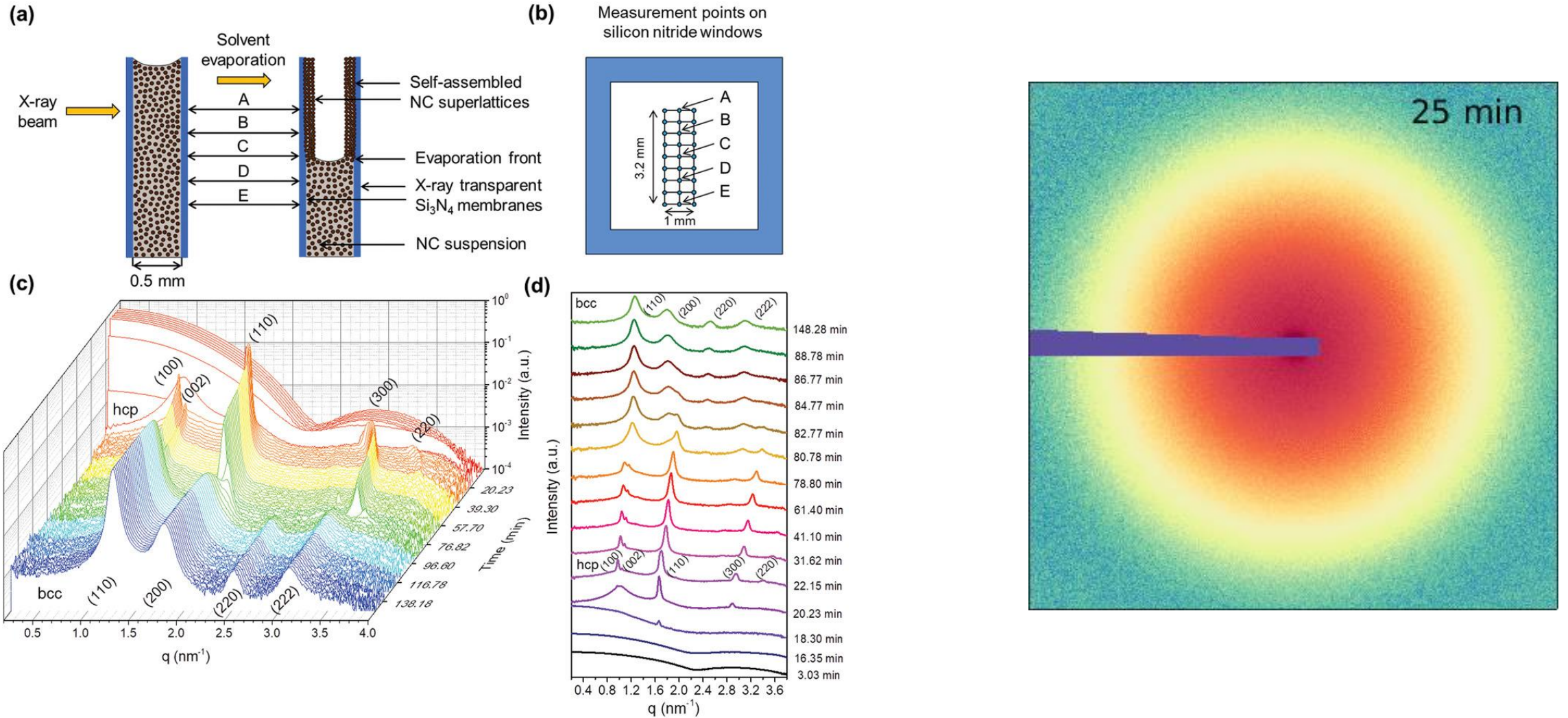


Example 2: In-situ self-assembly

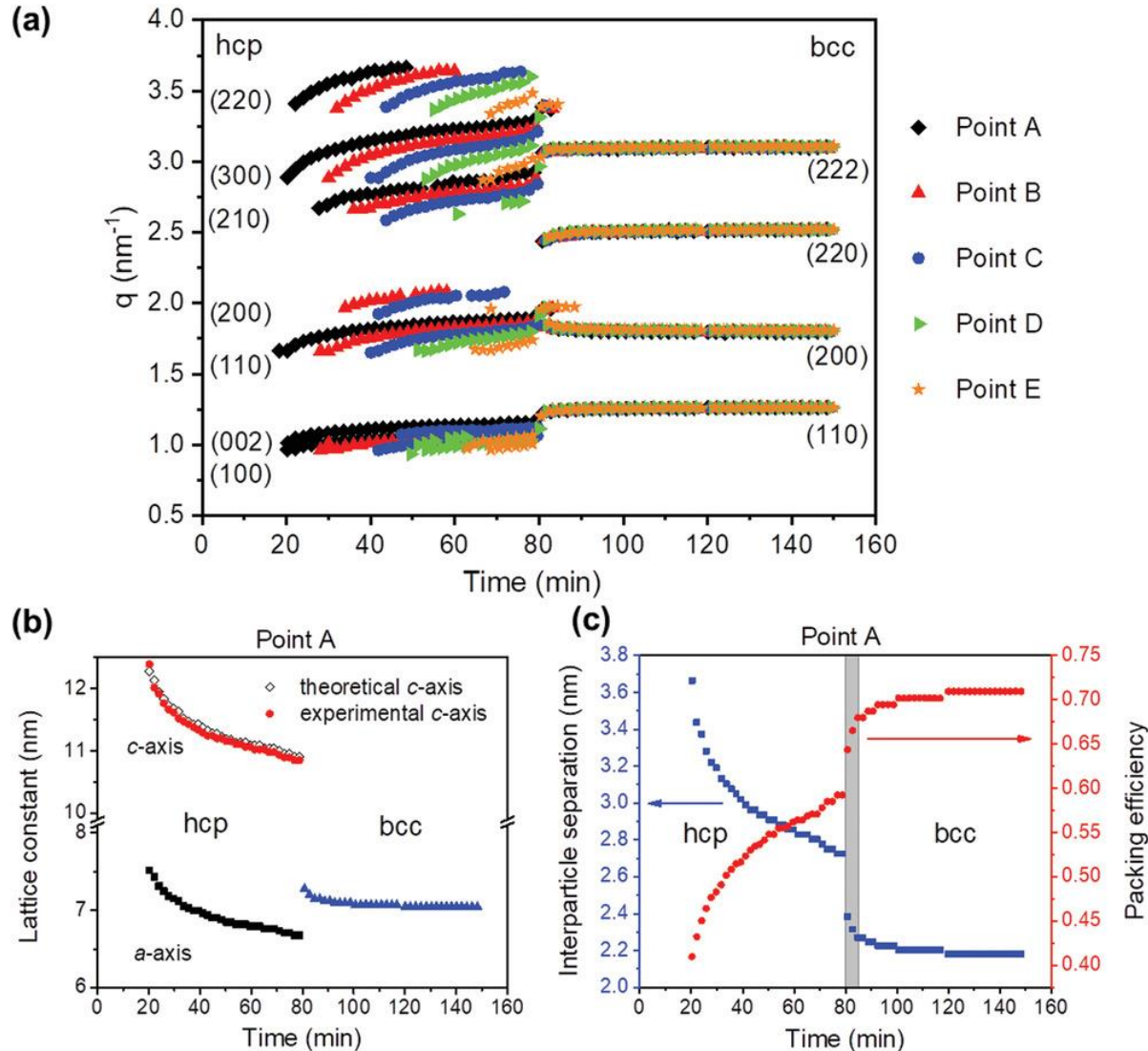
- Obtain information of the structure formation by self-assembly in-situ
- Bulk assembly: Time-resolved SAXS at ID02 (ESRF)
- PbS particles
 - radii between 3 nm to 8 nm
 - Stabilized by oleic acid
 - Dispersed in heptane (hexane, toluene, ...)
- About 25 μl sample volume
- Evaporation rate in the range of 0.25 $\mu\text{l}/\text{min}$ by helium flusing



Example 2: In-situ self-assembly



Example 2: In-situ self-assembly



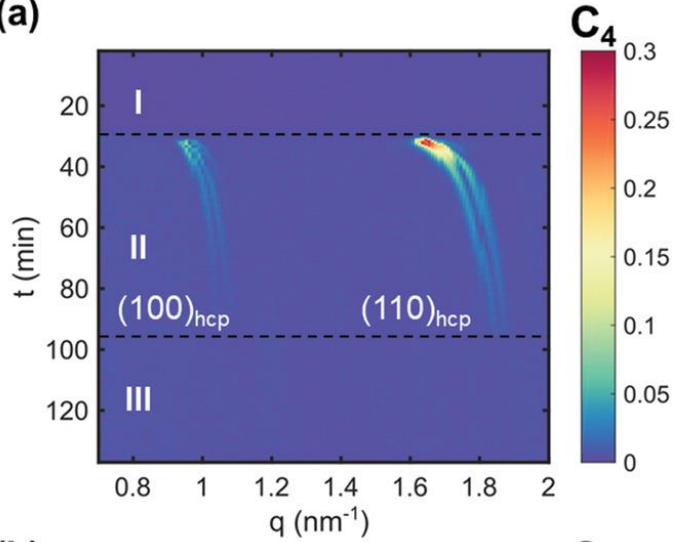
Two-step assembly

- hcp crystal form once the evaporation front passes the exposed spot \rightarrow swollen state
- Densification
- Transition to bcc when solvent has completely evaporated
- High packing efficiency of soft particles

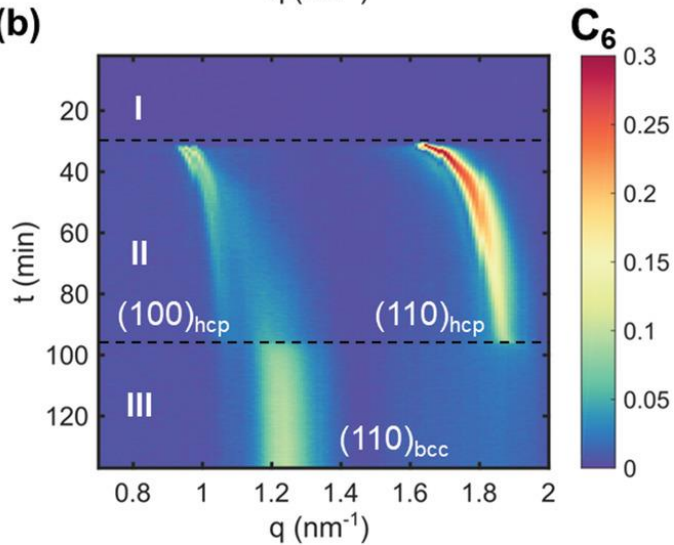
Example 2: In-situ self-assembly

Impact from XCCA

(a)

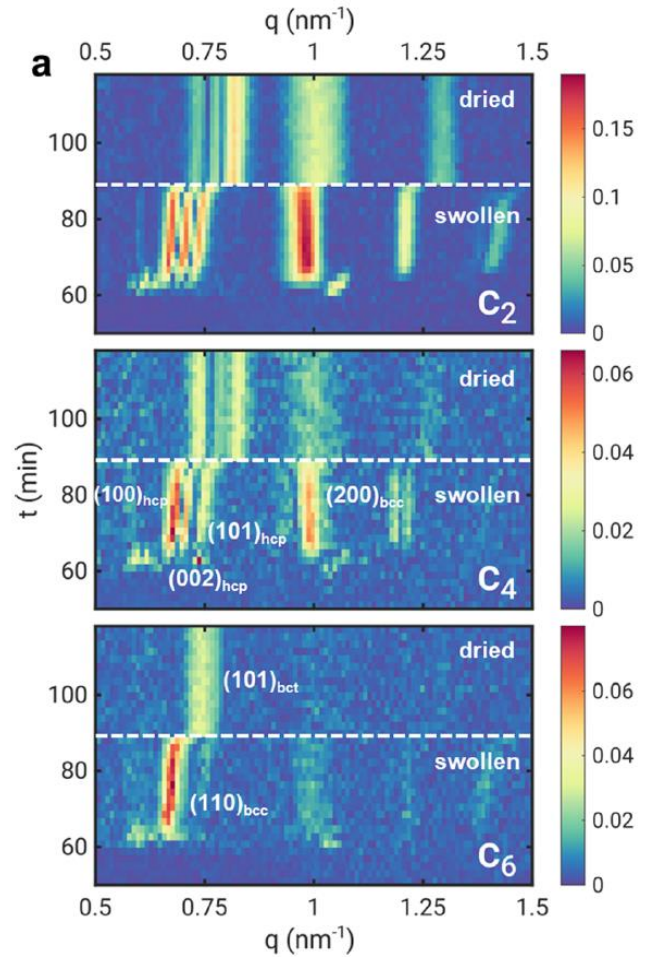
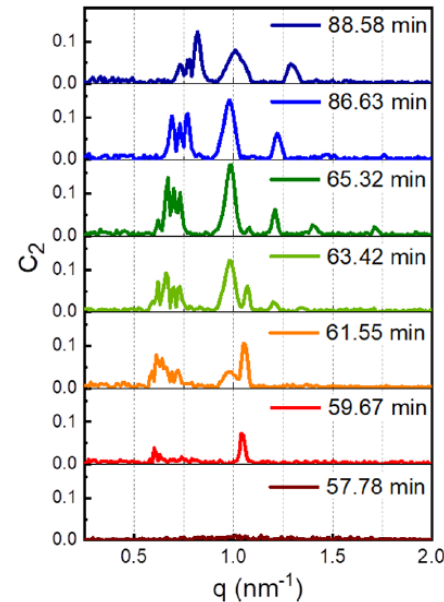
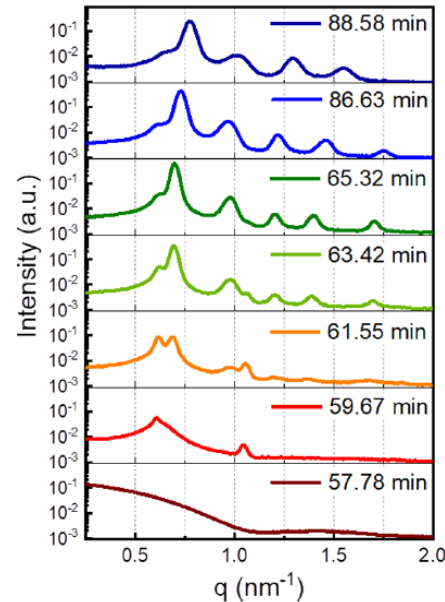


(b)



Symmetry of Bragg peaks

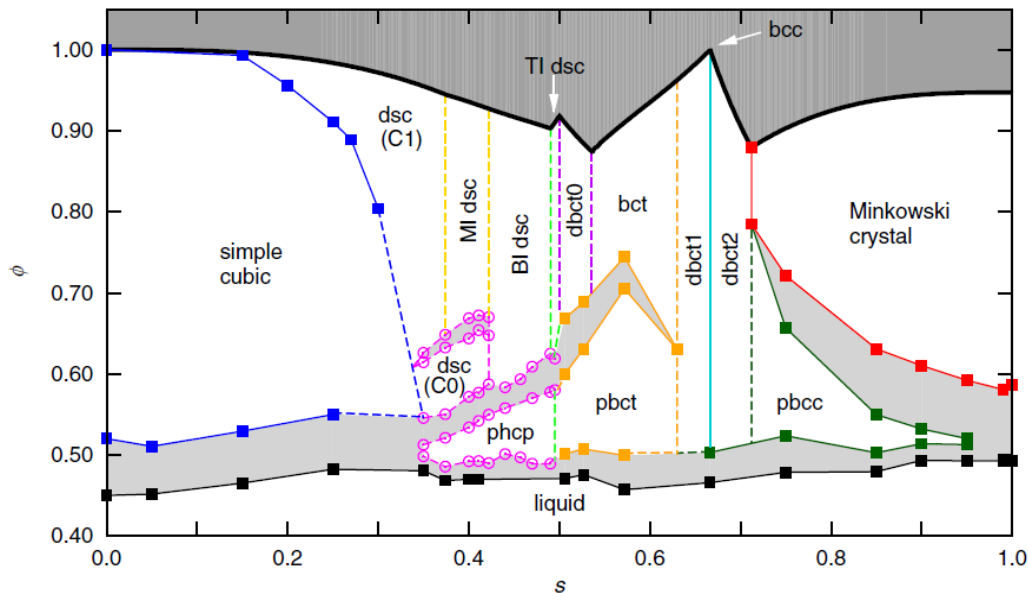
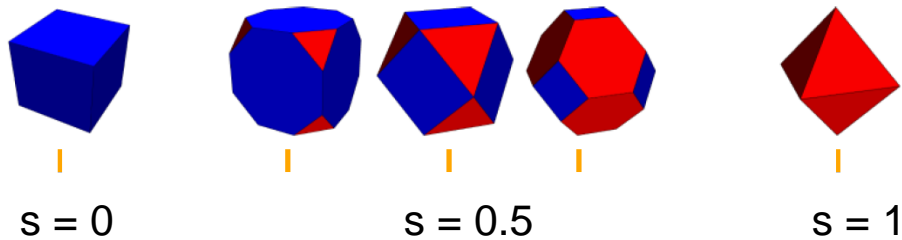
- Detection of „hidden peaks“
- Coexistence of different phases



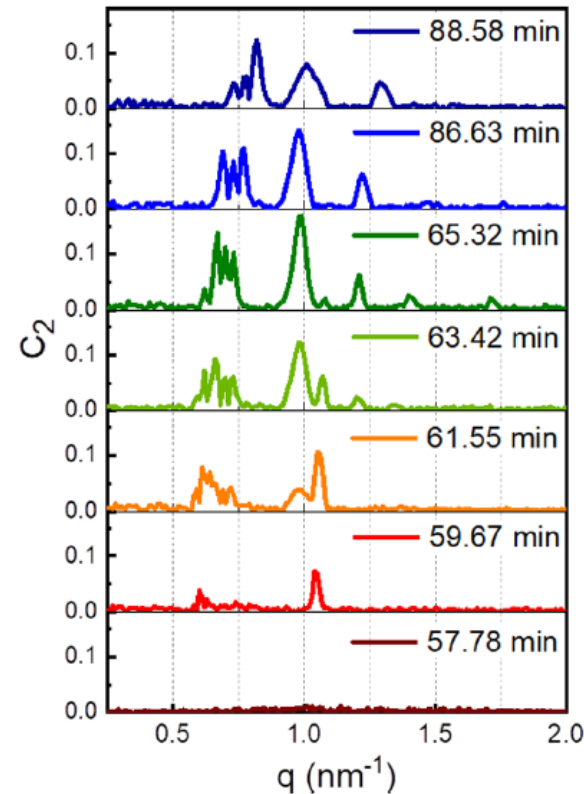
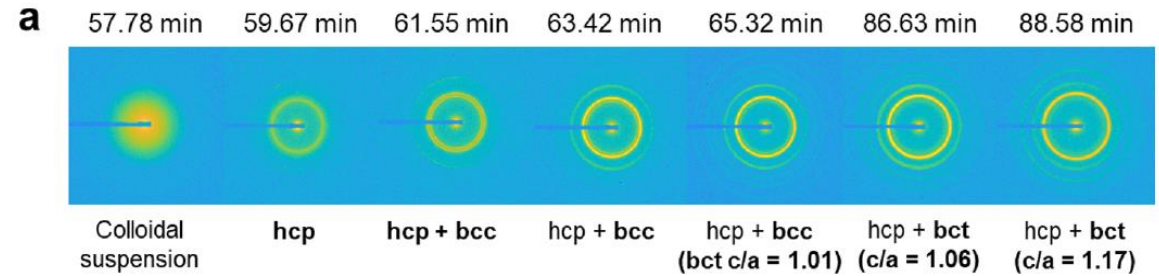
Example 2: In-situ self-assembly

Impact from XCCA

PbS particles as cuboctahedron
(truncated cubes with $s = 0.5$)

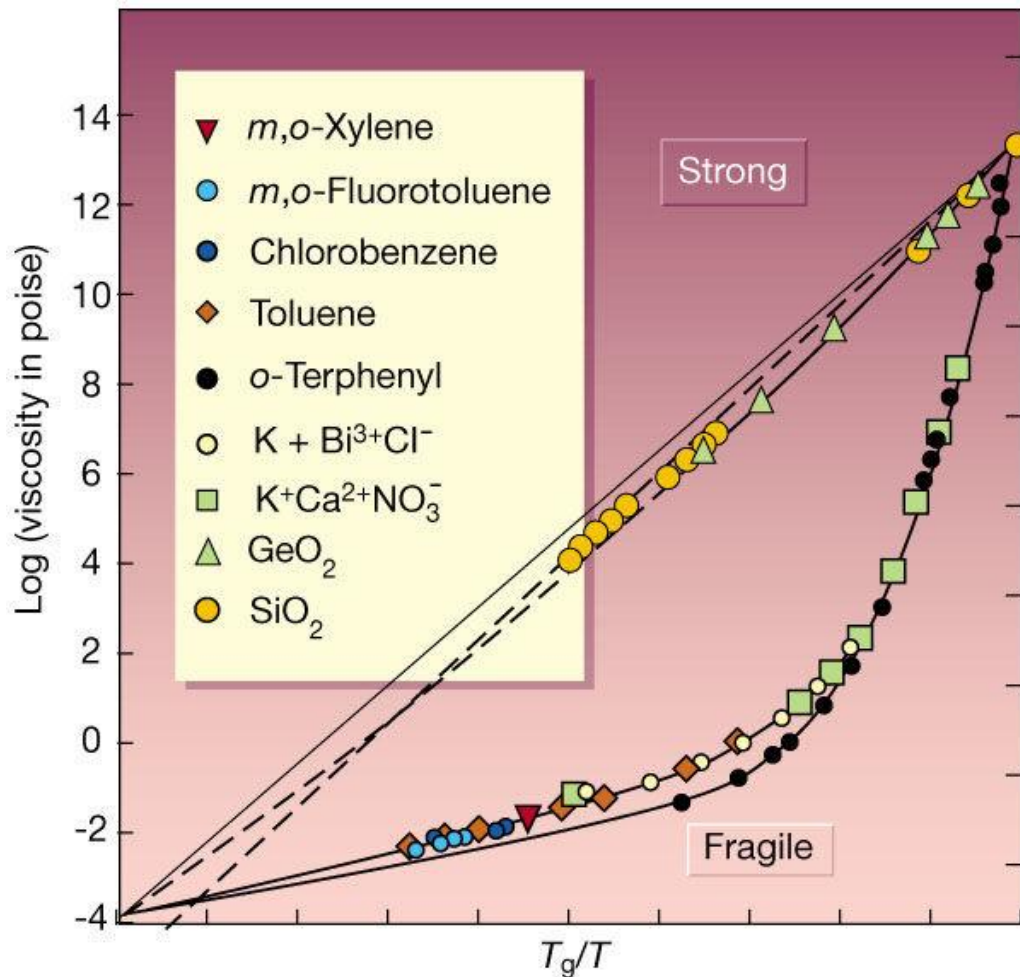


Gantapara et al. PRL 111, 015501 (2013)



→ Coexistence of plastic bct and hcp found in the final state of the assembly

Glass transition

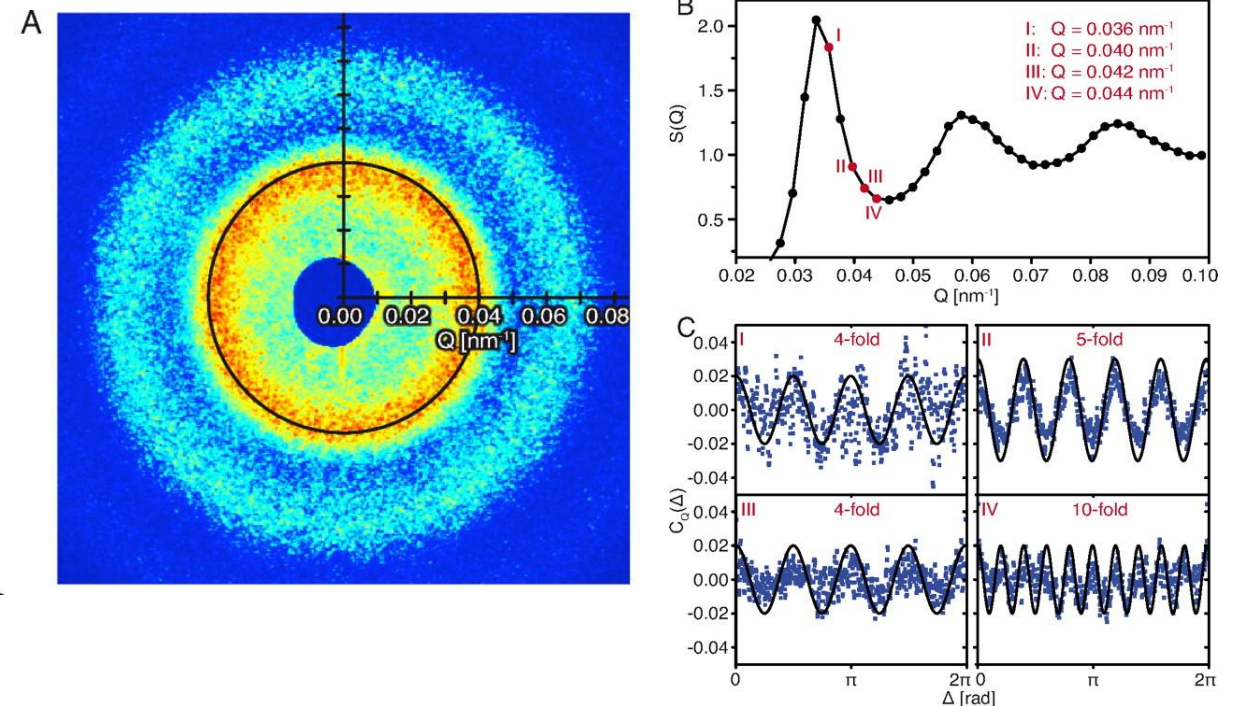


Science 267, 1927 (1995)

Nature 410, 259 (2001)

Approaching the glass transition

- Dynamics slow down by orders of magnitude
- (Average) structure remains unchanged
- Role of local order, e.g. icosahedrons?

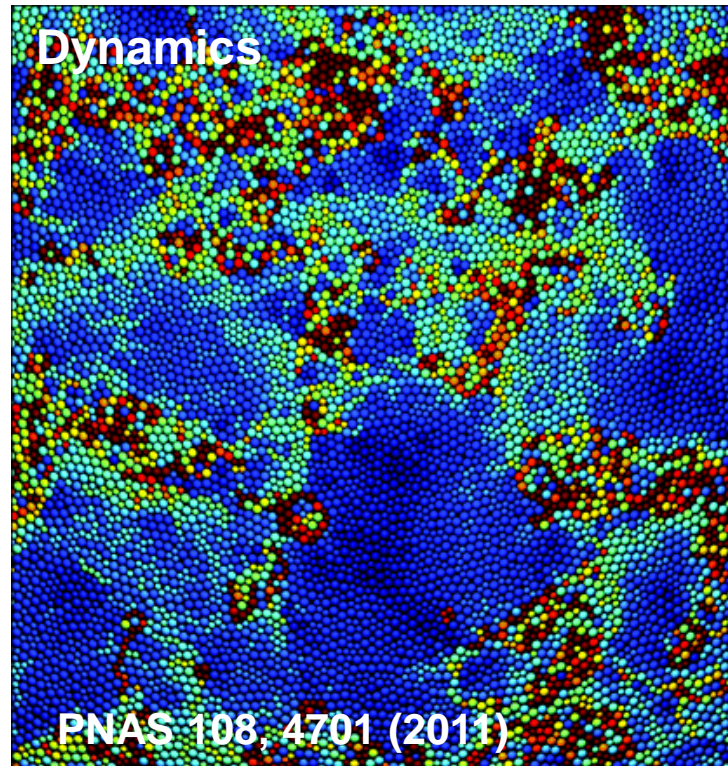
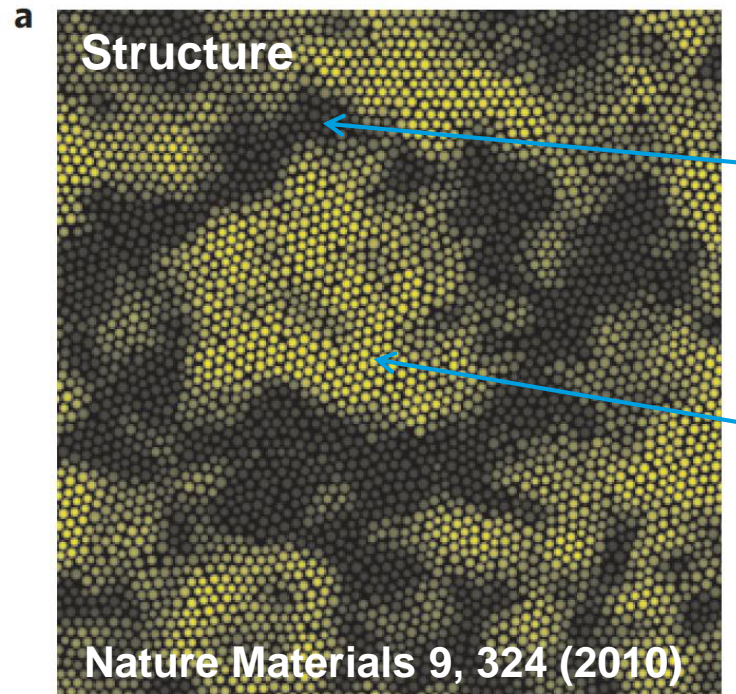


Wochner et al. PNAS 106 11511 (2009)

Glass transition

Spatial and dynamics heterogeneities

Spatial and temporal heterogeneities in the vicinity of the glass transition and crystallisation of soft matter



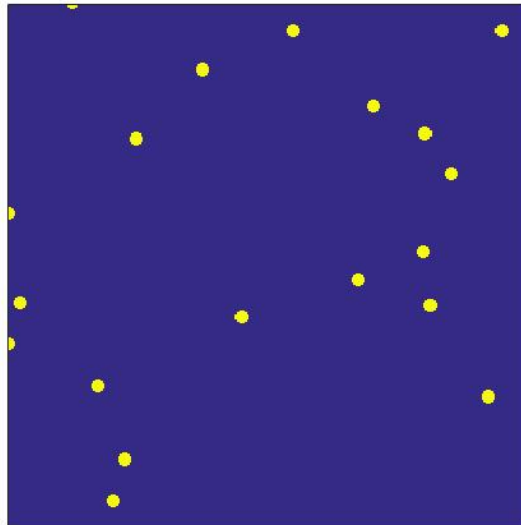
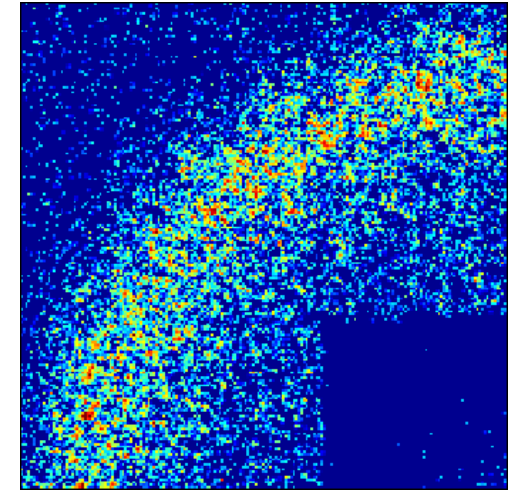
Access higher-order correlations in time (XPCS) and space (XCCA)



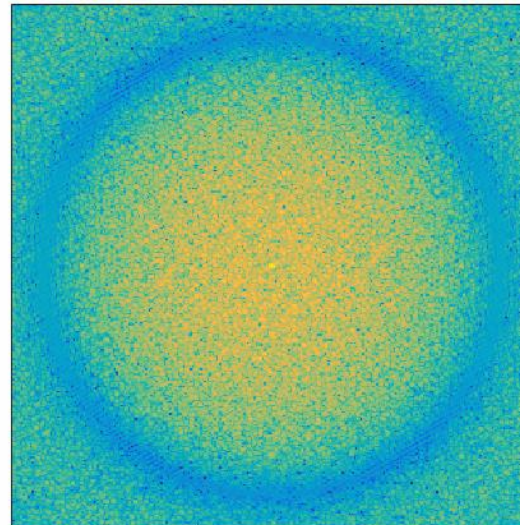
Local bond order parameter

X-ray Photon Correlation Spectroscopy

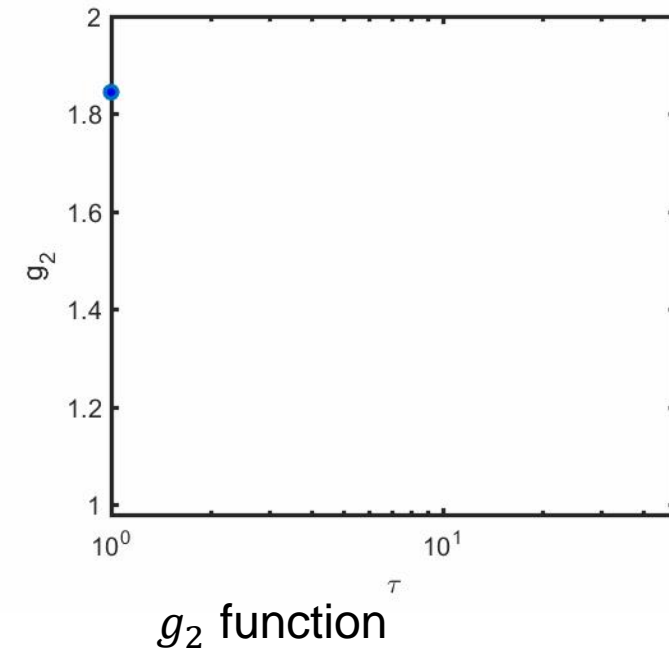
- **Time domain:** changing sample structure → change of speckle pattern
- Access to dynamical properties via $g_2(q, \tau) = \frac{\langle I(q, t)I(q, t+\tau) \rangle_t}{\langle I(q, t) \rangle_t^2} = \beta |f(q, \tau)|^2$
- Intermediate scattering function $f(q, \tau) = S(q, \tau)/S(q, 0)$



Diffusing particles



Speckle pattern



Example 3: Structure – dynamics correlations in hard spheres

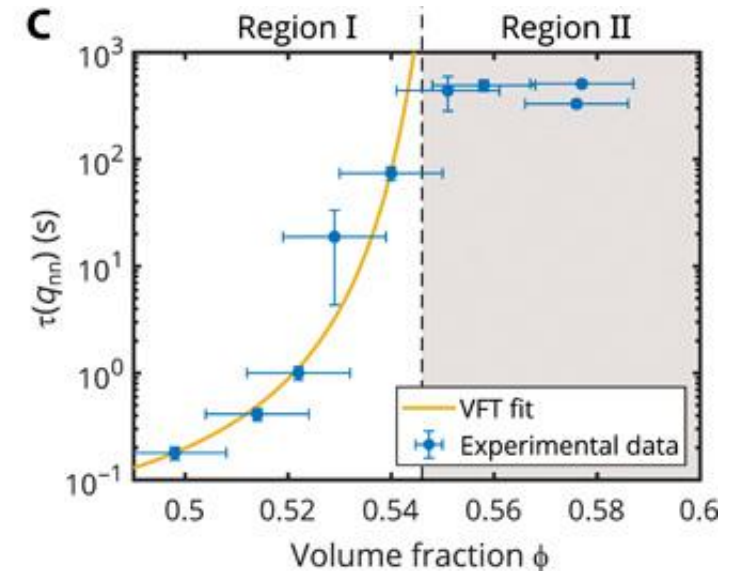
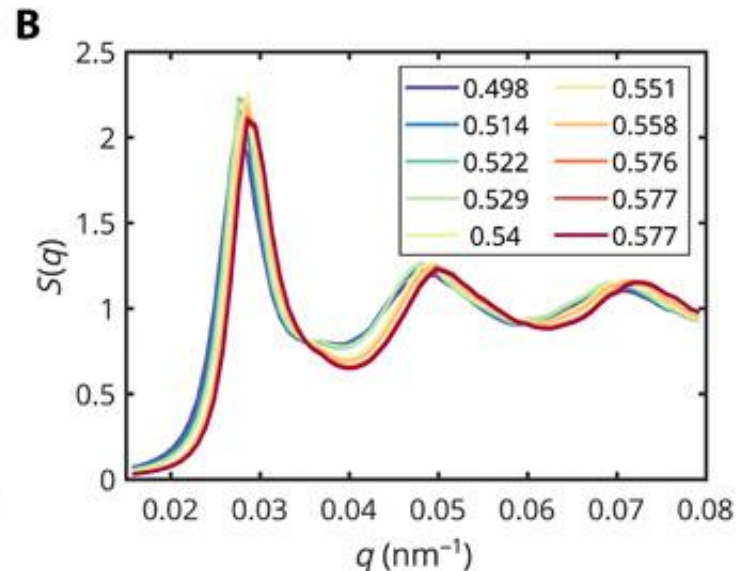
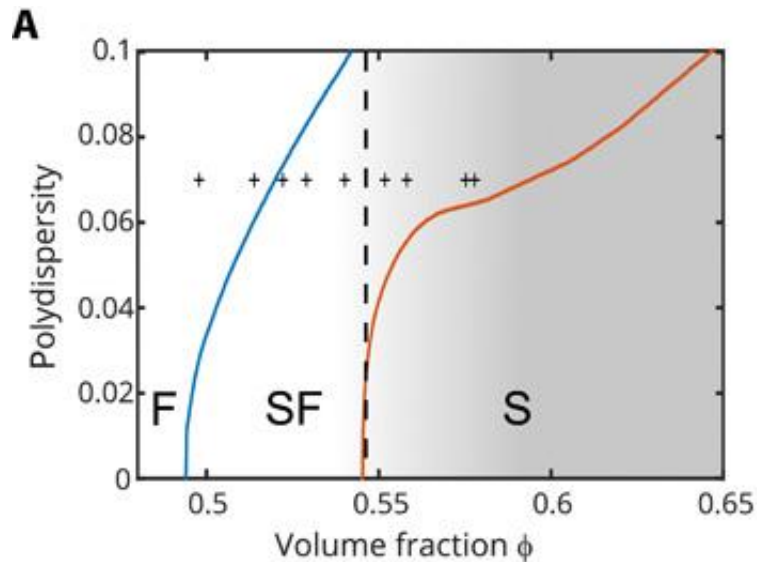
XPCS and XCCA

Hard spheres

- Phase defined by volume fraction
- Fluid, crystal, glass phases (and coexistence regions)
- ID10 experiment on structure and dynamics

Fluid-glass transition

- Structure factor $S(q)$ remains almost unchanged
- Dynamics slows down by orders of magnitude
- Impact from orientational local order \rightarrow XCCA

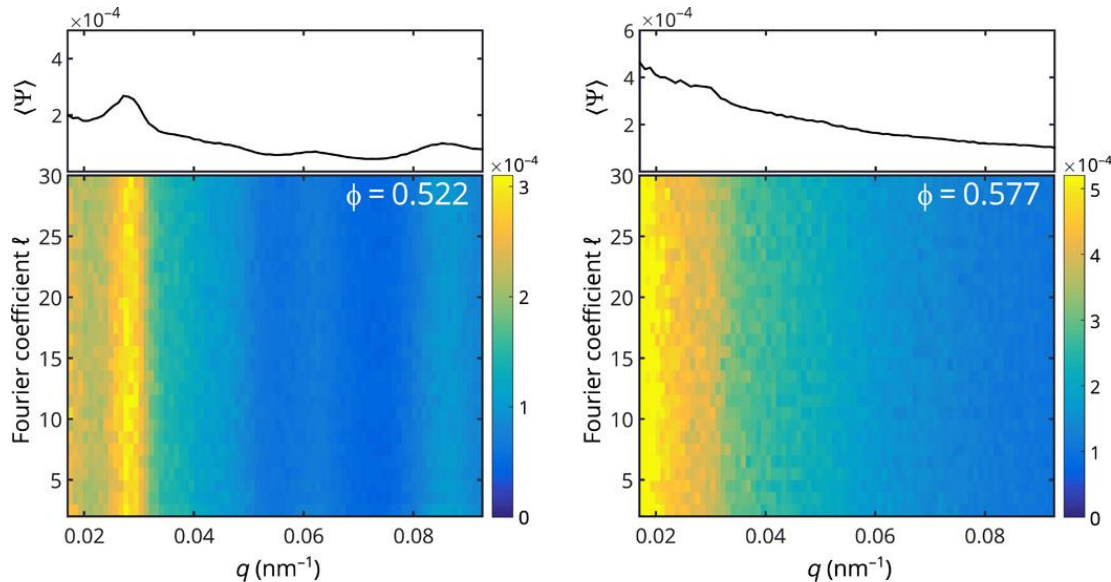


Example 3: Structure – dynamics correlations in hard spheres

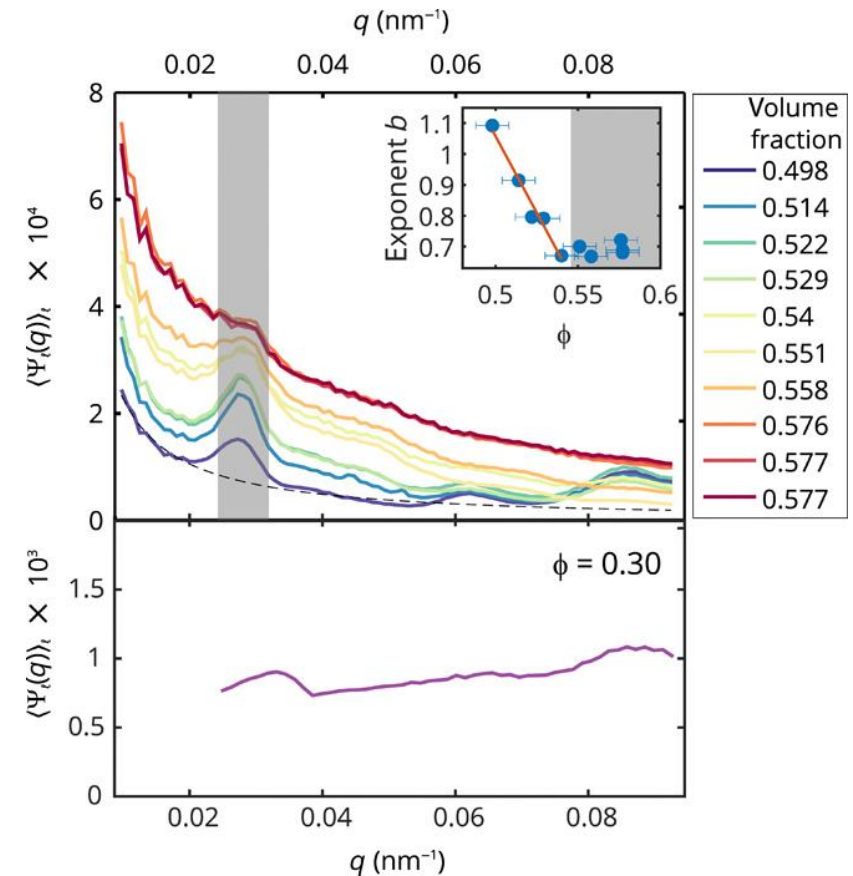
XPCS and XCCA

Map of Fourier coefficients

- Strict q -dependence
- Weak dependence on Fourier coefficient \rightarrow Use average over all Fourier coefficients



- „Order parameter“ from XCCA analysis
- Combine synchrotron and FEL data

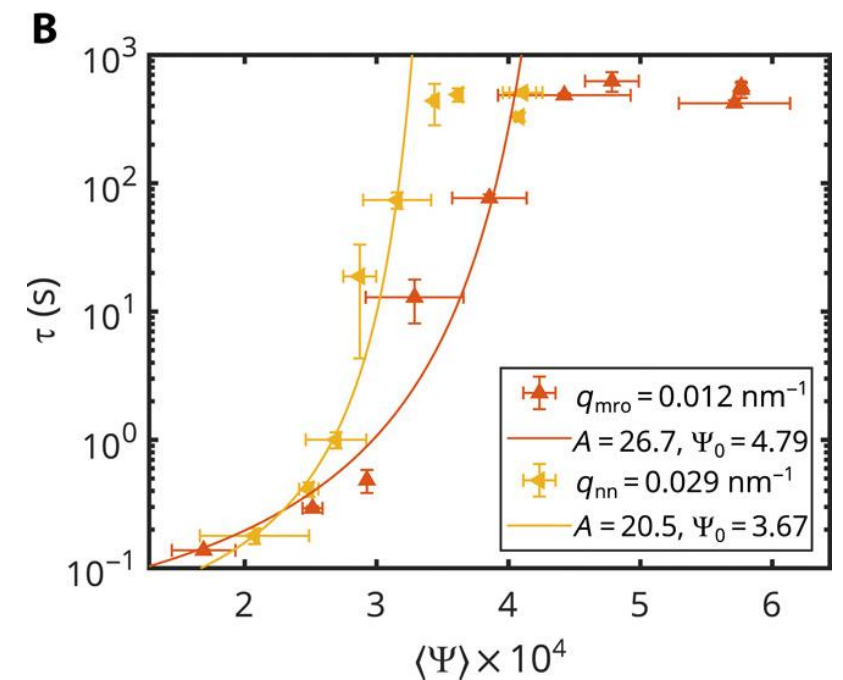
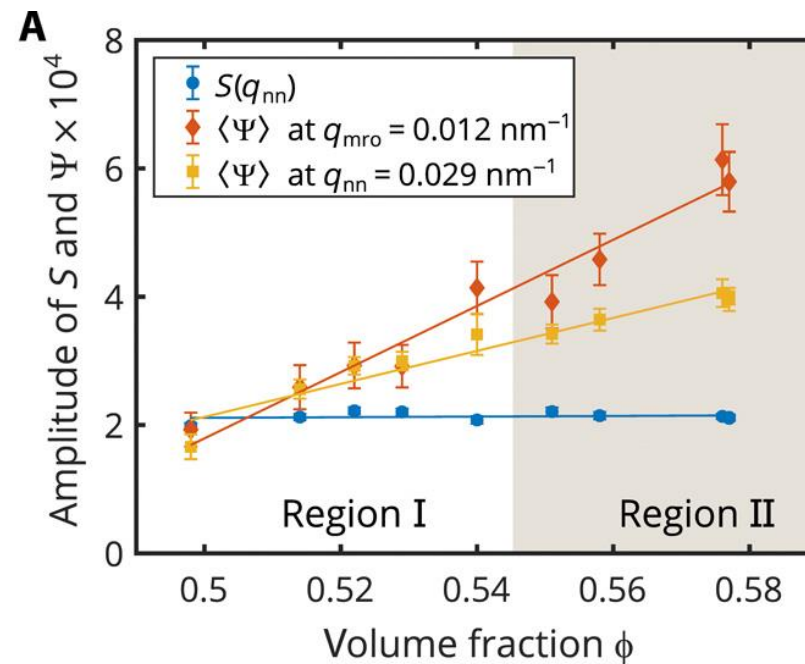


Example 3: Structure – dynamics correlations in hard spheres

XPCS and XCCA

Results

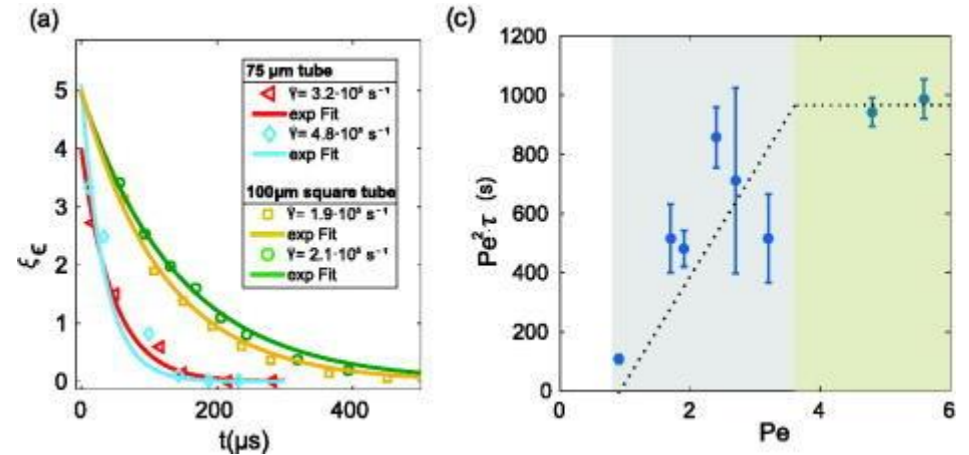
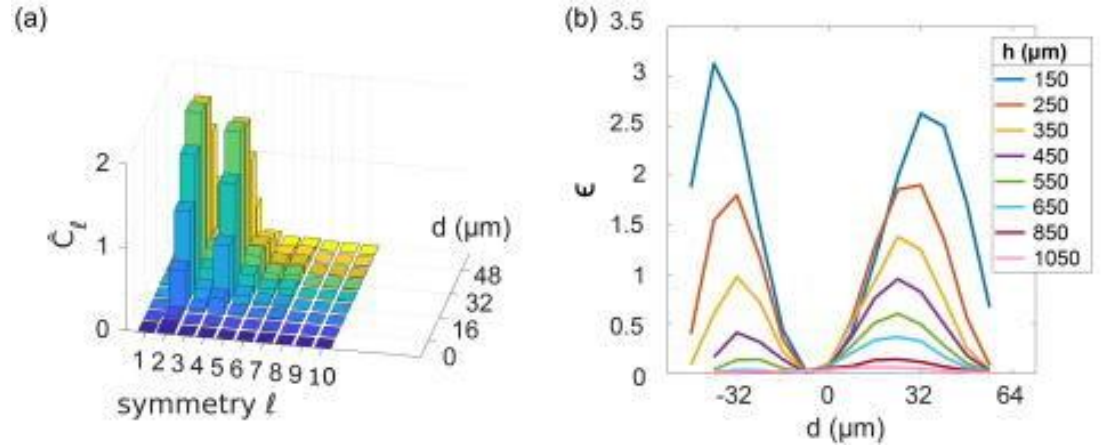
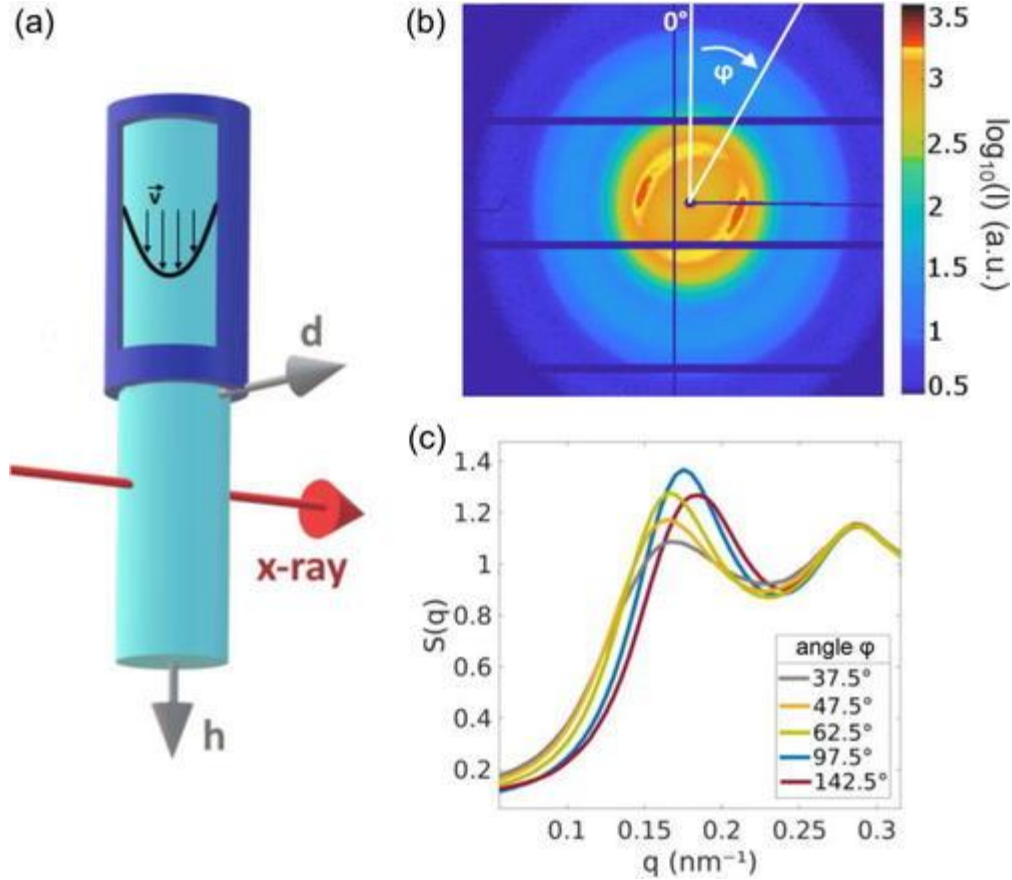
- Broad range of volume fractions: FEL and storage ring studies
- Growth of medium range order
- Ordered precursor at next-neighbour distance
- Correlation of structure and dynamics
- Growth of order inside glass phase



FL et al. *Sci. Adv.* 6, eabc5916 (2020)

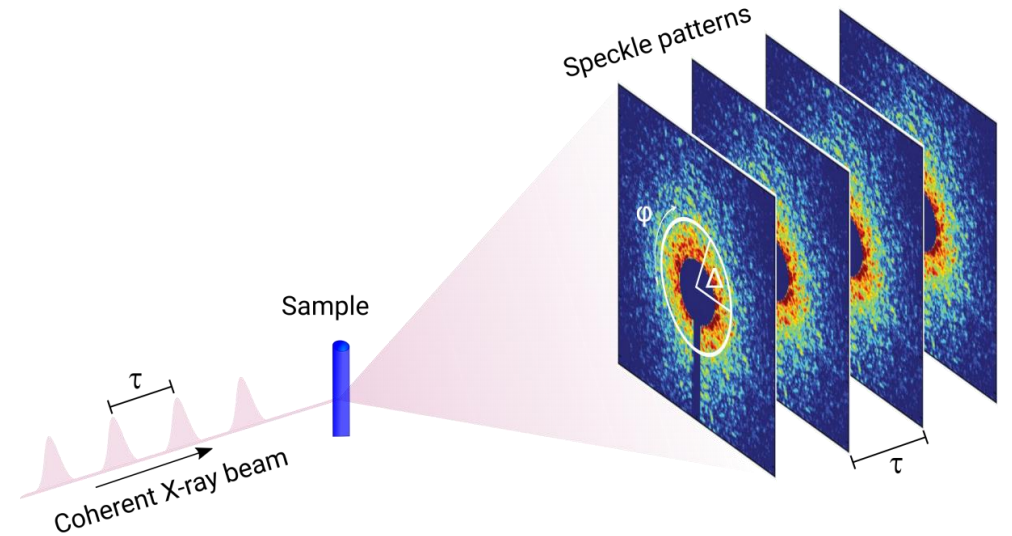
Example 4: Liquid jets

Quantifying non-isotropic structures



Wrap-up

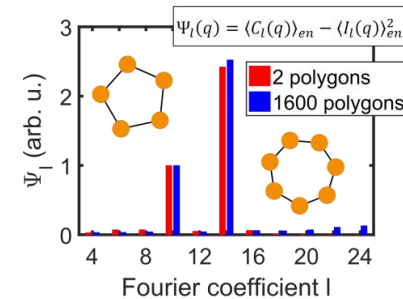
- Self-assembly of nanoparticles for functional devices
 - Ex-situ characterisation: domain structure, size, orientations
 - In-situ real time assemblies: „hidden“ structures and phase coexistence
- Glass transition in colloidal systems: structure-dynamics correlations
- Characterize non-isotropic structure in liquid jets
- What's next → New facilities?



XCCA

Cross-correlation function

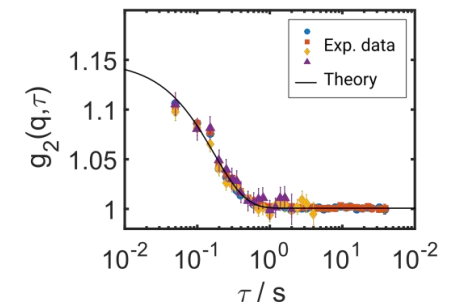
$$C(q, \Delta) = \frac{\langle I(q, \varphi) I(q, \varphi + \Delta) \rangle_{\varphi} - \langle I(q, \varphi) \rangle_{\varphi}^2}{\langle I(q, \varphi) \rangle_{\varphi}^2}$$



XPCS

Intensity-intensity time autocorrelation function

$$g_2(q, \tau) = \frac{\langle I(q, t) I(q, t + \tau) \rangle_t}{\langle I(q, t) \rangle_t^2}$$



Example: XPCS – time scales

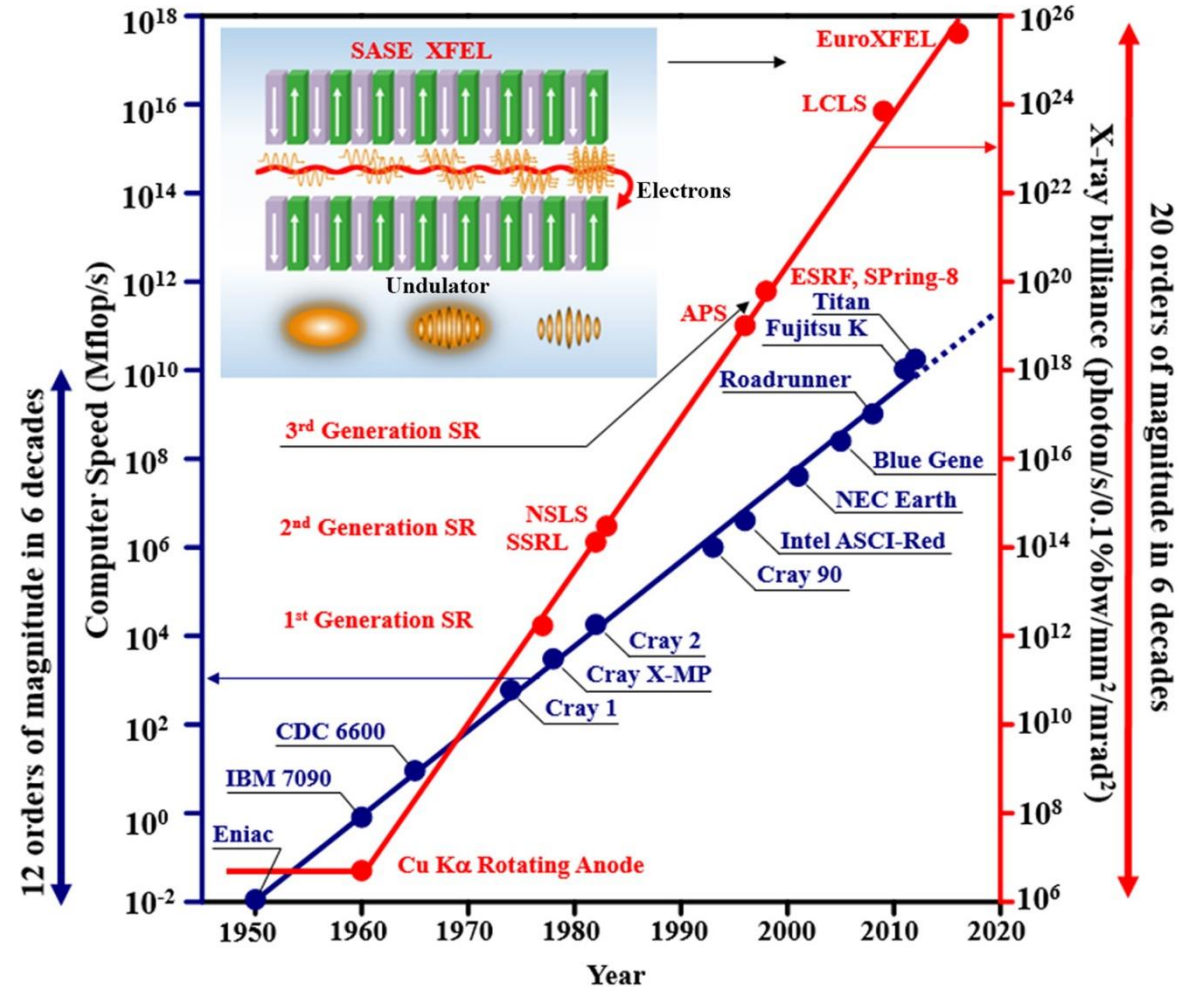
Role of brilliance B

XPCS signal-to-noise ratio

- $R_{SN} \propto I_{coh} \sqrt{\tau_c}$
- Coherent flux $I_{coh} \propto B$,
- Shortest correlation time τ_c
- Consequently, $\tau_c \propto 1/I_{coh}^2$
- XPCS performance scales $\sim B^2$
- **Many new possibilities at new facilities!**

Coherent flux (per s) compared to PETRA III

- PETRA IV: $\geq 100 \times$
- European XFEL: $10^5 \times$



http://www.physics.ucla.edu/research/imaging/research_CDI.html

XPCS – time scales at storage rings

VOLUME 74, NUMBER 11 PHYSICAL REVIEW LETTERS 13 MARCH 1995

X-Ray Intensity Fluctuation Spectroscopy Observations of Critical Dynamics in Fe₃Al

S. Brauer* and G. B. Stephenson

IBM Research Division, T. J. Watson Research Center, P.O. Box 218, Yorktown Heights, New York 10598

M. Sutton, R. Brüning, and E. Dufresne

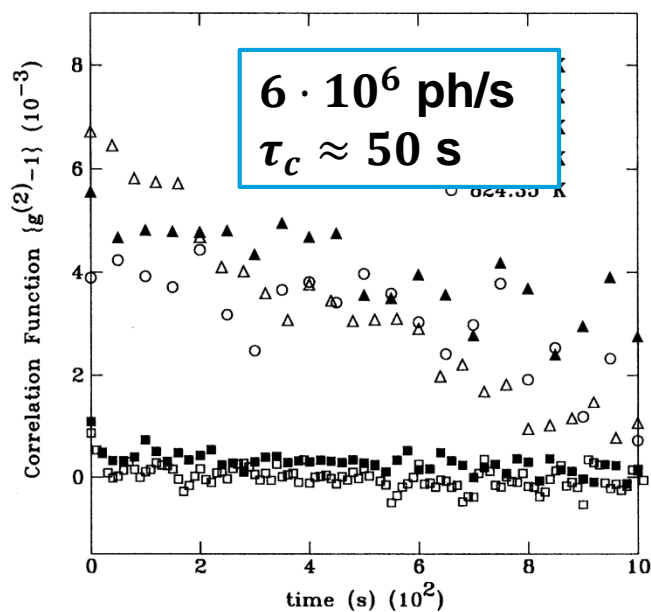
Center for the Physics of Materials and Department of Physics, McGill University, Montréal, Québec, Canada, H3A 2T8

S. G. J. Mochrie

Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

G. Grübel, J. Als-Nielsen,[†] and D. L. Abernathy

European Synchrotron Radiation Facility, B.P. 220, F-38043 Grenoble Cedex, France
(Received 31 October 1994)

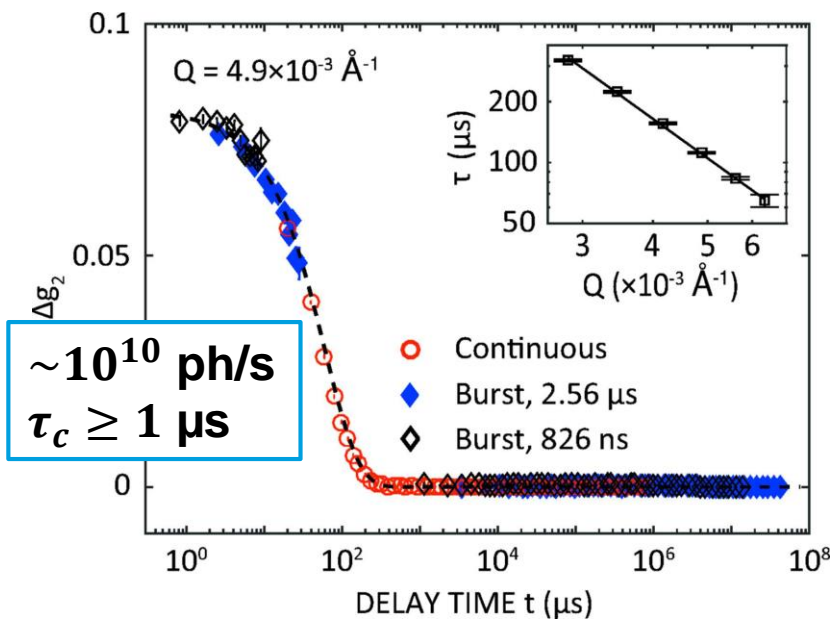


PRL 74, 2010 (1995)

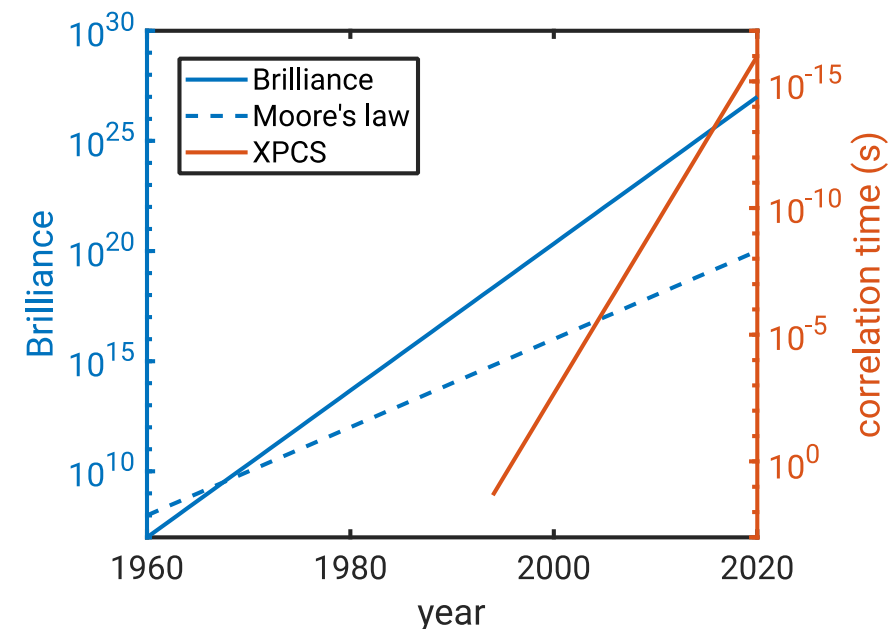
Sub-microsecond-resolved multi-speckle X-ray photon correlation spectroscopy with a pixel array detector

Qingteng Zhang,^a Eric M. Dufresne,^a Suresh Narayanan,^a Piotr Maj,^b Anna Koziol,^b Robert Szczygiel,^b Pawel Grybos,^b Mark Sutton^c and Alec R. Sandy^{a*}

^aX-ray Science Division, Argonne National Laboratory, 9700 South Cass Avenue, Lemont, IL 60439, USA, ^bAGH University of Science and Technology, al. Mickiewicza 30, Krakow 30-059, Poland, and ^cDepartment of Physics, McGill University, 3600 Rue University, Montréal, QC, Canada H3A 2T8. *Correspondence e-mail: asandy@anl.gov



JSR 25, 1408 (2018)

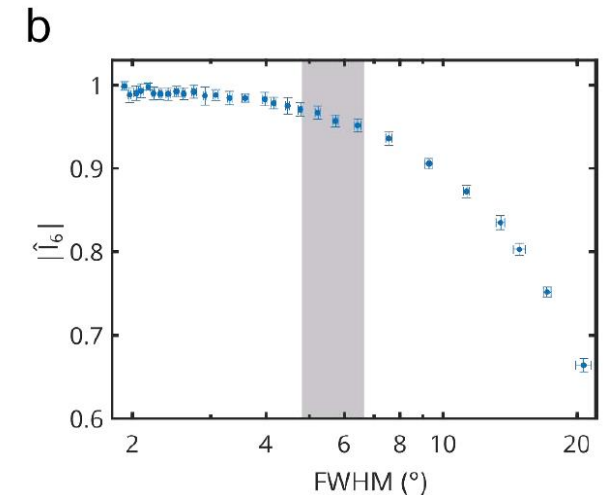
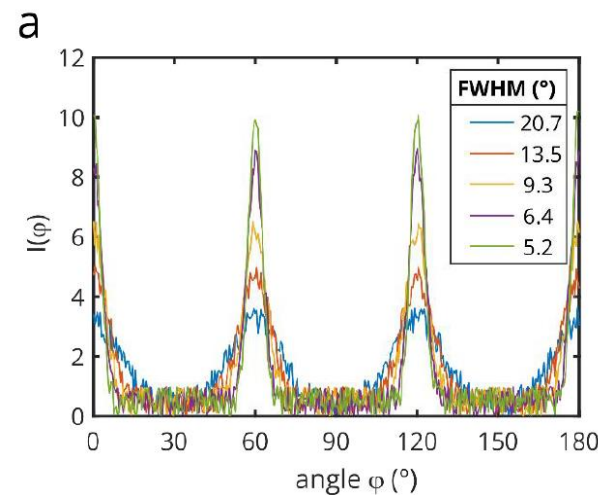
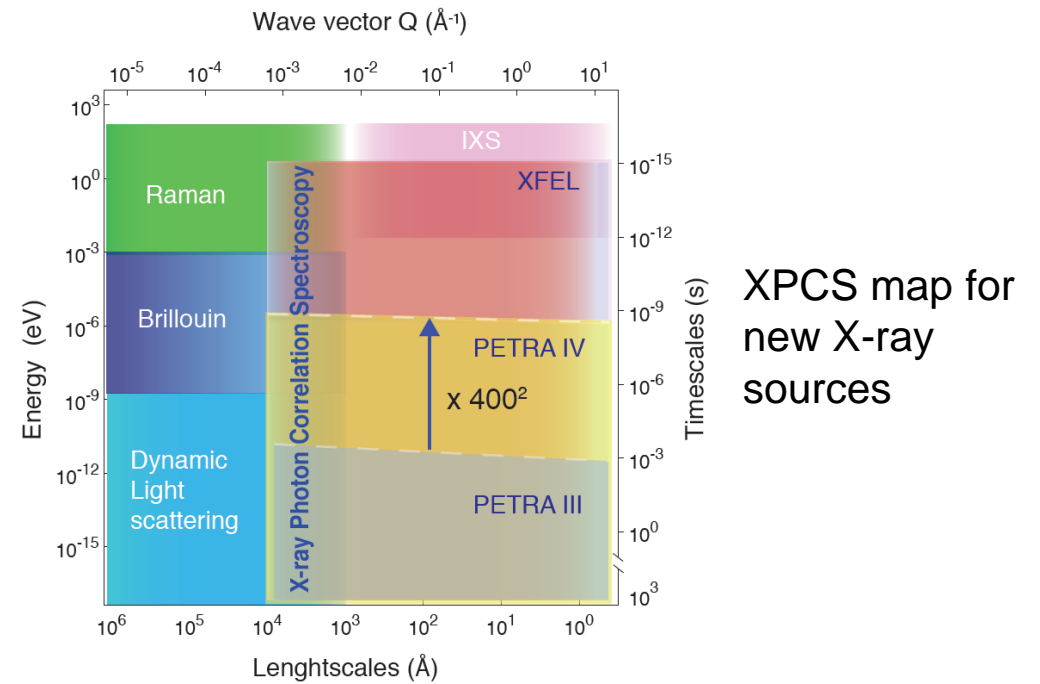


- XPCS: $\text{SNR} \propto I_0 \sqrt{\tau_c}$
- DLSR: 10^4 gain in $\tau_c \Rightarrow \tau_c \approx \text{ns}$
- European XFEL (avg. Brilliance): 10^{10} gain in $\tau_c \Rightarrow \tau_c \approx \text{fs}$
- Limitations by pulse length and repetition rate

XCCA – outlook

Possibilities at new light sources: towards molecular time and length scales

- Beyond „single shot“ experiments for static structures: FXS / XCCA probed in real-time
- Time limitations → SNR
- Intensity needs → correlation of events within the same pattern → radiation damage
- Detector limitations for studying molecular length scales → (partial) coherent illumination
- Quantitative results: Influences from experimental setup and geometry (e.g. speckle size, Bragg peak widths ...) → amplitudes and appearance of Fourier coefficients



Adv. Mater. Inferf. 7, 2000919 (2020)

Acknowledgements



Coherent X-ray scattering group (FS-CXS) at DESY

- *M. Schroer, D. Sheyfer, A. Jain, F. Dallari, I. Lokteva, L. Frenzel, M. Walther, M. Dartsch, V. Markmann, N. Striker, W. Roseker, and G. Grübel*

Hamburg University

- F. Schulz, H. Lange, B. Hankiewicz et al.

Siegen University

- C. Gutt

P10 at PETRA III

- M. Sprung, F. Westermeier et al.

ID10 at ESRF

- B. Ruta, Y. Chushkin, F. Zontone et al.

ID02 at ESRF

- A. Mariani, T. Narayanan et al.

SACLA / RIKEN

- K. Tono, T. Katayama, M. Yabashi, T. Ishikawa

Contact

DESY. Deutsches
Elektronen-Synchrotron

www.desy.de

Felix Lehmkuhler
Coherent X-ray Scattering (FS-CXS)
felix.lehmkuehler@desy.de
+49-40-8998-5671
desy.de/cxs