

# Precise description of heavy quark decays

Loops and Legs

Eisenach, April 2006

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# Outline

Introduction: semileptonic and hadronic decay modes of the b quark;

Theoretical prediction of the SL branching fraction and its conflict with experiment;

New perturbative corrections

Outlook: need to account for the charm mass

# 50<sup>th</sup> anniversary of radiative corrections (to charged particle decays)

1956: Behrends, Finkelstein, Sirlin,  
'Radiative corrections to decay processes'

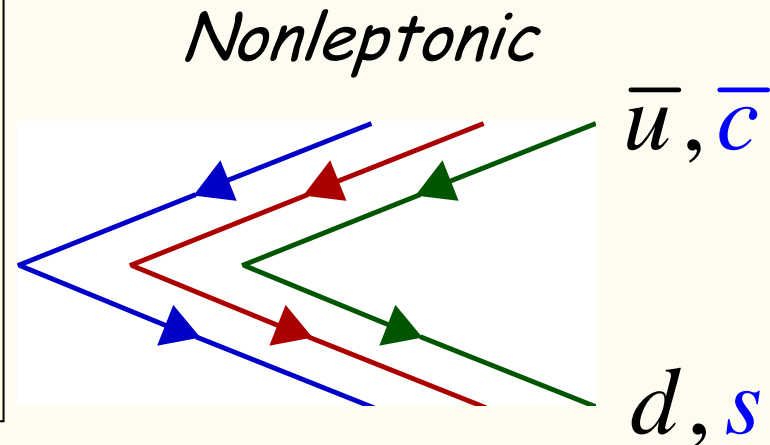
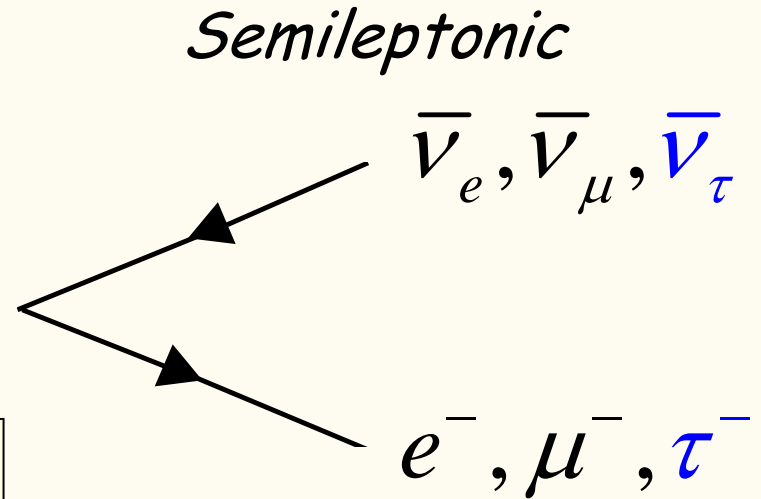
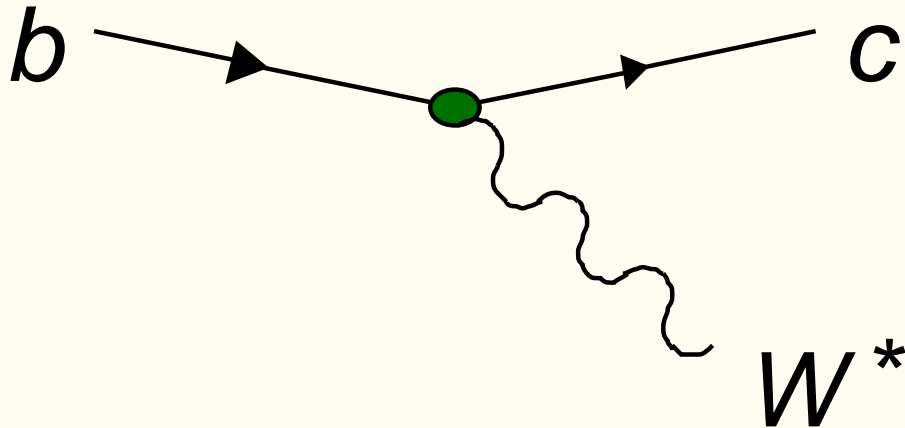
Muon decay: electron spectrum, total rate

1996: first result at two loops (zero recoil)

1999: complete muon lifetime (van Ritbergen, Stuart);  $b \rightarrow u$  ( $vR$ )

2005: complete muon spectrum (Anastasiou, Melnikov, Petriello)

# How does $b$ quark decay?



Semileptonic branching ratio  
(parton model without QCD)

$$B_{SL} \approx \frac{1}{3+6} \approx 11\%$$

$$\Delta B_{SL} = \frac{1}{3+6} - \frac{1}{3+6(1+\delta)} \approx \frac{6\delta}{81} = \frac{\delta}{13.5}$$

8% shift of the NL width shifts  $B_{SL}$  by 0.6 percentage points

# What do experiments get for $B_{SL}$ ?

World average:  $(10.76 \pm 0.23)\%$

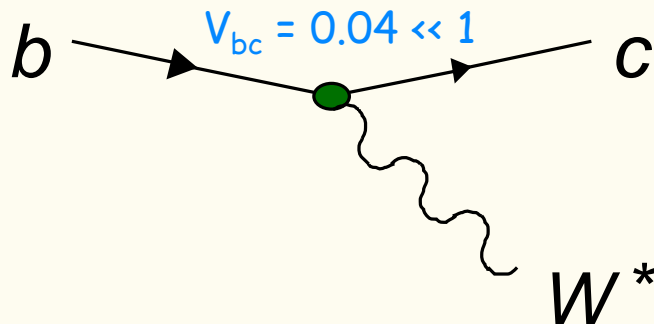
hep-ex/0505100  
(without  $b \rightarrow u$ )

Theoretical lower limit:

$$B_{SL}(b \rightarrow ce\bar{\nu}_e) > 11.5\%$$

*Bigi et al, 1994*  
*Voloshin, 2000*

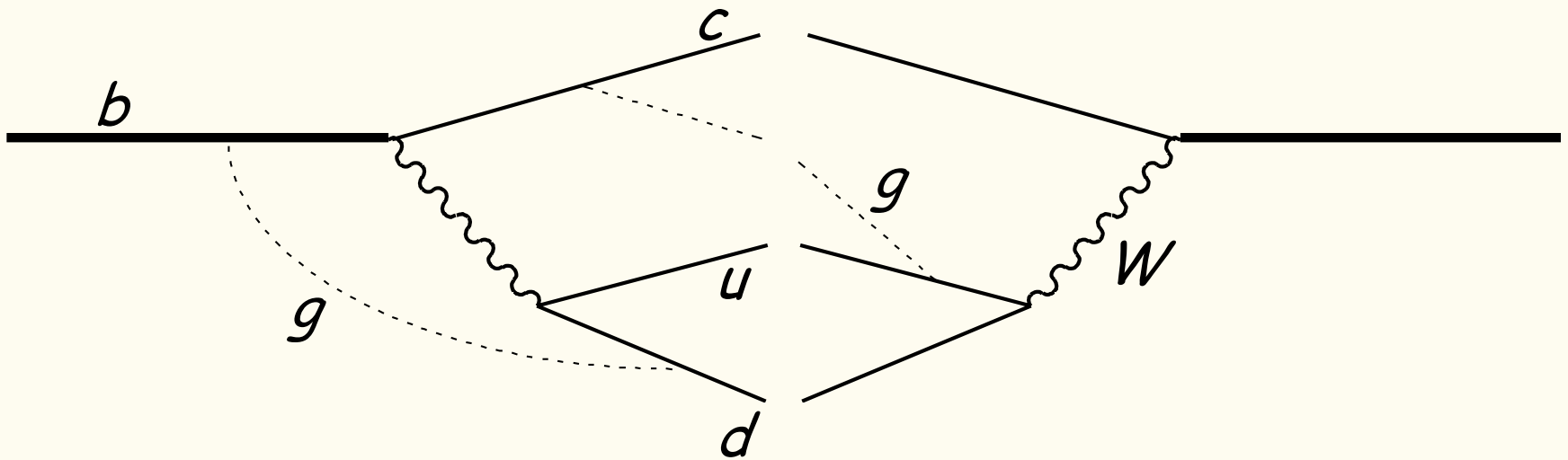
$3.2\sigma$  difference



Standard Model suppressed:  
good place to look for New Physics

# Missing in the theoretical bound: NNLO corrections to non-leptonic decays.

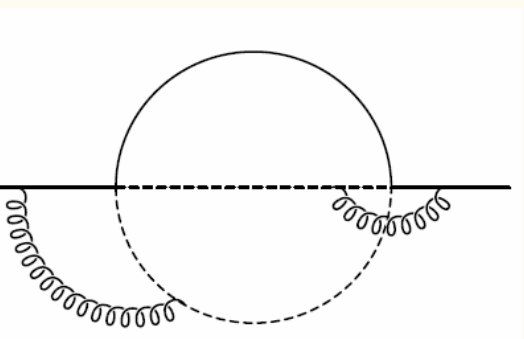
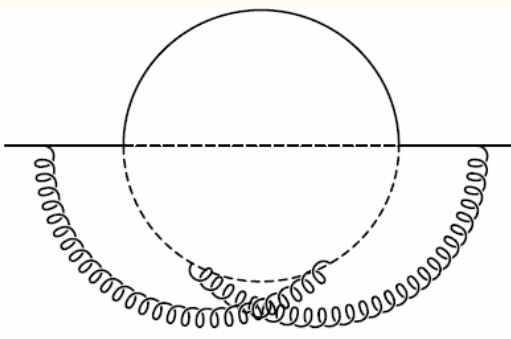
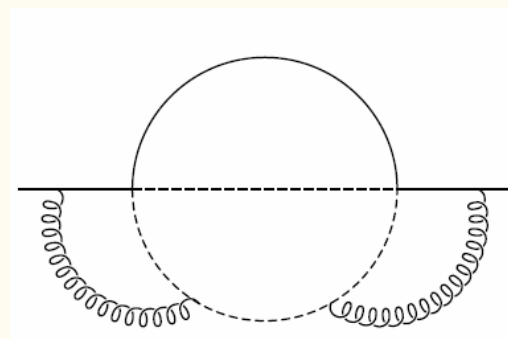
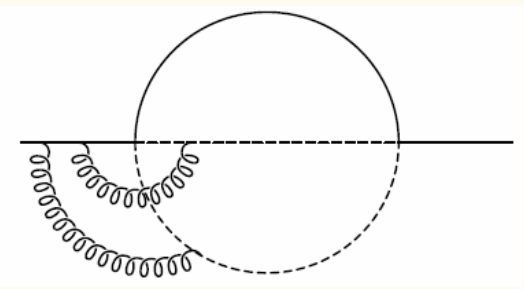
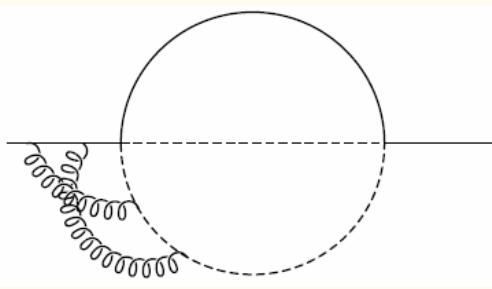
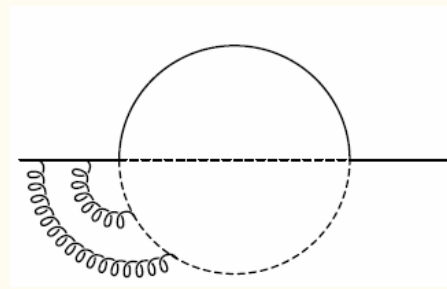
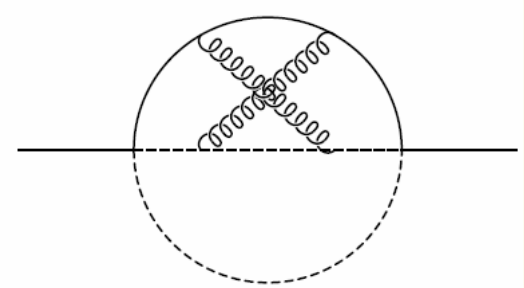
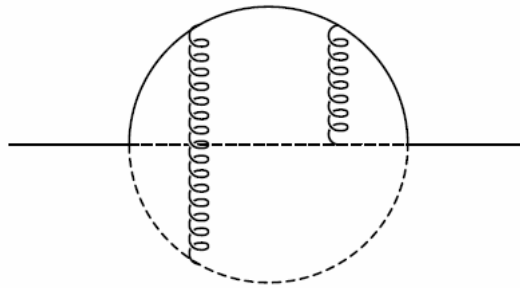
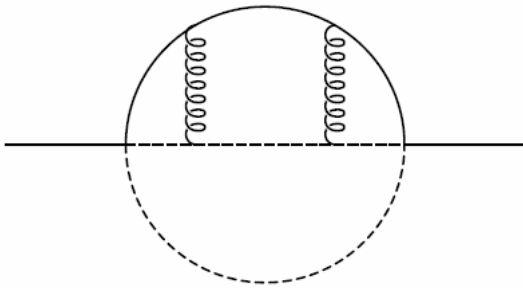
Example:



Four-loop diagrams with masses

Reduction via Laporta algorithm (ordering useful);  
Master integrals: recycle as much as possible.

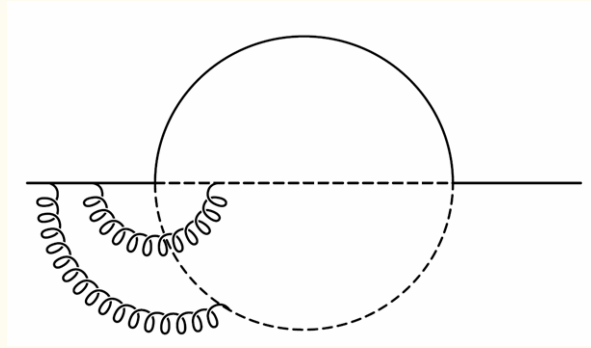
Fortunately: only a dozen `soft' diagrams!



etc.

# Results

Example for a single diagram:



$$-\frac{16}{3} \ln^2 \frac{M_W}{m_b} + \left( -\frac{311}{18} + \frac{10}{3} \pi^2 \right) \ln \frac{M_W}{m_b} + \frac{12287}{324} - \frac{143}{162} \pi^2 + \frac{53}{135} \pi^4 - \frac{14}{9} \zeta_3$$

(with Maciek Ślusarczyk)

Total correction for the non-leptonic width:

$$\frac{\Gamma(b \rightarrow c\bar{u}d) + \Gamma(b \rightarrow c\bar{u}s)}{3\Gamma(b \rightarrow ce\bar{\nu})} = 1 + \frac{\alpha_s}{\pi} + \left( \frac{\alpha_s}{\pi} \right)^2 \left[ 4 \ln^2 \frac{M_W}{m_b} + \frac{15}{2} \ln \frac{M_W}{m_b} + 12.4 \right]$$

About 5-8% increase of the NL width;  
lowers the theoretical lower bound on  $B_{SL}$



# Summary

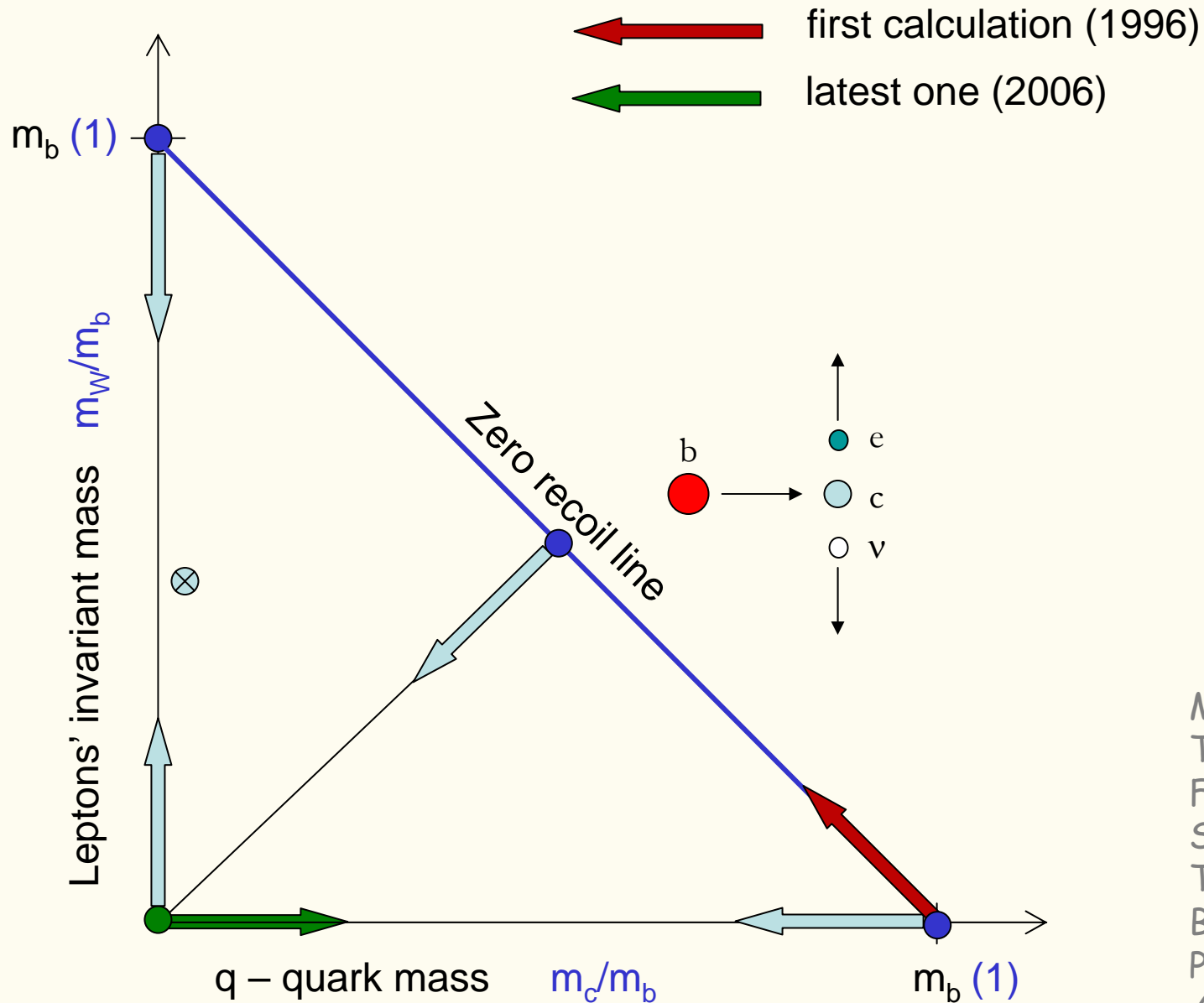
"Fair agreement" reached between theory and experiment;

More important: one can further improve the theoretical prediction (account for charm mass);

Charm mass effects may be very large - a new type of threshold phenomenon?

With new data forthcoming, will we discover competitors to  $W$  bosons?

# Known two-loop corrections on the $bc$ line



Melnikov,  
Tausk,  
Franzkowski,  
Slusarczyk,  
Tkachov,  
Blokland,  
Pak,  
AC

# Status of perturbative corrections to $B_{sl}$

➤  $b \rightarrow xlv$  known exactly at NLO, many results at NNLO (limit of massless quarks in the final state, ...)

➤  $b \rightarrow c\bar{c}s$  known at NLO

charm counting  $\implies$  cannot explain  $B_{sl}$  discrepancy

➤ dominant decay channels  $b \rightarrow c\bar{u}d$ ,  $b \rightarrow c\bar{u}s$  should be studied at NNLO

# The puzzle of the low semileptonic branching

PHYSICAL REVIEW D

VOLUME 51, NUMBER 3

## Inconclusive inclusive nonleptonic $B$ decays

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Physics Letters B 323 (1994) 408–416  
North-Holland

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branching ratio of  
crucially on the  
this assumption  
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arm quarks in  
l duality. We  
 $B$  decays.

## The baffling semileptonic branching ratio of $B$ mesons

I. Bigi<sup>a,b,1</sup>, B. Blok<sup>c,2</sup>, M. Shifman<sup>d,3</sup> and A. Vainshtein<sup>d,e,4</sup>

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December 1993

... the expected value for the semileptonic branching ratio of  $B$  mesons has become ... improved quality of the data and to the increasing maturity of the theoretical ... discuss various theoretical options to reduce the semileptonic  $B$  branching ratio; ... apparent puzzle is the possibility of an unorthodox enhancement in nonperturba- ... "New Physics". Phenomenological implications of such scenarios are pointed out.

The Economist

What's gone wrong for Blair's