

# Collins-Soper kernel from even T generators

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PB meeting

## Motivation

There is a lot of similarity between PB method and TMD factorization method. However, these approach are fundamentally different

### TMD factorization

- ▶ Based on OPE aka TMD factorization theorem
- ▶ Theoretically well-defined components (in terms of operators)
- ▶ Universality (!)
- ▶ Valid in a corner of phase space  
 $q_T \ll Q$
- ▶ Position space

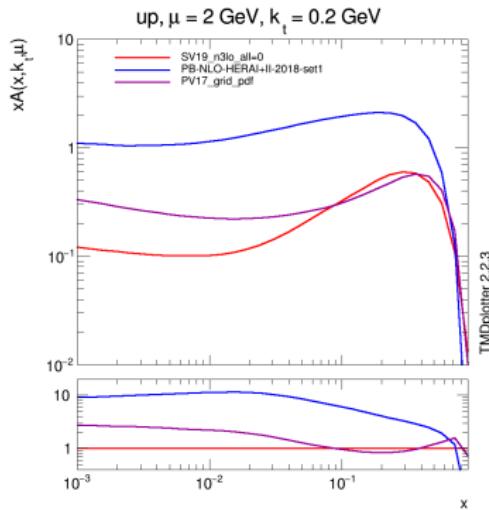
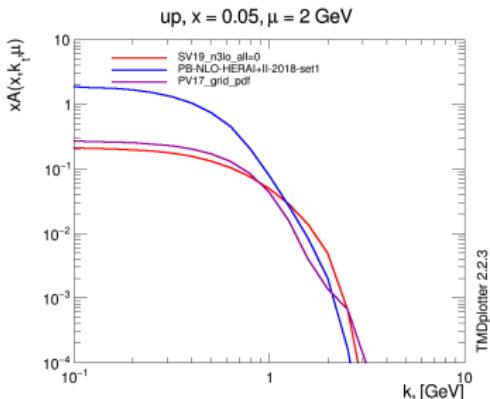
### Parton branching

- ▶ Based on probabilistic interpretation of Feynman graphs
- ▶ No explicit definition of components
- ▶ Universality (?)
- ▶ Valid in a large area of phase space
- ▶ Momentum space

### Main question

- ▶ How to compare elementary blocks of PB and TMD factorization?  
i.e. how to compare TMD distributions

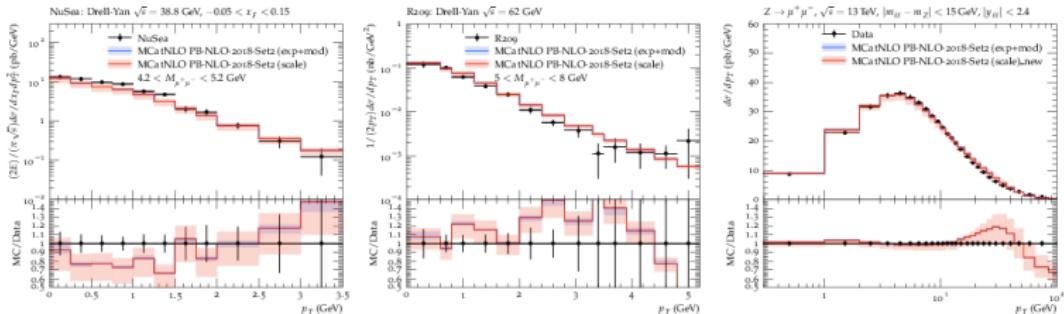
## Direct comparison is nonsense!



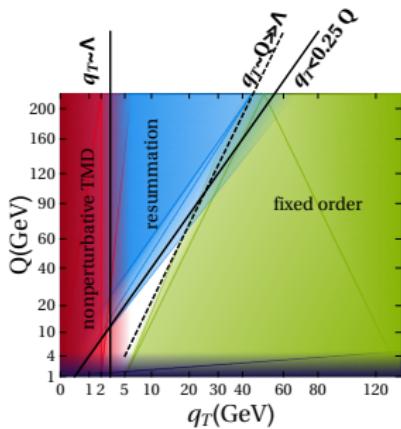
Most probably we compare different objects

What-one-can-do (easily?) is to  
extract and compare the NP evolution kernel (CS-kernel) from PB

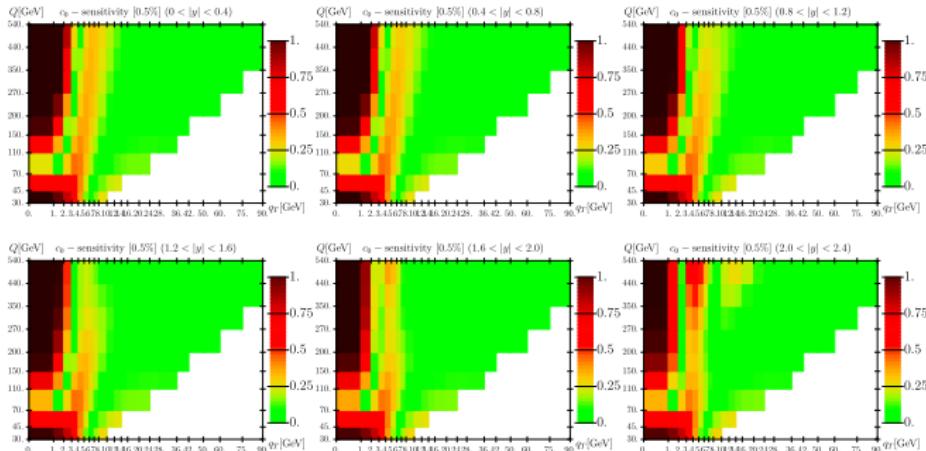
Non-perturbative physics from PB? → Yes, because it explains low- $q_T$



[A. Bermudez-Martinez, et al, 2001.06488]

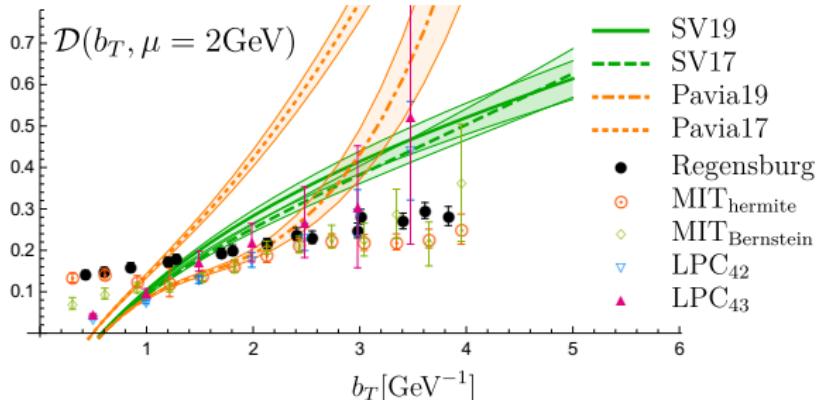


## Sensitivity to NP-evolution parameters (here in kinematics of LHC)

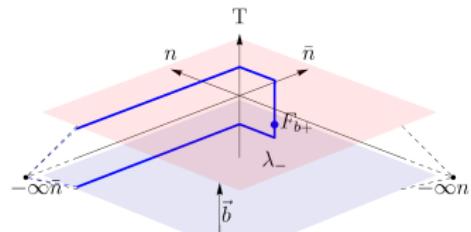


All below  $q_T < 5 - 10\text{GeV}$  is sensitive to NP evolution

## Why is it interesting?



- ▶ CS-kernel is fundamental QCD observable. It parametrizes the vacuum expectation of the Wilson loop with insertion of  $F_{\mu\nu}$  [AV, Phys.Rev.Lett. 125 (2020) 19, 192002]
- ▶ One can extract various NP QCD parameters from it: e.g.  $G_2$ ,  $\sigma$
- ▶ **So far, there is no agreement between extractions!**



$$\frac{d\sigma}{dQ^2 dy d^2 \mathbf{q}_T^2} = \frac{\alpha_{em}^2(Q) \sigma_0}{Q^2} |C_V|^2(Q) \sum_f e_q^f \int \frac{db}{2\pi} b J_0(b q_T) R[Q \rightarrow (\mu, \zeta)]^2 f_{1,f}(x_1, b, \mu, \zeta) f_{1,\bar{f}}$$

- ① Hankel Transform of cross-section

$$\Sigma(b, Q, y, s) = \int_0^\infty dq_T q_T J_0(b q_T) \frac{d\sigma}{dQ^2 dy d^2 \mathbf{q}_T^2} \quad (1)$$

- ② Make a ratio at same  $\{s, y(\text{could be integral}), b\}$  at different  $Q$ 's

$$\frac{\Sigma(b, Q_1, y, s)}{\Sigma(b, Q_2, y, s)} = \frac{\alpha_{em}^2(Q_1)}{\alpha_{em}^2(Q_2)} \frac{Q_2^2}{Q_1^2} \frac{|C_V|^2(Q_1)}{|C_V|^2(Q_2)} \frac{R[Q_1 \rightarrow (\mu, \zeta)]^2}{R[Q_2 \rightarrow (\mu, \zeta)]^2} \quad (2)$$

- ▶  $|C_V|^2(Q)$  is known up to  $\alpha_s^3$
- ▶  $(\mu, \zeta)$  independent
- ▶ Set  $(\mu, \zeta) = (Q_2, Q_2^2)$

- ③ Compute

$$\begin{aligned} R[Q_1 \rightarrow (Q_2, Q_2^2)]^2 &= \frac{\alpha_{em}^2(Q_2)}{\alpha_{em}^2(Q_1)} \frac{Q_2^2}{Q_1^2} \frac{|C_V|^2(Q_2)}{|C_V|^2(Q_1)} \frac{\Sigma(b, Q_1, y, s)}{\Sigma(b, Q_2, y, s)} \\ &= \exp \left( \int_{Q_2^2}^{Q_1^2} \frac{d\mu^2}{\mu^2} \gamma_F(\mu, Q_1) - \mathcal{D}(b, Q_2) \ln \left( \frac{Q_1^2}{Q_2^2} \right) \right) \end{aligned} \quad (3)$$

$$\mathcal{D}(b, Q_2) = \frac{\int_{Q_2^2}^{Q_1^2} \frac{d\mu^2}{\mu^2} \gamma_F(\mu, Q_1) - \ln \left( \frac{\alpha_{em}^2(Q_2)}{\alpha_{em}^2(Q_1)} \frac{Q_1^2}{Q_2^2} \frac{|C_V|^2(Q_2)}{|C_V|^2(Q_1)} \frac{\Sigma(b, Q_1, y, s)}{\Sigma(b, Q_2, y, s)} \right)}{\ln Q_1^2 - \ln Q_2^2} \quad (4)$$

Attention! Possible sign-mistakes

To make such computation one needs

- ▶ Fine binning in  $q_T$  for  $q_T < 5 - 10\text{GeV}$  **Smaller  $q_T$  = larger  $b$**
- ▶ Fine bin in  $Q$  **Smaller bin = smaller uncertainty**
- ▶ Y-bins are unimportant (could be fully integrated) **different Y-bins should give same result**