

$$= \sum_{i,j}^{primitive} F_j^i \mathcal{C}_i \bar{T}_j + (perms)$$