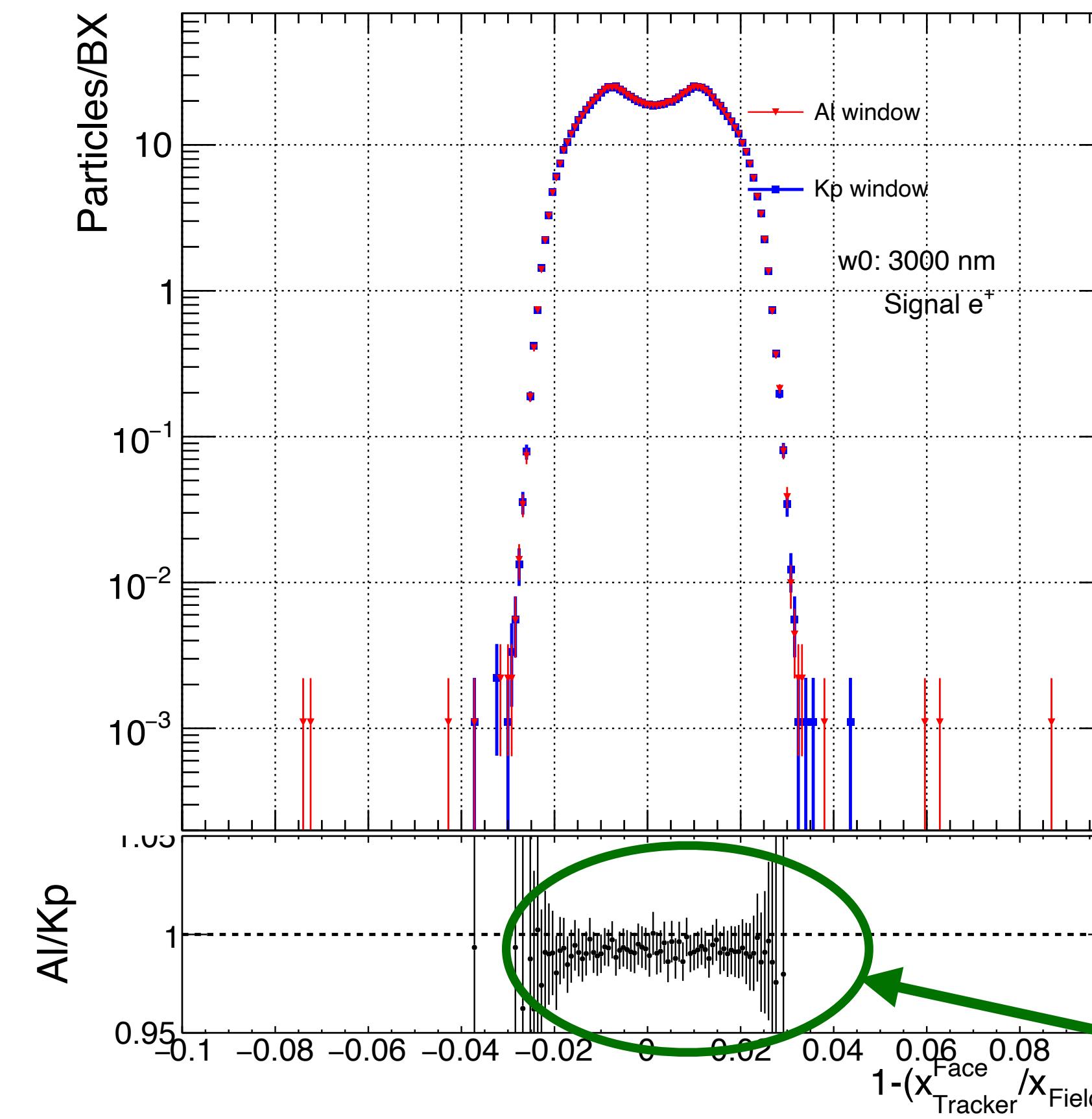


Signal positrons: Comparison with Aluminium window and Kapton window - An update

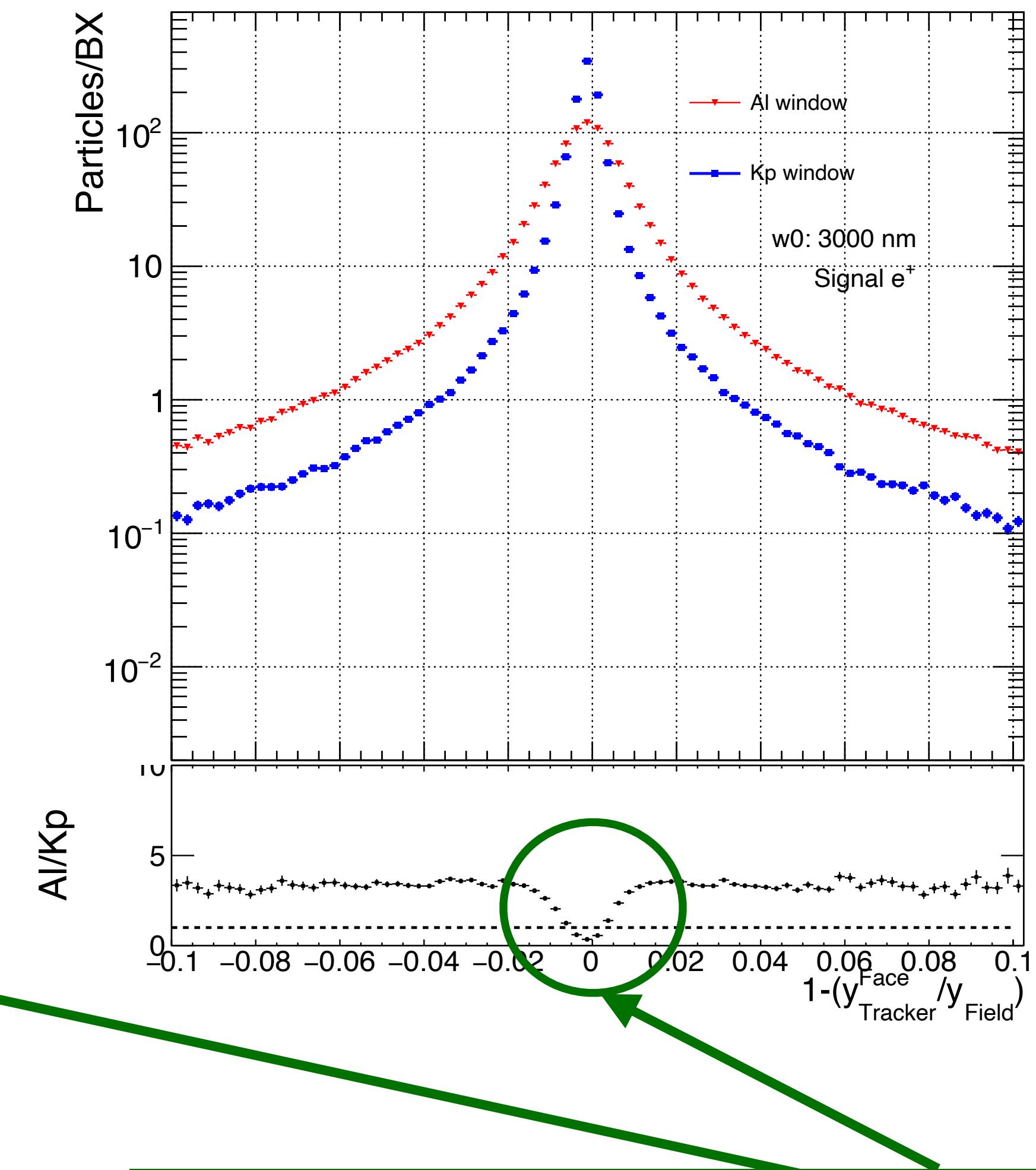
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Rehovot, Israel**

- e+laser hics setup
- Comparison between
 - Exit window of 200 μm of Kapton (Kp).
 - Exit window of 500 μm of Aluminum (Al).
- Looked at the signal positron particles:
 - $(x_{\text{Tracker}}^{\text{Face}}, y_{\text{Tracker}}^{\text{Face}})$ is the position of track at the face of the tracker first layer, coming from Geant4 simulation.
 - x_{Field} is the x position of the track at the face of the tracker first layer, calculated analytically given the magnetic field and momentum of the signal particle at the IP .
 - y_{Field} is the y position of the track at the face of the tracker first layer, calculated analytically given the p_y and p_z of the signal particle at the IP .

Position distribution for signals: Al window and Kapton window



- $(1 - x_{\text{Face Tracker}}^{\text{Field}} / x_{\text{Field}})$ distributions for different window.
- Similar distribution for $(1 - y_{\text{Face Tracker}}^{\text{Field}} / y_{\text{Field}})$.
- For Kapton window, more particles populate $(x_{\text{Field}} - x_{\text{Face Tracker}}^{\text{Field}}) \sim 0$ than that for aluminum window.
 - Similar conclusion for y position.



More particles for Kapton window around 0

Summary

- Aluminum window distorts signal tracks more than Kapton window.
 - The difference between calculated (x,y) and simulated (x,y) is larger for Aluminum window.
 - But the distortion is **negligible**, ~1.3%.
 - **Not a problem** in signal tracks if we use Aluminium window.

Back up

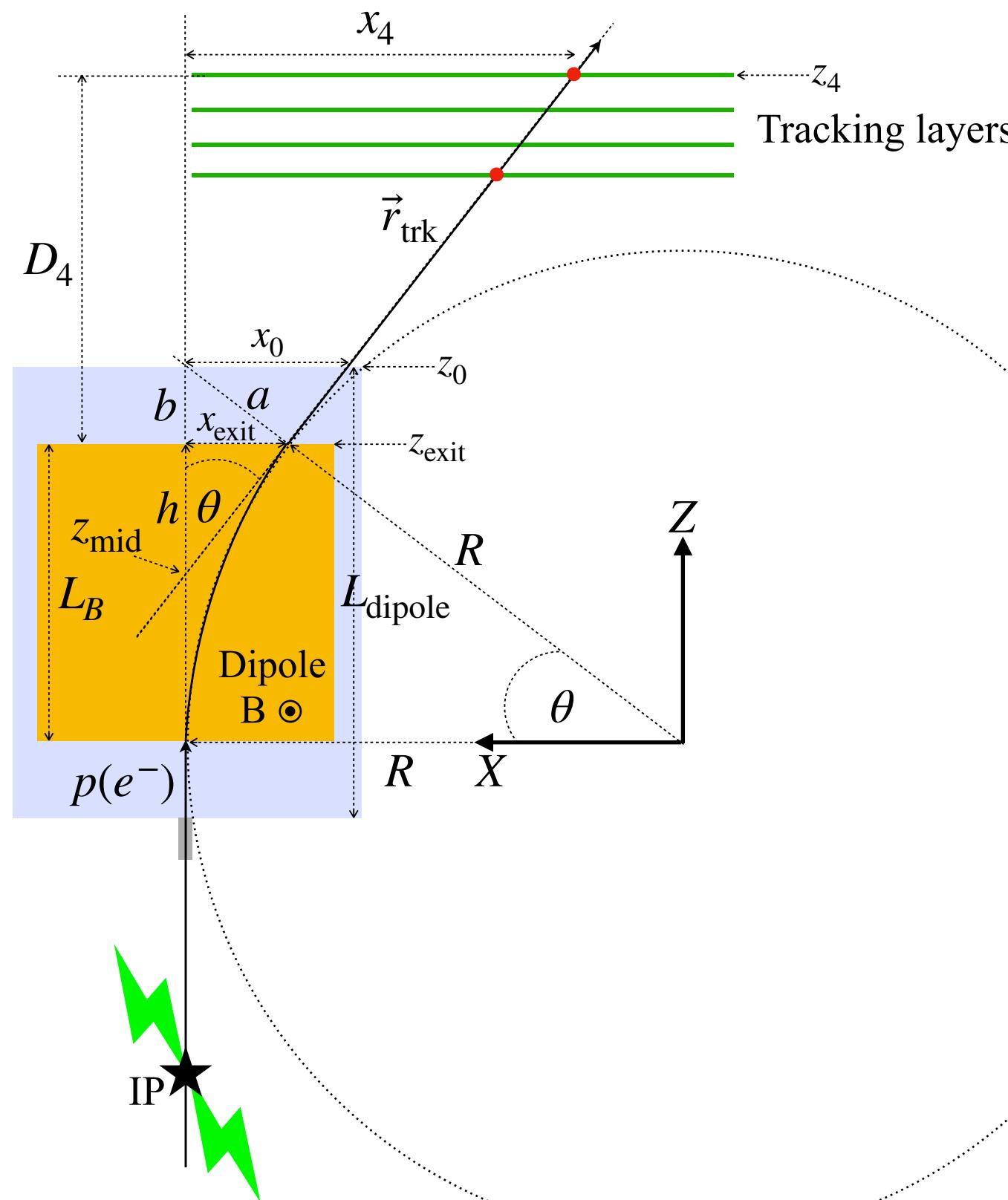
Electron in a B -field of a dipole

- Motion of electron in a uniform magnetic field
- $qBv = mv^2/R \longrightarrow p = qBR \longrightarrow p[\text{GeV}] = 0.3 \cdot B[\text{T}] \cdot R[\text{m}]$
- Getting the momentum from two measurements in the first layer (\vec{r}_1) and the last layer (\vec{r}_4) of the tracker
- Getting the predicted position in the exit plane and in the last layer

Positions prediction

$$p[\text{GeV}] = 0.3 \cdot B[\text{T}] \cdot R[\text{m}]$$

$$R = \frac{p}{0.3B}$$



Circle equation wrt the origin at the centre of the circle defined by the track: $X^2 + Z^2 = R^2$

$$Z_{\text{exit}} = L_B \longrightarrow X_{\text{exit}} = \sqrt{R^2 - L_B^2}$$

$$x_{\text{exit}} = R - X_{\text{exit}} = R - \sqrt{R^2 - L_B^2}$$

Tangent equation: $Z = m \cdot X + c$. The tangent gradient, m , is -1 over the gradient of the radius at the point where the tangent is defined, i.e.: $m = -1/(\Delta Z/\Delta X)$ at the point $(Z_{\text{exit}}, X_{\text{exit}})$

$$m = -1/(\Delta Z/\Delta X) = - (X_{\text{exit}} - 0)/(Z_{\text{exit}} - 0) = - \left(\sqrt{R^2 - L_B^2} \right)/L_B = - \sqrt{\frac{R^2}{L_B^2} - 1}$$

Using the point $(Z_{\text{exit}}, X_{\text{exit}})$ we get the intersection: $c = Z - m \cdot X$

$$c = L_B - \left(-\sqrt{\frac{R^2}{L_B^2} - 1} \right) \cdot \sqrt{R^2 - L_B^2} = L_B + \frac{R^2 - L_B^2}{L_B} = \frac{R^2}{L_B}$$

$$Z_{\text{tangent}} = - \sqrt{\frac{R^2}{L_B^2} - 1} \cdot X_{\text{tangent}} + \frac{R^2}{L_B}$$

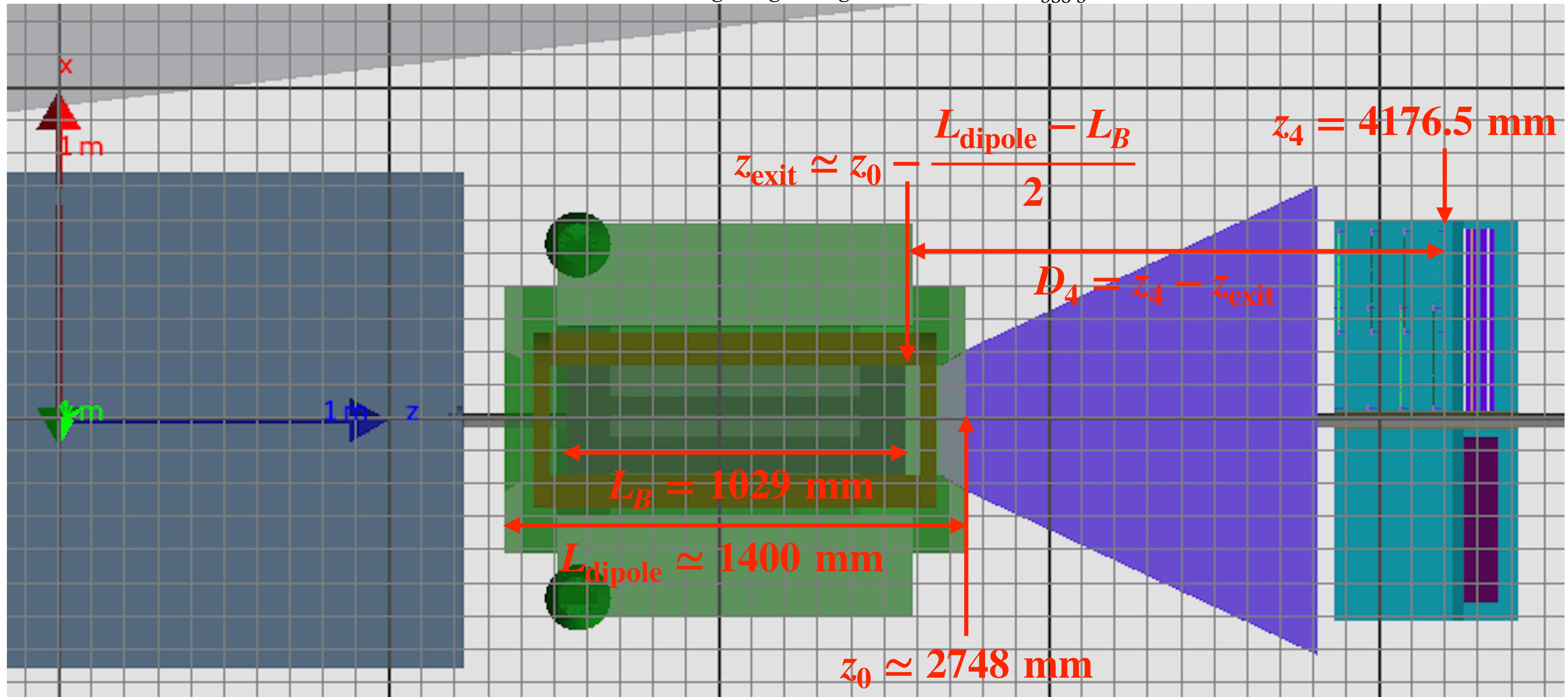
$$X_{\text{tangent}} = \left(\frac{R^2}{L_B} - Z_{\text{tangent}} \right) \frac{L_B}{\sqrt{R^2 - L_B^2}}$$

Putting $Z_4 = L_B + D_4$ or $Z_0 = L_B + \frac{L_{\text{dipole}} - L_B}{2} = \frac{L_B + L_{\text{dipole}}}{2}$ or $Z_{\text{exit}} = L_B$ in the X_{tangent} expression, it is possible to get the prediction for the distance x from the beam axis ($z = 0$), recalling that: $x = R - X_{\text{tangent}}$

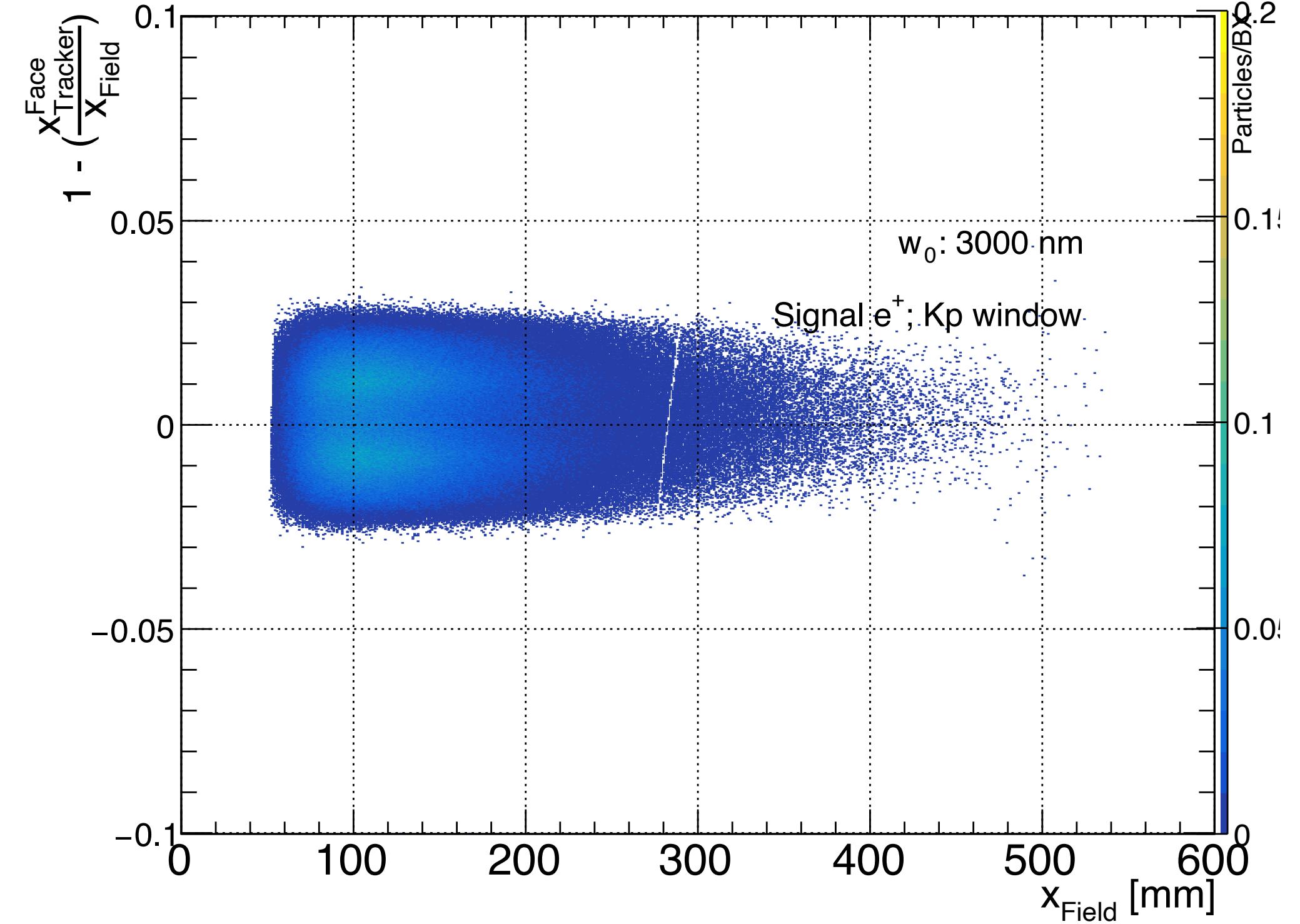
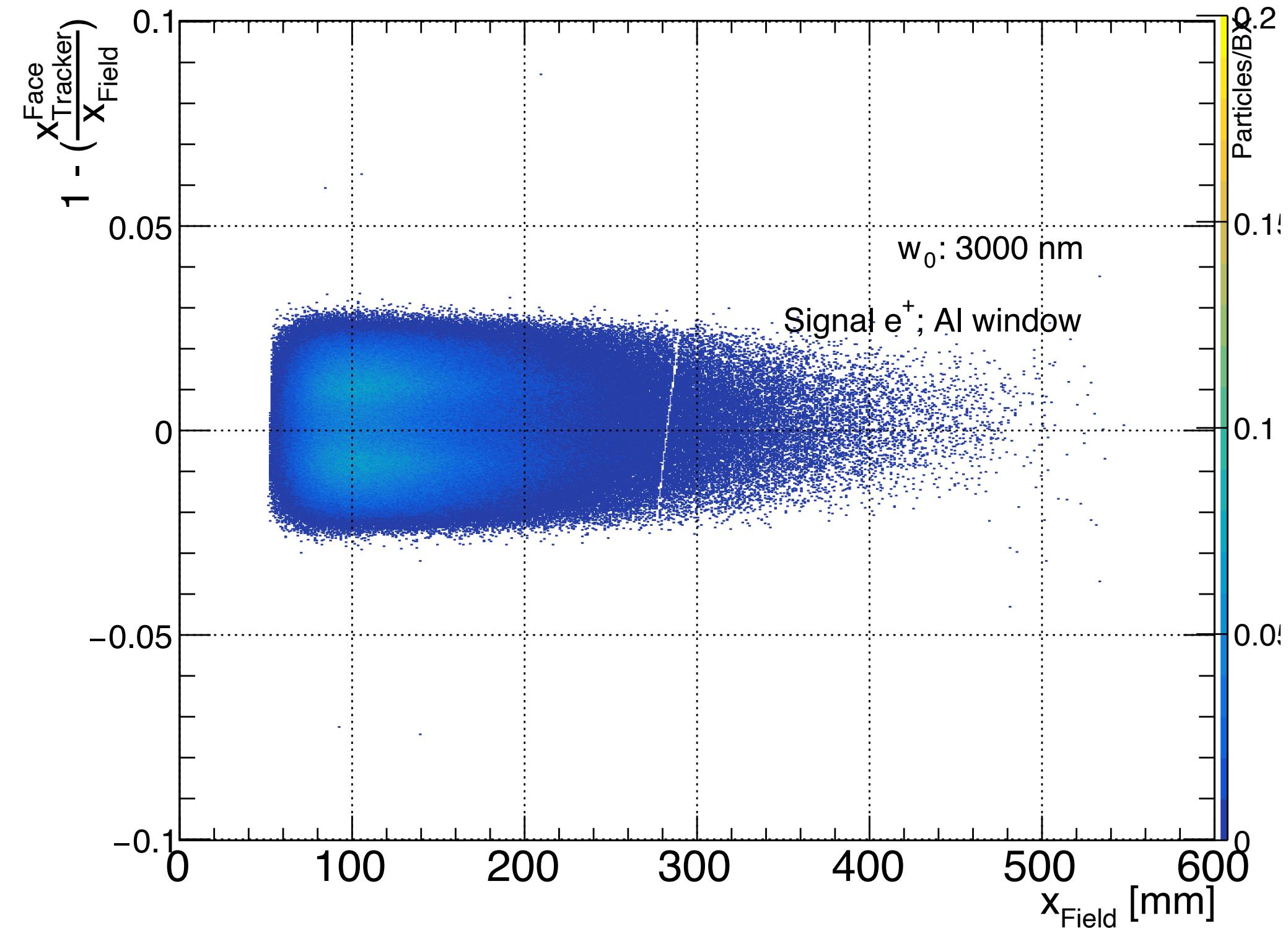
Numbers

z4: 4176.5 [mm], z0: 2748 [mm], zExit: 2562.5 [mm], D4: 1614 [mm]

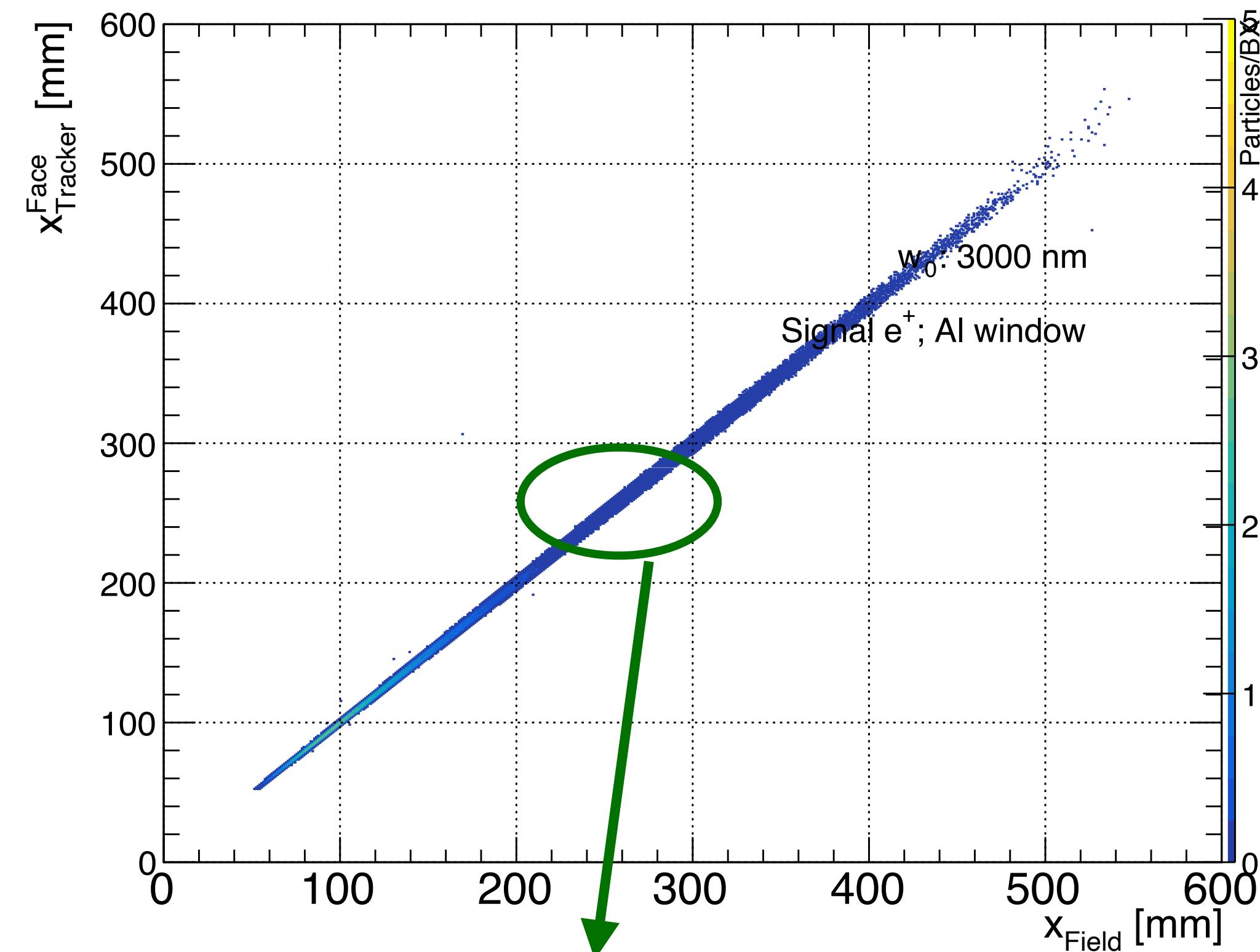
Beginning of Magnetic active volume: 1533.5 mm



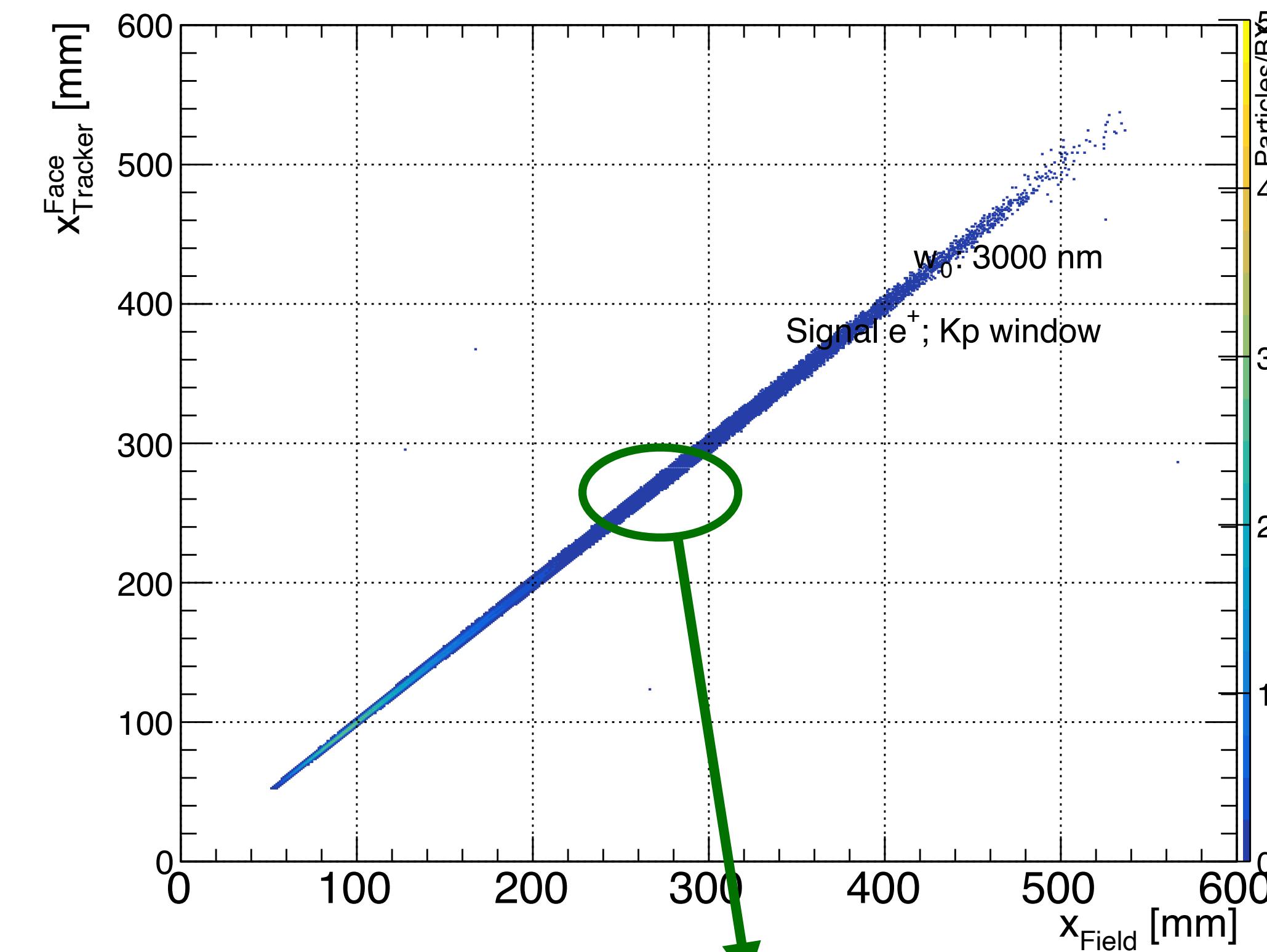
2D distribution of $1 - \frac{x_{\text{Face}}}{x_{\text{Tracker}}} / x_{\text{Field}}$ vs x_{Field}



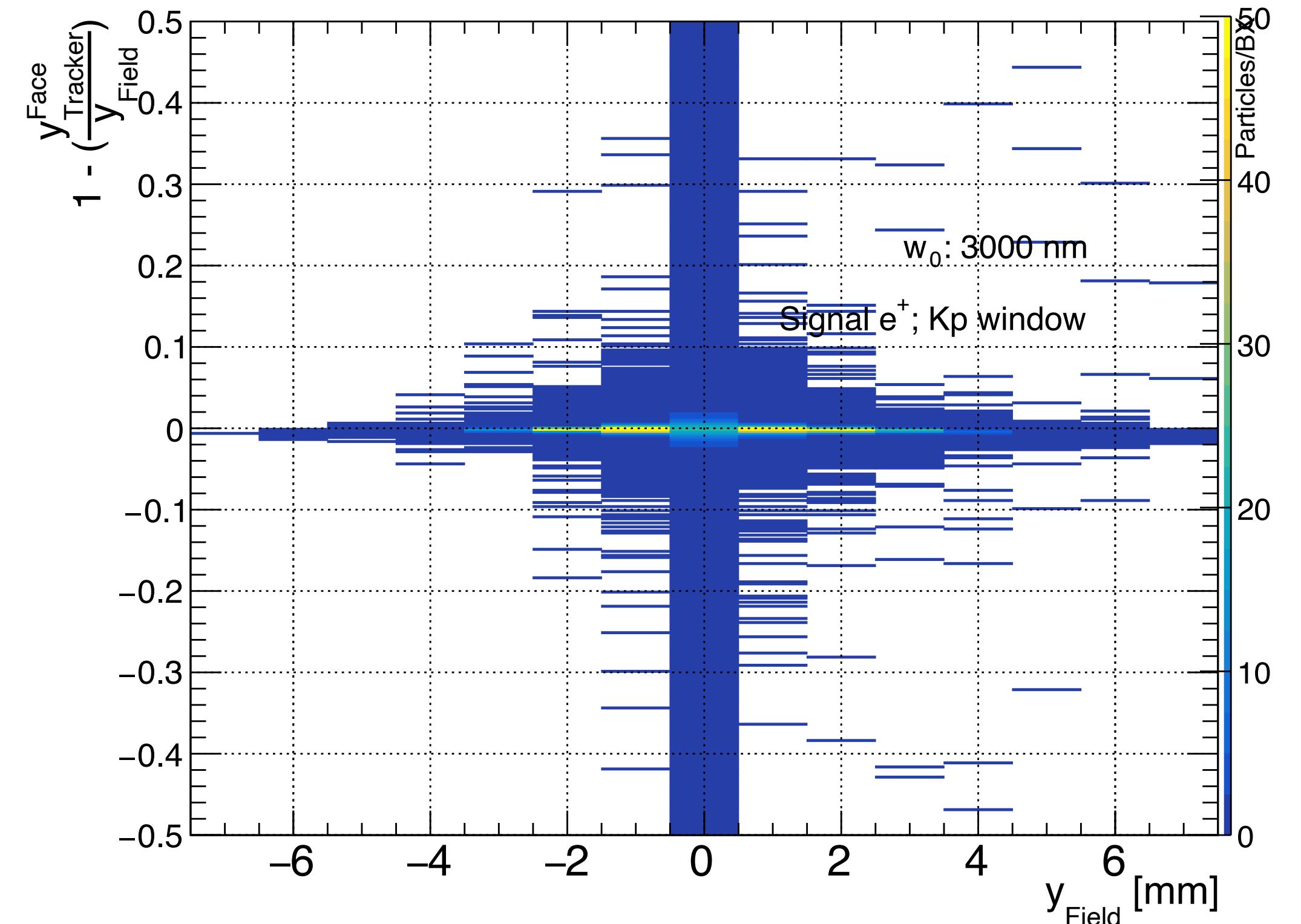
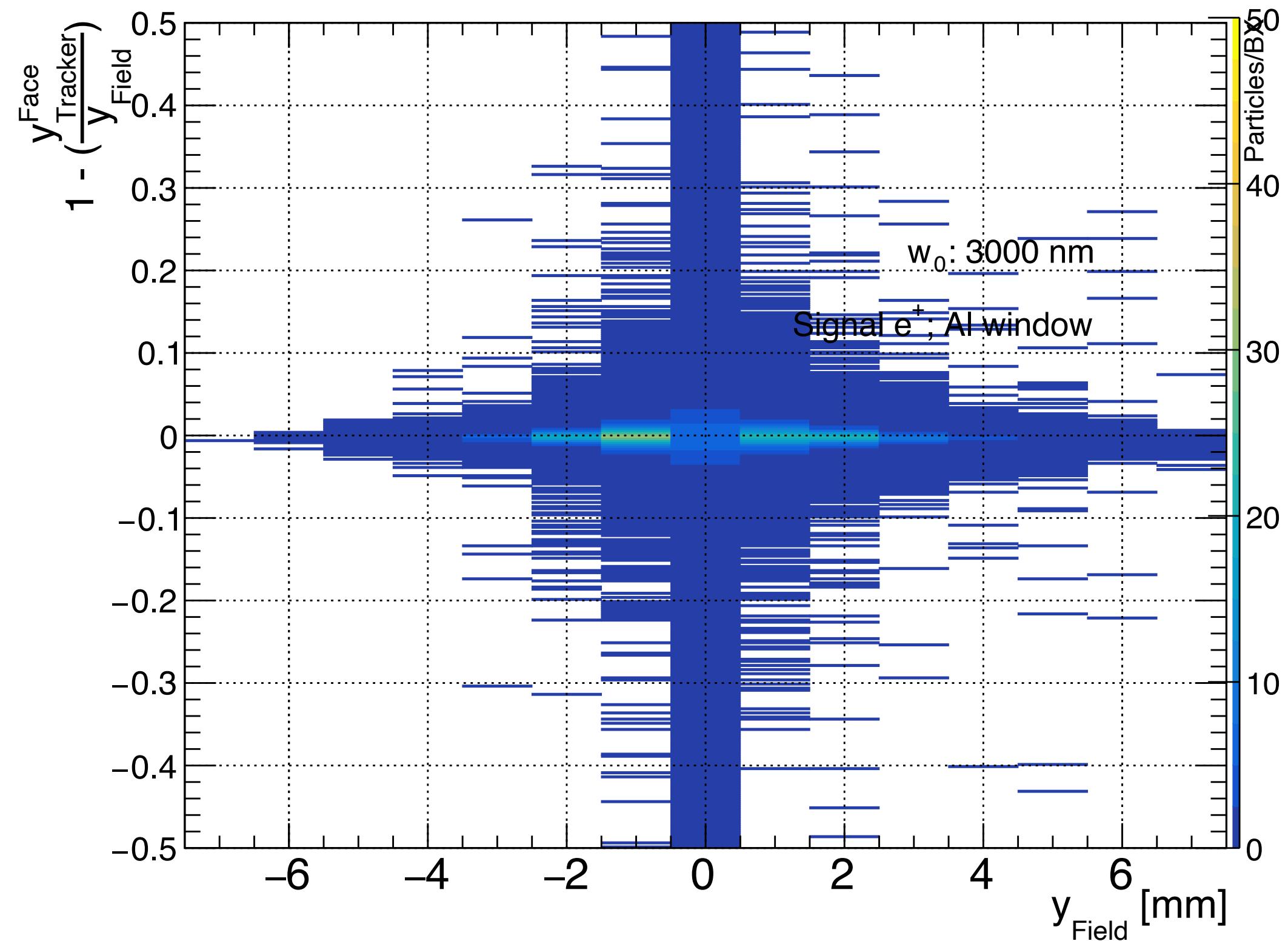
2D distribution of $1 - (x_{\text{Tracker}}^{\text{Face}}/x_{\text{Field}})$ vs x_{Field}



x_{Field} is continuous, while $x_{\text{Tracker}}^{\text{Face}}$ is discontinuous at the junction of two staves

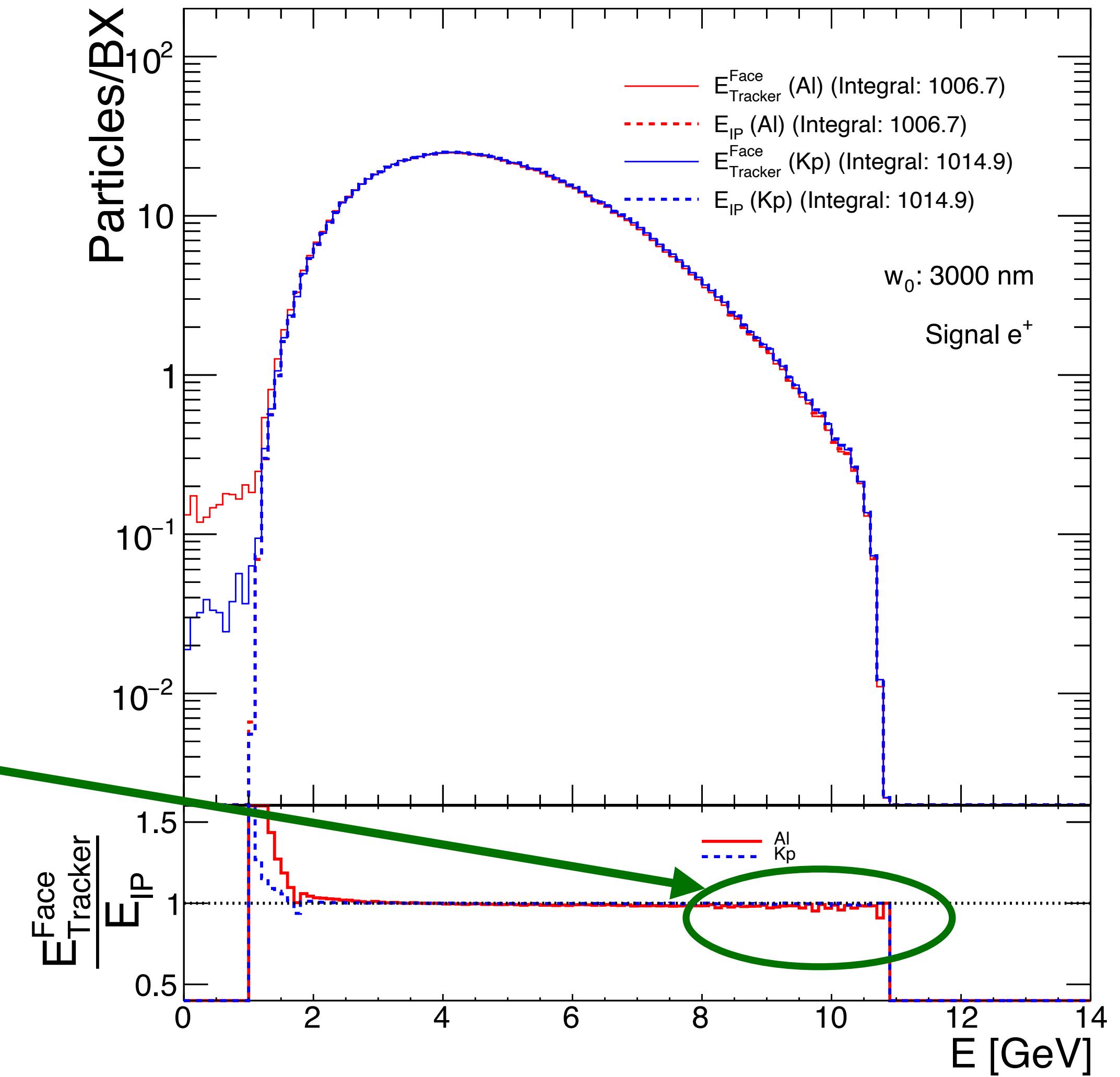


2D distribution of $1 - (y_{\text{Tracker}}^{\text{Face}}/y_{\text{Field}})$ vs y_{Field}



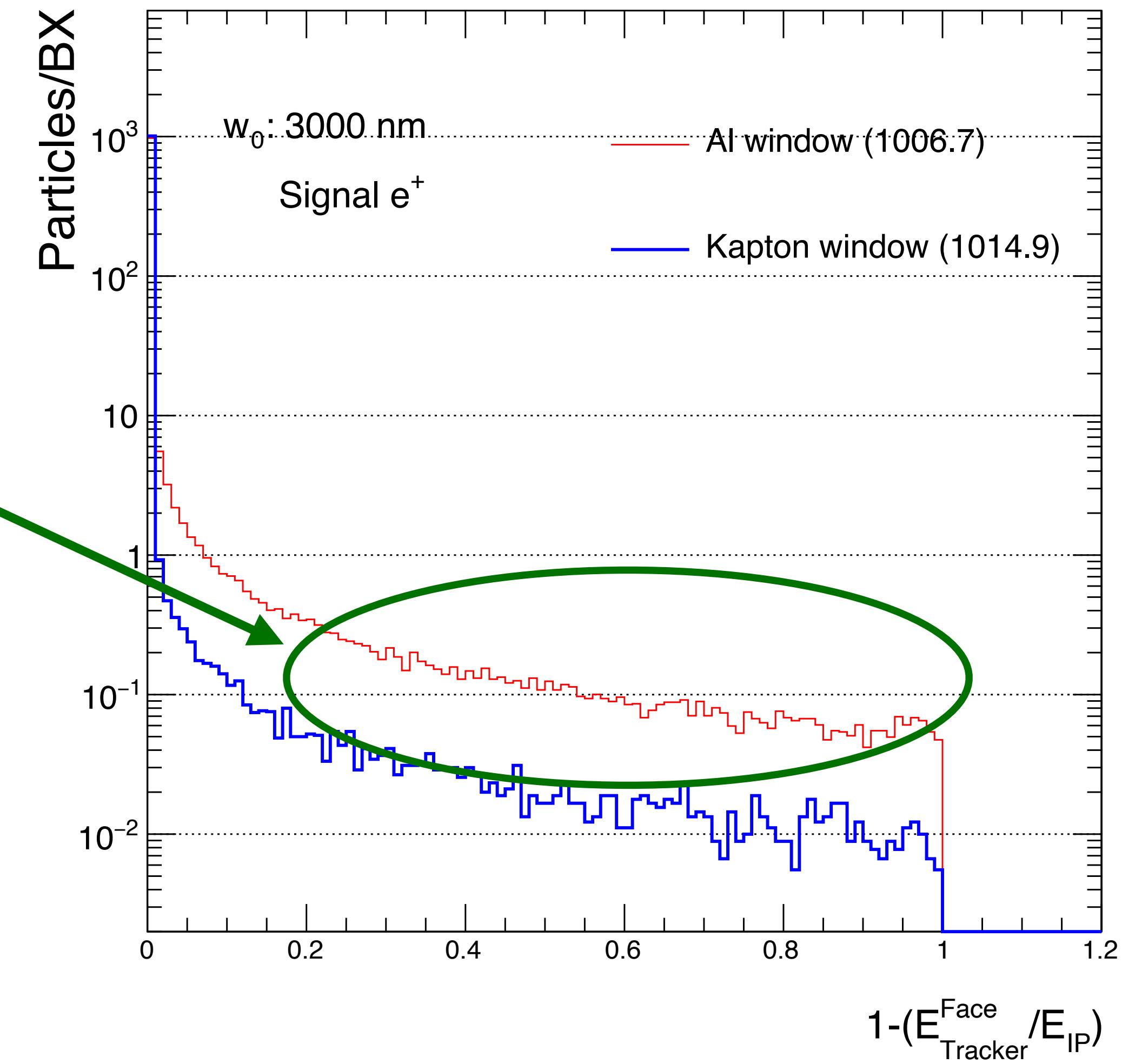
Energy distribution for signals: Al window and Kapton window

- $E_{\text{Tracker}}^{\text{Face}}$ and E_{IP} distributions for different window
- E_{IP} distributions are almost similar for both the window: expected
- For Aluminium window, $E_{\text{Tracker}}^{\text{Face}}$ is slightly less than E_{IP} at $E > 8 \text{ GeV}$.
 - This is not visible for Kapton window.
 - Not very informative plot to distinguish between Al window and Kapton window.

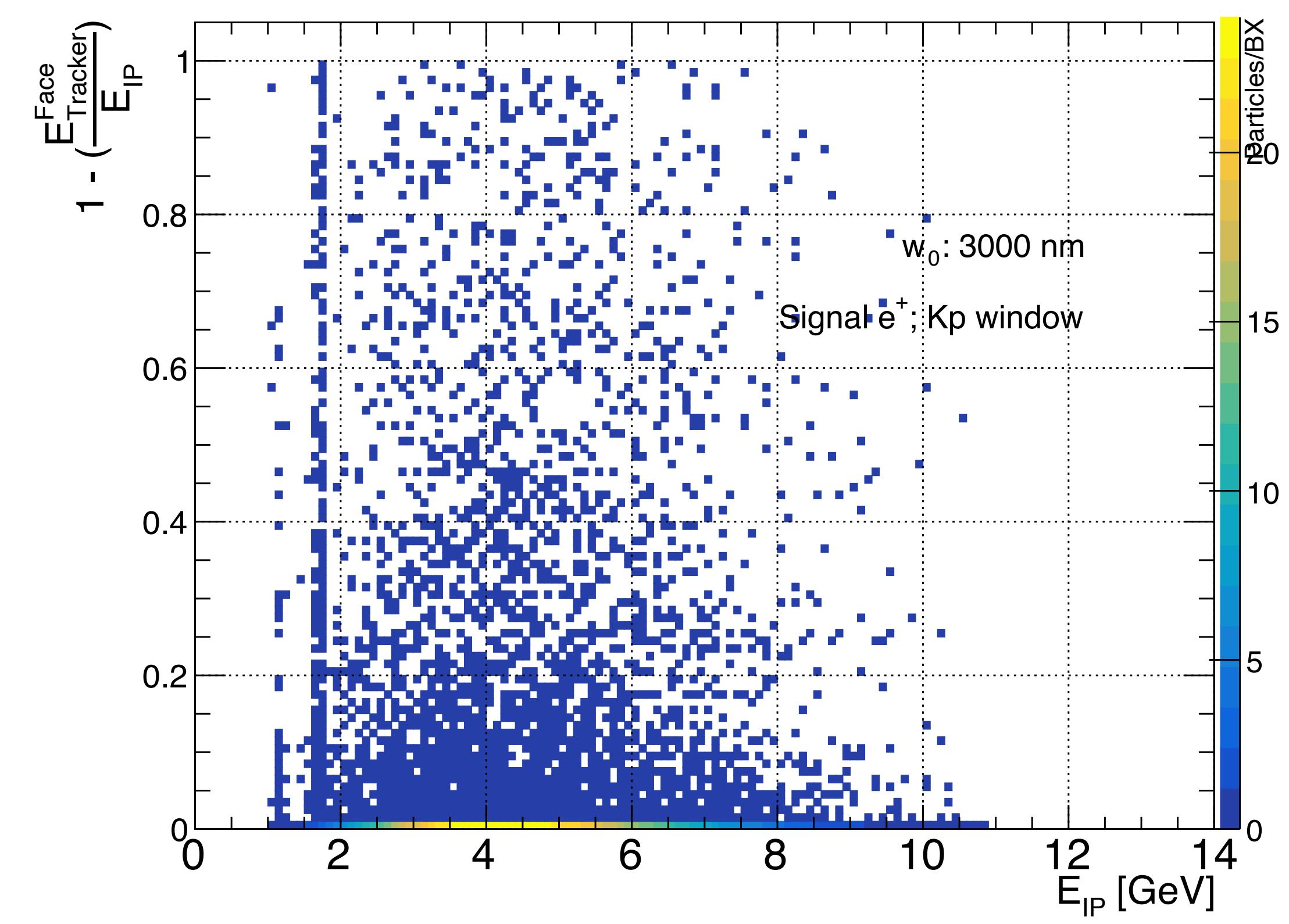
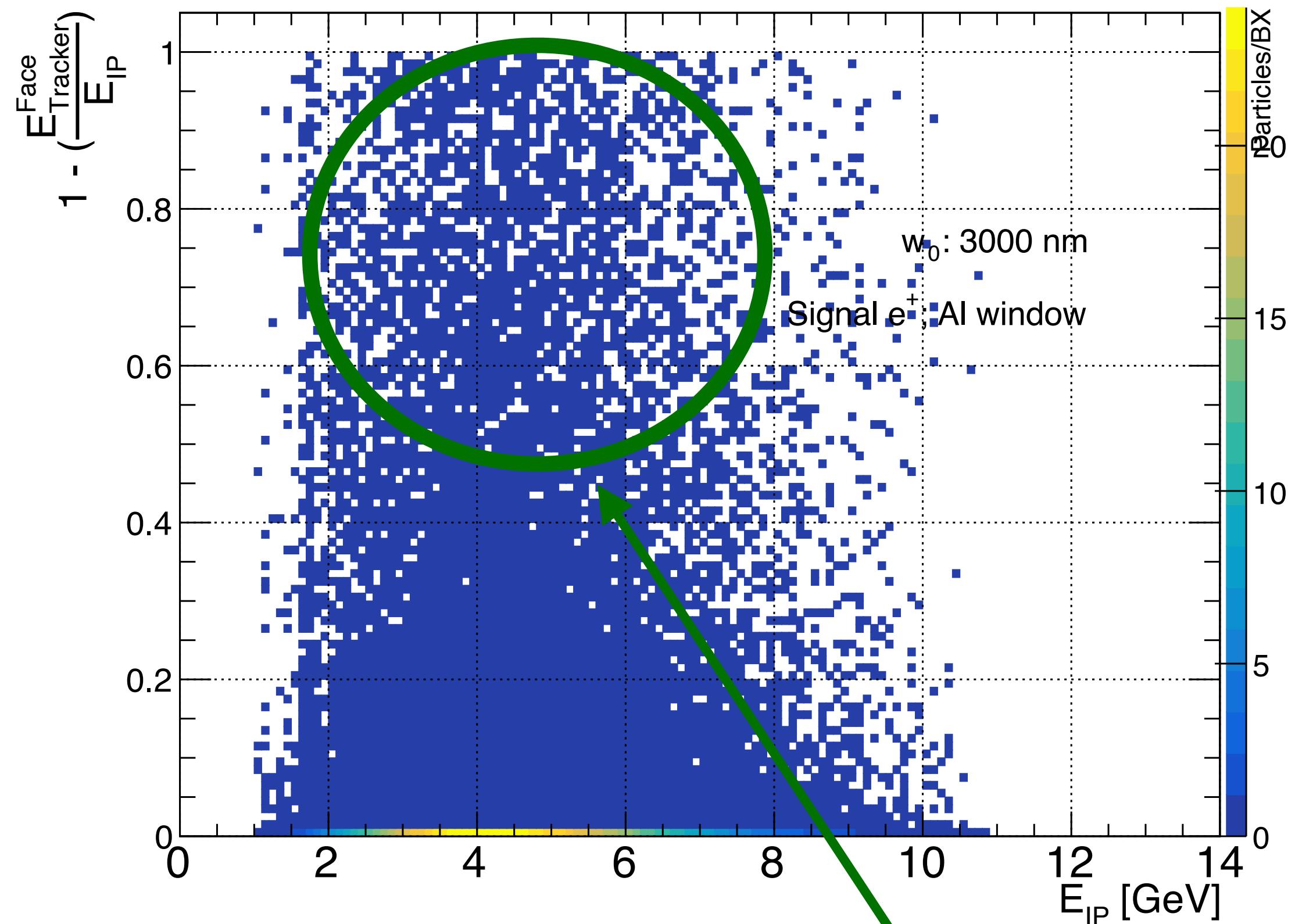


$1 - (E_{\text{Tracker}}^{\text{Face}} / E_{\text{IP}})$: Prominent difference of Al window and Kapton window

- For aluminum window more tracks are distorted compared to Kapton window.
- Fraction of tracks distorted for Al window: 1.3%
- Fraction of tracks distorted for Kp window: 0.2%
 - Distortion is measured as the fraction of tracks where $1 - (E_{\text{Tracker}}^{\text{Face}} / E_{\text{IP}})$ is greater than 10%.

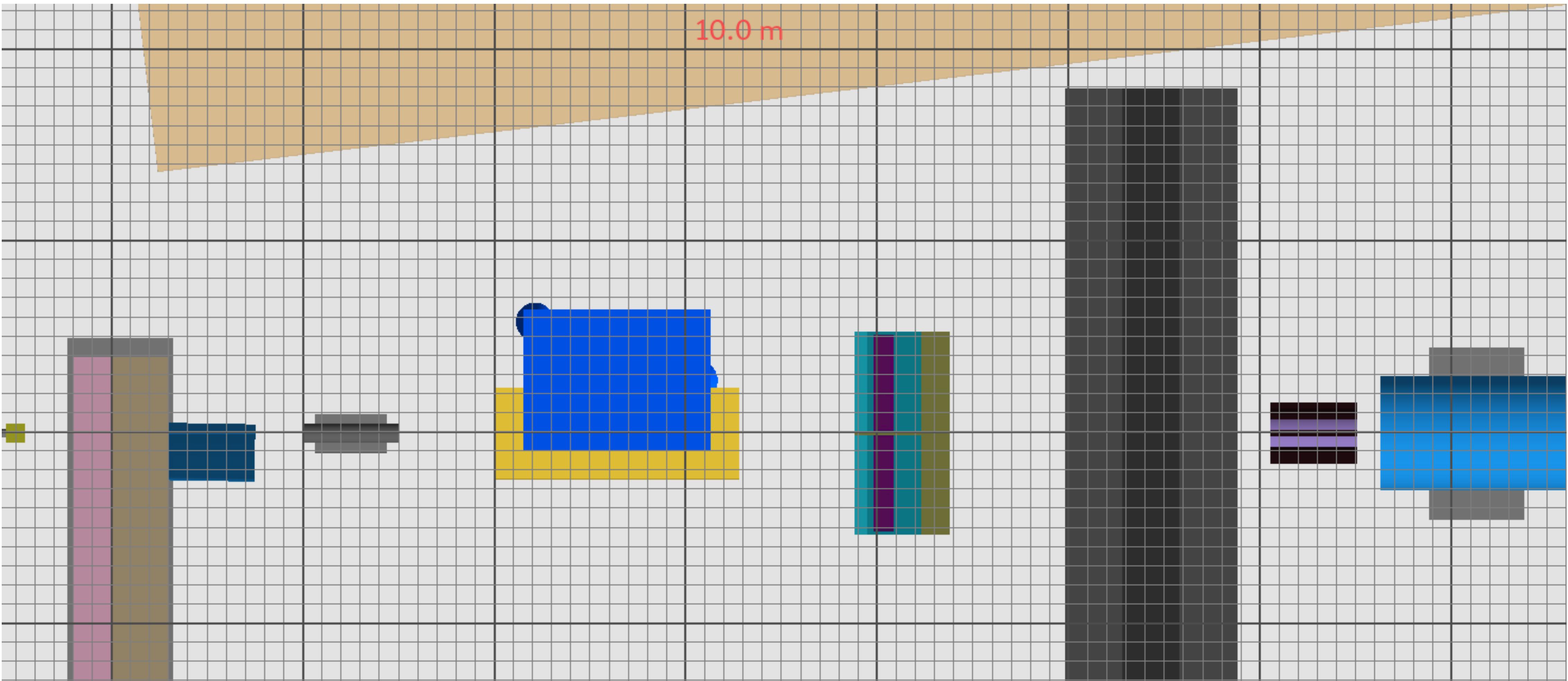


2D distribution of $1 - (\frac{E_{\text{Face}}}{E_{\text{Tracker}}} / E_{\text{IP}})$ vs E_{IP}



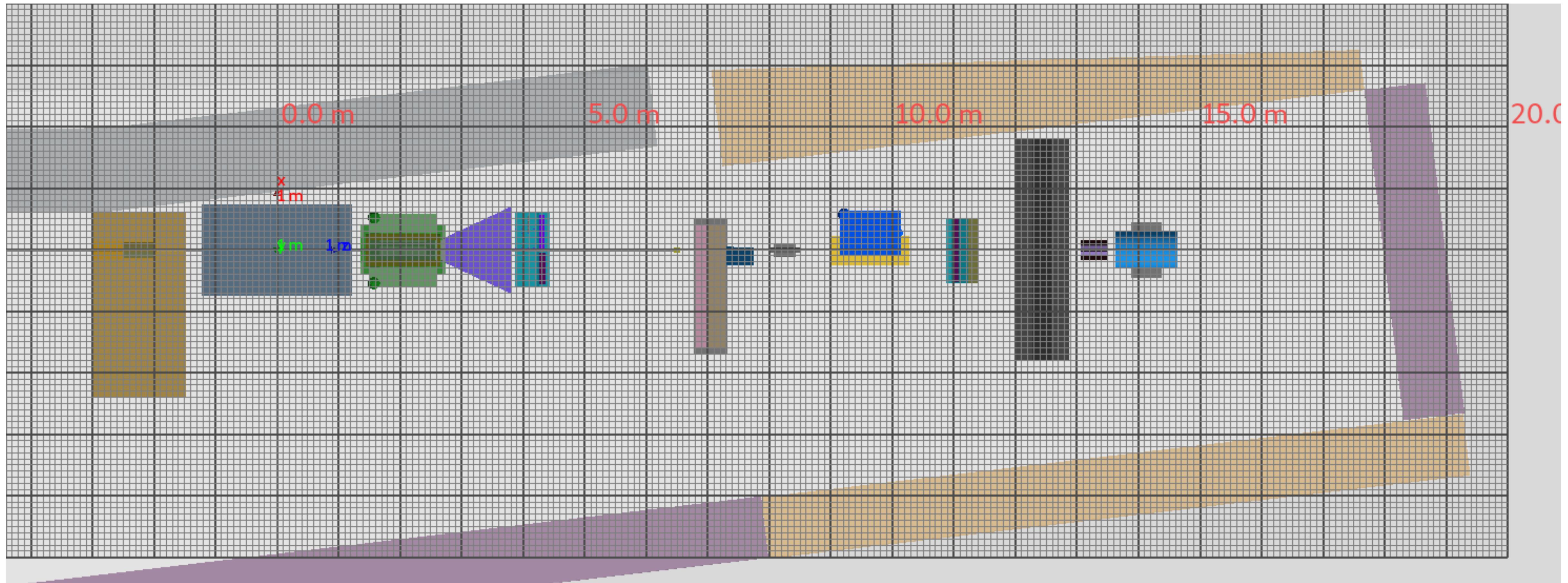
For Aluminium window, tracks with energy 3 GeV to 5 GeV are more distorted

The subsystems near the beam dump



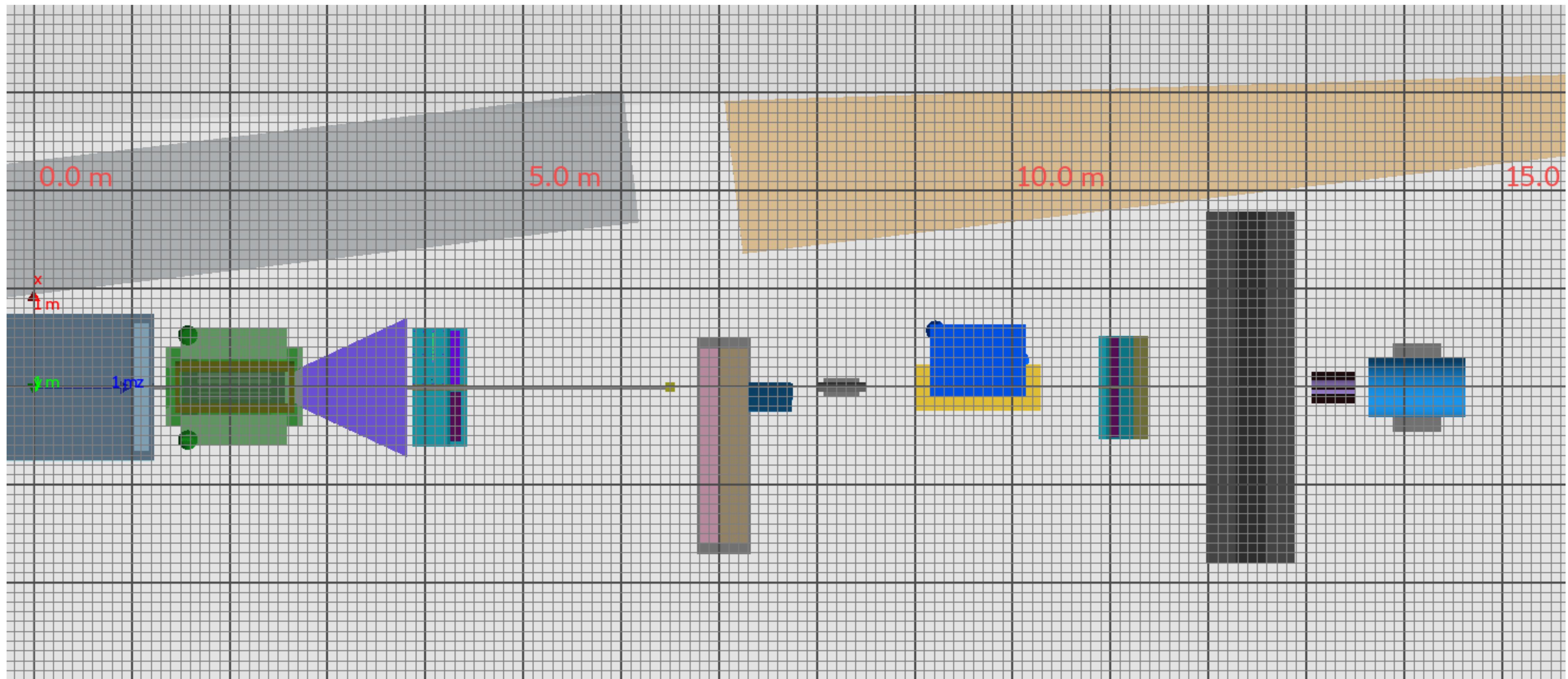
Plots from Sasha

The entire subsystem



Plots from Sasha

The subsystems from the IP to beam dump



Plots from Sasha