Resummation of low p<sub>T</sub> differential distributions in Soft-collinear Effective Theory

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# Outline

- Introductory Remarks
- Collins-Soper-Sterman approach to low-p<sub>T</sub> resummation
- Soft-collinear effective theory approach

-Factorization and resummation formula:

 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes \mathcal{G}^{ij} \otimes f_i \otimes f_j$ 

RG evolution

Soft-collinear emissions PDFs

Conclusions

## Factorization



- New physics at hard scale; M<sub>H</sub> for example
- Parton shower evolution from  $M_H$  to  $\Lambda_{QCD}$
- Final state hadronization at Λ<sub>QCD</sub>
  Parton distribution functions at Λ<sub>QCD</sub>
- Multiple parton interactions, hadron decays, ...

• How do we make sense of this environment?

**Factorization!** 

# Factorization $d\sigma = \sum_{i,j} d\sigma_{ij}^{\text{part}} \otimes f_i(\xi_a) \otimes f_j(\xi_b)$ Calculable in pQCD Extracted from data

Separates perturbative and non-perturbative scales
 Turns pQCD into a predictive framework in complicated hadron collider environments
 Factorization is not obvious, and is often difficult to prove lepton + A → lepton ' + X

$$e^+ + e^- \rightarrow A + X$$
  
 $A + B \rightarrow V + X$   
 $A + B \rightarrow \text{jet} + X$   
 $A + b \rightarrow \text{heavy quark} + X$ 

Factorization "expected to hold" Collins-Soper-Sterman, 2004 review

# Factorization and Resummation

• Fully inclusive Drell-Yan, Higgs:



$$\sigma = \sum_{i,j} \mathrm{d}\sigma_{ij}^{\mathrm{part}} \otimes f_i(\xi_a) \otimes f_j(\xi_b)$$

Lives at the hard scale; calculable in pQCD Live at non-perturbative scale; extract from data

RG evolve to hard scale

• Resummation done by evaluating PDFs at the hard scale after renormalization group running (DGLAP)

# Resummation

• In the presence of final state restrictions:

 $\mathrm{d}\sigma = \sum_{i,j} \mathrm{d}\sigma_{ij}^{\mathrm{part}} \otimes f_i(\xi_a) \otimes f_j(\xi_b)$ 

scales involved. scale.

Multiple disparate Live at non-perturbative

Additional resummation needed.

• Example: low transverse momentum distribution in Drell-Yan, Higgs production

# Why do logs arise from final state restrictions?Fully inclusive electron-positron annihilation:

Cancellation of infrared divergences between virtual and real graphs.

• Incomplete cancellation of IR divergences in presence of final state restrictions gives rise to large logarithms of restricted kinematic variable

# Low pT Region

• The schematic perturbative series for the pT distribution for  $pp \rightarrow (h,V)+X$ 



- Resummation of large logarithms required
- Low pT resummation has been studied in great detail

(Dokshitzer, Dyakonov, Troyan; Parisi, Petronzio; Curci et al.; Davies, Stirling; Collins, Soper, Sterman; Arnold, Kauffman; Berger, Qiu; Ellis, Ross, Veseli; Ladinsky, Yuan; Bozzi, Catani, de Florian, Grazzini,....)

• Low pT region important for W mass, Higgs searches, ...

# Higgs Search at the LHC



 $\sigma \times BR^2$  [pb]

1.24

7.4

62.0

 $\approx 6$ 

Accepted event fraction

cut 4-6

0.18

0.055

0.070

0.092

(Dittmar, Dreiner)

cut 7

0.080

0.039

0.001

0.013

cut 1-3

0.21

0.14

0.17

0.17

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LHC 14 TeV

reaction  $pp \to X$ 

 $pp \to H \to W^+W^- \ (m_H = 170 \text{ GeV})$ 

 $pp \to W^+W^-$ 

 $pp \rightarrow t\bar{t} \ (m_t = 175 \text{ GeV})$ 

 $pp \rightarrow Wtb \ (m_t = 175 \text{ GeV})$ 

# **Collins-Soper-Sterman Formalism**

 $A(P_A) + B(P_B) \rightarrow C(Q) + X, \quad C = \gamma^*, W^{\pm}, Z, h$ 

• The transverse momentum distribution is schematically given by:

 $\frac{d\sigma_{AB\to CX}}{dQ^2 \, dy \, dQ_T^2} = \frac{d\sigma_{AB\to CX}^{(\text{resum})}}{dQ^2 \, dy \, dQ_T^2} + \frac{d\sigma_{AB\to CX}^{(Y)}}{dQ^2 \, dy \, dQ_T^2}$ Most singular contribution; goes like  $I/Q_T^2$ Soft or collinear Contributions from hard jets gluon emissions

Focus of this talk  $\frac{d\sigma_{AB\to CX}}{dQ^2 \, dy \, dQ_T^2} = \frac{d\sigma_{AB\to CX}^{(\text{resum})}}{dQ^2 \, dy \, dQ_T^2} + \frac{d\sigma_{AB\to CX}^{(Y)}}{dQ^2 \, dy \, dQ_T^2}$ 

> Singular as at least Q<sub>T</sub><sup>-2</sup> as Q<sub>T</sub>→0
> Important in region of small Q<sub>T</sub>
> Treated with resummation

 Less singular terms (integrable without distributions)

• Important in region of large Q<sub>T</sub>

#### • The CSS resummation formula takes the form:

$$\frac{d^2\sigma}{dp_T dY} = \sigma_0 \int \frac{d^2b_\perp}{(2\pi)^2} e^{-i\vec{p}_T \cdot \vec{b}_\perp} \sum_{a,b} \left[ C_a \otimes f_{a/P} \right] (x_A, b_0/b_\perp) \left[ C_b \otimes f_{b/P} \right] (x_B, b_0/b_\perp) \right] \\ \times \exp\left\{ \int_{b_0^2/b_\perp^2}^{\hat{Q}^2} \frac{d\mu^2}{\mu^2} \left[ \ln \frac{\hat{Q}^2}{\mu^2} A(\alpha_s(\mu^2)) + B(\alpha_s(\mu^2)) \right] \right\}.$$

Coefficients with well defined perturbative expansions

# Why b-space?

 Both matrix elements and phase space simplify in softemission limit

Eikonal approximation  
(soft photons): 
$$\mathcal{M}_n \propto g^n \mathcal{M}_0 \left\{ \frac{p_1 \cdot \epsilon_1 \dots p_1 \cdot \epsilon_n}{p_1 \cdot k_1 \dots p_1 \cdot k_n} + (-1)^n \frac{p_2 \cdot \epsilon_1 \dots p_2 \cdot \epsilon_n}{p_2 \cdot k_1 \dots p_2 \cdot k_n} \right\}$$

Phase space:  

$$d\Pi_n \propto \nu(k_{T1}) d^2 k_{T1} \dots \nu(k_{Tn}) d^2 k_{Tn} \ \delta^{(2)} \left( \vec{p}_T - \sum_i \vec{k}_{Ti} \right)$$

$$\nu(k_T) = k_T^{-2\epsilon} \ln\left(\frac{s}{k_T^2}\right)$$

• Would be independent except for phase-space constraint; Fourier transform to b-space accomplishes this

$$\int \frac{d^2 b}{(2\pi)^2} e^{-i\vec{b}\cdot\vec{p}_T} \int d^2 k_{T1} f(k_{T1}) \dots d^2 k_{Tn} f(k_{Tn}) \,\delta^{(2)} \left(\vec{p}_T - \sum_i \vec{k}_{Ti}\right)$$
$$= \int \frac{d^2 b}{(2\pi)^2} e^{-i\vec{b}\cdot\vec{p}_T} \left[\tilde{f}(b)\right]^n, \quad \tilde{f}(b) = \int d^2 k_T e^{i\vec{b}\cdot\vec{k}_T} f(k_T)$$

$$\frac{d^{2}\sigma}{dp_{T} dY} = \sigma_{0} \int \frac{d^{2}b_{\perp}}{(2\pi)^{2}} e^{-i\vec{p}_{T}\cdot\vec{b}_{\perp}} \sum_{a,b} \left[ C_{a} \otimes f_{a/P} \right] (x_{A}, b_{0}/b_{\perp}) \left[ C_{b} \otimes f_{b/P} \right] (x_{B}, b_{0}/b_{\perp})$$

$$\times \exp \left\{ \int_{b_{0}^{2}/b_{\perp}^{2}}^{\hat{Q}^{2}} \frac{d\mu^{2}}{\mu^{2}} \left[ \ln \frac{\hat{Q}^{2}}{\mu^{2}} A(\alpha_{s}(\mu^{2})) + B(\alpha_{s}(\mu^{2})) \right] \right\}.$$
Landau Pole

• The integration over the impact parameter introduces a Landau pole

• Must specify a treatment of the Landau pole for any value of pT

# Landau-pole prescriptions

• Introduce cutoff for the large b region by evaluating at the point (Collins, Soper 1982)

$$b_* = \frac{b}{\sqrt{1 + \left(\frac{b}{b_{max}}\right)^2}}$$

• "Minimal prescription:" deform b-contour to avoid singularities (Catani, Mangano, Nason, Trentadue 1996; Laenen, Sterman, Vogelsang 2000)

$$b = \left[\cos\phi \pm i\sin\phi\right]t$$

# Matching to fixed-order

 Resummed exponent in bspace, fixed-order in p<sub>T</sub>
 space ⇒ leads to difficulties in matching



**EFT** Approach

# Effective Field Theory (EFT)

Low transverse momentum distribution has the scales

 $m_h \gg p_T \gg \Lambda_{QCD}$ 

• The most singular pT emissions are soft and collinear emissions ⇒Soft-Collinear Effective Theory (SCET) (Bauer, Fleming, Luke, Pirjol, Stewart)

• Study of SCET at the LHC, particularly for differential quantities, is still in its infancy

threshold resummation for inclusive Drell-Yan, Higgs, ttbar (Becher, Neubert et al.)
Factorization at the LHC for jet cross sections (Stewart, Tackmann, Waalewijn)

• Gain knowledge of how to apply SCET to hadronic collisions from this study

# EFT framework

 $QCD(n_f = 6) \rightarrow QCD(n_f = 5) \rightarrow SCET_{p_T} \rightarrow SCET_{\Lambda_{QCD}}$ 



Show derivation for Higgs, but identical for V=W, Z,  $\gamma^*$ 

# EFT framework

 $QCD(n_f = 6) \rightarrow QCD(n_f = 5) \rightarrow SCET_{p_T} \rightarrow SCET_{\Lambda_{QCD}}$ 





- All objects are field theoretically defined
- Large logarithms are summed via RG equations in EFTs
- Formulation avoids Landau pole

# SCET in a NutShell

• Effective theory with soft and collinear degrees of freedom:

 $p^{\mu} \equiv (p^{+}, p^{-}, p_{\perp})$  $p_{n} \sim m_{h}(\eta^{2}, 1, \eta), \quad p_{\bar{n}} \sim m_{h}(1, \eta^{2}, \eta), \quad p_{s} \sim m_{h}(\eta, \eta, \eta),$ 

• Well defined power counting:

 $\left(\eta \sim \frac{p_T}{m_h}\right) \longrightarrow$  Corresponds to soft and collinear modes with transverse momentum of order p<sub>T</sub>

• Soft and collinear fields are distinguished and are decoupled at leading order in  $\eta$ 

$$\langle \mathcal{O}_{\mathrm{SCET}} \rangle \rightarrow \langle \mathcal{O}_{coll.} \rangle \langle \mathcal{O}_{soft} \rangle$$

 Soft and Collinear gauge invariance restricts the form of SCET operators that can appear

# Soft-Collinear Decoupling

(Bauer, Fleming, Stewart, Pirjol)

• The SCET Lagrangian with a power counting scheme as:

$$\mathcal{L}_{SCET} = \mathcal{L}_{SCET}^{(0)} + \mathcal{L}_{SCET}^{(1)} + \mathcal{L}_{SCET}^{(2)} + \cdots$$

• At leading order the soft and collinear modes are decoupled:

 $\mathcal{L}_{SCET}^{(0)} = \mathcal{L}_{ ext{coll}}^{(0)} + \mathcal{L}_{ ext{soft}}^{(0)}$ 

 $p_{hc} \sim p_c + p_s \sim Q(\eta^2, 1, \eta) + Q(\eta, \eta, \eta) \sim Q(\eta, 1, \eta)$ 

$$p_{hc}^2 \sim Q^2 \eta \gg p_c^2, p_s^2$$

 $\mathbf{O}$ 

# Matching onto SCET

#### • Matching equation: $O_{QCD} = \int d\omega_1 \int d\omega_2 C(\omega_1, \omega_2) \mathcal{O}(\omega_1, \omega_2)$



Tree level matching (EFT graphs scale-less in dim-reg ⇒ finite part of virtual corrections)

Soft and collinear emissions build into Wilson lines determined by soft and collinear gauge invariance



#### Effective SCET

operator:

 $\mathcal{O}(\omega_1,\omega_2) = g_{\mu\nu}h T\{ \operatorname{Tr}\left[S_n(gB^{\mu}_{n\perp})_{\omega_1}S^{\dagger}_nS_{\bar{n}}(gB^{\nu}_{\bar{n}\perp})_{\omega_2}S^{\dagger}_{\bar{n}}\right] \}$ 



# SCET Cross-Section

#### • SCET differential cross-section:

 $\frac{d^2\sigma}{du\,dt} = \frac{1}{2Q^2} \left[\frac{1}{4}\right] \int \frac{d^2p_{h\perp}}{(2\pi)^2} \int \frac{dn \cdot p_h d\bar{n} \cdot p_h}{2(2\pi)^2} (2\pi)\theta(n \cdot p_h + \bar{n} \cdot p_h)\delta(n \cdot p_h \bar{n} \cdot p_h - \vec{p}_{h\perp}^2 - m_h^2)$   $\times \delta(u - (p_2 - p_h)^2)\delta(t - (p_1 - p_h)^2) \sum_{\text{initial pols. } X} \sum_X |C(\omega_1, \omega_2) \otimes \langle hX_n X_{\bar{n}} X_s | \mathcal{O}(\omega_1, \omega_2) | pp \rangle \right|^2$ 

× 
$$(2\pi)^4 \delta^{(4)}(p_1 + p_2 - P_{X_n} - P_{X_{\bar{n}}} - P_{X_s} - p_h),$$



 $\frac{d^2\sigma}{dp_T^2 dY} \sim \int PS |C \otimes \langle \mathcal{O} \rangle|^2$ 

Phase space integrals.

Hard matching coefficient. SCET matrix element.

Factorize using soft-collinear decoupling

- We are here

 $(\text{QCD} (n_f = 5))$ 

SCET<sub>p7</sub>

iSF

iBF

PDF

iBF

PDF

 $\frac{d^2\sigma}{dp_T^2 dY} \sim \int PS |C \otimes \langle \mathcal{O} \rangle|^2$ 

Factorize cross-section using soft-collinear decoupling in SCET

 $\frac{d^2\sigma}{dp_T^2 dY}$  $\otimes B_n \otimes B_{\bar{n}} \otimes S$ 

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Hard matching coefficient squared

Decoupled collinear and soft functions

We are here

 $\left( \text{QCD} \left( n_f = 5 \right) \right)$ 

 $\text{SCET}_{p_T}$ 

iSF

iBF

(PDF)

iBF

PDF

 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes B_n \otimes B_{\bar{n}} \otimes S$ 

Hard function

Impact-parameter Beam Functions (iBFs) Soft function

Physics of hard scale. Sums logs of mh/pT. Describes collinear pT emissions

Describes soft pT emissions



$$J_{n}^{\alpha\beta}(\omega_{1},x^{-},x_{\perp},\mu) = \sum_{\text{initial pols.}} \langle p_{1} | \left[ gB_{1n\perp\beta}^{A}(x^{-},x_{\perp})\delta(\bar{\mathcal{P}}-\omega_{1})gB_{1n\perp\alpha}^{A}(0) \right] | p_{1} \rangle$$

$$J_{\bar{n}}^{\alpha\beta}(\omega_{1},y^{+},y_{\perp},\mu) = \sum_{\text{initial pols.}} \langle p_{2} | \left[ gB_{1n\perp\beta}^{A}(y^{+},y_{\perp})\delta(\bar{\mathcal{P}}-\omega_{2})gB_{1n\perp\alpha}^{A}(0) \right] | p_{2} \rangle$$

$$S(z,\mu) = \langle 0 | \bar{T} \left[ \text{Tr} \left( S_{\bar{n}}T^{D}S_{\bar{n}}^{\dagger}S_{n}T^{C}S_{n}^{\dagger} \right)(z) \right] T \left[ \text{Tr} \left( S_{n}T^{C}S_{n}^{\dagger}S_{\bar{n}}T^{D}S_{\bar{n}}^{\dagger} \right)(0) \right] | 0 \rangle$$

We are here

 $\left( \text{QCD} \left( n_f = 5 \right) \right)$ 

 $SCET_{p_7}$ 

iSF

iBF

 $(_{PDF})$ 

iBF

PDF

 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes B_n \otimes B_{\bar{n}} \otimes S$ 

iBFs are proton matrix elements and sensitive to the non-perturbative scale

• The iBFs are matched onto PDFs to separate the perturbative and non-perturbative scales:

$$B_n = \mathcal{I}_{n,i} \otimes f_i$$

$$f_n = f_n \otimes f_n$$

coefficient

$$B_{\bar{n}} = \mathcal{I}_{\bar{n},i} \otimes f_i$$

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 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes B_n \otimes B_{\bar{n}} \otimes S$ 

• After matching the iBFs to the PDFs we get:

 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes [\mathcal{I}_{n,i} \otimes f_i] \otimes [\mathcal{I}_{\bar{n},j} \otimes f_j] \otimes S$ 

• Group the perturbative pT scale functions into transverse momentum dependent function:



• Factorization formula in full detail:

$$\frac{d^2\sigma}{dp_T^2 dY} = \frac{\pi^2}{4(N_c^2 - 1)^2 Q^2} \int_0^1 \frac{dx_1}{x_1} \int_0^1 \frac{dx_2}{x_2} \int_{x_1}^1 \frac{dx'_1}{x'_1} \int_{x_2}^1 \frac{dx'_2}{x'_2} \times \frac{H(x_1, x_2, \mu_Q; \mu_T) \mathcal{G}^{ij}(x_1, x'_1, x_2, x'_2, p_T, Y, \mu_T) f_{i/P}(x'_1, \mu_T) f_{j/P}(x'_2, \mu_T)}{\prod_{\substack{\text{Hard function}}} \prod_{\substack{\text{Transverse momentum} \\ \text{function}}} PDF_s$$
• The transverse momentum function is a convolution of the iBF matching coefficients and the soft function:

$$\begin{aligned} \mathcal{G}^{ij}(x_1, x_1', x_2, x_2', p_T, Y, \mu_T) &= \int dt_n^+ \int dt_{\bar{n}}^- \int \frac{d^2 b_\perp}{(2\pi)^2} J_0(|\vec{b}_\perp|p_T) \\ &\times \mathcal{I}^{\beta\alpha}_{n;g,i}(\frac{x_1}{x_1'}, t_n^+, b_\perp, \mu_T) \mathcal{I}^{\beta\alpha}_{\bar{n};g,j}(\frac{x_2}{x_2'}, t_{\bar{n}}^-, b_\perp, \mu_T) \\ &\times \mathcal{S}^{-1}(x_1 Q - e^Y \sqrt{p_T^2 + m_h^2} - \frac{t_{\bar{n}}^-}{Q}, x_2 Q - e^{-Y} \sqrt{p_T^2 + m_h^2} - \frac{t_n^+}{Q}, b_\perp, \mu_T) \end{aligned}$$

• Factorization formula in full detail:

 $\frac{d^{2}\sigma}{dp_{T}^{2} dY} = \frac{\pi^{2}}{4(N_{c}^{2}-1)^{2}Q^{2}} \int_{0}^{1} \frac{dx_{1}}{x_{1}} \int_{0}^{1} \frac{dx_{2}}{x_{2}} \int_{x_{1}}^{1} \frac{dx'_{1}}{x'_{1}} \int_{x_{2}}^{1} \frac{dx'_{2}}{x'_{2}} \times H(x_{1}, x_{2}, \mu_{Q}, \mu_{T}) \mathcal{G}^{ij}(x_{1}, x'_{1}, x_{2}, x'_{2}, p_{T}, Y, \mu_{T}) f_{i/P}(x'_{1}, \mu_{T}) f_{j/P}(x'_{2}, \mu_{T})$ 

RG evolution cut off at  $\mu_T \sim p_T$ , the matching scale from QCD  $\rightarrow$  SCET<sub>pT</sub>, not 1/b<sub>1</sub>

Impact parameter appears, but only to simplify iBF→PDF matching; can transform this formula to be completely in momentum space

$$\begin{aligned} \mathcal{G}^{ij}(x_1, x_1', x_2, x_2', p_T, Y, \mu_T) &= \int dt_n^+ \int dt_{\bar{n}}^- \int \underbrace{\frac{d^2 b_\perp}{(2\pi)^2}}_{(2\pi)^2} J_0(|\vec{b}_\perp|p_T) \\ &\times \mathcal{I}^{\beta\alpha}_{n;g,i}(\frac{x_1}{x_1'}, t_n^+, b_\perp, \mu_T) \mathcal{I}^{\beta\alpha}_{\bar{n};g,j}(\frac{x_2}{x_2'}, t_{\bar{n}}^-, b_\perp, \mu_T) \\ &\times \mathcal{S}^{-1}(x_1 Q - e^Y \sqrt{p_T^2 + m_h^2} - \frac{t_{\bar{n}}^-}{Q}, x_2 Q - e^{-Y} \sqrt{p_T^2 + m_h^2} - \frac{t_n^+}{Q}, b_\perp, \mu_T) \end{aligned}$$

Impact parameter appears, but only to simplify iBF→PDF matching; can transform this formula to be completely in momentum space

$$\mathcal{G}^{ij}(x_{1}, x_{1}', x_{2}, x_{2}', p_{T}, Y, \mu_{T}) = \frac{1}{2\pi} \int dt_{n}^{+} \int dt_{\bar{n}}^{-} \int d^{2}k_{n}^{\perp} \int d^{2}k_{\bar{n}}^{\perp} \int d^{2}k_{us}^{\perp} \frac{\delta(p_{T} - |\vec{k}_{n}^{\perp} + \vec{k}_{\bar{n}}^{\perp} + \vec{k}_{us}^{\perp}|)}{p_{T}} \\
\times \mathcal{I}_{n;g,i}^{\beta\alpha}(\frac{x_{1}}{x_{1}'}, t_{n}^{+}, k_{n}^{\perp}, \mu_{T}) \mathcal{I}_{\bar{n};g,j}^{\beta\alpha}(\frac{x_{2}}{x_{2}'}, t_{\bar{n}}^{-}, k_{\bar{n}}^{\perp}, \mu_{T}) \\
\times \mathcal{S}^{-1}(x_{1}Q - e^{Y}\sqrt{p_{T}^{2} + m_{h}^{2}} - \frac{t_{\bar{n}}^{-}}{Q}, x_{2}Q - e^{-Y}\sqrt{p_{T}^{2} + m_{h}^{2}} - \frac{t_{n}^{+}}{Q}, k_{us}^{\perp}, \mu_{T}) \\$$
(54)

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# Fixed order and Matching Calculations

# One loop Matching onto SCET



One loop SCET graphs

All graphs scaleless and vanish in dimensional regularization.

• Wilson Coefficient obtained from finite part in dimensional regularization of the QCD result for  $gg \rightarrow h$ . At one loop we have:

$$C(\bar{n}\cdot\hat{p}_{1}n\cdot\hat{p}_{2},\mu) = \frac{c\,\bar{n}\cdot\hat{p}_{1}n\cdot\hat{p}_{2}}{v}\left\{1 + \frac{\alpha_{s}}{4\pi}C_{A}\left[\frac{11}{2} + \frac{\pi^{2}}{6} - \ln^{2}\left(-\frac{\bar{n}\cdot\hat{p}_{1}n\cdot\hat{p}_{2}}{\mu^{2}}\right)\right]\right\}$$

## iBFs





 $\tilde{B}_{n}^{\alpha\beta}(x_{1},t_{n}^{+},b_{\perp},\mu) = \int \frac{db^{-}}{4\pi} e^{\frac{i}{2}\frac{t_{n}^{+}b^{-}}{Q}} \sum_{\text{initial pols. } X_{n}} \sum_{X_{n}} \langle p_{1} | [gB_{1n\perp\beta}^{A}(b^{-},b_{\perp})|X_{n} \rangle \\
\times \langle X_{n} | \delta(\bar{\mathcal{P}}-x_{1}\bar{n}\cdot p_{1})gB_{1n\perp\alpha}^{A}(0)] | p_{1} \rangle,$ 



## Soft function



• Soft function definition:

#### $S(z) = \langle 0 | \operatorname{Tr} \left( \bar{T} \{ S_{\bar{n}} T^D S_{\bar{n}}^{\dagger} S_n T^C S_n^{\dagger} \} \right) (z) \operatorname{Tr} \left( T \{ S_n T^C S_n^{\dagger} S_{\bar{n}} T^D S_{\bar{n}}^{\dagger} \} \right) (0) | 0 \rangle$







• Factorization formula:

 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes \mathcal{G}^{ij} \otimes f_i \otimes f_j$ 

• Schematic picture of running:



**4**I

# Running

• Factorization formula:

 $\frac{d^2\sigma}{dp_T^2 dY} \sim H \otimes \mathcal{G}^{ij} \otimes f_i \otimes f_j$ 

$$H = |C(\mu_Q, Q)|^2 \exp\left\{\int_{\mu_T}^{\mu_Q} \frac{d\mu}{\mu} \Gamma_c \left[\alpha_s(\mu)\right] \ln\left(\frac{Q^2}{\mu^2}\right) + \gamma \left[\alpha_s(\mu)\right]\right\}$$

$$\Gamma_{c} [\alpha_{s}] = A_{CSS},$$
  

$$\gamma^{(1)} = B^{(1)}_{CSS},$$
  

$$\gamma^{(2)} = B^{(2)}_{CSS} + \text{pieces from C, } \mathcal{G}$$

# Limit of very small pT

• We derived a factorization formula in the limit:

#### $m_h \gg p_T \gg \Lambda_{QCD}$

• For smaller values of pT, one can introduce a nonperturbative model for the transverse momentum function: field theoretically defined, running known

- In the limit p<sub>T</sub>=0, m<sub>h</sub>→∞, dσ/dp<sub>T</sub><sup>2</sup>→constant Parisi, Petronzio
  Dominated by back-to-back hard jets⇒in SCET, this is a power-suppressed operator
- Leading term Sudakov suppressed in this limit
- Working to understand this in SCET...

# Higgs at the LHC

Matching accomplished just by subtracting expanded exponent from fixed order



# Tevatron Z production



Missing 2-loop iBF, soft functions needed for full NNLL+NLO 45

## Conclusions

• Derived factorization formula for the Higgs transverse momentum distribution in an EFT approach:



• Resummation via RG equations in EFTs

• Formulation is free of Landau poles; easy matching to fixed-order

• Next steps: higher-order calculations of iBF, iSF to enable NNLL+NLO result, modeling of low p<sub>T</sub>