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on behalf of the Gfitter group (\*)

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<http://cern.ch/Gfitter>

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## The global electroweak fit and constraints on new physics with Gfitter

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## A **G**eneric **F**itter Project for HEP Model Testing

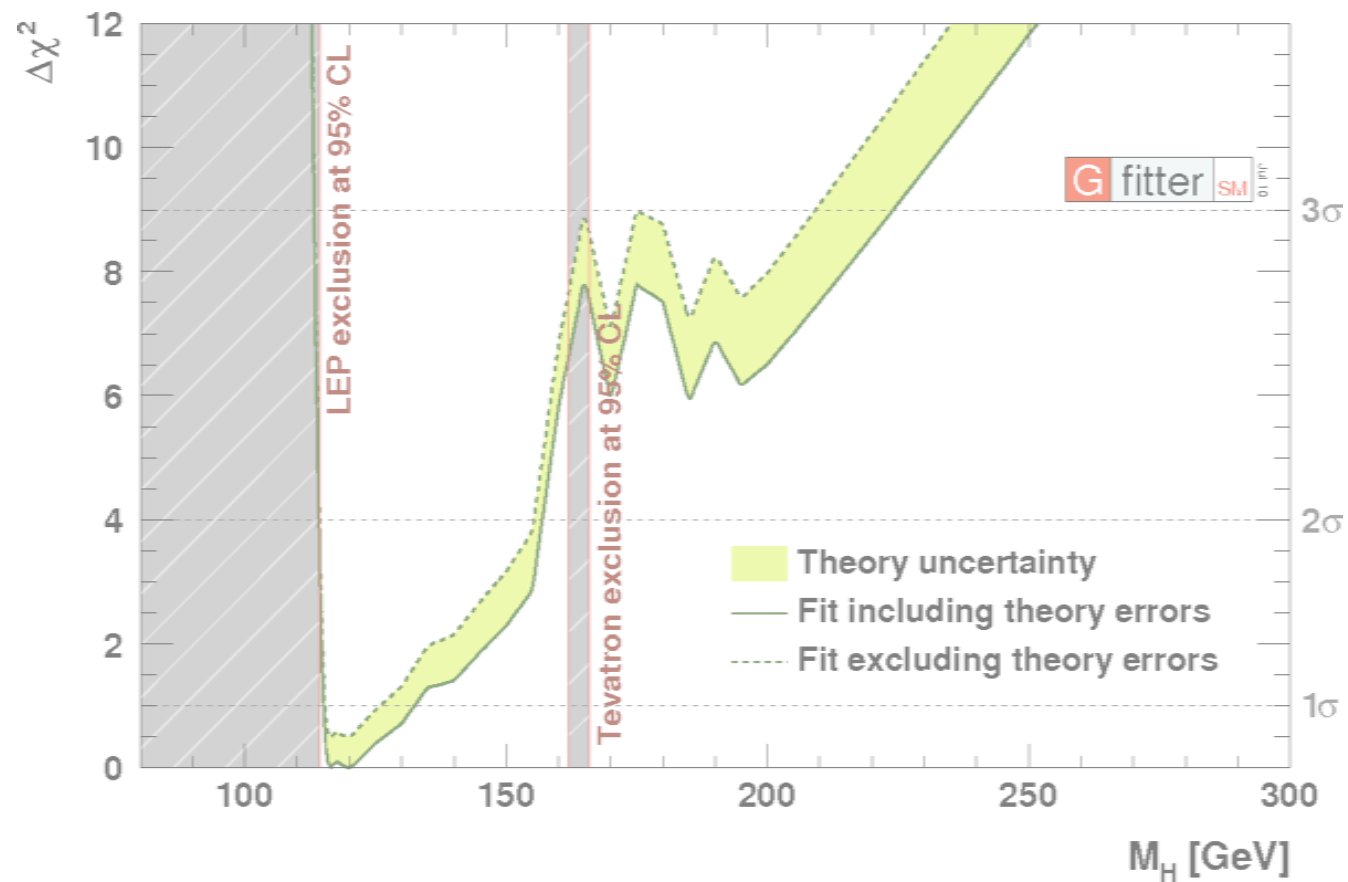
- Introduction to the Gfitter program
- Global electroweak fit of the Standard Model
- Oblique parameters
- Constraints on various BSM models
- Two-Higgs-Doublet Model
- Conclusion / Prospects



A **G**eneric **F**itter Project  
for HEP Model Testing

- **Gfitter = state-of-the-art model testing tool for LHC era**
- **Gfitter software**
  - Modular, object-oriented C++, relying on ROOT, XML, python
  - Core package with data-handling, fitting, and statistics tools
  - Independent “plug-in” physics libraries: SM, 2HDM, oblique parameters, SUSY, ...
- **Gfitter features**
  - Various fitting tools: Minuit (1/2), Genetic Algorithms, Simulated Annealing, etc.
  - Full statistics analysis: goodness-of-fit, p-values, parameter scans, MC analyses.
  - Consistent treatment of statistical, systematic, theoretical uncertainties (Rfit prescription), correlations, and inter-parameter dependencies.
    - Theoretical uncertainties included in  $\chi^2$  with flat likelihood in allowed ranges
- **Main publication: [EPJ C60, 543-583,2009 \[arXiv:0811.0009\]](#)**
  - Also available at: [www.cern.ch/Gfitter](http://www.cern.ch/Gfitter)
  - **Today: updates and new results**

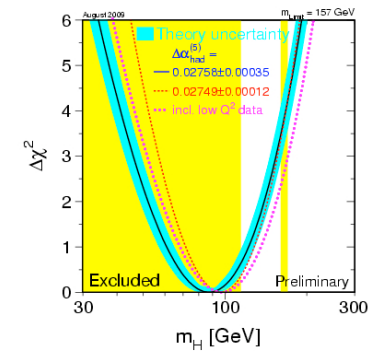
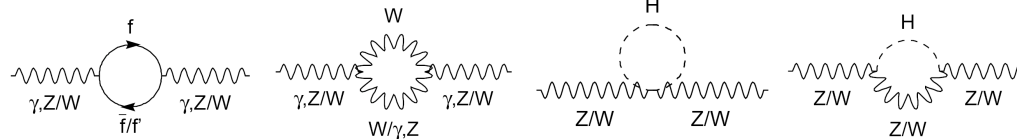
# The global electroweak fit of the SM



# The global electroweak fit with Gfitter



- A Gfitter package for the global EW fit of the SM
  - Complete reimplemention of SM predictions of EW precision observables
  - Based on huge amount of preparatory work by many people
  - Radiative corrections are important
    - Logarithmic dependence on  $M_H$  through virtual corrections



- State-of-the art calculations; in particular:
  - **Radiator functions**: N<sup>3</sup>LO of the massless QCD Adler function, used for Z and W hadronic decay widths  
[P.A. Baikov et al., Phys. Rev. Lett. 101 (2008) 012022]
  - $M_W$  and  $\sin^2\theta_{\text{eff}}^f$ : full two-loop + leading beyond-two-loop correction  
[M. Awramik et al., Phys. Rev D69, 053006 (2004) and ref.][M. Awramik et al., Nucl.Phys.B813:174-187 (2009) and refs.]
    - theoretical uncertainties:  $M_W$  ( $\delta M_W=4-6\text{MeV}$ ),  $\sin^2\theta_{\text{eff}}^f$  ( $\delta\sin^2\theta_{\text{eff}}^f=4.7\cdot 10^{-5}$ )

■ Wherever possible, calculations cross-checked against ZFITTER  
→ excellent agreement

# Electroweak Fit – Latest Experimental Input



- Z-pole observables: results from LEP / SLC  
[ADLO+SLD, Phys. Rept. 427, 257 (2006)]
- $M_W$  and  $\Gamma_W$  from LEP/Tevatron [ADLO,CFD+D0: arXiv:0908.1374v1]
- $m_{\text{top}}$  latest Tevatron average [CDF&D0: new combination ICHEP'10]
- $\overline{m}_c$ ,  $\overline{m}_b$  world averages [PDG, J. Phys. G33,1 (2006)]
- $\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$  including  $\alpha_S$  dependency  
[Hagiwara et al., PLB649,173,'07]
- Direct Higgs searches from LEP/Tevatron  
[ADLO: Phys. Lett. B565, 61 (2003)], [CDF+D0: arXiv:0911.3930]
  - LEP: Higgs strahlung ( $ee \rightarrow ZH$ ,  $H \rightarrow bb, \tau\tau$ )
  - Tevatron: gg fusion w/  $H \rightarrow WW$ , ass. prod., VBF
  - Stat. interpretation in global fit: 2-sided  $CL_{S+B}$

$M_Z$ [GeV]	$91.1875 \pm 0.0021$	LEP
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	LEP
$R_\ell^0$	$20.767 \pm 0.025$	
$A_{\text{FB}}^{0,\ell}$	$0.0171 \pm 0.0010$	SLC
$A_\ell^{(*)}$	$0.1499 \pm 0.0018$	
$A_c$	$0.670 \pm 0.027$	SLC
$A_b$	$0.923 \pm 0.020$	
$A_{\text{FB}}^{0,c}$	$0.0707 \pm 0.0035$	LEP
$A_{\text{FB}}^{0,b}$	$0.0992 \pm 0.0016$	
$R_c^0$	$0.1721 \pm 0.0030$	SLC
$R_b^0$	$0.21629 \pm 0.00066$	
$\sin^2\theta_{\text{eff}}^\ell(Q_{\text{FB}})$	$0.2324 \pm 0.0012$	

$M_H$ [GeV] <sup>(o)</sup>	Likelihood ratios
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$M_W$ [GeV]	$80.399 \pm 0.023$
$\Gamma_W$ [GeV]	$2.098 \pm 0.048$

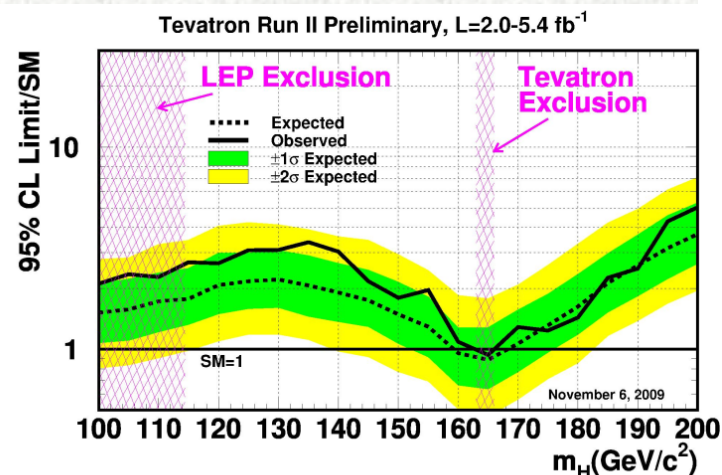
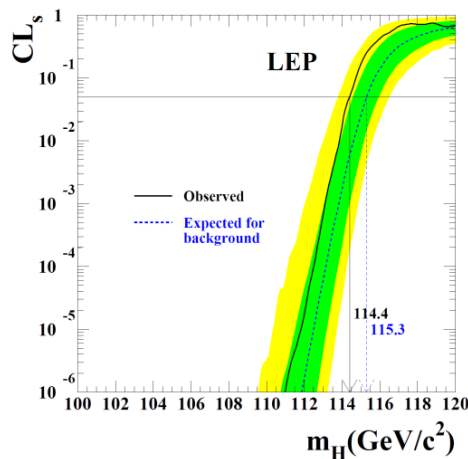
$\overline{m}_c$ [GeV]	$1.27^{+0.07}_{-0.11}$
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$\overline{m}_b$ [GeV]	$4.20^{+0.17}_{-0.07}$
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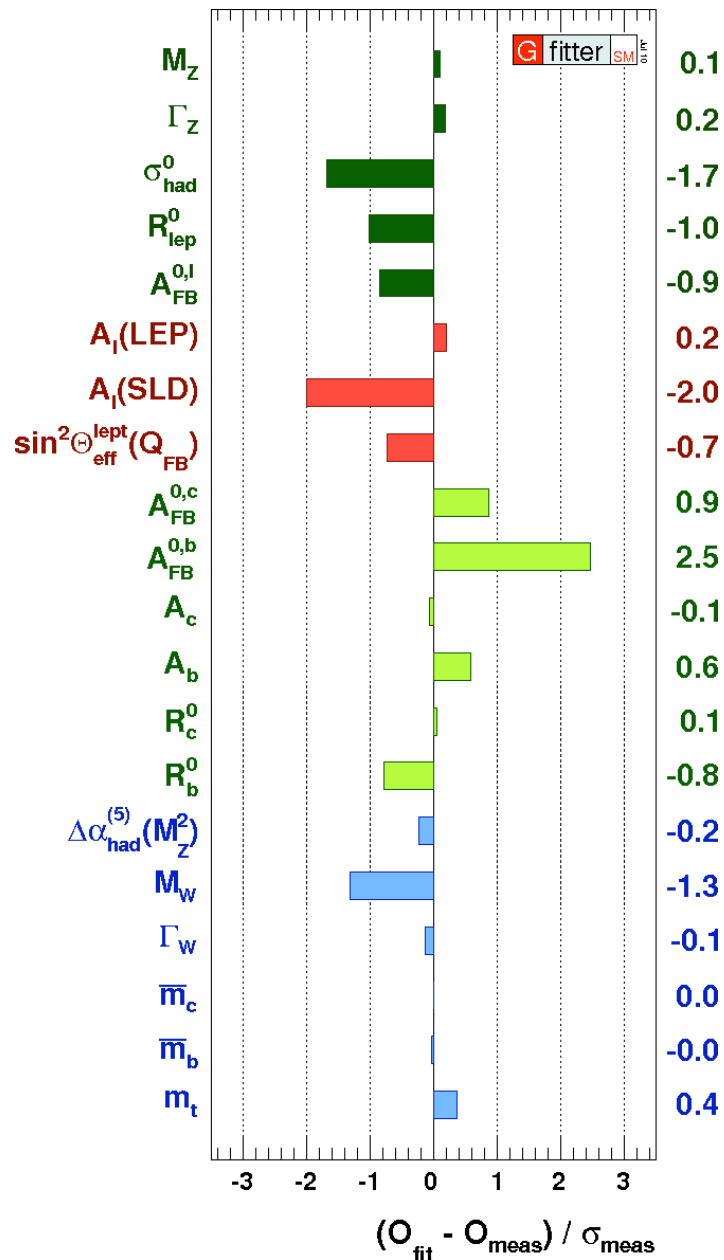
$m_t$ [GeV]	$173.3 \pm 1.1$
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$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ ( $\dagger\Delta$ )	$2769 \pm 22$
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$\alpha_s(M_Z^2)$	–
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# The Electroweak Fit I – SM Fit Results



- Floating fit parameters

- $M_Z, \Delta\alpha_{had}^{(5)}(M_Z^2), \alpha_S(M_Z^2), \bar{m}_c, \bar{m}_b, m_t, M_H$

- Pull values of complete fit

- No individual value exceeds  $3\sigma$
- FB asymmetry of bottom quarks  $\rightarrow$  largest contribution to  $\chi^2$
- Small contributions from  $M_Z, \Delta\alpha_{had}^{(5)}(M_Z^2), \bar{m}_c, \bar{m}_b$ : input accuracies exceed fit requirements

- Goodness of fit – naïve p-value:

- Excl. direct Higgs searches:  $\chi^2_{min}=16.4$   
 $\rightarrow \text{Prob}(\chi^2_{min}, 13) = 0.23$
- Incl. direct Higgs searches:  $\chi^2_{min}=17.8$   
 $\rightarrow \text{Prob}(\chi^2_{min}, 14) = 0.22$

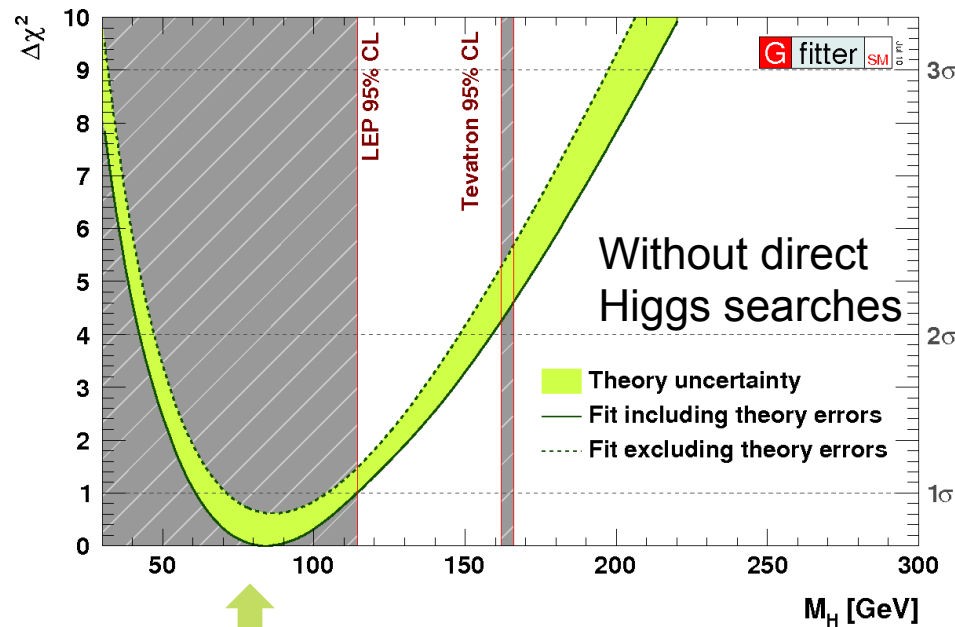
- No indication for new physics

# The Electroweak Fit II – Higgs Mass Constraints



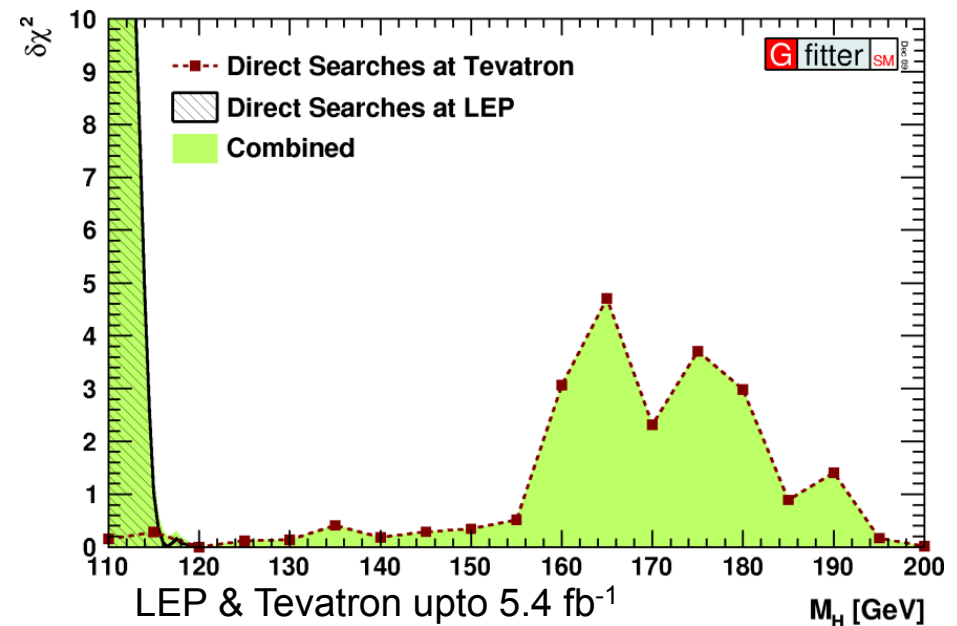
- $M_H$  from fit including all data except results from direct Higgs searches at LEP, Tevatron:

- Central value  $\pm 1\sigma$ :  $M_H = 80^{+30}_{-23}$  GeV
- $2\sigma$  interval: [42, 159] GeV



- $M_H$  from fit including results from direct Higgs searches at LEP, Tevatron:

- Resulting contributions added to  $\chi^2$  during fit
- Stat. interpretation: 2-sided  $CL_{S+B}$



- green** error band from including / excluding theoretical errors in fit
- Theoretical errors included in  $\chi^2$  with “flat likelihood term”



# The Electroweak Fit II – Higgs Mass Constraints

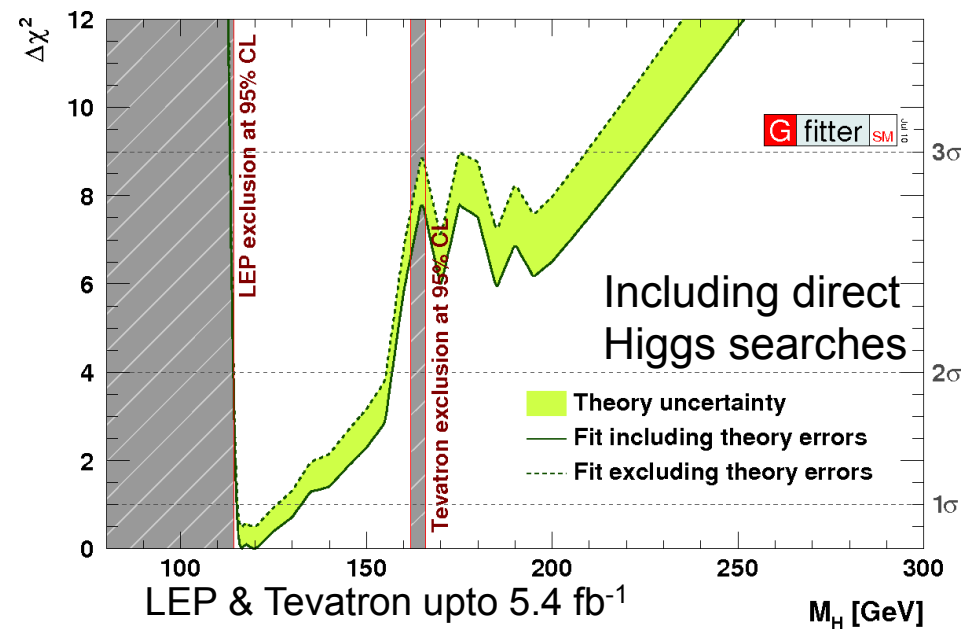
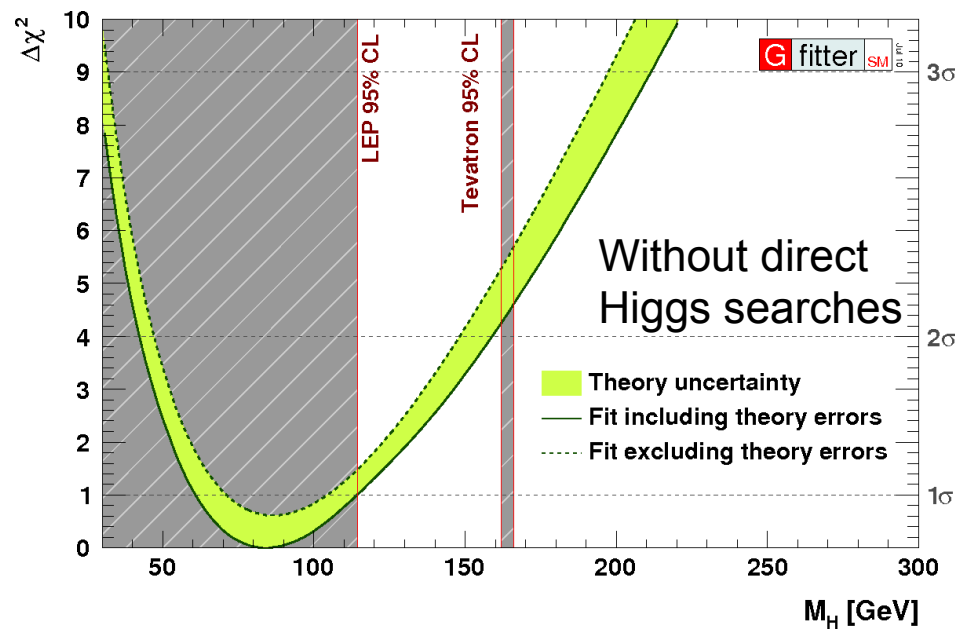


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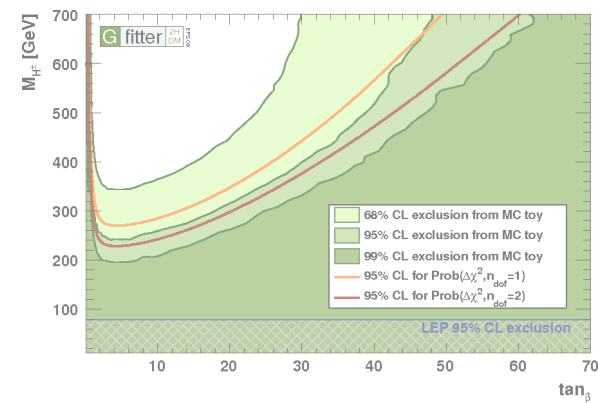
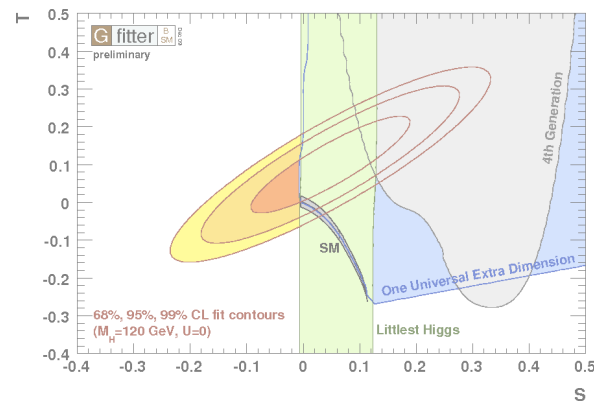
- $M_H$  from fit including results from direct Higgs searches at LEP, Tevatron:

- Central value  $\pm 1\sigma$ :  $M_H = 119.1^{+13.5}_{-4.0}$  GeV
- $2\sigma$  interval: [114, 157] GeV



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- Theoretical errors included in  $\chi^2$  with “flat likelihood term”

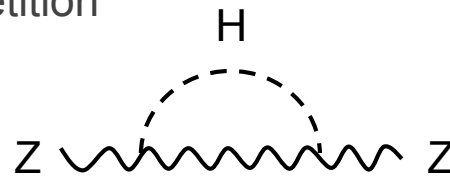
# Constraints on New Physics Models



# A Gfitter package for Oblique Corrections



- At low energies, BSM physics appears dominantly through vacuum polarization corrections
  - Aka, [oblique corrections](#)
- Oblique corrections reabsorbed into electroweak parameters
  - $\Delta\rho$ ,  $\Delta\kappa$ ,  $\Delta r$  parameters, appearing in:  $M_W^2$ ,  $\sin^2\theta_{\text{eff}}$ ,  $G_F$ ,  $\alpha$ , etc
- Electroweak fit sensitive to BSM physics through oblique corrections
  - In direct competition with sensitivity to Higgs loop corrections



- Oblique corrections from New Physics described through [STU parametrization](#) [Peskin and Takeuchi, Phys. Rev. D46, 1 (1991)]

$$O_{\text{meas}} = O_{\text{SM,REF}}(m_H, m_t) + c_S S + c_T T + c_U U$$

- S : New Physics contributions to neutral currents
  - T : Difference between neutral and charged current processes – sensitive to weak isospin violation
  - U : (+S) New Physics contributions to charged currents. U only sensitive to W mass and width, usually very small in NP models (often: U=0)
- Also implemented: correction to  $Z \rightarrow b\bar{b}$  coupling, extended parameters (VWX) [Burgess et al., Phys. Lett. B326, 276 (1994)] [Burgess et al., Phys. Rev. D49, 6115 (1994)]

# Fit to Oblique Parameters



- S,T,U obtained from fit to EW observables
  - $SM_{ref}$  chosen at:  $M_H = 120$  GeV and  $m_t = 173.1$  GeV
  - This defines  $(S,T,U) = (0,0,0)$

## Results for STU:

$$S = 0.02 \pm 0.11$$

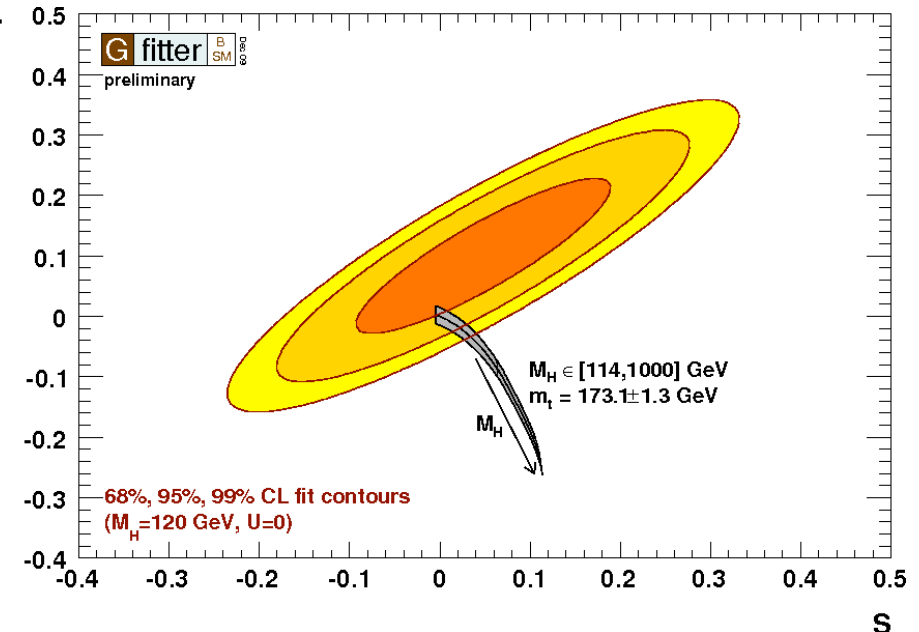
$$T = 0.05 \pm 0.12$$

$$U = 0.07 \pm 0.12$$

	S	T	U
S	1	0.879	-0.469
T		1	-0.716
U			1

- S, T: logarithmically dependent on  $M_H$
- Grey area: SM prediction
- Comparison of EW data w/ SM prediction:
  - Preference for small  $M_H$
  - No indication for new physics

ST-plane for  $U=0$



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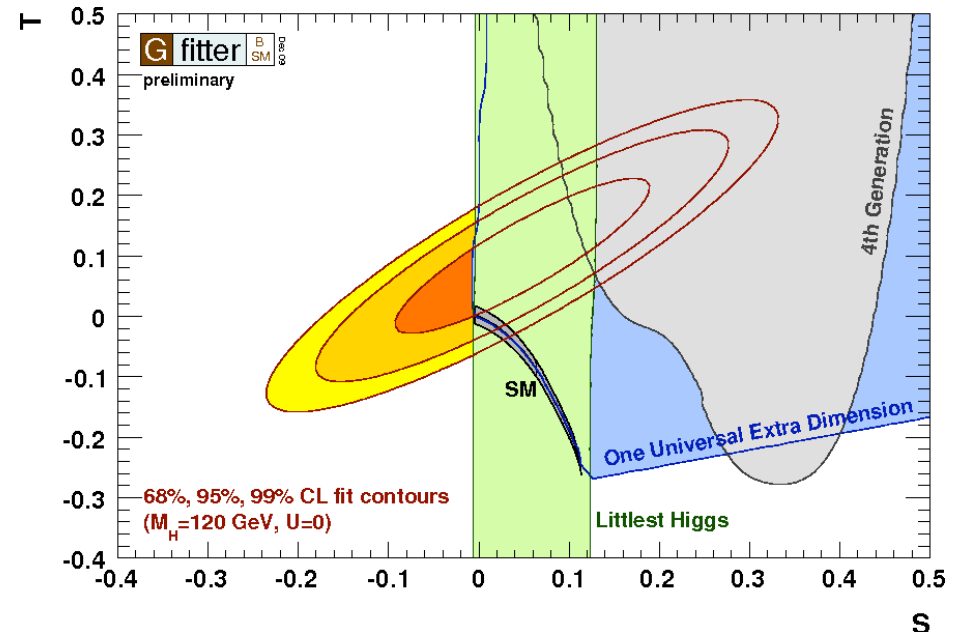
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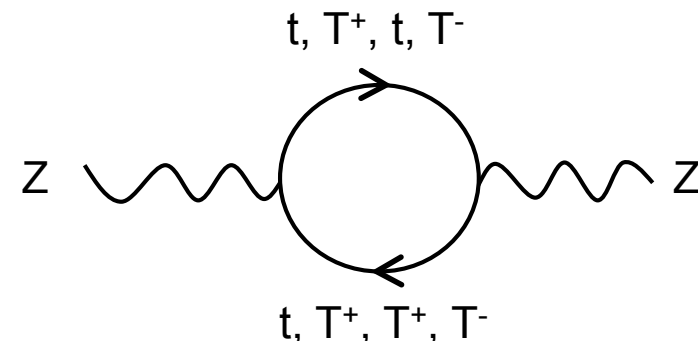
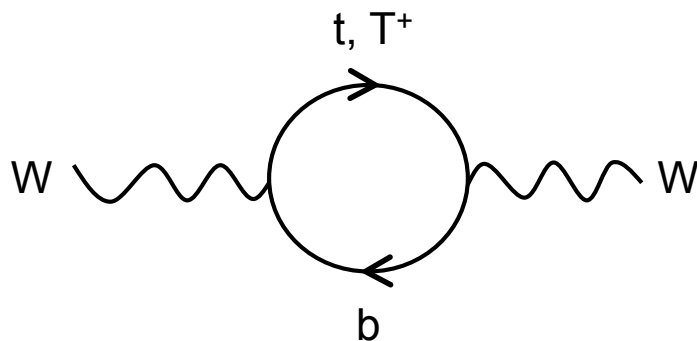
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- S, T: logarithmically dependent on  $M_H$
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- Comparison of EW data w/ SM prediction:
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- Many new physics models also compatible with the EW data:
  - Variation of model parameters often allows for large area in ST-plane.
  - Tested: UED, 4<sup>th</sup> fermion generation, Littlest Higgs, SUSY, etc.

- LHM: solves hierarchy problem, possible explanation for EWSM
  - SM contributions to Higgs mass cancelled by new particles
- Non-linear sigma model, broken Global SU(5)/SO(5) symmetry
  - Higgs = lightest pseudo-Nambu-Goldstone boson
  - New SM-like fermions and gauge bosons at TeV scale
- T-parity = symmetry like susy R-parity (not time-invariance)
  - Symmetry forbids direct couplings of new gauge bosons (T-odd) to SM particles (T-even)
  - LHM provides natural dark matter candidate
- Two new top states: T-even  $m_{T^+}$  and T-odd  $m_{T^-}$
- Dominant oblique corrections from weak isospin violation:

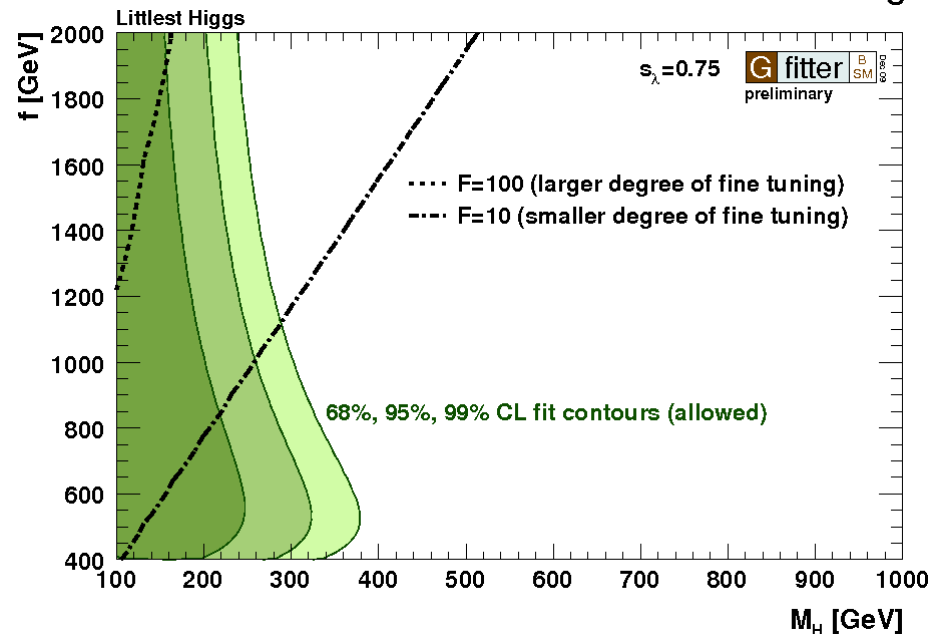
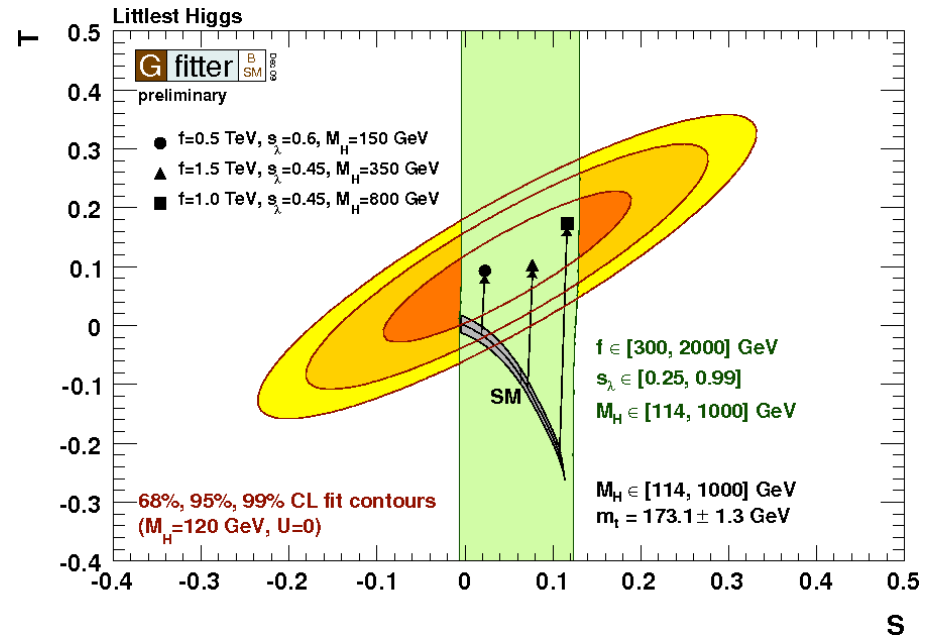


# Littlest Higgs with T-Parity



- STU predictions (oblique corrections) inserted for Littlest Higgs model  
[Hubisz et al., JHEP 0601:135 (2006)]
- Parameters of LH model
  - $f$ : symmetry breaking scale (scale of new particles)
  - $s_\lambda \equiv m_{T^-} / m_{T^+}$ : ratio of T-odd/-even masses in top sector
  - Order one-coefficient  $\delta_c$  (value depends on detail of UV physics)
    - Treated as theory uncertainty in fit (Rfit) :  $\delta_c = [-5, 5]$
- $F$ : degree of fine-tuning

■ LH model prefers large Higgs mass, with only small degree of fine-tuning

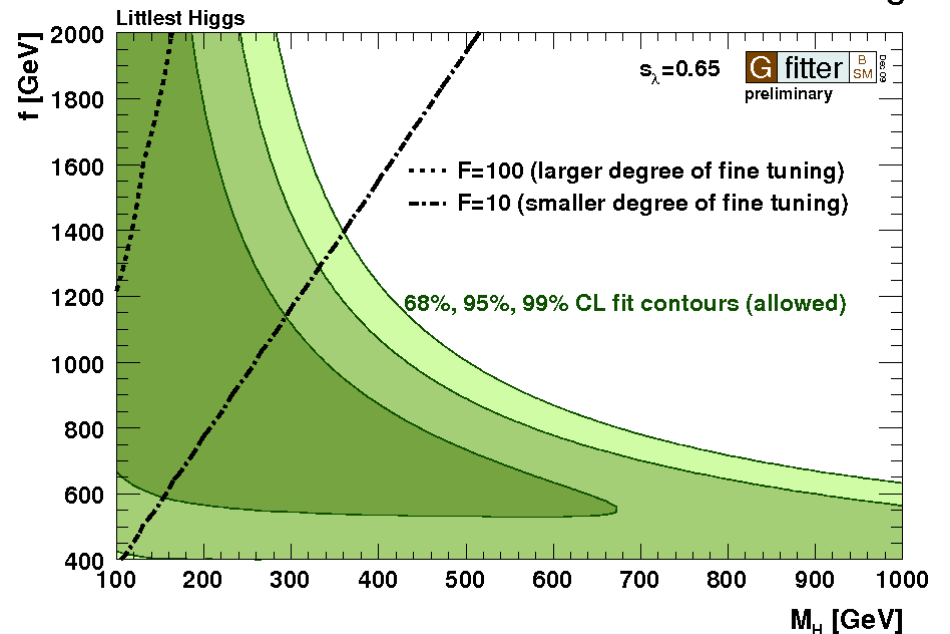
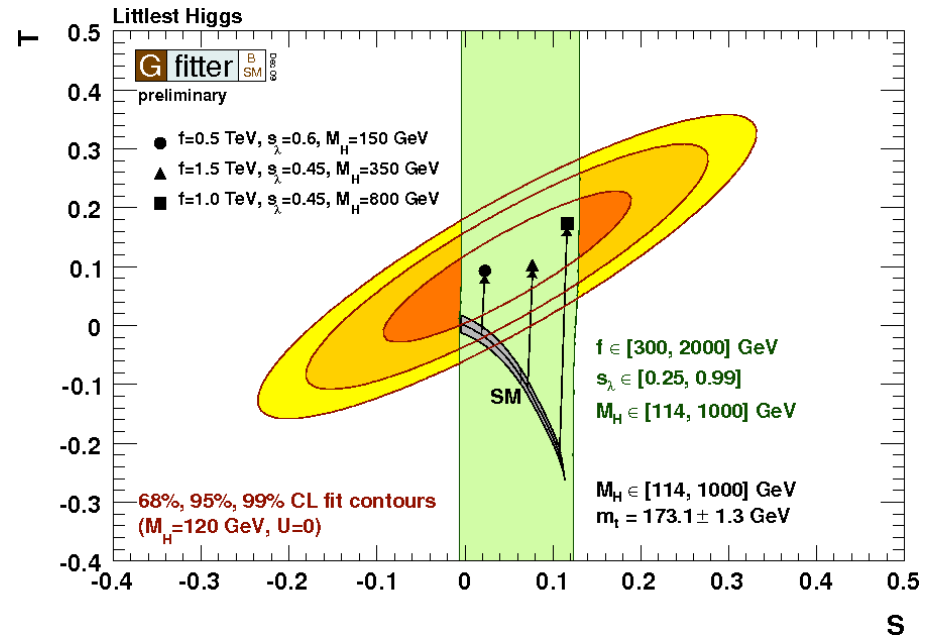


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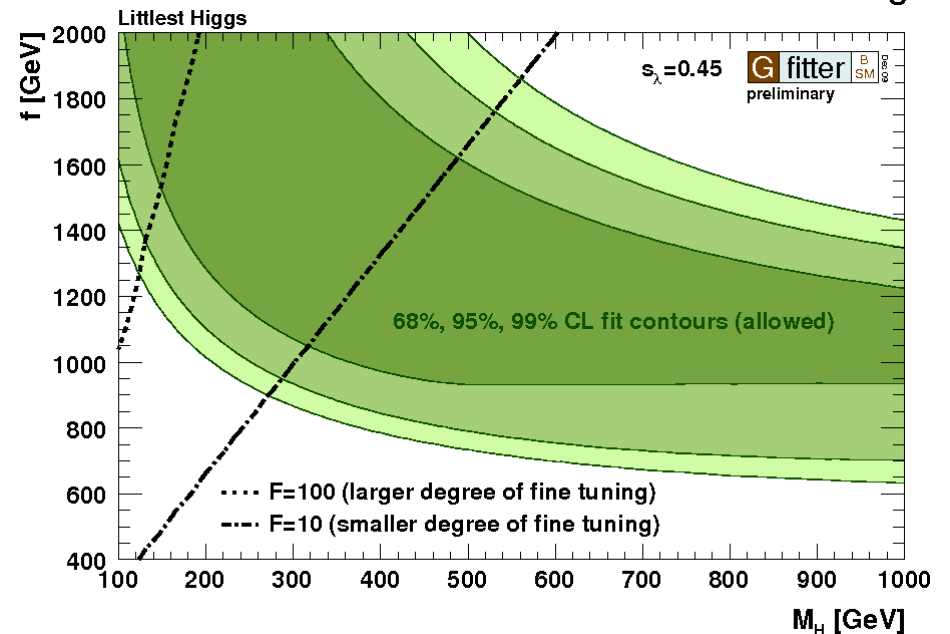
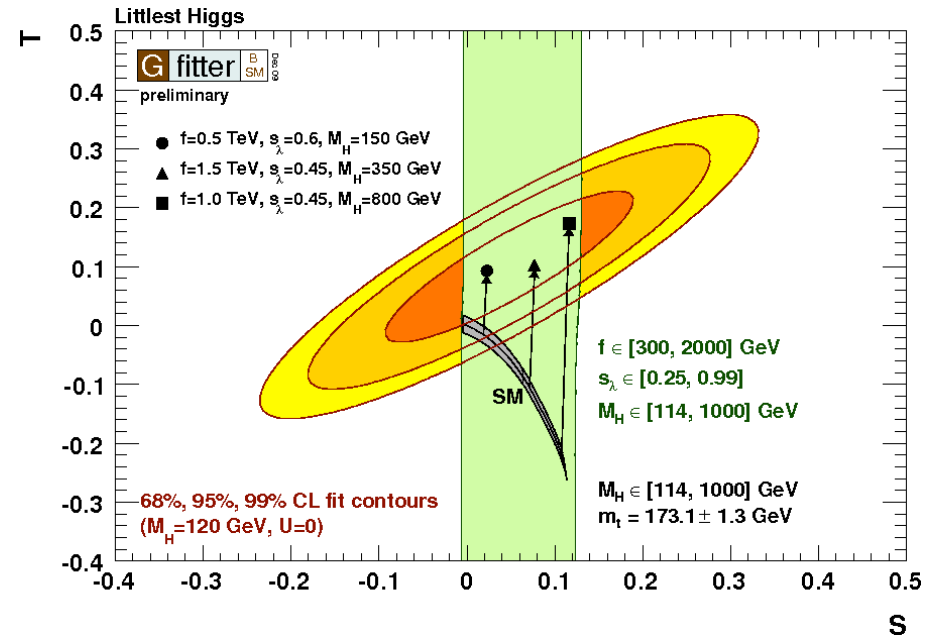




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[Appelquist et al., Phys. Rev. D67 055002 (2003)] [Gogoladze et al., Phys. Rev. D74 093012 (2006)]

## UED:

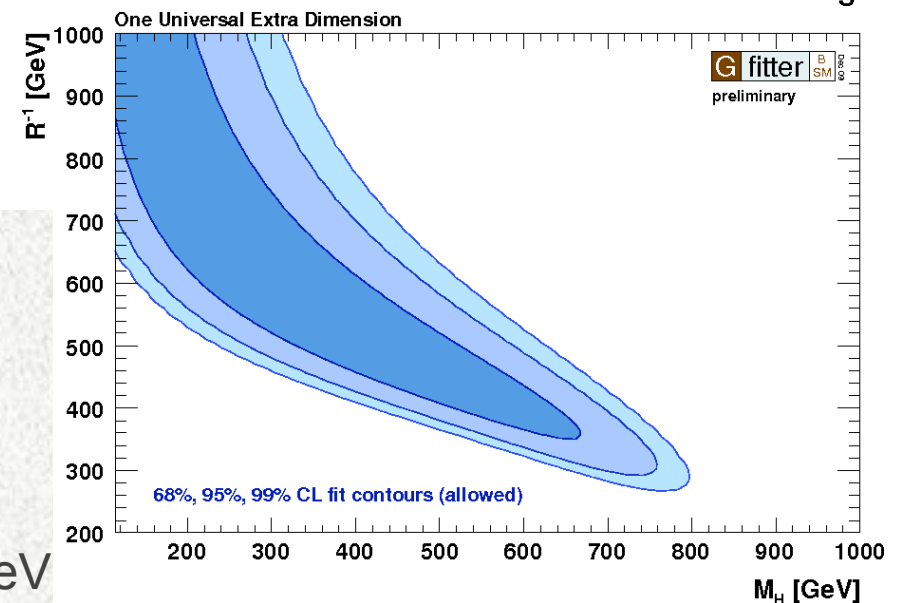
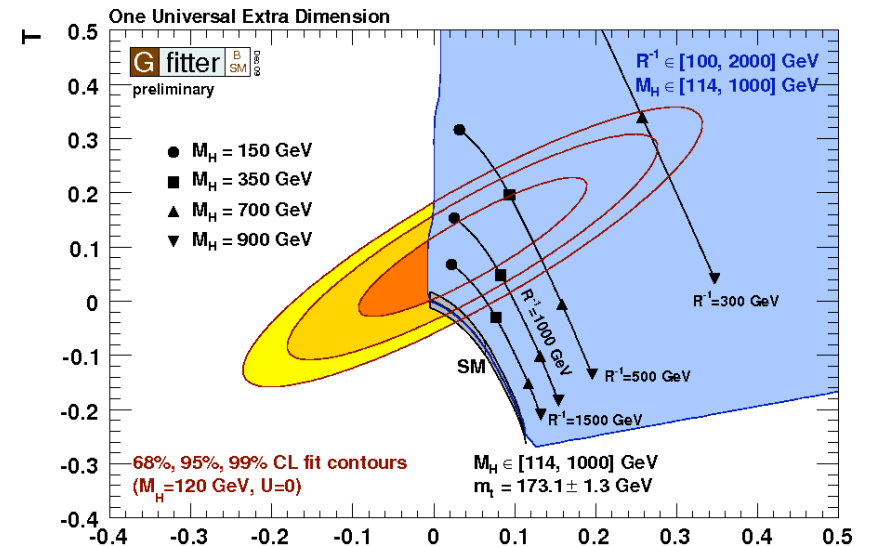
- All SM particles can propagate into ED
- Compactification  $\rightarrow$  KK excitations
- Conservation of KK parity
  - Phenomenology similar to SUSY
  - Lightest stable KK state: DM candidate
- Model parameters:
  - $d_{ED}$ : number of ED (fixed to  $d_{ED}=1$ )
  - $R^{-1}$ : compactification scale ( $m_{KK} \sim n/R$ )

## Contribution to vac. polarisation (STU):

- From KK-top/bottom and KK-Higgs loops
- Dependent on  $R^{-1}$ ,  $M_H$  (and  $m_t$ )

## Results:

- Large  $R^{-1}$ : UED approaches SM (exp.)
  - Only small  $M_H$  allowed
- Small  $R^{-1}$ : UED contribution compensated by large  $M_H$
- Excluded:  $R^{-1} < 300$  GeV and  $M_H > 800$  GeV

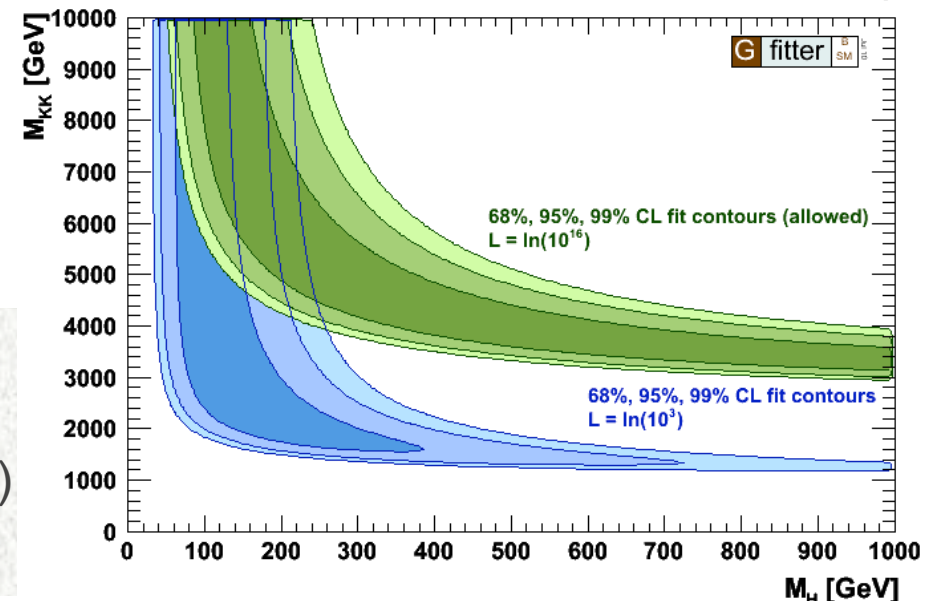
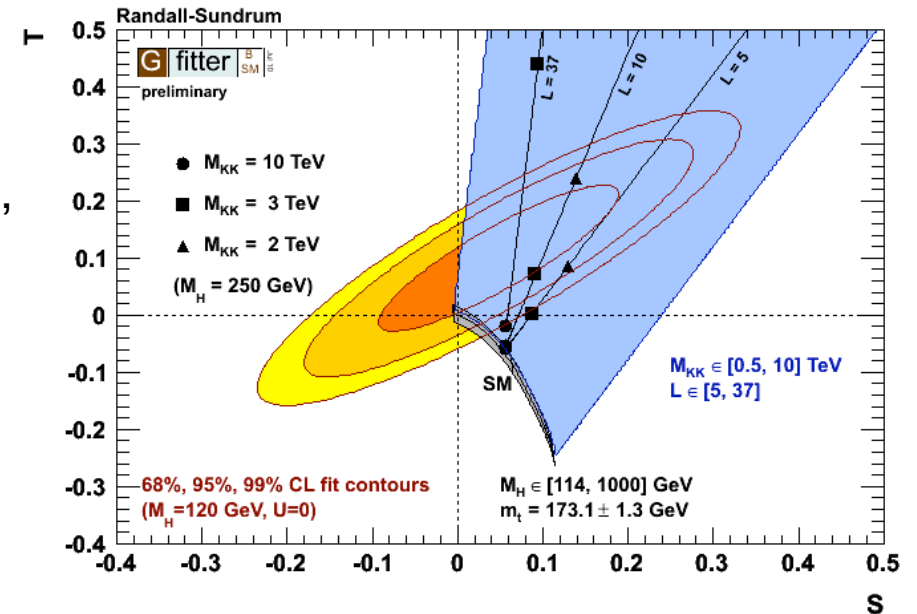


# Warped Extra Dimensions (Randall-Sundrum)



[L. Randall, R. Sundrum, Phys. Rev. Lett. 83, 3370 (1999)] [M. Carena et al., Phys. Rev. D68, 035010 (2003)]

- Introduction of one extra dimension (ED) to solve the hierarchy problem
- RS model characterized by one warped ED, confined by two three-branes
  - Higgs localized on “IR” brane
  - Gauge and matter fields allowed to propagate in bulk region
- SM particles accompanied by towers of heavy KK modes.
- Model parameters:
  - $L$ : inverse warp factor, function of compactification radius, explains hierarchy between EW and Planck scale
  - $M_{KK}$ : KK mass scale
- Results:
  - Excessive values of  $T$  possible
  - Large  $L$  forces large  $M_{KK}$  (several TeVs)
  - Some compensation if  $M_H$  is large



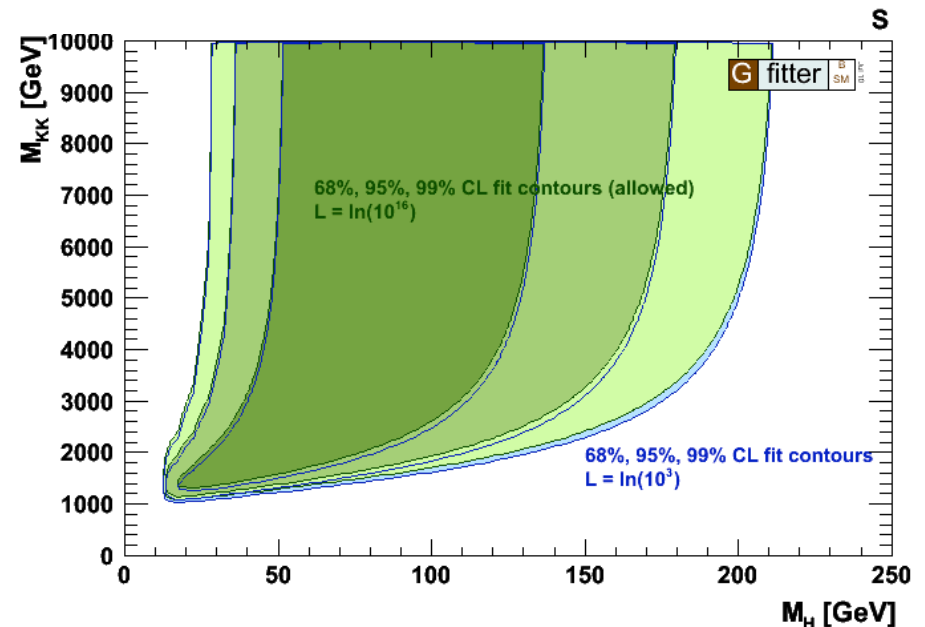
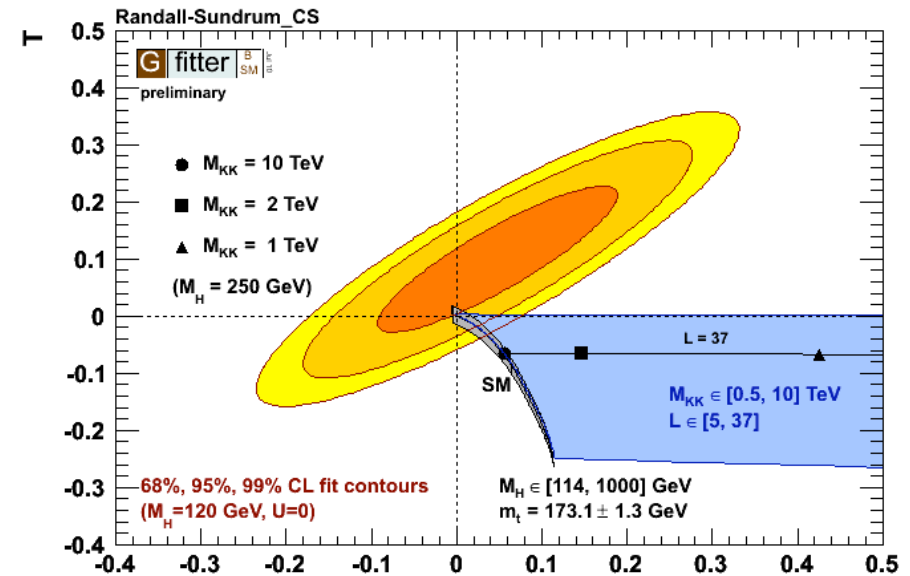
# Warped Extra Dimensions w/ custodial symmetry



[K. Agashe, A. Delgado, M. May, R. Sundrum, hep-ph/0308036v2]

- Goal: “cure” WED with large T values
- Introduction of so-called **custodial isospin gauge symmetry** in the bulk
- Extension of hypercharge group to  $SU(2)_R \times U(1)_X$ 
  - Bulk symmetry group:  
 $SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_X$
- Broken to SM  $SU(3)_C \times SU(2)_L \times U(1)_Y$  on “UV” brane
- IR brane  $SU(2)_R$  symmetric
- Right-handed fermionic fields occur in doublets

- Results:
  - Almost completely ruled out
  - Only small  $M_H$  allowed



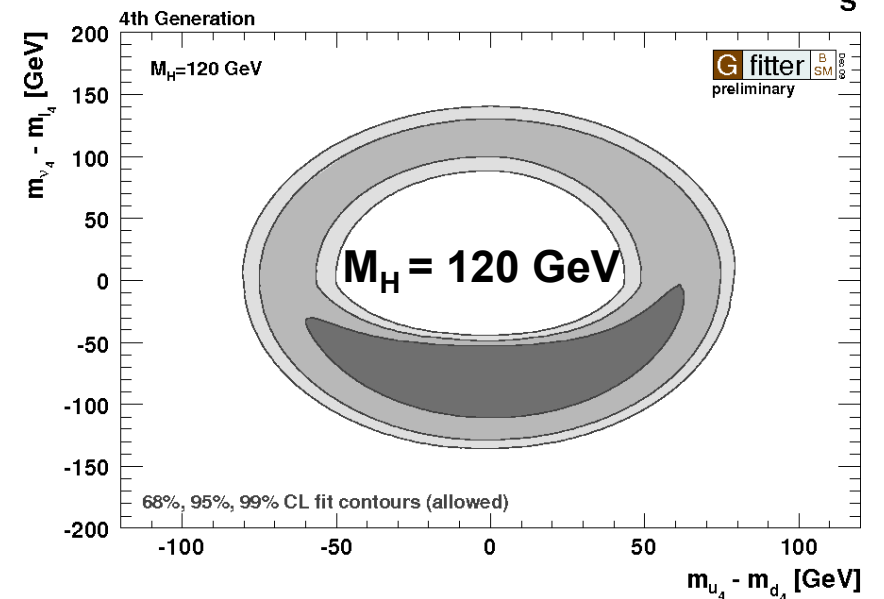
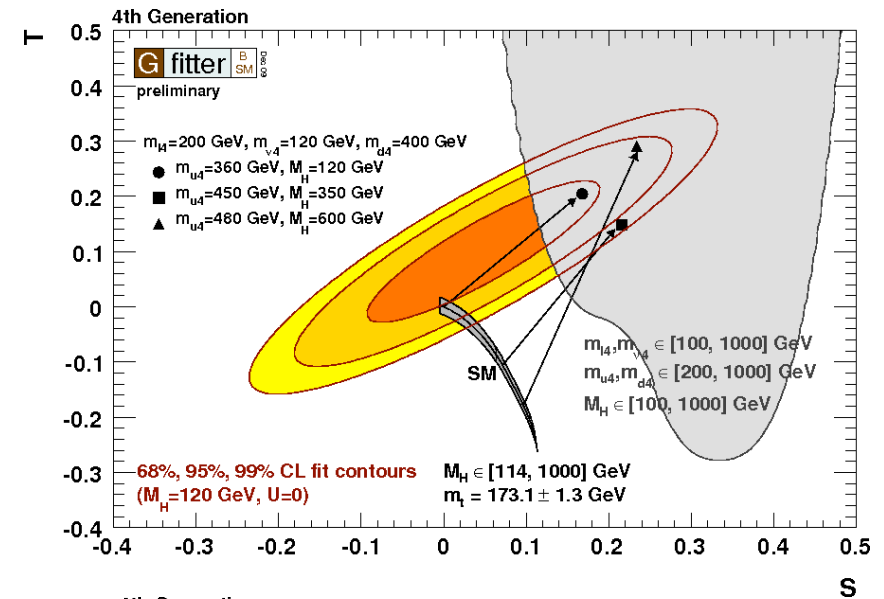
# 4<sup>th</sup> fermion generation



[H. He et al., Phys. Rev. D 64, 053004 (2001)]

- Models with a fourth generation
  - No explanation for  $n=3$  generations
  - Intr. new states for leptons and quarks
    - $\Psi_L = (\Psi_1, \Psi_2)_L, \Psi_{1,R}, \Psi_{2,R}$
  - Free parameters:  $m_{u_4}, m_{d_4}, m_{e_4}, m_{\nu_4}$ 
    - masses of new quarks and leptons
    - assume: no mixing of extra fermions
- Contrib. to  $STU$  from new fermions
  - Discrete shift in  $S$  from extra generation
  - Sensitive to mass difference between up- and down-type fields.  
(not to absolute mass scale)

- Results:
  - With appropriate mass differences: 4<sup>th</sup> fermion model consistent with EW data
    - In particular a large  $M_H$  is allowed
  - 5+ generations disfavored
  - Data prefer a heavier charged lepton / up-type quark (which both reduce size of  $S$ )



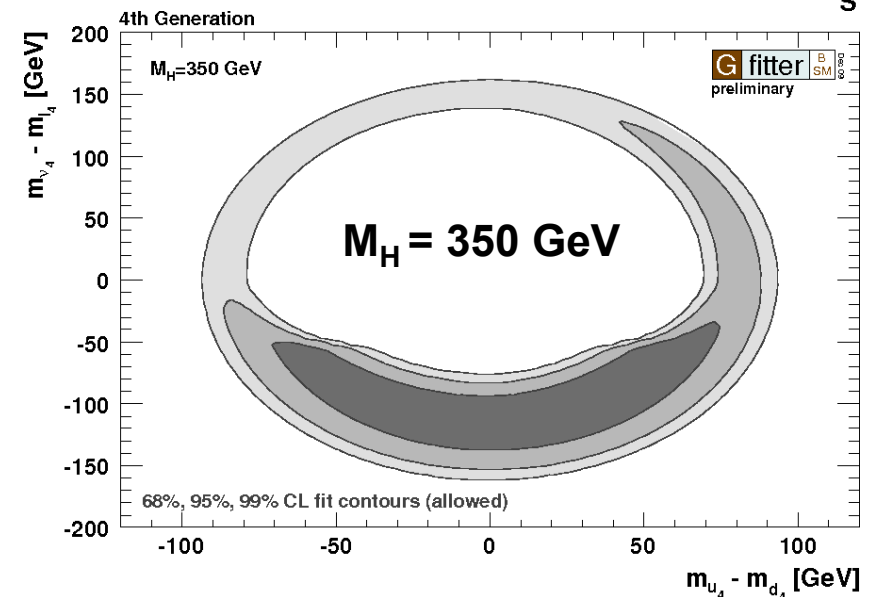
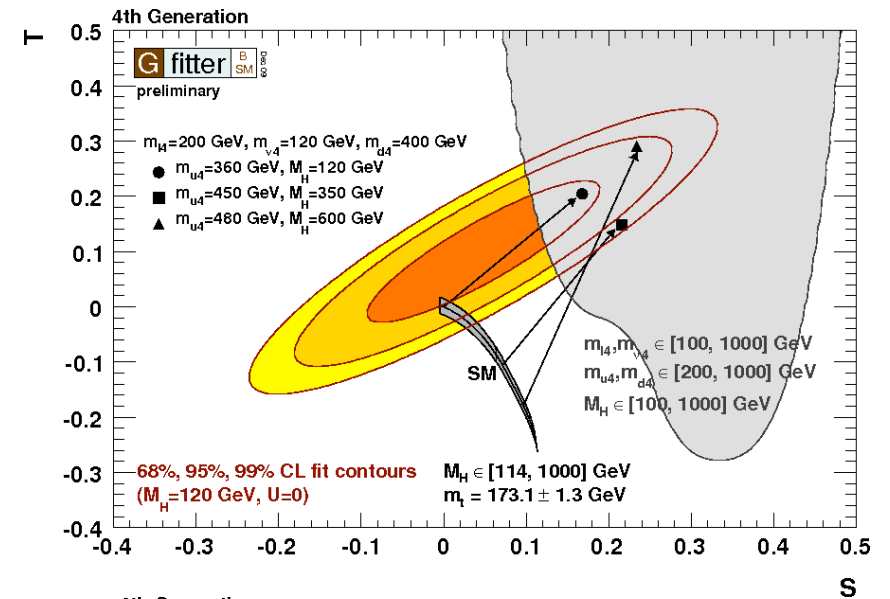
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    - masses of new quarks and leptons
    - assume: no mixing of extra fermions
- Contrib. to  $STU$  from new fermions
  - Discrete shift in  $S$  from extra generation
  - Sensitive to mass difference between up- and down-type fields.  
(not to absolute mass scale)

- Results:
  - With appropriate mass differences: 4<sup>th</sup> fermion model consistent with EW data
    - In particular a large  $M_H$  is allowed
  - 5+ generations disfavored
  - Data prefer a heavier charged lepton / up-type quark (which both reduce size of  $S$ )



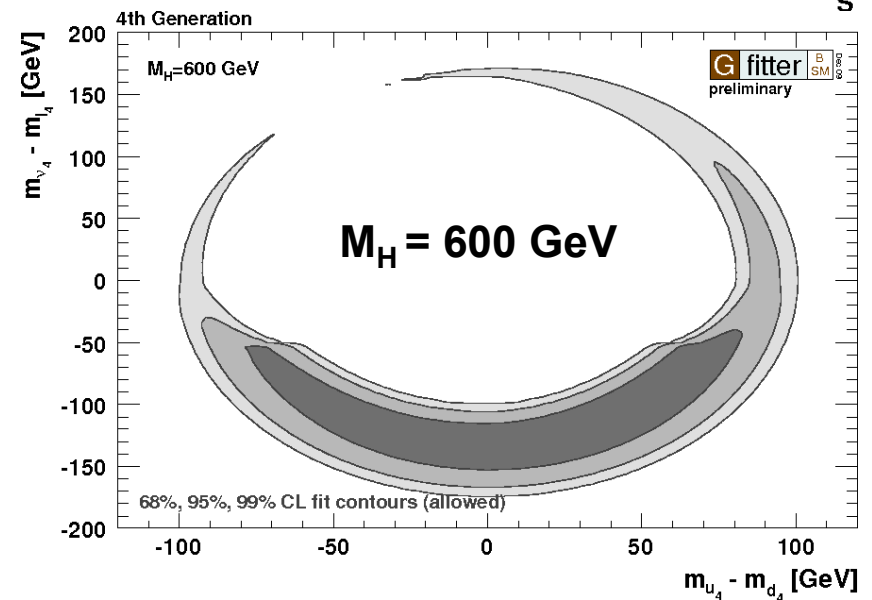
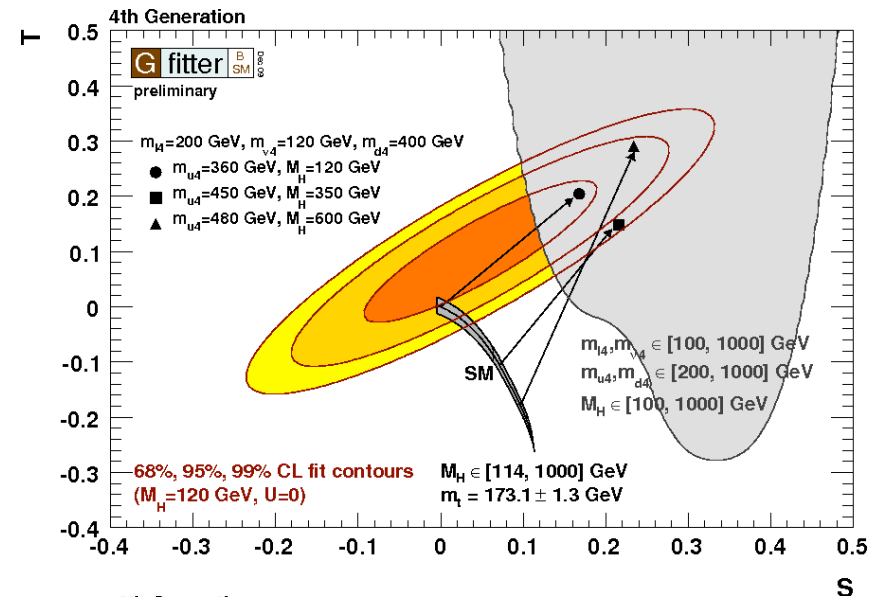
# 4<sup>th</sup> fermion generation



[H. He et al., Phys. Rev. D 64, 053004 (2001)]

- Models with a fourth generation
  - No explanation for  $n=3$  generations
  - Intr. new states for leptons and quarks
    - $\Psi_L = (\Psi_1, \Psi_2)_L, \Psi_{1,R}, \Psi_{2,R}$
  - Free parameters:  $m_{u_4}, m_{d_4}, m_{e_4}, m_{\nu_4}$ 
    - masses of new quarks and leptons
    - assume: no mixing of extra fermions
- Contrib. to  $STU$  from new fermions
  - Discrete shift in  $S$  from extra generation
  - Sensitive to mass difference between up- and down-type fields.  
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# Minimal SuperGravity (preliminary)

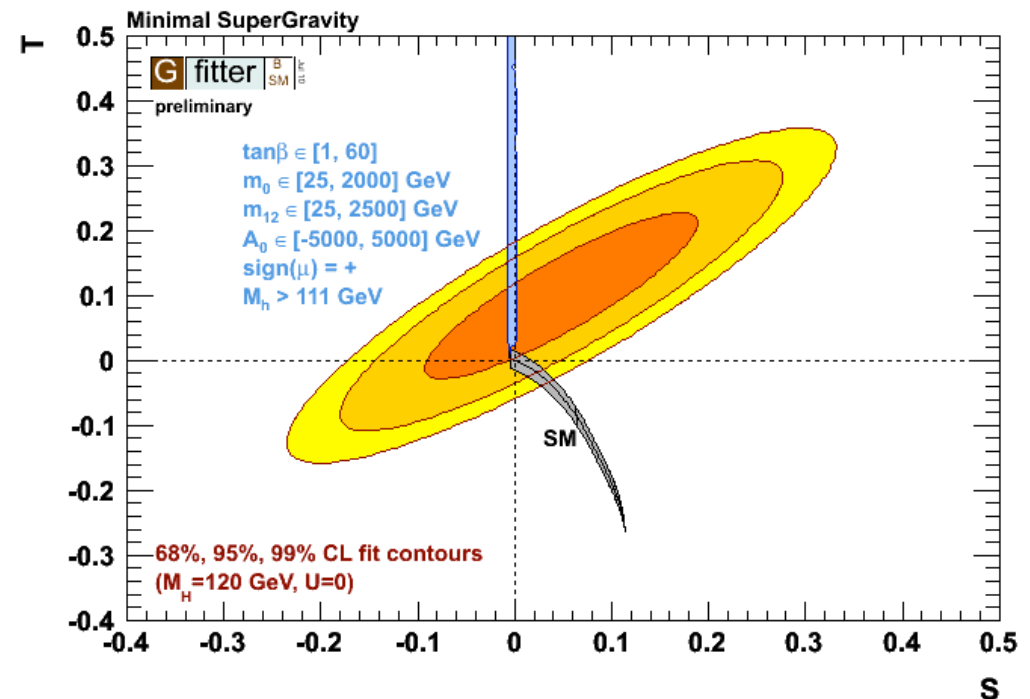


[G. Weiglein: arXiv:hep-ph/9712226v1][S. Heinemeyer, W. Hollik, G. Weiglein: arXiv:hep-ph/0412214v1]

- Supersymmetry solves many shortcomings of SM: hierarchy problem, unification of coupling constants, DM candidate, ...
- mSUGRA: highly constrained breaking mechanism at GUT scale
  - SUSY breaking mediated by **gravitational interaction**

- mSUGRA determined by 5 parameters:
  - $m_{1/2}$ : mass of fermions at GUT scale
  - $m_0$ : mass of scalars at GUT scale
  - $\tan\beta$ : ratio of two Higgs vacuum expectation values
  - $A_0$ : trilinear coupling of the Higgs
  - $\text{sgn}(\mu)$ : sign of Higgsino mass term

- Oblique corrections dominated by weak isospin violation between  $m_{\tilde{b}_1}$ ,  $m_{\tilde{t}_1}$ , and  $m_{\tilde{t}_1}, m_{\tilde{t}_2}$ 
  - $\delta M_W \lesssim 35 \text{ MeV}$ ,  $\delta \sin^2 \theta_{\text{eff}}^l \lesssim 2 \times 10^{-4}$
- By construction of the oblique parameters  $\rightarrow$  T parameter has dominant contribution





# Additional constraints on mSUGRA



- Extra constraints on top of EW precision observables

- LEP limits on Higgs mass, neutralinos, sleptons
- Kaon-, B-physics
- $(g_\mu - 2)$
- relic density

- Using theoretical predictions by:

- microMegas
- FeynHiggs
- SuperIso
- SoftSUSY

- Dedicated C++ interfaces to Gfitter

- No exchange of Les Houches files

Parameter	Input value	meas. error	theoretical error
$\Omega h^2$	0.1131	0.0034	0.012
$a_\mu(\text{meas}) - a_\mu(\text{SM})$	$20.5 \times 10^{-10}$	$8.2 \times 10^{-10}$	$2.0 \times 10^{-10}$
$\text{BF}(B \rightarrow X_s \gamma)_{\text{meas}} / \text{BF}(B \rightarrow X_s \gamma)_{\text{SM}}$	1.117	0.076	0.096
$\Delta m_s(\text{meas}) / \Delta m_s(\text{SM})$	1.015	0.122	
$\text{BF}(B_s \rightarrow \mu\mu)$	$< 4.7 \times 10^{-8}$		
$\text{BF}(B \rightarrow \tau\nu)_{\text{meas}} / \text{BF}(B \rightarrow \tau\nu)_{\text{SM}}$	2.16	+0.62 -0.53	
$R_{l23}$	1.004	0.007	
$\text{BF}(B \rightarrow D\tau\nu) / \text{BF}(B \rightarrow D\ell\nu)$	0.42	0.13	
$M_h$ [GeV]	$> 114$		3
$M_{\chi_0}$ [GeV]	$> 50$		
$M_{\chi_1^+}$ [GeV]	$> 103$		
$M_{\tilde{e}_R}$ [GeV]	$> 90$		
$M_{\tilde{\mu}_R}$ [GeV]	$> 90$		
$M_{\tilde{\tau}_R}$ [GeV]	$> 90$		

Average of  $e^+e^-$  and  $\tau$  predictions for  $a_\mu^{\text{had}} [\pi\pi]$ , with scaled error.  
arXiv:0908.4300v2, 0906.5443

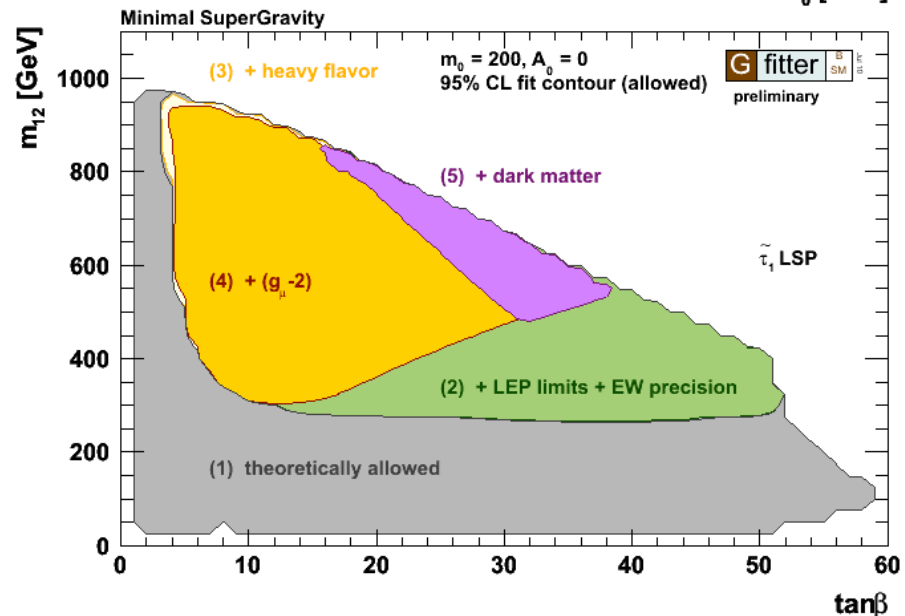
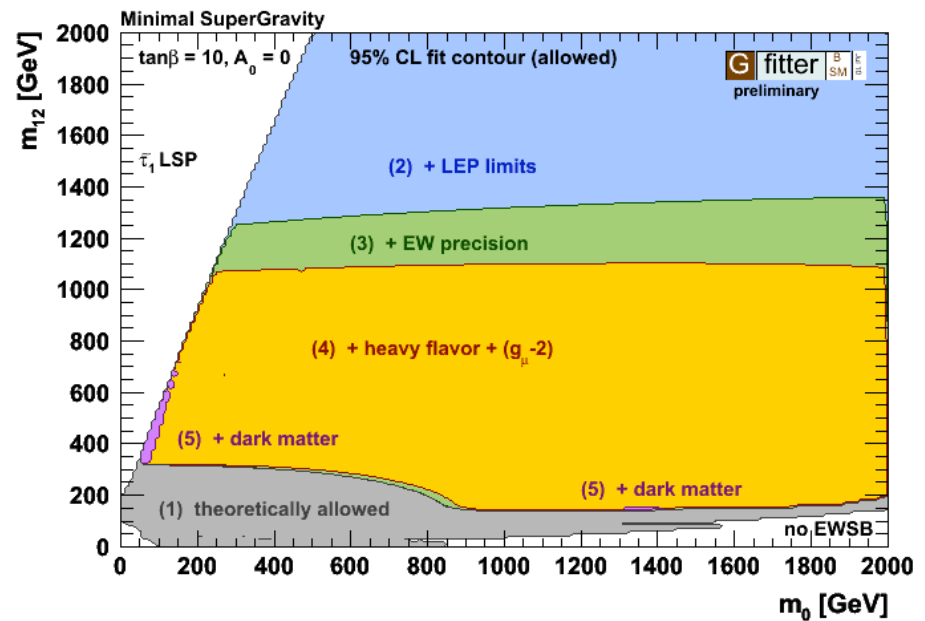
SoftSUSY - [B.C. Allanach, Comp. Phys. Com. 143 (2002) 305-331], Feynhiggs - [M. Frank et al., JHEP0702:047, 2007], SuperIso - [F. Mahmoudi, JHEP12 (2007), 026], microMegas - [G. B'elanger et al., IRFU-10-24, LAPTH-012-10]

# mSUGRA: Parameter Scans



[G. Weiglein: arXiv:hep-ph/9712226v1][S. Heinemeyer, W. Hollik, G. Weiglein: arXiv:hep-ph/0412214v1]

- Low  $m_0$  area excluded by requiring a non-charged LSP.
- Limits on  $m_0$ ,  $m_{1/2}$ ,  $\tan\beta$ ,  $A_0$  by including in the fit:
  1. Theoretically allowed region
  2. LEP limits in Higgs mass, neutralinos, sleptons
  3. Electroweak precision observables (STU)
  4. Constraints from K-, B-physics and  $(g_\mu - 2)$
  5. From the relic density
- 95% CL contours of allowed regions are shown

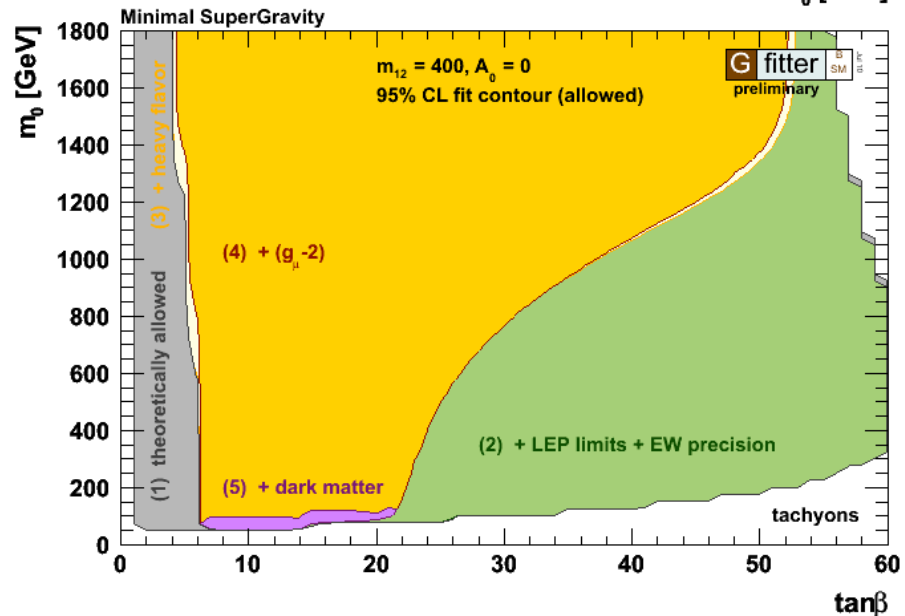
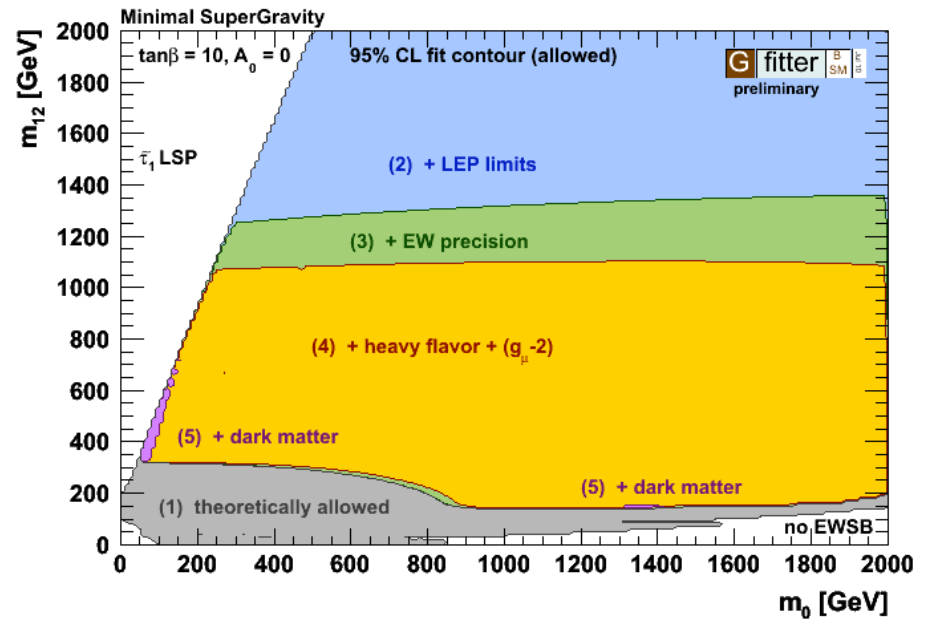


# mSUGRA: Parameter Scans



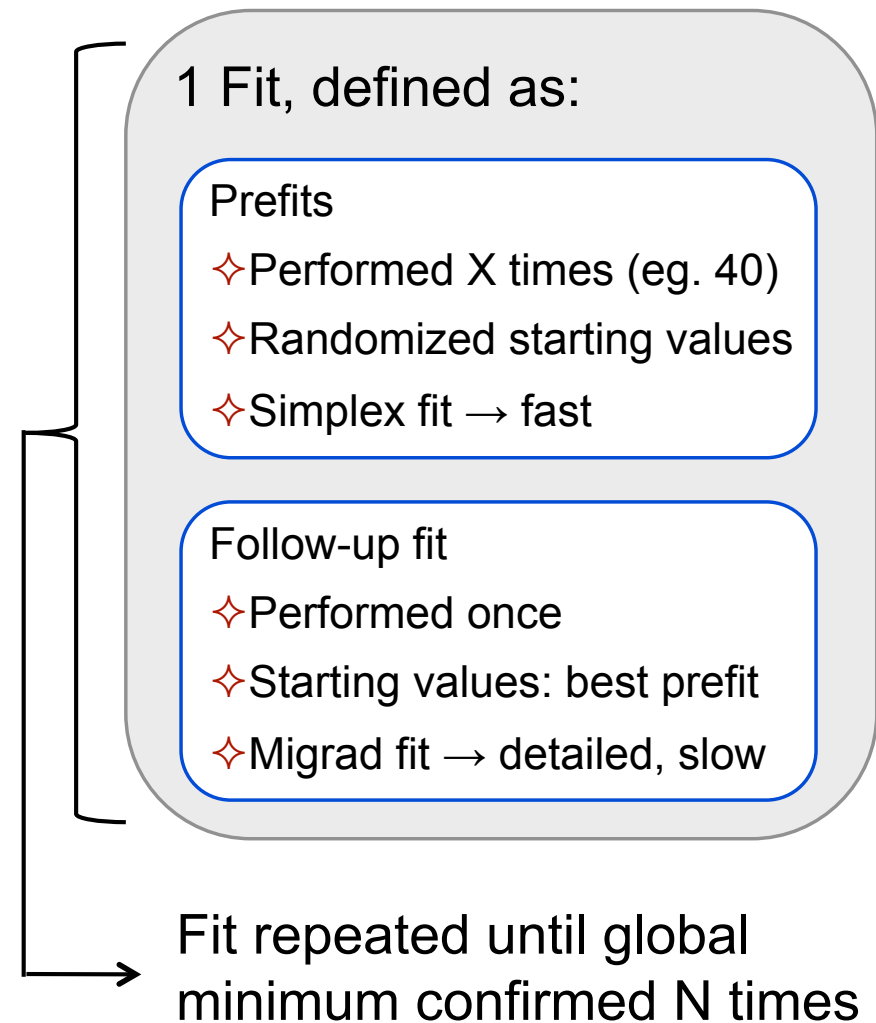
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- No fit results shown here yet – still preliminary ;-)
  - Results so far consistent with MasterCode and Fittino groups.
- Main challenge: finding global mSUGRA minimum in constrained fits
  - Eg. LSP mass-scan:  $\chi^2_{\min}$  when predicted  $M_{\text{LSP}} = 150$  GeV?
- Solution: “brute force” fit strategy
  - 1 Fit takes ~15 mins
    - O(1000) Minuit iterations, dominated by calc. of SUSY particle spectrum
  - Parameter scans fully parallelized
- Need lots of computing power ...

“brute force”  
fit strategy:





## A Gfitter Package for 2HDM SM Extensions

- Two Higgs Doublet Model (Type-II)
  - SM extended by additional Higgs doublet (2HDM)
  - One Higgs doublet couples to up-type fermions, other doublet couples to down-type fermions
  - Five Higgs bosons: 3 neutral ( $A^0$ ,  $h^0$ ,  $H^0$ ), two charged ( $H^\pm$ )
  - 6 Free parameters  $\rightarrow M_{H^\pm}$ ,  $M_{A^0}$ ,  $M_{H^0}$ ,  $M_h$ ,  $\tan\beta$ ,  $|\alpha|$
  - [Type-II 2HDM resembles Higgs sector in MSSM]

- Have looked at processes sensitive to charged Higgs interactions

$$\mathcal{L}_{H^\pm ff} = \frac{g}{2\sqrt{2}m_W} \left\{ H^+ \bar{U} \left[ M_U V_{CKM} (1 - \gamma_5) \cot\beta + V_{CKM} M_D (1 + \gamma_5) \tan\beta \right] D + \text{h.c.} \right\}$$

- Interaction has similar structure as W-boson
  - Left-handed coupling:  $1/\tan\beta$ , right-handed coupling:  $\tan\beta$
- Sensitive parameters  $\rightarrow M_{H^\pm}, \tan\beta$
- LEP limit:  $M_{H^\pm} > 78.6 \text{ GeV}$  (95%CL), for any value of  $\tan\beta$

- Measurements of interest from B-physics

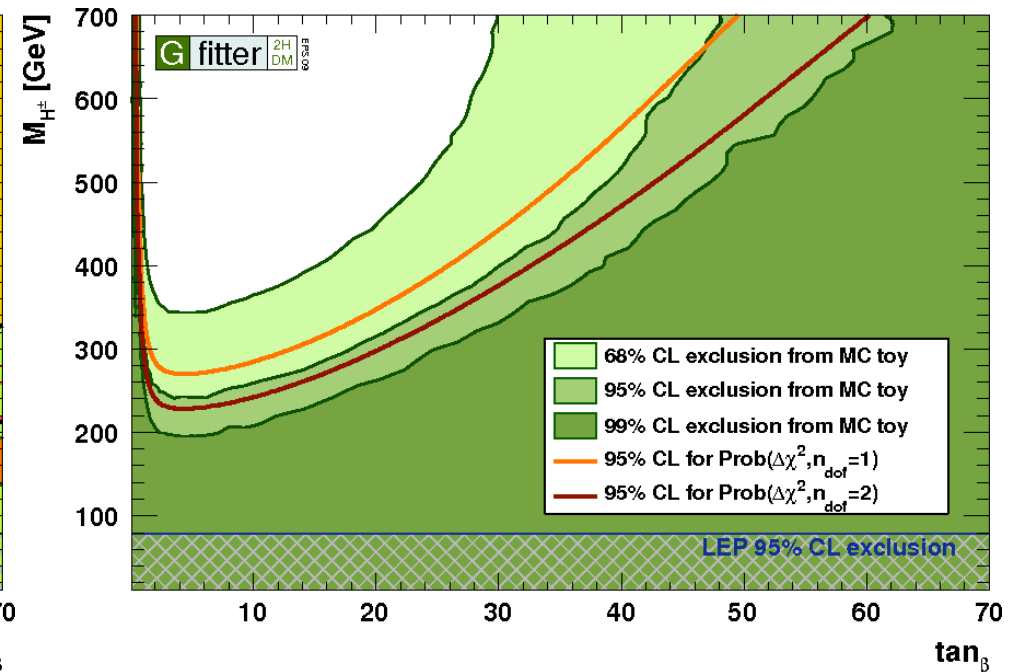
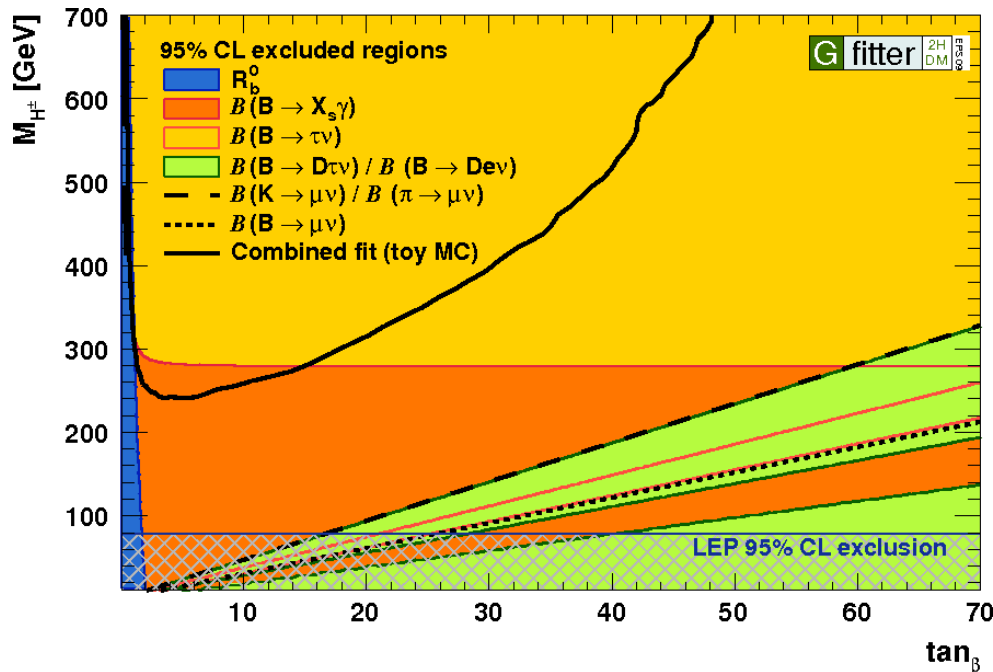
Observable	Input value	Exp. Ref.	Calculation
$R_b^0$	$0.21629 \pm 0.00066$	[ADLO, Phys. Rept. 427, 257 (2006)]	[H. E. Haber and H. E. Logan, Phys. Rev. D62, 015011 (2000)]
BR (B $\rightarrow$ X $_s$ $\gamma$ )	$(3.52 \pm 0.23 \pm 0.09) \cdot 10^{-4}$	[HFAG, latest update]	[M. Misiak et al., Phys. Rev. Lett. 98, 022002 (2007)]
BR (B $\rightarrow$ $\tau\nu$ )	$(1.73 \pm 0.33) \cdot 10^{-4}$	[P.Chang, Talk at ICHEP 2008]	[W. S. Hou, Phys. Rev. D48, 2342 (1993)]
BR (B $\rightarrow$ $\mu\nu$ )	$(-5.7 \pm 6.8 \pm 7.1) \cdot 10^{-4}$	[E. Baracchini, Talk at ICHEP 2008]	[W. S. Hou, Phys. Rev. D48, 2342 (1993)]
BR (K $\rightarrow$ $\mu\nu$ ) / BR( $\pi$ $\rightarrow$ $\mu\nu$ )	$1.004 \pm 0.007$	[FlaviaNet., arXiv: 0801.1817]	[FlaviaNet, arXiv: 0801.1817]
BR(B $\rightarrow$ D $\tau\nu$ ) / BR(B $\rightarrow$ D $e\nu$ )	$0.416 \pm 0.117 \pm 0.052$	[Babar, Phys. Rev. Lett 100, 021801 (2008)]	[J. F. Kamenik and F. Mescia, arXiv:0802.3790]

# 2HDM: Combined Fit



- Below: overlay of individual 95% CL excluded regions
- Combined exclusion area depends on assumption on number of dof.
  - ndof=1 : where single constraint dominates.
  - ndof=2 : several observables contribute.
- MC toy study to resolve exclusion area
  - Assuming  $n_{\text{dof}}=1$  and 2-sided limits

- Combined limit not necessarily stronger than single constraint due to increasing  $n_{\text{dof}}$
- Fit minimum:  $\chi^2=3.9$  for  $M_H=858$  GeV and  $\tan\beta=6.8$
- Excluded at 95% CL
  - Small  $\tan\beta$
  - $M_H < 240$  GeV for all  $\tan\beta$
  - $M_H < 780$  GeV for  $\tan\beta=70$



- **G** **fitter** is a powerful framework for HEP model fits
- Latest results/updates and new results always available at:
  - <http://cern.ch/Gfitter>
- **Results obtained sofar**
  - New and updated global fit of the electroweak SM
    - Higgs mass strongly constrained. Light Higgs preferred by SM.
  - Oblique parameters (still!) a powerful method to constrain BSM theories
    - Presented constraints on various BSM theories
    - Heavy Higgs boson allowed in various BSM models
  - Constraints on the Two-Higgs-Doublet-Model
- **The future**
  - Maintain and extend existing fits.
    - Tevatron updates and of course LHC results
  - More models in preparation for oblique parameters fit (STU)
  - Expect SUSY fit results to come out soon!





A **G**eneric **F**itter Project for HEP Model Testing

# Backup

# Statistical interpretation Higgs limits

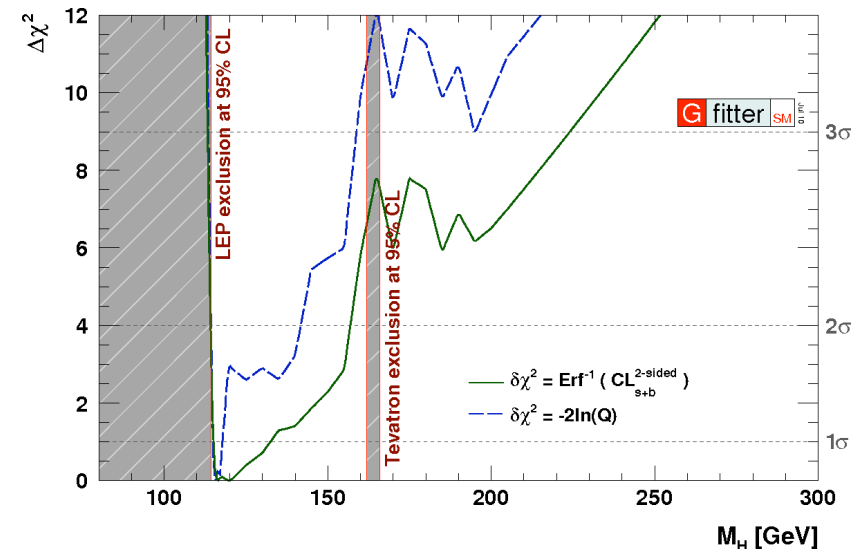
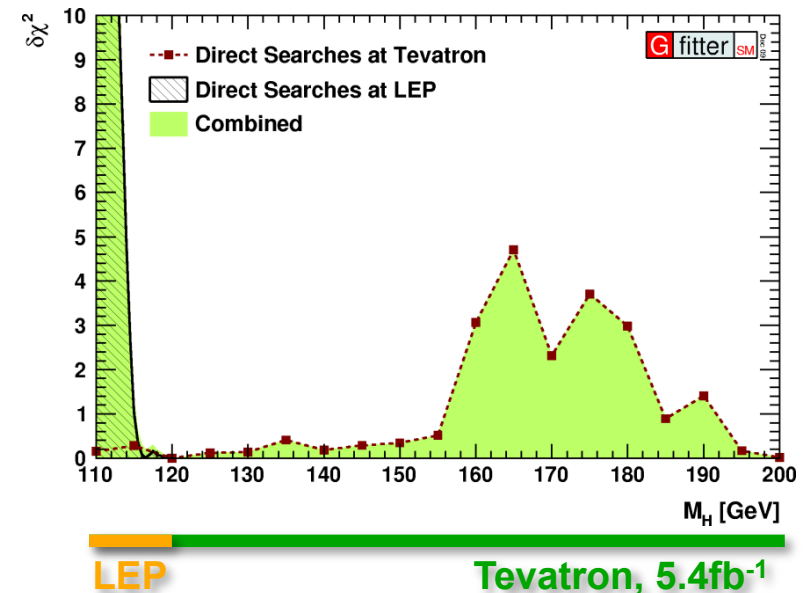


## Stat. interpretation in global fit: 2-sided $CL_{S+B}$

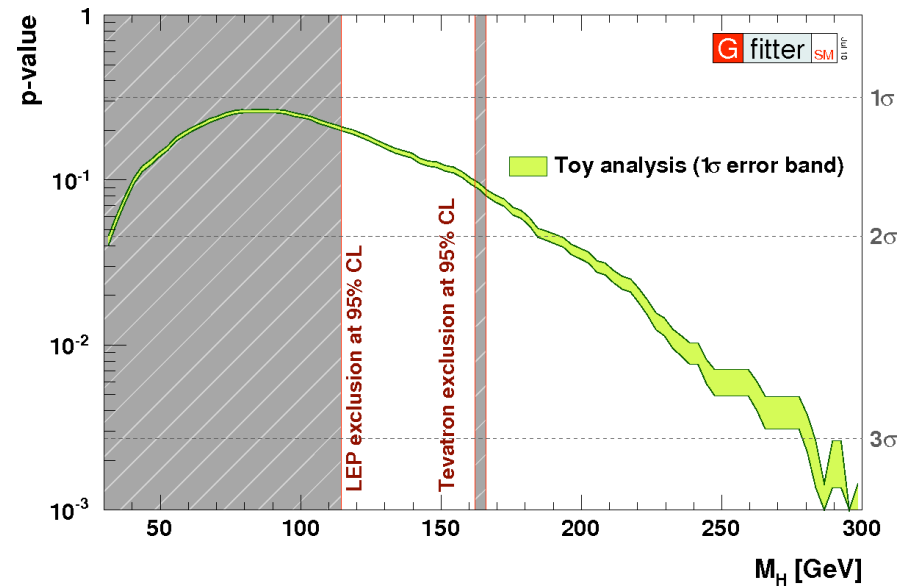
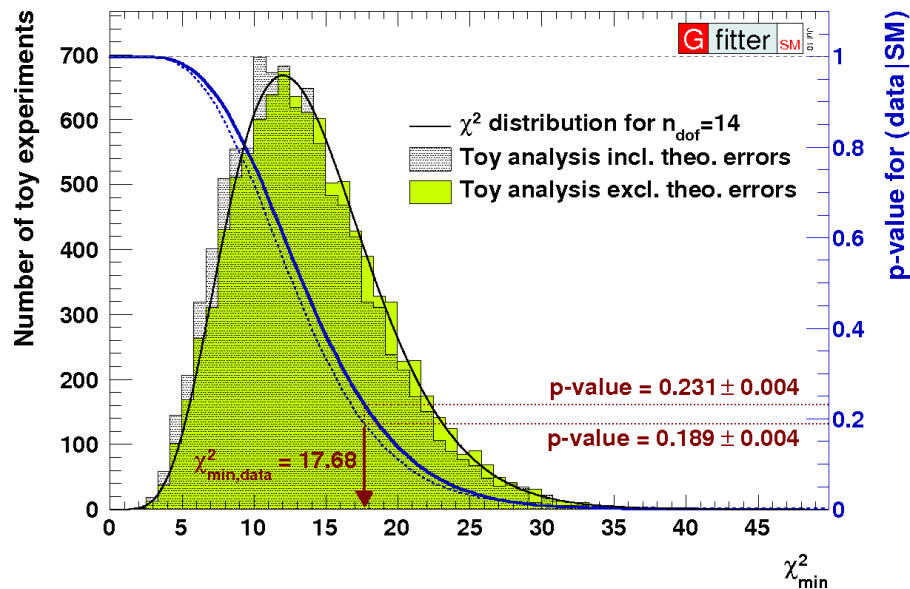
- Experiments measure test statistics:  
 $LLR = -2\ln Q$ , where  $Q=L_{S+B}/L_B$
- $LLR$  is transformed by experiments into one-sided  $CL_{S+B}$  using toy-MC experiments
  - Sensitive to too few Higgs-like events
- We transform 1-sided  $CL_{S+B}$  into 2-sided  $CL^{2s}_{S+B}$ 
  - We measure deviations from the SM.
  - Eg. also interested in too many Higgs-like events.
- $\chi^2$  contribution calculated via inverse error function, assuming symmetric pdf :  
 $\delta\chi^2 = \text{Erf}^{-1}(1 - CL^{2s}_{S+B})$

## Alternative treatments (thanks to fruitful discussion with Tevatron people):

- Use one-sided  $CL_{S+B}$ : however, different interpretation – want SM Higgs (not any Higgs)
- Directly use  $\delta\chi^2 \approx LLR$ : Bayesian interpretation, lacks pseudo-MC information



- determine p-value by using MC toy experiments
  - p-value: probability for wrongly rejecting the SM
  - p-value: probability for getting a  $\chi^2_{\min, \text{toy}}$  larger than the  $\chi^2_{\min, \text{data}}$  from data



- for each toy complete fit is performed
- p-value =  $(23 \pm 1.2)\%$ 
  - no significant requirement for new physics

- derivation of p-value for standard fit as function of  $M_H$
- small p-values for large Higgs masses ( $M_H \sim 280$  GeV)

- usually unable to indicate signals for physics beyond SM
  - sensitive observables mixed with insensitive ones

# $b \rightarrow s \gamma$ and $R_b^0$

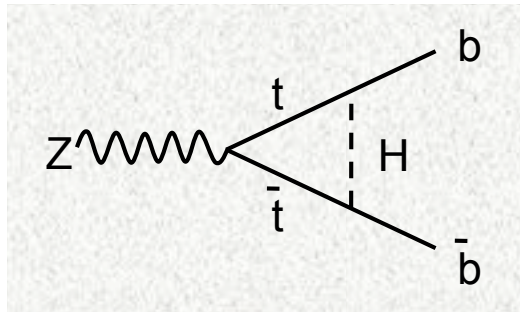


- Penguin dipole-moment of  $b \rightarrow s \gamma$  allows combination of left- and right-handed Higgs couplings.

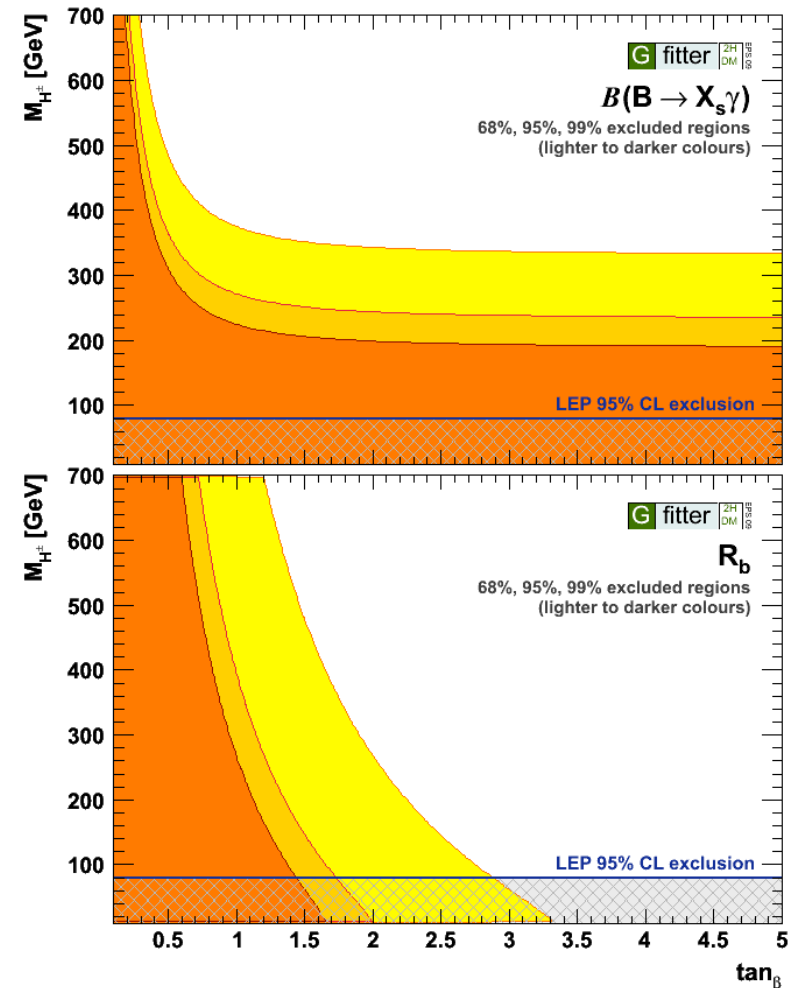
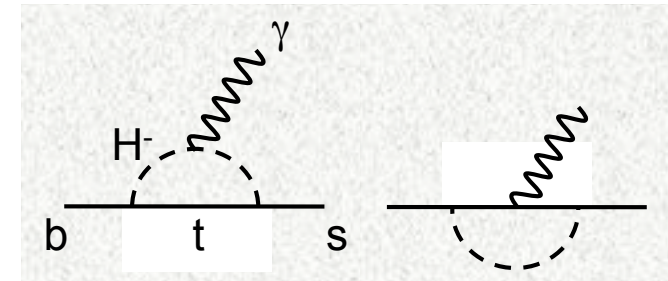
- Wilson coefficient:

$$C_7^H \approx -\frac{m_t^2}{2M_H^2} \left( \frac{7}{36} \frac{1}{\tan^2 \beta} - \frac{2}{3} \ln \frac{m_H^2}{m_t^2} - \frac{1}{2} \right)$$

- $B \rightarrow X_s \gamma$  :  $M_H > 200$  GeV for  $\tan \beta > 1$



- Z vertex contribution suppressed by  $1/\tan^2 \beta$
- $R_b^0$  sensitive to small  $\tan \beta$  only

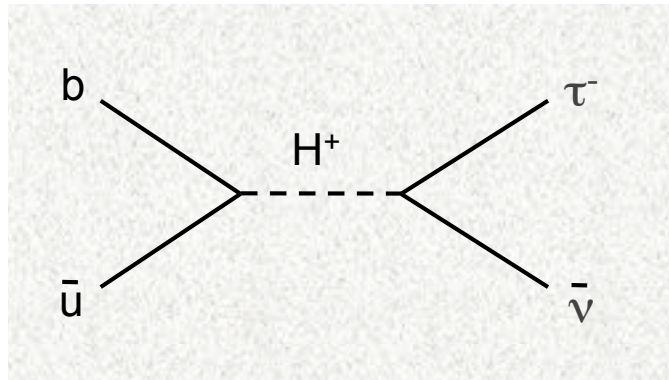


# Strongest constraint: $B \rightarrow \tau\nu$

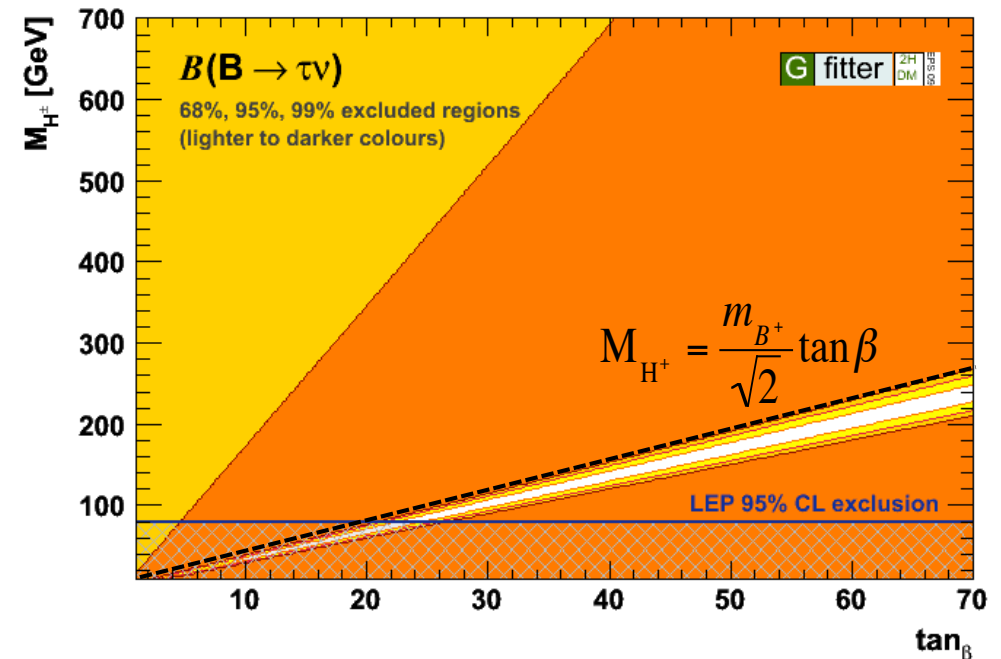


(BRx10 <sup>-4</sup> )	Oct '08	EPS '09	Reference
$BR(B \rightarrow \tau\nu)_{\text{meas}}$	$1.51 \pm 0.33$	$1.73 \pm 0.35$	FPCP 2009
$BR(B \rightarrow \tau\nu)_{\text{SM}}$	$1.53 \pm 0.49$	$1.12 \pm 0.25$	(Vub direct-measurements.)
$V_{ub} (\times 10^{-3})$	$3.81 \pm 0.47$	$3.70 \pm 0.33$	Gambino, Giordano, Ossola, Uraltsev
$f_B$ (MeV)	$216 \pm 22$	$190 \pm 13$	HPQCD '09 using NRQCD, Davies at FPCP'09
$BR(B \rightarrow \tau\nu)_{\text{CKM}}$	$0.83^{+0.27}_{-0.10}$	$0.80^{+0.15}_{-0.09}$	CKM Fitter '09, indirect Vub

- We use prediction based on direct measurements of  $V_{ub}$ .
- [2.4 $\sigma$  deviation between measurement and CKM-fitter prediction for  $BR(B \rightarrow \tau\nu)$ ]



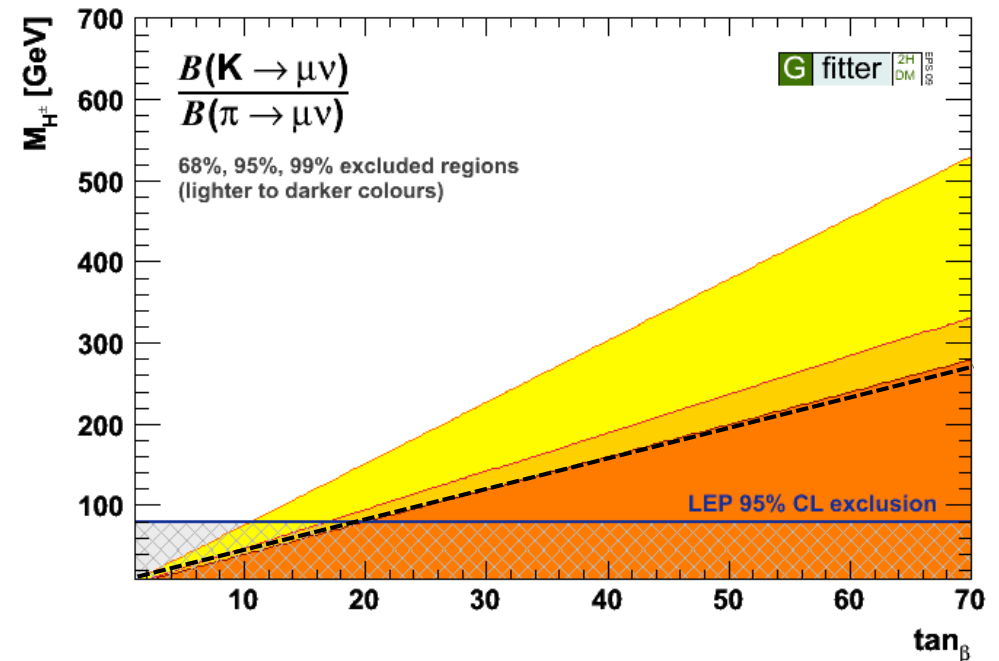
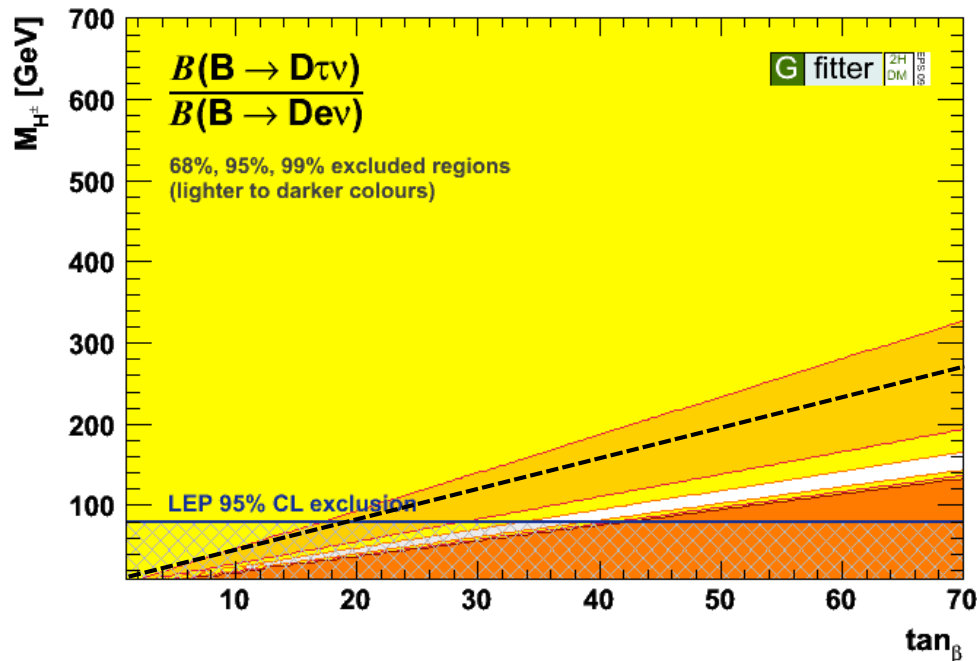
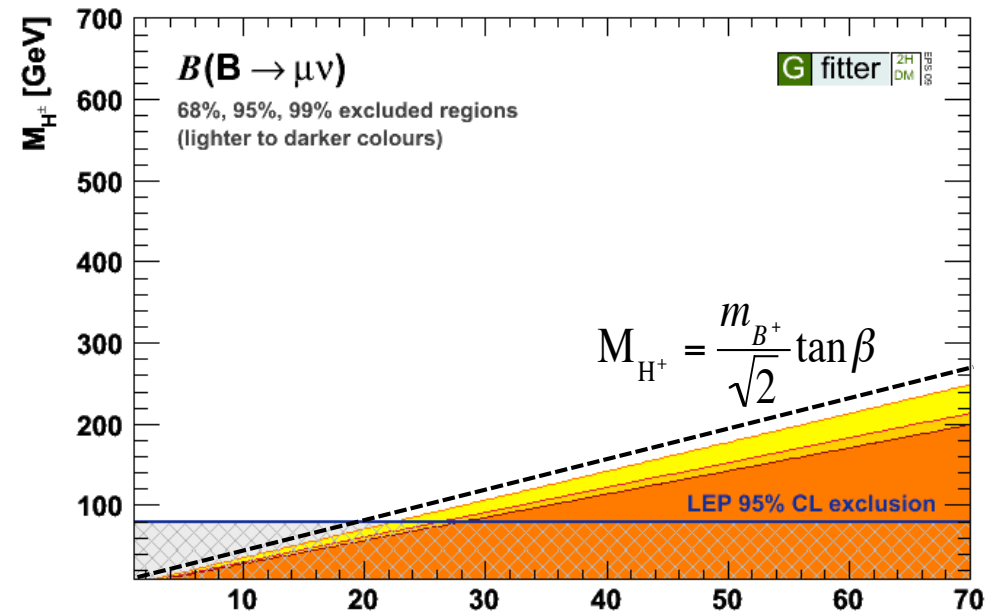
$$\frac{BR(B \rightarrow \tau\nu)_{2\text{HDM}}}{BR(B \rightarrow \tau\nu)_{\text{SM}}} = \left[ 1 - m_B^2 \frac{\tan^2 \beta}{M_{H^\pm}^2} \right]^2$$



# Other measurements w/ tree-level contributions

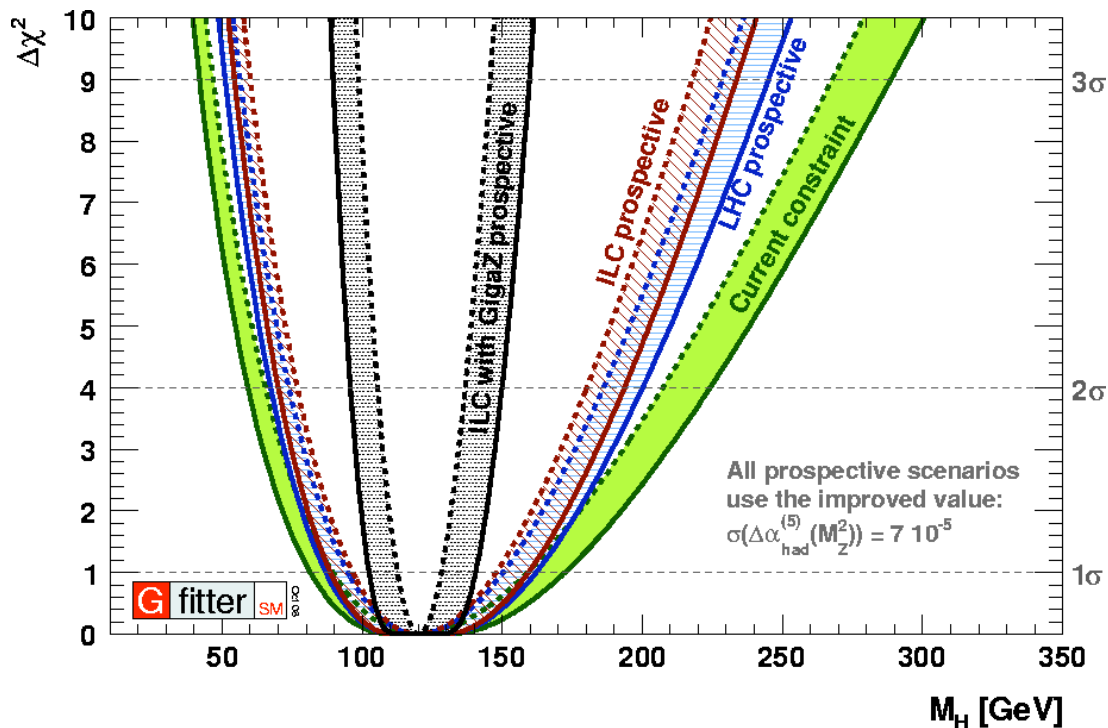


- Weak upper-limit on  $BR(B \rightarrow \mu\nu)$
- Favored solution of  $BR(B \rightarrow \tau\nu)$  excluded by combination of:
  - $B \rightarrow X_s \gamma$
  - $BR(K \rightarrow \mu\nu) / BR(\pi \rightarrow \mu\nu)$
  - $BR(B \rightarrow D\tau\nu) / BR(B \rightarrow D\mu\nu)$



- LHC, ILC (+GigaZ)\***
  - exp. improvement on  $M_W, m_t, \sin^2\theta_{\text{eff}}^l, R_l^0$
  - in addition improved  $\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$   
[F. Jegerlehner, hep-ph/0105283]

Quantity	Present	Expected uncertainty		
		LHC	ILC	GigaZ (ILC)
$M_W$ [ MeV]	25	15	15	6
$m_t$ [ GeV]	1.2	1.0	0.2	0.1
$\sin^2\theta_{\text{eff}}^l$ [ $10^{-5}$ ]	17	17	17	1.3
$R_l^0$ [ $10^{-2}$ ]	2.5	2.5	2.5	0.4
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ [ $10^{-5}$ ]	22 (7)	22 (7)	22 (7)	22 (7)
$M_H (= 120 \text{ GeV})$ [ GeV]	$+56$ ( $+52$ ) [ $+39$ ] $-40$ ( $-39$ ) [ $-31$ ]	$+45$ ( $+42$ ) [ $+30$ ] $-35$ ( $-33$ ) [ $-25$ ]	$+42$ ( $+39$ ) [ $+28$ ] $-33$ ( $-31$ ) [ $-23$ ]	$+27$ ( $+20$ ) [ $+8$ ] $-23$ ( $-18$ ) [ $-7$ ]
$\alpha_s(M_Z^2)$ [ $10^{-4}$ ]	28	28	27	6



- assume  $M_H=120$  GeV by adjusting central values of observables
- improvement of  $M_H$  prediction
  - to be confronted with direct measurement  $\rightarrow$  goodness-of-fit
  - broad minima: Rfit treatment of theo. uncertainties
- GigaZ: significant improvement for  $M_H$  and  $\alpha_s(M_Z^2)$

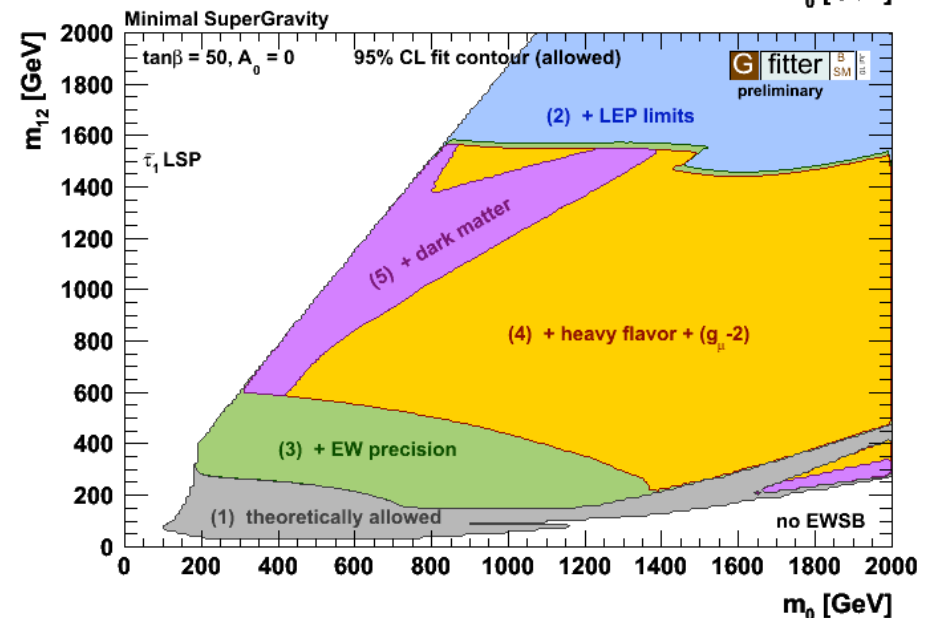
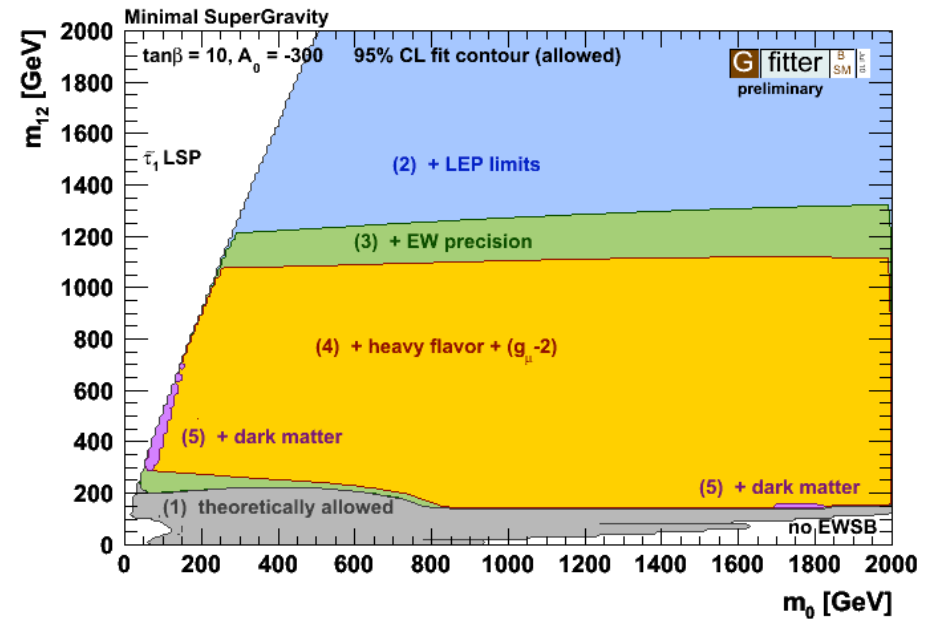
\*[ATLAS, Physics TDR (1999)][CMS, Physics TDR (2006)][A. Djouadi et al., arXiv:0709.1893][I. Borjanovic, EPJ C39S2, 63 (2005)][S. Haywood et al., hep-ph/0003275][R. Hawkins, K. Mönig, EPJ direct C1, 8 (1999)][A. H. Hoang et al., EPJ direct C2, 1 (2000)][M. Winter, LC-PHSM-2001-016]

# mSUGRA: Parameter Scans



[G. Weiglein: arXiv:hep-ph/9712226v1][S. Heinemeyer, W. Hollik, G. Weiglein: arXiv:hep-ph/0412214v1]

- Low  $m_0$  area excluded by requiring a non-charged LSP.
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  5. From the relic density
- 95% CL contours of allowed regions are shown

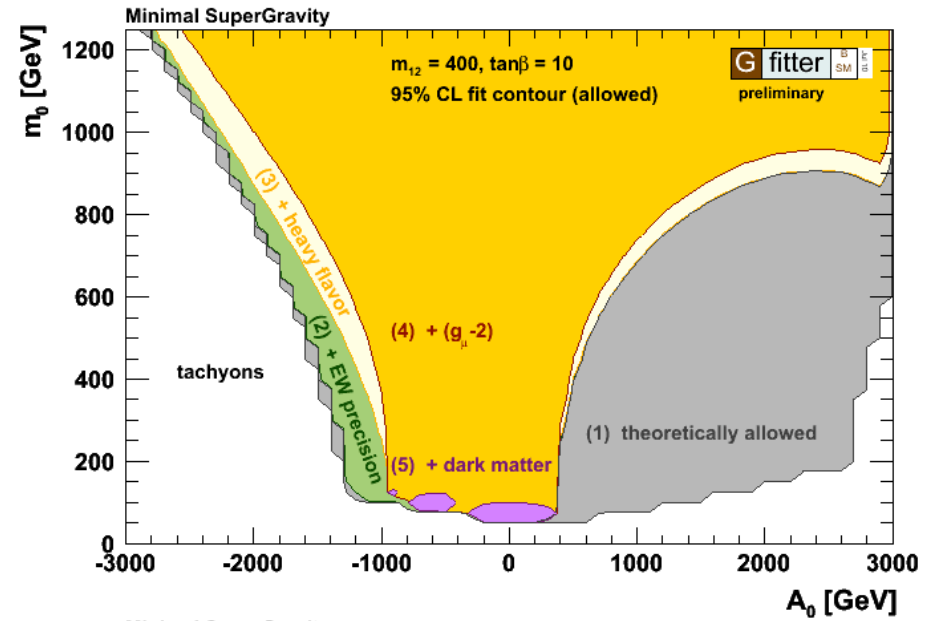
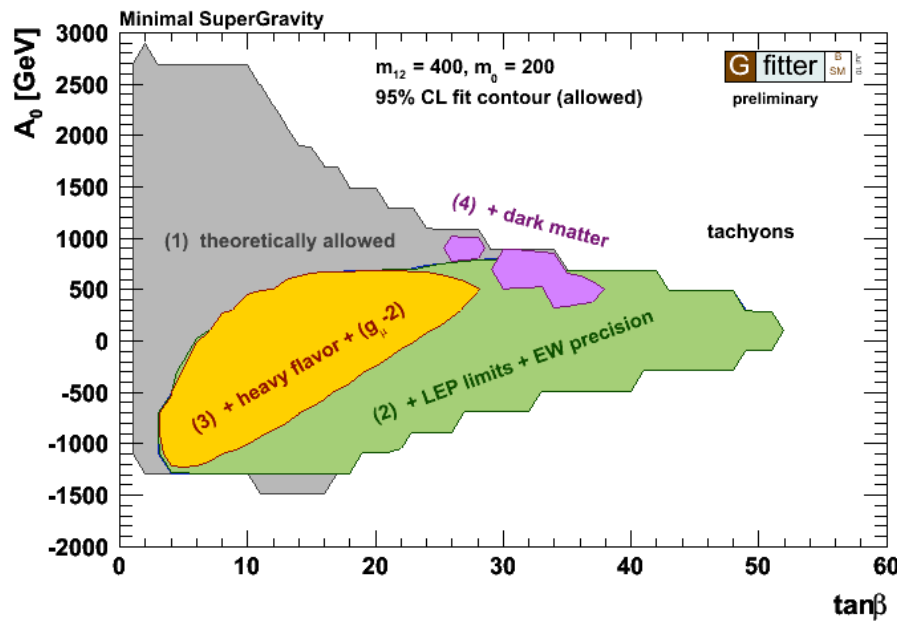




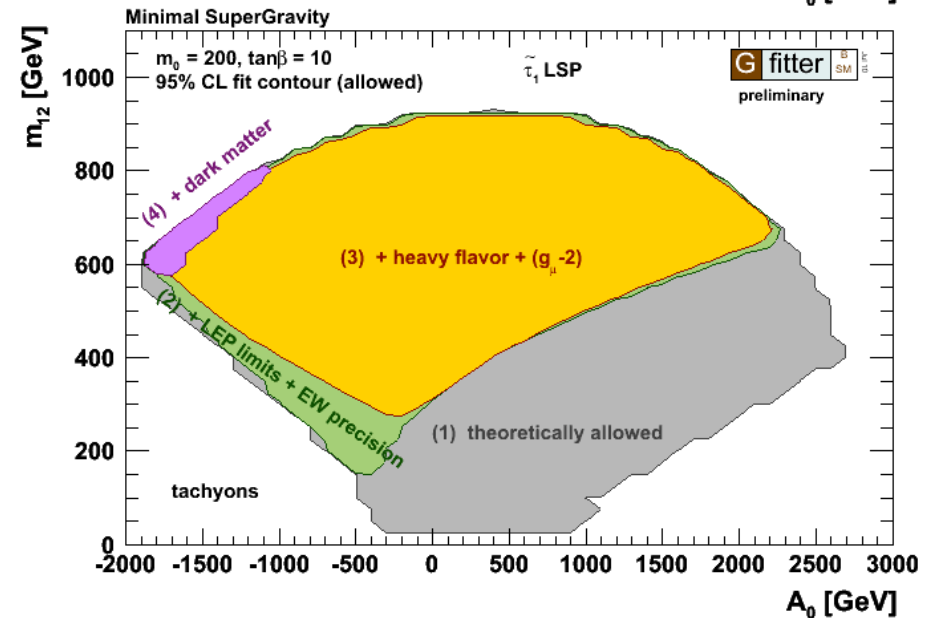
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# Electroweak Fit – Latest Experimental Input



- **Z-pole observables: results from LEP / SLC**  
[ADLO+SLD, Phys. Rept. 427, 257 (2006)]
- **$M_W$  and  $\Gamma_W$  from LEP/Tevatron** [ADLO,CFD+D0: arXiv:0908.1374v1]
- **$m_{\text{top}}$  latest Tevatron average** [CDF&D0: new combination ICHEP'10]
- **$\overline{m}_c$ ,  $\overline{m}_b$  world averages** [PDG, J. Phys. G33,1 (2006)]
- **$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$  including  $\alpha_S$  dependency**  
[Hagiwara et al., PLB649,173,'07]
- **Direct Higgs searches from LEP/Tevatron**  
[ADLO: Phys. Lett. B565, 61 (2003)], [CDF+D0: arXiv:0911.3930]
  - LEP: Higgs strahlung ( $ee \rightarrow ZH$ ,  $H \rightarrow bb$ ,  $\tau\tau$ )
  - Tevatron: gg fusion w/  $H \rightarrow WW$ , ass. prod., VBF
  - **Stat. interpretation in global fit: 2-sided  $CL_{S+B}$**

- Not considered:  $\sin^2\theta_{\text{eff}}$  results from NuTeV (uncertainties from NLO and nucl. effects of bound nucleon PDF) and APV and polarized Möller scattering (exp. accuracy too low)

$M_Z$ [GeV]	$91.1875 \pm 0.0021$	LEP
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	
$R_\ell^0$	$20.767 \pm 0.025$	
$A_{\text{FB}}^{0,\ell}$	$0.0171 \pm 0.0010$	SLC
$A_\ell^{(*)}$	$0.1499 \pm 0.0018$	
$A_c$	$0.670 \pm 0.027$	
$A_b$	$0.923 \pm 0.020$	
$A_{\text{FB}}^{0,c}$	$0.0707 \pm 0.0035$	LEP
$A_{\text{FB}}^{0,b}$	$0.0992 \pm 0.0016$	
$R_c^0$	$0.1721 \pm 0.0030$	SLC
$R_b^0$	$0.21629 \pm 0.00066$	
$\sin^2\theta_{\text{eff}}^\ell(Q_{\text{FB}})$	$0.2324 \pm 0.0012$	
$M_H$ [GeV] <sup>(o)</sup>	Likelihood ratios	LEP & Tevatron
$M_W$ [GeV]	$80.399 \pm 0.023$	
$\Gamma_W$ [GeV]	$2.098 \pm 0.048$	
$\overline{m}_c$ [GeV]	$1.27^{+0.07}_{-0.11}$	LEP & Tevatron
$\overline{m}_b$ [GeV]	$4.20^{+0.17}_{-0.07}$	
$m_t$ [GeV]	$173.3 \pm 1.1$	Tevatron
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ ( $\dagger\Delta$ )	$2769 \pm 22$	
$\alpha_s(M_Z^2)$	–	