

PHYSICS

PHYSICS AT THE TERASCALE





LHC Status

by Helmut Burkhardt / CERN BE/ABP for the LHC team

• introduction

- current LHC status
- recent bunch train commissioning

Helmholtz Alliance

- luminosity optimisation & normalisation
- schedule and next steps this year
- 2011 and beyond

LHC Physics Workshop 2010, Hamburg, 01/10/2010









The CERN accelerator complex : injectors and transfer





Beam parameters determined by injectors size of protons decreases with energy : area $\sigma^2 \propto 1 / E$ Beam size largest at injection, using the full aperture simple rational fractions for synchronization based on a single frequency generator at injection; 25 ns : multiple of 40 MHz

[†]at PS extraction with h=84 for nominal 25 ns



Peak luminosity











2010 : first year of high energy operation

mostly commissioning to safely increase the intensity and luminosity + physics



2010/09/27 11.38



Luminosity production week end of August





Excellent performance in stable physics period in August

Then as planned technical stop in the 1st September week

followed by a major commissioning step :

full commissioning of bunch trains, ± 170 μrad crossing angles in injection + ramp which is the nominal configuration for full LHC intensity with factor 10 increase planned for the rest of this years run ----> more details on this in the following

26-Aug-2010 04:24:46	Fill #: 1303	Energy: 3500 GeV	I(B1): 5.51e+12	I(B2): 5.23e+12
	ATLAS	ALICE	CMS	LHCb
Experiment Status	PHYSIC	NOT READY	STANDBY	PHYSICS
Instantaneous Lumi (ub.s)	^ -1 10.456	5 0.138	10.719	8.882
BRAN Luminosity (ub.s)^	-1 9.573	0.137	7.914	7.327
Fill Lumiosity (nb)^-1	2.0	0.0	2.0	1.7
BKGD 1	0.018	0.019	20.644	0.197
BKGD 2	16.000	0.290	0.002	4.773
BKGD 3	5.000	0.008	0.003	0.106
LHCb VELO Position	Gap: 58.0 mm	STABLE BEAMS	S TOTE	M: STANDBY

Factors left to go to nominal : #bunches 2808/36 = 78; $\beta^* 3.5/0.55 = 6.4$; $E_b 7/3.5 = 2$ together 1000 which gets us to 1.e34 cm⁻²s⁻¹

30-Sep-2010 02:27:38	Fill #: 1381	Energy: 3500 GeV	/ I(B1): 1.55e+1	3 I(B2): 1.56e+13
	ATLAS	ALICE	CMS	LHCb
Experiment Status	PHYSICS	STANDBY	STANDBY	PHYSICS
Instantaneous Lumi (ub.s)^-	-1 48.706	0.000	48.535	45.034
BRAN Luminosity (ub.s)^-1	41.219	0.883	49.887	43.331
Fill Luminosity (nb)^-1	5.5		5.2	4.6

peak luminosity $L \approx 5e31 \text{ cm}^{-2}\text{s}^{-1}$ already within factor 2 of this years goal of 1.e32cm⁻²s⁻¹ Factors left to go to nominal : #bunches 2808/140 = 20 ; $\beta \approx 3.5/0.55 = 6.4$; $E_b 7/3.5 = 2$ together 257 $257 \times 4.9e31 = 1.3e34 \text{ cm}^{-2}\text{s}^{-1}$

Very well corrected machine. Example closed orbit deviation measured around the ring

Bunch trains in the SPS before injection into the LHC

SPS ready to inject (3 or) 4 batches

here each batch with 12 bunches spaced by 150 ns as one of the options these days nominal LHC is 72 bunches per batch spaced by 25 ns

LHC 10/09/2010 after RF adjust at injection :

Complete injection sequence of 13×4 bunches per beam was executed and went smoothly with very little uncaptured beam. This week : 8 bunch inj. + studies 16 bunch injection

Batches in the LHC and abort gap

LHC (1-RING) = 88.924 µs

dump trigger

LHC :

End of 2009 first collisions, mostly at injection energy 2x450 GeV

2010 : commissioning and first year of operation with collisions at high energy;

- already 3.5 pb⁻¹ delivered per high L experiment
- main LHC challenge : damage potential,
- enormous stored energy : nominal is 10 GJ in magnets, 362 MJ in beam
- currently 2.5 GJ in magnets, 10 MJ in beam going up to 20 MJ end of 2010 run
- Now (30/09/10) 150ns_152b_140_16_140_8bpi11inj 152 bunches of which 140 colliding in 1,5,8

	LHC design	now
Momentum at collision, TeV/c	7	3.5
Luminosity, cm ⁻² s ⁻¹	1.0E+34	3.5E+31
Dipole field at top energy, T	8.33	4.17
Number of bunches, each beam	2808	50> 500
Particles / bunch	1.15E+11	1E+11 (up to 1.3E+11)
Typical beam size in ring, μm	200 - 300	300-500
Beam size at IP, µm	17	59

Damage potential : confirmed in controlled SPS experiment

controlled experiment with beam extracted from SPS at 450 GeV in a single turn, with perpendicular impact on Cu + stainless steel target

450 GeV protons

r.m.s. beam sizes $\sigma_{x/y} \approx 1 \text{ mm}$

SPS results confirmed :
8×10¹² clear damage
2×10¹² below damage limit
for details see V. Kain et al., PAC 2005 <u>RPPE018</u>

For comparison, the LHC nominal at 7 TeV : $2808 \times 1.15 \times 10^{11} = 3.2 \times 10^{14} \text{ p/beam}$ at $< \sigma_{x/y} > \approx 0.2 \text{ mm}$ over 3 orders of magnitude above damage level for perpendicular impact

Layout of the LHC

60 m single beam pipe

without crossing angle limited to 156 bunches Crossing angle needed for bunch spacing $< 2 \times 60m$ or < 400 ns avoid encounters closer than $\sim 6 \sigma$ Angle scales with σ or $1/\sqrt{\beta^*}$ and $1/\sqrt{E_b}$ 2×15 parasitic crossings $\pm 58m$ from IP at 7.5 – 13 σ

E _b [TeV]	β* [m]	angle [µrad]	
0.45	10, 11	± 170 µrad	injection+ramp
3.5	3.5	± 100 µrad	current phys.
7.0	0.55	± 142.5 µrad	nominal phys

commissioned now

started 1&5 end of June, now all IPs, 120µrad IP2

Reference numbers, nominal LHC $f_{RF} = 400.7896$ MHz $\lambda_{RF} = 0.748$ m or 2.4951 ns 35 640 RF buckets Bunches spaced by multiples of 25 ns or 10 buckets, allowing for a maximum of 3564 bunches

Gaps required for kicker timing with a 119 bunch abort gap $\sim 3 \ \mu s$ Inject batches of 2, 3 or 4 x 72 bunches 1 batch = 72 bunches total 39×72 = **2808 bunches**

A full LHC turn is 88.9244 μs

Illustration of collisions from few bunches as relevant for current operation

3 batches of 8 bunches each, spacing 150 ns → up to 6 LR interactions per bunch

10/9/2010 Werner Herr et al.

Good news from beam-beam studies :

excellent lifetime with nominal 170 μ rad crossing angle at injection

lifetime started to drop at 90 µrad

100 μrad crossing angle as in physics could still be acceptable – allowing potentially to keep the crossing angle constant through the cycle for this year

Going to operation with crossing angles potentially dangerous -- beam getting much closer to aperture limits just next to the experiments !

Aperture and losses were measured at injection with the crossing angle on Friday 10 Sept.

Measurements of aperture with crossing angle at injection

Looking here at IR4 were aperture is expected to be tighest "n1=7" measured significantly more "n1=10–12"

11/9/2010 R.A. et al.

Conclusion from aperture studies 9-12 Sept. with crossing angles at injection :

- Plenty of aperture at triplets: > 13 σ (n1 > 10)
- Can open tertiary collimators, from 8.5 to 13 σ at injection.
- Can provide 6σ margin to injection and dump protection to fulfill the machine protection and dump requirements.
- \bullet Can stay with 170 μrad crossing angle at injection
- 100 µrad would currently simplify operations but may reduce flexibility in future
- decided to go for 170 μ rad (S. Myers, meeting Sat. morning, 11/09/2010)
- and to open up tertiary collimators at injection from 8.5 to 13 σ
- subject to further tests with beam including asynchronous dump

In addition to these major changes there are other recent changes / improvements :

- Increased ramp speed 10A/s
- Injection steering, transfer lines, collimators re-adjusted
- energy matching and RF adjusts : smother ramp, allow for higher V_{rf} in coast
 3.5-4 MV injection, from 5.5 MV to now ~ 8 MV (max. ~12 MV in 2010) at top energy
- β -beating corrected, for the first time globally with many quadrupoles \rightarrow

β-beating measured and corrected

An estimate from M. Lamont July 2010

Table 2: Projected intensity increases and associated performance in 2010 with around nominal bunch intensity (1.1×10^{11}) . All numbers approximate.

$\begin{array}{c c c c c c c c c c c c c c c c c c c $					
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	l h	hy fa	octo	or	
96 96 $\times 10^{12}$ 5.9 2.9×10^{31} 10 5.1 September 144 1.4×10^{13} 8.9 4.4×10^{31} 10 7.6 October 192 192×10^{13} 11.8 5.9×10^{31} 10 10.1 October		Dy 1a	ii ii	UI	4
$\begin{array}{cccccccccccccccccccccccccccccccccccc$					
192 192 1.9×10^{13} 11.8 5.9×10^{31} 10 10.1 October					
240 240 2.4×10^{13} 14.8 7.3×10^{31} 10 12.7 November					

currently in very active phase of commissioning for a strong increase in intensity with excellent rapid progress – but not much too time for production very hard to predict, max. 8 days in November for protons not excluded we do better than the above estimate (by factor 2-3 ??)

Ambitious schedule : increase #bunches, 2 steps every week, to get to $L = 1.e32 \text{ cm}^{-2}\text{s}^{-1}$

Start n	on-LHC
physics	program

		Apr			May			June					
Wk	13	14	15	16	17	18	19	20	21	22	23	24	25
Мо	28	4	11	18	Easter	2	9	16	23	30	6	Whit 13	20
Tu													
We													
Th					(Ascension			
Fr				G. Friday									
Sa					(
Su					May day				() () () () () () () () () ()				

- Restart 4th February
- 9 months protons, 4 weeks ions
- Integrated luminosity target driven 1 fb⁻¹
- Need to run flat out above 1e32 cm⁻²s⁻¹

Table 4:	e 4: Possible 2011 ball-park scenarios with 1.1×10^{11} protons per bu											
	N_b	β^*	Energy per	Peak Luminosity	Int. Lumi per							
		[m]	beam [MJ]	$[cm^{-2}s^{-1}]$	month $[pb^{-1}]$							
	432	3.5	27	1.3×10^{32}	61							
	432	2.5	27	1.8×10^{32}	85							
	796	3.5	49	2.4×10^{32}	113							
	796	2.5	49	3.4×10^{32}	157							

Getting to nominal (dates indicative)

$$L = \frac{N^2 k_b f}{4\pi\sigma_x \sigma_y} F = \frac{N^2 k_b f \gamma}{4\pi\varepsilon_n \beta^*} F$$

2010	2011	2012	2013	2014	2015	2016				
Energy	3.5TeV			Increase Beam	Energy to 7TeV	,				
β* ο	f 2m	Splices, Collimators in IR3	Decrease β* to 0.55m							
20 of I	nom		Increase k _b to 2808							
Ini	tial		Nominal							
2 1	0 ³²		10 ³⁴							
11	1 D -1		≤ 50 fb ⁻¹ /yr							

Overall strategy beyond 2016 (dates indicative)

2017	2018	2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	2034	2035	etc.
															•	•	•	* 	*
															Increa	ase Be to 16.	eam E 5 TeV	inergy	/
														-					
New interaction region (β*to 0.2m, luminosity leveling)										-									
Increase beam brightness																			
	1114:00															U.E.			
	Ultir	nate						HL-I						HE-LHC					
	2.3	10 ³⁴						5 1	034					2 10 ³⁴					
	≤ 100	fb ⁻¹ /y	r	≤ 200 fb ⁻¹ /yr									≤ 100 fb ⁻¹ /yr						

Luminosity reduction; hourglass effect and crossing angle

Hourglass effect. Relevant when β^* is *x*, *y* $\beta^* = 2 \text{ m}$ decreased close to the bunch length σ_z Define $r = \beta^* / \sigma_z$. Luminosity gets 1. $\beta^* = 0.55 \text{ m}$ reduced. For round beams the factor is *s* [m] - 0.4 0.2 0.4 - 0.2 $H(r) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{\infty} \frac{e^{-s^2}}{1 + s^2/r^2} \, ds = \sqrt{\pi} \, r \, e^{r^2} \, \text{Erfc}(r)$ - 1. H(r)10. 132. 0.999972 LHC nominal 0.999289 2. 26.5 $\sigma_{z} = 7.55 \text{ cm}$ 1. 13.2 0.997174 0.55 7.28 0.990833 or 1 ns for 4σ ; 16 MV currently ~ 1.2 ns, 12 MV **negligible** effect for $\beta^* > 2m$ and still small for nominal β^*

Factor	from cro	ossing a	angle in	one plane (x) : $S = \frac{1}{\sqrt{1+1}}$	$\frac{1}{\left(\frac{\sigma_z}{\sigma_x}\tan\frac{\Phi}{2}\right)^2} \qquad \Phi/2$
σ_x	σ_z	$\Phi/2$	S		
$[\mu m]$	[mm]				
59.3	0.0755	100	0.992	$3.5 \text{ TeV}, \beta^* = 3.5 \text{ m}, \text{July 2010}$	small effect
16.6	0.0755	142.5	0.840	7 TeV, $\beta^* = 0.55 \mathrm{m}$, nominal	

Beam-beam effects

for small x approx. linear kick x' \propto x like quadrupole but same in both planes, defocusing if beam1, 2 have same charge (LHC) and focusing for opposite charge (e+e-, $p\bar{p}$)

tune shift from linear kick

$$\Delta Q_x = -rac{eta_x}{4\pi} rac{\Delta x'}{x}$$

beam2

this maximum tune shift - effective for particles at the bunch centre - is used to quantify the beam-beam effect.

N = bunch population,

 r_c = classical particle (e, p) radius

$$\xi_{x,y} = \frac{r_c \ N \beta_{x,y}^*}{2\pi \gamma \sigma_{x,y} \ (\sigma_x + \sigma_y)} \qquad \begin{array}{c} \text{LEP} \\ \xi_{x,y} \sim .03 - .08 \end{array}$$

LHC round beams, const ε_{N} $\sigma_{x,y} = \sqrt{\beta_{x,y} \epsilon_{N} / \gamma}$ $\xi = \frac{r_{c} N}{4\pi \epsilon_{N}}$ $N \qquad \xi = \frac{N \qquad \xi}{5 \times 10^{9} \quad 0.000163} \\ 4 \times 10^{10} \quad 0.00130 \\ 1.15 \times 10^{11} \quad 0.00374$

at the design emittance $\epsilon_N = 3.75 \ \mu m$ already exceeded by factor 1.5 with N = 1.e11; $\epsilon_N = 2.2 \ \mu m$; $\xi \approx 0.0056$

Beam-beam footprint and tune diagram

Some ref.

W. Herr, M. Zorzano LHC Project Report 462; Tatiana Pieloni thesis

Figures above from S. M. White, H. Burkhardt, S. Fartoukh, T. Pieloni, Optimization of the LHC Separation Bumps Including Beam-Beam Effects WE6PFP018, PAC'09

The overlap area is directly measured in separation scans, pioneered by Simon Van der Meer @ ISR

length scale calibrated displacing both beams using the vertex information from detectors

H.B., R. Schmidt, Intensity and Luminosity after Beam Scraping, CERN-AB-2004-032

Tails measured by extended scans. Limited by aperture. Also possible to measure / reduce with scraping

11:34:26 - Scan Scan562{2010-04-24 11:15:53.918,1058,P5,VERTICAL,3500.0,2.000000087,30,2,0PTIMIZATION,Beam12} inserted successfully

Example for illustration from online data sent by CMS to the CCC Showing a scan by ± 3 nominal σ for CMS in LHC fill 1089 2e10 protons / bunch; single colliding pair

Beam shape very well described by a double gaussian. Low background. No extended tails.

Offline analysis done by the experiments – in close contacts with us : Working groups <u>LBS</u> + <u>LPC</u>, <u>BCNWG</u> on intensity measurement

Overall uncertainty from very first scans ~ 11%, dominated by the uncertainty in the intensity determination

- the first experience from the scans (~ two per experiment) done so far was very promising two different types of uncertainties
- intensity "N1 × N2"; 3-4 % from BCT specification JJ. Gras et al. Beam Instrum. group • luminous region " $\sigma_x \times \sigma_y$ "; very clean nearly Gaussian beams,
- we can hope to get down to 5% in the second round of calibration scans scheduled now using the current LHC beam setup with fewer bunches (~10), moderate bunch intensity (≤ 8e10, matched for good BCT precision); ATLAS + CMS calibration in same fill increase #points in the length scale calibration

Is there an interest to push this further ? -- Recent answer : Yes !! What might be the ultimate precision ? \rightarrow Lumi workshop in Jan 10. week 2011

What about 1% as for the ISR ?G. Carboni et al., Nucl. Phys. B 254 (1985) 697; K. Potter CAS'92Would certainly require much more work and probably extra instruments

One idea exotic -- other ideas welcome Intensity normalisation by proton counting (for example with diamond detectors) when slowly scraped off : 40 MHz × 100 sec = 4×10⁹ protons

Documentation of details in forthcoming PhD thesis : Simon White, Determination of the Absolute Luminosity in the LHC; thesis defense Paris XI, Orsay 11/10/2010

Yngve Levinsen, Study of LHC Experimental Conditions and Machine Induced Detector Backgrounds; Autumn 2011

H.B. and Per Grafstrom; Absolute Luminosity from Machine Parameters, LHC Report 1019 May 2007

IPAC2010 proceedings : First Luminosity Scans in the LHC, <u>MOPEC014</u> Beam-gas Loss Rates in the LHC, <u>TUPEB072</u> Dependence of Background Rates on Beam Separation in the LHC, <u>TUPEB073</u> Characterization of Interaction-Point Beam Parameters .. in the ATLAS Detector at the LHC, <u>MOPEC008</u>

The LHC performs very well in the early physics operation Single beam parameters (intensity, b.b. tune shift) reached nominal parameters The increase in single bunch intensities was rather fast and smooth Potential limitations : beam-beam effects and now the aperture in the presence of crossing angles – less critical then conservative estimates

Next : increase the number of bunches - mostly a challenge for beamprotection including beam-dump and collimation but also : improved and tighter control of many parameters and tolerances, decrease differences between beams and bunches; identify and reduce any sources of blow up pick-up and vibrations

Optimization tools : lumi scans, tunes (and b1, b2 tune split), minimize optics errors like beta beating, transverse damper,

Backup Slides

Nominal 25 ns batch, PS

Batches (or bunch trains) of up to 72 bunches with 25 ns spacing are made in the PS from 6 bunches from Booster, using splitting in 2 steps $6 \times 3 = 18$ $18 \times 4 = 72$

from R. Garoby, Chamonix 2003

75 ns batch, PS

Batches of up to 24 bunches with 75 ns spacing are made in the PS from 6 bunches, double splitting in 2 steps $6 \times 2 = 12$ $12 \times 2 = 24$

Compared to 25 ns : starting from much less intense 6 bunches, from R. Garoby, Chamonix 2003 less blowup in splitting, resulting in similar long. emittance

Gaussian beams of elliptical cross section, beam-beam deflection angle and kicks using Basetti-Erskine function f_{BS}

$$\theta_{0\pm} = \frac{N_{\mp}e^2}{2\pi \,\epsilon_0 \, E_{\pm} \, (\sigma_{x\mp} + \sigma_{y\mp})} = \frac{2N_{\mp}r_c}{\gamma_{\pm} \, (\sigma_{x\mp} + \sigma_{y\mp})}$$
$$\Delta x'_{\pm} - i\Delta y'_{\pm} = -\theta_{0\pm} \, f_{\rm BS}(x_{\pm} - \overline{x}_{\mp}, y_{\pm} - \overline{y}_{\mp}; \sigma_x^{\mp}, \sigma_y^{\mp})$$

Round gaussian beams, $\sigma_x = \sigma_y = \sigma_r \sim$ the case of the LHC

$$\theta_0 = \frac{Ne^2}{2\pi \epsilon_0 E (\sigma_x + \sigma_y)} = \frac{Ne^2}{2\pi \epsilon_0 E 2 \sigma_r} = \frac{Nr_c}{\gamma \sigma_r}$$

 $60 \mu rad LEP2$, measurable, deflection scans 1.4 μrad for nominal LHC parameters visible in RHIC :

$$\Delta r' = -\frac{N e^2}{2\pi\epsilon_0 E} \frac{1 - \exp\frac{-r^2}{2\sigma_r^2}}{r} = -2 \sigma_r \theta_0 \frac{1 - \exp\frac{-r^2}{2\sigma_r^2}}{r}$$

two types of magnetic separation bumps :

parallel separation to avoid collisions in beam preparation, off in physics crossing angle to avoid parasitic collisions, always required for > 156 bunches IR1 : horizontal separation and vertical crossing angle IR5 : vertical separation and horizontal crossing angle

adjust orbits such, that the beam 1 and 2 difference left/right of the IP is the same beams must then collide. This is independent of mechanical offsets and crossing angles

measured with special (beam-) directional strip-line couplers BPMSW, at about L = 21 m left and right of the IP in front of Q1 in each IR. Resolution each plane $\delta_{IP} = \sigma_{BPM}$

Expected resolution for small separation and 0 crossing angle ; in each plane.

- ~ 50 μm using selected, paired electronics; otherwise ~ 100 200 μm beam 1 and beam 2 have separate electronics
- ~10 μ m with extra BPMWF button pick-ups. Installed in 1&5, for large bunch spacing, <u>EDMS</u> doc 976179

Low β insertion ; LHC

 $\beta[m]$ $\beta^* = 0.55 \text{ m}$ 100. г the β -function in a field free region $\beta(s) = \beta^* + \frac{(s - s_0)^2}{\beta^*}$ $\beta^* = 90 \text{ m}$ $\beta^* = 2 \text{ m}$ 80. has a form of a parabola with 60. the beam size of a beam of emittance ε 40. $\sigma = \sqrt{\beta \varepsilon}$ in a dispersion free region is 20 $\beta^* = 11 \text{ m}$ 01 Q1 š⁻ĺm $s_0 = 0$ -20. -10. 10. 20. $\sigma' = \sqrt{\frac{\varepsilon}{\beta}}$ and the angular beam size divergence σ [mm] 1.0 0.8 $\beta^* = 0.55 \text{ m}$ 0.6 $\beta^* = 2 m$ the beam size increases about linearly from the IP to the first 0.4 quadrupole, by a factor s / β^* (for $s >> \beta^*$) 0.2 --> aperture limit for low β^* $\beta^* = 11 \text{ m}$ -20 -10 0 10 20 LHC triplet aperture currently 70 mm (50 mm with screen) upgrade studies --> 130 mm aperture, NbTi for the nominal emittance $\varepsilon_{\rm N} = 3.75 \ \mu m, \quad \varepsilon_{\rm N} = \varepsilon \ \beta \ \gamma$

 $\varepsilon = 0.503 \text{ nm}$ at 7 TeV

Early Heavy Ion Run Parameters

John Jowett

		Early (2010/11)	Nominal
\sqrt{s} per nucleon	TeV	2.76	5.5
Initial Luminosity (L ₀)	cm ⁻² s ⁻¹	1.25 × 10 ²⁵	I 0 ²⁷
Number of bunches		62	592
Bunch spacing	ns	1350	99.8
β*	m	2	0.5
Pb ions/bunch		7×10 ⁷	7×10 ⁷
Transverse norm. emittance	μm	1.5	I.5
Luminosity half life (1,2,3 expts.)	h	τ _{IBS} =7-30	8, 4.5, 3

Initial interaction rate: 100 Hz (10 Hz central collisions b = 0 - 5 fm)

 $\sim 10^8$ interaction/10⁶s (~ 1 month)

Summary of Luminosity progress

Event	TeV	OEF	β*	Nb	lb	ltot	MJ	Nc	Peak luminosity	Date
1	3.5	0.2	10	2	1.00E+10	2.0E+10	0.0113	1	8.9E+26	30 March 2010
2	3.5	0.2	10	2	2.00E+10	4.0E+10	0.0226	1	3.6E+27	02 April 2010
3	3.5	0.2	2	2	2.00E+10	4.0E+10	0.0226	1	1.8E+28	10 April 2010
4	3.5	0.2	2	4	2.00E+10	8.0E+10	0.0452	2	3.6E+28	19 April 2010
5	3.5	0.2	2	6	2.00E+10	1.2E+11	0.0678	4	7.1E+28	15 May 2010
6	3.5	0.2	2	13	2.60E+10	3.4E+11	0.1910	8	2.4E+29	22 May 2010
7	3.5	0.2	3.5	3	1.10E+11	3.3E+11	0.1865	2	6.1E+29	26 June 2010
8	3.5	0.2	3.5	6	1.00E+11	6.0E+11	0.3391	4	1.0E+30	02 July 2010
9	3.5	0.2	3.5	8	9.00E+10	7.2E+11	0.4069	6	1.2E+30	12 July 2010
10	3.5	0.2	3.5	13	9.00E+10	1.2E+12	0.6612	8	1.6E+30	15 July 2010
11	3.5	0.2	3.5	25	1.00E+11	2.5E+12	1.4129	16	4.1E+30	30 July 2010
12	3.5	0.2	3.5	48	1.00E+11	4.8E+12	2.7127	36	9.1E+30	19 August 2010

Maximum reached is 10.7x10³⁰ cm⁻²s⁻¹

calculated

Steve Myers LHCC 22/09/2010