

# Higgs decays in the complex MSSM

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# Outline

- 1 Introduction
  - The Higgs sector of the MSSM
  - Higgs decays
- 2 Higher order corrections
- 3 Preliminary results
  - Formfactors
  - The decay width
- 4 Summary

# The Higgs sector of the MSSM

- In the MSSM, the Higgs sector needs to contain two Higgs doublets, which leads to 5 physical Higgs states:

$$h, H, A, H^+, H^-$$

- At tree level the Higgs sector is described by  $\tan\beta$  and  $M_A$
- The tree level masses  $m_h$  and  $m_H$  are found by diagonalising the Higgs mass matrix

$$M_H^{2,tree} = \begin{pmatrix} M_A^2 \sin^2 \beta + M_Z^2 \cos^2 \beta & -(M_A^2 + M_Z^2) \sin \beta \cos \beta \\ -(M_A^2 + M_Z^2) \sin \beta \cos \beta & M_A^2 \cos^2 \beta + M_Z^2 \sin^2 \beta \end{pmatrix}$$

↓ diagonalisation,  $\alpha$

$$M_H^{2,tree} = \begin{pmatrix} m_H^{2,tree} & 0 \\ 0 & m_h^{2,tree} \end{pmatrix}$$

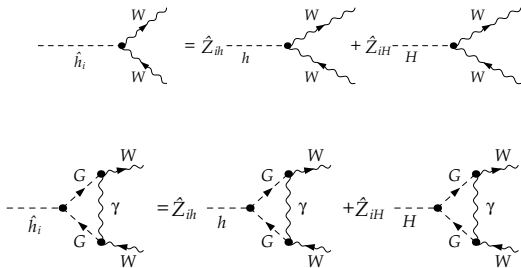
# The MSSM with complex parameters

- In general, some of the parameters of the MSSM can be complex. For instance,
  - gluino mass parameter  $M_3$
  - trilinear coupling parameter  $A$
- When complex phases are included, interesting (non-excluded) phenomenology can result
- Complex phases allow mixing between all three neutral Higgs bosons

$$M(p^2) = \begin{pmatrix} m_h^2 - \hat{\Sigma}_{hh}(p^2) & -\hat{\Sigma}_{hH}(p^2) & -\hat{\Sigma}_{hA}(p^2) \\ -\hat{\Sigma}_{hH}(p^2) & m_H^2 - \hat{\Sigma}_{HH}(p^2) & -\hat{\Sigma}_{HA}(p^2) \\ -\hat{\Sigma}_{hA}(p^2) & \hat{\Sigma}_{HA}(p^2) & m_A^2 - \hat{\Sigma}_{AA}(p^2) \end{pmatrix}$$

# Higgs propagator corrections I

- At tree level there is no CP-violation in the Higgs sector of the MSSM with complex parameters
- Finite wavefunction normalisation factors have been used to give external particles the correct on-shell properties to take Higgs mixing into account



$$\begin{pmatrix} \hat{\Gamma}_1 \\ \hat{\Gamma}_2 \\ \hat{\Gamma}_3 \end{pmatrix} = \hat{Z} \begin{pmatrix} \hat{\Gamma}_h \\ \hat{\Gamma}_H \\ \hat{\Gamma}_A \end{pmatrix}$$

# Higgs propagator corrections II

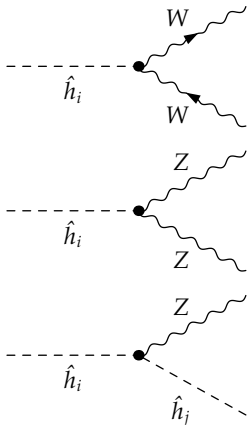
- The non-unitary  $\hat{Z}$  matrix is given by

$$\hat{Z} = \begin{pmatrix} \sqrt{Z_h} & \sqrt{Z_h} Z_{hH} & \sqrt{Z_h} Z_{hA} \\ \sqrt{Z_H} Z_{Hh} & \sqrt{Z_H} & \sqrt{Z_h} Z_{HA} \\ \sqrt{Z_h} Z_{Ah} & \sqrt{Z_A} Z_{AH} & \sqrt{Z_A} \end{pmatrix}$$

- When producing a Higgs  $i$ ,  $\sqrt{Z_i}$  is a normalisation factor (dependent on the  $ij$  propagator), and  $Z_{ij}$  involves the  $ij$  propagator and takes account of diagrams where there is a tree level Higgs  $j$  connected directly to the vertex.
- These corrections can be very important numerically. They are calculated using `FeynHiggs*`, which includes the dominant two-loop contributions as well as the full one-loop corrections.

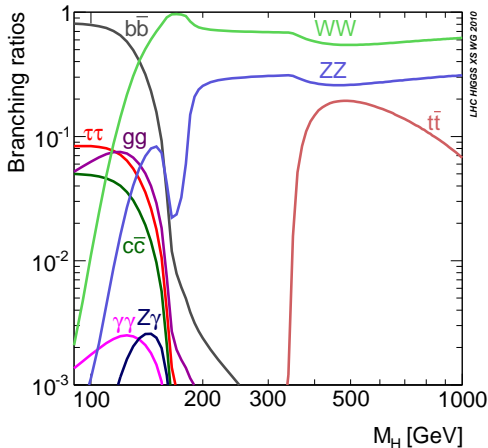
\* `FeynHiggs` can be found at [www.feynhiggs.de](http://www.feynhiggs.de)

# Higgs decays at the LHC



## Branching ratios in the SM\*

\* Figure from: <https://twiki.cern.ch/twiki/bin/view/LHCPhysics/CrossSections>



# Decay widths and formfactors

- Loop corrections to the Higgs vertex can be represented using an effective coupling

$$T^{\mu\nu} = Ag^{\mu\nu} + Bp^\mu q^\nu + C\epsilon^{\mu\nu\rho\sigma} p_\sigma q_\rho$$

- The formfactors  $B$  and  $C$  arising from loop corrections are small – too small to affect the decay width
- The decay width can be considered to be

$$\Gamma \propto |A|^2$$

- By studying the behaviour of the formfactor  $A$ , we can understand the behaviour of the width

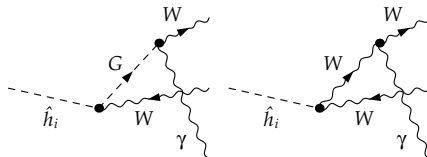


## Virtual corrections

- The programs `FeynArts`, `FormCalc` and `LoopTools`\* have been used in order to calculate the loop corrections
- Masses and weak boson field renormalisation constants are renormalised on-shell, and Higgs field renormalisation constants are calculated in the  $\overline{DR}$  scheme
- The LO result is parametrised in terms of  $\alpha(M_Z)$ , and the charge renormalisation constant is adjusted accordingly

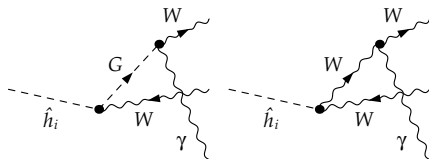
\* Programs can be found at [www.feynarts.de](http://www.feynarts.de)

# Real corrections



$$\begin{aligned}
 \Gamma_{real} &= \Gamma_0 \frac{\alpha}{\pi} \left[ - \left\{ \frac{1 + \beta_0^2}{\beta_0} \log \frac{1 + \beta_0}{1 - \beta_0} - 2 \right\} \log \frac{\lambda^2}{M_W^2 \beta_0} + 2(2 - \log 2) + \right. \\
 &\quad \left. \frac{1 + \beta_0^2}{\beta_0} \left( \text{Li}_2 \frac{2\beta_0}{\beta_0 - 1} - \text{Li}_2 \frac{2\beta_0}{\beta_0 + 1} + \text{Li}_2 \frac{1 - \beta_0}{2} + \frac{1}{2} \log(1 - \beta_0^2) \log \frac{1 + \beta_0}{1 - \beta_0} \right) \right] + \\
 &\quad \frac{M_{h_i} \alpha |S|^2}{16 \sin^2 \theta_w (1 - \beta_0^2)} \frac{\alpha}{\pi} \left[ (\beta_0^4 + \beta_0^2 - \beta_0^6 - 1) \log \frac{1 + \beta_0}{1 - \beta_0} + 2\beta_0^5 + 2\beta_0 - \frac{4}{3} \beta_0^3 \right] \\
 \beta_0 &= \sqrt{1 - \frac{4M_W^2}{M_{h_i}^2}}
 \end{aligned}$$

# Real corrections



In order to include these corrections when considering the formfactors, we let

$$\Gamma_0 \propto |A_0|^2$$

$$\Gamma_{real} \propto K_{real} |A_0|^2$$

# Higgs propagator-type corrections: Improved Born Approximation

- Propagator factors are included at leading order, but the correction is kept strictly at one-loop level

$$|A_{cor}|^2 = |A_{h_2}|^2 + 2\text{Re}[A_{H,tree}^* \Delta A_H]$$

LO:  $\left| \hat{Z}_{ih} \text{---} h \text{---} \begin{array}{c} W \\ \nearrow \\ W \end{array} + \hat{Z}_{iH} \text{---} H \text{---} \begin{array}{c} W \\ \nearrow \\ W \end{array} \right|^2$

# Higgs propagator-type corrections: Improved Born Approximation

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$$|A_{cor}|^2 = |A_{h_2}|^2 + 2\text{Re}[A_{H,tree}^* \Delta A_H]$$

CORN:  $2 \text{Re}$

The diagram shows two Feynman diagrams enclosed in large square brackets. The left diagram is the tree-level process: a dashed line labeled 'H' enters from the left and splits into two wavy lines labeled 'W'. The right diagram is a one-loop correction: a dashed line labeled 'H' enters from the left and splits into two wavy lines labeled 'W'. A loop is formed by a dashed line labeled 'G' and a wavy line labeled 'gamma'.

- This gives a correction of 0 to  $h_3$  decay

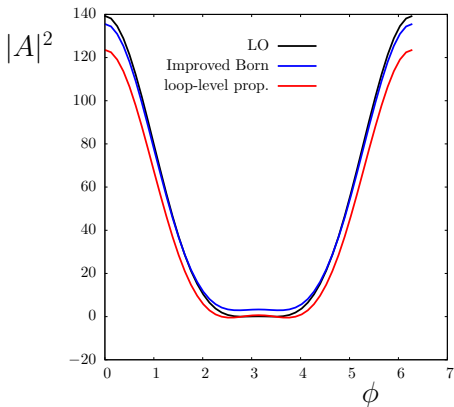
# Higgs propagator-type corrections: At loop level

$\hat{Z}$  factors are applied at loop level as well as at leading order

$$\text{CORN: } 2 \text{ Re} \left[ \hat{Z}_{ih}^h \left( \text{tree-level } h \rightarrow W W \right) + \hat{Z}_{iH}^H \left( \text{tree-level } H \rightarrow W W \right) \right]^* \left[ \hat{Z}_{ih}^h \left( \text{loop-level } h \rightarrow W W \right) + \hat{Z}_{iH}^H \left( \text{loop-level } H \rightarrow W W \right) \right]$$

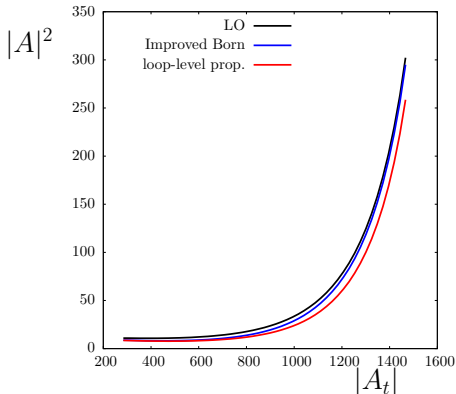
Several methods of applying these corrections were investigated in order to ensure IR-safety

# The effect of propagator-type corrections



$$h_2 \rightarrow W^+ W^-$$

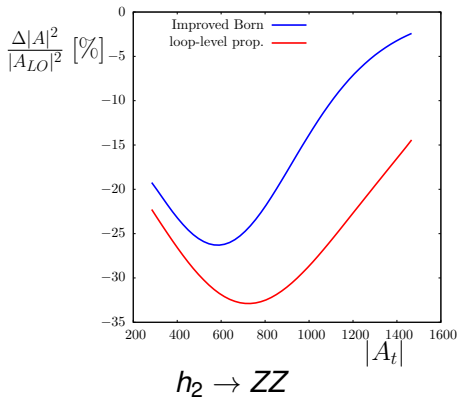
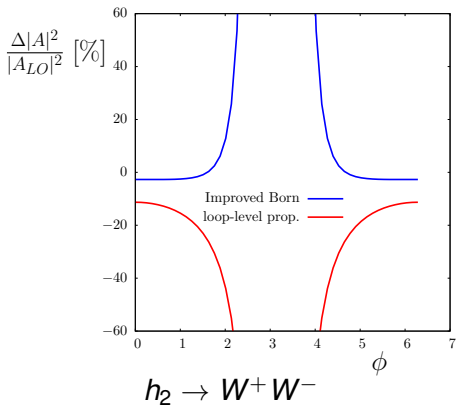
where  $A_t = |A_t| \exp(i\phi)$



$$h_2 \rightarrow ZZ$$

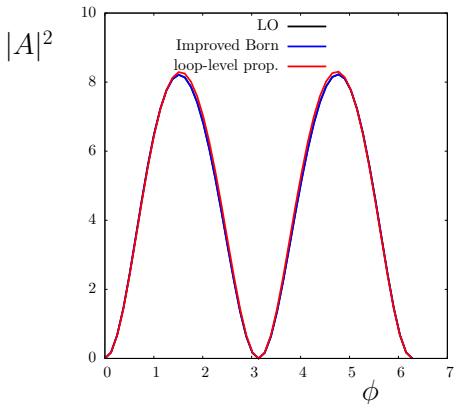
# The effect of propagator-type corrections

The propagator-type contributions can have a dramatic effect on the behaviour of the corrections

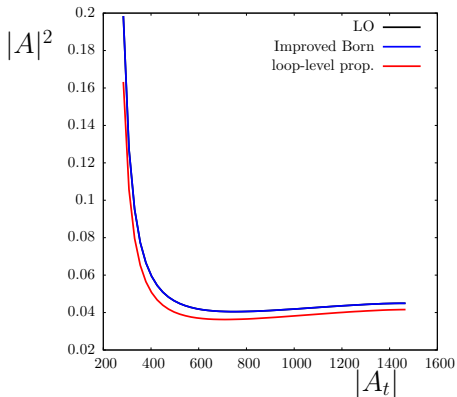




# The effect of propagator-type corrections



$h_3 \rightarrow W^+ W^-$



$h_3 \rightarrow ZZ$

# Scanning over formfactors

- Once interesting 'benchmark' scenarios have been identified, we can scan around these points in order to discover which parameters have the largest effect on the correction

# Parameter Scans

- In order to find the region of parameter space where the cross section (and corrections) are reasonable and which is experimentally allowed, we perform adaptive parameter scans\*
- 9 parameters are varied in order to maximise the size of the corrections
  - $M_{H^\pm}, \tan \beta, M_{SUSY}, m_{\tilde{t}}, \mu, M_2, |A_t|, |M_3|$
  - $\phi$ , where  $A_t = |A_t|e^{i\phi}$  and  $M_3 = |M_3|e^{i\phi}$
- All thresholds are avoided
- HiggsBounds\*\* is used to ensure that the scenario being studied is not already experimentally excluded
- Limits on the sfermion and chargino masses are imposed

\* [hep-ph/04072340](#), O. Brein

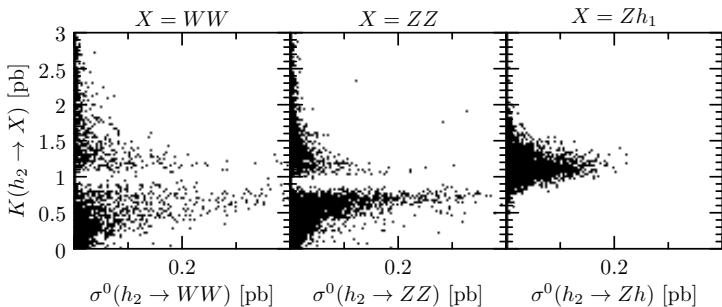
\*\* [arXiv:0811.4169\[hep-ph\]](#), P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein, K.E. Williams

# Parameter Scans: Outlook

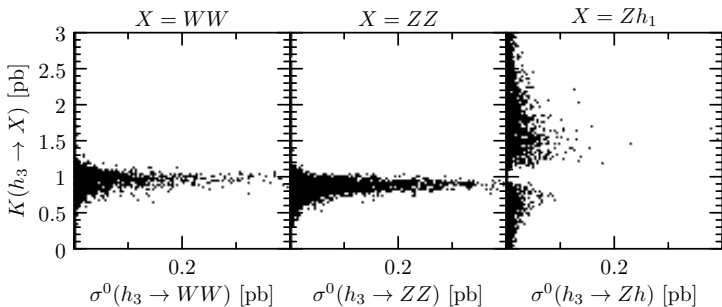
Additions are being made to the parameter scans

- The corrected partial width  $\Gamma_{h_i \rightarrow h_j h_k}$  will be included
- Further limits will be imposed from the electroweak precision data
  - $g_\mu - 2$
  - $\Delta\rho$
  - Electric dipole moments (electron, neutron, mercury)
  - $B \rightarrow X_s \gamma$

# Scans of the decay width for $h_2$



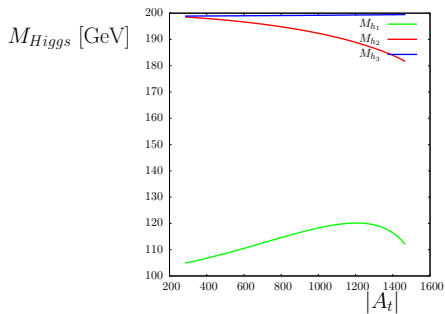
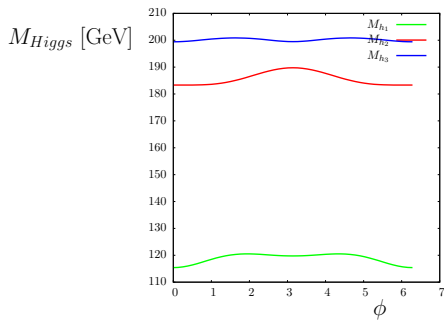
# Scans of the decay width for $h_3$



# Summary

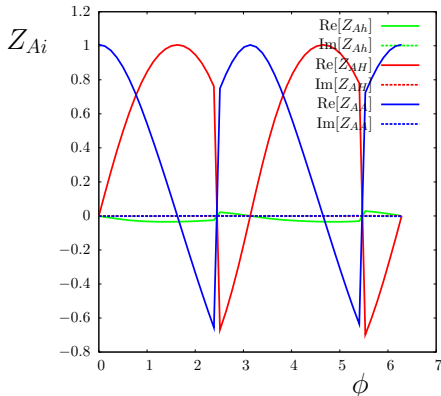
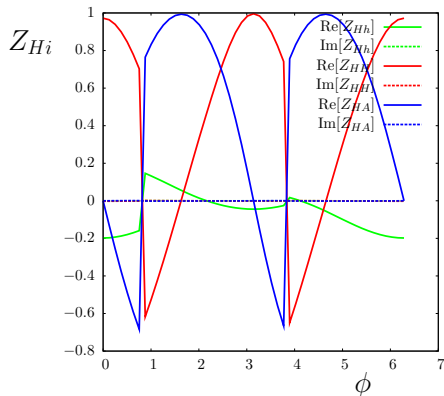
- The decays  $h_i \rightarrow WW$ ,  $h_i \rightarrow ZZ$  and  $h_i \rightarrow Zh_j$  can be important in the complex MSSM
- Mixing between the neutral MSSM Higgs bosons can be very significant – including this effect at loop level can dramatically alter the corrections
- The full corrections to these decays have been calculated and scans are being performed to discover the most interesting areas of parameter space
- The corrections to the decay width can be phenomenologically relevant

# Backup: Higgs masses





# Backup: Propagator factors



# Backup: Propagator factors

