

# Bilinear RPV at ATLAS and ILC

**Benedikt Vormwald**

University of Würzburg  
DESY Hamburg

**4<sup>th</sup> Annual Workshop of the Helmholtz Alliance**  
**„Physics at the Terascale“**

Dresden

Friday, 03. December 2010

**BMBF-Forschungsschwerpunkt**  
**ATLAS Experiment**

Physics on the TeV-scale at the Large Hadron Collider

**FSP 101**  
**ATLAS**



Bundesministerium  
für Bildung  
und Forschung





1. Bilinear R parity violation
2. ATLAS: LSP mass reconstruction using a pure leptonic LSP decay channel
3. ILC: polarized cross sections of e+/e- collider
4. Conclusion/Outlook



- 1. Bilinear R parity violation**
- 2. ATLAS: LSP mass reconstruction using a pure leptonic LSP decay channel**
- 3. ILC: polarized cross sections of e+/e- collider**
- 4. Conclusion/Outlook**

## What is R parity?

- $B$  and  $L$  violating terms allowed in superpotential ( $\Leftrightarrow$ SM)
- $B$  and  $L$  violation never observed (proton decay)  
→ Invent new symmetry which is a combination of  $B$ ,  $L$  (and  $S$ )

$$P_R = (-1)^{3B+L+2S}$$

- SM particles:  $P_R = +1$   
→ SUSY partners:  $P_R = -1$

## Consequences of conservation

- proton decay prohibited
- sparticles can only be produced in pairs
- SUSY decay products contain odd number of LSPs
- LSP absolutely stable



## What is R parity?

- $B$  and  $L$  violating terms allowed in superpotential ( $\Leftrightarrow$ SM)
  - $B$  and  $L$  violation never observed (proton decay)
- Invent new symmetry which is a combination of  $B$ ,  $L$  (and  $S$ )

$$P_R = (-1)^{3B+L+2S}$$

- SM particles:  $P_R = +1$   
 → SUSY partners:  $P_R = -1$

## ~~Consequences of conservation~~

- proton decay prohibited
  - sparticles can only be produced in pairs
  - SUSY decay products contain odd number of LSPs
  - LSP absolutely stable
- just break  $L$  or  $B$
- } holds for **small RPV parameters**
- **LSP decays!**

**BUT**

claim for conservation arbitrary  
from theoretical point of view



W. Porod et. al. arXiv:hep-ph/0011248

## Superpotential

$$W = \underbrace{\mathcal{E}_{ab} \left( h_U^{ij} \hat{Q}_i^a \hat{U}_j \hat{H}_u^b + h_D^{ij} \hat{Q}_i^b \hat{D}_j \hat{H}_d^a + h_E^{ij} \hat{L}_i^b \hat{R}_j \hat{H}_u^a - \mu \hat{H}_d^a \hat{H}_u^b \right)}_{\text{MSSM superpotential}} + \boxed{\mathcal{E}_i \hat{L}_i^a \hat{H}_u^b}$$

bRPV term  
 $i=1..3$

→ Higgs/Slepton-mixing

→ Sneutrinos acquire VEV  $\langle \tilde{\nu}_i \rangle = \nu_i$

→ corresponding RPV soft SUSY breaking term  $L_{soft}^{BRpV} = -B_i \mathcal{E}_{ab} \mathcal{E}_i \tilde{L}_i^a H_u^b$

## masses and mixings of neutral fermions

Basis of neutral fermions:  $\psi^{0T} = (-i\lambda', -i\lambda^3, \tilde{H}_d^1, \tilde{H}_u^2, \nu_e, \nu_\mu, \nu_\tau)$

Mass terms in the Lagrangian are given by:  $L_m = -\frac{1}{2} (\psi^0)^T \mathbf{M}_N \psi^0 + h.c.$

4x4 MSSM neutralino  
mixing matrix

$$\mathbf{M}_N = \begin{pmatrix} M_{\chi^0} & m^T \\ m & 0 \end{pmatrix}$$

4x3 RPV matrix



W. Porod et. al. arXiv:hep-ph/0011248

## Approximate diagonalization of M<sub>N</sub>

$$\mathbf{M}_N = \begin{pmatrix} M_{\chi^0} & m^T \\ m & 0 \end{pmatrix}$$

$\mathbf{M}_N$  can be block-diagonalized for small RPV parameters via the Seesaw-like diagonalization:  $\mathbf{M}_N = \text{diag}(M_{\chi^0}, m_{\text{eff}})$

$$m_{\text{eff}} = -m M_{\chi^0} m^T = \frac{M_1 g^2 + M_2 g'^2}{4 \det M_{\chi^0}} \begin{pmatrix} \Lambda_e^2 & \Lambda_e \Lambda_\mu & \Lambda_e \Lambda_\tau \\ \Lambda_\mu \Lambda_e & \Lambda_\mu^2 & \Lambda_\mu \Lambda_\tau \\ \Lambda_\tau \Lambda_e & \Lambda_\tau \Lambda_\mu & \Lambda_\tau^2 \end{pmatrix}$$

where  $\Lambda_i = \epsilon_i v_d + \mu v_i$  „alignment parameters“

A final diagonalization of  $M_{\chi^0}$  leads to the neutralino masses  $m_{\chi_i^0}$  and a diagonalization of  $m_{\text{eff}}$  leads to one tree level neutrino mass.

W. Porod et. al. arXiv:hep-ph/0011248

## Some results of this model

- **largest neutrino mass** at tree level
- **2 mixing angles** at tree level
- remaining masses/angles at 1-loop-level
- **correct scales** of mass differences  $\Delta m_{ij}^2$

$$m_\nu = \frac{M_1 g^2 + M_2 g'^2}{4 \det M_{\chi^0}} |\vec{\Lambda}|^2$$

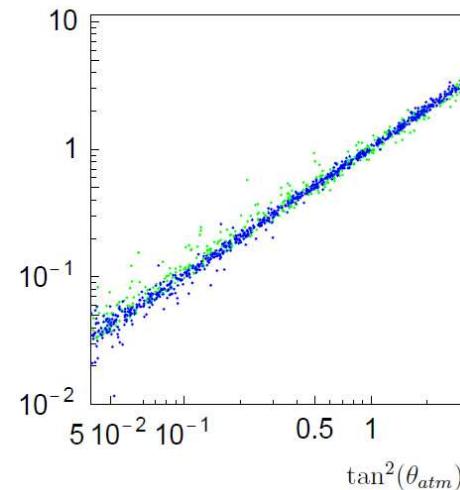
$$\tan \theta_{23} = \frac{\Lambda_\mu}{\Lambda_\tau}$$

$$\tan \theta_{13} = -\frac{\Lambda_e}{\sqrt{\Lambda_\mu^2 + \Lambda_\tau^2}}$$

## How is that connected to colliders?

dominant part of  $\tilde{\chi}_1^0 - W - l_i$  coupling:  $O_i^L = \Lambda_i \cdot f(M_1, M_2, \mu, \tan \beta, v_d, v_u) \propto \Lambda_i$

a)  $\text{Br}(\mu qq')/\text{Br}(\tau qq')$



$$\tan^2 \theta_{23} = \left| \frac{\Lambda_\mu}{\Lambda_\tau} \right|^2 \cong \frac{BR(\tilde{\chi}_1^0 \rightarrow \mu W)}{BR(\tilde{\chi}_1^0 \rightarrow \tau W)}$$

→ Neutrino physics at collider experiments



1. Bilinear R parity violation
2. **ATLAS: LSP mass reconstruction using a pure leptonic LSP decay channel**
3. ILC: polarized cross sections of e+/e- collider
4. Conclusion/Outlook

## (Semi-)leptonic LSP decay channels (@ATLAS benchmark point SU3)

$\tilde{\chi}_1^0 \rightarrow \tau^\pm + e^\mp + \nu$	9 %
$\tilde{\chi}_1^0 \rightarrow \tau^+ + \tau^- + \nu$	24 %
$\tilde{\chi}_1^0 \rightarrow \mu^\pm + \tau^\mp + \nu$	16 %
$\tilde{\chi}_0^1 \rightarrow W + l$	13 %

(data created with Spheno3.0beta36)

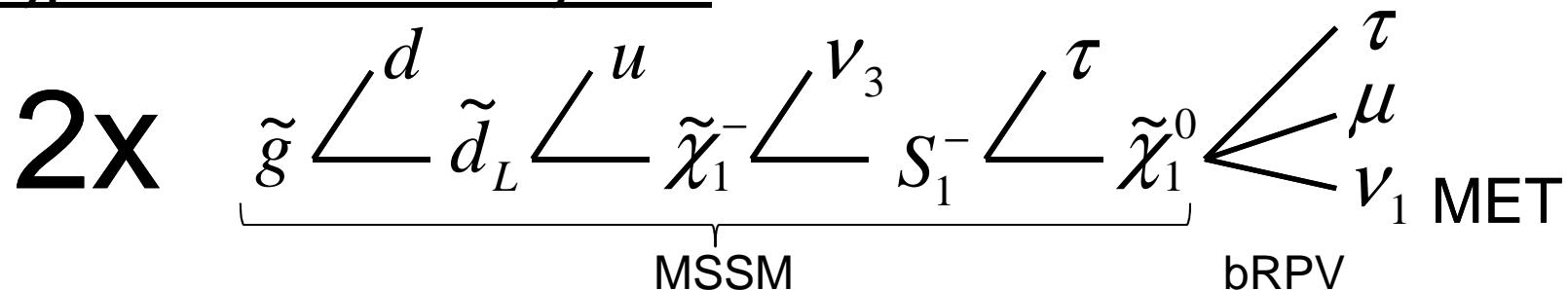
Why muon channel?

→ ATLAS has a very good muon spectrometer!  
→ Working group is interested in muons

Group in Valencia working on  $\tilde{\chi}_1^0 \rightarrow W\mu$

(CERN-ATL-COM-PHYS-2009-543)

## Typical bRPV SUSY decay chain

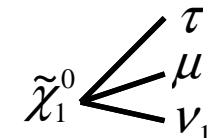


- bRPV (in that case) doesn't affect SUSY cascade
- two cascades with two neutralino decays in each event
- neutralino decays!

## Standard model backgrounds:

- ttbar
- single top
- W+jets
- Z+jets
- WW+WZ+ZZ
- QCD dijets

(officially produced Monte Carlo samples,  
CM=10TeV)



## Reasonable Triggers

**Signal final state signature:**  
mu, tau, missing  $E_T$

mu10	tau20i	tau20i_mu10
------	--------	-------------

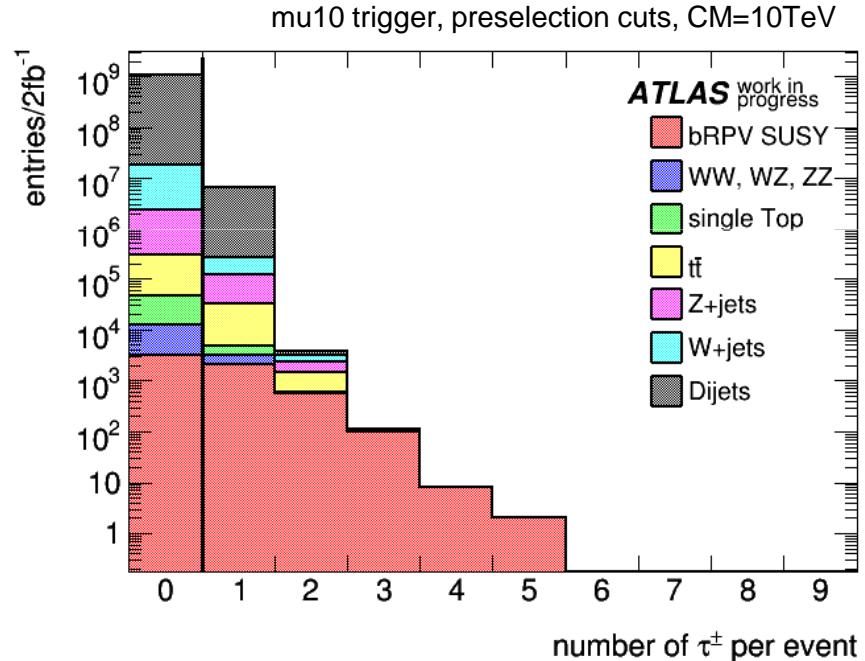
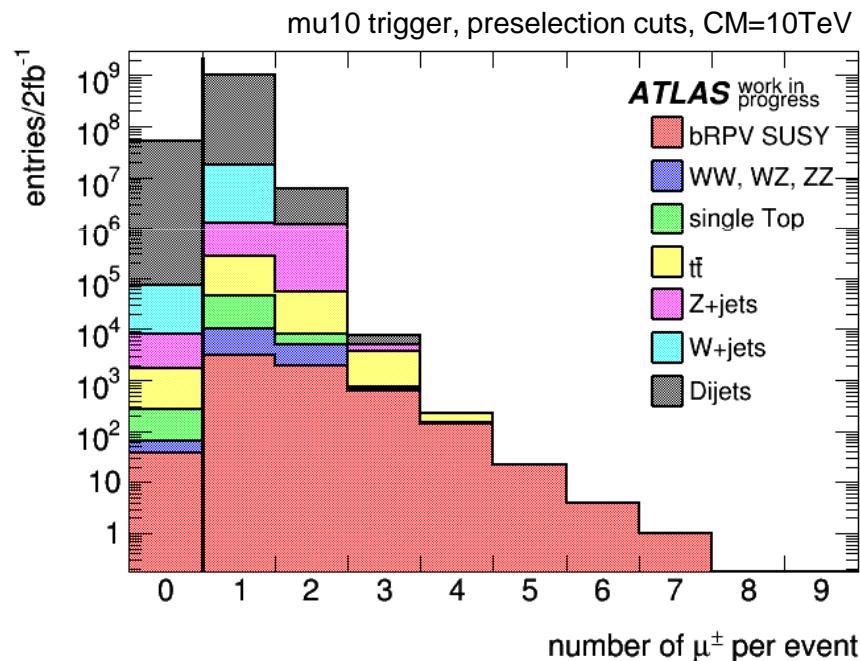
Trigger	Signal eff.	BG eff.
mu10	0.58	$4.15 \cdot 10^{-5}$
tau20i	0.65	$8.81 \cdot 10^{-4}$
tau20i_mu10	0.38	$1.35 \cdot 10^{-6}$

- trigger **mu10** chosen
- available in L31 trigger menu
- very good background reduction

mu10	BG eff.
QCD dijets	$4.1 \cdot 10^{-5}$
W+jets	0.29
Z+jets	0.43
ttbar	0.36
single top	0.30
WW+WZ+ZZ	0.39

## Observables

### Number of mu/tau

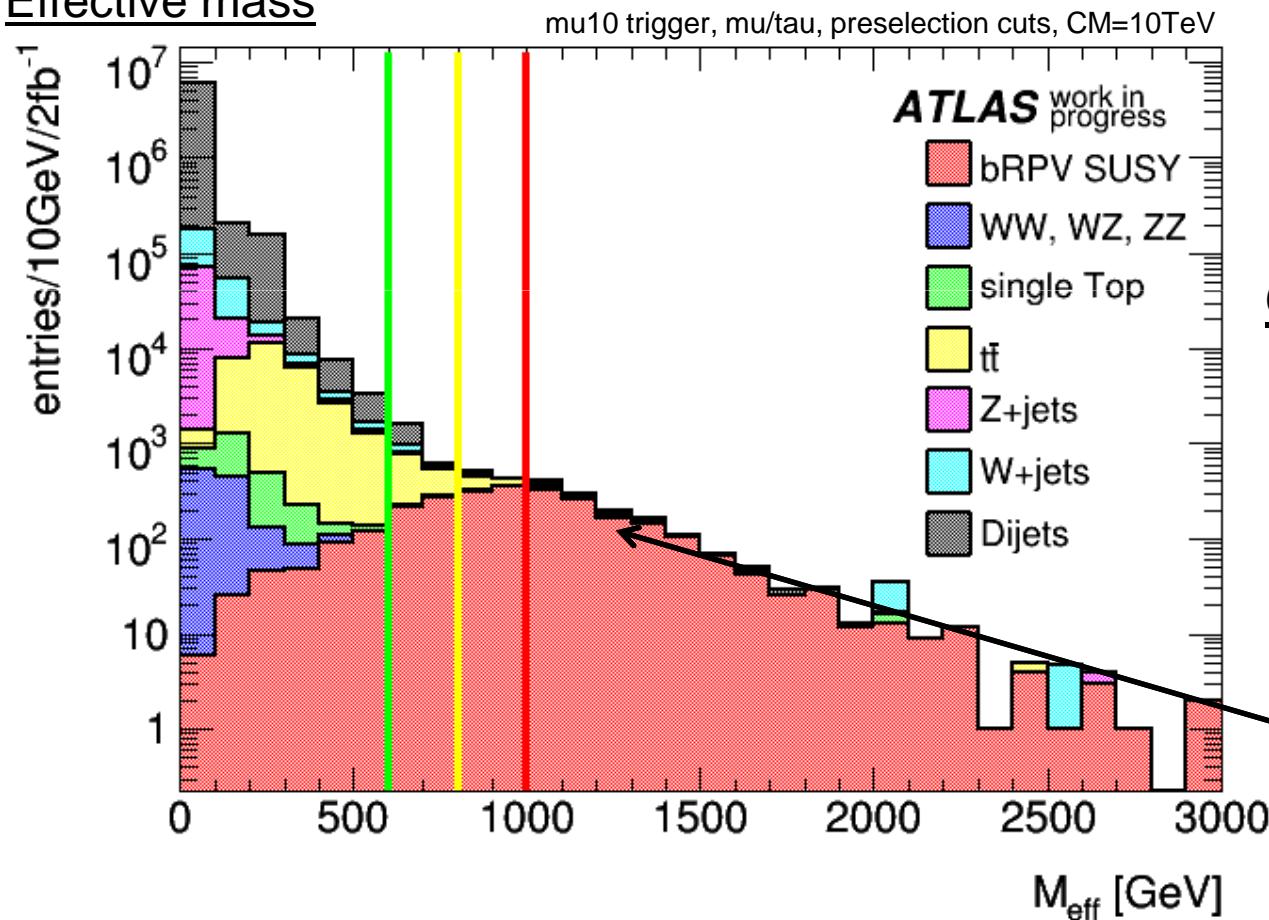


Asking for at least one muon and one tau in final state is very selective!

## Observables

$$M_{eff} = E_T^{miss} + \sum_{1...4} p_T^{jet} + \sum p_T^e + \sum p_T^\mu$$

Effective mass



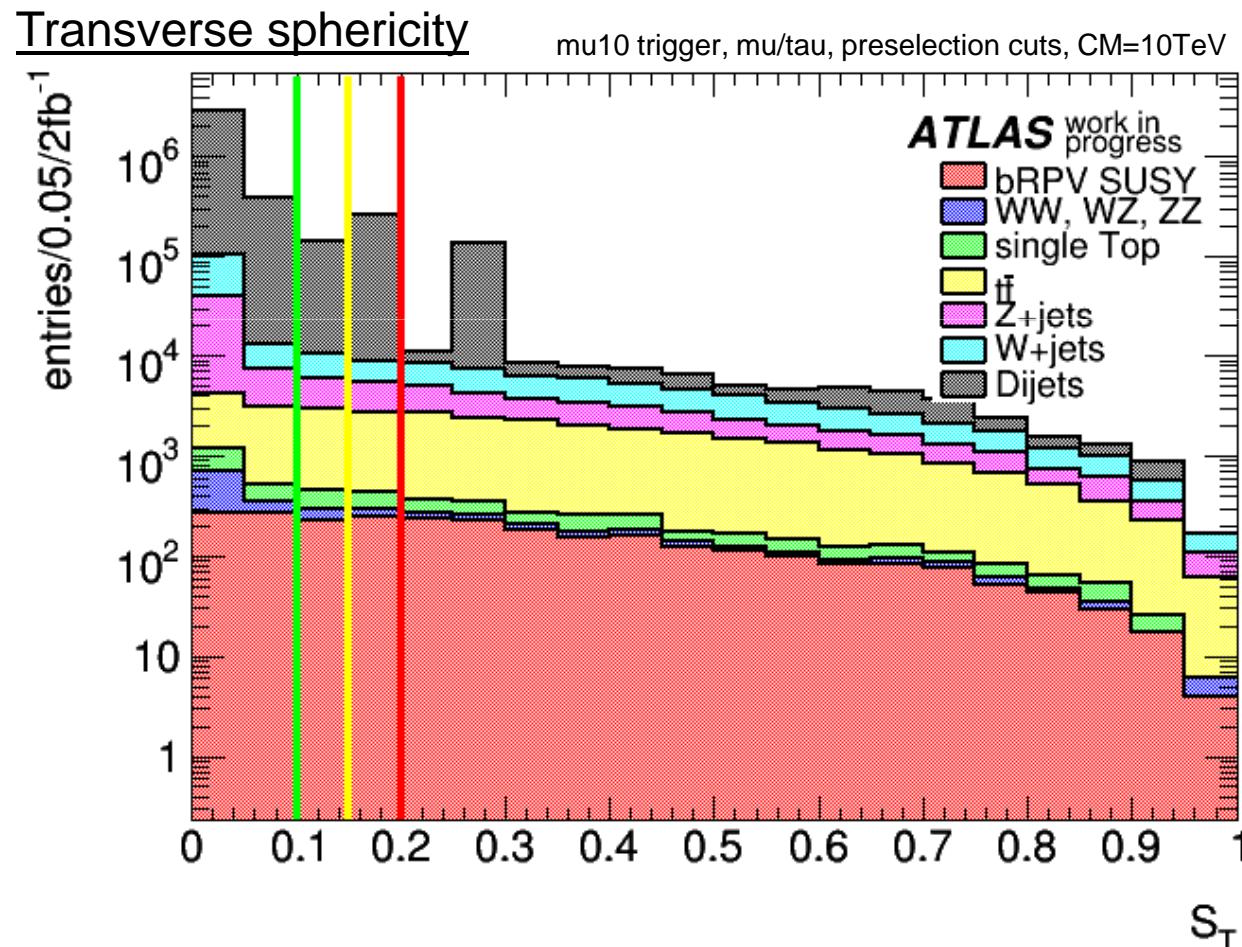
**Cuts:**

- loose:  $M_{eff} > 600 \text{ GeV}$
- medium:  $M_{eff} > 800 \text{ GeV}$
- tight:  $M_{eff} > 1000 \text{ GeV}$

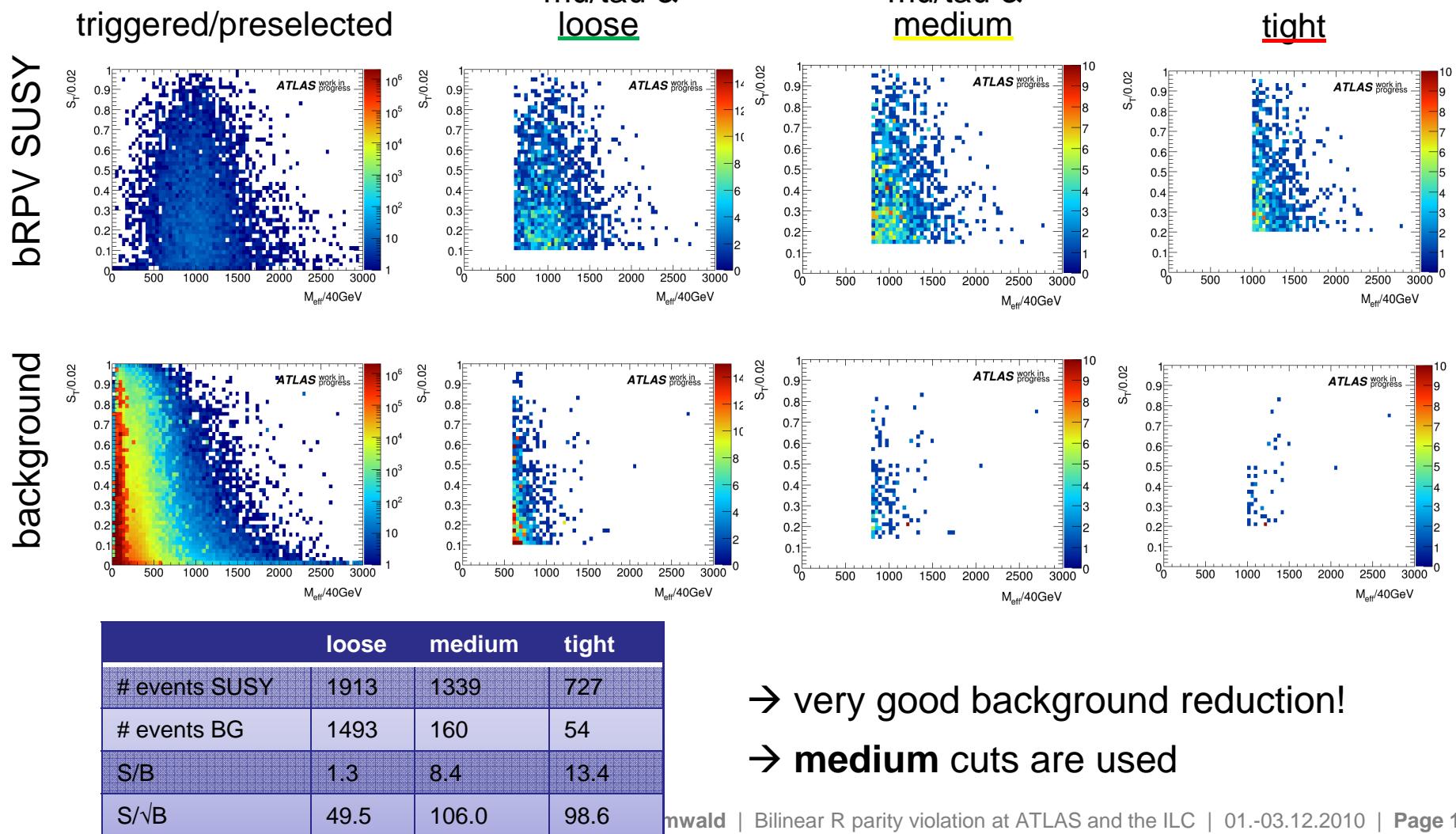
Maximum of (SUSY)  
signal  $M_{eff}$  at higher  
energy

## Observables

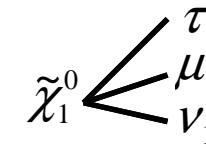
$$S_T = \frac{2\lambda_2}{\lambda_1 + \lambda_2} \quad \lambda_1, \lambda_2 \text{ eigenvalues of sphericity tensor}$$



## Cuts - summary

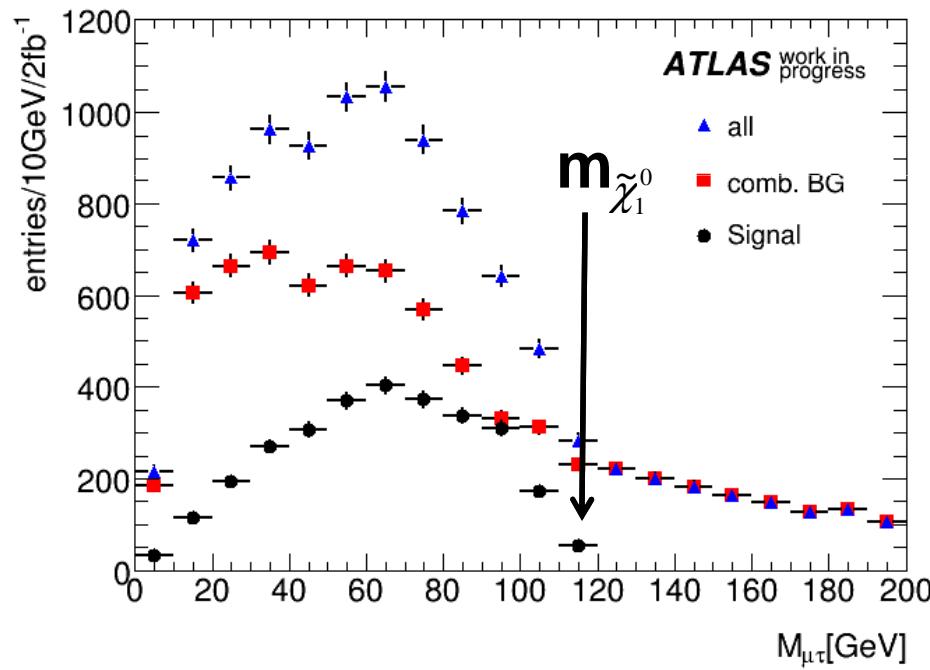


## Signal channel/ SUSY background



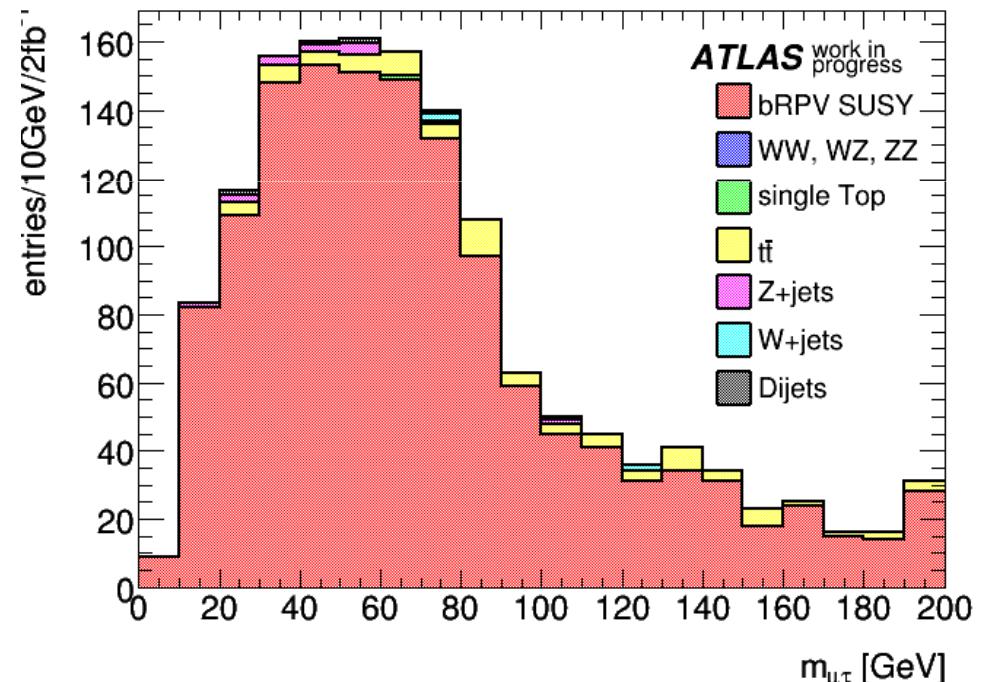
### Calculation of invariant mass of $\mu$ and $\tau$

Truth:



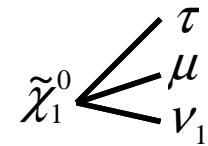
→ dilepton edge (Three-body-decay)

Reco:



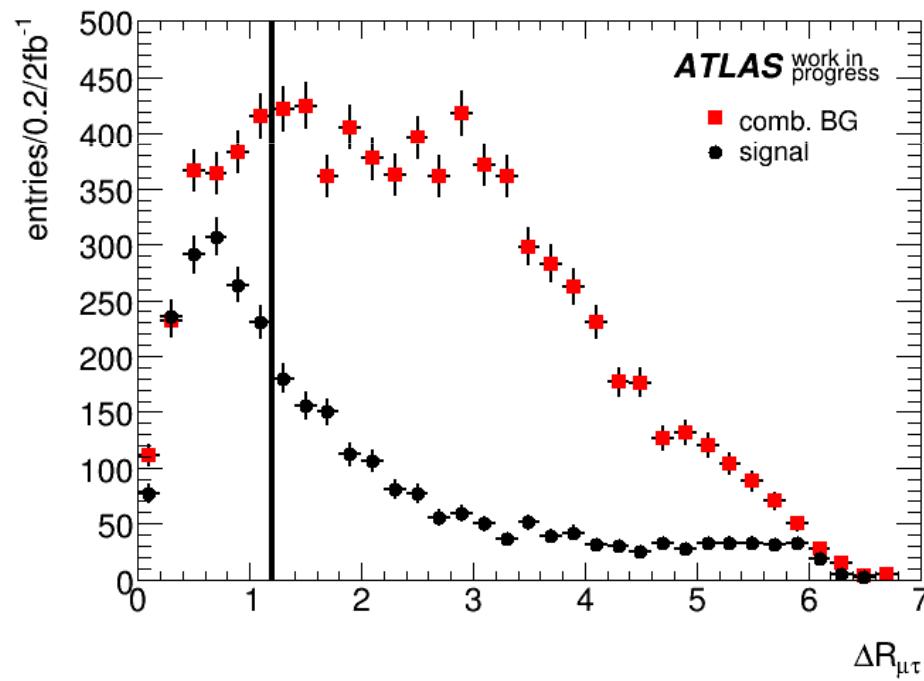
→ reduction of combinatorical BG necessary

## Signal channel/ SUSY background

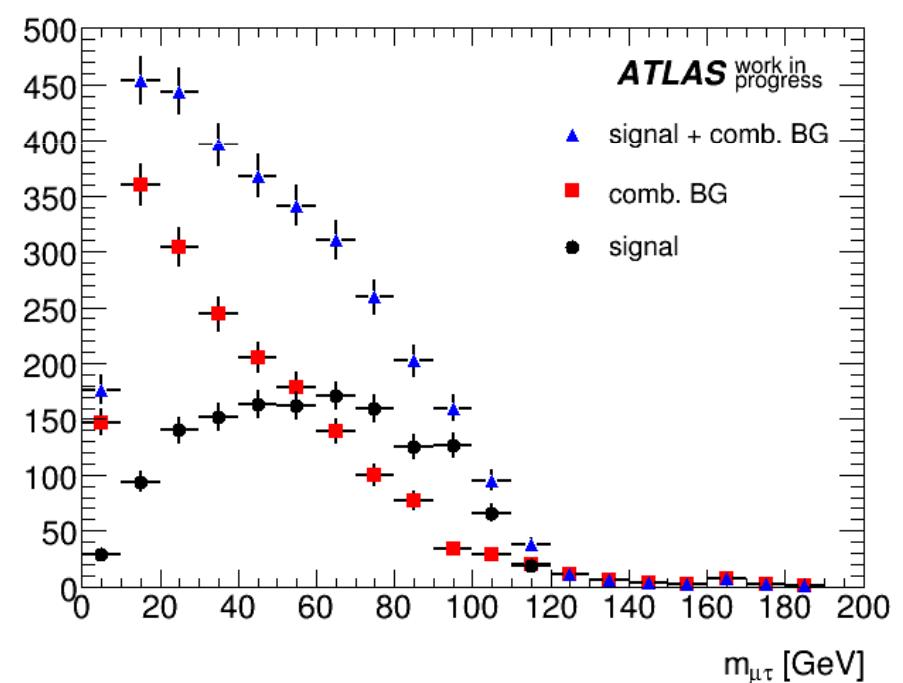


### 1. $\Delta R_{\mu\tau}$ cut for different $\mu\tau$ -pairs (truth)

$\Delta R_{\mu\tau}$  distribution of signal and BG pairs:

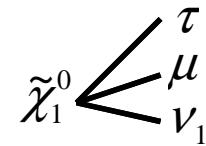


Resulting  $m_{\mu\tau}$  distribution:

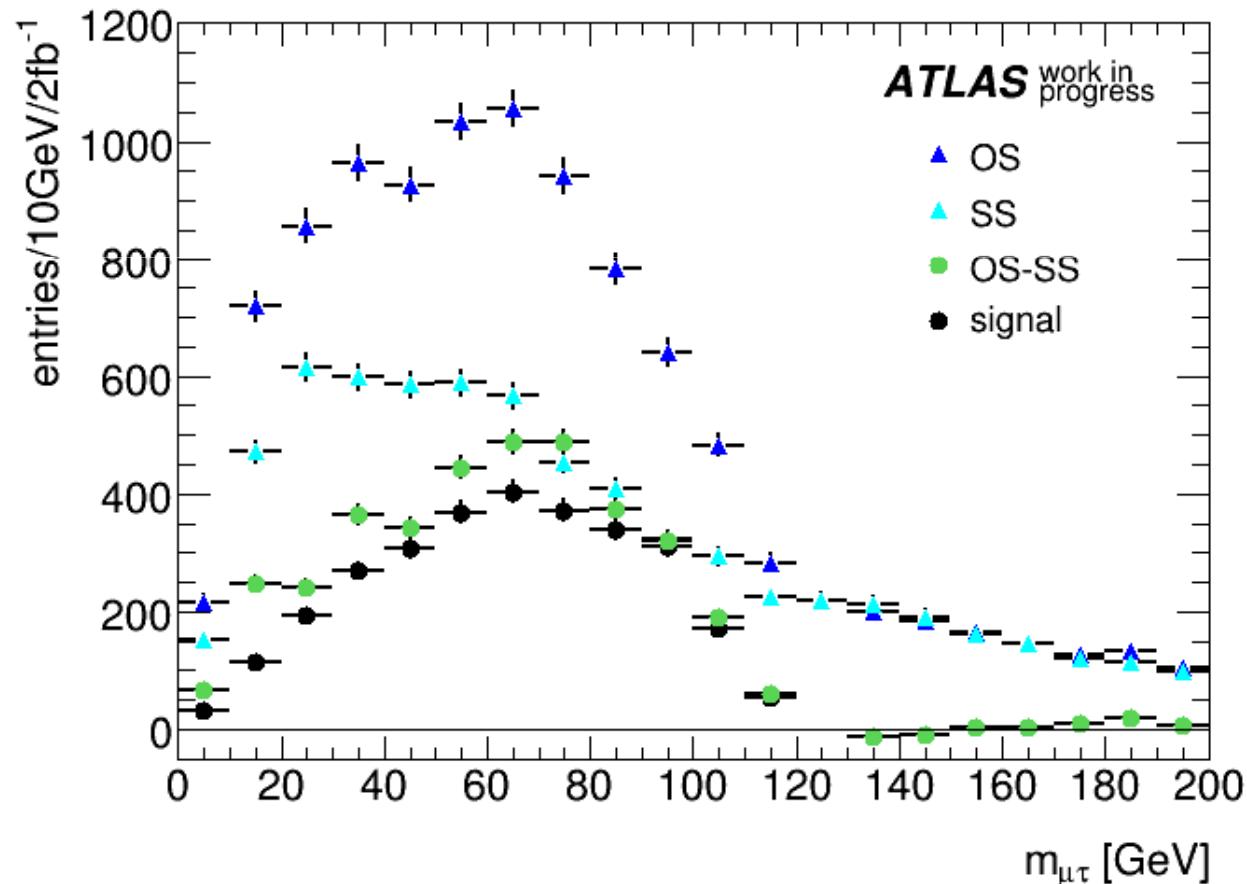


→ reasonable cut:  $\Delta R_{\mu\tau} < 1.2$  ( $\chi$  decay products boosted)

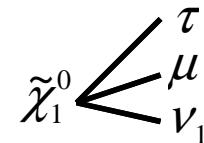
## Signal channel/ SUSY background



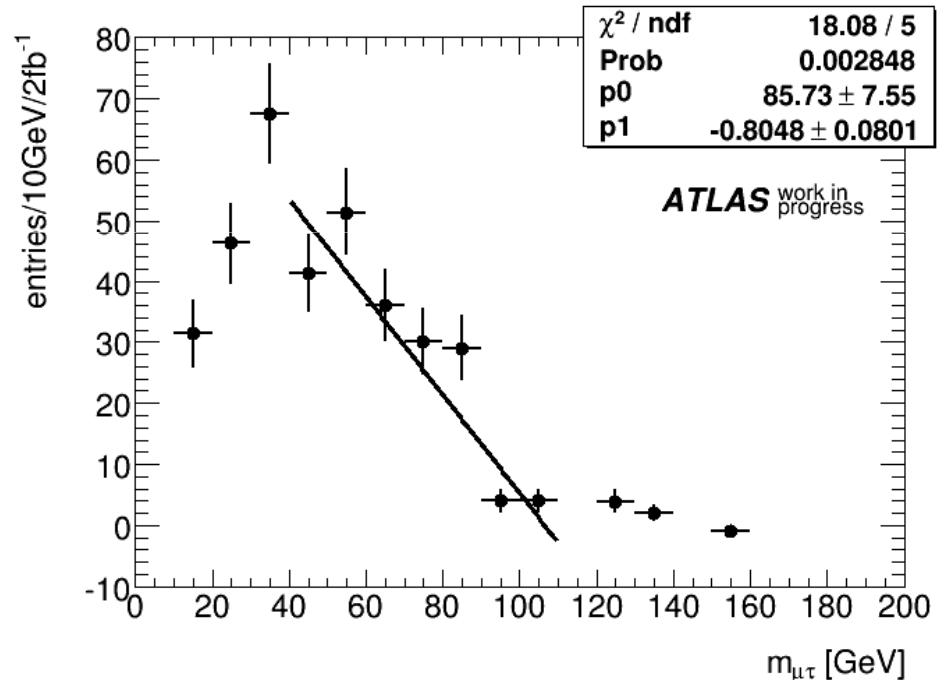
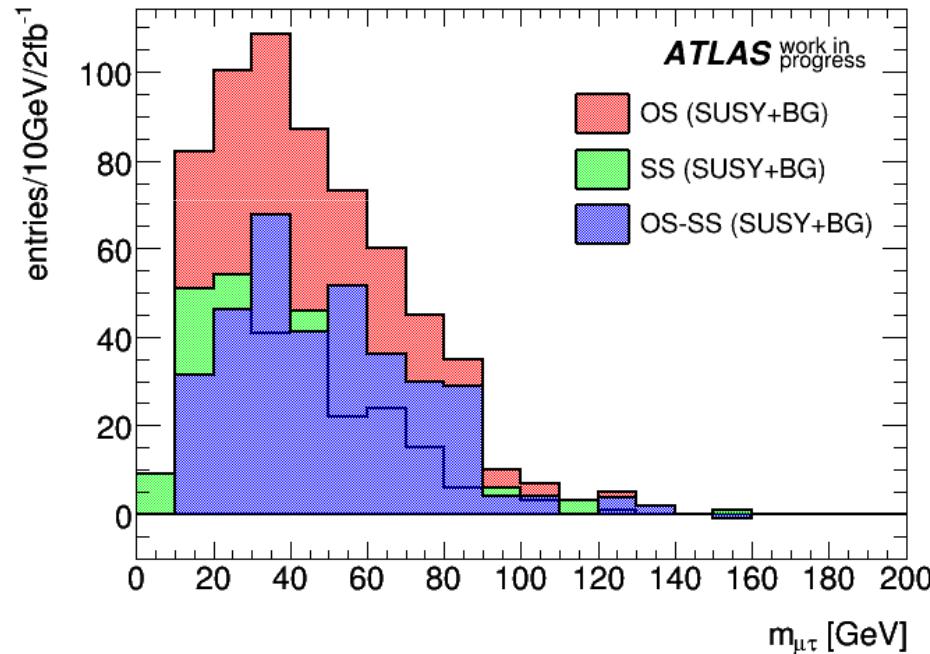
### 2. Opposite sign- same sign subtraction (truth)



## Signal channel/ SUSY background



Invariant mass of  $\mu$  and  $\tau$  after  $\Delta R_{\mu\tau}$  cut and OS-SS subtraction (reco)



Simple linear fit leads to mass-endpoint:

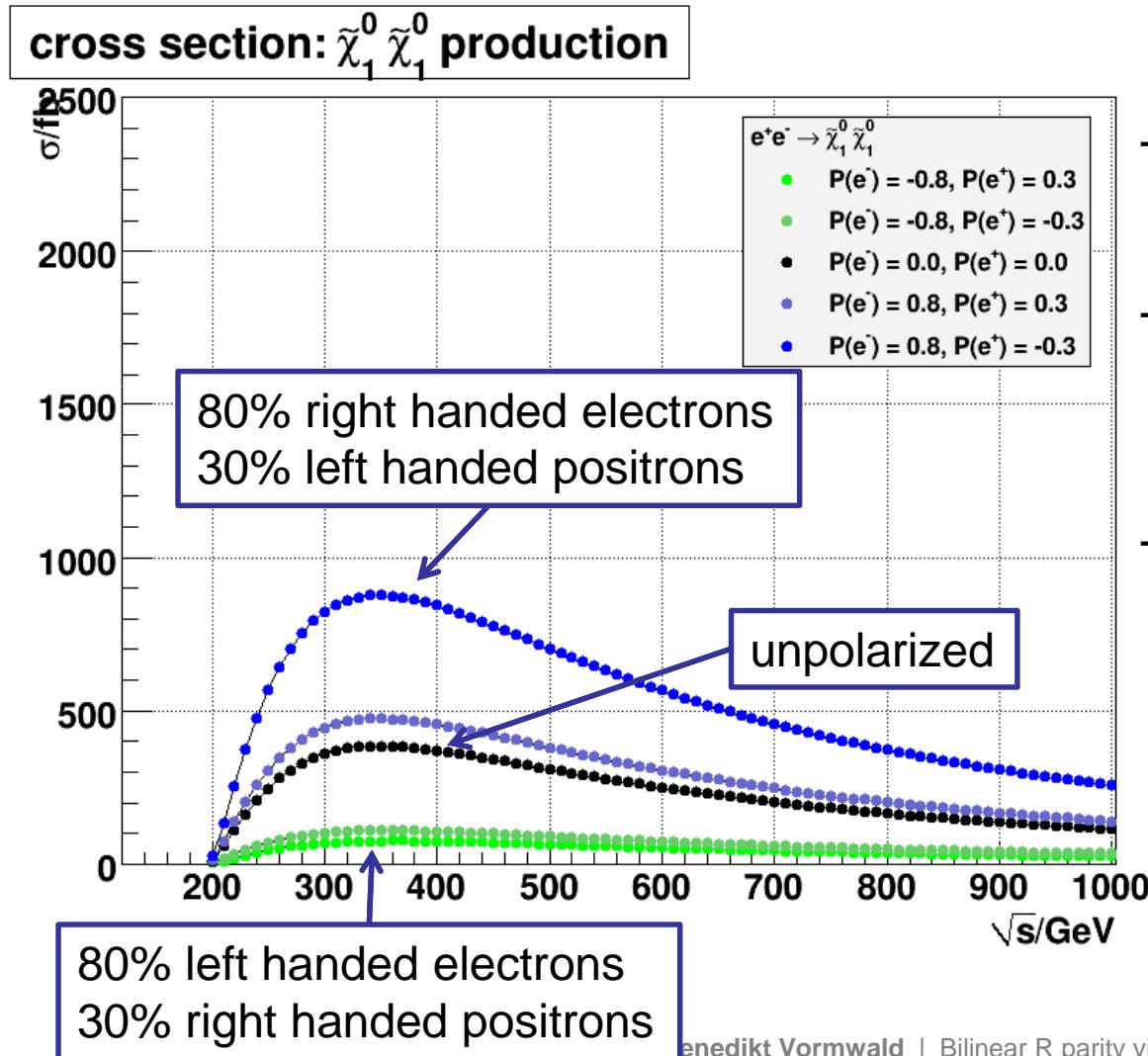
$$m_{\chi}^{EP} = (107 \pm 14) \text{ GeV}$$

$$m_{\chi}^{\text{theory}} = 118 \text{ GeV}$$



1. Bilinear R parity violation
2. ATLAS: LSP mass reconstruction using a pure leptonic LSP decay channel
3. **ILC: polarized cross sections of e+/e- collider**
4. Conclusion/Outlook

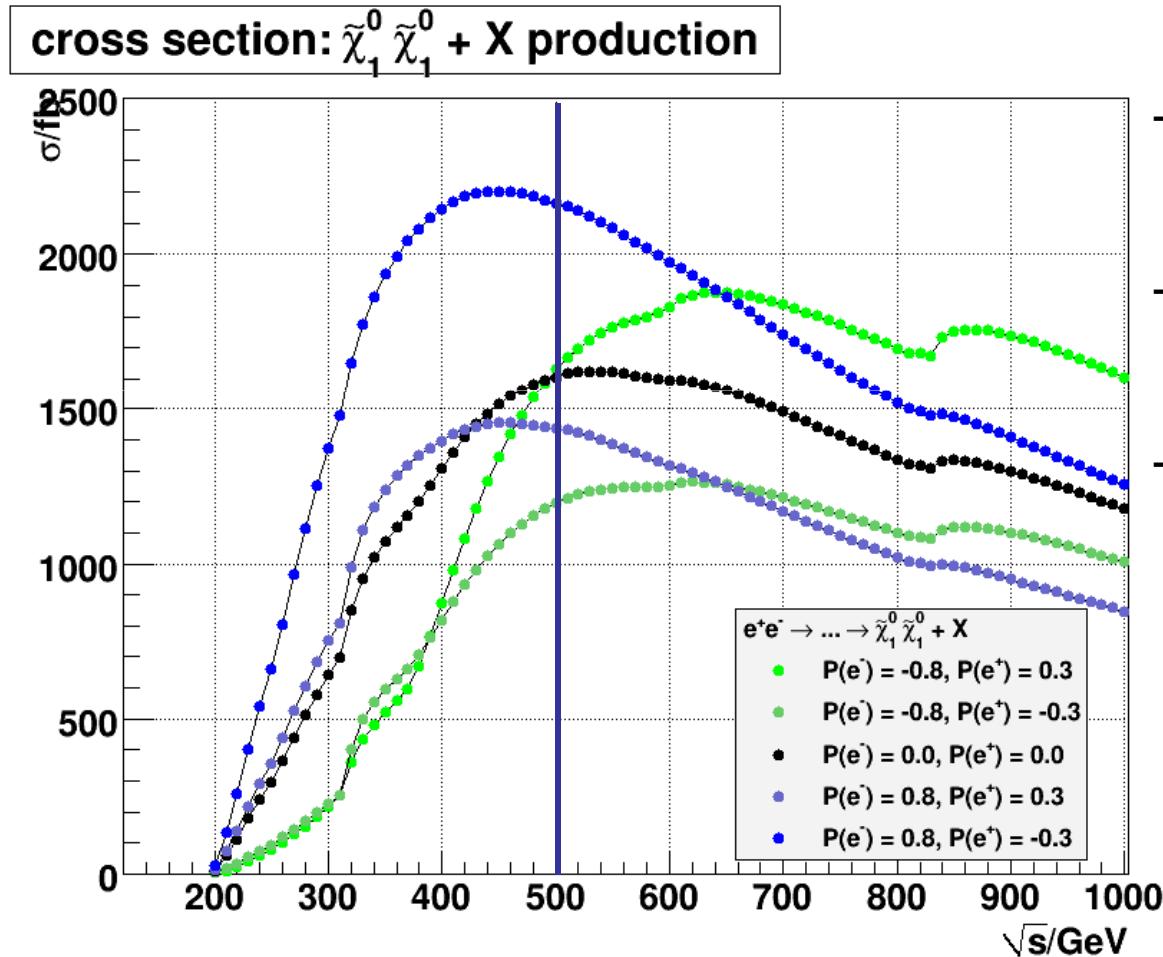
## Production cross section



*Attention: SPS1a'*

- ILC can collide polarized incoming particles ( $\Leftrightarrow$ LHC)
- ILC design parameters:
  - 0.3 (left)  $\leq P(e^+) \leq$  0.3 (right)
  - 0.8 (left)  $\leq P(e^-) \leq$  0.8 (right)
- production cross sections highly dependent on polarization

## Production cross section



- small RPV parameters  
→ LSP decays into SM
- typical SUSY cascades with LSP decay in the end
- almost all sparticle-production processes can be used to study LSP decays

→ ILC design energy: 500GeV

→  $\sigma_{+-}(500\text{GeV}) = 2200 \text{ fb}$



## Most important decay channels of LSP (@SPS1a')

LSP decay	Branching ratio
W $\mu$	0.034
W $\tau$	0.031
$\nu_2 b \bar{b}$	0.035
$\nu_1 \tau e$	0.159
$\nu_1 \tau \mu$	0.279
$\nu_1 \tau \tau$	0.453

}

**Study neutrino parameters**

neutrino mixing, ...

**Study LSP parameters**

mass (endpoint), mixing character, ..

## Decay width of LSP

$$\overline{\Gamma} = 3.77 \cdot 10^{-13} \text{ GeV} \rightarrow \overline{l} \approx 523 \text{ } \mu\text{m}$$

**Displaced vertices expected!**

## Analysis strategy

- Looking for:
- LFV signal
  - two displaced vertices per event (+cascade products from IP)
  - high effective mass per event



## Statistical uncertainties on $\theta_{\text{atm}}$

$\int L dt = 500 \text{ fb}^{-1}$  (4 years of ILC running)

$\sigma_{+-}(500\text{GeV}) = 2200 \text{ fb}$

Detection efficiency = 0.5

$$\rightarrow N_{W\mu} = 37500 \cdot 0.5 = 18750 \quad \sigma_{\text{rel}}^{\text{stat}} = 0.74\%$$

$$\rightarrow N_{W\tau} = 34100 \cdot 0.5 = 17050 \quad \sigma_{\text{rel}}^{\text{stat}} = 0.77\%$$

$$\sigma_{\text{rel}}^{\text{stat}}(\text{Br}(X \rightarrow W\mu) / \text{Br}(X \rightarrow W\tau)) \approx 1\%$$

$$\rightarrow \theta_{\text{atm}} = (46.36 \pm 0.15)^\circ$$

## Signal/background estimation

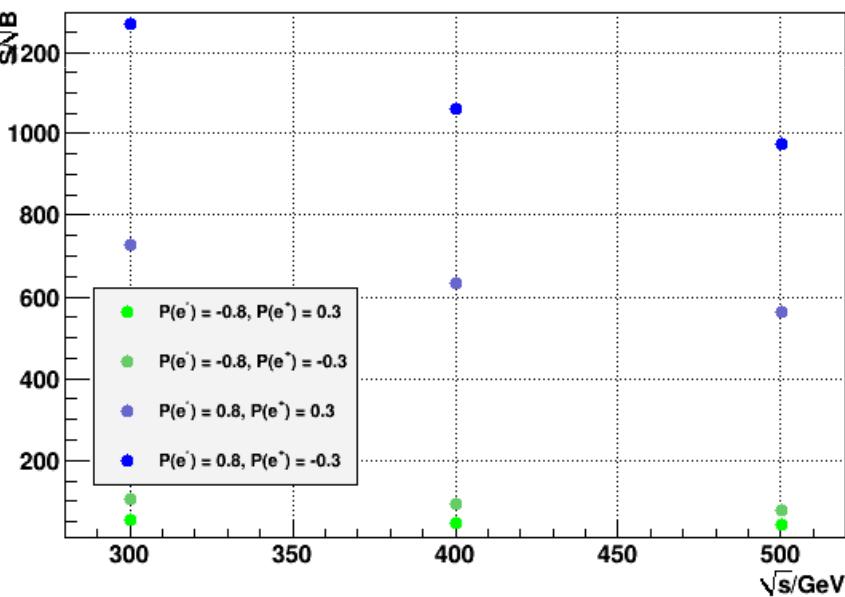
- tree level cross sections for SM BG (Whizard 2.0; arXiv:0708.4233 )
  - just looking for similar final states
- for example:

$$e^+ e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow (\nu\tau\tau)(\nu\tau\mu)$$

$$e^+ e^- \rightarrow SM \rightarrow \tau\tau\tau\nu\mu\nu$$

$$= 3\tau + 1\mu + \text{MET}$$

S/N/B for  $3\tau + 1\mu + \text{MET}$



→ Comparable results for almost all LSP decay channels (at least  $S/\sqrt{B} > 10$ )



1. Bilinear R parity violation
2. ATLAS: LSP mass reconstruction using a pure leptonic LSP decay channel
3. ILC: polarized cross sections of e+/e- collider
4. Conclusion/Outlook



## Conclusion

- bRPV enables access to **neutrino physics at the collider**
- ATLAS detector simulation:
  - **RPV signal should be observable**
  - dilepton edge can be used to **determine the mass of neutralino** (ATLAS)
  - Analysis should be redone at  $\sqrt{s}=7$  TeV (ATLAS)
- ILC case:
  - Polarisation is a very useful tool to increase signal over background (ILC)
  - ILC is highly capable to look at that kind of models

## Outlook

- Implementation of bRPV in Whizard using FeynRules on the way
- Detailed ILC study in progress

# Thank you for your attention!

# References

Romao: *Testing Neutrino Parameters at Future Accelerators.*  
arXiv:hep-ph/0211276v1

Hirsch, Díaz, Porod, Romae, Valle: *Neutrino Masses and Mixings from Supersymmetry with Bilinear R-Parity Violation: A Theory for Solar and Atmospheric Neutrino Oscillations.*  
arXiv:hep-ph/0004115v2

Torro, Mitsou, Garcia: *Probing Bilinear R-Parity Violating Supersymmetry in the Muon plus Jets Channel.*  
ATL-COM-PHYS-2009-543

ATLAS Collaboration: ATLAS CSC Note. Supersymmetry Searches with ATLAS

# Backup Slides



## The model

### Mass matrices

$$M_{\chi^0} = \begin{pmatrix} M_1 & 0 & -\frac{1}{2}g'v_d & \frac{1}{2}g'v_u \\ 0 & M_2 & \frac{1}{2}gv_d & -\frac{1}{2}gv_u \\ -\frac{1}{2}g'v_d & \frac{1}{2}g'v_u & 0 & -\mu \\ \frac{1}{2}gv_d & -\frac{1}{2}gv_u & -\mu & 0 \end{pmatrix}$$

$$m = \begin{pmatrix} -\frac{1}{2}g'v_1 & \frac{1}{2}gv_1 & 0 & \epsilon_1 \\ -\frac{1}{2}g'v_2 & \frac{1}{2}gv_2 & 0 & \epsilon_2 \\ -\frac{1}{2}g'v_3 & \frac{1}{2}gv_3 & 0 & \epsilon_3 \end{pmatrix}$$

W. Porod et. al. [arXiv:hep-ph/0011248](https://arxiv.org/abs/hep-ph/0011248)

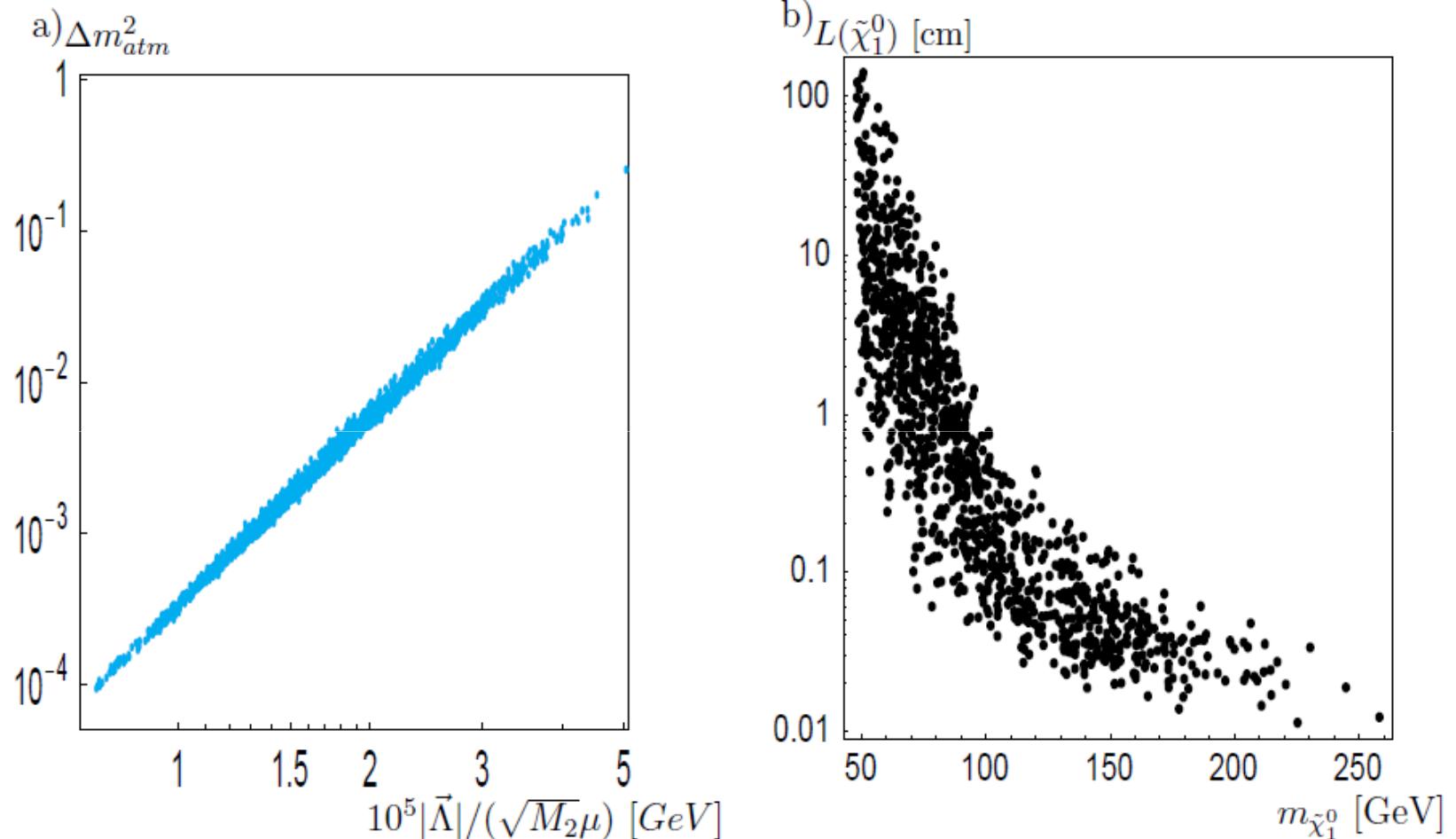


Figure 4: a)  $\Delta m_{atm}^2$  and b) neutralino decay length.

## Benchmark scenarios

### mSUGRA

SUSY has to be broken!      **mSUGRA**      (105 parameters → 5 parameters)

$$M_3 = M_2 = M_1 = m_{1/2}$$

$$\mathbf{m}_{\tilde{Q}}^2 = \mathbf{m}_{\tilde{u}}^2 = \mathbf{m}_{\tilde{d}}^2 = \mathbf{m}_{\tilde{L}}^2 = \mathbf{m}_{\tilde{e}}^2 = m_0 \mathbf{1} \quad m_{H_u}^2 = m_{H_d}^2 = m_0^2$$

$$\mathbf{a}_u = A_0 \mathbf{y}_u \quad \mathbf{a}_d = A_0 \mathbf{y}_d \quad \mathbf{a}_e = A_0 \mathbf{y}_e$$

$$\tan \beta$$

$$\text{sgn}(\mu)$$

**Planck scale**

SUSY spectrum & couplings

**electroweak scale**

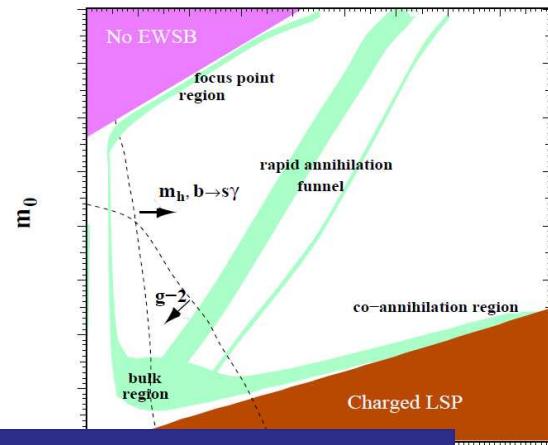
**RGE**  
*SPheNo 3.0*

(W. Porod ,  
arXiv:hep-ph/0301101)

## Benchmark scenarios

SUSY benchmark points

Special benchmark points for ATLAS:



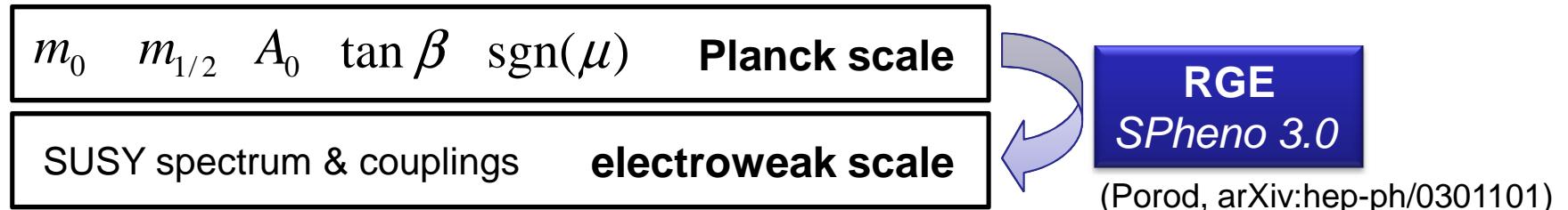
Name	$m_0$ [GeV]	$m_{1/2}$ [GeV]	$A_0$ [GeV]	$\tan \beta$	$\text{sgn } \mu$	Characteristics
<b>SU1</b>	70	350	0	10	+	Coannihilation region
<b>SU2</b>	3550	300	0	10	+	Focus point region
<b>SU3</b>	100	300	-300	6	+	Bulk region
<b>SU4</b>	200	160	-400	10	+	Low mass point
<b>SU6</b>	320	375	0	50	+	
<b>SU8.1</b>	210	360	0	40	+	Funnel region
<b>SU9</b>	300	425	20	20	+	

(ATLAS CSC Note)

## Phenomenology

### mSUGRA

SUSY has to be broken!      **mSUGRA**      (105 parameters → 5 parameters)



### Comparison of SU benchmark points for LSP decay

#### **SU benchmark points**

- ATLAS specific mSUGRA benchmark scenarios
- SU3 chosen for analysis

Name	Characteristics	$m_{\chi^{10}} [\text{GeV}]$	Decay length [ $\mu\text{m}$ ]
SU1	Coannihilation region	139	124
SU2	Focus point region	120	2037
SU3	Bulk region	118	291
SU4	Low mass point	60	$102 - 10^3$
SU6		152	408
SU8.1	Funnel region	145	314
SU9		173	20



## Phenomenology

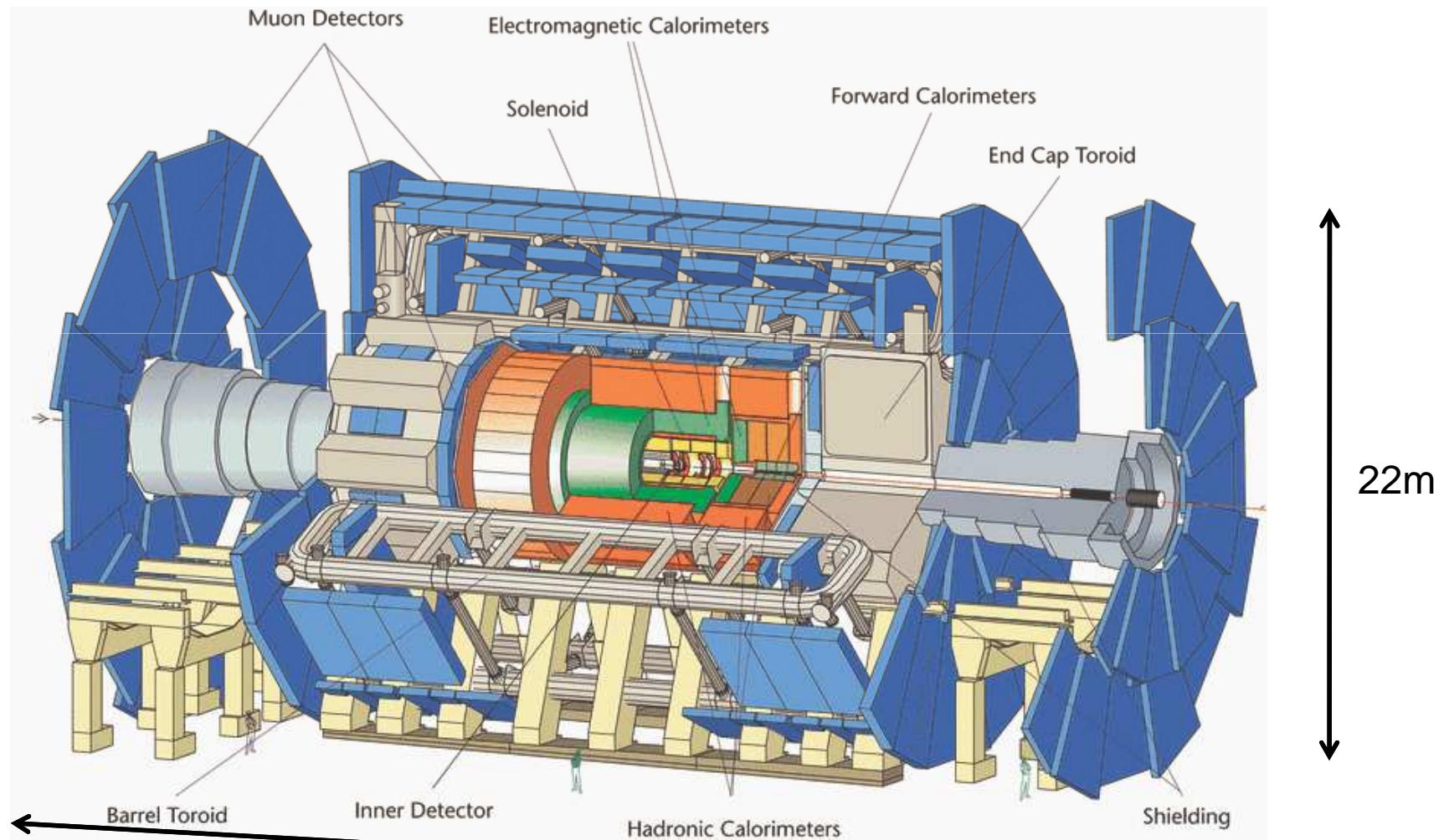
### Comparison of SU points for LSP decay

Chosen LSP-decay to investigate:  $\tilde{\chi}_1^0 \rightarrow \mu^\pm + \tau^\mp + \nu$

Name	$m_{\chi^{10}}$	Decay length [m]	BR(2BD)	BR(3BD- non/semilept.)	BR(3BD- leptonic)	BR( $\chi^{10}$ $\rightarrow \tau \tau \nu$ )	BR( $\chi^{10}$ $\rightarrow \mu \tau \nu$ )
SU1	139	$1,2 \cdot 10^{-4}$	0,32	0,02	0,66	0,33	0,10
SU2	120	$2,0 \cdot 10^{-3}$	0,85	0,09	0,06	0,01	0,01
SU3	118	$2,9 \cdot 10^{-4}$	0,46	0,05	0,49	0,25	0,08
SU4	60	0,1	~0	0,36	0,64	0,30	0,08
SU6	152	$4,1 \cdot 10^{-4}$	0,73	0,01	0,26	0,14	0,03
SU8.1	145	$3,1 \cdot 10^{-4}$	0,48	0,01	0,51	0,28	0,06
SU9	173	$2,0 \cdot 10^{-5}$	0,88	0,01	0,11	0,06	0,01

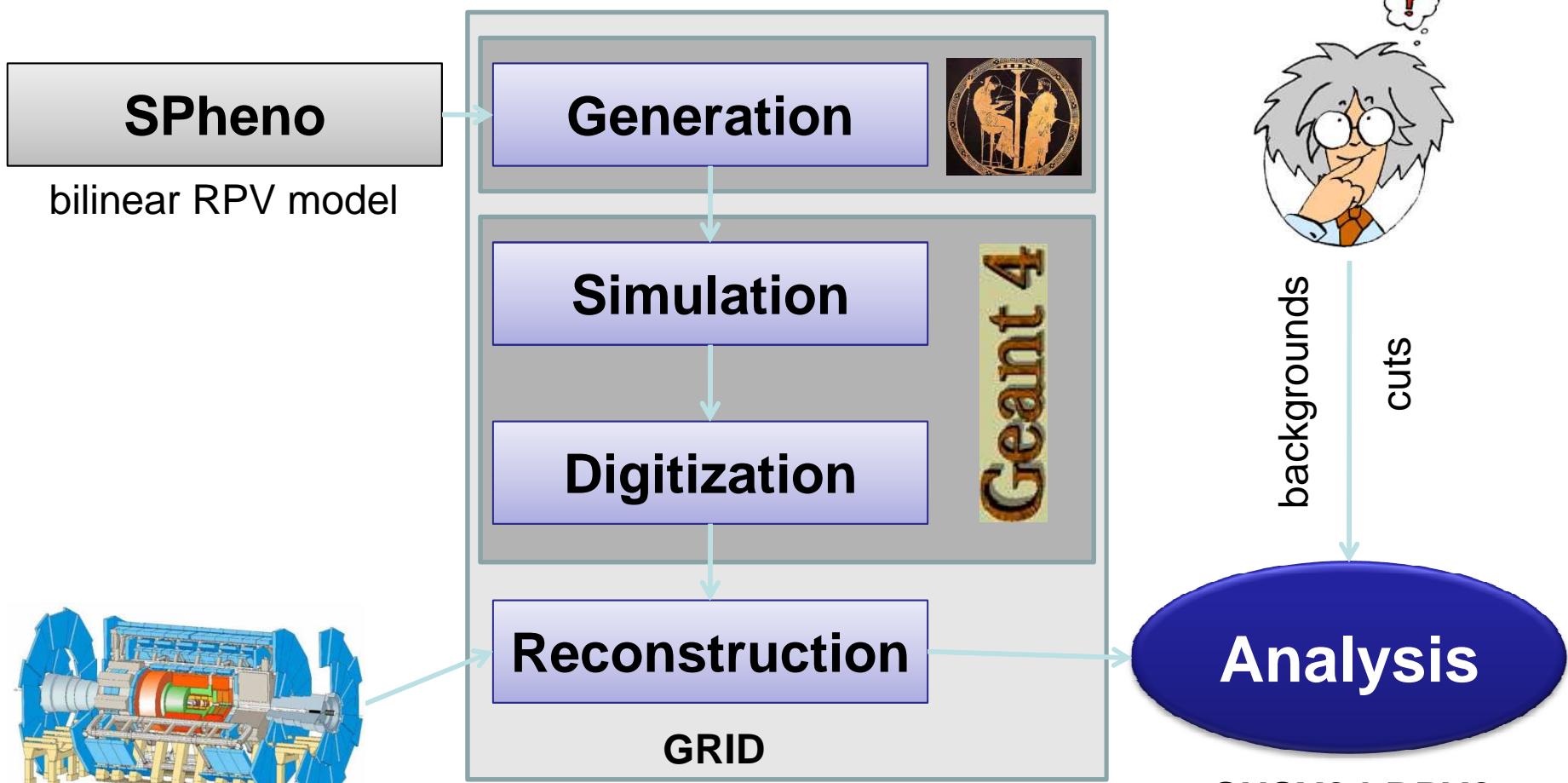
(data created with Spheno 3beta36,  
W. Porod , arXiv:hep-ph/0301101)

## ATLAS detector



## Software workflow

Reconstruction chain





## SPheno Parameters in bRPV

9 extra parameters for bRPV

Define them explicitly

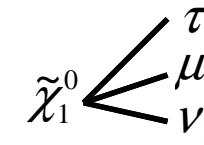
OR

Constraints:

- Successful electroweak symmetry breaking corresponds to minimization of effective potential; technically:  
**3 extra tadpole equations** linear in  $B_i$
- Results from neutrino oscillation data (2 mass differences, 3 mixing angles) fix **5 bilinear parameters** ( $\varepsilon_i, v_i$ )
- Remaining parameter should be of the same order as the others

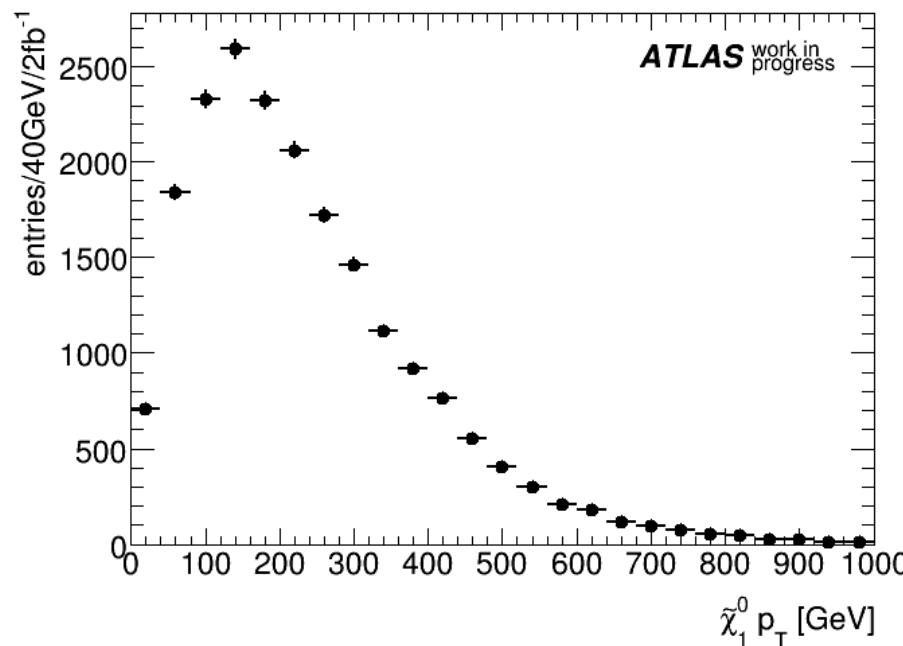


# Signal channel/ SUSY background



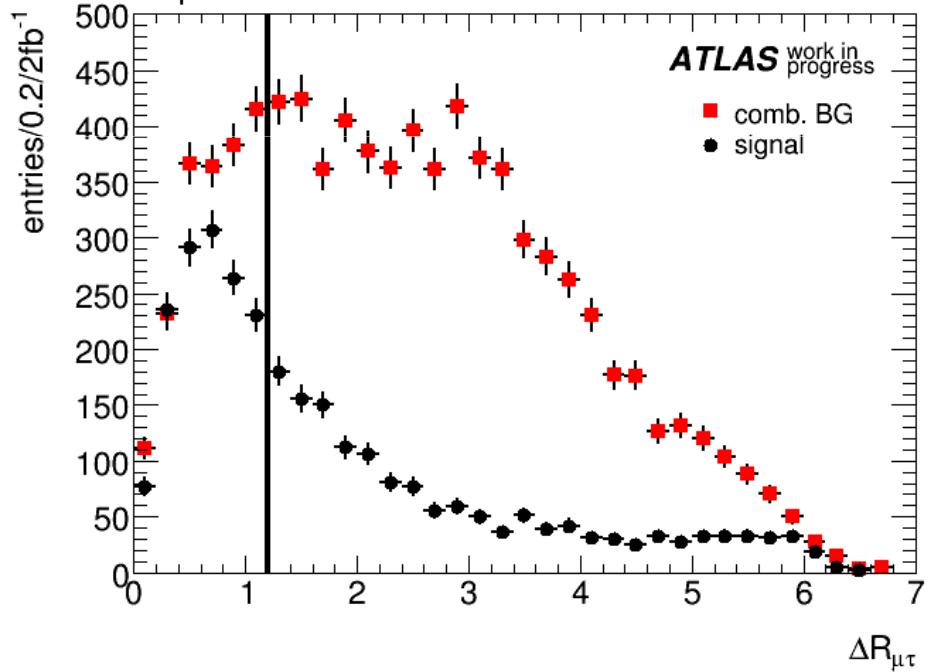
Calculation of invariant mass of  $\mu$  and  $\tau$

$p_T$  distribution of neutralinos:



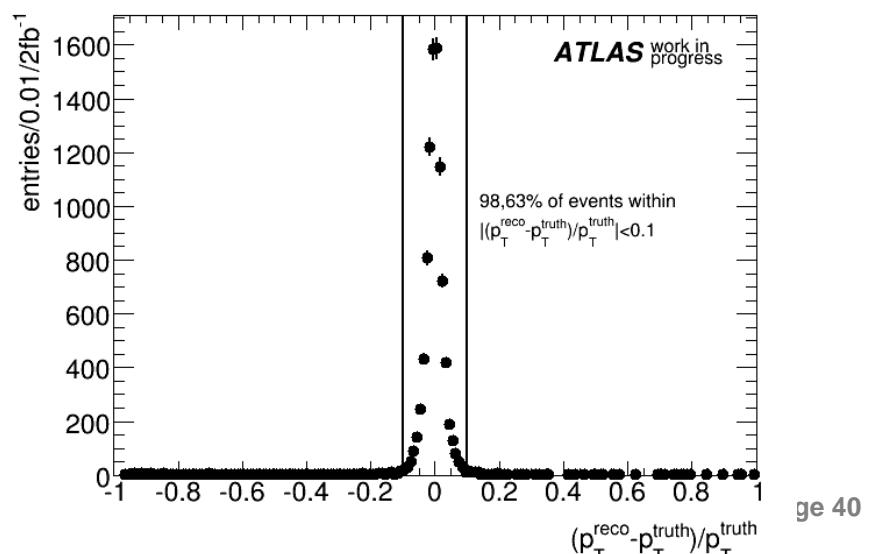
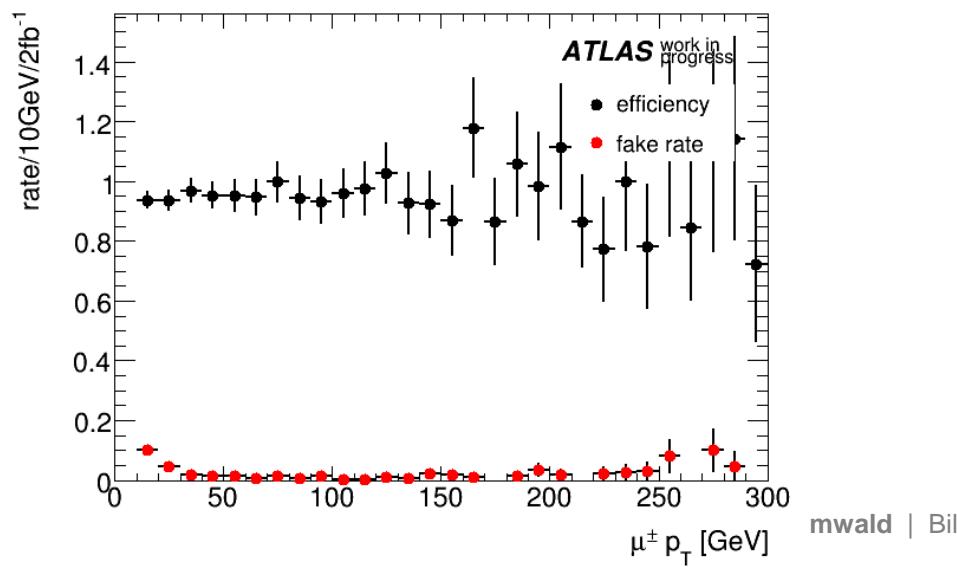
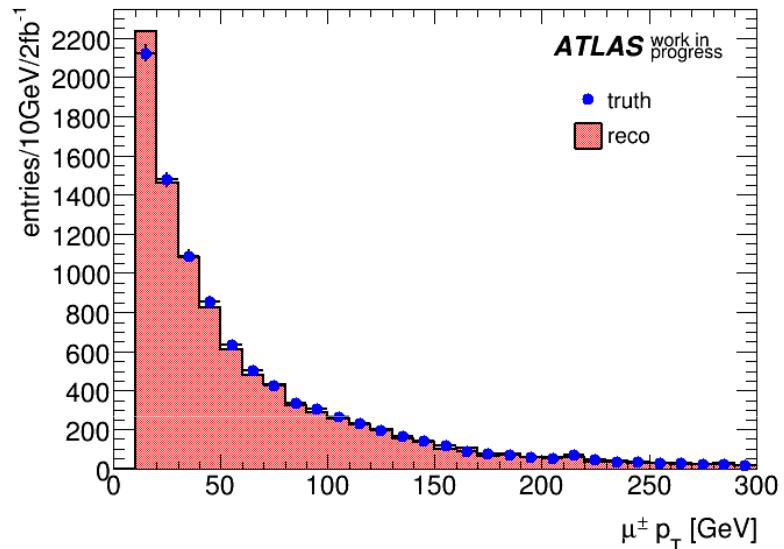
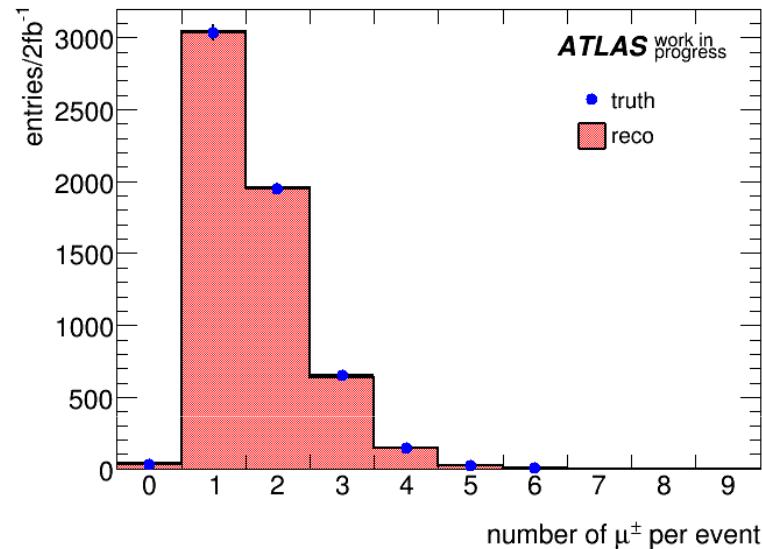
→ Decay products should be boosted

$\Delta R_{\mu\tau}$  distribution of signal and BG pairs:

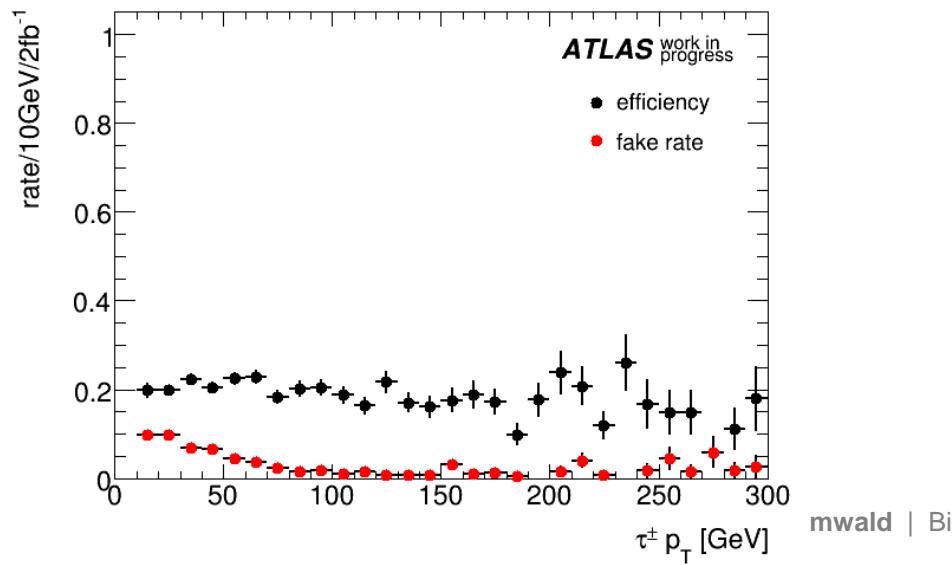
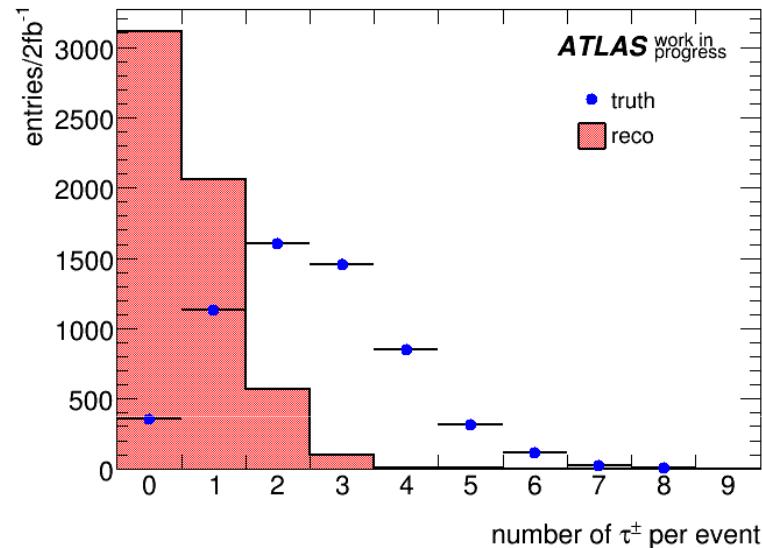


→ Reasonable cut:  $\Delta R_{\mu\tau} < 1.2$

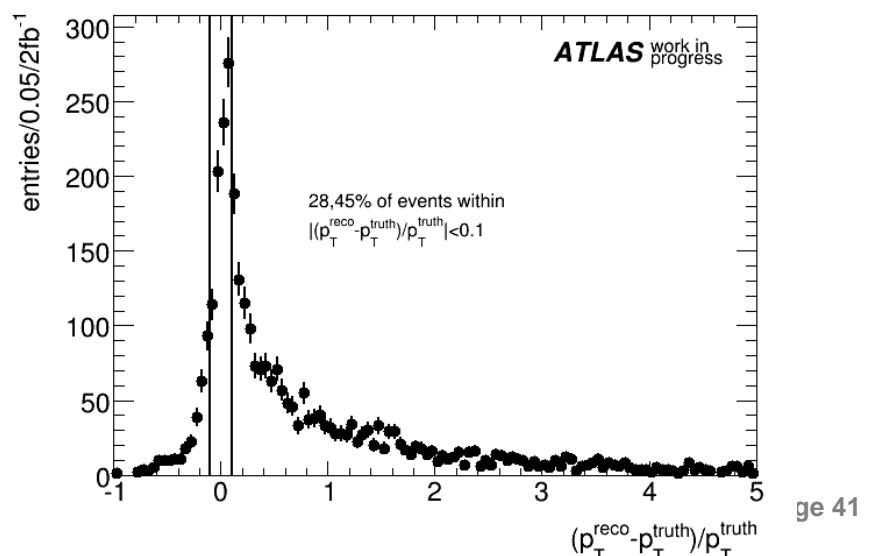
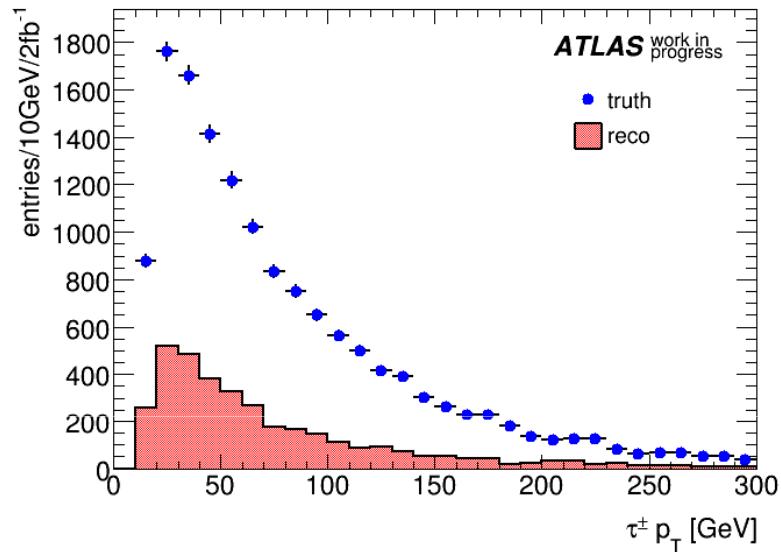
# Reconstruction of muons



# Reconstruction of taus



# Truth including leptonic tau decays





## Object Selection

### Muons:

- combined muon
- $\text{pt} > 10 \text{ GeV}$
- $|\eta| < 2.7$
- isolation cone  $0.2/ 10 \text{ GeV}$

### Jets:

- $\text{pt} > 20 \text{ GeV}$
- $|\eta| < 2.5$

### Electrons:

- isEm flag: „medium“
- $\text{pt} > 10 \text{ GeV}$
- $|\eta| < 2.5$  and  $|\eta| \notin [1.37, 1.52]$

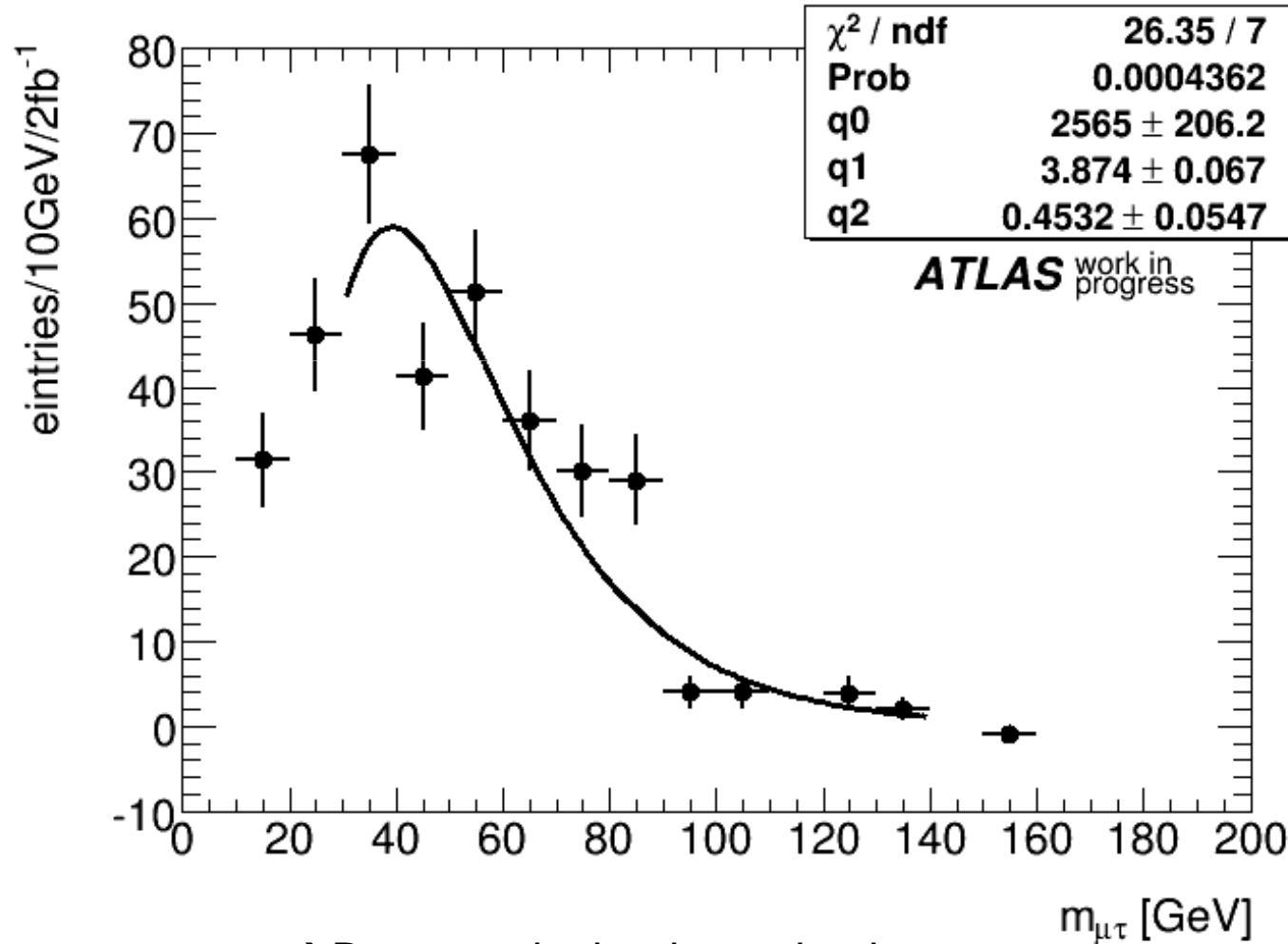
### Taus:

- 1 / 3 tracks
- charge =  $\pm 1$
- $\text{pt} > 10 \text{ GeV}$
- $|\eta| < 2.5$  and  $|\eta| \notin [1.37, 1.52]$
- Likelihood flag: „Loose“

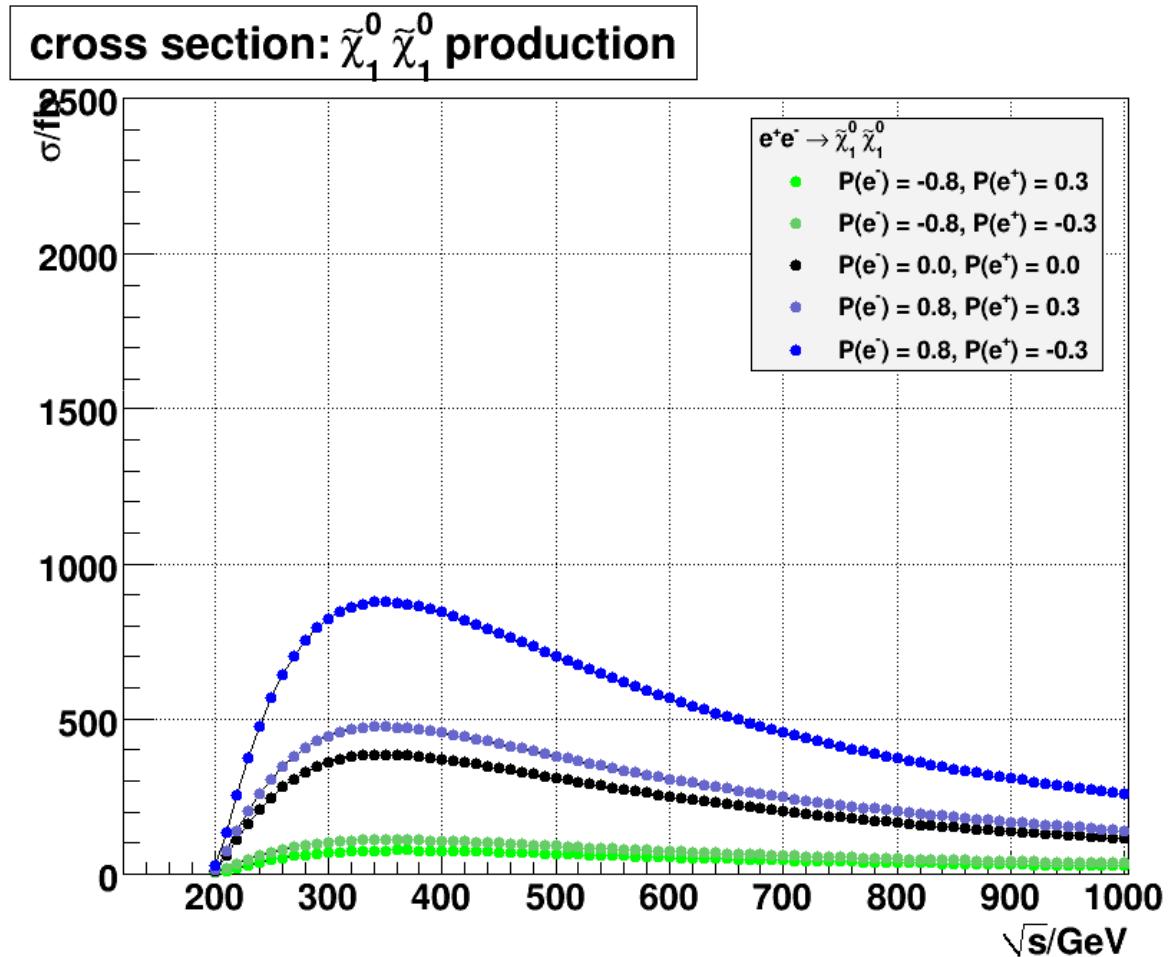
### Overlap removal:

- remove electrons within  $0.2 < \Delta R < 0.4$  to a jet
- remove jets within  $\Delta R < 0.2$  to an electron
- remove jets within  $\Delta R < 0.4$  to another particle

## Inflection point method



## Production cross section

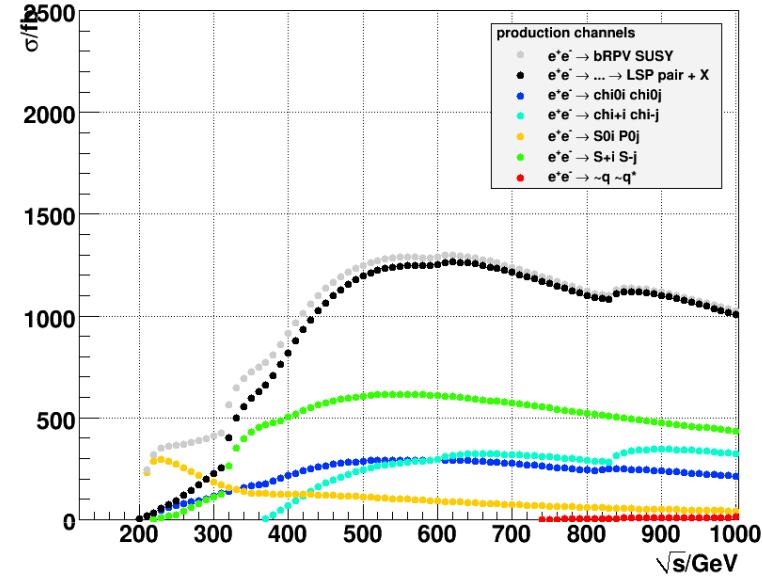


*Attention: SPS1a'*

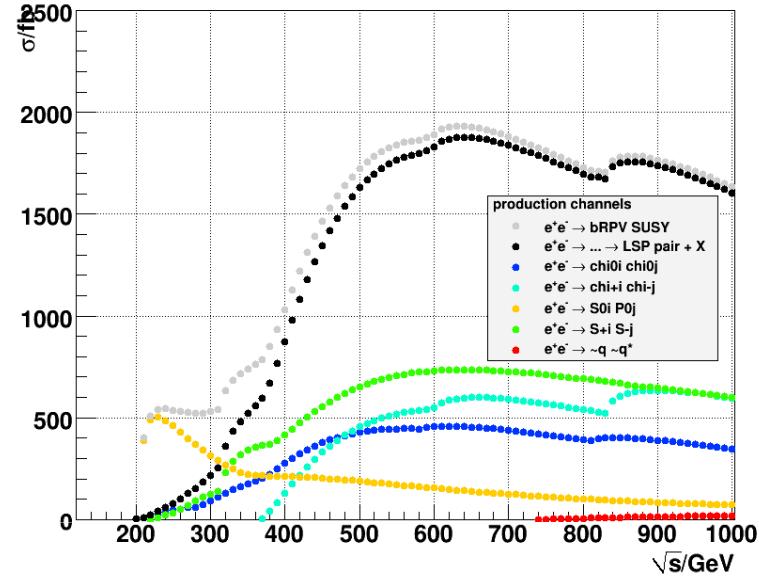
LSP mixing character:  
 83,9% Bino  
 4,0% u Higgsino  
 4,0% d Higgsino  
 8,1% Wino

- main production processes:  
 t-, u-channel
- „selectron“ exchange  
 $(S^-_3 \approx \sim e^-_R, S^-_4 \approx \sim e^-_L)$
- $m(S^-_3) < m(S^-_4) \rightarrow \sigma_{+-} > \sigma_{-+}$

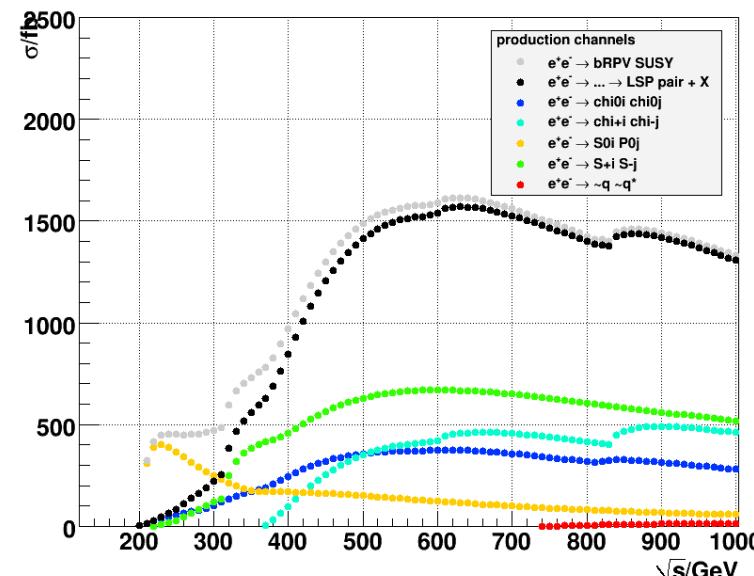
**cross sections ( $P(e^-) = -0.8, P(e^+) = -0.3$ )**

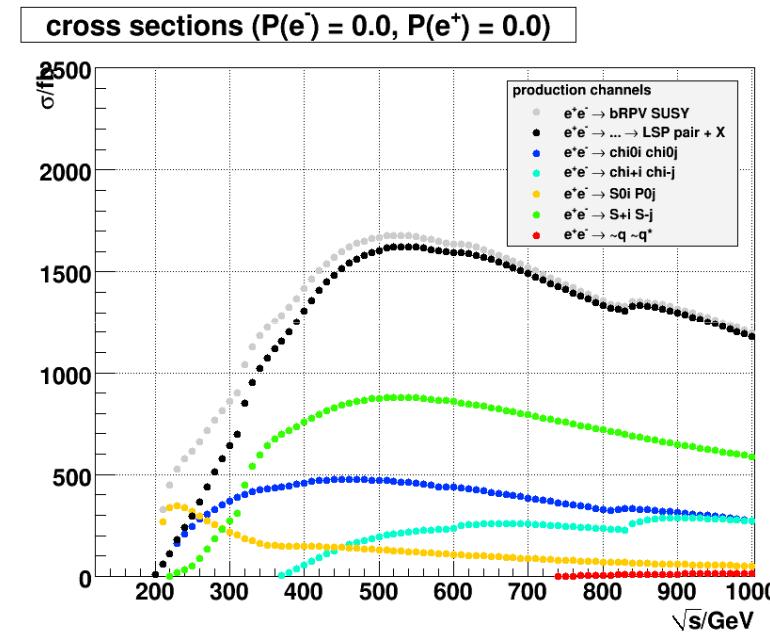


**cross sections ( $P(e^-) = -0.8, P(e^+) = +0.3$ )**

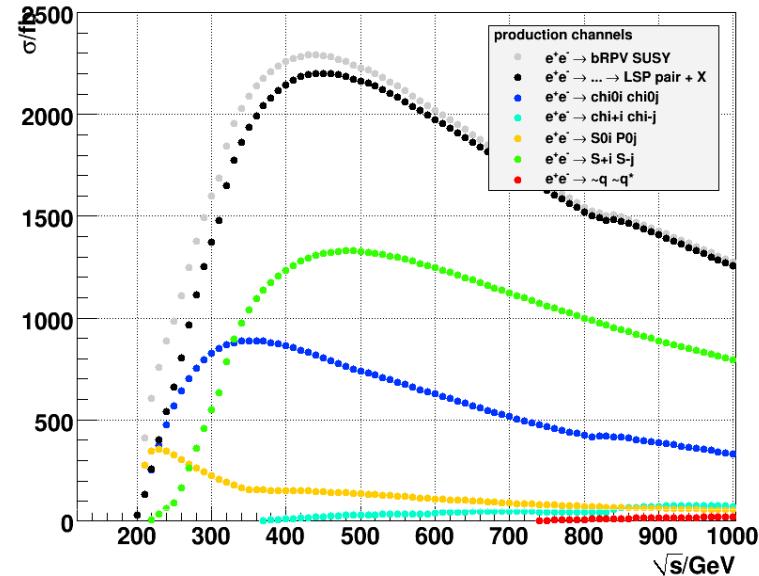


**cross sections ( $P(e^-) = -0.8, P(e^+) = 0.0$ )**

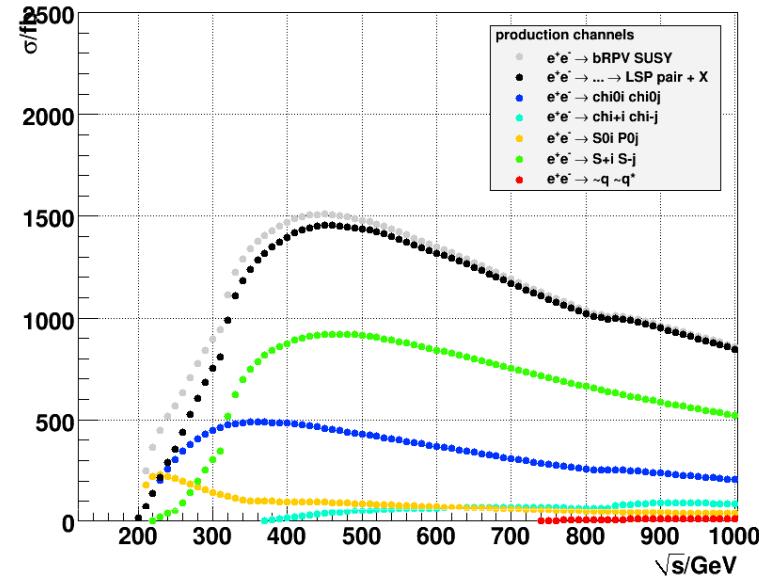




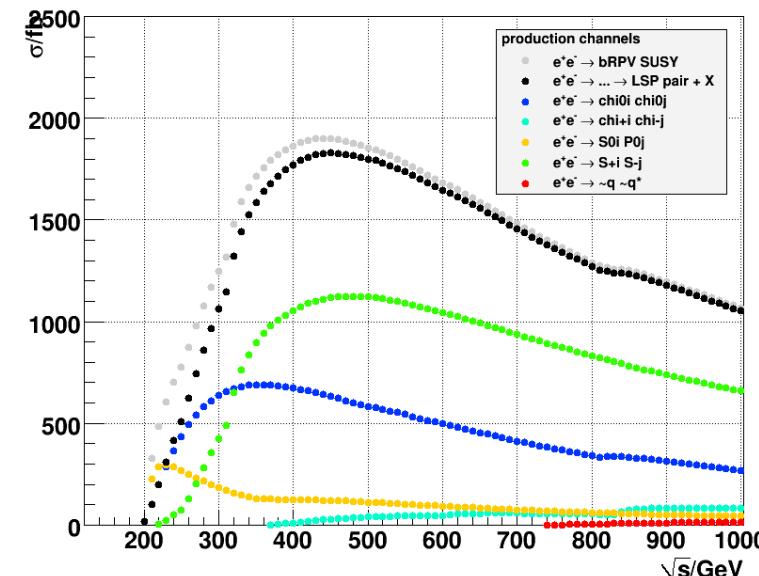
**cross sections ( $P(e^-) = 0.8, P(e^+) = -0.3$ )**



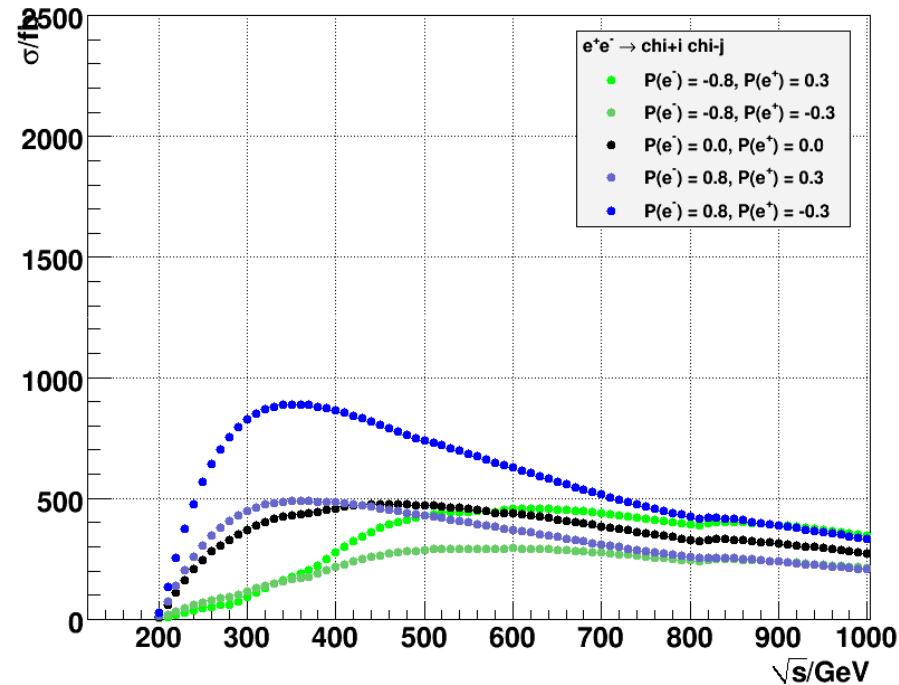
**cross sections ( $P(e^-) = 0.8, P(e^+) = 0.3$ )**



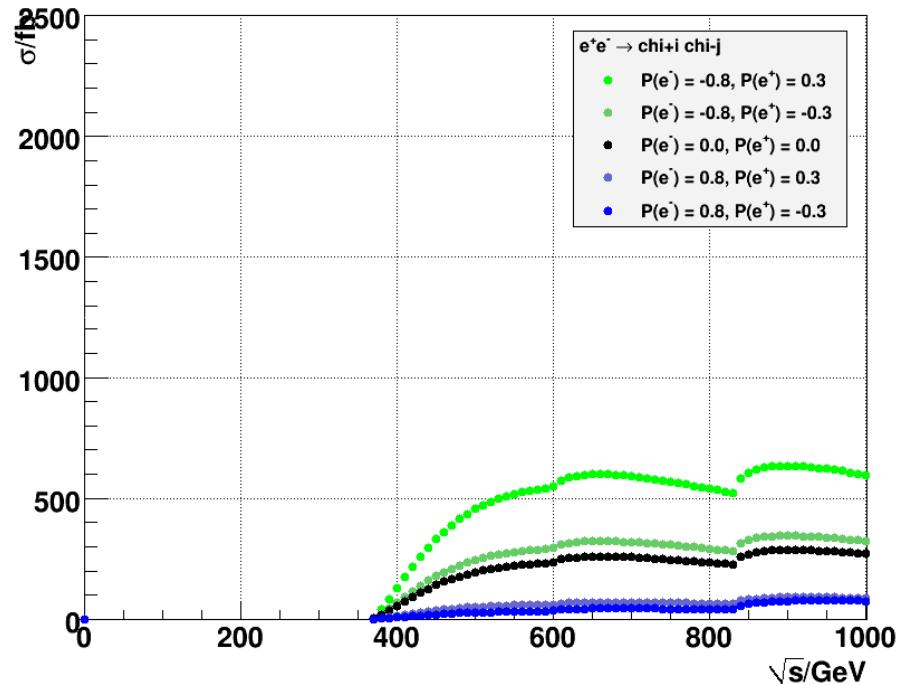
**cross sections ( $P(e^-) = 0.8, P(e^+) = 0.0$ )**



**cross section: neutralino production**

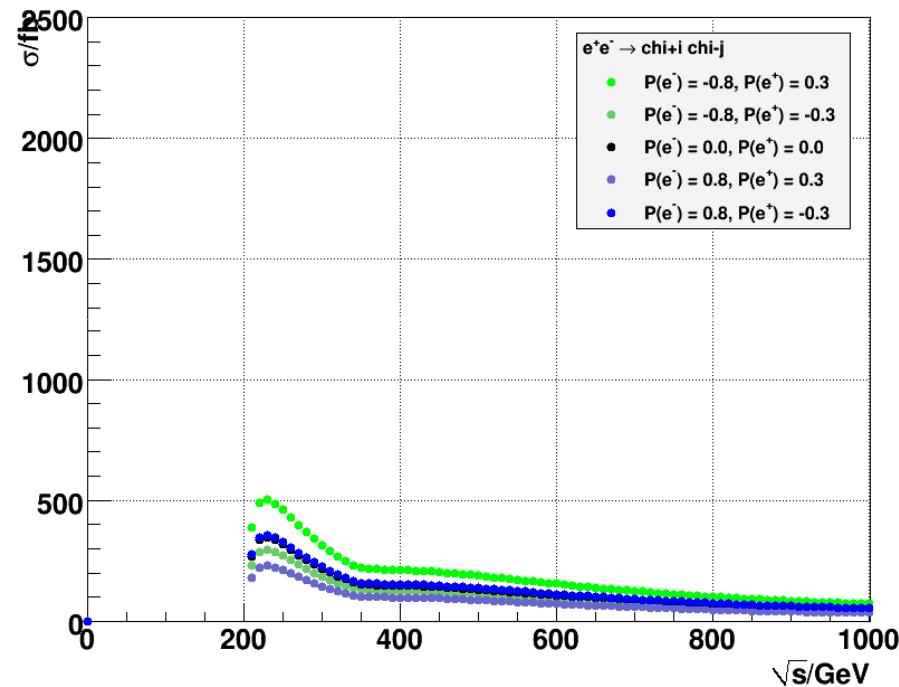


**cross section: chargino production**





cross section neutral scalar production



cross section charged scalar production

