

# Measurement of 1-jettiness in deep-inelastic $ep$ scattering at HERA

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14th Annual Meeting of the Helmholtz Alliance "Physics at the Terascale"

Technische Universität München,  
Max-Planck-Institut für Physik

23.11.2021



# Neutral current deep-inelastic scattering

## Neutral current deep-inelastic scattering

- Process  $e p \rightarrow e' X$
- Electron or positron scattering

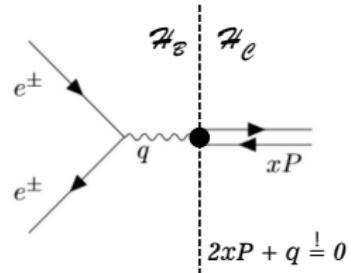
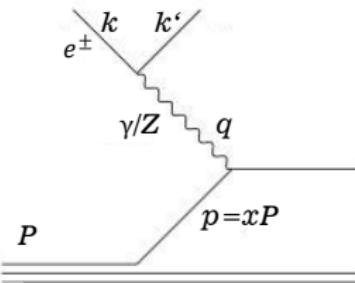
## Kinematic variables

- Virtuality of exchanged boson  $Q^2$   
 $Q^2 = -q^2 = -(k - k')^2$
- Inelasticity, Bjorken-x and centre-of-mass energy

$$y = \frac{P \cdot q}{P \cdot k} \quad Q^2 = x_{Bj} \cdot y \cdot s$$

## Breit frame

- Exchanged boson completely space-like
- Collides head-on with parton (brick-wall frame)



# The 1-jettiness event shape observable

## 1-jettiness

- Axes incoming parton and  $q + xP$ :

$$\tau_1^b = \frac{2}{Q^2} \sum_{i \in X} \min\{xP \cdot p_i, (q + xP) \cdot p_i\}$$

- Infrared safe and free of non-global logs
- Sensitive to strong coupling  $\alpha_s$  and PDFs

## DIS thrust normalised to boson axis

- Normalisation with  $Q/2$  of the event:

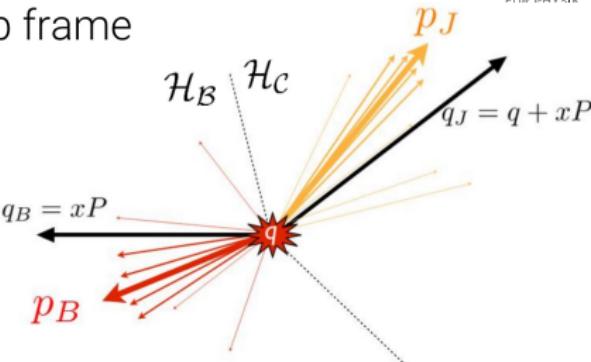
$$\tau_Q = 1 - \frac{2}{Q} \sum_{i \in \mathcal{H}_C} P_{z,i}^{Breit}$$

- Only particles in the current hemisphere contribute

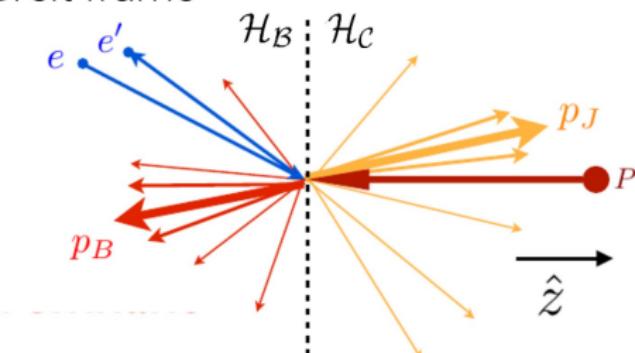
**Equivalence** follows from momentum conservation:

$$\tau_Q = \tau_1^b$$

## Lab frame

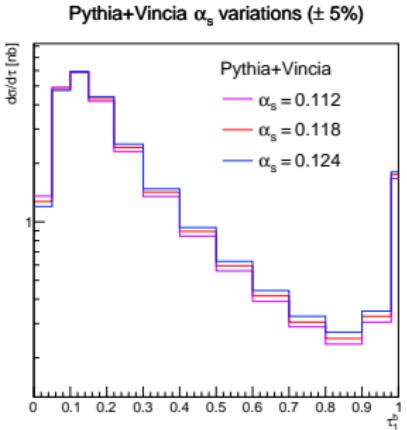
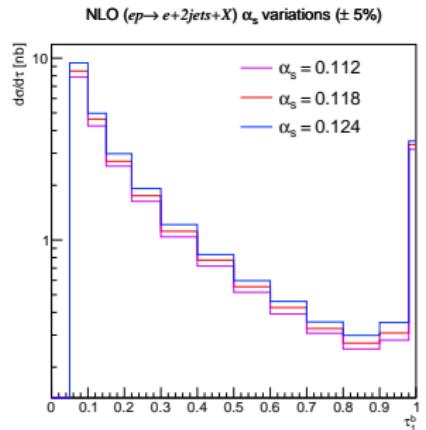


## Breit frame



Sketch taken from Kang, Lee, Stewart [Phys.Rev.D 88 (2013) 054004]

# Sensitivity of $\tau_1^b$ to $\alpha_s$



- Plot shows fixed order NLO calculation  $e p \rightarrow e + 2\text{jets}$  for  $\tau_1^b$  on PARTON LEVEL
- First bin is empty by definition
- Prediction scales linearly with strong coupling  $\alpha_s$

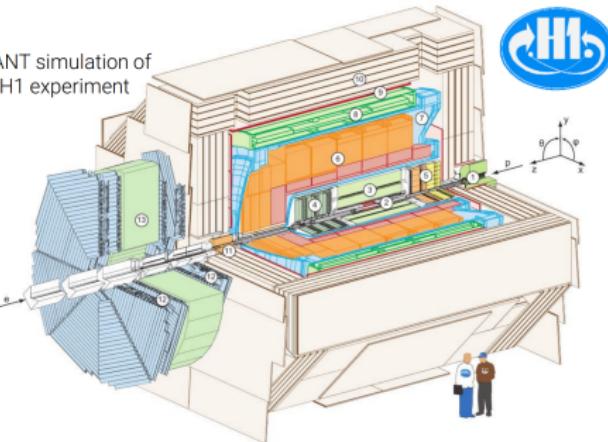
- Plot shows Pythia 8.3 + Vincia prediction for  $\tau_1^b$  on PARTICLE LEVEL
- High sensitivity in tail region
- No sensitivity in peak region (Born level kinematics)

# The H1 detector



- Integrated luminosity  $L = 351.6 \text{ pb}^{-1}$
- Electron and positron runs
- $E_e = 27.6 \text{ GeV}, E_p = 920 \text{ GeV}$   
 $\rightarrow \sqrt{s} = 319 \text{ GeV}$

GEANT simulation of  
the H1 experiment



- Asymmetric design with trackers, calorimeter, solenoid, muon-chambers, forward & backward detectors
- Trigger requires high-energetic cluster in LAr calorimenter  
 $\rightarrow$  electron or hadron  
 $\rightarrow > 99\% \text{ efficient for } y \lesssim 0.7$
- Particles are reconstructed using a particle flow algorithm  
 $\rightarrow$  Combining cluster and track information without double-counting of energy

## DPHEP Collaboration and data-preservation

- MPP is among founding institutions in the initiative Data Preservation in High Energy Physics (DPHEP)
- Involved experiments are e.g. JADE, OPAL, H1 and ZEUS

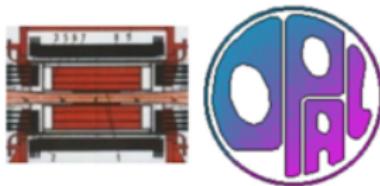
## Data preservation has many facets...

- Data (raw, already analysed (n-tuples), simulated (MC))
- Software (Simulation/ reconstruction/ analysis software, analysis workflows,...)
- Documentation (internal/external webpages, technical documentation, int-notes, analysis notes, wiki-pages, code-documentation, ... )
- Keep specific knowledge  
⇒ Best practise: Continue analysing data!

## DP at H1

- Total volume at H1  $\approx 0.5$  PB
- Preservation through modernisation (c.f. D. Britzger's talk in the computing session)

Emerging new interest in HERA data because of EIC (and LHeC)



# Inclusive DIS data

## HERA-II data

- High- $Q^2$  region:  
 $Q^2 > 150 \text{ GeV}^2$
- Luminosity:  $L = 351 \text{ pb}^{-1}$

## Signal Monte Carlo models

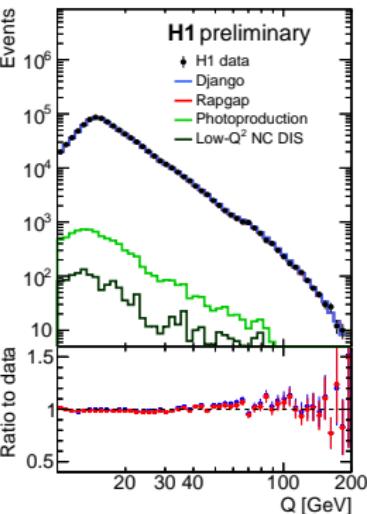
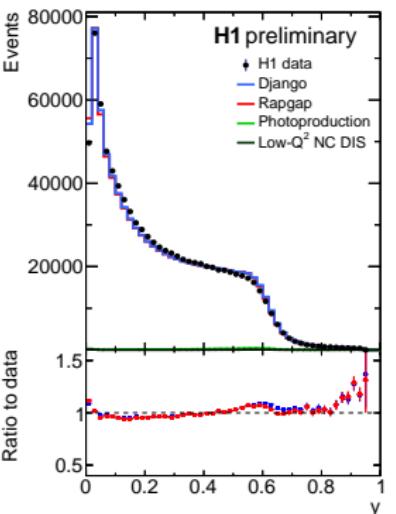
- Rapgap (ME + PS)
- Djangoh (CDM)

## Little background in incl. DIS

- Photoproduction
- Low- $Q^2$  NC DIS
- Other sources are negligible  
(QECD, CC DIS, di-lepton production)

## Reconstruction

- Use the  $\Sigma$  method  
→ Independent of electron ISR



$$y = y_\Sigma = \frac{\Sigma}{\Sigma + E_{e\prime}(1 - \cos \vartheta_{e\prime})}$$

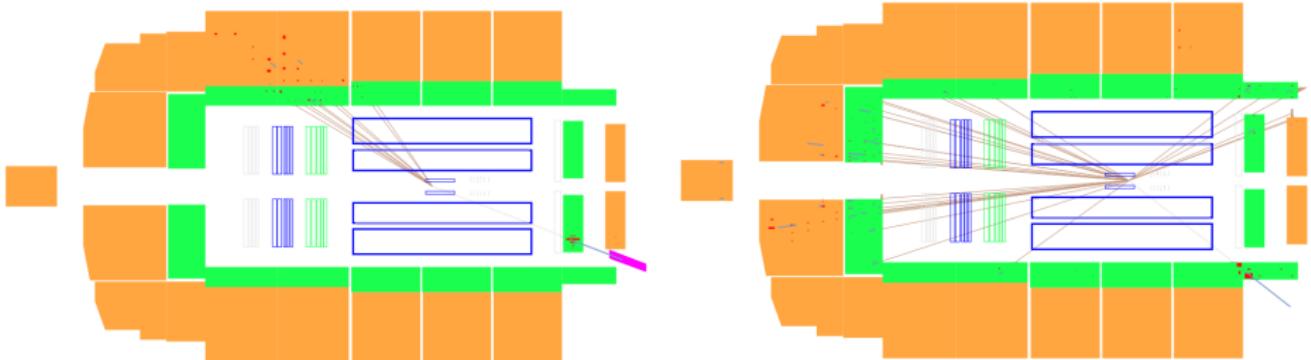
$$Q^2 = Q_\Sigma^2 = \frac{E_{e\prime}^2 \sin \vartheta_{e\prime}}{1 - y_\Sigma}$$

# The 1-jettiness event shape observable

## 1-jettiness

$$\tau_1^b = \frac{2}{Q^2} \sum_{i \in X} \min\{xP \cdot p_i, (q + xP) \cdot p_i\}$$

### Visualisation of the 1-jettiness with event displays

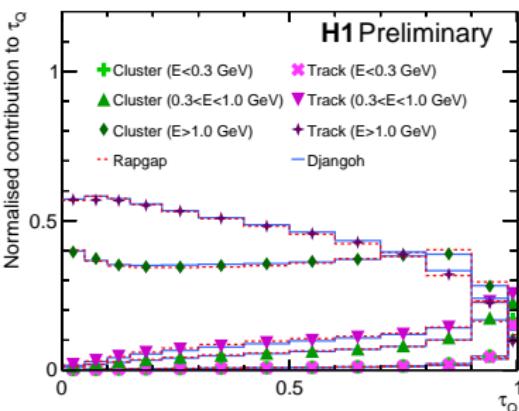
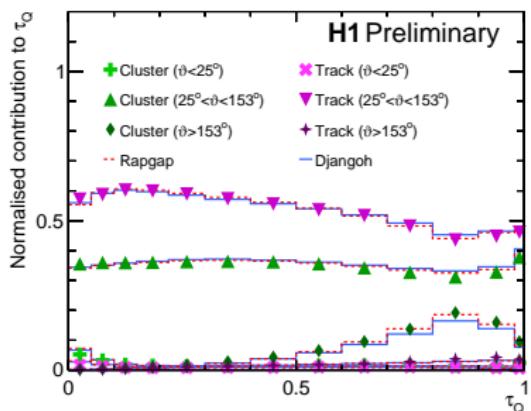


- DIS 1-jet configuration
- Most HFS particles collinear to scattered parton  
 $\rightarrow$  Small  $\tau_1^b$

- Dijet event
- More and larger contributions to the sum over the HFS  
 $\rightarrow$  Large  $\tau_1^b$

# DIS thrust - a $4\pi$ observable

- All particle candidates in all DIS events contribute  $\left( \tau_Q = 1 - \frac{2}{Q} \sum_{i \in \mathcal{H}_C} P_{z,i}^{Breit} \right)$
- Normalised contribution to  $\tau_Q$  for different ranges in polar angle  $\vartheta$  and energy

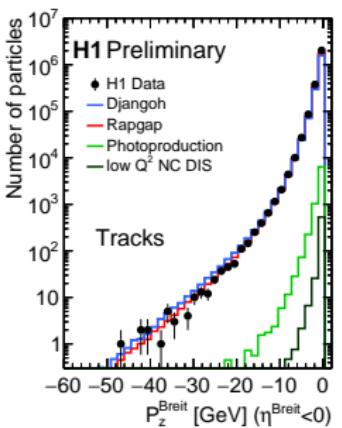
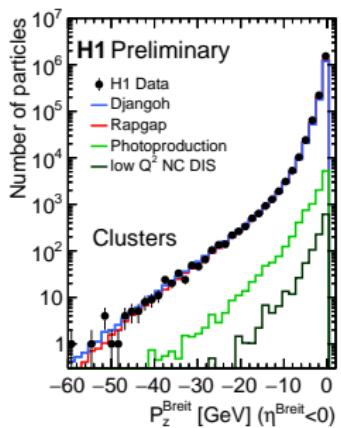


- Mainly tracks and clusters in the central part of the detector contribute ( $25^\circ < \vartheta < 153^\circ$ )
- Mainly particles with high energy contribute ( $E > 1$  GeV)  
 $\Rightarrow$  Well measured particles dominate in  $\tau_Q$

# 1-jettiness - DIS thrust

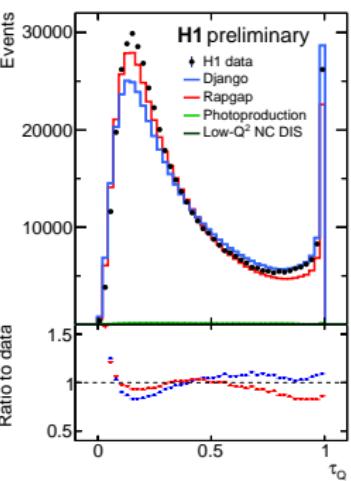
## DIS thrust: Sum of longitudinal momenta

- Longitudinal momentum distribution of single particles in the current hemisphere
- Particles are well modelled by simulation for clusters and tracks



## DIS thrust

- $\tau_Q \rightarrow 0$  : DIS 1-jet events
- $\tau_Q \rightarrow 1$  : Dijet events
- $\tau_Q = 1$  : Dijet event, both jets in beam hemisphere



- Reasonable agreement between data and MC
- Full  $\tau_Q$  range measurable

# Purity distribution

Purity defined as  $N_{\text{stay}}/N_{\text{rec}}$

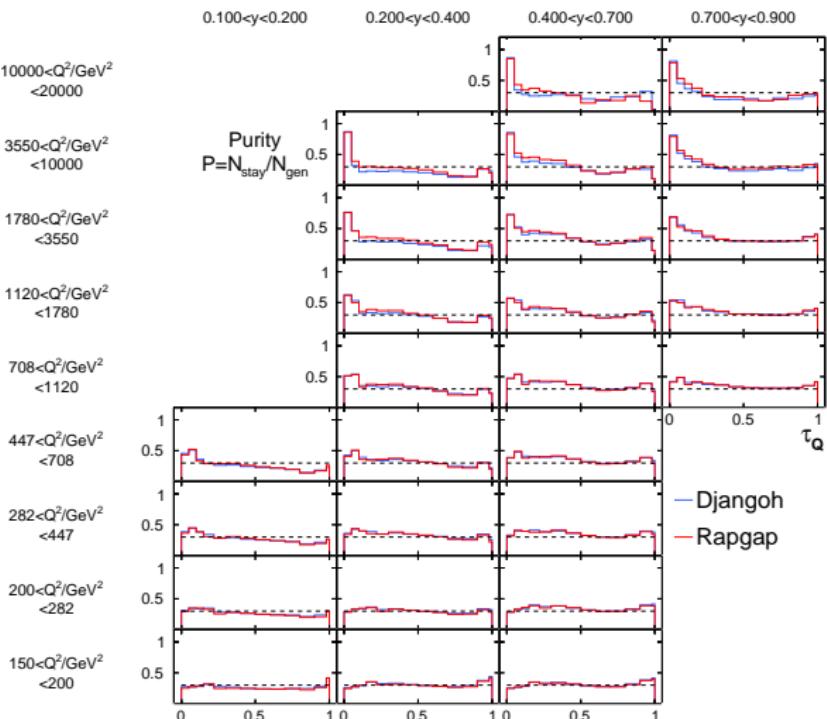
- $N_{\text{rec}}$ : Events on detector level in one bin
- $N_{\text{stay}}$ : Events that are reconstructed in the same bin they were generated

## Purity

- Rapgap and Djangoh behave similarly
- Flat distribution in all  $y-Q^2$  bins
- Purities  $> 30\%$  in most bins

## From different binnings and 2D migration matrices

- Purity mainly limited by bin-to-bin resolution effects
- Not an effect from limited detector acceptance



Measure  $\tau_Q$  but present cross sections as a function of  $\tau_1^b$

## 1-jettiness cross section

$$\left( \frac{d\sigma}{d\tau_1^b} \right)_i = \frac{N_{data,i} - N_{bkgd,i}}{\Delta_i \cdot L} \cdot c_{QED,i} \cdot c_{unfold,i}$$

- Unfolded using bin-by-bin method  $c_{unfold}$
- Corrected for QED radiative effects  $c_{QED}$
- Divide by  $\tau_1^b$ -bin width  $\Delta_i$
- Integrated luminosity  $L = 351.6 \text{ pb}^{-1}$

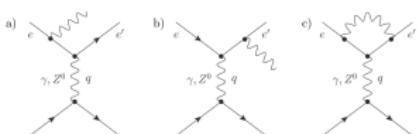
## Phase space

- Momentum transfer  $150 < Q^2 < 20.000 \text{ GeV}^2$
- Inelasticity  $0.2 < y < 0.7$  (single differential)
- Inelasticity  $0.1 < y < 0.9$  (triple differential)

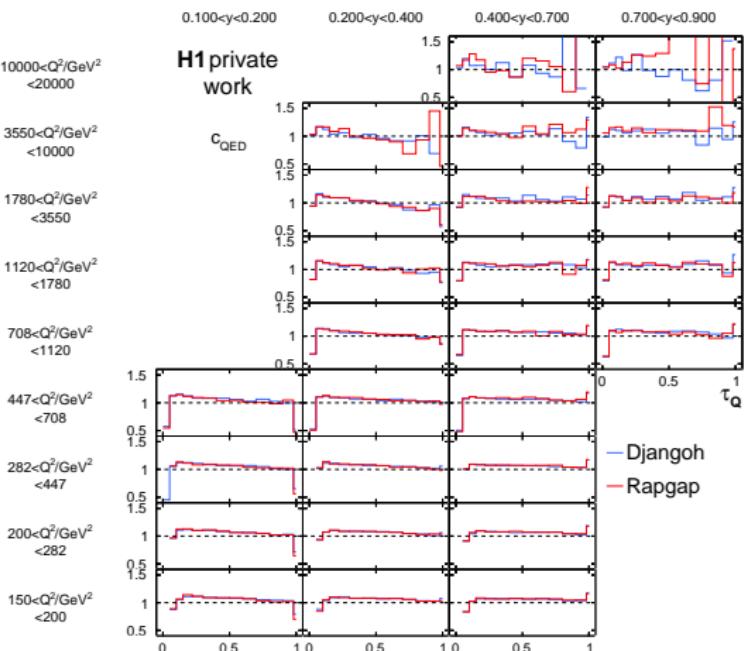
# QED corrections

## Correct for electron QED radiative effects

- Real emissions of photons (a,b)
- Vertex corrections (c)



- QED processes simulated with HERACLES
- Size of corrections depends on reconstruction method
  - Corrections around 10%
  - Large effect in the first bin



# Single differential cross section

## Comparison with MC models

- Djangoh 1.4: Colour-dipole-model
- Rapgap 3.1: ME + parton shower
- Pythia 8.3 + Dire

## Dire Parton Shower

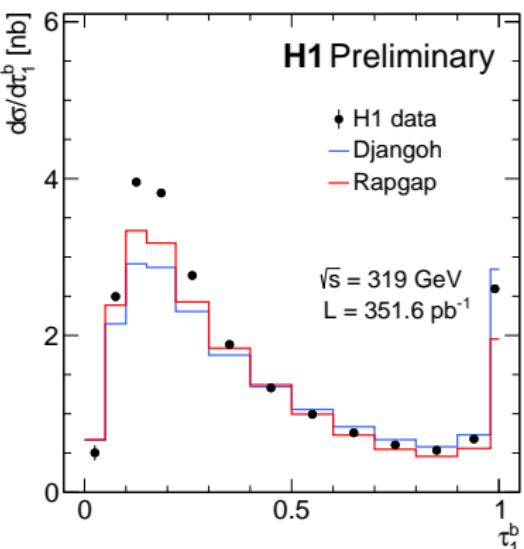
- Dipole-like shower
- Including inclusive NLO DGLAP corrections to the shower evolution

## Peak region ( $\tau_1^b \lesssim 0.2$ )

- Resummation region
- Not well described by the models

## Tail region ( $\tau_1^b \gtrsim 0.3$ )

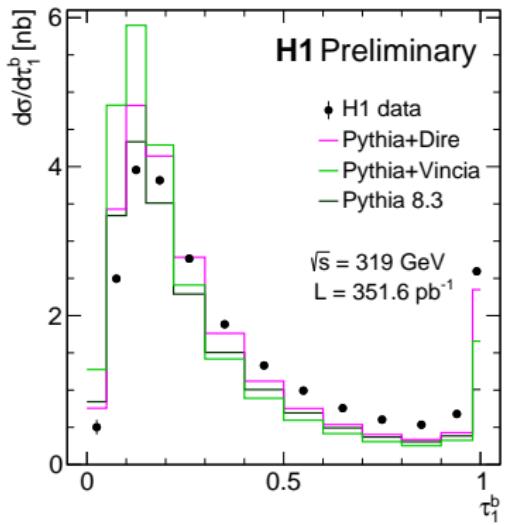
- Fixed order region ( $\mathcal{O}(\alpha_s)$ )
- Djangoh and Rapgap perform well
- Pythia+Dire underestimates the data



# Single differential cross section

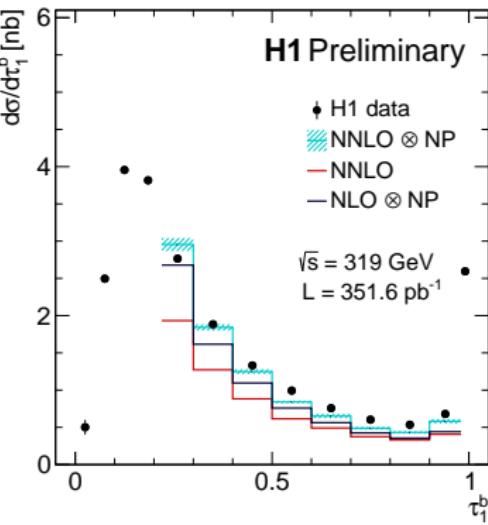
## Comparison with parton shower models

- Peak region has strong dependence on different parton showers
- No PS model provides a fully satisfactory description
- 'Pythia default' underestimates  $\tau = 1$



## $\gamma p \rightarrow 2 \text{ jets} + X$ NNLO prediction form NNLOJET

- NP corrections from Pythia 8.3 (sizeable)
- NNLO provides a reasonable description of fixed-order region
- NNLO improves over NLO



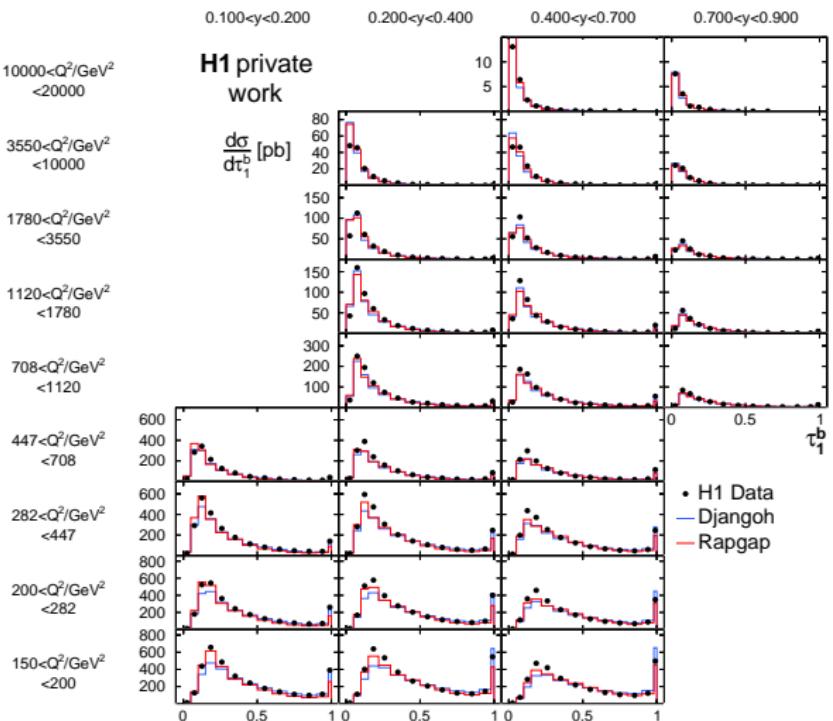
# Triple differential cross sections

## Large cross section and sizeable data

→ Triple-diff. cross sections as a function of  $Q^2, y, \tau$

## 3D cross sections

- increasing  $Q^2$ 
  - Peak moves to lower  $\tau$
  - Tail region lowers
- Increasing  $y$ 
  - $\tau = 1$  becomes enhanced



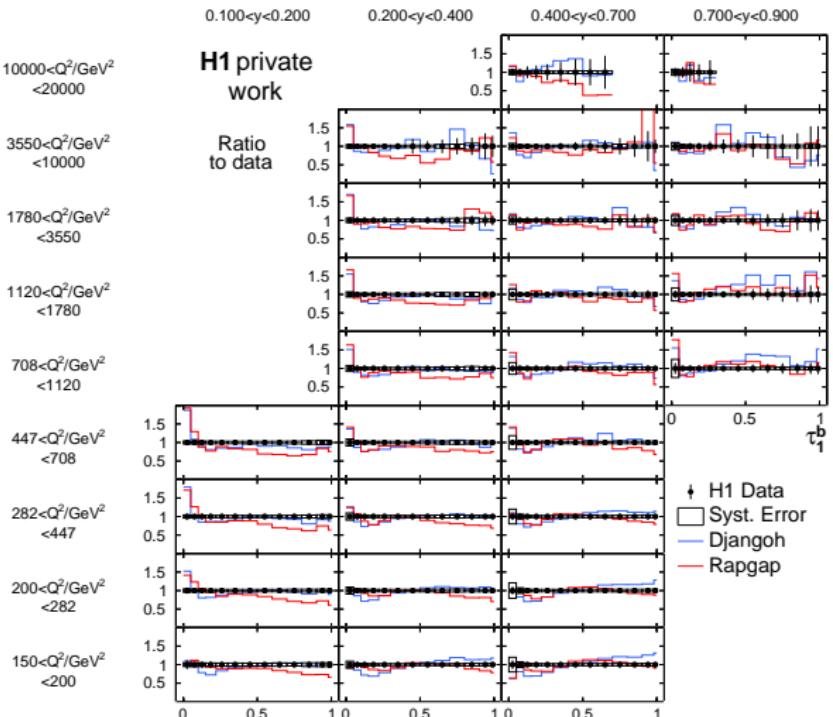
# Triple differential cross sections

## Ratio to data

- Stat. uncertainties of a few to  $O(10\%)$
- Syst. uncertainties are in the range of 5%

→ 'Classical' MC models perform reasonably well over entire phase space

→ Pythia+Dire similar to Rapgap at low  $y$ , but too large at low  $\tau$



# Triple differential cross sections



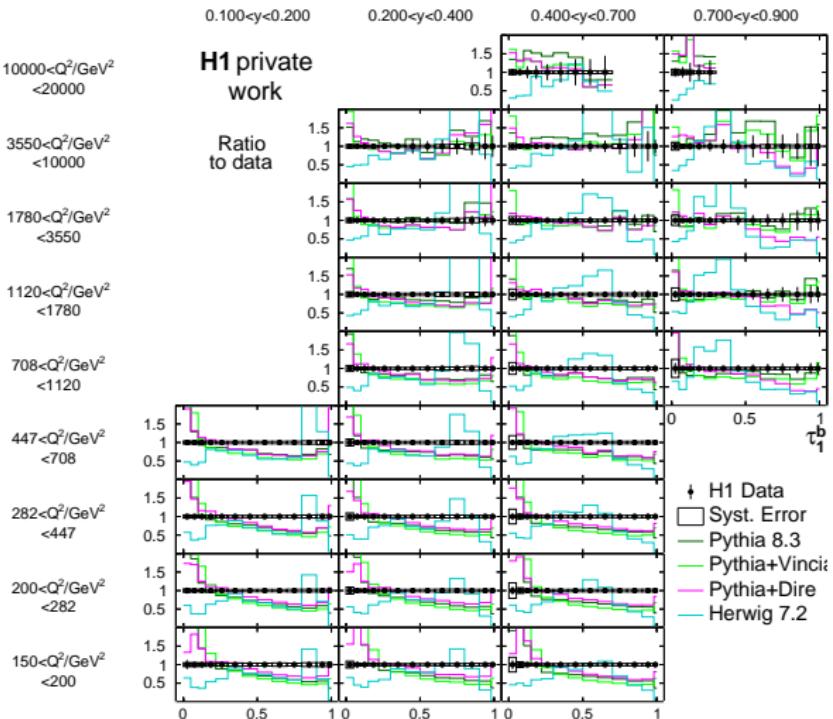
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## Comparison with further MC models

- Pythia+Vincia
- Pythia w/ default shower

## Herwig 7.2

- Often similar to Pythia, but peak region too low (DIS cross section too low)
- Some structure at high  $\tau$

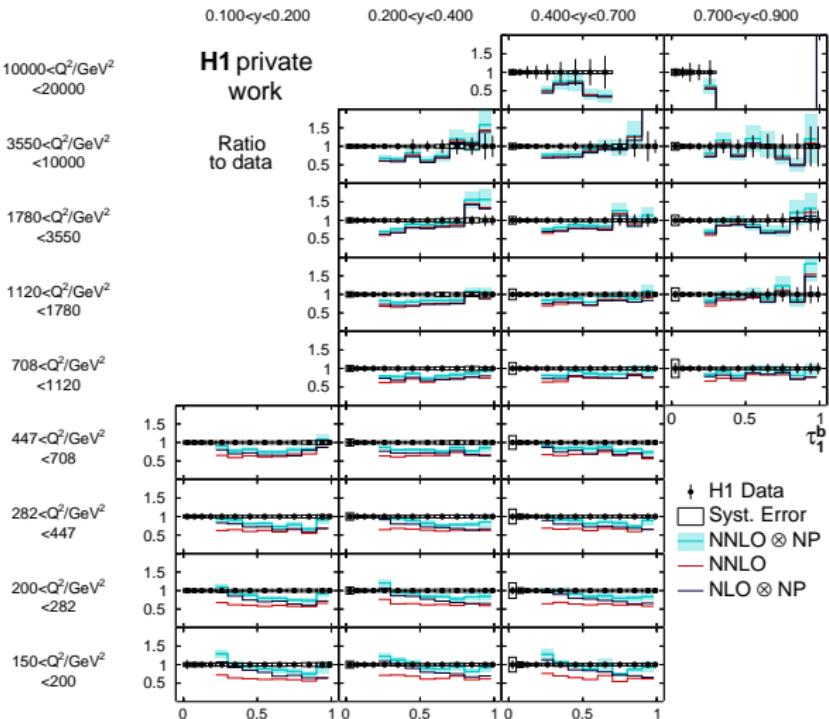


# Triple differential cross sections

## NNLO pQCD ( $ep \rightarrow 2 \text{ jets} + X$ )

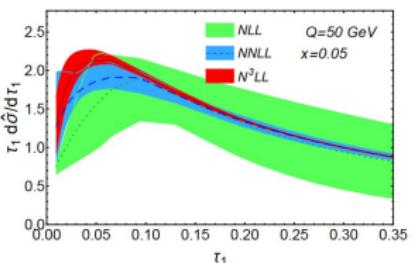
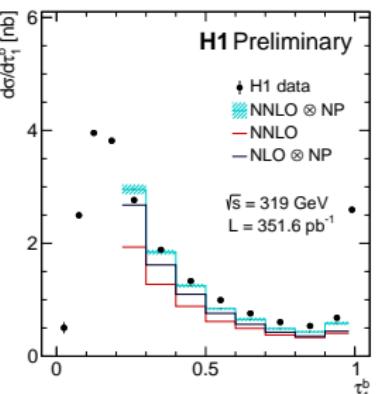
- Reasonable description in entire phase space
- Improved description with increasing  $Q^2$
- Small scale uncertainties

→ Altogether: NNLO improves over NLO but NP corrections are sizeable



## Summary and outlook

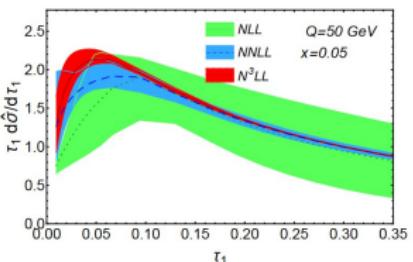
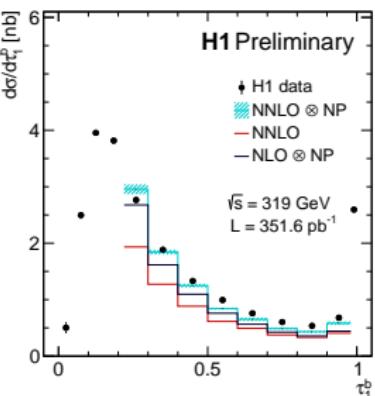
- A first measurement of the 1-jettiness event shape observable in NC DIS was presented  
(Analysis team J. Hessler, D. Britzger, S. Lee  
[J. Kretzschmar, E. Elsen])
- 1-jettiness is equivalent to DIS thrust normalised with  $Q/2$   
→ Defined for every NC DIS event
- Classical Monte Carlo provides a good description of the data
- Modern Monte Carlo provides a reasonable description
- NNLO fixed order predictions ( $ep \rightarrow 2$  jets) provide good description in the region of validity, but hadronisation corrections are large



Kang, Lee, Stewart, [PoS DIS2015 (2015) 142]

## Outlook

- Apply advanced unfolding methods
- Predictions need to be confronted with data
  - N3LL ([PoS DIS2015 (2015) 142])
  - N3LO (Phys.Lett.B 792 (2019) 182, [1812.06104])
  - NNLO + Power Corrections (Eur.Phys.J.C 79 (2019) 1022 [1909.02760])
  - NNLO+PS (Phys. Rev. D 98, 114013 (2018) [1809.04192]) (UN<sup>2</sup>LOPS)
  - N3LO+PS (first concepts for N3LO+PS available [arXiv:2106.03206])
- Sensitivity to  $\alpha_s$  and PDFs needs to be explored
- Data will become useful for improving (DIS) MC generators
  - ⇒ Improved parton showers & smaller PDF uncertainties



Kang, Lee, Stewart, [PoS DIS2015 (2015) 142]

- [1] Z. Kang, X.Liu, S. Mantry, The 1-Jettiness DIS event shape: NNLL + NLO results, *arXiv:1312.0301v2*, 2014
- [2] D. Kang, C. Lee, I. Stewart, Using 1-Jettiness to Measure 2 Jets in DIS 3 Ways, *arXiv:1303.6952v2*, 2013.
- [3] D. Kang, DIS Event Shape at  $N^3 LL$ ,  
<https://indico.cern.ch/event/341292/contributions/1739091/attachments/670208/921244/DIS2015-kang.pdf>, 2015
- [4] R. Kogler, Measurement of Jet Production in Deep-Inelastic  $ep$  Scattering at HERA, DESY-THESIS-2011-003, 2010
- [5] U. Bassler, G. Bernardi, On the Kinematic Reconstruction of Deep Inelastic Scattering at HERA: the  $\Sigma$  Method, *arXiv:hep-ex/9412004v1*, 1994
- [6] D. Kang, C. Lee, I. Stewart, Analytic Calculation of 1-Jettiness in DIS at  $O(\alpha_s)$ , *arXiv:1407.6706v1*, 2014.