

# Kinematic fitting for ParticleFlow Detectors at Future Higgs Factories

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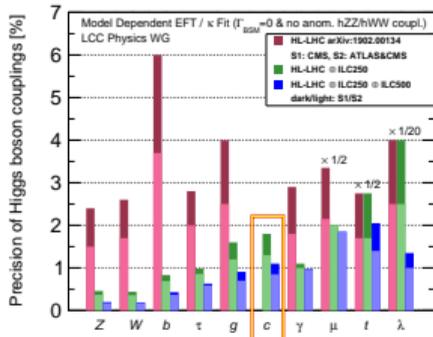
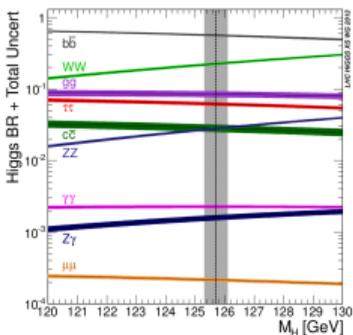
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RESEARCH FOR GRAND CHALLENGES



# $b$ - and $c$ -jets for Higgs physics studies

- ▶ Most frequent Higgs decay mode:  $H \rightarrow b\bar{b}$



- ▶ at least ONE semi-leptonic decay in  $Z/H \rightarrow b\bar{b}/c\bar{c}$

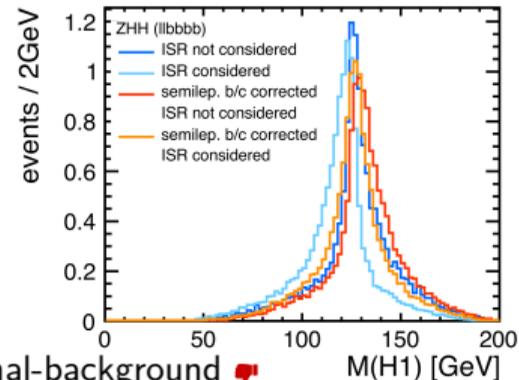
		$N_{SLD}^B$		
		0	1	2
$N_{SLD}^C$	0	34%	24%	4%
	1	18%	12%	2%
	2	3%	2%	0%

\*SLD: semi-leptonic decay

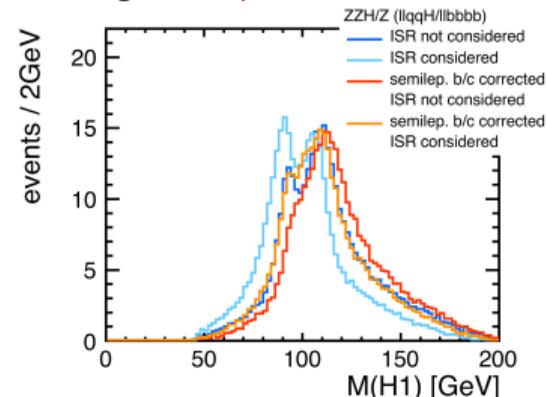
⇒ degrade the invariant di-jet mass

$Z/H$  separation by  $m_{jj}$ : crucial for Higgs self-coupling analysis

- ▶ sharper signal peak with simple SLD-correction 🟢

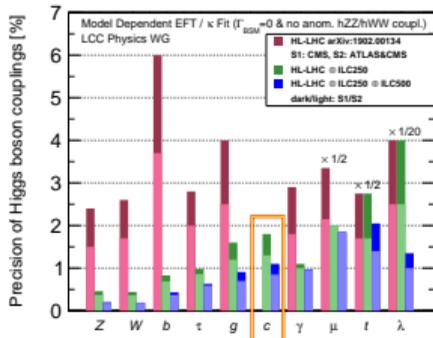
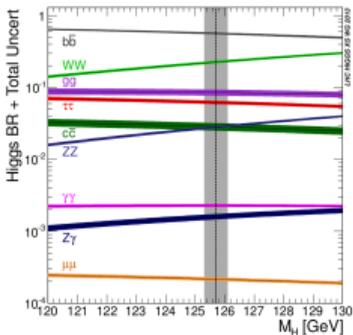


- ▶ merge signal-background 🟡



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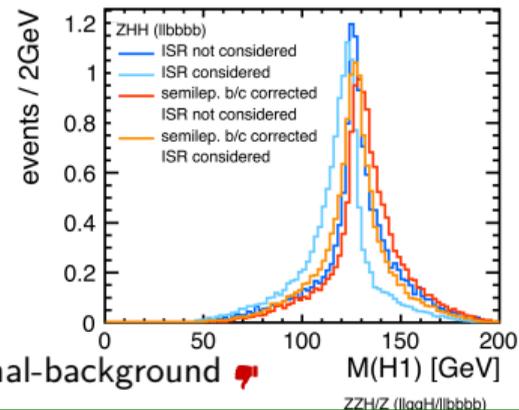
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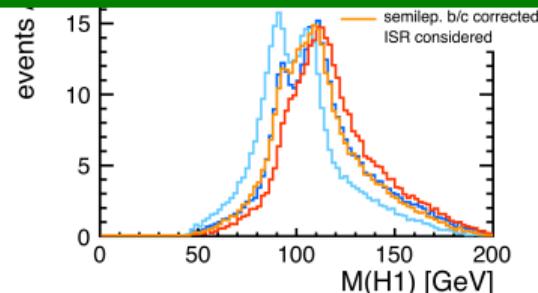
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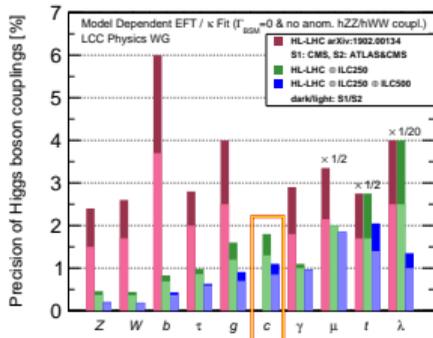
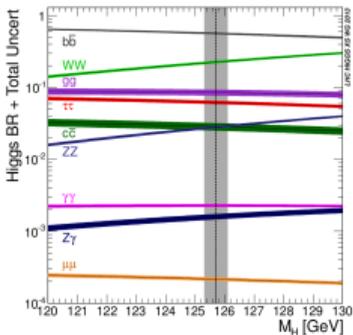
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perfect reco  $m_{jj} \Rightarrow$  improve  $\frac{\delta\lambda}{\lambda}$  by  $\sim 40\%$



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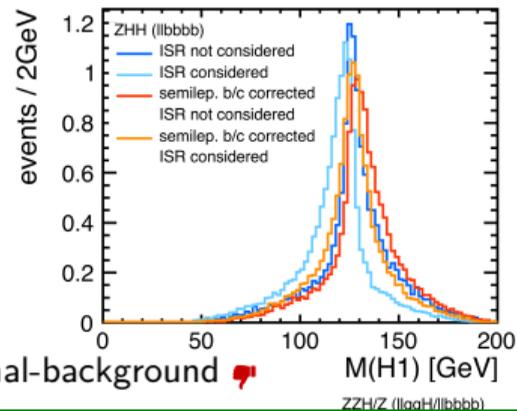
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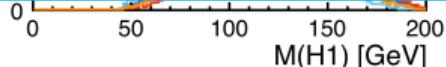
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better neutrino correction?

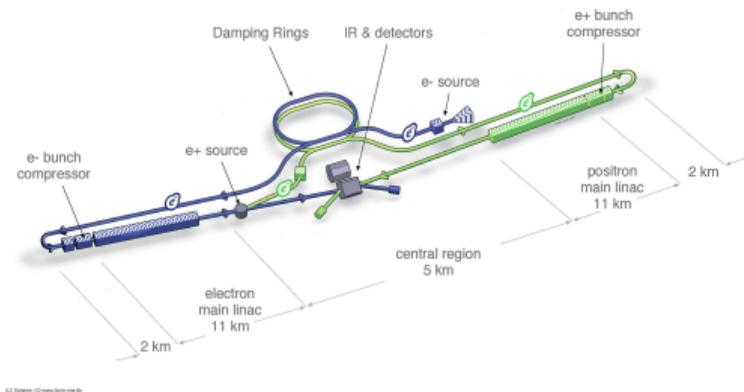
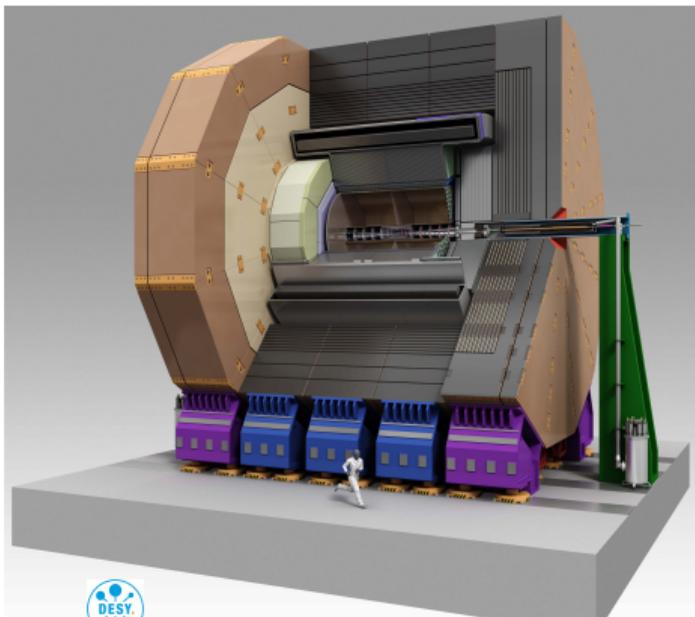
better jet error parameterisation?



# International Large Detector (ILD)

foreseen for the International Linear Collider (ILC)

- ▶ Polarized  $e^+e^-$  beams colliding at  $\sqrt{s} = 250\text{GeV}$  (upgrades: 500GeV and 1TeV)
  - ▶ detailed knowledge of initial states
  - ▶ clean collision environment



## ▶ International Large Detector:

- ▶ momentum resolution:

$$\sigma_{\frac{1}{pT}} \sim 2 \times 10^{-5} \text{ GeV}^{-1}$$

- ▶ impact parameter:

$$\sigma_{d_0} \sim 5 \mu\text{m}$$

- ▶ jet energy resolution:

$$\frac{\sigma_{E_j}}{E_j} \sim 3 - 4\%$$

- ▶ designed and optimized for Particle flow

## Concept of $\nu$ -correction in a semi-leptonic decay

- ▶ Find heavy-quark jets: Identify  $b$  or  $c$  jet  $\rightarrow$  flavour tag
- ▶ Find semi-leptonic decay(s): Identify lepton in jet if present  $\rightarrow$  possible using detector's high granularity
- ▶ Estimate neutrino energy from decay kinematics:
  - ▶ Assign  $B^0$  or  $D^0$  meson mass to mother hadron ( $m_X$ ).
  - ▶ Reconstruct flight direction of mother hadron ( $\parallel, \perp$ ) from position of primary and secondary vertex.
  - ▶ Calculate neutrino momentum: up to a **sign** ambiguity.

$$E_\nu = E_X - E_{vis} = \frac{E_{vis}E'_{vis} - \vec{p}_{vis\parallel} \cdot \vec{p}'_{vis\parallel}}{m_{vis}^2 + \vec{p}_{vis\perp}^2} m_X - E_{vis}$$

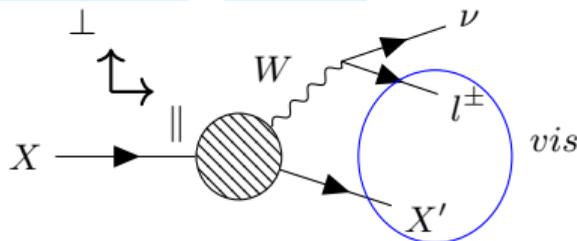
$$E'_{vis} = \frac{m_X^2 + m_{vis}^2}{2m_X} \quad \vec{p}'_{vis\parallel} = \pm \sqrt{\left(\frac{m_X^2 - m_{vis}^2}{2m_X}\right)^2 - \vec{p}_{vis\perp}^2}$$

( $E'_{vis}, \vec{p}'_{vis}$ ): visible 4-momentum in the rest frame of  $X$

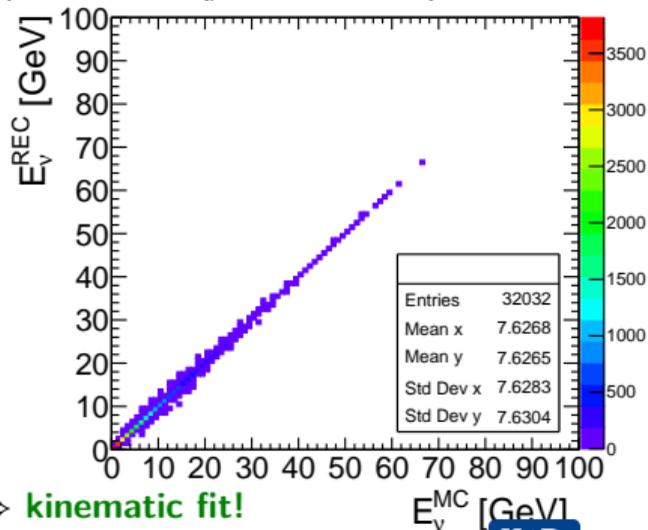
- ▶ As proof-of-principle: CHEAT from MC truth

The neutrino momentum can be determined up to a two-fold ambiguity

Can we use overall event kinematics to decide between solutions?  $\Rightarrow$  **kinematic fit!**



- ▶ Closure test: fully cheated information ( $H \rightarrow b\bar{b}$  at  $\sqrt{s} = 250$  GeV)



## $\nu$ -correction with reconstructed information

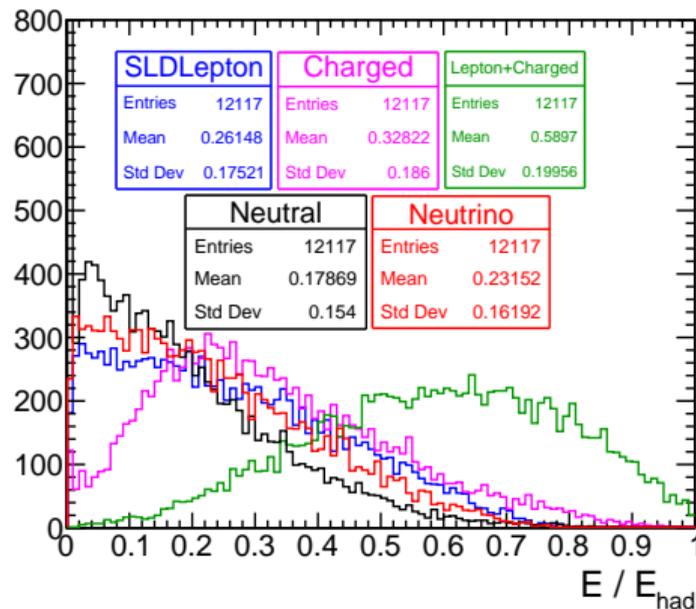
### reconstructed 4-momentum

Energy of parent hadron is distributed between:

- ▶ **Charged decay products:** reconstructed using tracker information:  
 $\Rightarrow$  rather **easy** to assign to  $2^{nd}$  vertex
  - ▶ lepton from semi-leptonic decay
  - ▶ other charged decay products
- ▶ **Neutral Particles:** reconstructed using calorimeter information:  
 $\Rightarrow$  difficult to assign to  $2^{nd}$  vertex  
 Many decays **without** extra neutral!
- ▶ **Neutrinos:** missing energy, needs  $\nu$ -correction

Charged particles profit excellent momentum resolution in ILD

Neutral particles have least contribution to the 4-momentum of parent hadron

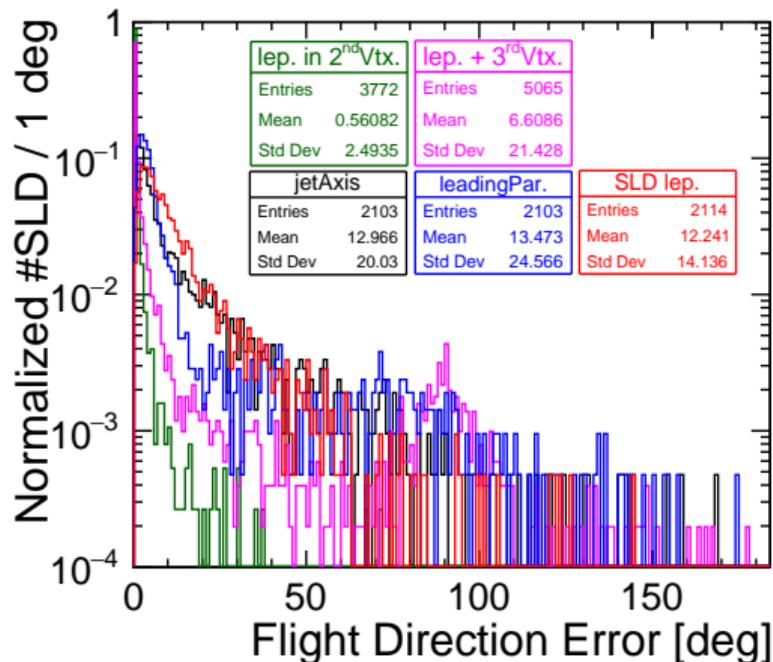


## $\nu$ -correction with reconstructed information

reconstructed flight direction of parent hadron

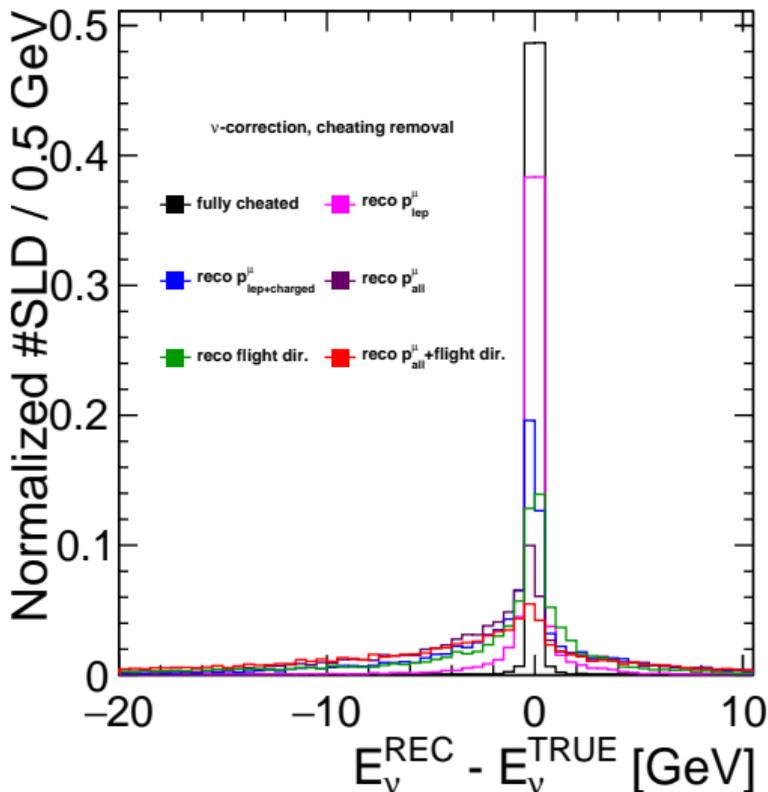
Probable scenarios:

- ▶ **lepton is in  $2^{nd}$  vertex**: direction from primary vertex to secondary vertex ( $\sim 30\%$  of SLD's)
- ▶ **lepton +  $3^{rd}$  vertex**: lepton is not in  $2^{nd}$  vertex, but a vertex exists in the jet ( $\sim 40\%$  of SLD's)  
 $\Rightarrow$  intersecting  $track_{lep}$  and  $\vec{p}_{3^{rd} vtx}$
- ▶ options for no vertex in jet ( $\sim 17\%$  of SLD's):
  - ▶ use **jet axis** as flight direction
  - ▶ use flight direction of **leading particle** in jet
  - ▶ use flight direction of **lepton from semi-leptonic decay**



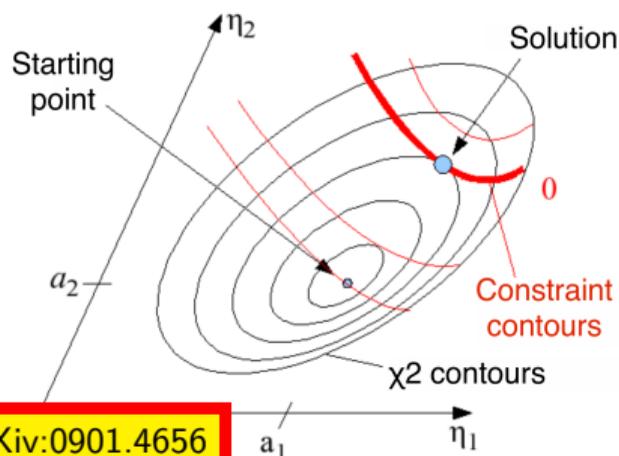
## $\nu$ -correction with reconstructed information

- ▶ use **reco 4-momentum** mainly affected by:
  - ▶  $\sigma_{p_T}$  for charged particles
  - ▶  $\sigma_{E_{CAL}}$  for neutral particles
- ▶ use **reco flight direction** mainly affected by:
  - ▶  $l$  in  $2^{nd}$  Vtx. /  $l+3^{rd}$  Vtx.: vertex finding algorithm and detector IP resolution ( $\sigma_{d_0}$  and  $\sigma_{z_0}$ )
  - ▶ no  $2^{nd}/3^{rd}$  Vtx.: hadrons decay so close to the IP, no chance to get the vertex!  
⇒ use jet axis
- ▶ **overall uncertainty** ( $\sigma_{E_\nu}$ ,  $\sigma_{\theta_\nu}$  and  $\sigma_{\phi_\nu}$ ) can be parameterized step-by-step
- ▶ **still cheated**: lepton ID, particle assignment (ongoing)



## Kinematic fit

- ▶ Kinematic fit: adjustment of measured quantities under certain kinematic constraints:
  - ▶ Energy and momentum conservation
  - ▶ Invariant masses of particles



- ▶ Minimize  $\chi^2$ :

$$\chi^2(\mathbf{a}, \boldsymbol{\xi}, \mathbf{f}) = (\boldsymbol{\eta} - \mathbf{a})^T \mathbf{V}^{-1} (\boldsymbol{\eta} - \mathbf{a}) - 2\boldsymbol{\lambda}^T \mathbf{f}(\mathbf{a}, \boldsymbol{\xi})$$

$\boldsymbol{\eta}$ : vector of measured kinematic variables ( $x$ )

$\mathbf{a}$ : vector of fitted quantities

$\boldsymbol{\xi}$ : vector of unmeasured kinematic variables

$\mathbf{V}$ : **covariance matrix**

$\boldsymbol{\lambda}$ : Lagrange multipliers

$\mathbf{f}(\mathbf{a}, \boldsymbol{\xi})$ : vector of constraints

Exploit well-known initial state in  $e^+e^-$  colliders

⇒ **need error parametrization, in particular for jets**

## Jet specific energy resolution

Parametrize sources of uncertainties (assumed uncorrelated) in jet energy measurements (`ErrorFlow`):

$$\sigma_{E_{jet}} = \sigma_{Det} \oplus \sigma_{Conf} \oplus \sigma_{\nu} \oplus \sigma_{Clus} \oplus \sigma_{Had}$$

- ▶  $\sigma_{Det}$ : Detector resolution using track and cluster parameters
- ▶  $\sigma_{Conf}$ : Particle confusion in Particle Flow Algorithm  
Estimated based on jet energy and neutral hadron / photon energy fractions
- ▶  $\sigma_{\nu}$ : Semi-leptonic decays: error propagation from neutrino correction  
currently none since cheating
- ▶  $\sigma_{Clus}$ : Misassignment of particles in the jet clustering, has not been included yet
- ▶  $\sigma_{Had}$ : Mismodeling of QCD effects in parton shower and hadronization, has not been included yet

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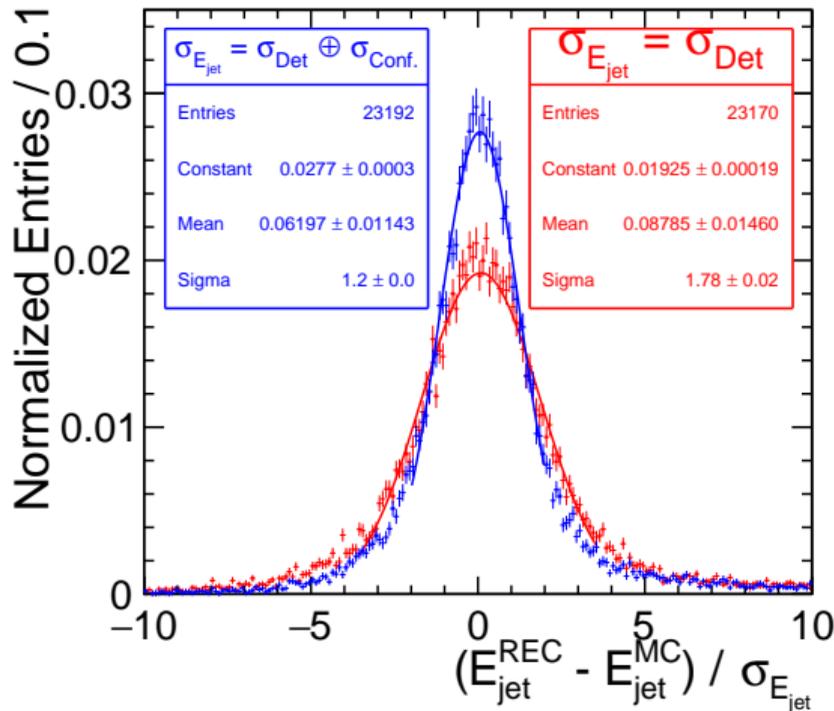


## Uncertainties in jet-level: Energy

Propagation of errors from PFOs to jets:

- ▶ Transform the covariance matrix of each PFO ( $E, x, y, z$  for clusters, track parameters for charged) to ( $E, p_x, p_y, p_z$ )
- ▶ Add up covariance matrices of all PFOs
- ▶ Add confusion term for jet energy
  - ▶ calculate using jet energy composition
- ▶ Transform to ( $E, \theta, \phi, m$ )

arXiv:2105.08480



Confusion term improves the estimate of the jet energy uncertainty, but not quite enough  $\Rightarrow$  need adjustment  
 $\Rightarrow$  **use scaling factor 1.2 in Kinematic fit**

## Application of kinematic fit to $e^+e^- \rightarrow ZH \rightarrow \mu\bar{\mu}b\bar{b}$ events

Parameters of jets and leptons are varied within their uncertainties to satisfy 5 constraints:  
Conservation of momentum (hard constraints):

- ▶  $p_x$ :  $e^+e^-$  crossing angle: 14 mrad  
 $\Sigma p_x = \sqrt{s} \times \sin 0.007 \approx 1.75$  GeV
- ▶  $p_y$ :  $\Sigma p_y = 0$
- ▶  $p_z$ :  $\Sigma p_z = 0$

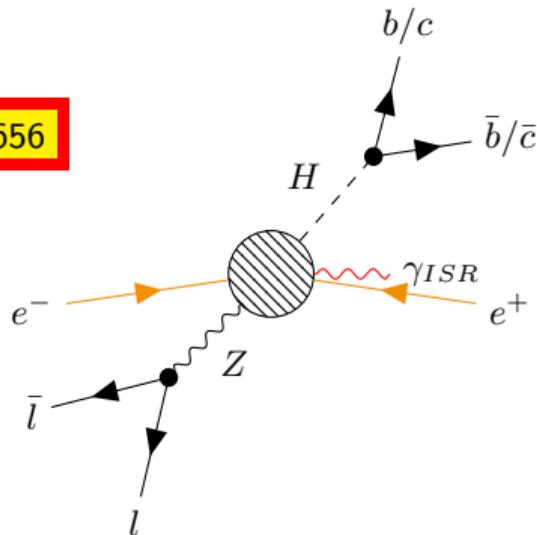
Conservation of total energy (hard constraint):

- ▶  $E_{lab} = 2\sqrt{(\frac{\sqrt{s}}{2})^2 + (\Sigma p_x)^2}$

Constrain di-muon mass to agree with  $m_Z$  within its natural width  
(soft constraint):

- ▶  $m_Z = 91.2$  GeV ,  $\sigma_{m_Z} = \frac{2.5}{2}$

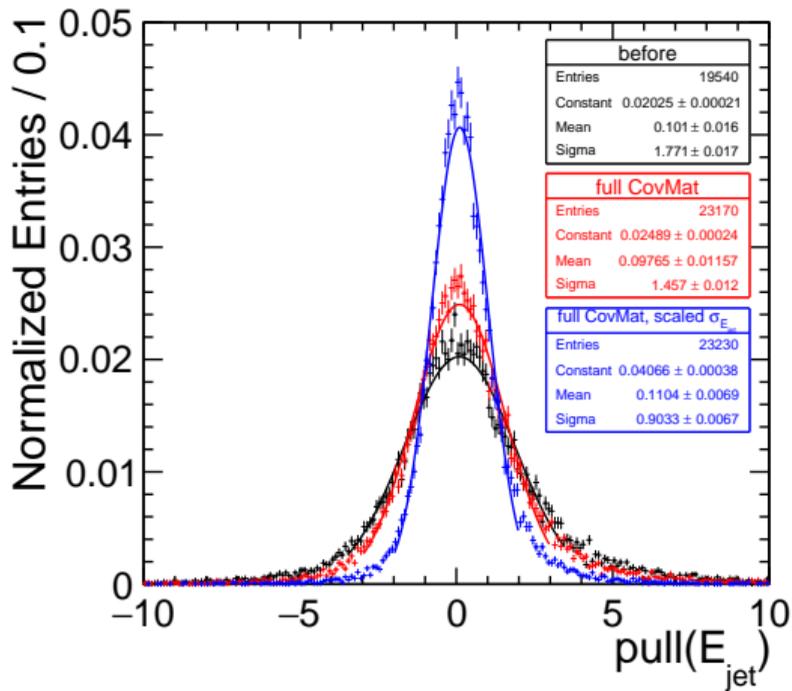
arXiv:0901.4656



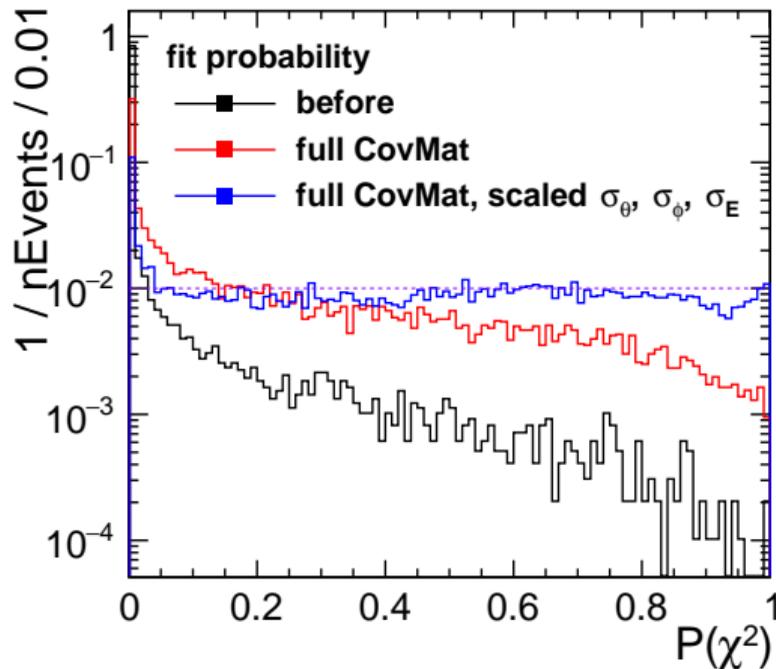
# Kinematic fit performance in $e^+e^- \rightarrow ZH \rightarrow \mu\bar{\mu}b\bar{b}$ at $\sqrt{s} = 250$ GeV

without semi-leptonic decays

► pull distribution



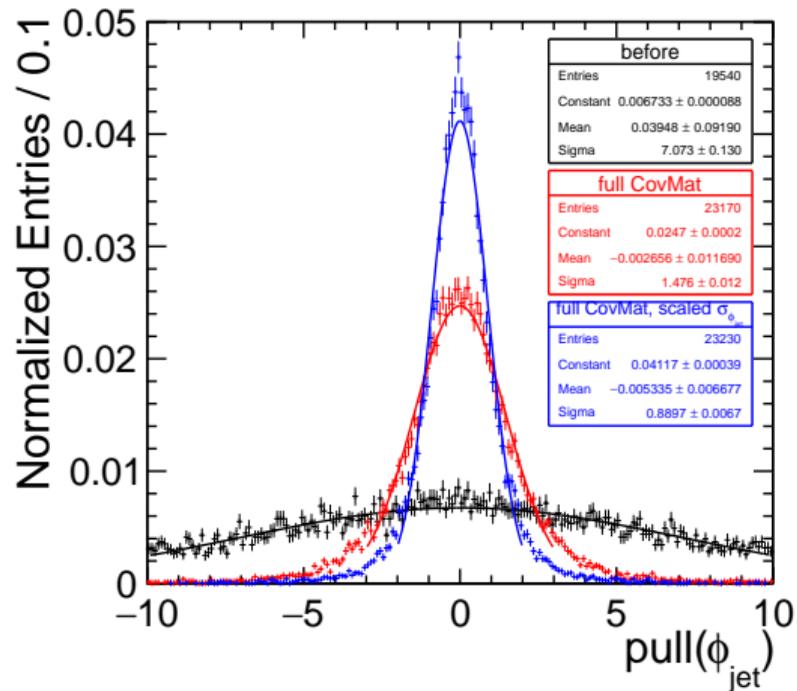
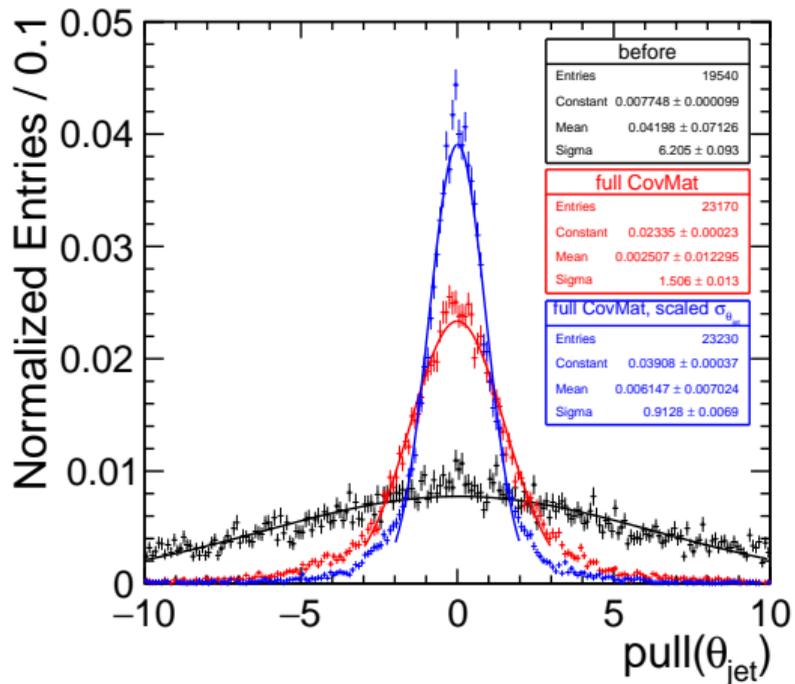
► fit probability



Improved kinematic fit performance with full CovMat of jets + scaled jet energy uncertainty

# Kinematic fit performance in $e^+e^- \rightarrow ZH \rightarrow \mu\bar{\mu}b\bar{b}$ at $\sqrt{s} = 250$ GeV (cntd.)

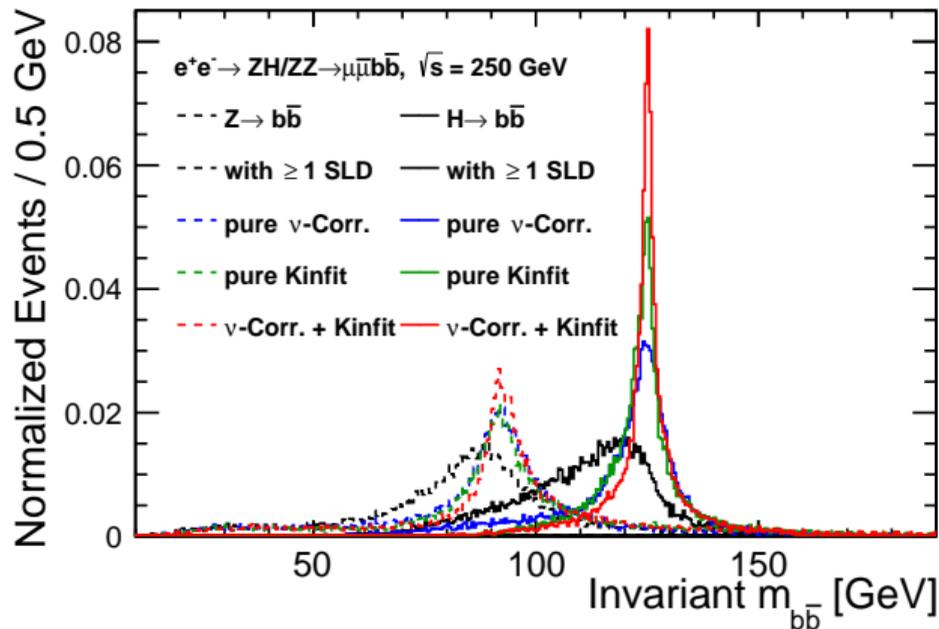
without semi-leptonic decays



Improved kinematic fit performance with full CovMat of jets + scaled jet angular uncertainties

## Z/Higgs mass reconstruction in presence of SLDs

- ▶  $\nu$ -correction alone recovers  $Z/H$  mass:
  - ▶ resolve sign ambiguity by kinematic fit
  - ▶ pre-fit  $(E_\nu, \vec{p}_\nu)$  is used
- ▶ striking improvement from new jet error parametrisation fed to kinematic fit even without  $\nu$ -correction
- ▶ significant further improvement by combined kinematic fit and  $\nu$ -correction (fully cheated), especially for the Higgs peak
- ▶ less powerful  $\nu$ -correction  $\Rightarrow$  performance is expected between Green and Red



## Conclusions

- ▶ Higgs mass reconstruction essential eg in  $ZZH$  vs  $ZHH$  separation (Higgs self-coupling measurement)
- ▶ Heavy flavour jets are essential for Higgs physics
- ▶ Correction of semi-leptonic decays of heavy flavour jets is important for Higgs mass reconstruction
  - ▶ Neutrino momentum can be reconstructed up to a sign ambiguity
  - ▶ Ambiguity can be resolved by kinematic fit
  - ▶ Next: remove the partial cheating from the neutrino correction
- ▶ Kinematic fit exploits well-known initial state in  $e^+e^-$  colliders and requires excellent understanding of jet measurement
- ▶ ILD as a Particle Flow detector provides full detail for estimating jet measurement uncertainties
- ▶ huge improvement on  $Z/H \rightarrow b\bar{b}$  di-jet mass reconstruction has been achieved
- ▶ Tools (`ErrorFlow`, `MarlinKinfitProcessors`, ...) available in [github.com/iLCSoft](https://github.com/iLCSoft)

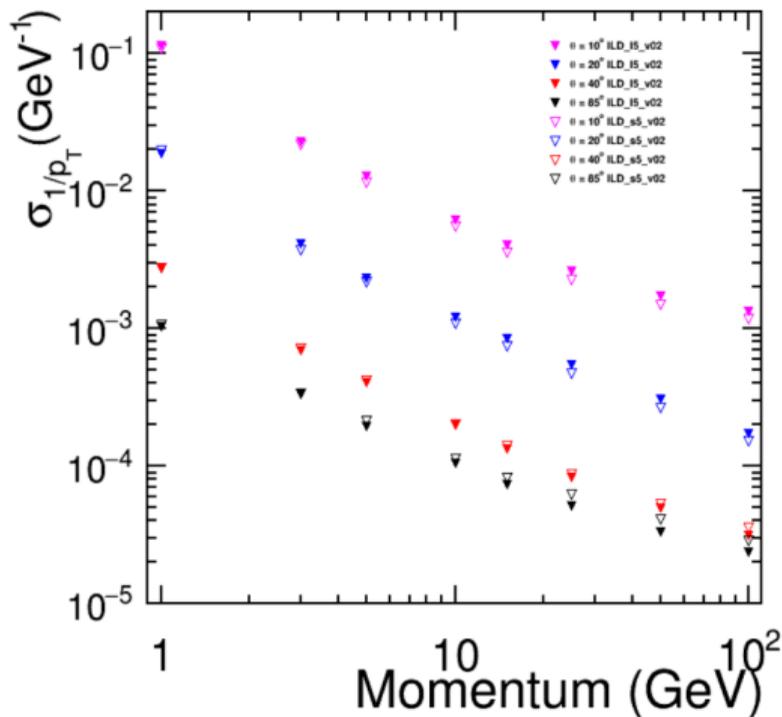


# BACKUP

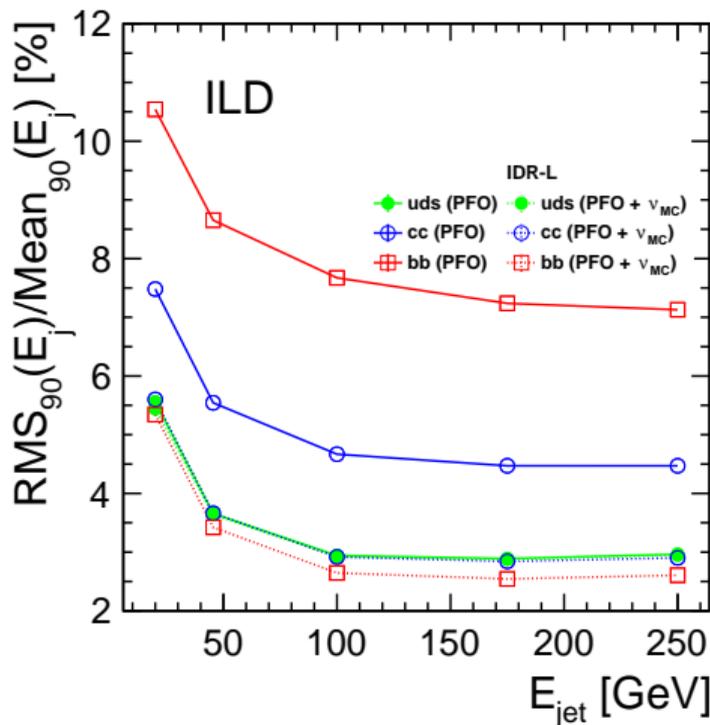
# International Large Detector (ILD)

arXiv:2003.01116

## ► Momentum Resolution



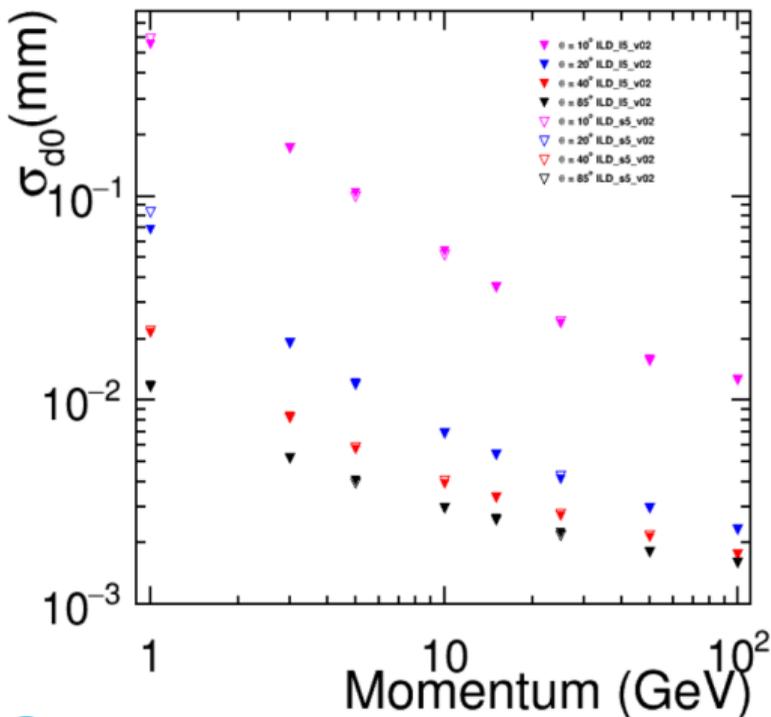
## ► Jet Energy Resolution ( $E_{PFO} + E_V^{MC}$ )



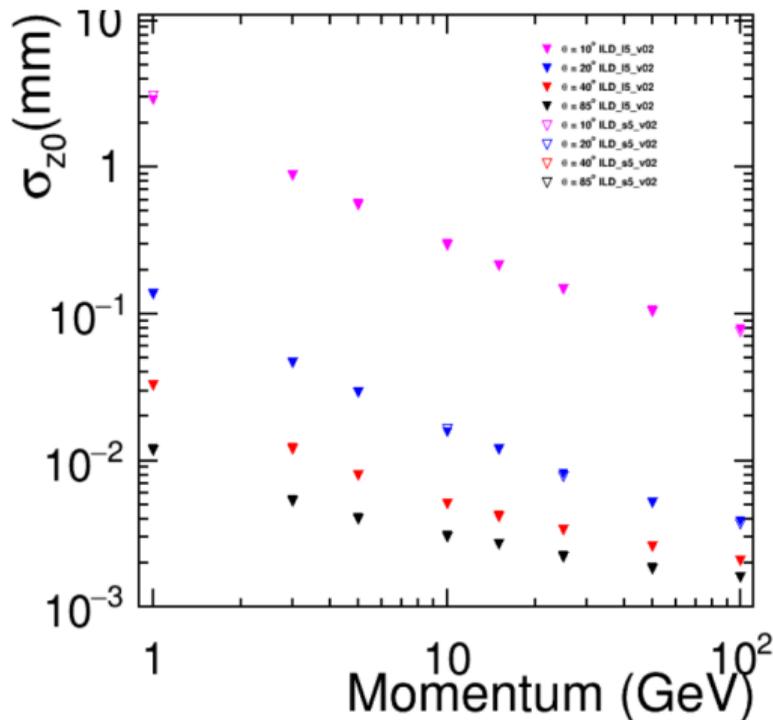
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## ► Impact Parameter Resolution, $d_0$



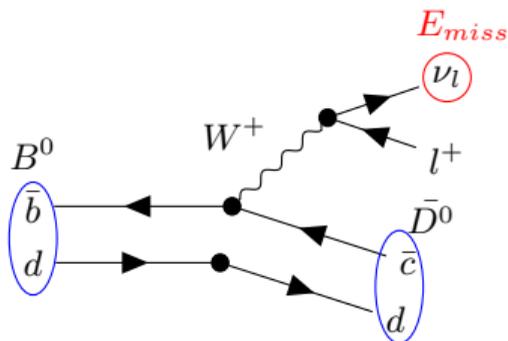
## ► Impact Parameter Resolution, $z_0$



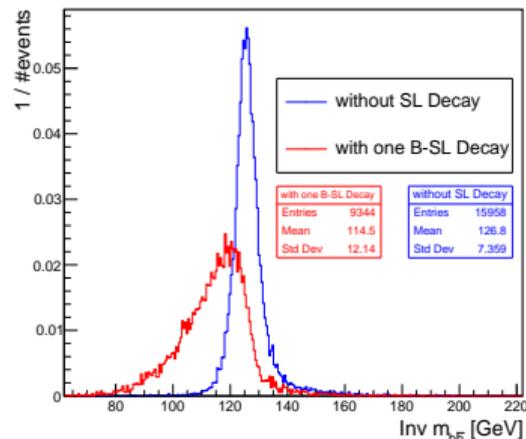
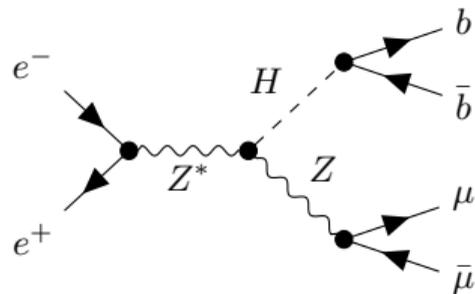
## Semi-leptonic $b / c$ decays

- ▶ Number of B-/C-hadron semileptonic decays (SLD) in  $e^+e^- \rightarrow b\bar{b}$  events

		nBSLD		
		0	1	2
nCSLD	0	34%	24%	4%
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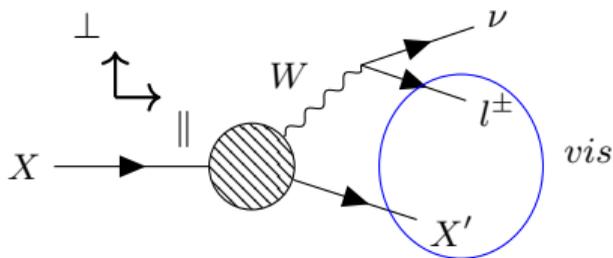
- ▶ Mis-reconstruction of  $b\bar{b}$  invariant mass due to **missing neutrino energy** from semi-leptonic decays
- ▶ Can the **missing momentum** be retrieved from event and decay kinematics?



# correcting neutrino energy

## 4-vector based approach

- ▶  $(E, \vec{p})$ -based approach



$$\vec{p}_{\nu, \perp} = -\vec{p}_{vis, \perp}$$

$$\vec{p}_{\nu, \parallel} = \frac{1}{2D}(-A \pm \sqrt{A^2 - BD})\hat{n}$$

$$A = p_{vis, \parallel} (2p_{vis, \perp}^2 + m_{vis}^2 - m_X^2)$$

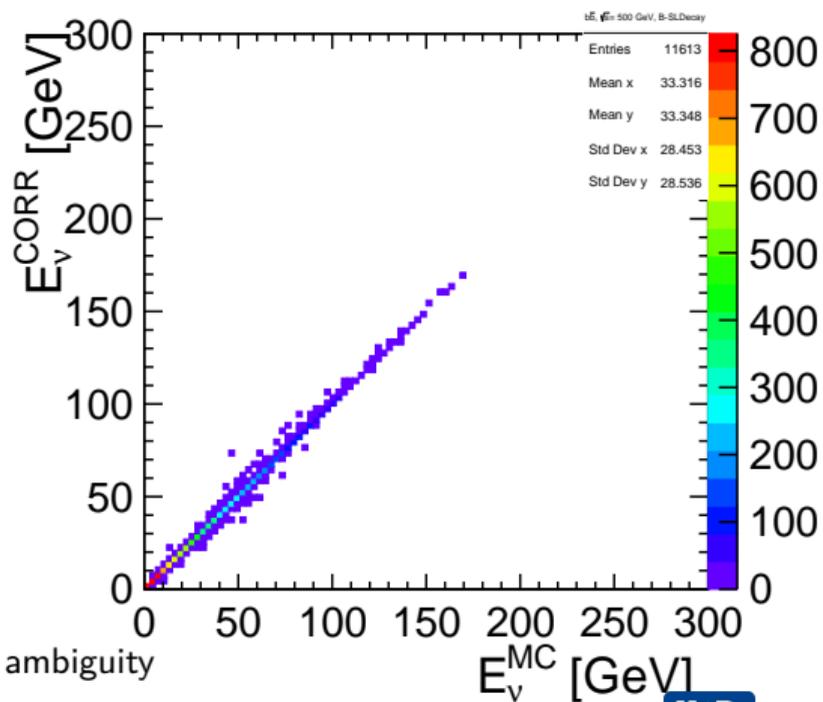
$$B = 4p_{vis, \perp}^2 E_{vis}^2 - (2p_{vis', \perp}^2 + m_{vis}^2 - m_X^2)^2$$

$$D = E_{vis}^2 - p_{vis, \parallel}^2$$

$$\hat{n} = \frac{p_{vis, \parallel}}{|p_{vis, \parallel}|}$$

The neutrino momentum can be determined up to a two-fold ambiguity

- ▶ closure test: apply correction with fully cheated information and compare with true neutrino energy

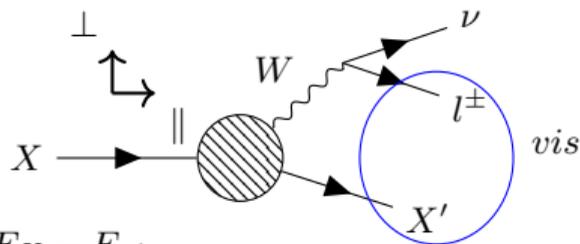


# Correcting neutrino energy

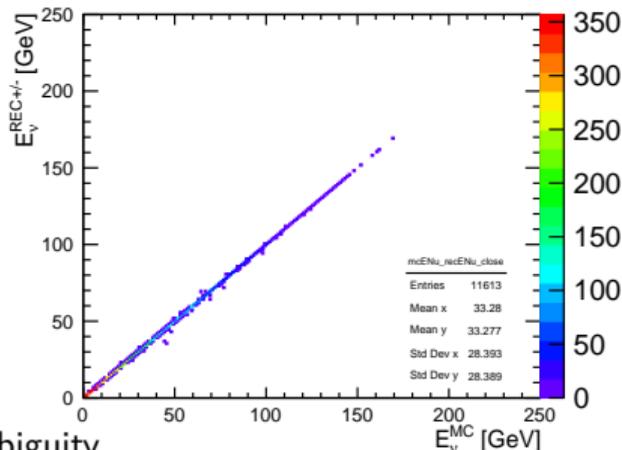
## Rapidity based approach

Rapidity under Lorentz-transformations  $\sim$  velocity under Galileo-transformations:  $\omega = \omega_X + \omega'$ ;  $\omega = \frac{1}{2} \ln \frac{E+p'_{\parallel}}{E-p'_{\parallel}}$

$\omega$ : rapdity in lab frame,  $\omega'$ : rapdity in rest frame of  $X$ ,  $\omega_X$ : rapdity of  $X$  in lab frame



- Closure test: fully cheated information ( $e^+e^- \rightarrow b\bar{b}$  at  $\sqrt{s} = 500$  GeV)



$$E_\nu = E_X - E_{vis}$$

$$E_X = \frac{E_{vis}E'_{vis} - p_{vis\parallel}p'_{vis\parallel}}{m_{vis}^2 + p_{vis\perp}^2} m_X$$

$$E'_{vis} = \frac{m_X^2 + m_{vis}^2}{2m_X}$$

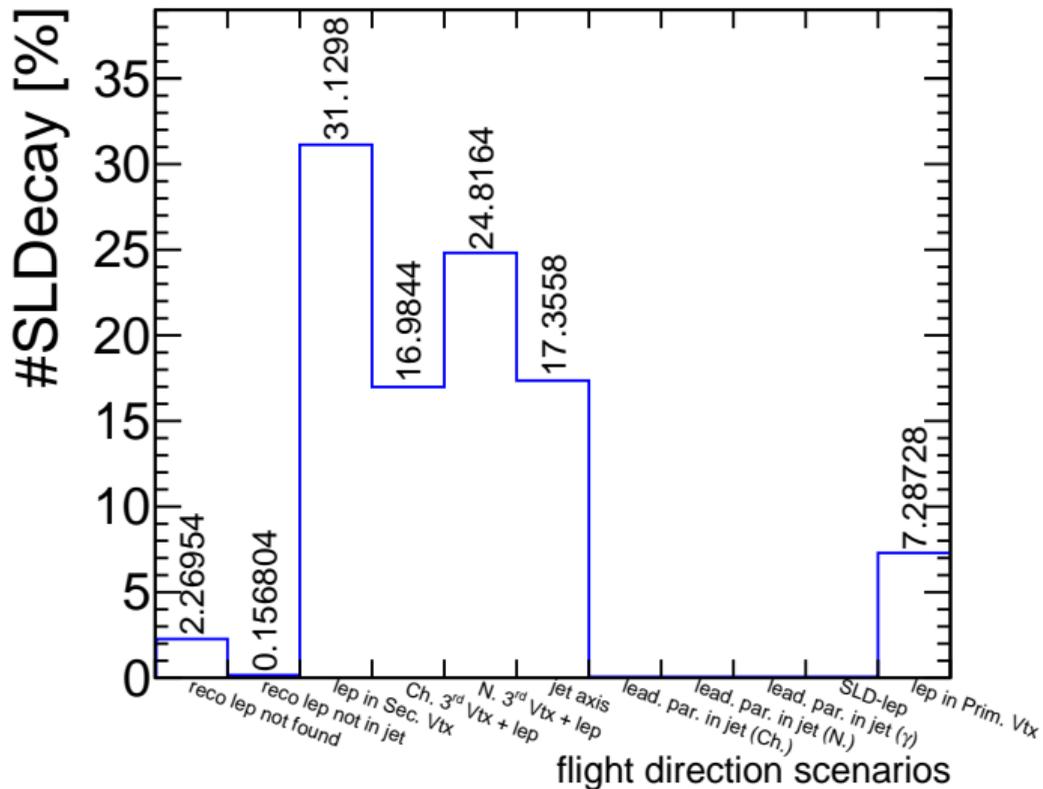
$$p'_{vis\parallel} = \pm \sqrt{\left(\frac{m_X^2 - m_{vis}^2}{2m_X}\right)^2 - p_{vis\perp}^2}$$

The neutrino momentum can be determined up to a two-fold ambiguity

Can we use overall event kinematics to decide between solutions?  $\Rightarrow$  kinematic fit!

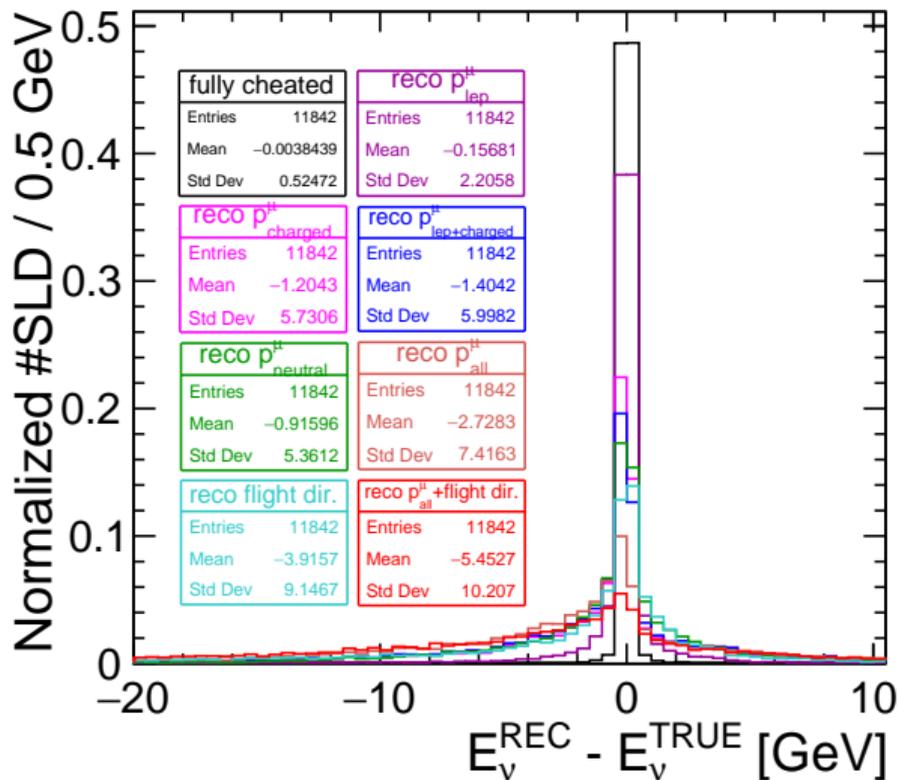
# $\nu$ -correction with reconstructed information

reconstructed flight direction of parent hadron



## $\nu$ -correction with reconstructed information

- ▶ use reco  $4p$  mainly affected by:
  - ▶  $\sigma_{p_T}$  for charged particles
  - ▶  $\sigma_{E_{CAL}}$  for neutral particles
- ▶ use reco flight direction mainly affected by vertex finding algorithm and detector IP resolution ( $\sigma_{d_0}$  and  $\sigma_{z_0}$ )
- ▶ overall uncertainty ( $\sigma_{E_\nu}$ ,  $\sigma_{\theta_\nu}$  and  $\sigma_{\phi_\nu}$ ) can be parameterized step-by-step
- ▶ still cheated: lepton ID, particle assignment (ongoing)

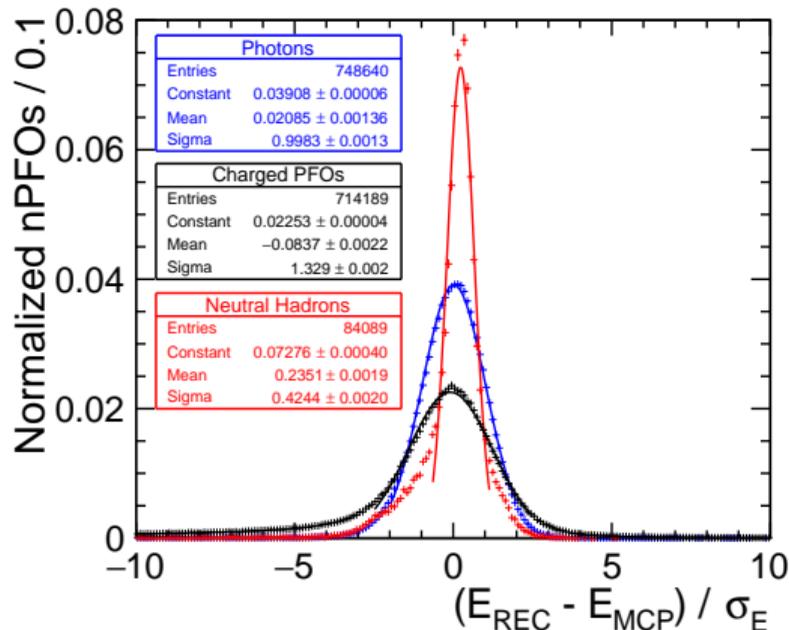


# ErrorFlow: Jet Error Parametrisation from Particle Flow Objects (PFO)

## Energy

Error estimation in PFO level:

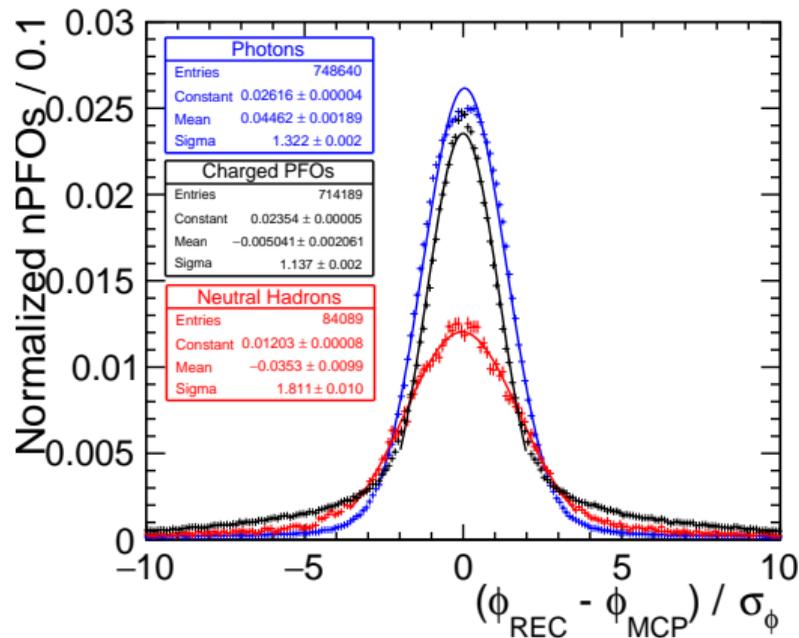
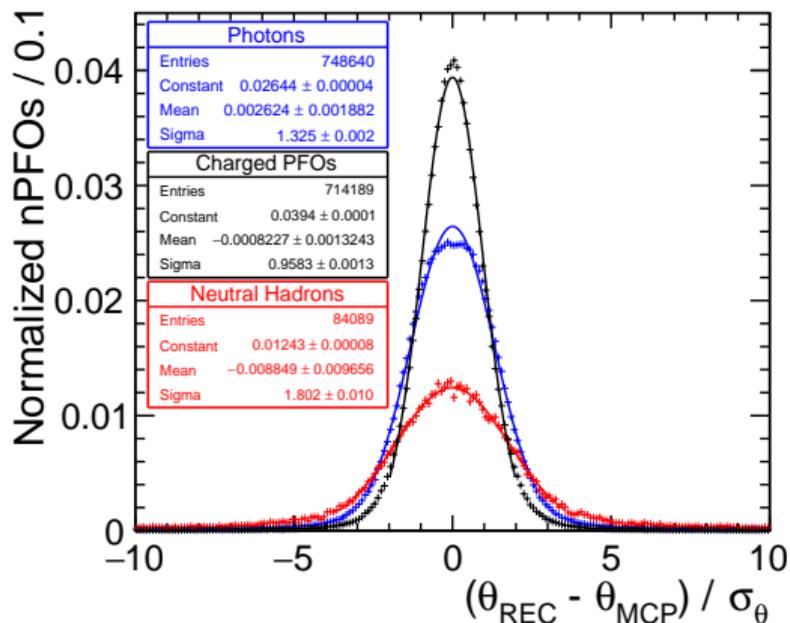
- ▶ **Photons:** energy error is perfectly modeled.  
(sigma  $\sim 1$ )
- ▶ **Charged PFOs:** uncertainties propagated from track fit covariance matrix
  - ▶ uncertainties 30% too small
  - ▶ possible future improvement from track refitting with specific mass hypothesis after particle ID
- ▶ **Neutral Hadrons:** energy and energy error are significantly overestimated.  
work on improvement in progress.



# ErrorFlow: Jet Error Parametrisation from Particle Flow Objects (PFO)

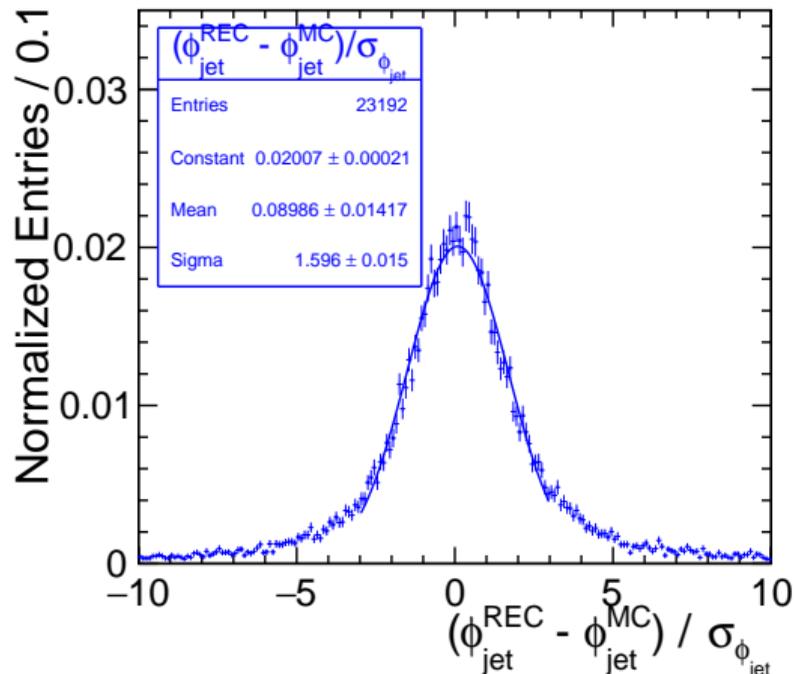
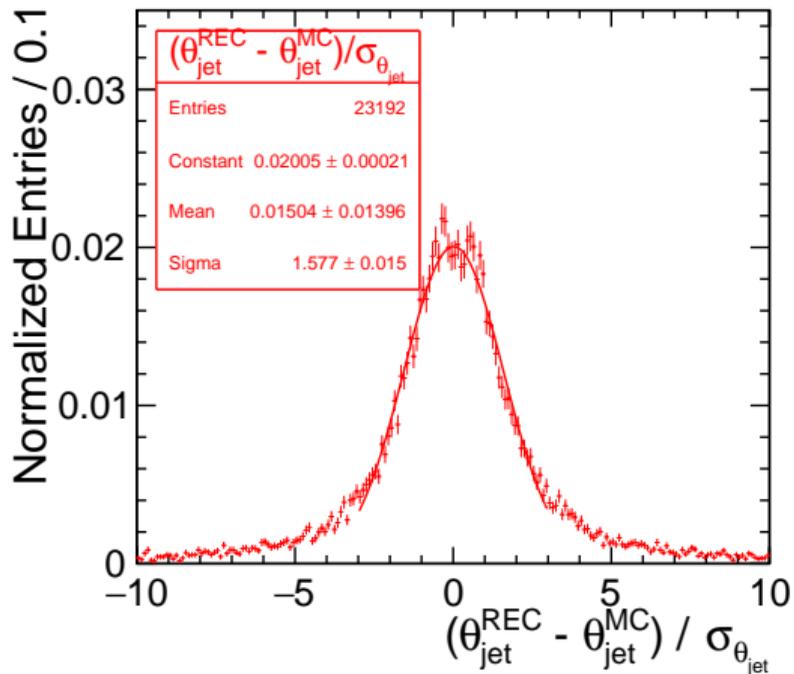
## Angles

The angular uncertainties obtained directly from track parameters / cluster position errors



⇒ Scale  $\sigma_{\theta}$  and  $\sigma_{\phi}$  by factor  $\sim 1.3$  (for photons) and  $\sim 1.8$  (for neutral hadrons)

## Uncertainties in jet-level: $\theta$ & $\phi$



Jet angular uncertainties need scaling factor  $\sim 1.6$

## Event selection

Select  $e^+e^- \rightarrow ZH \rightarrow \mu\bar{\mu}b\bar{b}$  events at  $\sqrt{s} = 250$  GeV with (exactly) 2-leptons + 2-jets final state:

### ► IsolatedLeptonTagging

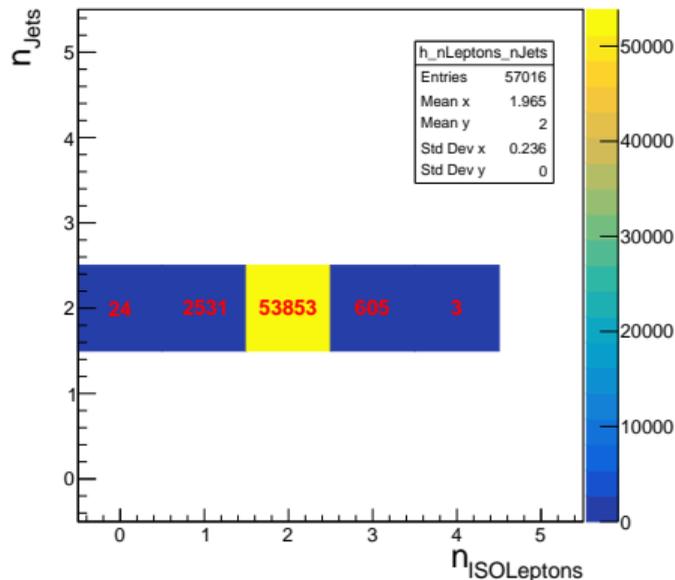
Training for the IDR 500 GeV samples is used,

1. Lepton ID:  $\mu^\pm$   
Deposited energy in subdetectors
2. Vertex: primary or secondary  
Significance of impact parameters ( $d_0, z_0$ )
3. Isolated: not belong to jets

### ► FastJetProcessor

- Exclusive  $k_t$  (Durham) algorithm (no overlay)
- Find smallest of  $(d_{ij}, d_{iB})$   

$$d_{ij} = 2 \min(E_i^2, E_j^2)(1 - \cos \theta_{ij})$$
 $i, j$ : particles,  $B$ : Beam
- $d_{ij} < d_{iB}$ : combine  $i$  &  $j$  as pseudojet( $p$ ):  $p_i + p_j$
- $d_{iB} < d_{ij}$ : remove particle  $i$  from list
- Repeat iteration until  $d_{ij}$  or  $d_{iB} > d_{cut}$ (threshold)

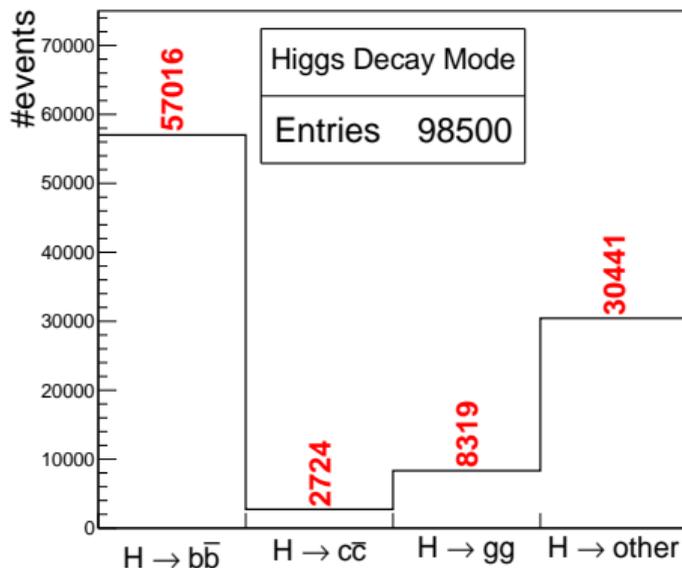


IsolatedLeptonTagging has not been trained for new software at 250 GeV yet!



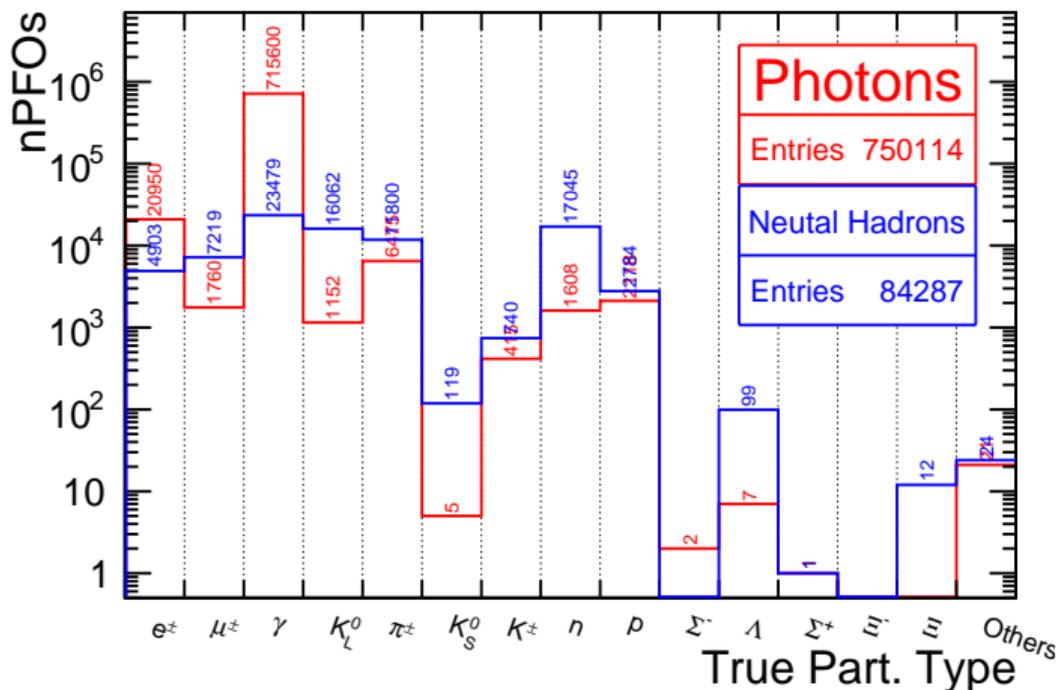
## event selection

separate Higgs decay modes:  $H \rightarrow b\bar{b}$ , cheat from MCTruth



$\frac{2}{3}$  of  $b\bar{b}$  jets contain at-least one semi-leptonic decay  $\Rightarrow$  Frequent  $H \rightarrow b\bar{b}$  needs neutrino correction.

## Neutral PFO identification by Pandora



Majority of identified photons are true photons.

No explicit decision for mass of identified neutral hadrons due to their multiplicity.



## Pandora treatment with Neutral Hadrons

What Pandora does:

- ▶ Cluster energy is assigned to PFO(massless) energy  
 $E_{PFO} = |\vec{p}_{PFO}| = E_{cluster}$
- ▶ Neutral Hadrons are identified as neutron
- ▶ neutron mass is set for PFO  $\Rightarrow$  **inconsistent 4-momentum!**
- ▶ CovMat of Neutral PFO is calculated (using inconsistent 4-momentum):

$$\text{CovMat}(\vec{p}, E) = J^T \text{CovMat}(\vec{x}_{clu}, E_{clu}) J$$

$$J = \begin{pmatrix} \frac{\partial p_x}{\partial x_c} & \frac{\partial p_y}{\partial x_c} & \frac{\partial p_z}{\partial x_c} & \frac{\partial E}{\partial x_c} \\ \frac{\partial p_x}{\partial y_c} & \frac{\partial p_y}{\partial y_c} & \frac{\partial p_z}{\partial y_c} & \frac{\partial E}{\partial y_c} \\ \frac{\partial p_x}{\partial z_c} & \frac{\partial p_y}{\partial z_c} & \frac{\partial p_z}{\partial z_c} & \frac{\partial E}{\partial z_c} \\ \frac{\partial p_x}{\partial E_c} & \frac{\partial p_y}{\partial E_c} & \frac{\partial p_z}{\partial E_c} & \frac{\partial E}{\partial E_c} \end{pmatrix}$$

CovMat( $\vec{p}, E$ ) of Neutral PFOs depend on the mass assumption.

Suggestion: Take consistent 4-momentum of massive neutral hadrons for CovMat calculations.

## CovMat of Neutral PFOs

- ▶ Current CovMat calculation (MarlinReco/Analysis/AddClusterProperties)

$$E_{PFO} = |\vec{p}_{PFO}| = E_{clu} , p_x = E_{clu} \frac{x}{r} , p_y = E_{clu} \frac{y}{r} , p_z = E_{clu} \frac{z}{r}$$

- ▶ Alternative CovMat calculation (taking consistent 4-momentum of neutral hadrons)

$$E_{PFO} = \sqrt{|\vec{p}_{PFO}|^2 + m_{PFO}^2} = \sqrt{E_{clu}^2 + m_n^2}$$

$$J = \begin{pmatrix} E_{clu} \frac{r^2 - x^2}{r^3} & -E_{clu} \frac{xy}{r^3} & -E_{clu} \frac{xz}{r^3} & 0 \\ -E_{clu} \frac{xy}{r^3} & E_{clu} \frac{r^2 - y^2}{r^3} & -E_{clu} \frac{yz}{r^3} & 0 \\ -E_{clu} \frac{xz}{r^3} & -E_{clu} \frac{yz}{r^3} & E_{clu} \frac{r^2 - z^2}{r^3} & 0 \\ \frac{x}{r} & \frac{y}{r} & \frac{z}{r} & 1 \end{pmatrix} \rightarrow J = \begin{pmatrix} E_{clu} \frac{r^2 - x^2}{r^3} & -E_{clu} \frac{xy}{r^3} & -E_{clu} \frac{xz}{r^3} & 0 \\ -E_{clu} \frac{xy}{r^3} & E_{clu} \frac{r^2 - y^2}{r^3} & -E_{clu} \frac{yz}{r^3} & 0 \\ -E_{clu} \frac{xz}{r^3} & -E_{clu} \frac{yz}{r^3} & E_{clu} \frac{r^2 - z^2}{r^3} & 0 \\ \frac{E}{E_{clu}} \cdot \frac{x}{r} & \frac{E}{E_{clu}} \cdot \frac{y}{r} & \frac{E}{E_{clu}} \cdot \frac{z}{r} & 1 \end{pmatrix}$$

using error propagation, PFO angular uncertainties are calculated directly from cluster position error:

$$\sigma_\theta^2 = \left(\frac{\partial\theta}{\partial x}\right)^2 \sigma_x^2 + \left(\frac{\partial\theta}{\partial y}\right)^2 \sigma_y^2 + \left(\frac{\partial\theta}{\partial z}\right)^2 \sigma_z^2 + \frac{\partial\theta}{\partial x} \frac{\partial\theta}{\partial y} \sigma_{xy} + \frac{\partial\theta}{\partial x} \frac{\partial\theta}{\partial z} \sigma_{xz} + \frac{\partial\theta}{\partial y} \frac{\partial\theta}{\partial z} \sigma_{yz}$$

$$\sigma_\phi^2 = \left(\frac{\partial\phi}{\partial x}\right)^2 \sigma_x^2 + \left(\frac{\partial\phi}{\partial y}\right)^2 \sigma_y^2 + \frac{\partial\phi}{\partial x} \frac{\partial\phi}{\partial y} \sigma_{xy}$$

**MUST:** angular and energy uncertainties remain unchanged!

## CovMat of Jets

- ▶ AddClusterProperties/FourMomentumCovMat:  $\text{CovMat}(\text{cluster}/\text{track}) \rightarrow \text{CovMat}(\vec{p}, E)$

- ▶ Current CovMat calculation (inconsistent 4-momentum of neutral hadrons):

$$E_{PFO} = |\vec{p}_{PFO}| = E_{clu}, \quad p_x = E_{clu} \frac{x}{r}, \quad p_y = E_{clu} \frac{y}{r}, \quad p_z = E_{clu} \frac{z}{r}, \quad m_{PFO} = m_n$$

- ▶ Alternative CovMat calculation (taking consistent 4-momentum of neutral hadrons)

$$E_{PFO} = \sqrt{|\vec{p}_{PFO}|^2 + m_{PFO}^2} = \sqrt{E_{clu}^2 + m_n^2}$$

$J_{(wrong)} \rightarrow J_{(right)}$

$$\begin{pmatrix} E_{clu} \frac{r^2 - x^2}{r^3} & -E_{clu} \frac{xy}{r^3} & -E_{clu} \frac{xz}{r^3} & 0 \\ -E_{clu} \frac{xy}{r^3} & E_{clu} \frac{r^2 - y^2}{r^3} & -E_{clu} \frac{yz}{r^3} & 0 \\ -E_{clu} \frac{xz}{r^3} & -E_{clu} \frac{yz}{r^3} & E_{clu} \frac{r^2 - z^2}{r^3} & 0 \\ \frac{x}{r} & \frac{y}{r} & \frac{z}{r} & 1 \end{pmatrix}_{wrong} \rightarrow \begin{pmatrix} E_{clu} \frac{r^2 - x^2}{r^3} & -E_{clu} \frac{xy}{r^3} & -E_{clu} \frac{xz}{r^3} & 0 \\ -E_{clu} \frac{xy}{r^3} & E_{clu} \frac{r^2 - y^2}{r^3} & -E_{clu} \frac{yz}{r^3} & 0 \\ -E_{clu} \frac{xz}{r^3} & -E_{clu} \frac{yz}{r^3} & E_{clu} \frac{r^2 - z^2}{r^3} & 0 \\ \frac{E}{E_{clu}} \cdot \frac{x}{r} & \frac{E}{E_{clu}} \cdot \frac{y}{r} & \frac{E}{E_{clu}} \cdot \frac{z}{r} & 1 \end{pmatrix}_{right}$$

- ▶ ErrorFlow:

$$\text{CovMat}(\vec{p}_{jet}, E_{jet}) = \sum_{PFO} \text{CovMat}(\vec{p}, E) \quad : \quad \sigma_{E_{jet}}^2 = \sigma_{conf}^2 + \sum_{PFO} \sigma_{E_{PFO}}^2$$

- ▶ MarlinKinfitProcessors:

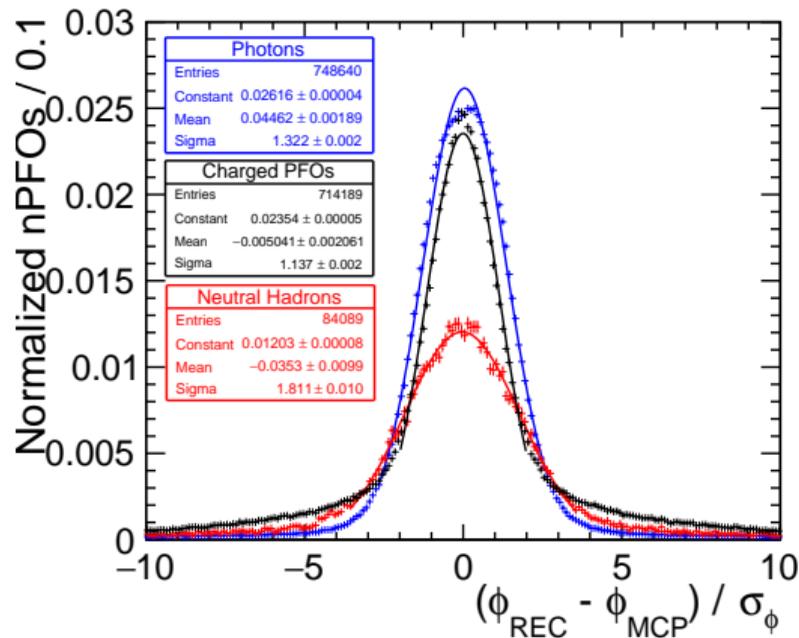
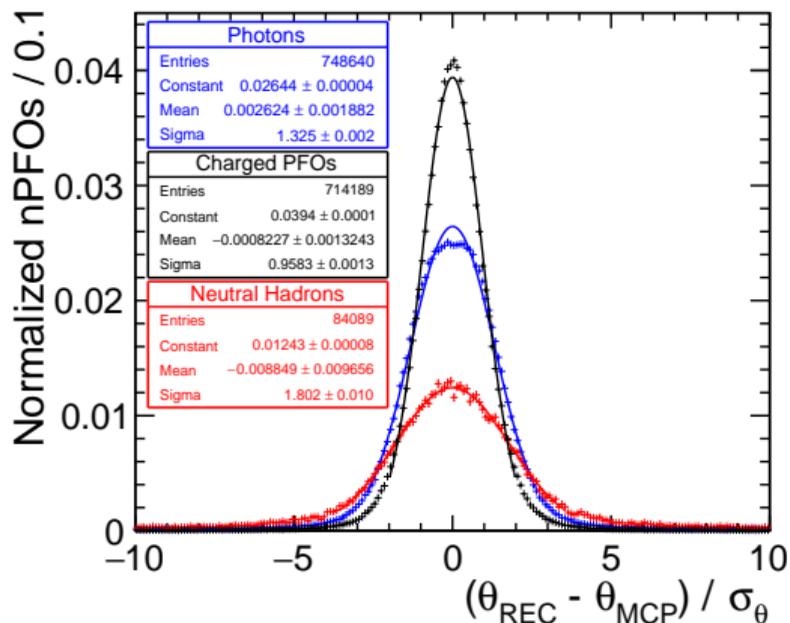
$$\text{CovMat}(\vec{p}_{jet}, E_{jet}) \rightarrow (\sigma_{\theta_{jet}}, \sigma_{\phi_{jet}}, \sigma_{E_{jet}})$$



# ErrorFlow: Jet Error Parametrisation from Particle Flow Objects (PFO)

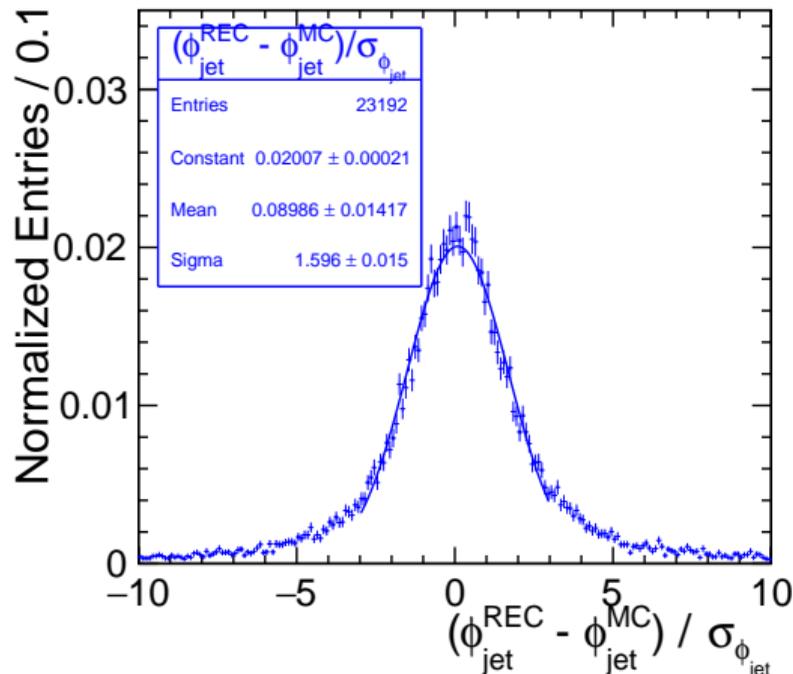
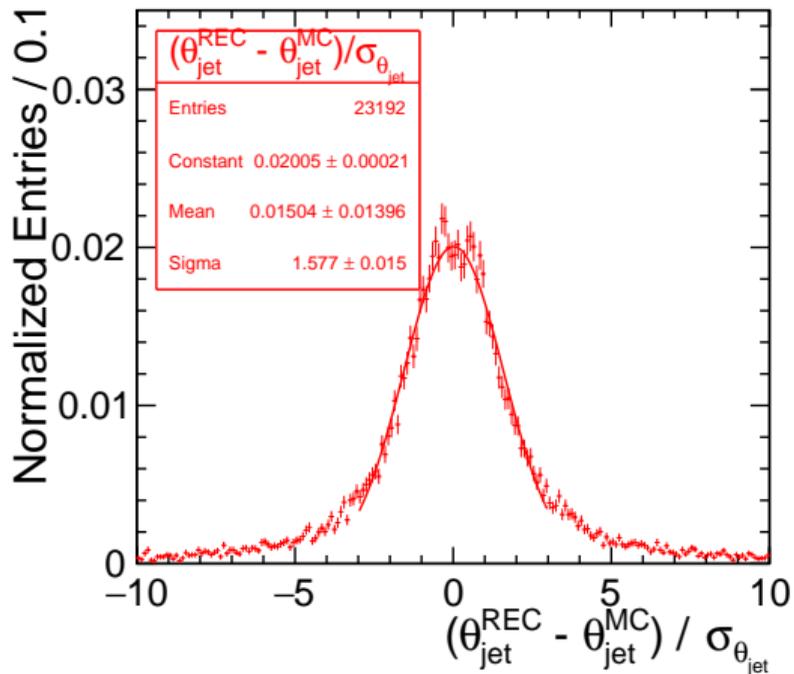
## Angles

The angular uncertainties obtained directly from track parameters / cluster position errors



⇒ Scale  $\sigma_{\theta}$  and  $\sigma_{\phi}$  by factor  $\sim 1.3$  (for photons) and  $\sim 1.8$  (for neutral hadrons)

## Uncertainties in jet-level: $\theta$ & $\phi$



Jet angular uncertainties need scaling factor  $\sim 1.6$

## Neutrino correction hypothesis

- ▶ Assign semi-leptonic decays to jets
- ▶ Add neutrino momentum to 4-momentum of assigned jet:  
Test three hypothesis for neutrino energy in each semi-leptonic decay:  $E_\nu^+$ ,  $E_\nu^-$ , 0  
 $3^{nSLD}$  combination of  $E_\nu$ 's for adding to jet 4-momentum:

Number of semileptonic decays in a jet:  $nSLD = nSLDB + nSLDC$

Example:

If an event contains two jets: jet-1 contains 2 semi-leptonic decays and jet-2 contains 1 semi-leptonic decay,  $27(=3^2 \times 3^1)$  combinations of  $E_\nu$ 's are available for neutrino correction in the event:

▶ jet-1:

comb.	1	2	3	4	5	6	7	8	9
$\vec{p}_{\nu,1}$	-	+	0	-	+	0	-	+	0
$\vec{p}_{\nu,2}$	-	-	-	+	+	+	0	0	0

▶ jet-2:

comb.	1	2	3
$\vec{p}_{\nu,3}$	-	+	0

$\vec{p}_{\nu,1} + \vec{p}_{\nu,2}$  is added to 4-momentum of jet-1 and  $\vec{p}_{\nu,3}$  is added to 4-momentum of jet-2.

$\vec{p}_{\nu,1} + \vec{p}_{\nu,2} + \vec{p}_{\nu,3} = 0$  allows fitter to neglect neutrino correction

Combination with highest fit probability is chosen as best neutrino correction.



# Simple neutrino correction for Higgs mass reconstruction

- ▶ Neutrino energy correction:

Estimating neutrino energy as a fraction of corresponding lepton energy:

$$E_{jet}^{corr} = E_{jet} + E_{\nu} = E_{jet} + \left(\frac{1}{x} - 1\right)E_{lep}$$

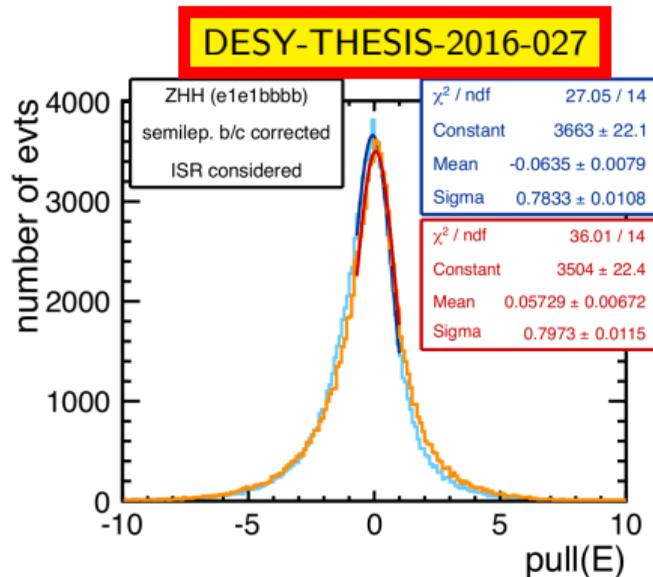
- ▶ Uncertainty on jet energy parametrised as:

$$\sigma_{E_{jet}}^{corr} = \frac{100\%}{\sqrt{E_{jet}}} \oplus \sigma_{\nu}$$

$$\sigma_{\nu}^2 = \left(\frac{\sigma_{\langle x \rangle}}{\langle x \rangle^2}\right)^2 E_{lep}^2 + \left(\frac{1}{x} - 1\right)\Delta E_{lep}^2$$

- ▶ Fixed uncertainties on angles:

$$\Delta\theta_{jet} = \Delta\phi_{jet} = 100 \text{ mrad}$$

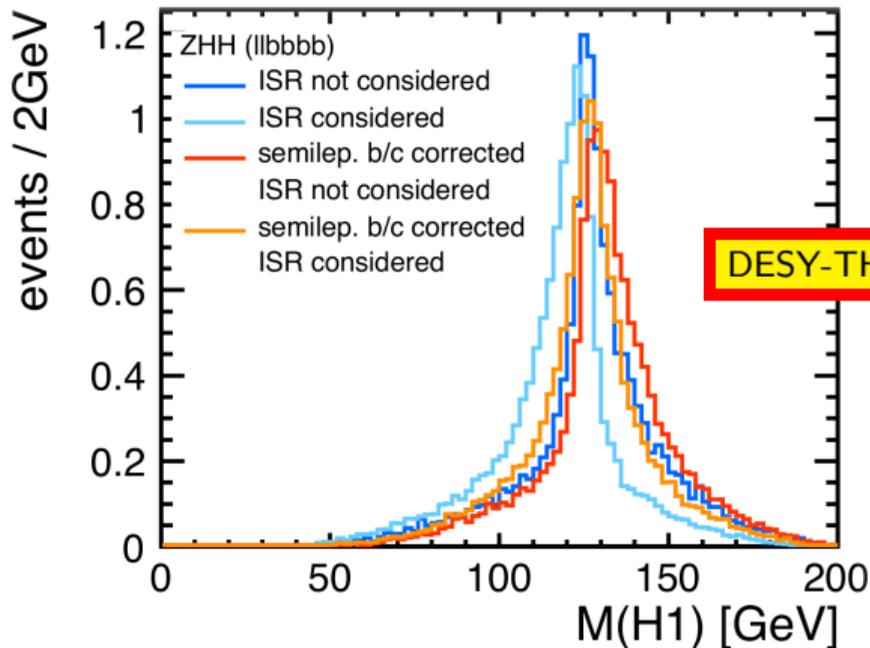


**Blue:** before neutrino energy correction

**Orange:** After neutrino energy correction

Simple correction to jet energy improves jet energy pull distribution as a measure of fit performance.

## Simple neutrino correction for Higgs mass reconstruction



- Bias and asymmetry in  $m_H$  is removed by correcting jet energy and adding ISR

## Error flow and application in kinematic fit

Jet specific energy resolution for  $e^+e^- \rightarrow ZH \rightarrow q\bar{q}b\bar{b}$  process at  $\sqrt{s} = 350$  GeV

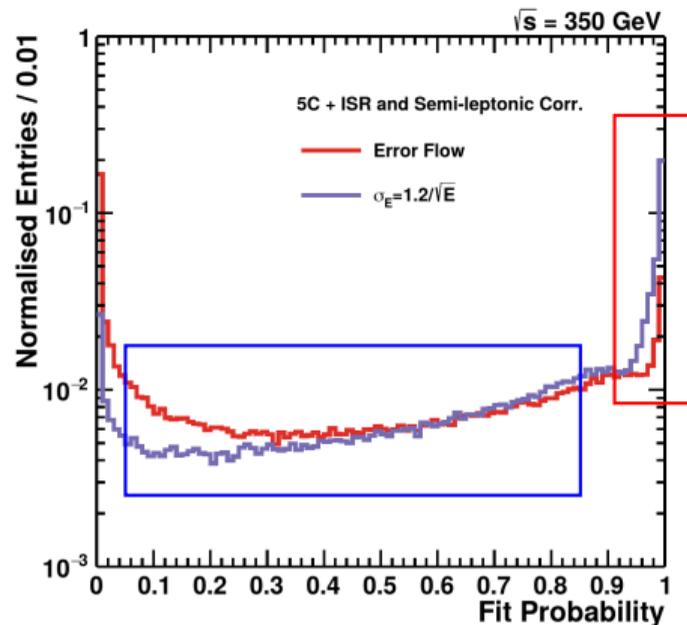
DESY-THESIS-2017-045

- ▶ Full  $4 \times 4$  CovMatrix on 4-momentum of jets  $\sigma(\vec{p}, E)$ :
  - ▶  $\sigma_{Det}$ : computed using subdetector momentum/energy resolution
  - ▶  $\sigma_{Conf}$ : computed using jet energy and particle content (charged, neutral and photon)
  - ▶  $\sigma_\nu = 0.73 \cdot E_l$
  - ▶  $\sigma_{Had}, \sigma_{Clus}$  are not accounted for error flow procedure yet.
- ▶ **Fixed (and wide) angular resolution:**  $\sigma_\theta = \sigma_\phi = 100$  mrad

Kinematic fit: vary jet quantities  $(E, \theta, \phi)$  within uncertainties  $(\sigma_E, \sigma_\theta, \sigma_\phi)$

Improved fit probability by applying Error Flow on jet energy

⇒ Further improvements by error parametrization and handling sl-decays

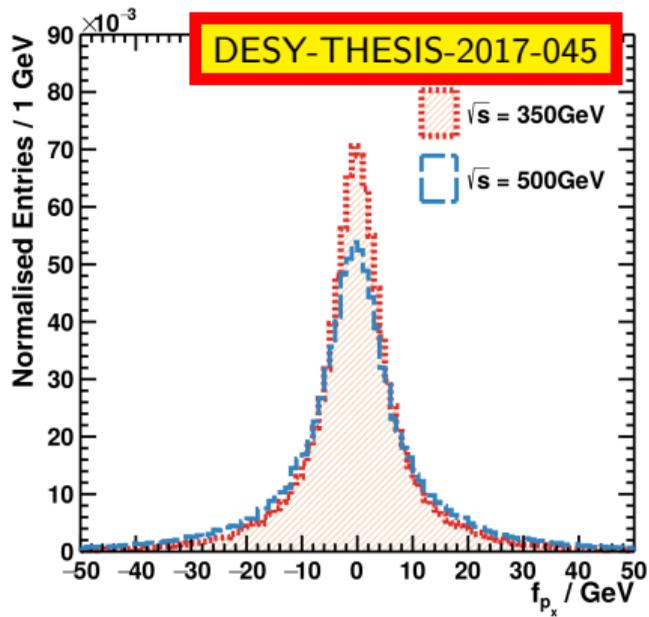


## fit constraints

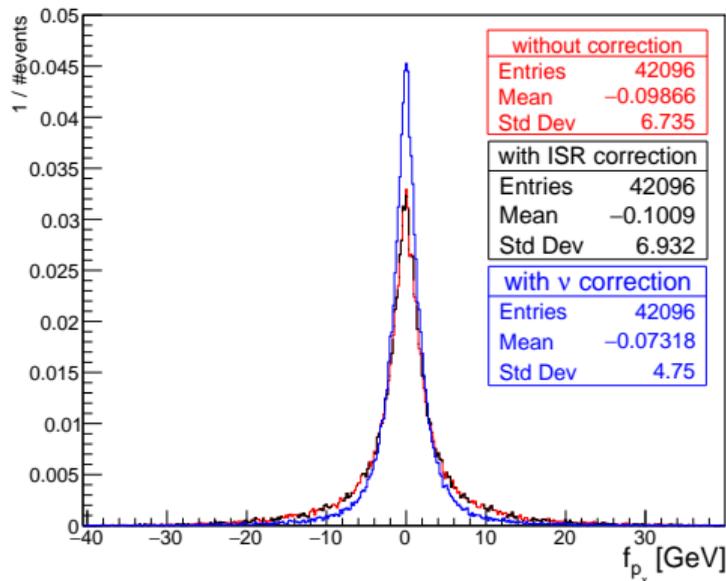
momentum conservation:  $p_x$

ISR is initialized to satisfy momentum conservation on  $x$  direction

- by error flow on jet energy



- by error flow on CovMatrix (new)



angular resolution for individual jets: improved constraint on momentum conservation

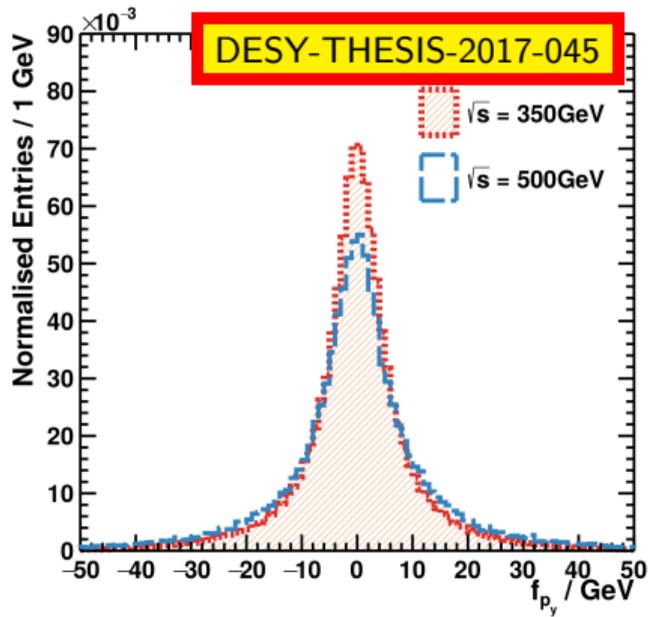
Kinematic fitting for ParticleFlow Detectors at Future Higgs Factories | Yasser Radkhorrani | November 24, 2021 |

## fit constraints

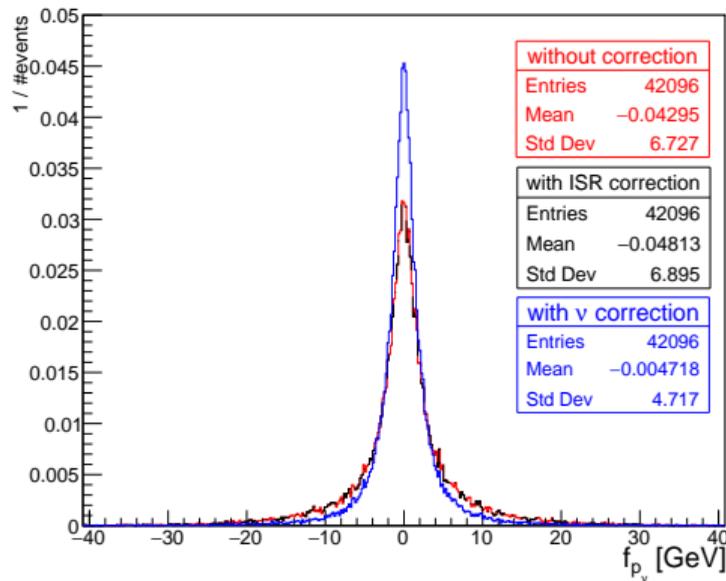
momentum conservation:  $p_y$

ISR is initialized to satisfy momentum conservation on  $z$  direction

- by error flow on jet energy



- by error flow on CovMatrix (new)



angular resolution for individual jets: improved constraint on momentum conservation

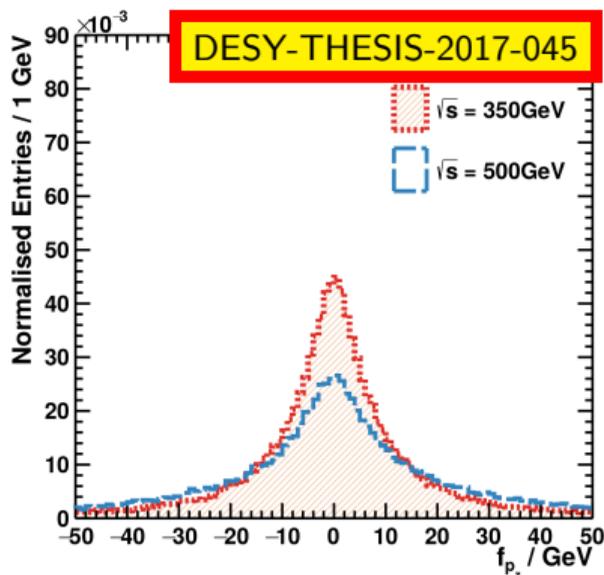
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## Fit constraints

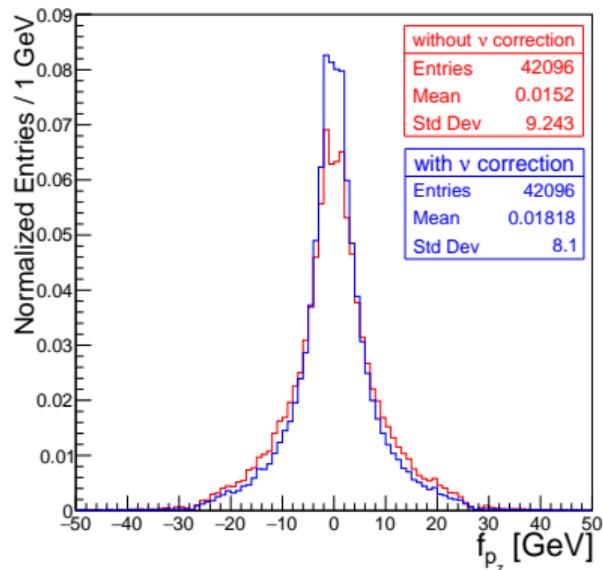
Momentum conservation:  $p_z$

Adding 4-momentum of neutrino improves jet fit object initialization

► DBD 350/500 GeV samples



► MC-2020 250 GeV prod. samples



Proper neutrino correction for jets: improved constraint on momentum

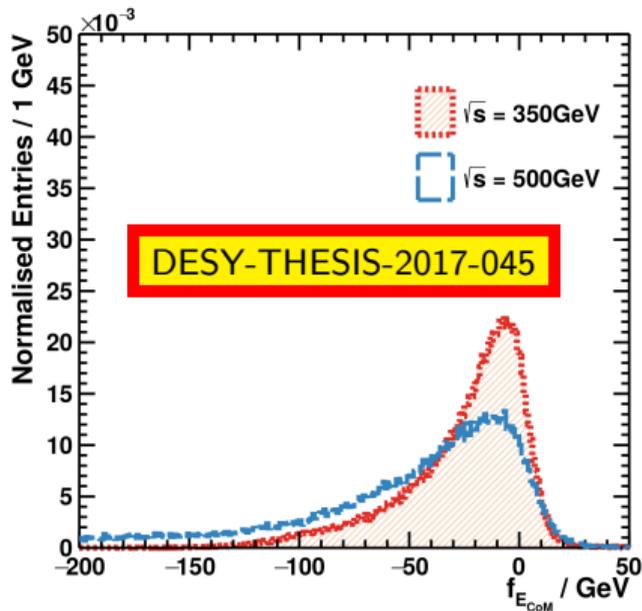


## fit constraints

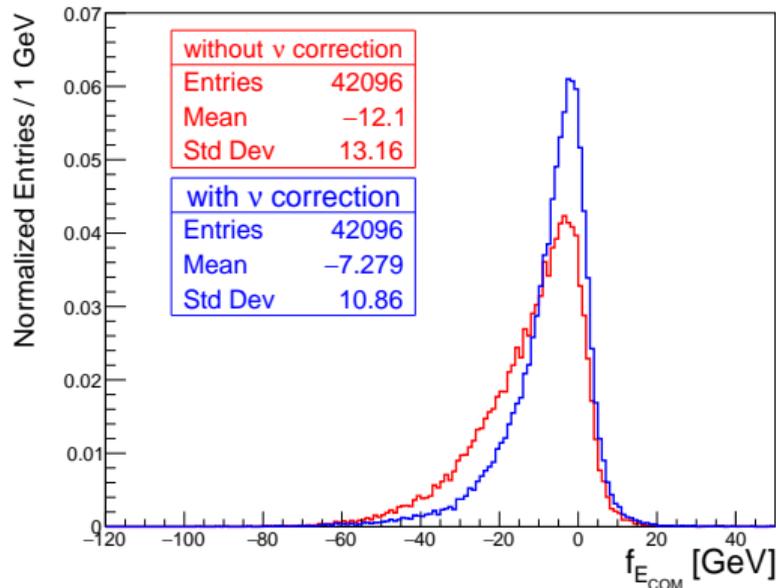
energy conservation:  $E$

Neutrino correction (best pre-fit  $\vec{p}_\nu$  for succesful fits) improves start values  $\Rightarrow$  better fit object initialization

- DBD 350/500 GeV samples



- MC-2020 250 GeV prod. samples



By neutrino correction, initial value of constraint function closer to target  $\Rightarrow$  fit should work better!