





SLOW AND SAFE GRAVITINOS

Based on :

E.D., M.A.G.Garcia, Y.Mambrini, K.A.Olive, M.Peloso and S.Verner, Phys. Rev. **D103** (2021), 123519 [arXiv:2104.03749 [hep-th]]



Valery Rubakov symposium nov. 8, 2021 DESY-TH

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Outline

1) The swampland program

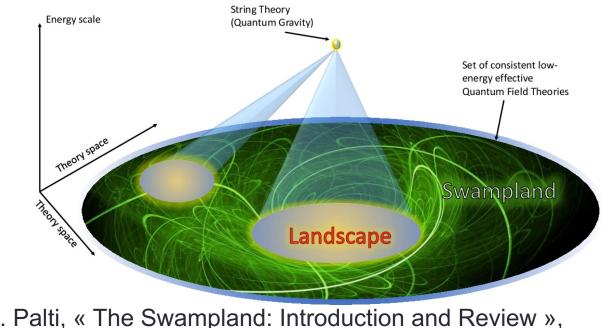
- Spin 3/2, potential problems
- 2) Gravitino sound speed in supergravity
- 3) Complete eqs. for the longitudinal gravitino
- 4) Results, gravitino swampland conjecture5) Conclusions

(Instant) The swampland program



Are all consistent Quantum Field Theories obtainable from a Quantum Gravity Theory (ex. String Theory) ? Probably NO

Swampland = the set of consistent QFT with no consistent coupling to Quantum Gravity (Vafa,2005)



(taken from E. Palti, « The Swampland: Introduction and Review », [arXiv:1903.06239 [hep-th]]) E. Dudas – CNRS and E. Polytechnique



There are various, related or unrelated swampland conjectures: (Vafa+Ooguri ...see review E.Palti)



 de Sitter: impossibility of constructing a vacuum with positive cosmological constant

- KKLT-type constructions are in the swampland ?
- quintessence-like dark energy models are then the only viable possibility ?
- Weak Gravity Conjecture (WGC)
 Gravity is the weakest force
- The distance conjecture: not possible to have super-Planckian field excursions



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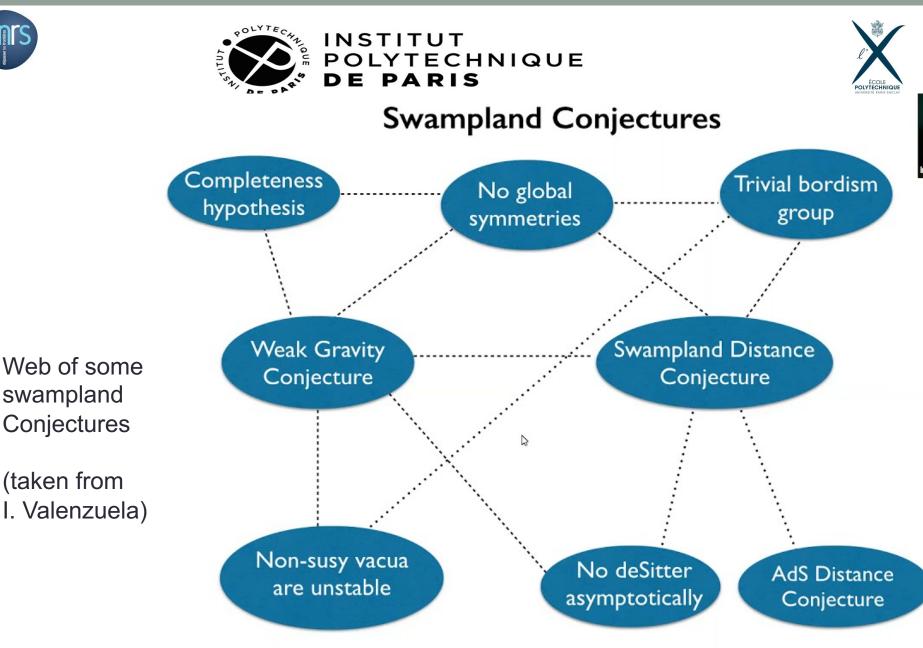


- Anti-de Sitter phobia: non-supersymmetric AdS vacua cannot be stable
- Scalar weak gravity conjecture, finite number of tunings in EFT, festina lente bound,...

Final goal swampland program ?

Supplement rules of effective QFT with additional constraints, which would guide Beyond the Standard Model and cosmology constructions.





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On the other hand, the consistency of low-energy actions for the spin 3/2 Rarita-Schwinger field has a long history :

- 1941: Rarita-Schwinger action
- 1969: Velo-Zwanziger pointed out potential acausal propagation for a charged gravitino in an em background
- 1977: Deser-Zumino proved that gravitino propagation in minimal supergravity is causal
- 2001: Deser-Waldron proved that gravitino propagation in gauged supergravities is causal
- 2021 Gravitino swampland conjecture, gravitino distance conjecture







History of the subject strongly suggest that usual supergravities should have no problems with gravitino propagation.

Recently, simple nonlinear SUSY/SUGRA models were constructed. More minimal inflationary models, fewer fields.

Even possible to construct models with only:

- graviton
- massive gravitino
- inflaton (real scalar)





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Example constrained superfields

 Volkov-Akulov action can be constructed in superspace (Rocek,78) introducing a constrained, nilpotent superfield

 $X^2 = 0$

whose solution is no fundamental scalar

$$X = \frac{GG}{2F_X} + \sqrt{2}\theta G + \theta^2 F_X$$

The full VA action is

$$\mathcal{L}_{VA} = \left[X \overline{X} \right]_{D} + \left[fX + h.c. \right]_{F}$$

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Analogy with the sigma model :

- O(N) linear sigma model

$$\mathcal{L} = \partial_m \phi_a \partial^m \phi_a - \lambda (\phi_a \phi_a - v^2)^2.$$

has 1 massive (« Higgs ») and N-1 goldstone bosons, versus the

- O(N)/ O(N-1) nonlinear sigma model ($\lambda
ightarrow \infty$ limit)

$$\mathcal{L} = \partial_m \phi_a \partial^m \phi_a$$

+ constraint $\phi_a \phi_a = v^2$, describes self-interactions of the N-1 goldstone's. O(N) symmetry is nonlinearly realized.







My talk deals with the propagation (« speed of sound » C_S) of gravitino in supergravity, in an inflationary setup.

Usually
$$0 < c_s \le 1$$

Recently, two potential problematic behaviours were discussed:

- $c_s = 0$ at particular points on the inflationary trajectory
 - Large (catastrophic) production of gravitinos
- $c_s > 1$ acausal behaviour at particular points on the inflationary trajectory







2) Gravitino sound speed in supergravity

Supergravity = Supersymmetry + Gravity

It contains :

- gravity multiplet: Gravito

Graviton
$$g_{\mu
u}$$
 , gravitino ψ_{μ} ,

- « matter » fields: (complex) Scalars
 chiral superfields

 ϕ_{i}

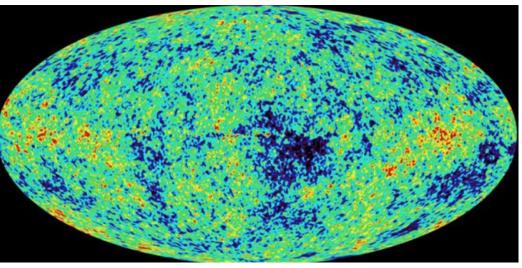
, Weyl Fermions







Why Supergravity for early cosmology?



- Inflation with super-Planckian field variations needs an UV completion String Theory
- Supersymmetry crucial ingredient in String Theory, supergravity its low-energy effective action





- In supergravity, the gravitino Ψ_{μ} becomes massive by absorbing the goldstino \mbox{G}

$$\begin{split} \Psi_{\mu} \begin{pmatrix} 3/2 \\ - \\ - \\ -3/2 \end{pmatrix} + G \begin{pmatrix} - \\ 1/2 \\ -1/2 \\ - \end{pmatrix} = \Psi_{\mu} \begin{pmatrix} 3/2 \\ 1/2 \\ -1/2 \\ -3/2 \end{pmatrix} \\ \text{and its mass is} \qquad m_{3/2} = e^{\frac{K}{2}} |W| \end{split}$$





The sound speed C_s is defined from the dispersion relation

$$\omega^2 = c_s^2 \mathbf{k}^2 + a^2 m^2$$

The transverse spin 3/2 component in a FRW background has a standard dispersion relation with $c_s=1$

$$(\gamma^0 \partial_0 + i \gamma^i k_i + a m_{3/2}) \Psi_{3/2,\mathbf{k}} = 0$$
 scale factor

Reminder: Supergravity solves potential pathological behaviour of Rarita-Schwinger spin 3/2 fields pointed out by Velo-Zwanziger in 1969.







The longitudinal (goldstino) component satisfies a more involved equation

$$(\gamma^0 \partial_0 - i\gamma^i k_i \frac{\alpha_1 + \gamma^0 \alpha_2}{\alpha} + am_{3/2})\Psi_{1/2,\mathbf{k}} = 0$$

with α_1,α_2,α specific functions of scalar fields in SUGRA, with the sound speed depending generically on time

$$c_s^2 = \frac{|\alpha_1|^2 + |\alpha_2|^2}{\alpha^2}$$

 $c_s < 1 \implies \text{Slow gravitino} \quad \text{(Benakli, Darmé, Oz, 2014)}$







A general expression for longitudinal gravitino speed sound is

$$c_s^2 = \frac{\left(p - 3m_{3/2}^2\right)^2}{\left(\rho + 3m_{3/2}^2\right)^2} + \frac{4\dot{m}_{3/2}^2}{\left(\rho + 3m_{3/2}^2\right)^2} + \frac{4\dot{m}_{3/2}^2}{\left(\rho + 3m_{3/2}^2\right)^2}$$
energy density

 $c_s=0$ is possible if $m_{3/2}$ is const. and $p=3m_{3/2}^2$

In this case, there would be a catastrophic production of gravitinos during inflation

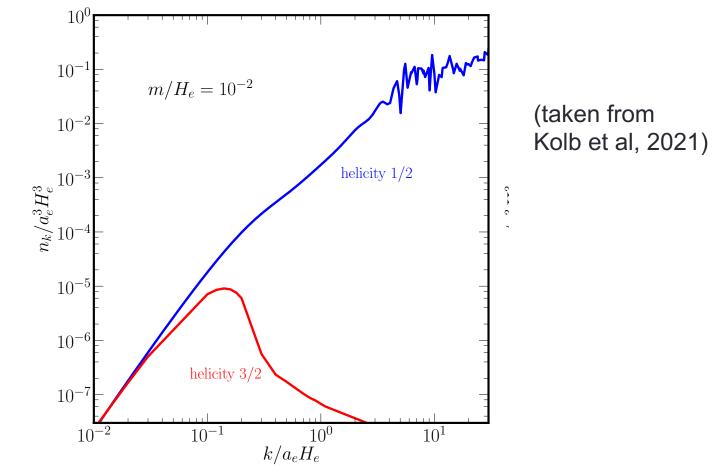
(Hasegawa et al, 2017; Kolb, Long, McDonough, 2021).







The problem was argued to arise for $m_{3/2} < H$. If the problem is generic \longrightarrow potential issue for low-energy SUSY models.



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The explicit formula in SUGRA is

$$c_s^2 = 1 - \frac{4}{\left(|\dot{\varphi}|^2 + |F|^2\right)^2} \left\{ |\dot{\varphi}|^2 |F|^2 - |\dot{\varphi} \cdot F^*|^2 \right\}$$

where $F^i \equiv e^{K/2} K^{ij^*} D_{j^*} W^*$ in <u>standard</u> SUGRA ,

$$D_i W \equiv \frac{\partial W}{\partial \varphi^i} + \frac{\partial K}{\partial \varphi^i} W$$

and we used the compact notation $|\dot{arphi}|^2=\dot{arphi}^i\,K_{ij^*}\,\dot{arphi}^{j*}$,etc

Obs: Cauchy-Schwarz inequality \implies causality $c_s \leq 1$ respected in all standard SUGRA's







3) Complete eqs. for the longitudinal gravitino

In an expanding background, the longitudinal gravitino $\,\theta\,$ is coupled to another fermion, the inflatino

$$\Upsilon = K_{ij^*} \left(\chi^i \partial_0 \varphi^{j^*} + \chi^{j^*} \partial_0 \varphi^i \right)$$

(Kallosh,Kofman,Linde, Van Proeyen,2000; Nilles,Peloso,Sorbo, 2001)

heta and Υ are coupled via

$$\left(\gamma^0 \partial_0 + i\gamma^i k_i N + M\right) X = 0 \quad , \quad X = \left(\begin{array}{c} \tilde{\theta} \\ \tilde{\Upsilon} \end{array}\right)$$







where the « sound speed matrix »

$$N = \begin{pmatrix} -\frac{\alpha_1}{\alpha} - \gamma^0 \frac{\alpha_2}{\alpha} & -\gamma^0 \Delta \\ -\gamma^0 \Delta & -\frac{\alpha_1}{\alpha} + \gamma^0 \frac{\alpha_2}{\alpha} \end{pmatrix}$$

with $\Delta = \sqrt{1 - c_s^2}$, is now the key to the « slow gravitino » problem.

When
$$c_s=0$$
 , then $N=\left(egin{array}{cc} 0 & -\gamma^0 \ -\gamma^0 & 0 \end{array}
ight)$

is nonsingular, leading to a nonvanishing sound speed for the physical eigenstates.

(DGMOPV,2021; see also Antoniadis,Benakli, Ke, 2021)







4) Results, gravitino swampland conjecture

For the (large) majority of SUGRA models we investigated , we found no problems, $~0 < c_s^i \leq 1 \,$:

- <u>standard</u> SUGRA models with two chiral superfields (inflaton+SUSY breaking): general statement
- SUGRA models with nilpotent SUSY breaking field

$$S^2 = 0$$







$$S(\Phi - \overline{\Phi}) = 0$$

Only $Re \ \phi$ is a dynamical degree of freedom. $Im \ \phi$, the inflatino ψ_{ϕ} and the auxiliary field F_{ϕ} are determined by the constraint.

In particular F_{ϕ} is a bilinear in fermions and does not appear in the scalar potential : $F^{\Phi} \neq e^{K/2} K^{\Phi \overline{i}} D_{i^*} W^*$







Consequences:

- There is no inflatino $\implies \Upsilon=0$, the gravitino sound speed problem can reappear (model-dependent)
- The Cauchy-Schwarz argument for $c_s \leq 1$ not valid. We found examples with $c_s > 1$!
- On the other hand, the UV origin of the orthogonal constraint is not clear (dall'Agata, E.D., Farakos, 2006)
 - Potential pathological behaviour reminiscent of the swampland program !







Interesting to contemplate a « gravitino swampland conjecture »

« In all 4d effective field theories that are low-energy limits of quantum gravity, at all points in moduli space and for all initial conditions, the sound speed of the gravitino(s) must be non-vanishing $c_s > 0$ » (Kolb,Long,McDonough)

refined version

« In all 4d effective field theories that are low- energy limits of quantum gravity, at all points in moduli space and for all initial conditions, all eigenvalues of the sound speed matrix for fermions must be non-vanishing and subluminal $0 < c_s^i \leq 1$ »







- Gravitino production constraints important for viability of SUGRA models.
- Very often, the inflatino is produced, alleviating the gravitino problem.
- Important to check and impose sound speed $0 < c_s \le 1 \implies \text{gravitino swampland conjecture}$
- We found that most SUGRA models do satisfy it, except peculiar models with orthogonal constraint. Interesting to test inflation against other swampland conjectures.







Congratulations for the Hamburg prize, Valery !

Thank you for sharing your insights and time during your visits in Paris !





