TRACK RECONSTRUCTION WITH QUANTUM COMPUTERS AT LUXE

Annabel Kropf¹, Beate Heinemann^{1,2}, Cenk Tüysüz^{1,3}, David Spataro¹, Federico Meloni¹, Karl Jansen¹, Lena Funcke⁴, Stefan Kühn⁵, Tobias Hartung^{6,5}, **Yee Chinn Yap**¹

¹Deutsches Elektronen-Synchrotron DESY ²Albert-Ludwigs-Universität Freiburg ³Humboldt-Universität zu Berlin ⁴Perimeter Institute for Theoretical Physics ⁵CaSToRC, The Cyprus Institute ⁶University of Bath

ACAT 2021, 30th November 2021, Virtual and Daejeon, South Korea





LUXE EXPERIMENT

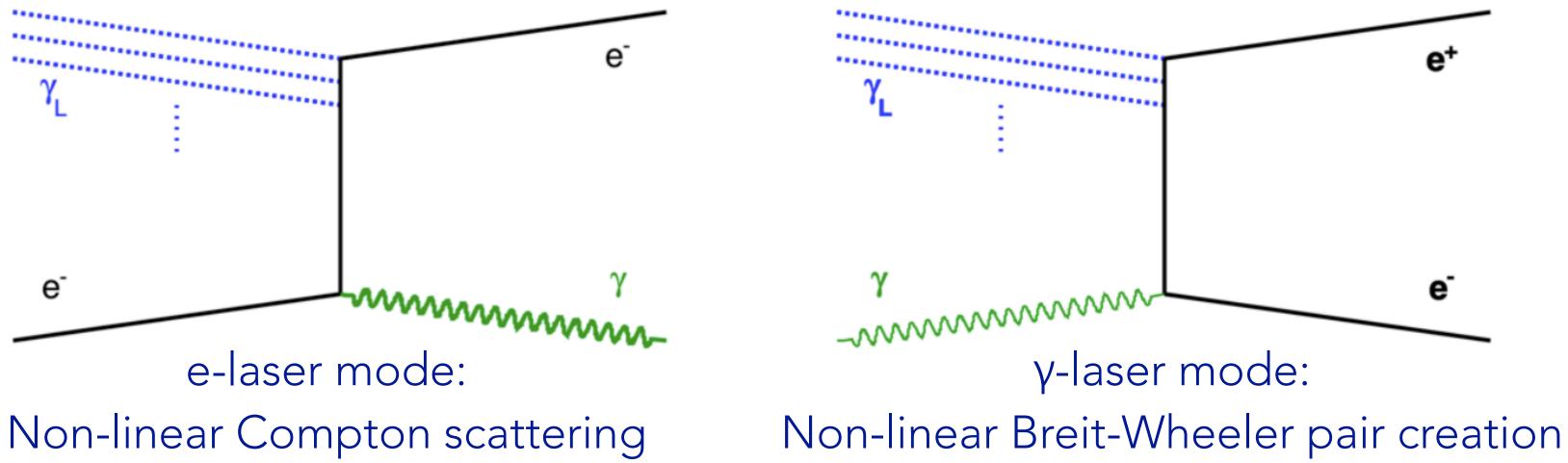
- Use European XFEL electron beam and high-power laser.
- CDR: <u>arXiv:2102.02032</u>, website: <u>https://luxe.desy.de/</u>

/----/ /----/ -----**Field intensity parameter** $\xi = \sqrt{4\pi\alpha}$ e

Yee Chinn Yap

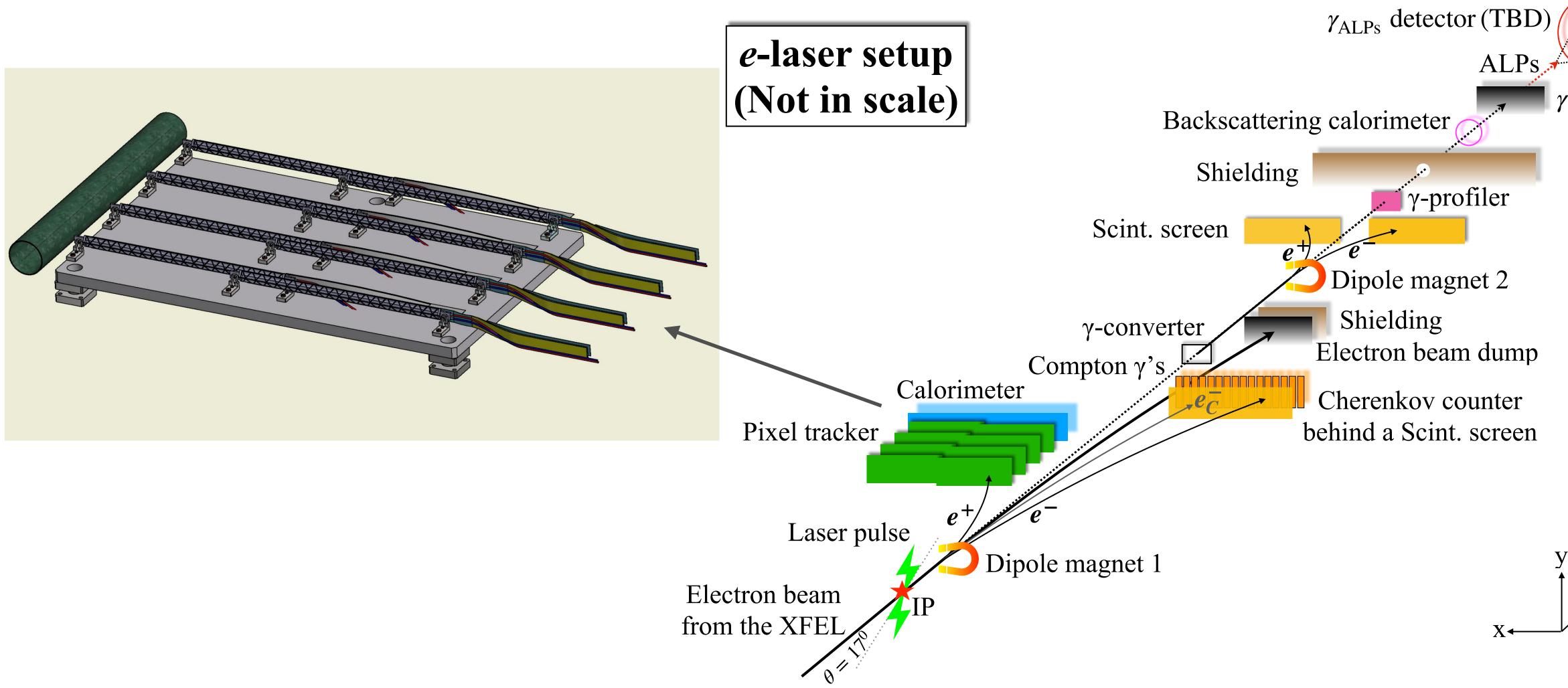


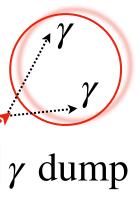
• LUXE (Laser Und XFEL Experiment) is a proposed experiment at DESY aiming to study QED in the strong-field regime where it becomes non-perturbative.





LUXE EXPERIMENT SETUP



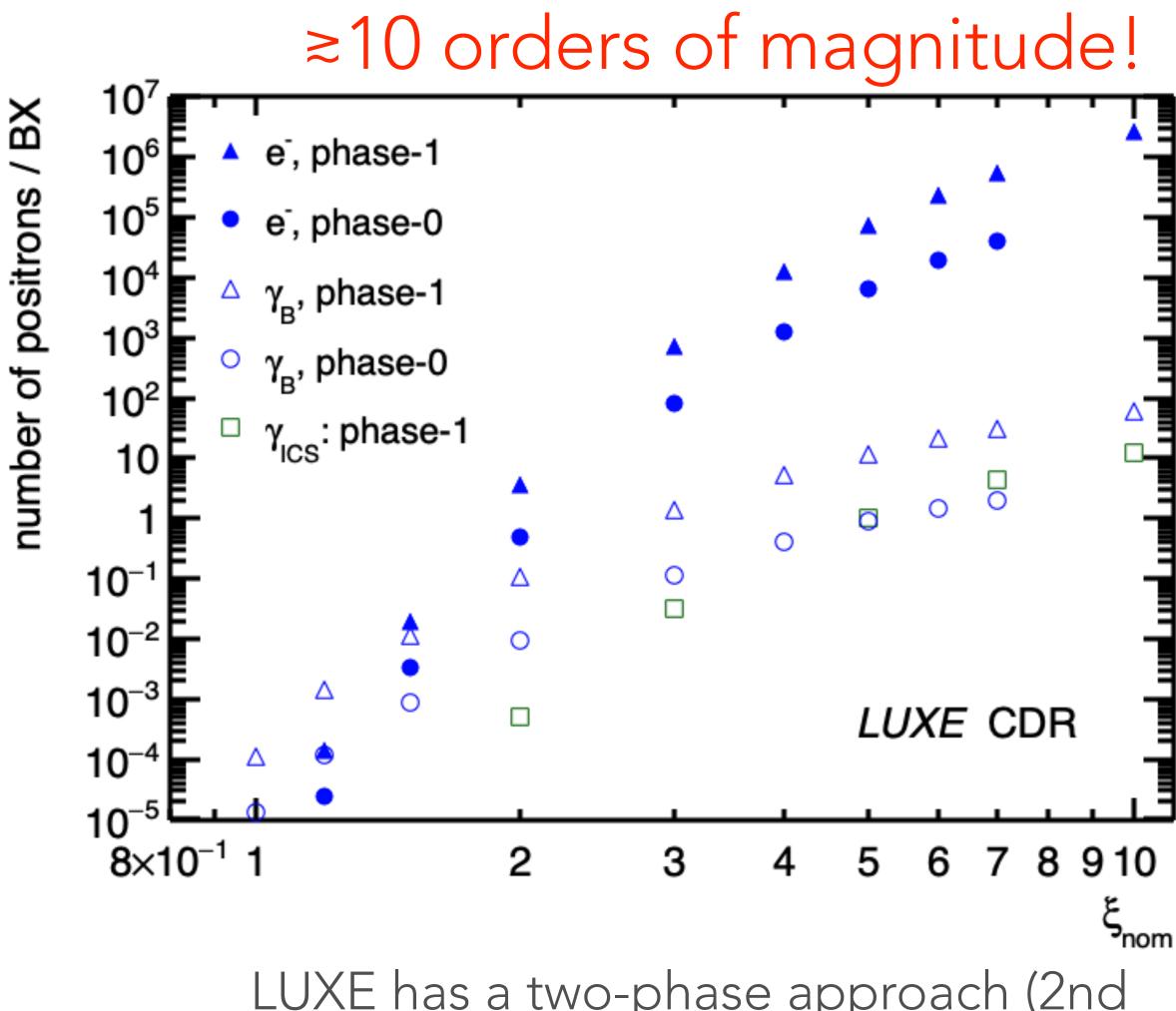






TRACKING CHALLENGE

- One of the main measurements at LUXE is the positron flux vs ξ.
- Two challenges:
 - Good linearity up to a multiplicity of $O(10^6)$.
 - Background rate needs to be below 10-³/BX at low ξ.
- Study the use of quantum computing.

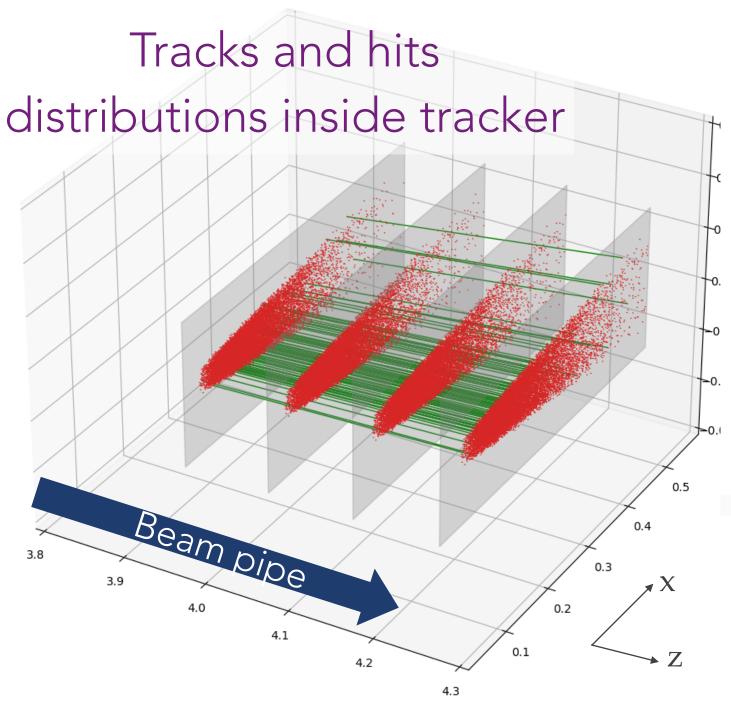


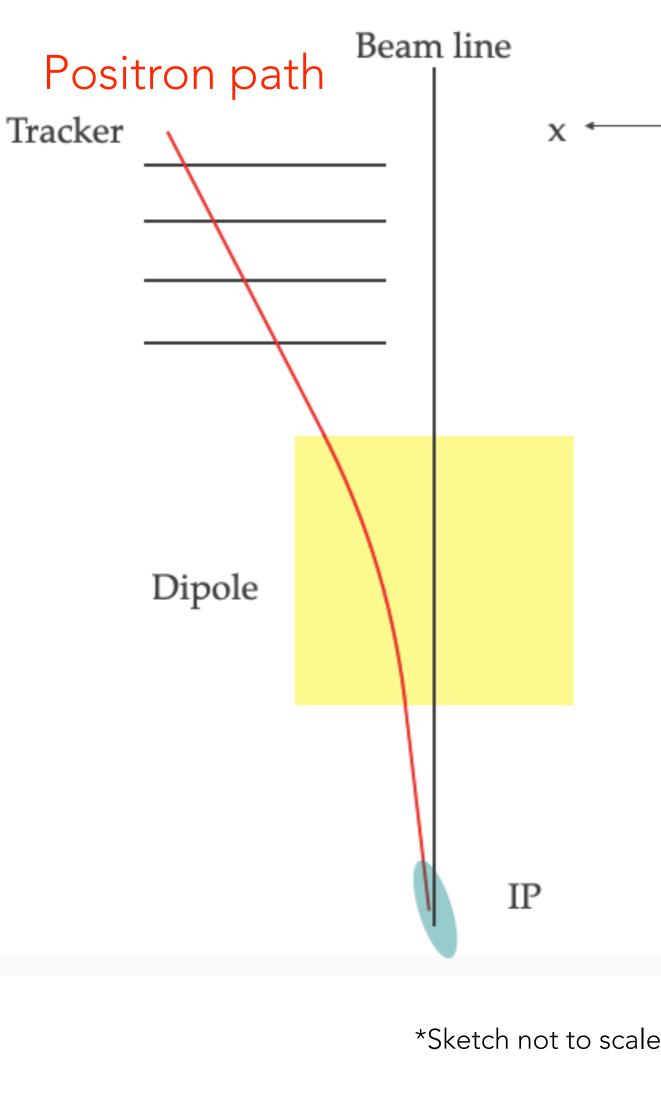
LUXE has a two-phase approach (2nd phase with an upgraded laser).

SIMULATION

- Signal interactions at the IP are generated with a custom MC (T. G. Blackburn, A. J. MacLeod, B. King, <u>arXiv:2103.06673</u>).
- The resulting positrons are propagated through the dipole magnet and tracking detector using a simplified simulation.
- For simplicity, consider four detection layers without gap/overlap.
- Ability to turn on/off the detector resolution effect, parametric multiple scattering, etc.

3.8







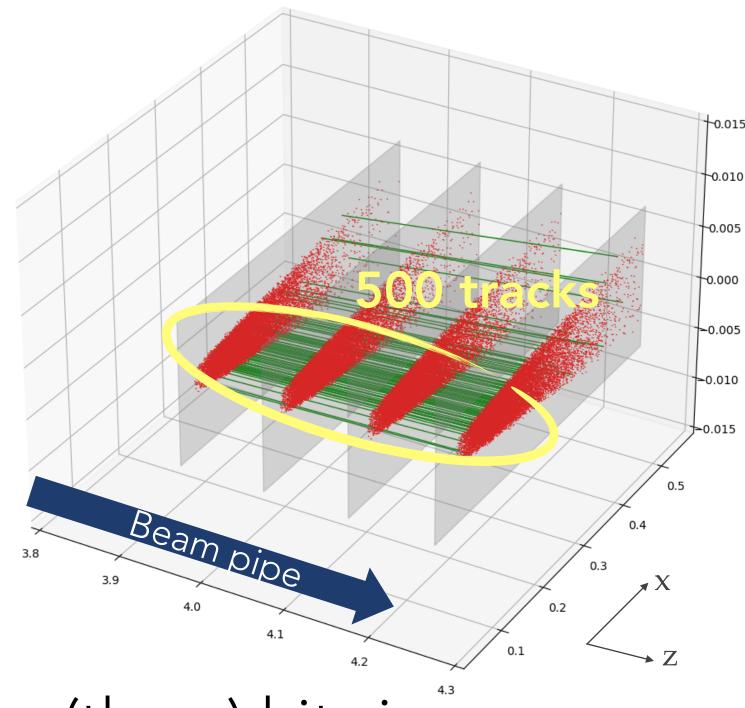




TRACKING PROBLEM

- ranges from 800 to 500,000.
- Limit to the **500 tracks** closest to the beam line (typically densest region) such that the size of the problem is constant.
 - But the complexity increases due to increasing track density with ξ.
- Starting point: doublets (triplets) which is a set of two (three) hits in consecutive layers.

• Study $\xi=3, 4, 5$ and 7 in the e-laser phase-1 scenario. Number of positrons

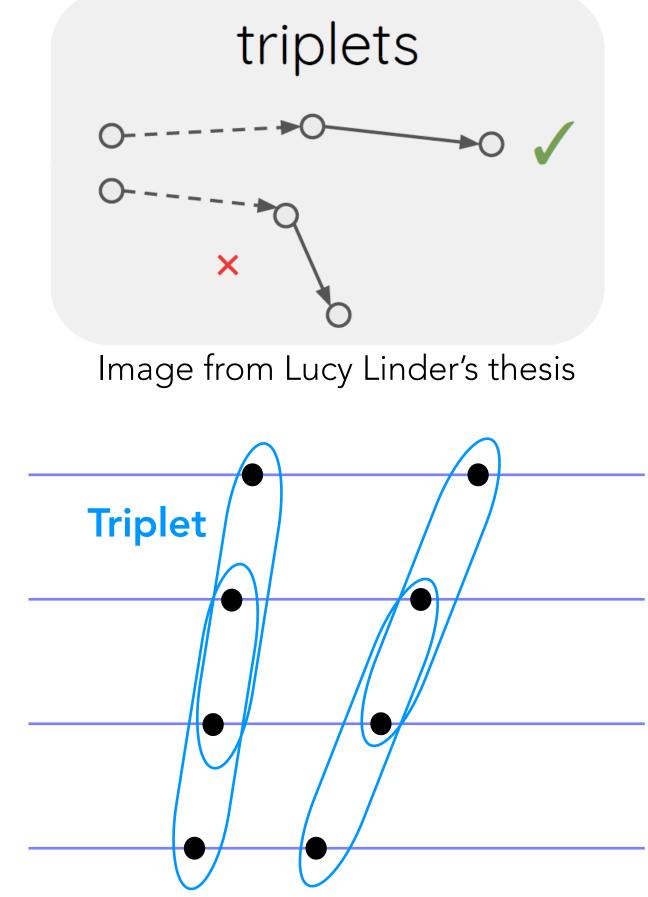




PRE-SELECTION

- combinatorial candidates at ~100 % efficiency.
- Triplets are formed starting from doublets.
- Pre-selection based on the expected angles from geometry (doublet level) and the straightness of the triplet candidates.
- Triplets are formed from 1st to 3rd layer, and 2nd to 4th layer.

• Pre-selection is applied on the initial doublet/triplet candidates to reduce the



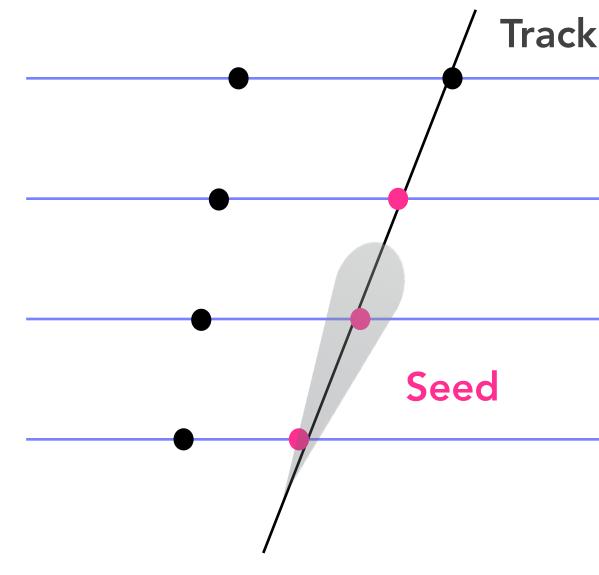
CLASSICAL BENCHMARK

- As benchmark, we use an ACTS*-based tracking with combinatorial Kalman Filter (CKF) technique for the track finding and fitting.
 - Seeding using the first three layers, similar to the triplet pre-selection.
 - Initial estimate of track parameters from seed is used to predict next hit and updated progressively, with the measurement search performed at the same time as the fit.
- Ambiguity solving applied to remove tracks with shared hits from the initial track collection.

*ACTS: A Common Tracking Software <u>https://acts.readthedocs.io</u>





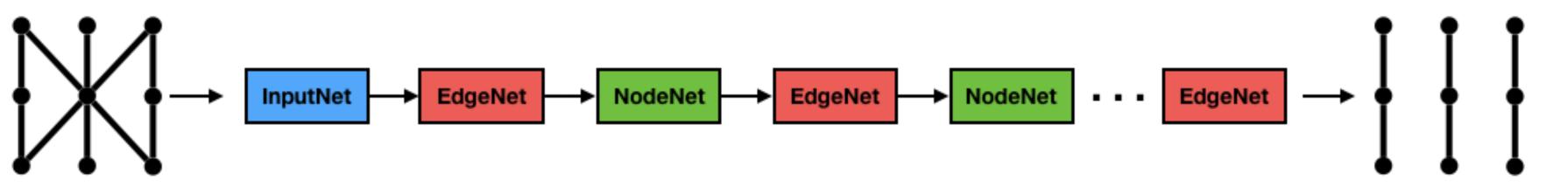


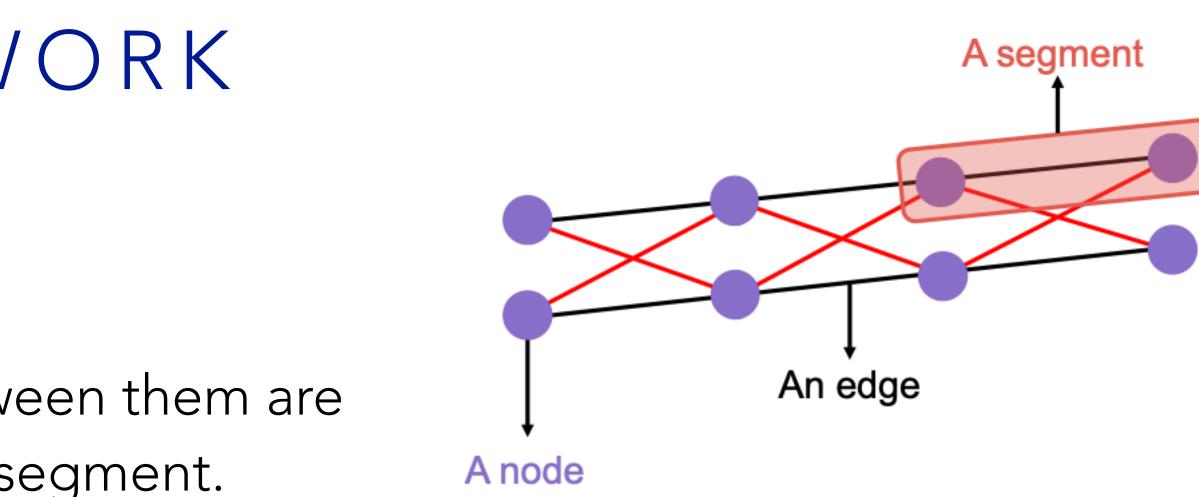




GRAPH NEURAL NETWORK

- Graph constructed from doublets.
- Hits are nodes and the connections between them are edges. The doublet structure is called a segment.
- All nodes of consecutive layers are connected, and only the ones that satisfy preselection cuts are kept.





Developed in HEP.TrkX project (arXiv:1810.06111) and further extended in Exa.TrkX (arXiv:2103.06995). Hybrid quantum-classical version also exists (Q.TrkX, <u>arXiv:2109.12636</u>)





THE QUANTUM APPROACH

- <u>10.1007/s41781-019-0032-5*</u>.

$$O(a, b, T) = \sum_{i=1}^{N} a_i T_i + \sum_{i=1}^{N} \sum_{j < i}^{N} b_{ij} T_i T_j$$
Ouality of triplets Compatibility

between triplet pairs

*Bapst, F., Bhimji, W., Calafiura, P. et al. A Pattern Recognition Algorithm for Quantum Annealers. Comput Softw Big Sci 4, 1 (2020).

Yee Chinn Yap

• The triplets are identified to form tracks by expressing the problem as a quadratic unconstrained binary optimisation (QUBO), problem similar to <u>https://doi.org/</u>

• Minimising the QUBO is equivalent to finding the ground state of the Hamiltonian.

b_{ii} quantify the compatibility between $T_i, T_i \in \{0, 1\}$ triplet pairs. $b_{ii} = 0$, if no shared hit = + 1, if in conflict $= -S(T_i, T_i)$, if two hits are shared







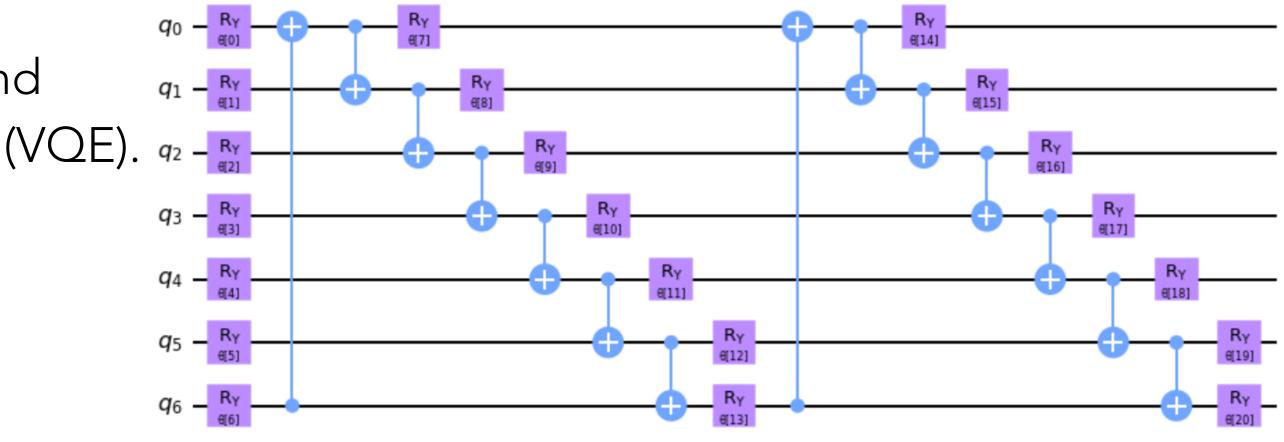


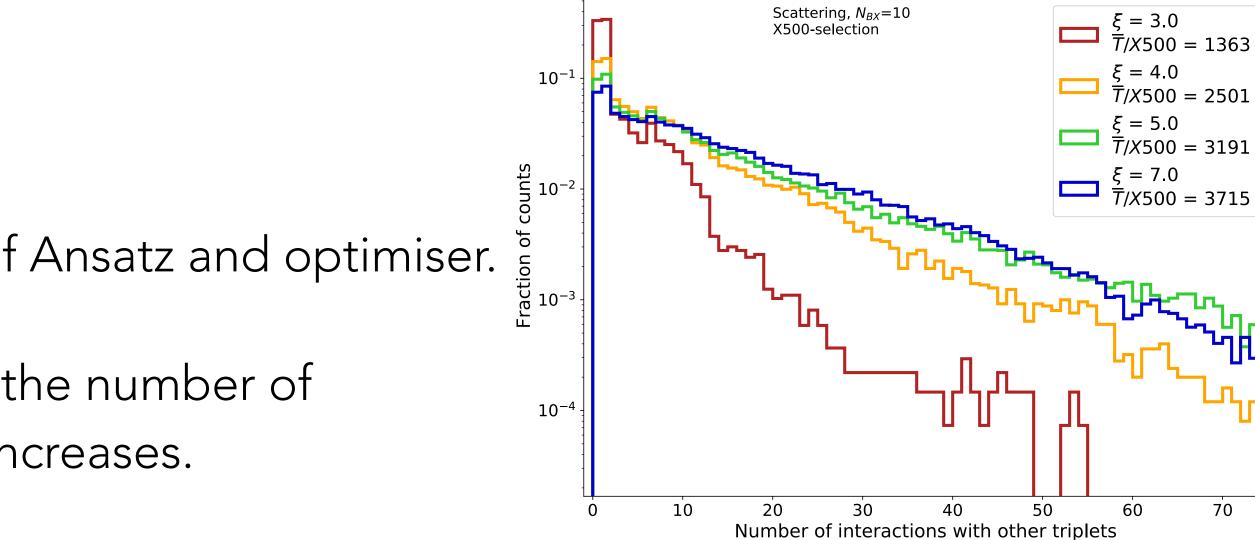
SOLVING QUBO

• QUBO can be mapped to Ising Hamiltonian and solved using Variational Quantum Eigensolver (VQE).

$$\mathcal{H} = -\sum_{n=1}^{N} \sigma_n^x \sigma_{n+1}^x - \alpha \sum_{n=1}^{N} \sigma_n^x$$

- Use Qiskit from IBM.
- Two sets of results:
 - Exact solution using matrix diagonalisation (NumPy Eigensolver) for benchmarking
 - VQE (without QC noise) using one choice of Ansatz and optimiser.
- As ξ increases, the track density increases and the number of interactions of a triplet with other triplets too increases.

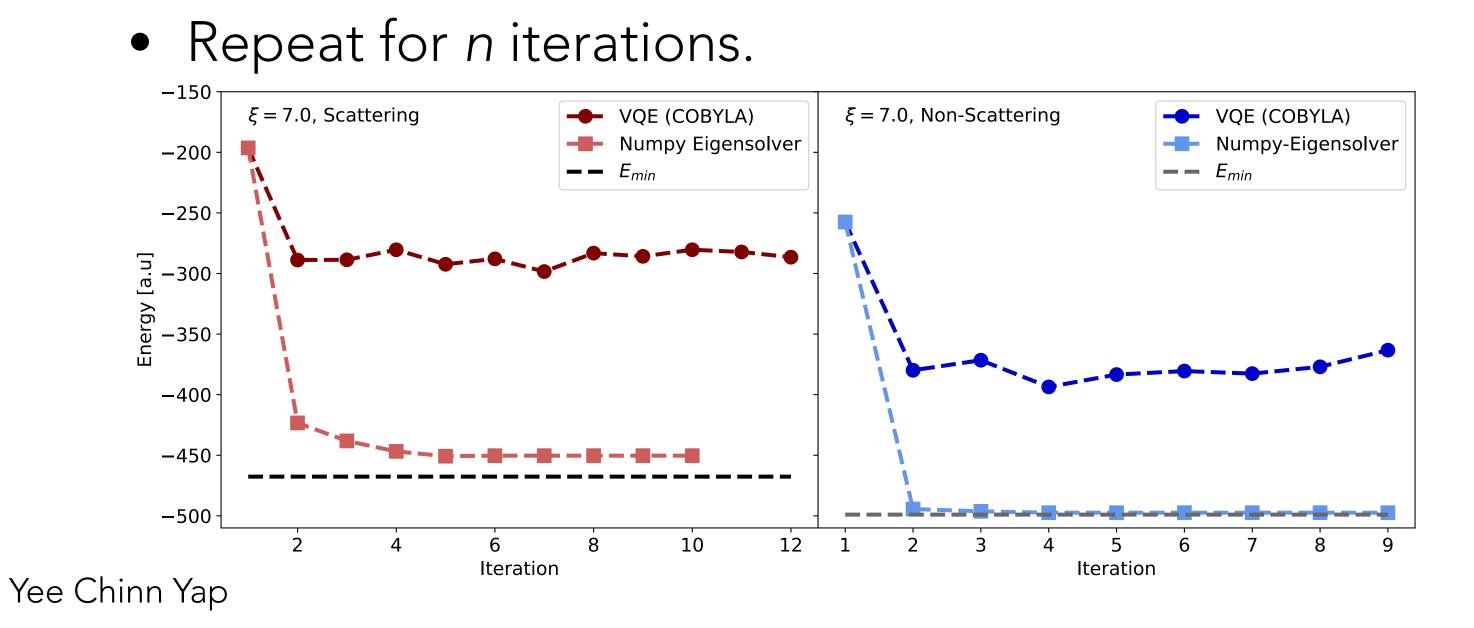




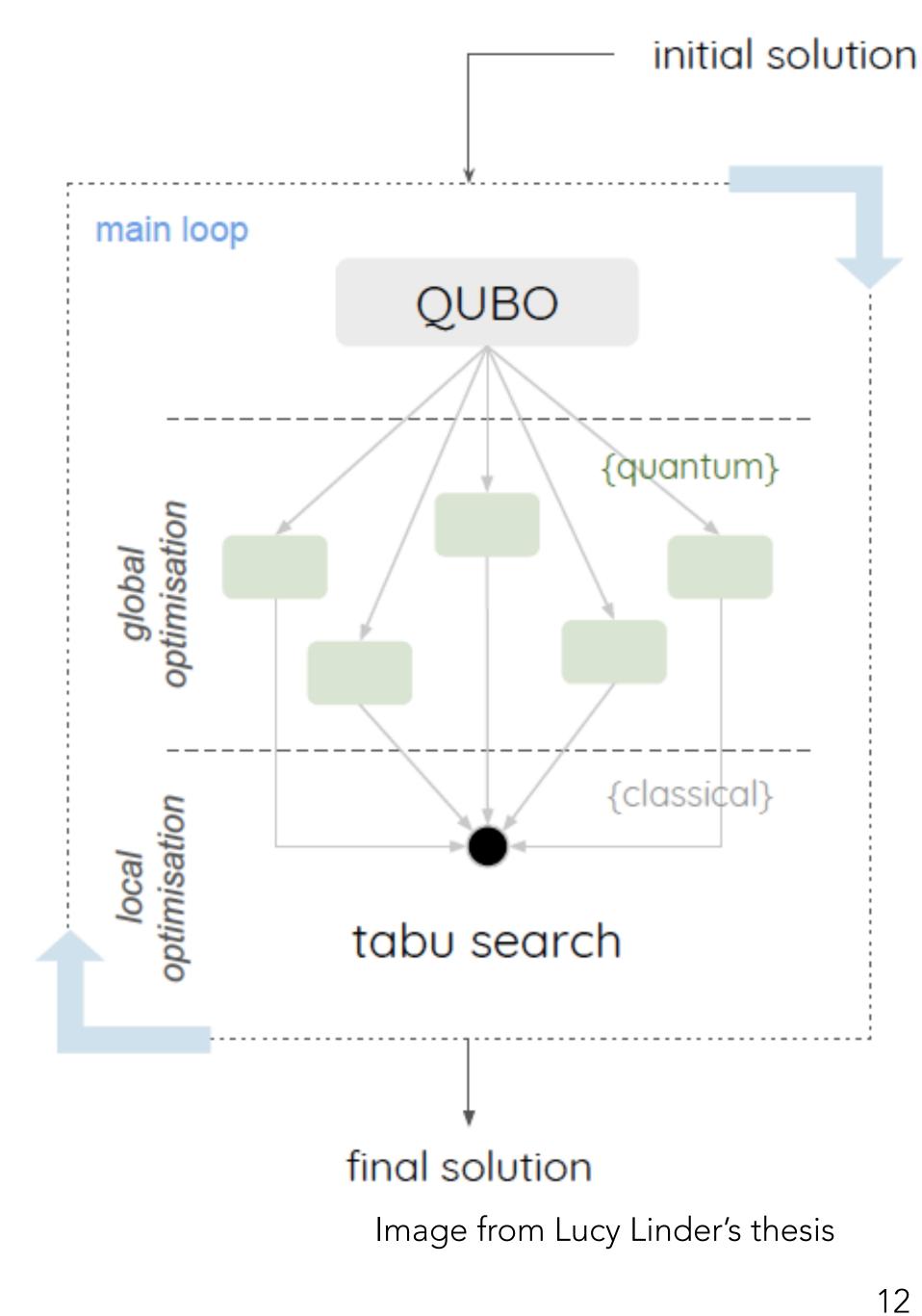


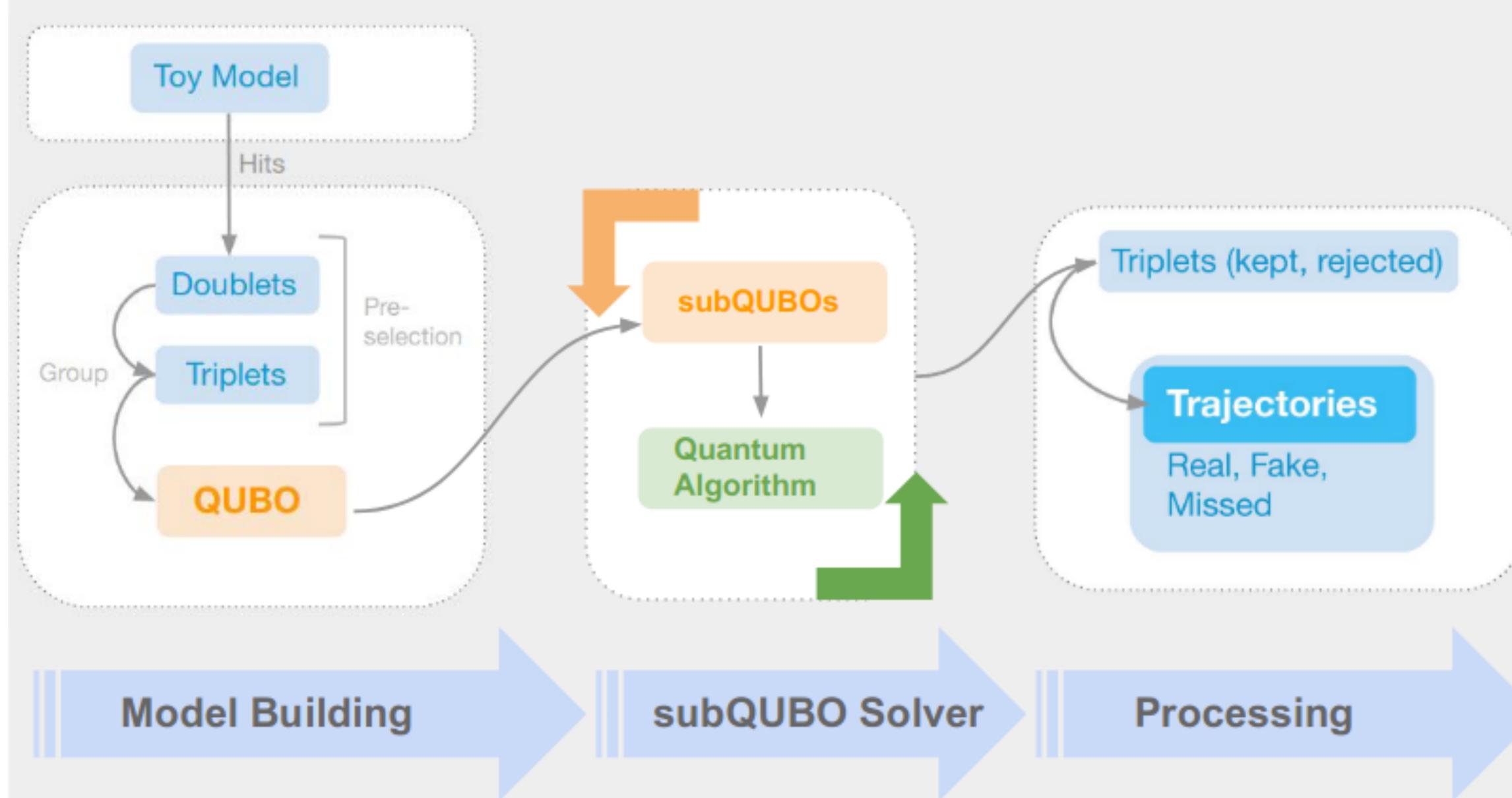
SUB-QUBO

- Need as many qubits as there are triplets.
- Due to the limited number of qubits, the QUBO is split into sub-QUBOs (of size 7) to be solved.
 - After the sub-QUBOs are solved, the results are combined and a tabu search performed.









Yee Chinn Yap



PERFORMANCE

- selected triplet pairs into quadruplets if they share two hits between them.
 - A correct track has **all four hits matched** to the same generated particle.
- Efficiency = $\frac{N_{\text{tracks}}^{\text{matched}}}{N_{\text{tracks}}^{\text{generated}}}$ and Fake races • Performance metrics:
- Noise and real quantum device also tested but at a smaller scale.

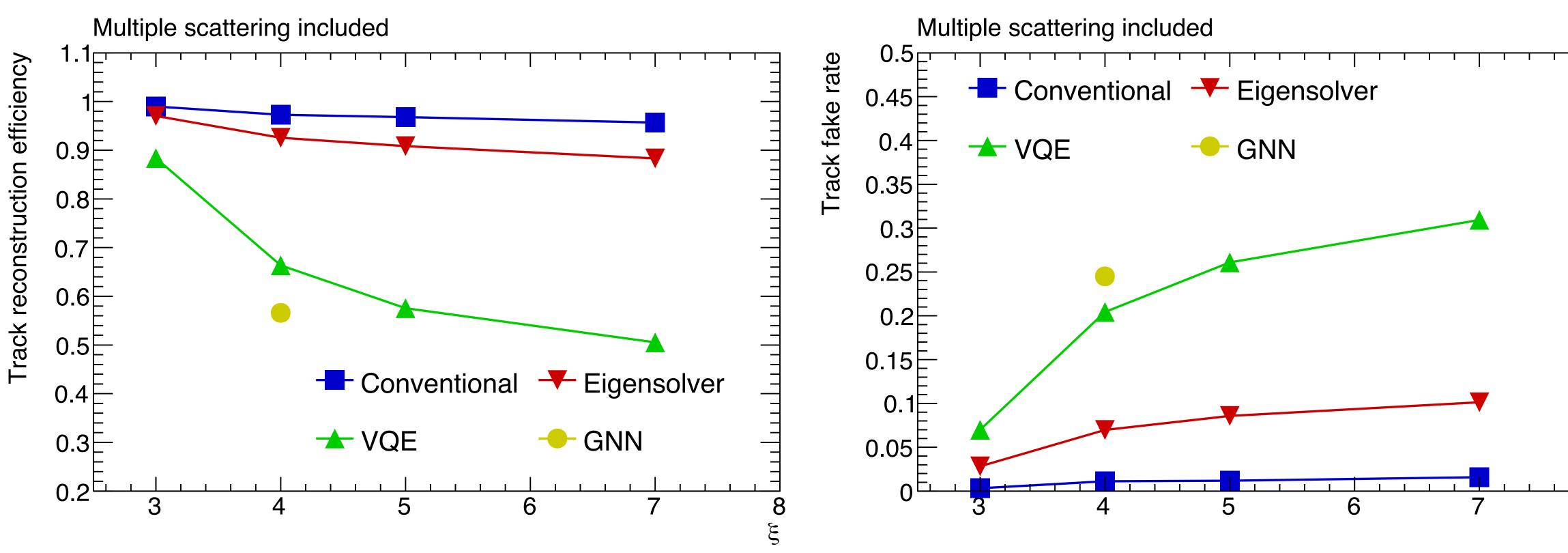
• Track must contain four hits, found either with classical CKF tracking or combining

rate =
$$\frac{N_{\text{tracks}}^{\text{fake}}}{N_{\text{tracks}}^{\text{reconstructed}}}$$

• Compare classical (CKF and GNN) and quantum (VQE and exact solution) approaches.



RESULTS



*GNN performance limited by training data size.

Yee Chinn Yap

• Conventional tracking as benchmark shows the performance that can be realistically achieved. Room for improvement for other tracking methods (preliminary results shown).





SUMMARY AND NEXT STEPS

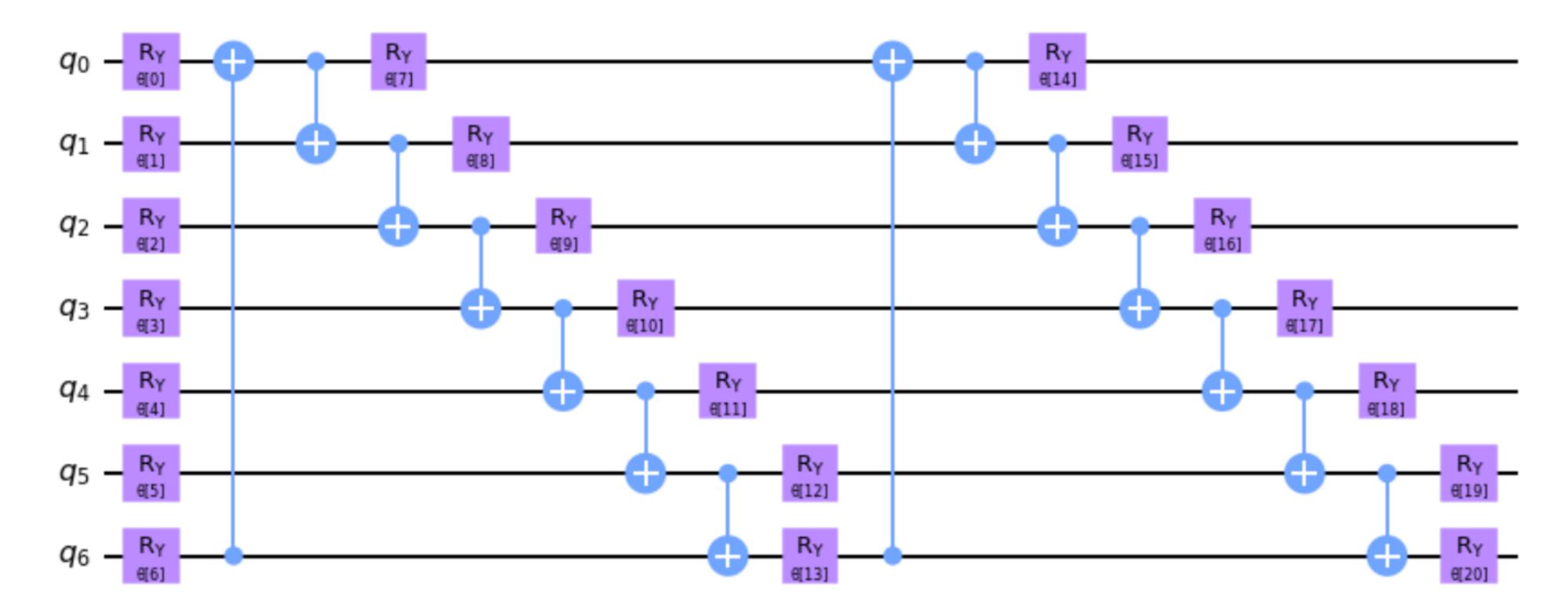
- Tracking challenge in LUXE presented.
- Study the use of a hybrid quantum-classical algorithm in track reconstruction along with conventional tracking method as well as GNN-based tracking.
- A first implementation of track reconstruction in LUXE using quantum devices is in place. • Preliminary study shows performance similar to traditional algorithms, however
 - limited by the size of the device.
- Next:
 - Study the performance in more extreme environments, take into account the QC noise and explore regions where QC could outperform the traditional methods.



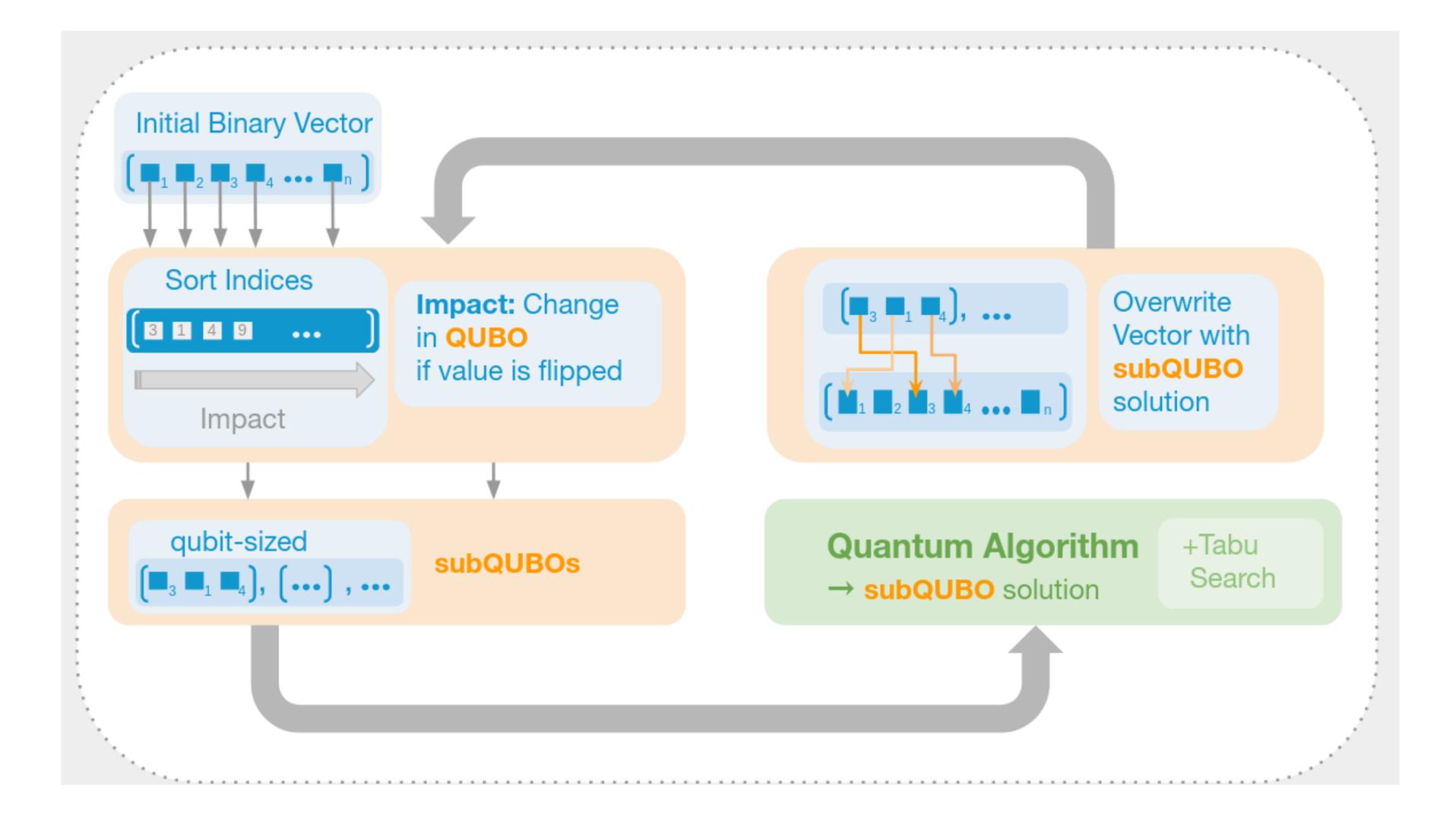
BACK-UP SLIDES

VQE

- VQE ansatz: TwoLocal with R_Y, and circular CNOT entangler.
- Optimiser: COBYLA









QUANTUM DEVICE

- Comparison of real quantum hardware and ideal noise-free simulation.
- 2 tracks, 5 triplets, 5 qubits.
- Correct triplet identified.

