

ON THE FUTURE OF THE PLANET:

***THE UNIVERSAL LAWS OF LIFE, GROWTH, DEATH &
SUSTAINABILITY FROM ORGANISMS TO CITIES***

GEOFFREY WEST

SANTA FE INSTITUTE

GREEN-TEMPLETON COLLEGE, OXFORD UNIVERSITY

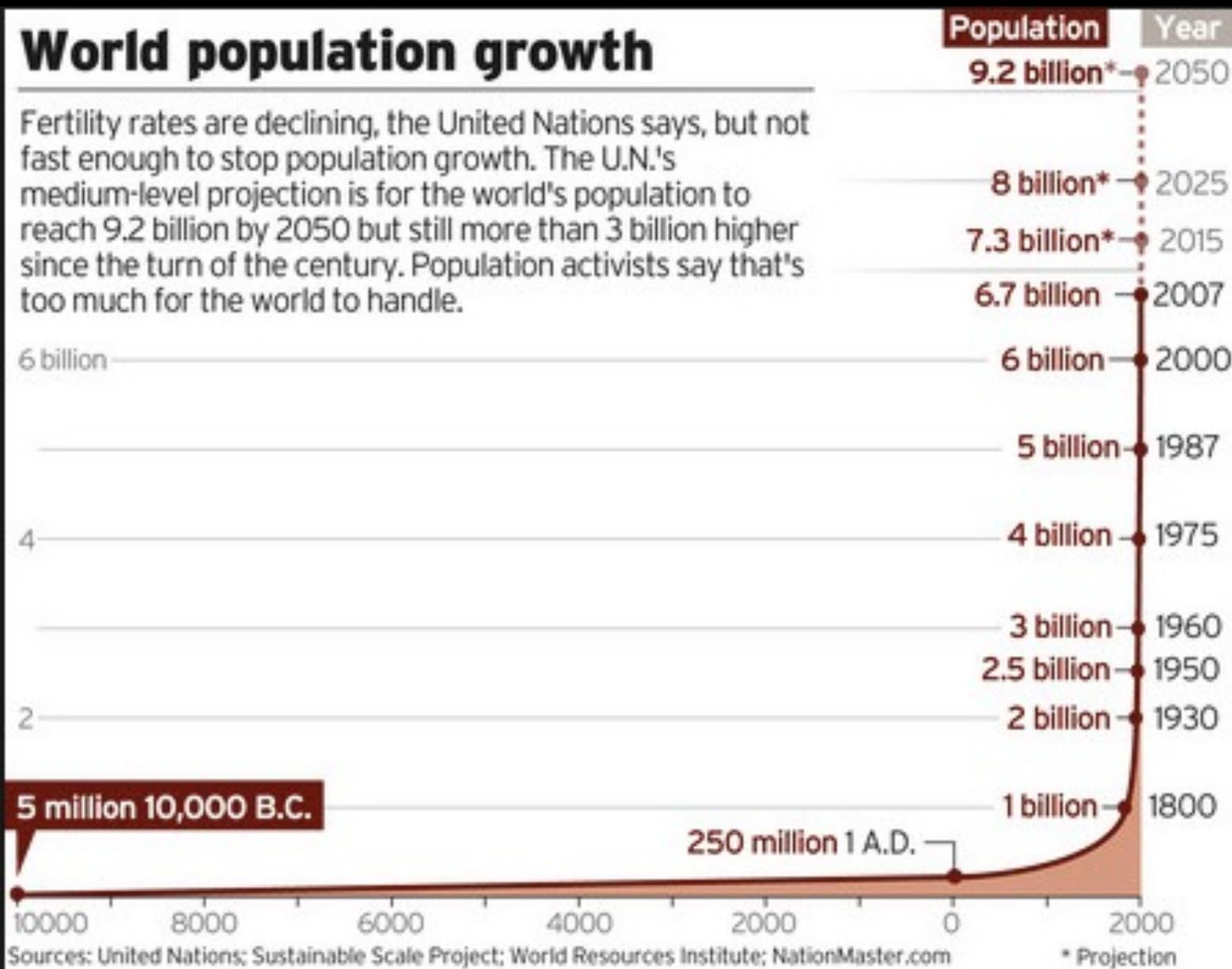
The ever accelerating progress of technology....gives the appearance of approaching some essential singularity in the history of the race beyond which human affairs, as we know them, could not continue.



**John von
Neumann
(1953)**

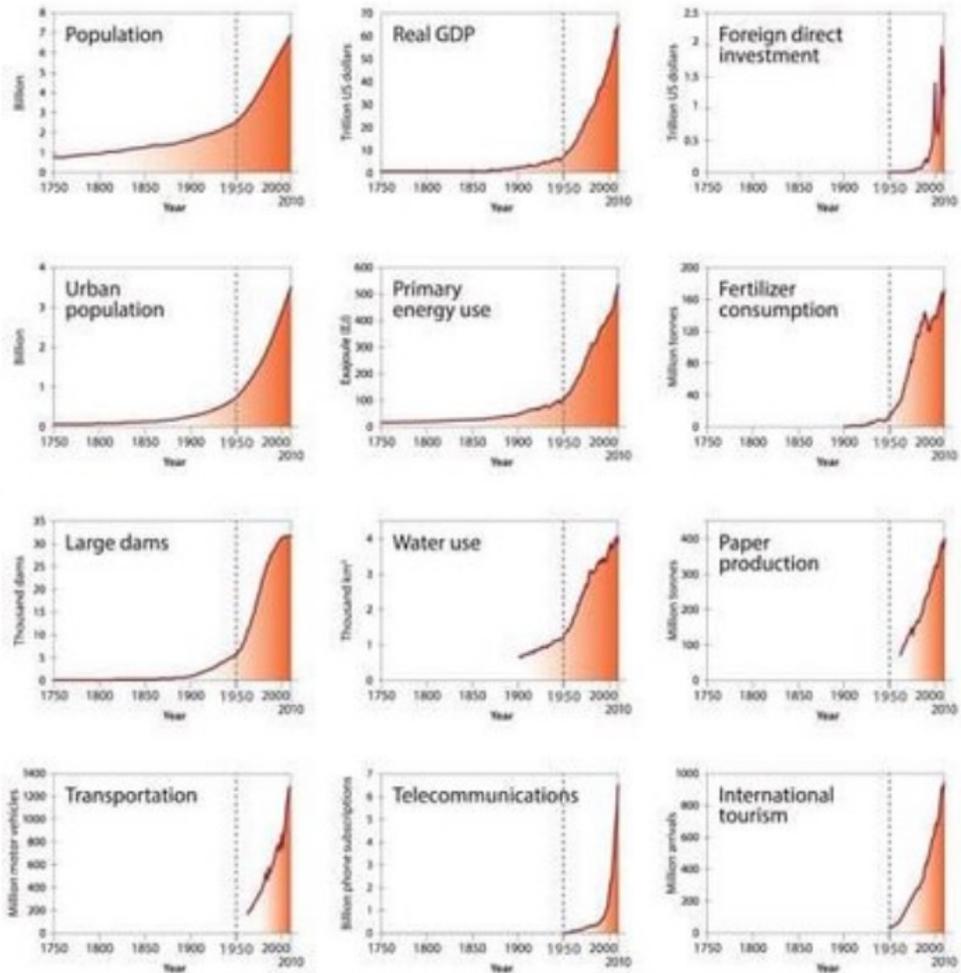
World population growth

Fertility rates are declining, the United Nations says, but not fast enough to stop population growth. The U.N.'s medium-level projection is for the world's population to reach 9.2 billion by 2050 but still more than 3 billion higher since the turn of the century. Population activists say that's too much for the world to handle.

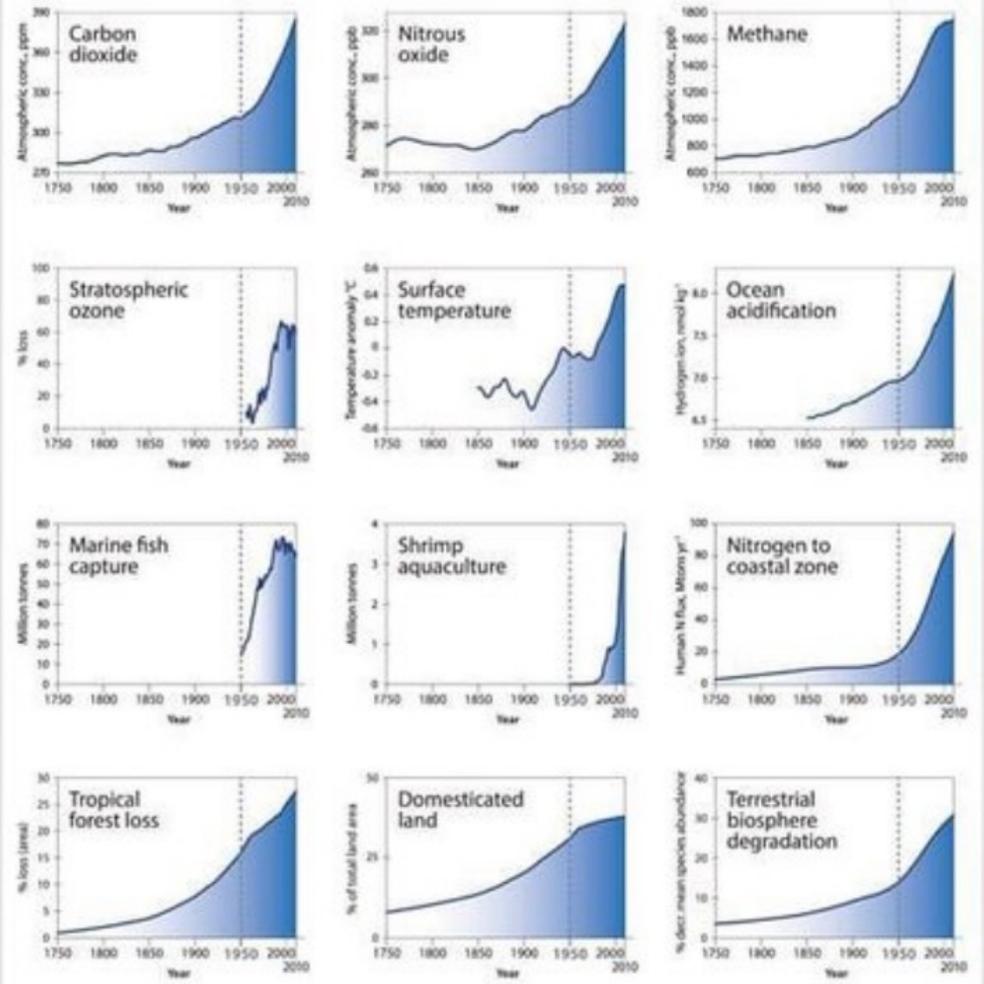


THE GREAT ACCELERATION

Socio-economic trends



Earth system trends



Updated Great Acceleration Graphs

Source: Will Steffen et al. "The trajectory of the Anthropocene: The Great Acceleration." *The Anthropocene Review*, March 2015

***WE LIVE IN AN EXPONENTIALLY
EXPANDING SOCIO-ECONOMIC
UNIVERSE!!***





***AVERAGED FROM FROM NOW TILL
2050 WE ARE URBANISING OVER ONE
MILLION PEOPLE EVERY WEEK***

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***EQUIVALENT TO ADDING A NEW YORK
METROPOLITAN AREA EVERY THREE MONTHS***

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2050 WE ARE URBANISING OVER ONE
MILLION PEOPLE EVERY WEEK***

***EQUIVALENT TO ADDING A NEW YORK
METROPOLITAN AREA EVERY THREE MONTHS***

OR.....A HAMBURG EVERY 9-10 DAYS



FATE OF OUR PLANET IS
the fate of our cities









**THE CITY IS THE MARVELLOUS MACHINE WE
DEVELOPED FOR FACILITATING THE
CREATION OF**

THE CITY IS THE MARVELLOUS MACHINE WE DEVELOPED FOR FACILITATING THE CREATION OF

- *WEALTH*
- *KNOWLEDGE, INNOVATION AND IDEAS*
- *INCREASED STANDARDS & QUALITY OF LIFE*

**BUT UNINTENTIONALLY AND INEVITABLY IT
ALSO CREATES**

**SOCIAL AND PHYSICAL
ENTROPY:**









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FRIDAY

**MASSIVE
INCREASE
IN KNIFE
CRIME
SURVEYS**

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Standard

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DISEASE AND PANDEMICS!



SOCIAL UNREST!

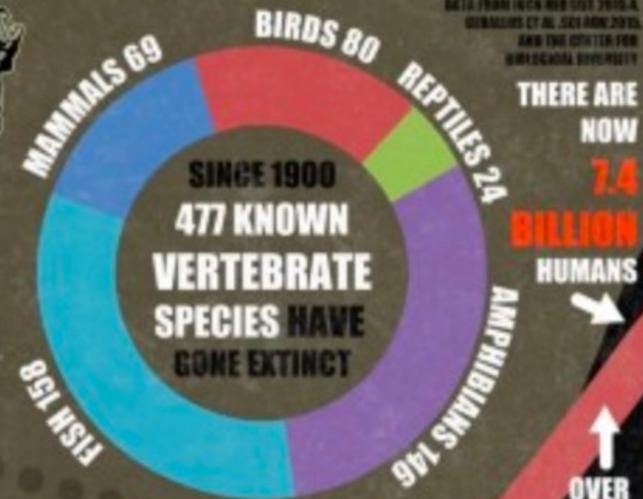


ARE WE EXPERIENCING THE 6TH MASS EXTINCTION?

ECO Sapien ecosapien.org

CURRENT RATE OF SPECIES EXTINCTION IS THOUGHT TO BE UP TO **10,000x** GREATER THAN WOULD NATURALLY BE EXPECTED WITHOUT HUMANS

PROPORTION OF EXINCTION-THREATENED SPECIES WITHIN TAXON



DATA FROM IUCN RED LIST 2014, WILKINS ET AL. 2014 AND THE CENTER FOR BIODIVERSITY

THERE ARE NOW **7.4 BILLION** HUMANS

ONLY **5%** OF THE 1.9 MILLION KNOWN SPECIES HAVE BEEN ASSESSED, SO THE TRUE EXTINCTION RISK OF MANY SPECIES MAY BE EVEN GREATER

OVER **1.5%** OF IUCN ASSESSED VERTEBRATES ARE NOW EXTINCT

GLOBAL HUMAN POPULATION



London After Climate Change?



Population, health,
well-being,...

Energy,
resources, food, ...
Thermodynamics
, metabolics, ...

Social,
political, cultural, ...
Organization,
structure, ...

Economy, finance,
development, ...
Risk, information,
innovation, ...

Ecology,
environment,
climate, ...

The background is a dark blue gradient with several light green geometric elements: thin lines forming a partial frame, and several circles of varying sizes, some filled with diagonal hatching. The text is centered in white and light green.

THESE ARE NOT INDEPENDENT

They are all highly coupled, inter-related,
multi-scale *complex adaptive systems*.

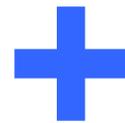
**CAN'T WAIT FOR THE ROAD
TO BE WIDENED!**





***CITIES ARE QUINTESSENTIAL COMPLEX
ADAPTIVE SYSTEMS***

**ENERGY & RESOURCES
(METABOLISM, INFRASTRUCTURE)**



**INFORMATION
(GENOMICS, INNOVATION)**

Q: Some say that while the 20th century was the century of physics, we are now entering the century of biology. What do you think of this?

Stephen Hawking interview,
January, 2000

Q: Some say that while the 20th century was the century of physics, we are now entering the century of biology. What do you think of this?

A: I think the next century will be the century of complexity.

Stephen Hawking interview,
January, 2000

***CAN THERE BE “NEWTON’S LAWS OF
COMPLEX ADAPTIVE SYSTEMS”?***

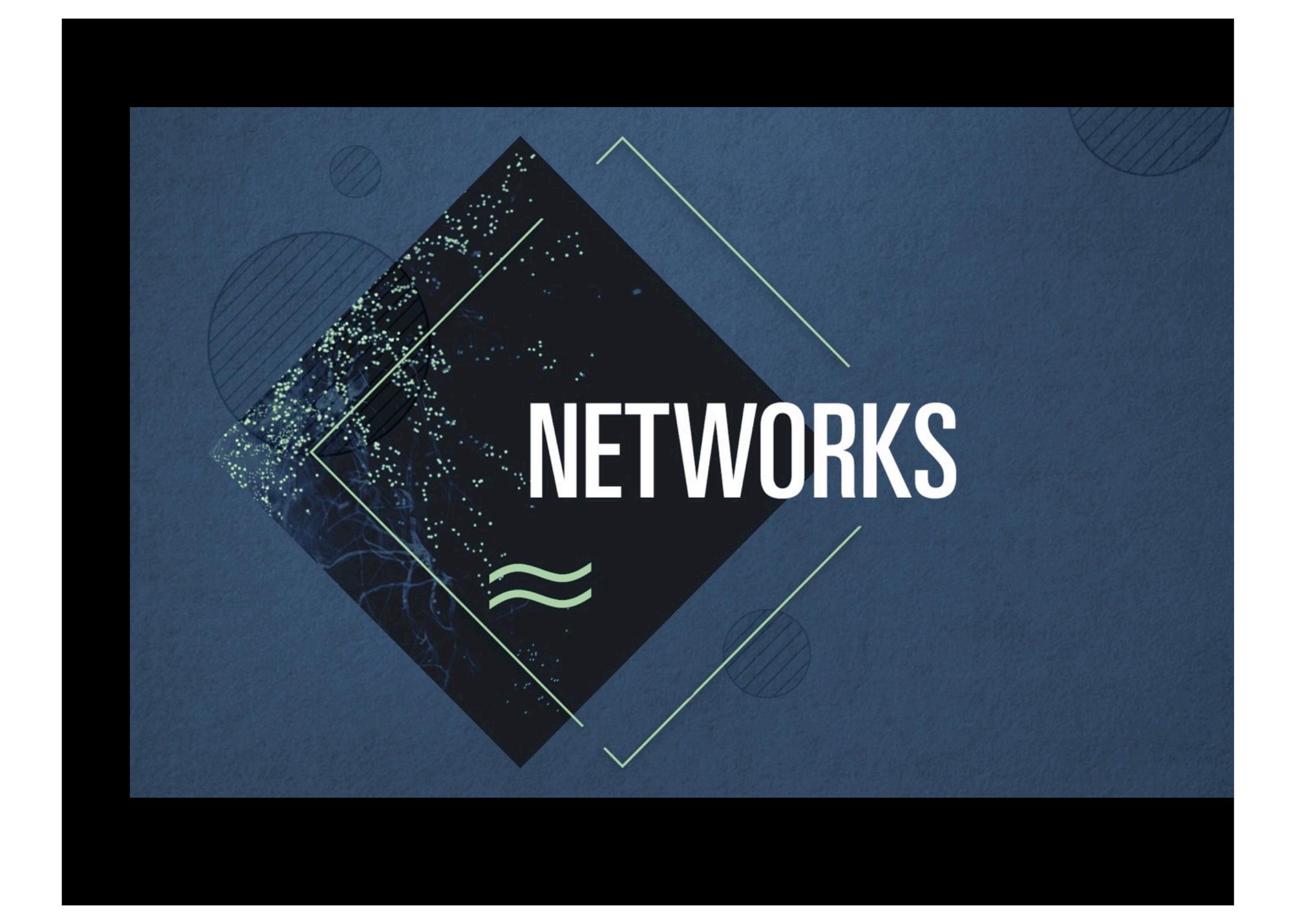
***CAN THERE BE “NEWTON’S LAWS OF
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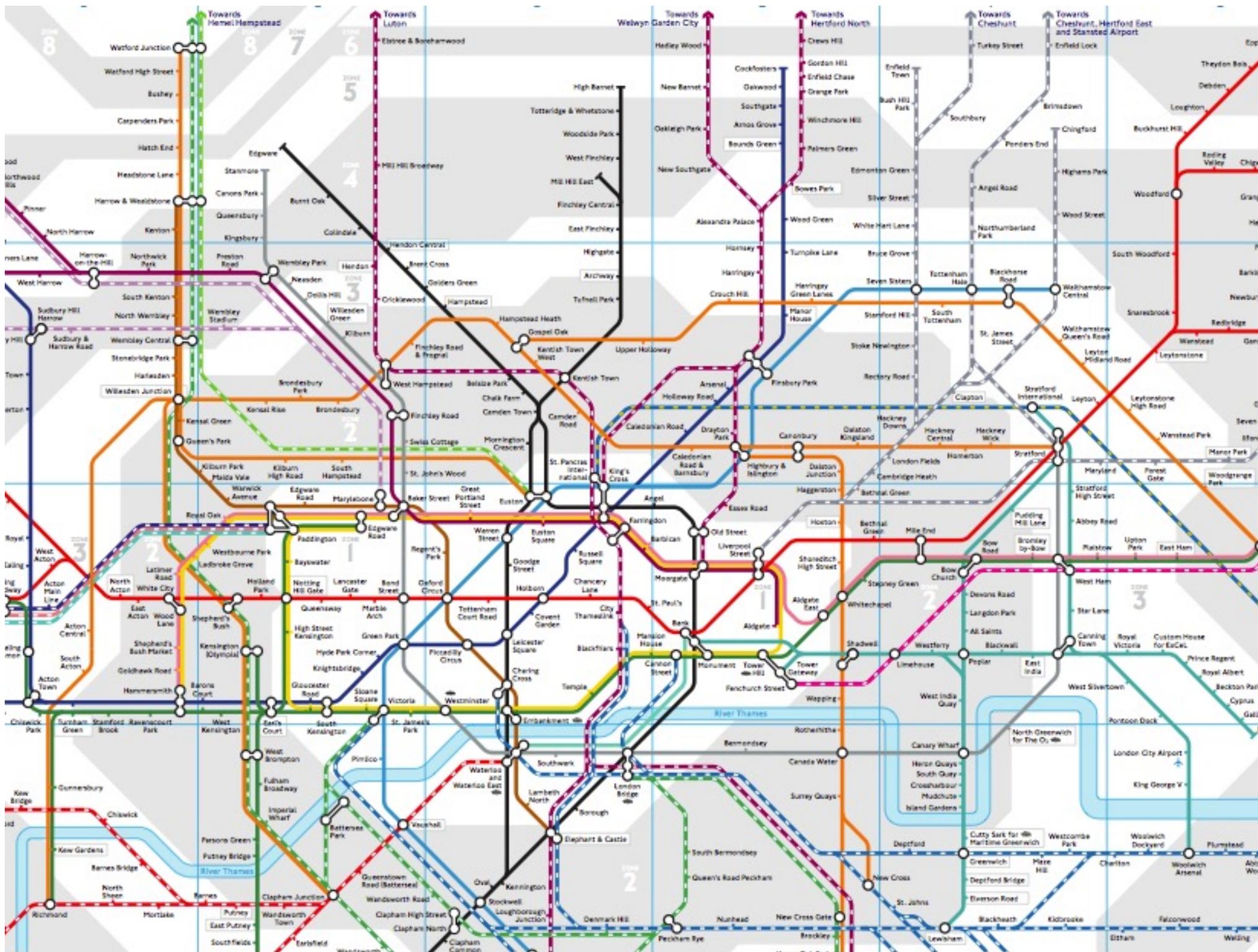
***BUT, CAN STILL ASK WHETHER
THERE ARE EMERGENT COARSE -
GRAINED LAWS AND PRINCIPLES
THAT LEAD TO A QUANTITATIVE
COMPUTATIONAL
(MATHEMATISABLE) PREDICTIVE
CONCEPTUAL FRAMEWORK***



NETWORKS



SATELLITE IMAGING CORPORATION
12777 JONES ROAD, SUITE 370
HOUSTON, TEXAS 77070-4647 USA
TEL: 1.832.237.2900
FAX: 1.832.237.2810







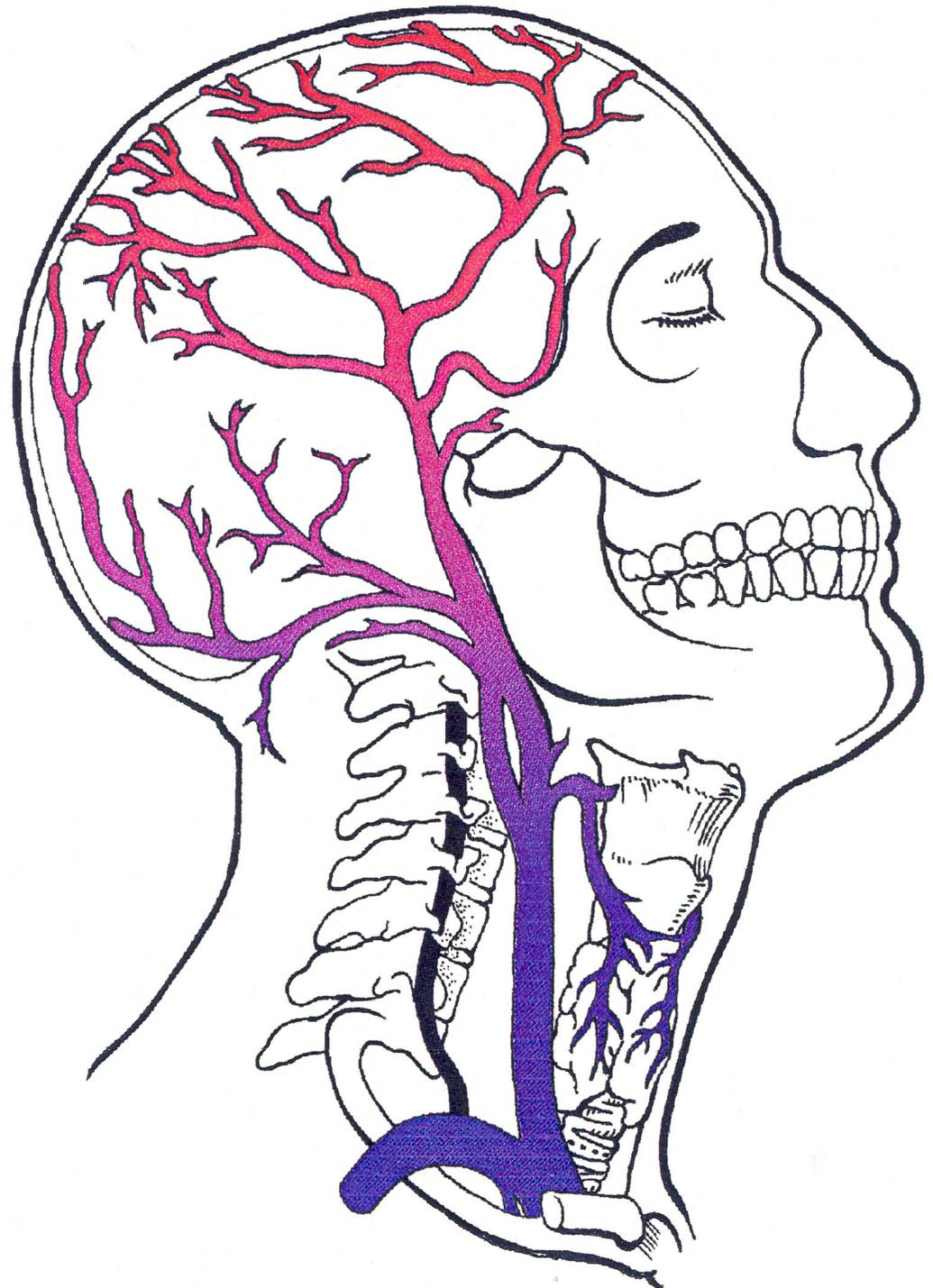




**Large vessels
branch into
smaller ones**

Beating heart

**Pulse wave
propagates
through elastic
vessels**



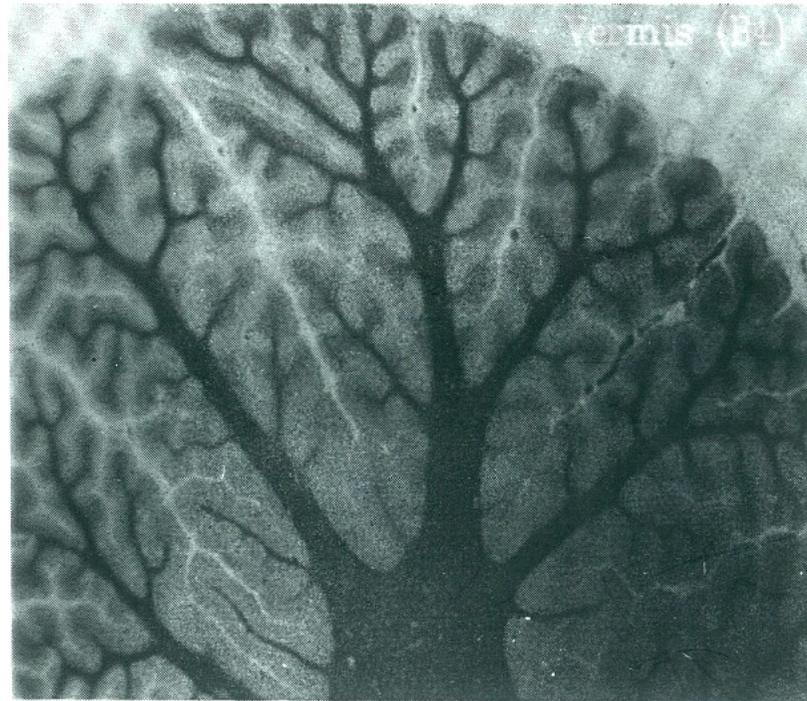
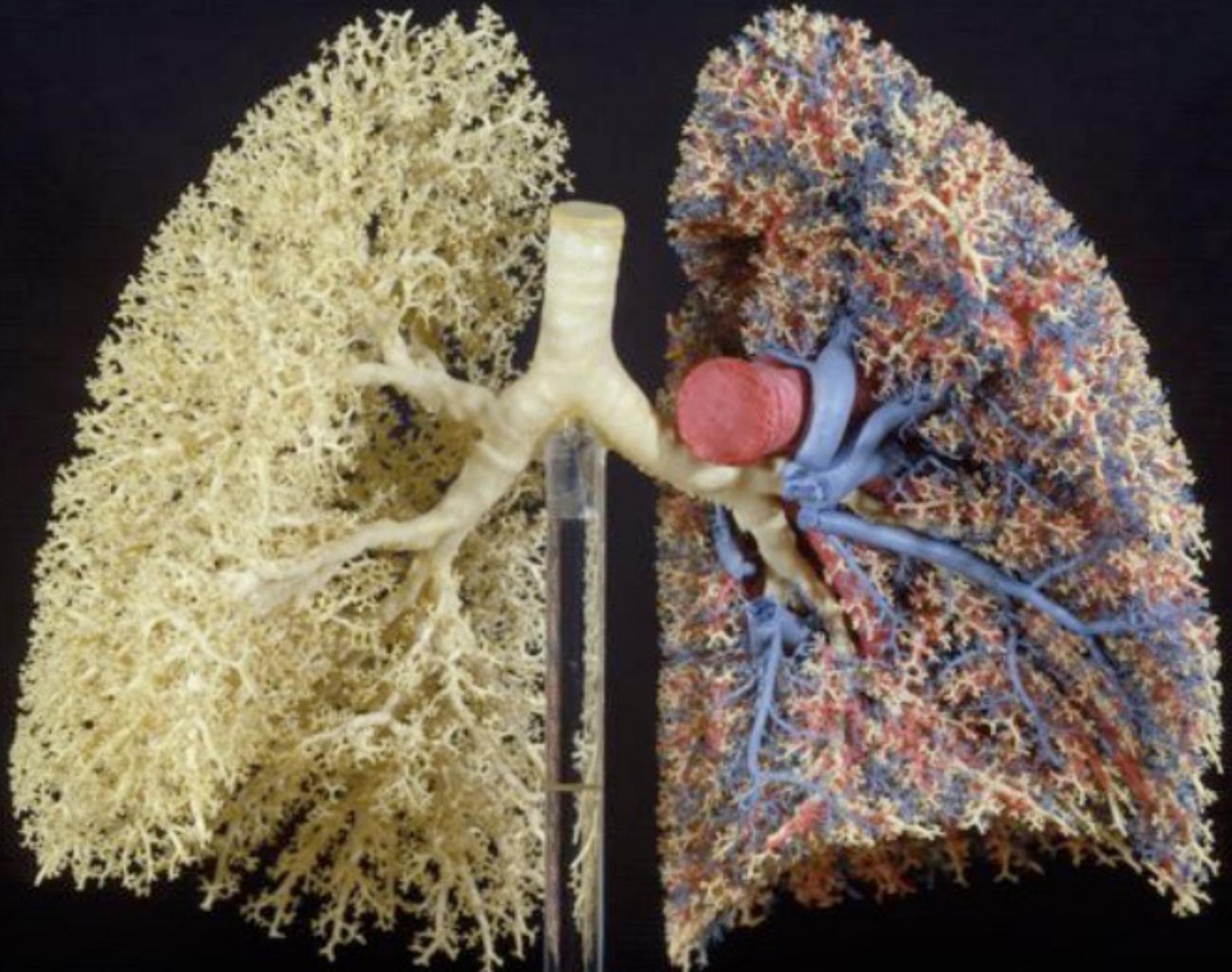
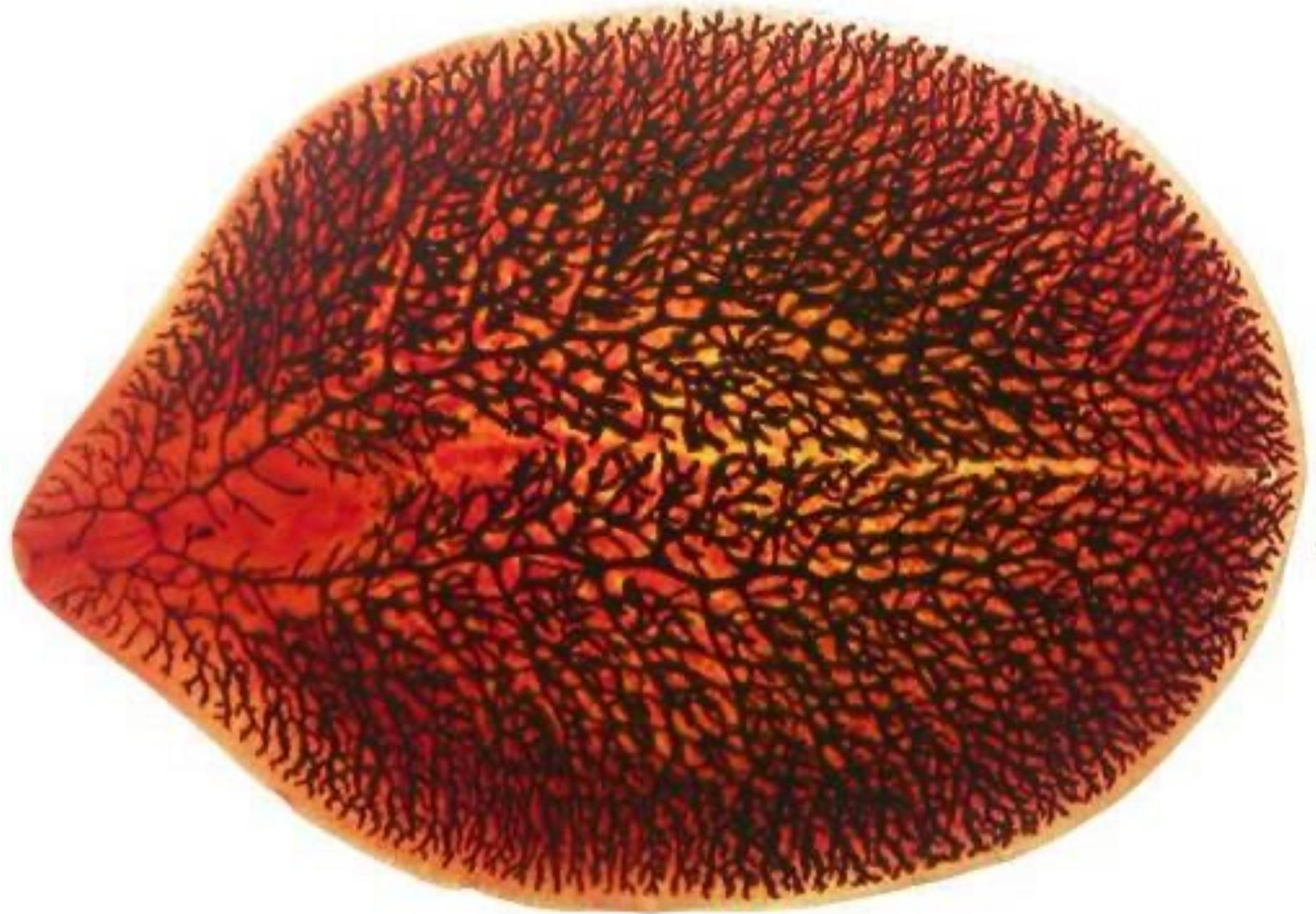


Figure 5: A slice through the cerebellum showing the progressive branching structure. The white matter is distributed throughout the cerebellar volume. The geometric complexity of these structures provides for rapid dissemination of information (or energy) via a large surface area in a compact space. This feature is a hallmark of structures which maximize the surface area within a finite volume.



Relation between number and size of branches within a tree





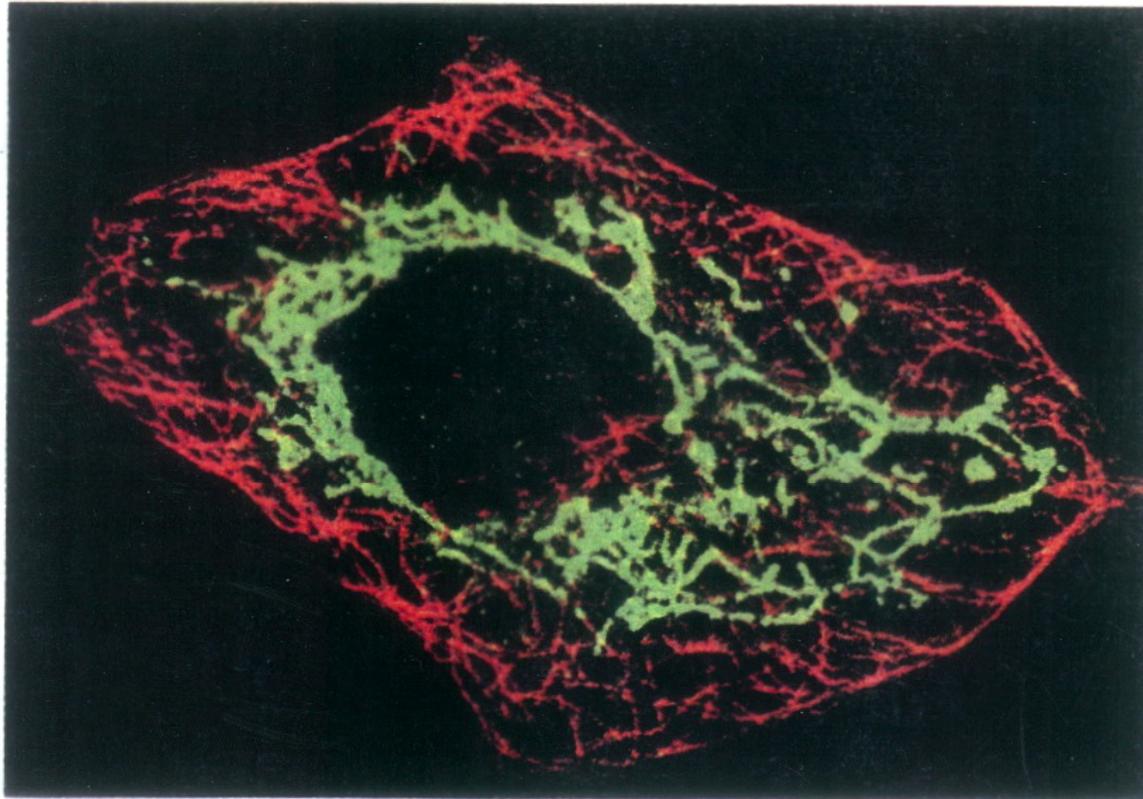
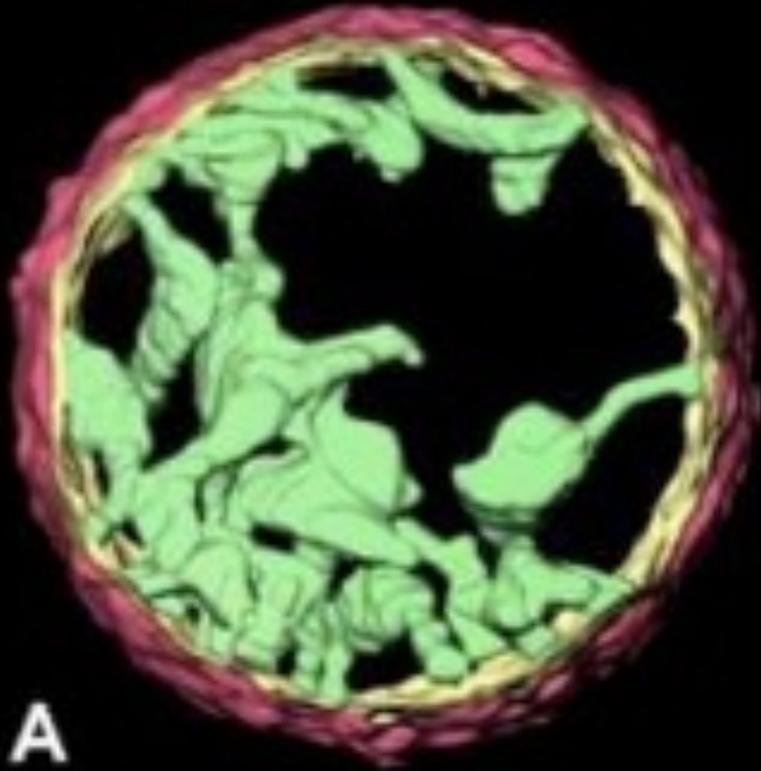
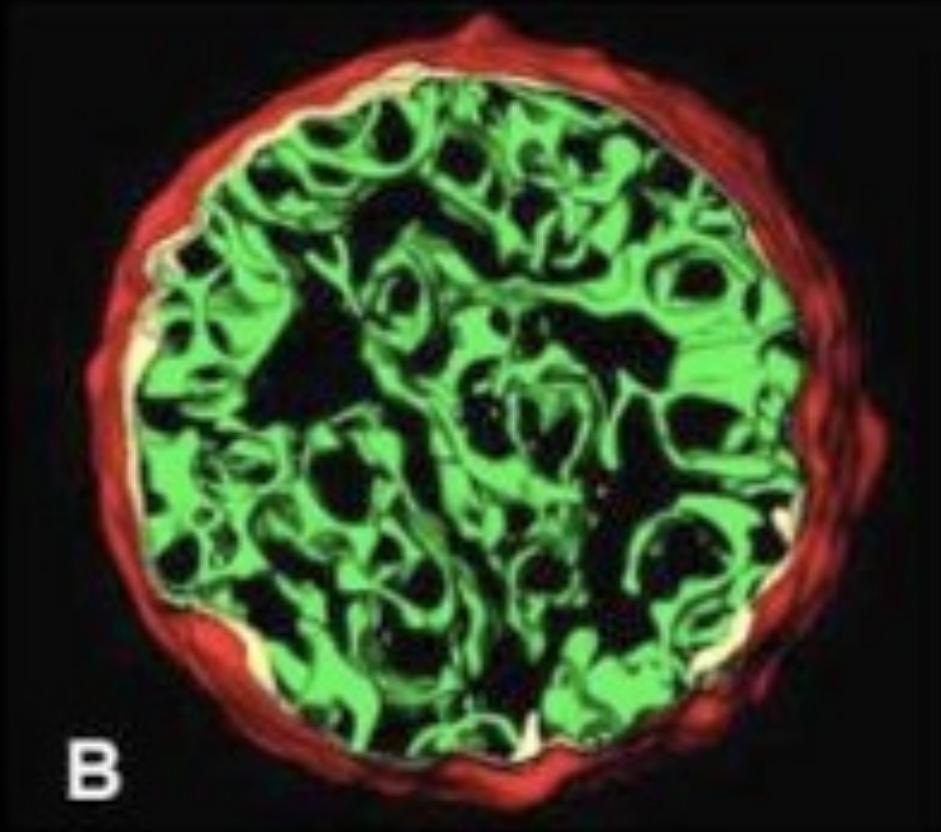


Fig. 1. Mitochondrial network in a mammalian fibroblast. A COS-7 cell labeled to visualize mitochondria (green) and microtubules (red) was analyzed by indirect immunofluorescence confocal microscopy. Mitochondria were labeled with antibodies to the β subunit of the F_1 -ATPase and a rhodamine-conjugated secondary antibody. Microtubules were labeled with antibody to tubulin and a fluorescein-conjugated secondary antibody. Pseudocolor was added to the digitized image. Scale: 1 cm = 10 μ m.

From M. P. Yaffe, *Science*, 283, 1493 (1999).



A



B

FUNDAMENTAL PRINCIPLES

(NATURAL SELECTION)

- I. AT ALL SCALES ORGANISMS ARE SUSTAINED BY THE TRANSPORT OF ENERGY AND ESSENTIAL MATERIALS THROUGH HIERARCHICAL BRANCHING NETWORK SYSTEMS IN ORDER TO SUPPLY ALL LOCAL PARTS OF THE ORGANISM
- II. THESE NETWORKS ARE SPACE-FILLING
- III. THE TERMINAL BRANCHES OF THE NETWORK ARE INVARIANT UNITS
- IV. ORGANISMS HAVE EVOLVED BY NATURAL SELECTION SO AS TO
 - i) MINIMISE ENERGY DISSIPATED IN THE NETWORKS
 - AND/OR ii) MAXIMISE THE SCALING OF THEIR AREA OF INTERFACE WITH THEIR RESOURCE ENVIRONMENT

"EVERYTHING" FOLLOWS FROM THE 4 BASIC PRINCIPLES

I. HIERARCHICAL "FRACTAL-LIKE" BRANCHING

NETWORKS

II. SPACE-FILLING

"AVERAGE
IDEALISED
ORGANISM
OR SYSTEM"

III. INVARIANT TERMINAL UNITS

IV. ENERGY DISSIPATED IS MINIMISED

II \Rightarrow i) SPACE-FILLING $\frac{L_{tot}}{L_h} = \frac{1}{2^{1/3}} \quad \frac{1}{n^{1/4}}$

III \Rightarrow ii) INV. TERMINAL UNITS

IV \Rightarrow $\left\{ \begin{array}{l} \text{iii) AREA-PRESERVING BRANCHING} \quad \frac{T_{tot}}{T_h} = \frac{1}{2^{1/4}} \\ \text{iv) VOLUME OF NETWORK (BLOOD)} \\ \quad \sim \text{VOLUME OF WHOLE BODY} \sim M \end{array} \right.$

$\Rightarrow B \propto M^{3/4}$ (AND MUCH MORE)

[MORE GENERALLY: $B \propto M^{b(M)}$ WITH $b(M) \geq 3/4$ M LARGE
 $< 3/4$ M SMALL
 $= 1$ M $< \mu$]
NOT A STRICT POWER LAW!

IN d DIMENSIONS

$$B \propto M^{\frac{d}{d+1}}$$

WE LIVE IN 3 SPATIAL DIMENSIONS SO $B \propto M^{3/4}$

⇒ "3" REPRESENTS DIMENSIONALITY OF SPACE

"4" INCREASE IN DIMENSIONALITY DUE TO
FRACTAL-LIKE SPACE FILLING

LIFE HAS TAKEN ADVANTAGE OF THE POSSIBILITY OF
USING SPACE-FILLING FRACTAL-LIKE SURFACES
(WHERE ENERGY AND RESOURCES ARE EXCHANGED)

TO MAXIMISE ENERGY TRANSFER FROM THE
ENVIRONMENT

NON-FRACTAL :

AREA

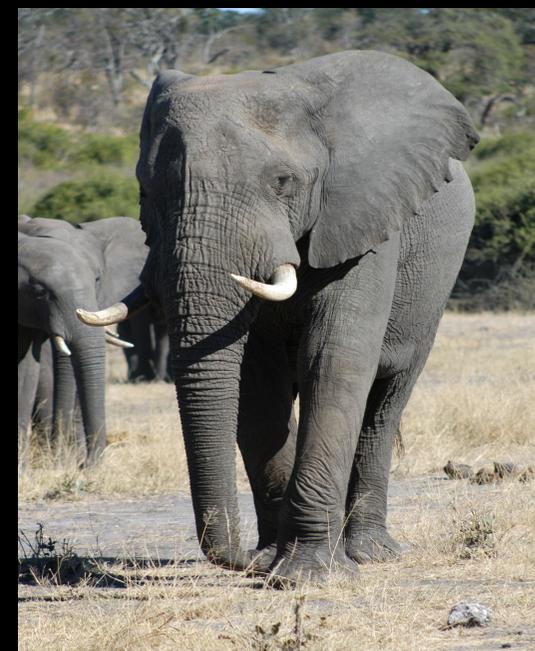
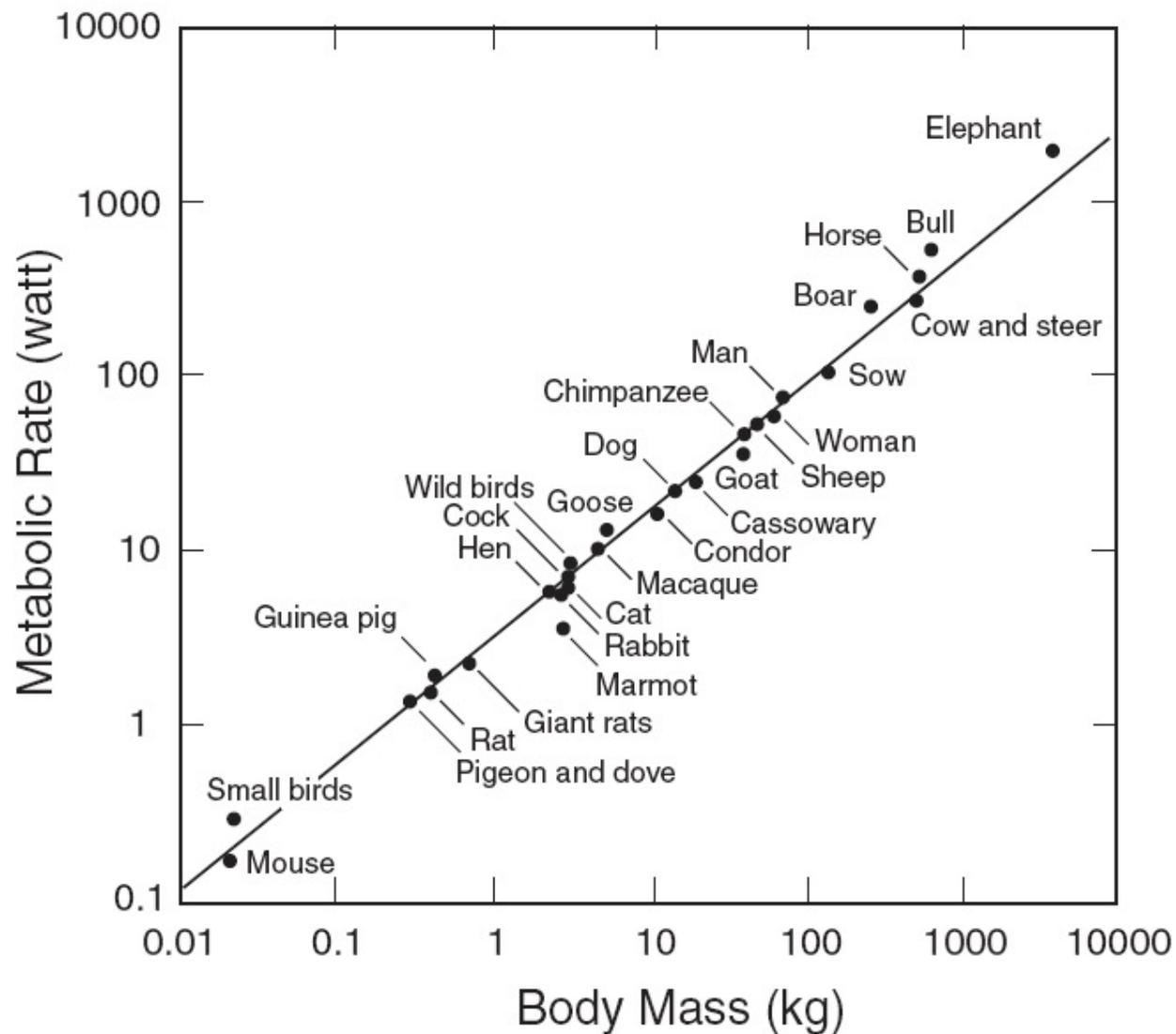
$M^{2/3}$ ← DIMENSIONALITY OF SPACE (VOLUME)

BIOLOGICAL (FRACTAL)

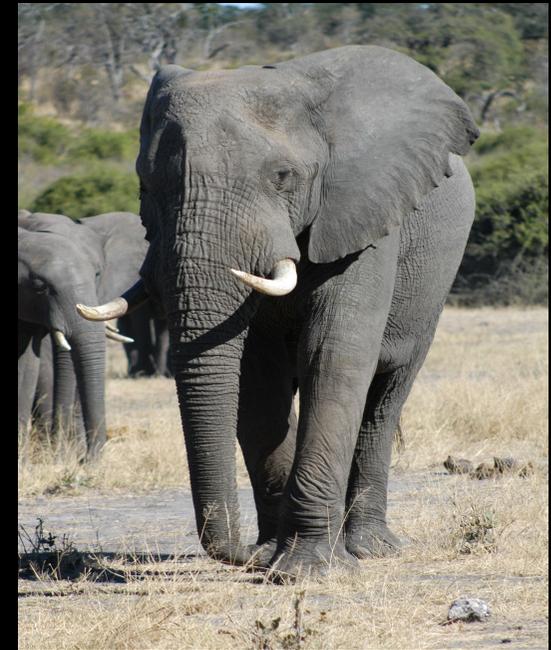
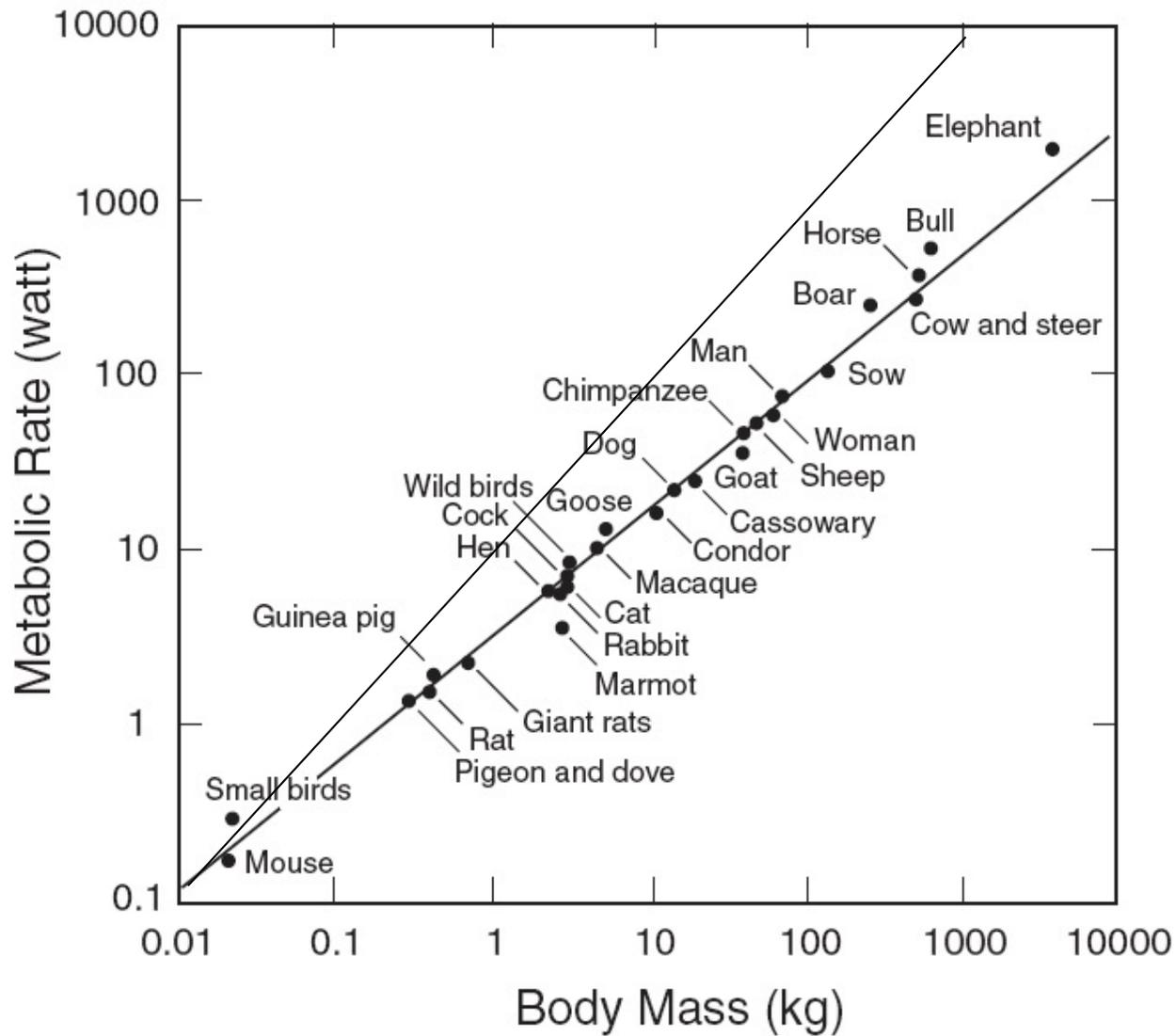
$$M^{3/4}$$

BY ANALOGY : LIFE EFFECTIVELY OPERATES IN
FOUR SPATIAL DIMENSIONS

[FIVE IF TIME IS INCLUDED]

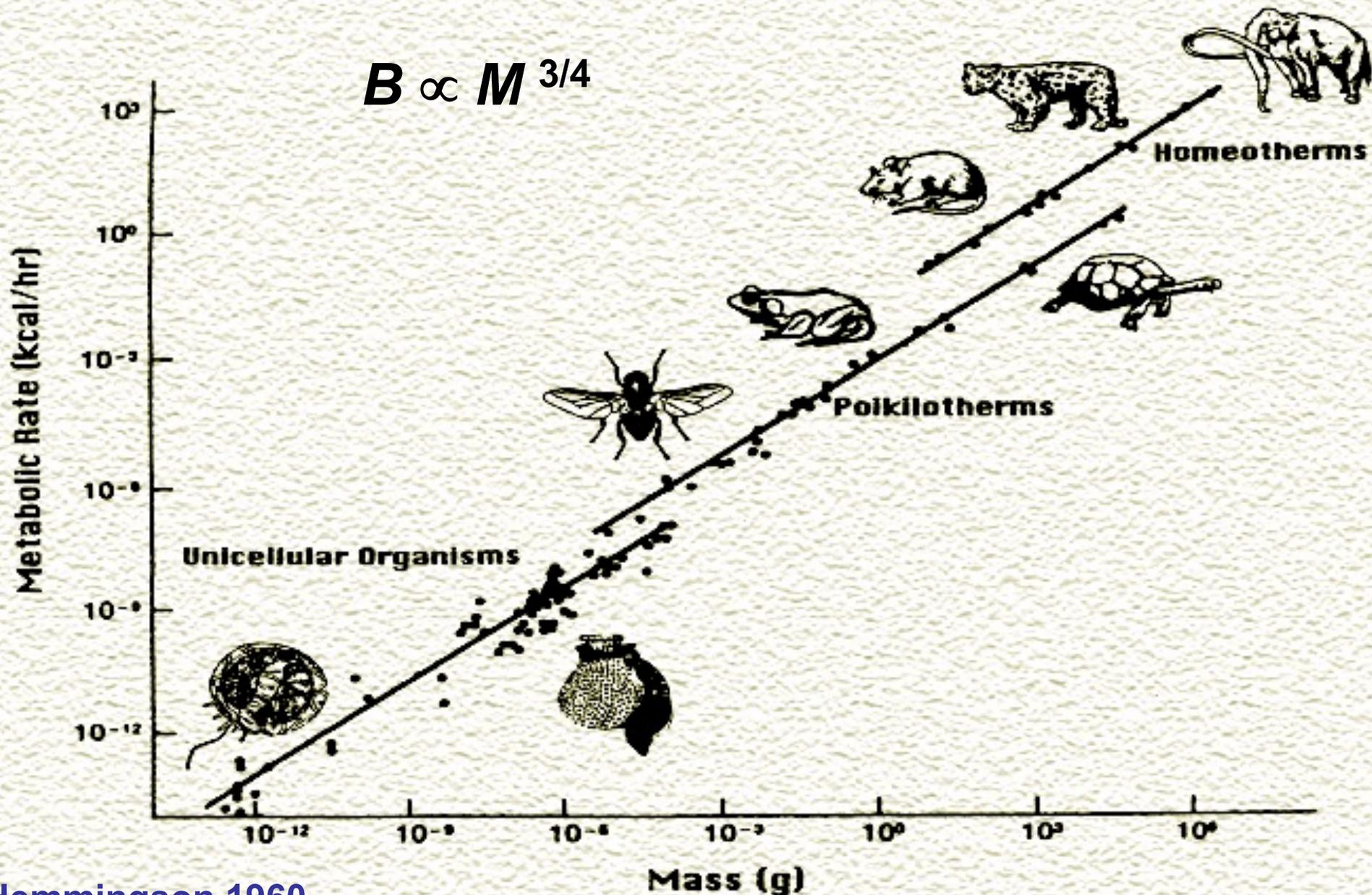


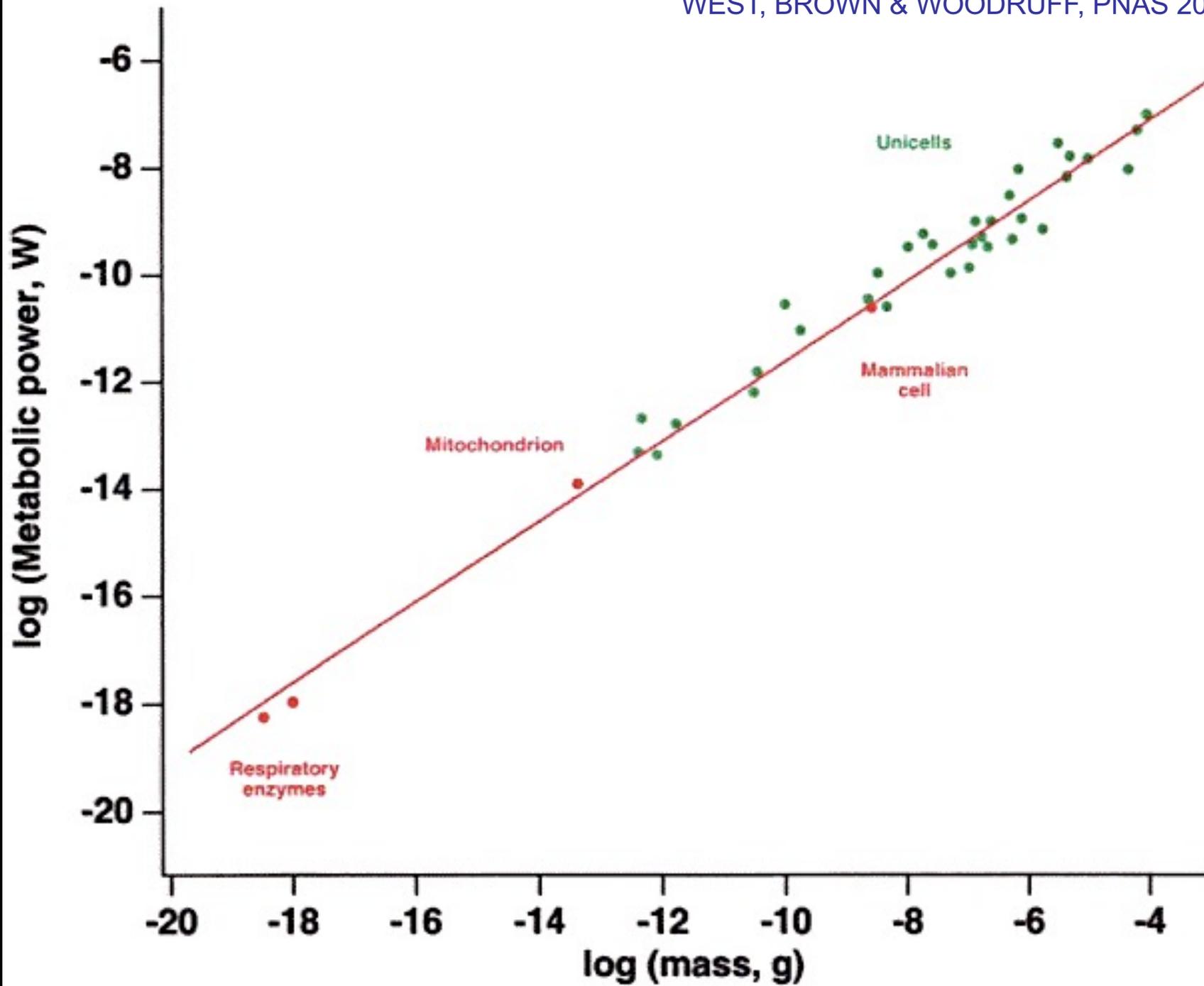
SLOPE = $\frac{3}{4}$ < 1 SUB-LINEAR ECONOMY OF SCALE



SLOPE = $\frac{3}{4}$ < 1 SUB-LINEAR ECONOMY OF SCALE

Whole-organism metabolic rate (B) scales as the $3/4$ power of body mass (M)





Cardiovascular

Variable	Exponent	
	Predicted	Observed
Aorta radius r_o	$3/8 = 0.375$	0.36
Aorta pressure Δp_o	$0 = 0.00$	0.032
Aorta blood velocity u_o	$0 = 0.00$	0.07
Blood volume V_b	$1 = 1.00$	1.00
Circulation time	$1/4 = 0.25$	0.25
Circulation distance l	$1/4 = 0.25$	ND
Cardiac stroke volume	$1 = 1.00$	1.03
Cardiac frequency ω	$-1/4 = -0.25$	-0.25
Cardiac output \dot{E}	$3/4 = 0.75$	0.74
Number of capillaries N_c	$3/4 = 0.75$	ND
Service volume radius	$1/12 = 0.083$	ND
Womersley number α	$1/4 = 0.25$	0.25
Density of capillaries	$-1/12 = -0.083$	-0.095
O_2 affinity of blood P_{50}	$-1/12 = -0.083$	-0.089
Total resistance Z	$-3/4 = -0.75$	-0.76
Metabolic rate B	$3/4 = 0.75$	0.75

Respiratory

Variable	Exponent	
	Predicted	Observed
Tracheal radius	$3/8 = 0.375$	0.39
Interpleural pressure	$0 = 0.00$	0.004
Air velocity in trachea	$0 = 0.00$	0.02
Lung volume	$1 = 1.00$	1.05
Volume flow to lung	$3/4 = 0.75$	0.80
Volume of alveolus V_A	$1/4 = 0.25$	ND
Tidal volume	$1 = 1.00$	1.041
Respiratory frequency	$-1/4 = -0.25$	-0.26
Power dissipated	$3/4 = 0.75$	0.78
Number of alveoli N_A	$3/4 = 0.75$	ND
Radius of alveolus r_A	$1/12 = 0.083$	0.13
Area of alveolus A_A	$1/6 = 0.083$	ND
Area of lung A_L	$11/12 = 0.92$	0.95
O_2 diffusing capacity	$1 = 1.00$	0.99
Total resistance	$-3/4 = -0.75$	-0.70
O_2 consumption rate	$3/4 = 0.75$	0.76

Table 1 Predicted values of scaling exponents for physiological and anatomical variables of plant vascular systems.

Variable	Plant mass		Branch radius		
	Exponent predicted	Symbol	Symbol	Exponent	
				Predicted	Observed
Number of leaves	$\frac{3}{4}$ (0.75)	n_0^l	n_k^l	2 (2.00)	2.007 (ref. 12)
Number of branches	$\frac{3}{4}$ (0.75)	N_0	N_k	-2 (-2.00)	-2.00 (ref. 6)
Number of tubes	$\frac{3}{4}$ (0.75)	n_0	n_k	2 (2.00)	n.d.
Branch length	$\frac{1}{4}$ (0.25)	l_0	l_k	$\frac{2}{3}$ (0.67)	0.652 (ref. 6)
Branch radius	$\frac{3}{8}$ (0.375)	r_0			
Area of conductive tissue	$\frac{7}{8}$ (0.875)	A_0^{CT}	A_k^{CT}	$\frac{7}{3}$ (2.33)	2.13 (ref. 8)
Tube radius	$\frac{1}{16}$ (0.0625)	a_0	a_k	$\frac{1}{6}$ (0.167)	n.d.
Conductivity	1 (1.00)	K_0	K_k	$\frac{8}{3}$ (2.67)	2.63 (ref. 12)
Leaf-specific conductivity	$\frac{1}{4}$ (0.25)	L_0	L_k	$\frac{2}{3}$ (0.67)	0.727 (ref. 17)
Fluid flow rate			\dot{Q}_k	2 (2.00)	n.d.
Metabolic rate	$\frac{3}{4}$ (0.75)	\dot{Q}_0			
Pressure gradient	$-\frac{1}{4}$ (-0.25)	$\Delta P_0/l_0$	$\Delta P_k/l_k$	$-\frac{2}{3}$ (-0.67)	n.d.
Fluid velocity	$-\frac{1}{8}$ (-0.125)	u_0	u_k	$-\frac{1}{3}$ (-0.33)	n.d.
Branch resistance	$-\frac{3}{4}$ (-0.75)	Z_0	Z_k	$-\frac{1}{3}$ (-0.33)	n.d.
Tree height	$\frac{1}{4}$ (0.25)	h			
Reproductive biomass	$\frac{3}{4}$ (0.75)				
Total fluid volume	$\frac{25}{24}$ (1.0415)				

PLANTS

**VERY DIFFERENT
EVOLVED
ENGINEERING
DESIGN (NON-
PULSATILE FIBRE
BUNDLES) BUT
SAME NETWORK
PRINCIPLES**



Table 1. Similarity of predicted scaling relations for branches within a tree [quantities denoted by uppercase symbols and subscripts i (20)], and for trees within a forest (denoted by lowercase symbols and subscripts k)*

Scaling quantity	Individual tree	Entire forest
Area preserving	$\frac{R_{i+1}}{R_i} = \frac{1}{n^{1/2}}$	$\frac{r_{k+1}}{r_k} = \frac{1}{\lambda^{1/2}}$
Space filling	$\frac{L_{i+1}}{L_i} = \frac{1}{n^{1/3}}$	$\frac{l_{k+1}}{l_k} = \frac{1}{\lambda^{1/3}}$
Biomechanics	$R_i^2 = L_i^3$	$r_k^2 = l_k^3$
Size distribution*	$\Delta N_i \propto R_i^{-2} \propto M_i^{-3/4}$	$\Delta n_k \propto r_k^{-2} \propto m_k^{-3/4}$
Energy and material flux*	$B_i \propto R_i^2 \propto N_i^L \propto M_i^{3/4}$	$B_k \propto r_k^2 \propto n_k^L \propto m_k^{3/4}$

Stand property

Predicted stem radius, r_k , based scaling function

Size class neighbor separation

$$d_k \propto r_k$$

Canopy scaling

$$r_k^{\text{can}} \propto r_k^{2/3}$$

Canopy spacing

$$d_k^{\text{can}} = c_1 r_k \left[1 - \left(\frac{r_k}{r_{\bar{k}}} \right)^{1/3} \right]$$

Energy Equivalence

$$\Delta n_k B_k \propto r_k^0$$

Total forest resource use

$$B_{\text{Tot}} \propto \sum \Delta n_k r_k^2 \leq \dot{R}$$

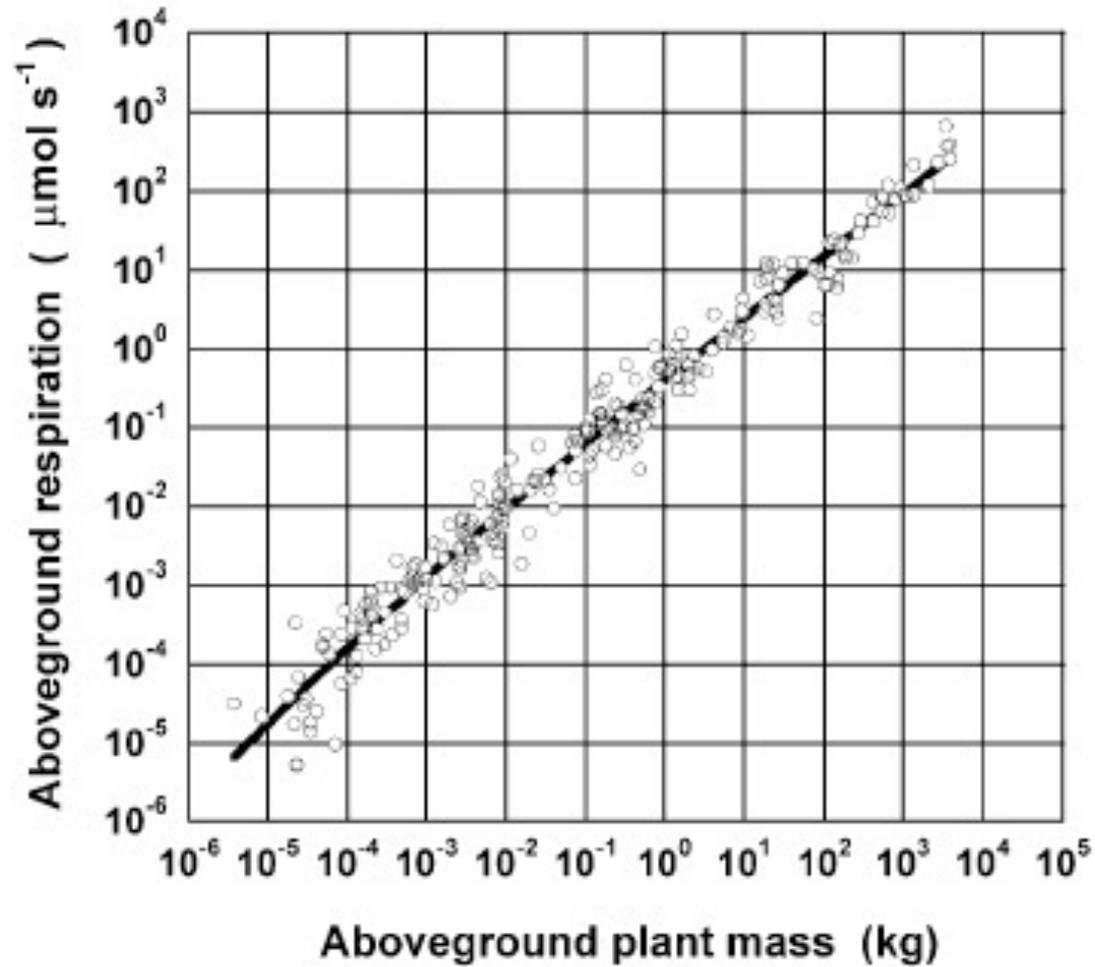
Mortality rate

$$\mu_k \approx A r_k^{-2/3}$$

Size distribution

$$N_k \approx \frac{\dot{R}}{(K+1)b_0} r_k^{-2}$$

PLANTS/TREES



$$B \propto M^{0.780 \pm 0.037}$$

SINCE $B \sim M^{3/4}$

(OVER 27 ORDERS OF MAGNITUDE)

SPECIFIC METABOLIC RATE (PER UNIT MASS)

$$\frac{B}{M} \propto M^{-1/4}$$

AND METABOLIC RATE OF AVERAGE CELL

$$B_{cell} \propto M^{-1/4}$$

THIS DECREASE OF B_c WITH SIZE IS DRIVEN

BY THE HEGEMONY OF THE NETWORK

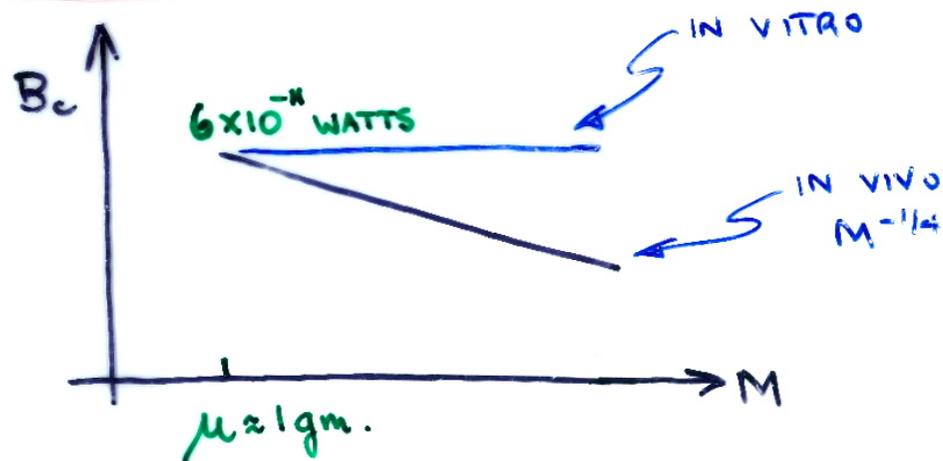
(CONTROLS FUNDAMENTAL BIOCHEMICAL RATES)

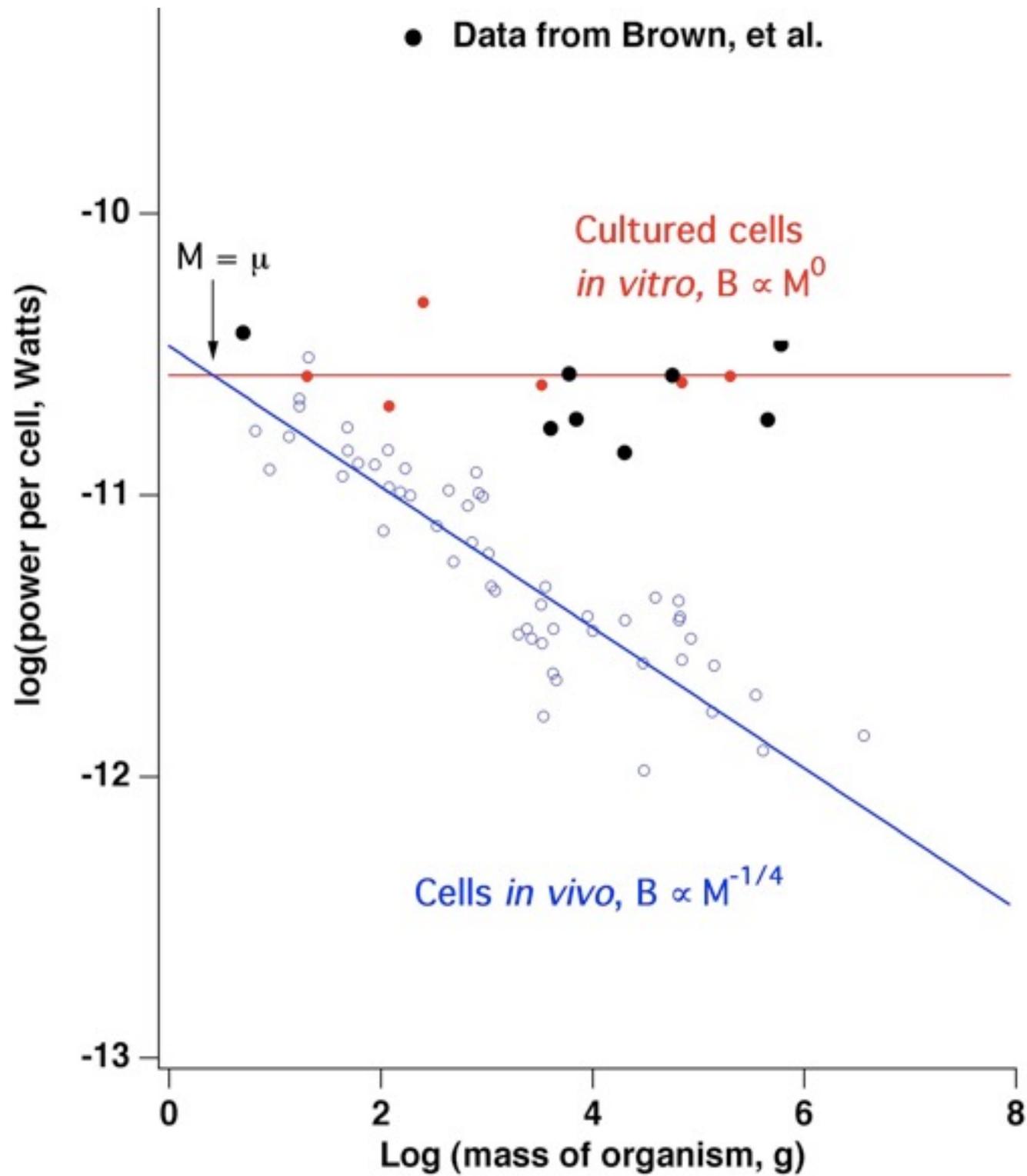
⇒ IF THE NETWORK WERE REMOVED SO CELLS

BECOME FREE (IN VITRO) B_c SHOULD BECOME

INDEPENDENT OF WHAT MAMMAL THEY ORIGINATED

IN: PREDICT





***EXTRAORDINARY SYSTEMATIC
ECONOMY OF SCALE
(THE BIGGER YOU ARE, THE LESS
ENERGY/FOOD YOU NEED PER CELL)***

***EXTRAORDINARY SYSTEMATIC
ECONOMY OF SCALE
(THE BIGGER YOU ARE, THE LESS
ENERGY/FOOD YOU NEED PER CELL)***

***SIMILAR SCALING LAWS HOLD FOR
ALMOST ALL PHYSIOLOGICAL AND LIFE
HISTORY EVENTS ACROSS THE ENTIRE
SPECTRUM OF LIFE FROM CELLS TO
ECOSYSTEMS***

Slopes (exponents) are typically
sub-linear and simple multiples of $\frac{1}{4}$

“quarter-power scaling”

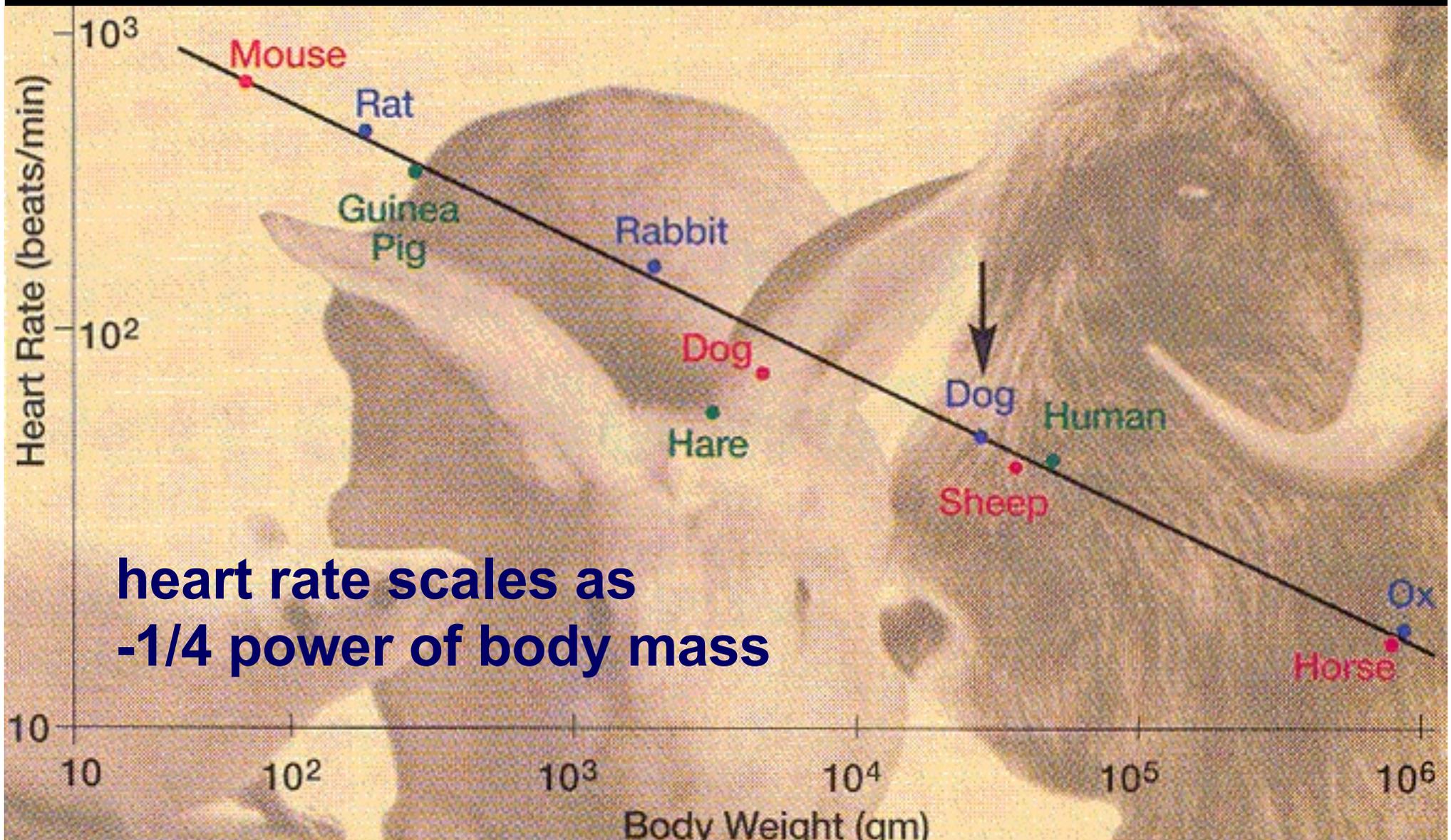
***NETWORK GEOMETRY AND DYNAMICS
CONTROLS THE PACE OF LIFE AT ALL
SCALES LEADING TO AN EMERGENT
“UNIVERSAL” TIME SCALE***

$$B_{cell} \propto \frac{B}{M} = B_0 M^{-1/4}$$

***THE PACE OF LIFE SYSTEMATICALLY
SLOWS WITH INCREASING SIZE***

Metabolic rate sets the pace of life

Small animals live fast and die young



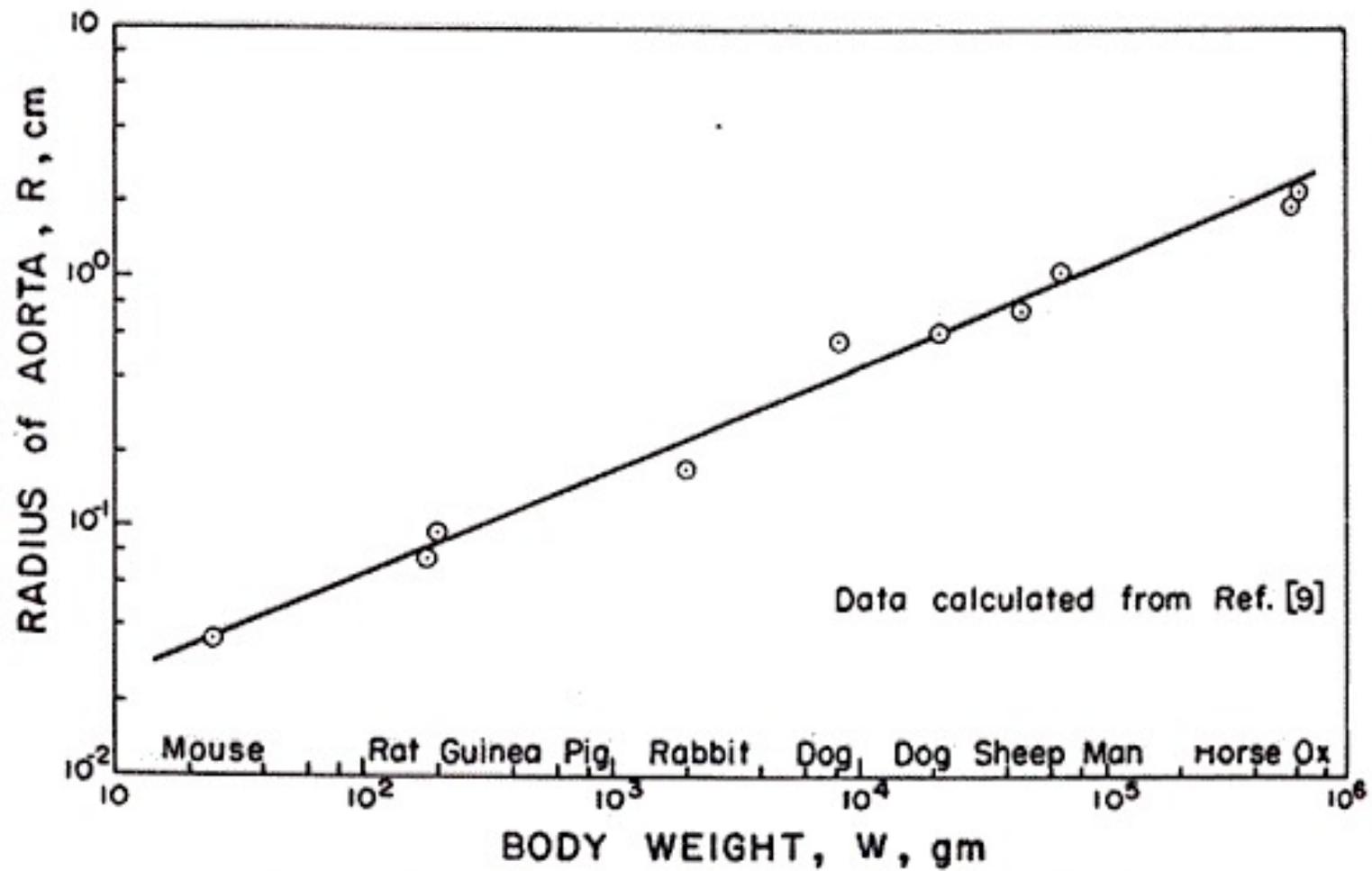
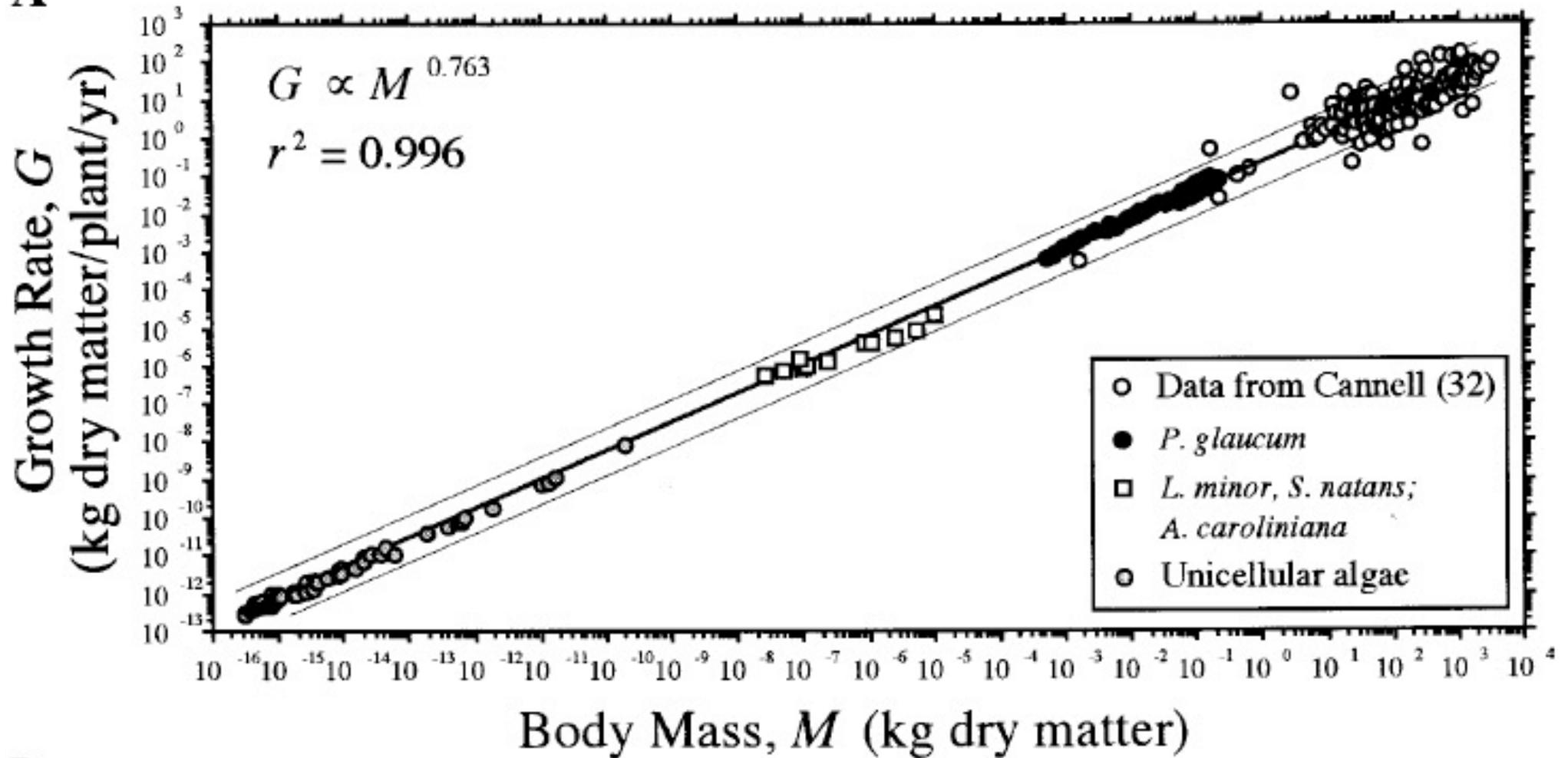


FIG. 4 - VARIATION IN RADIUS OF AORTA WITH BODY WEIGHT

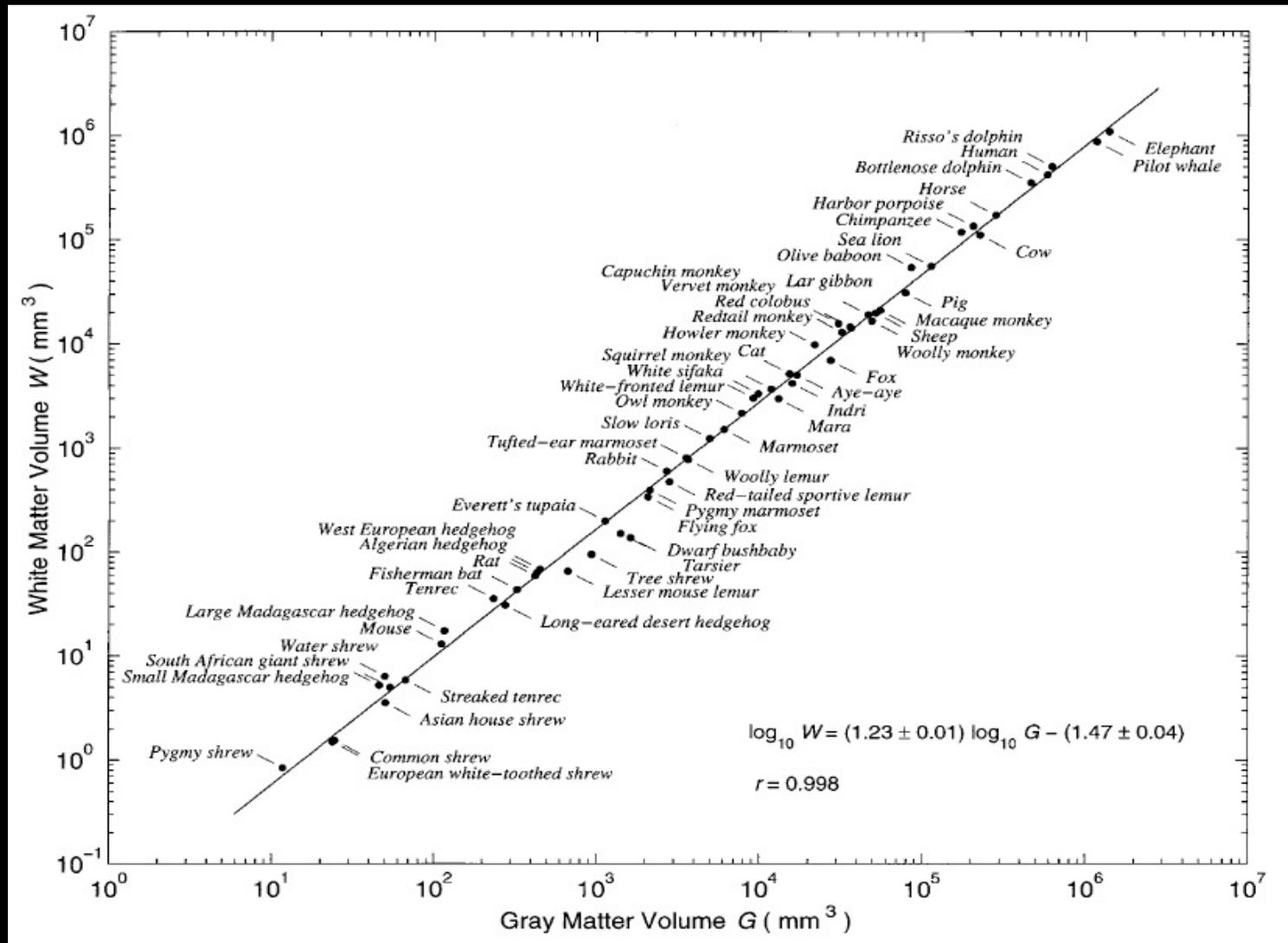
$$r \sim M^{3/8}$$

SAME SCALING FOR TREE TRUNKS

A



WHITE & GREY MATTER IN BRAINS



LIFESPAN

$$T \sim M^{1/4}$$

IF HEART-RATE (NUMBER OF BEATS PER SEC.)

$$\sim M^{-1/4}$$

⇒ TOTAL NUMBER OF HEART-BEATS IN A

TYPICAL LIFE-TIME IS INDEPENDENT OF SIZE!

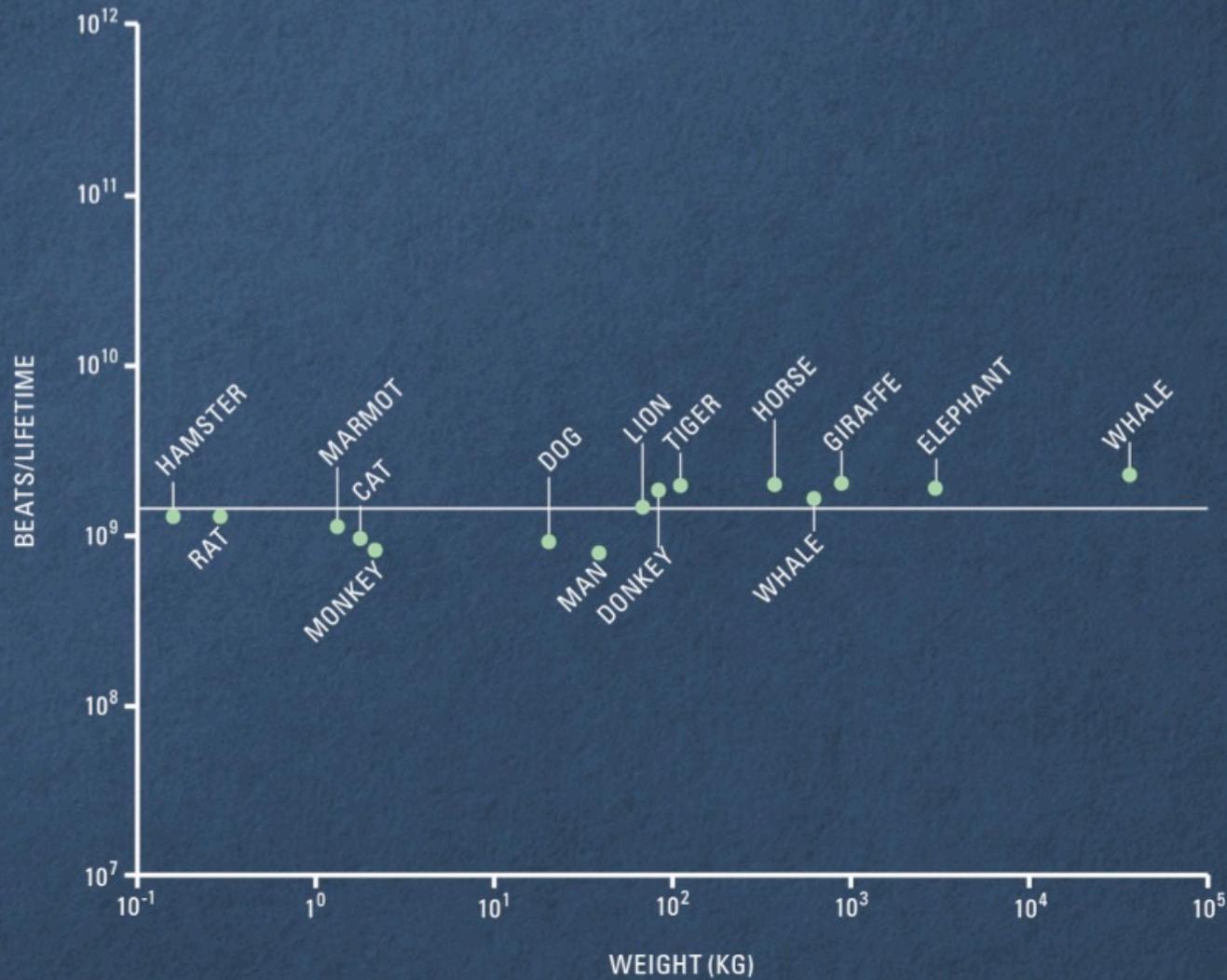
$$\approx 1.5 \times 10^9$$

EACH ANIMAL SPECIES REGARDLESS OF SIZE

HAS APPROXIMATELY THE SAME NUMBER OF HEART-

BEATS IN ITS LIFE-TIME (ROUGHLY 1 BILLION)

NUMBER OF HEARTBEATS PER LIFETIME OF ANIMALS



RECALL SPECIFIC METABOLIC RATE

$$\bar{B} = \frac{B}{M} \propto M^{-1/4}$$

⇒ TOTAL ENERGY NEEDED TO SUPPORT UNIT MASS OF AN ANIMAL DURING A LIFETIME IS THE SAME FOR ALL ANIMALS REGARDLESS OF SIZE :

$$\begin{aligned} E_{\text{TOT}} &\approx 1.2 \times 10^6 \text{ JOULES / gm} \\ &\approx 300 \text{ kcal / gm} \end{aligned}$$

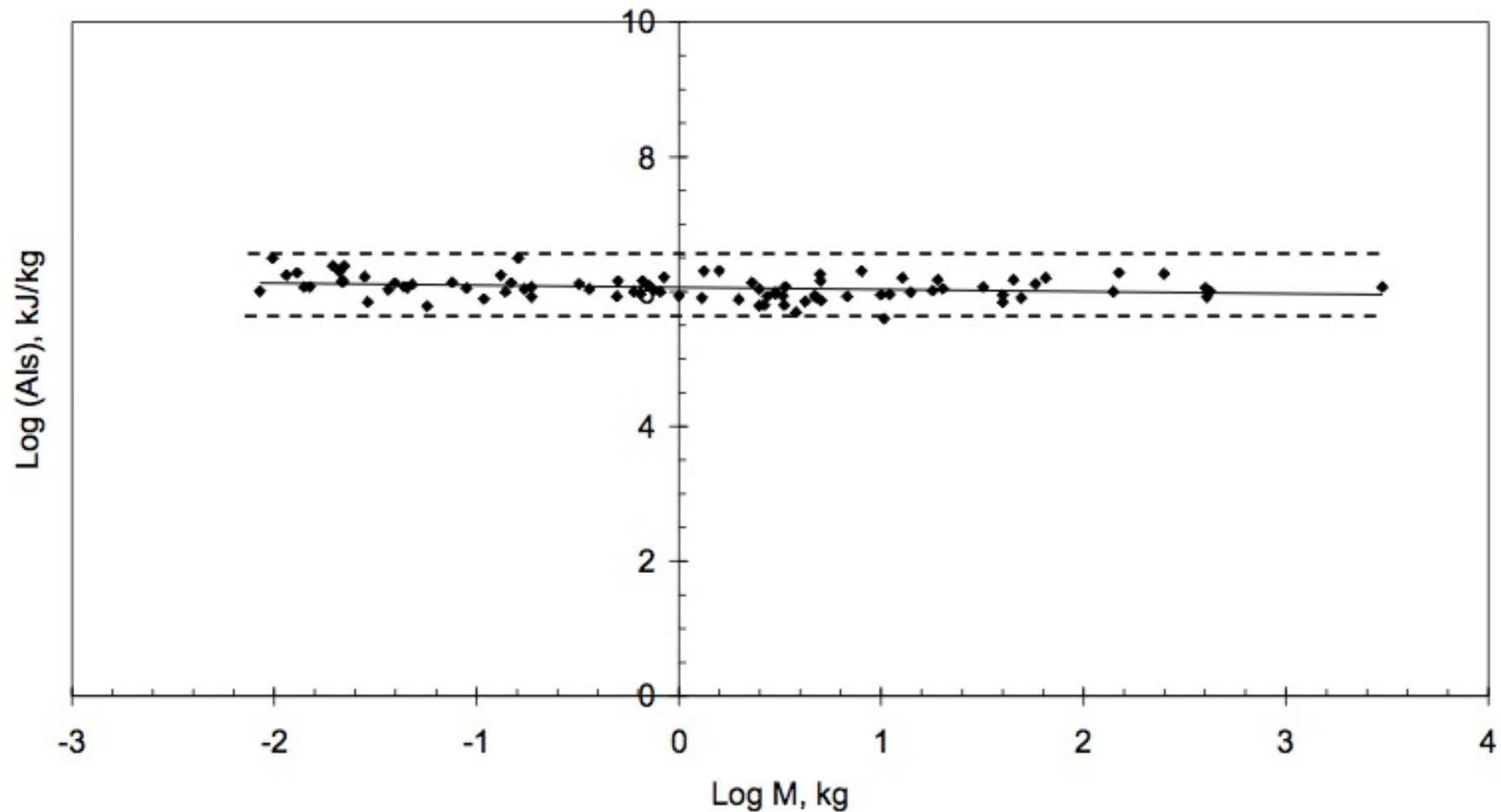


Fig. 2. Relationship between the total metabolic energy per life span per unit body mass ($A_{ls}=PT_{ls}/M$ kJ/kg) and the body mass (M , kg) for 86 terrestrial mammals in captivity (Prototheria, Metatheria and Eutheria). The 95% confidence limits are shown by dashed lines.

TEMPERATURE DEPENDENCE

METABOLIC RATE IS THE SUM OF ALL CONTRIBUTING REACTION SUB-PROCESSES (IN PARALLEL):

$$B = \sum_i P_i$$

$P_i \sim$ (CONCENTRATIONS) x (FLUXES) x (KINETICS)

(CONCENTRATIONS) x (FLUXES) \sim NETWORK $\sim M^{3/4}$

(KINETICS) \sim BOLTZMANN - ARRENIUS $\sim e^{-E/kT}$

**E = AVERAGE ACTIVATION ENERGY FOR RATE-LIMITING PROCESS IN RESPIRATORY COMPLEX
(PRODUCTION OF ATP) ~ 0.7 eV $\sim 2 \times 10^{-20}$ cal**

ALL RATES ~ $M^{-1/4}$

METABOLISM

GROWTH

EVOLUTION

LONGEVITY

DIFFUSION

FLUXES

.....

ALL TIMES ~ $M^{1/4}$

LIFESPANS

TURNOVER TIMES

TIMES TO MATURITY

CIRCULATION TIMES

.....

TEMPERATURE

REACTION RATES GOVERNED BY STATISTICAL PHYSICS (BOLTZMANN-ARRENIHUS)

ALL RATES ~ $M^{-1/4}e^{-E/kT}$ ALL TIMES ~ $M^{1/4}e^{E/kT}$

METABOLISM

GROWTH

EVOLUTION

LONGEVITY

DIFFUSION

FLUXES

.....

LIFESPANS

TURNOVER TIMES

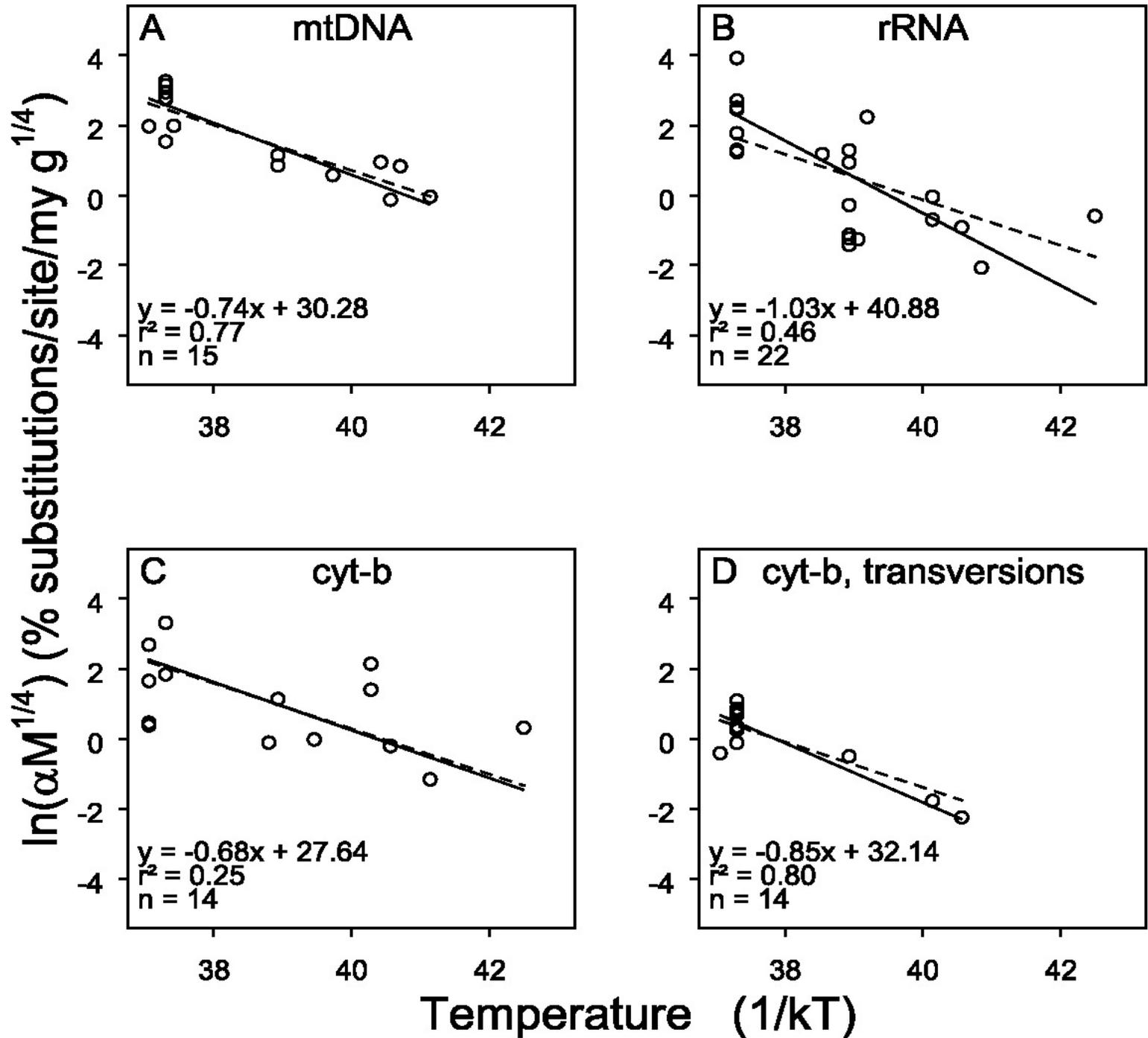
TIMES TO MATURITY

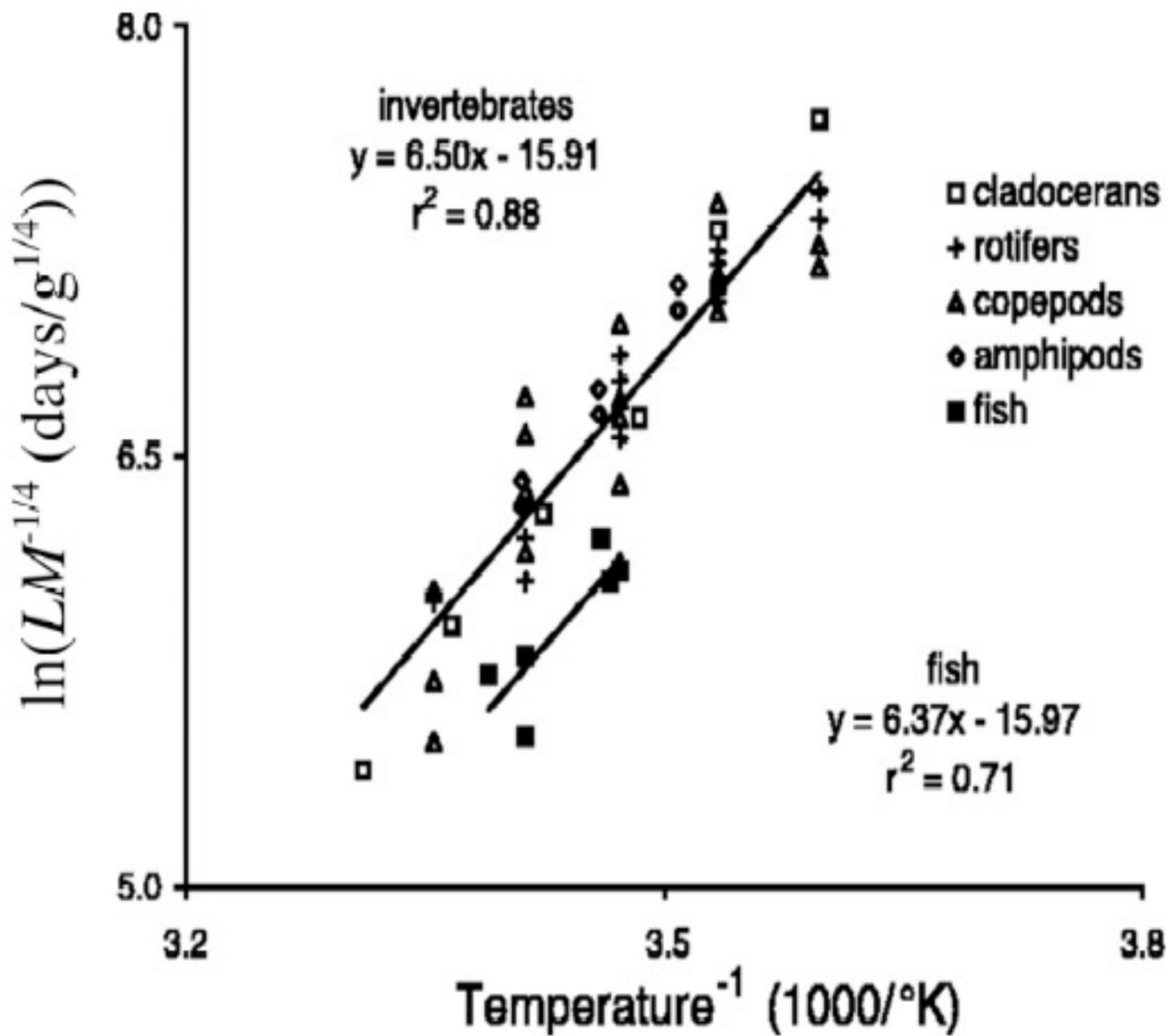
CIRCULATION TIMES

.....

Rates of molecular evolution

temperature
dependence





**MASS AND TEMPERATURE ARE THE MAJOR
DETERMINANTS OF THE MEASURABLE TRAITS OF
ORGANISMS ACROSS THE ENTIRE SPECTRUM OF LIFE**

GOVERNED BY JUST TWO PARAMETERS:

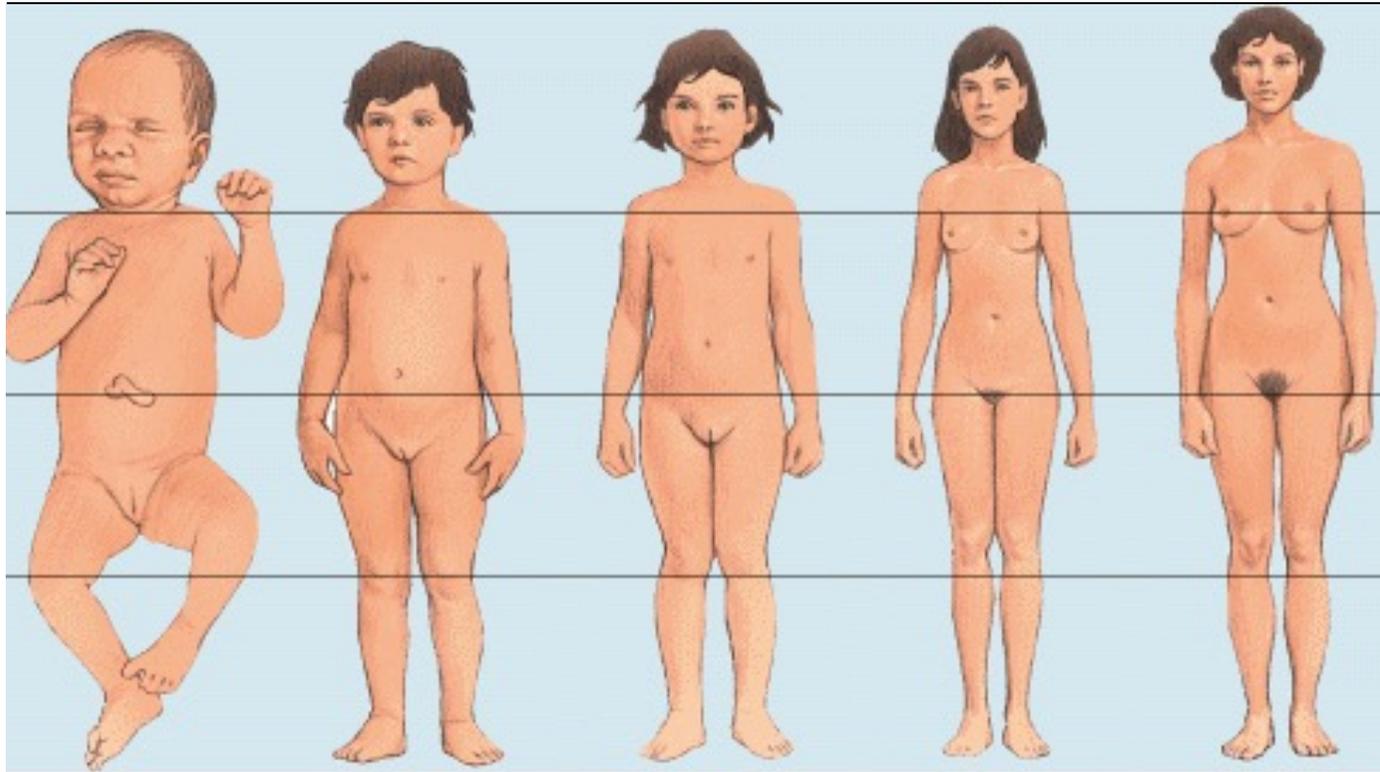
$1/4$ AND $E \sim 0.7$ eV

**IF THE MASS AND TEMPERATURE DEPENDENCIES ARE
ACCOUNTED FOR, OR COMPENSATED FOR, THEN:**

(TIMES) $\times M^{-1/4} e^{-E/kT}$

(RATES) $\times M^{1/4} e^{E/kT}$

**ARE INVARIANT, IMPLYING A “UNIVERSAL” RATE OF
LIVING, DYING, GROWING, REPRODUCING, EVOLVING,.....**



Newborn

2 years

5 years

15 years

Adult

GROWTH



Energy and human life



Chemical energy

- Carbohydrates
- Fats
- Others

Chemical waste

- Carbon dioxide
- Water

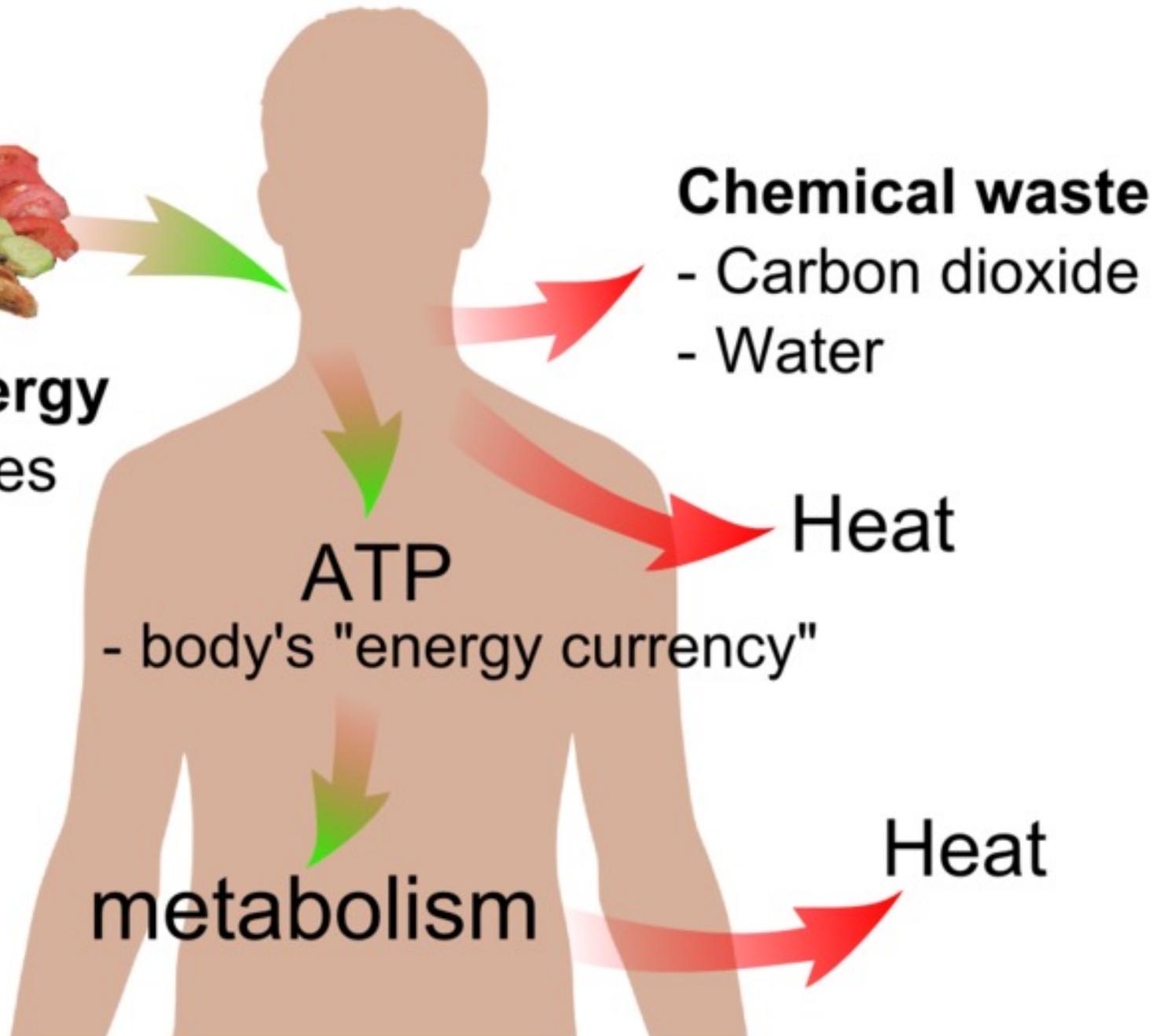
ATP

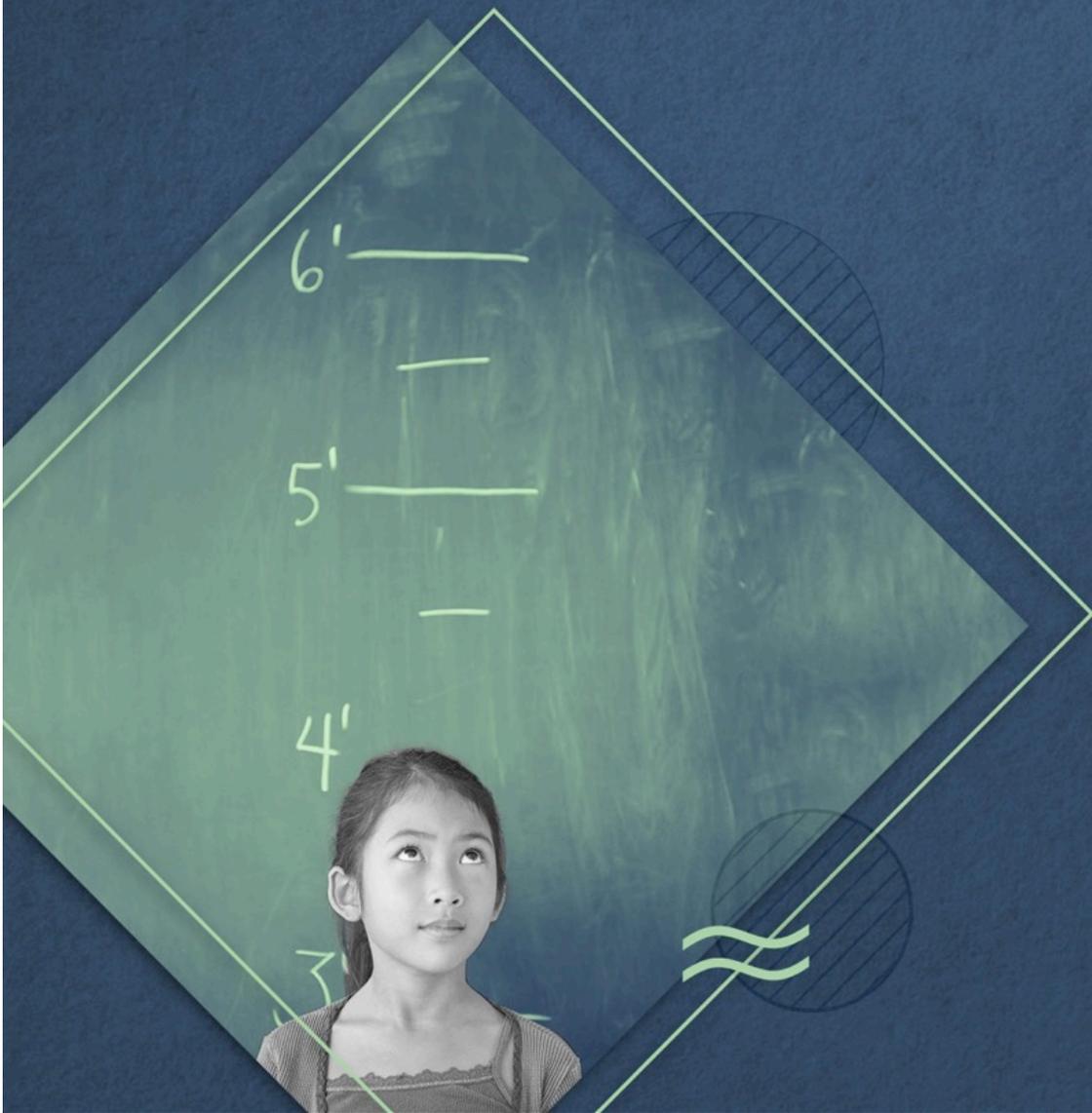
- body's "energy currency"

Heat

metabolism

Heat





Growth

Incoming
Metabolized Energy



Maintenance
(of Existing Cells)



New Growth
(of New Cells)

$$B = N_{cells} B_{cell} + E_{cell} \frac{dN_{cell}}{dt}$$

IN TERMS OF MASS AT AGE t

$$\Rightarrow \frac{dm}{dt} = am^{3/4} - bm$$

where
e

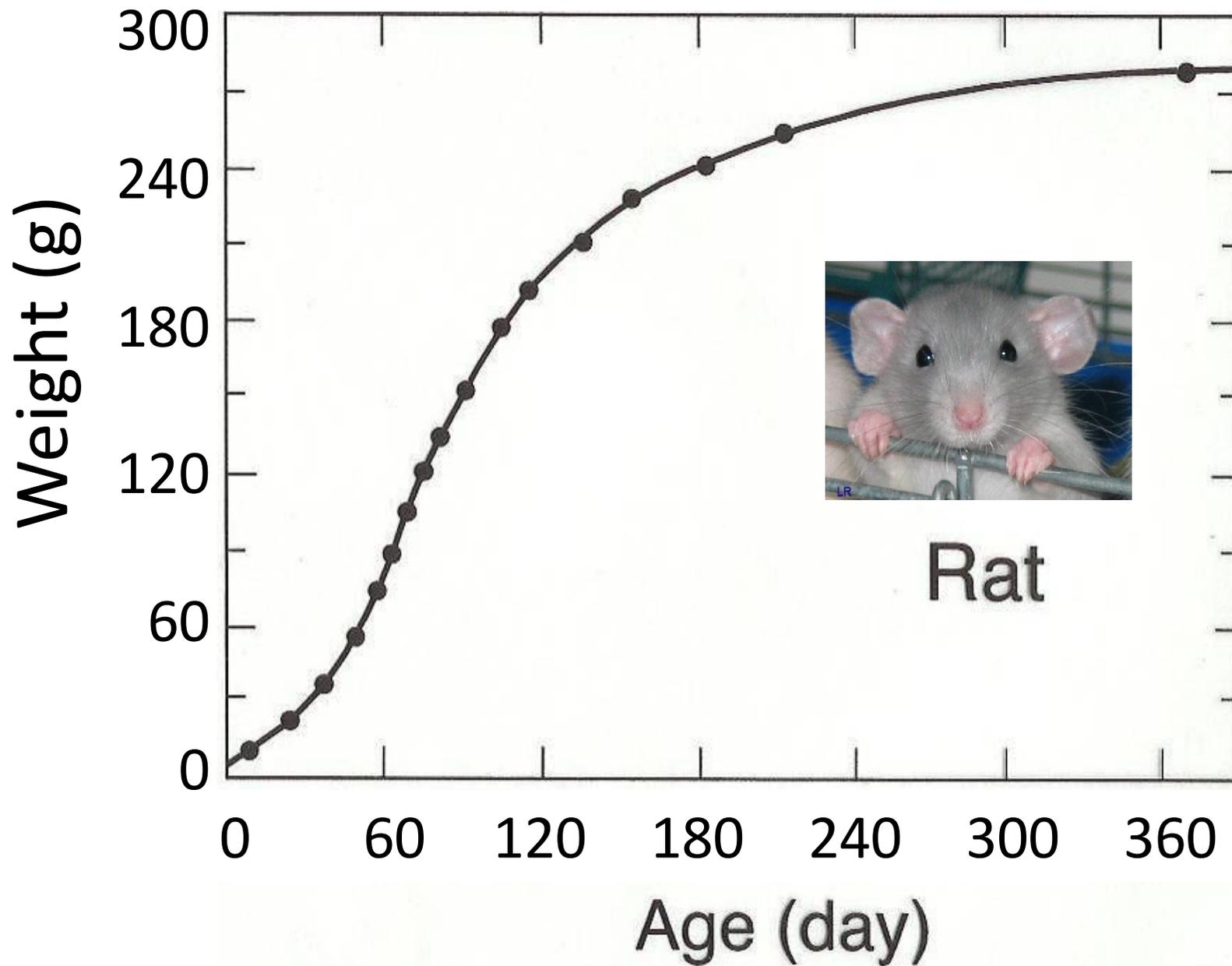
$$a \equiv \frac{B_0 m_c}{E_c}$$

$$b \equiv \frac{B_c}{E_c}$$

SOLUTION:

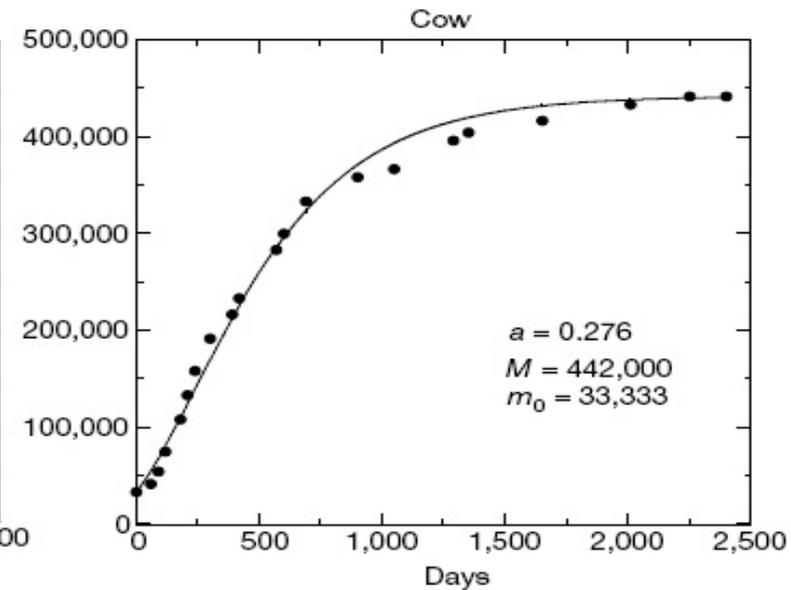
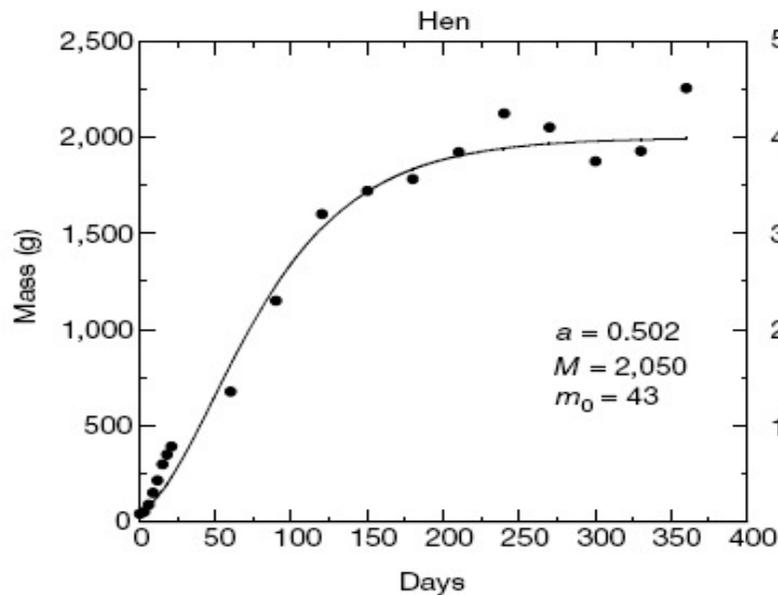
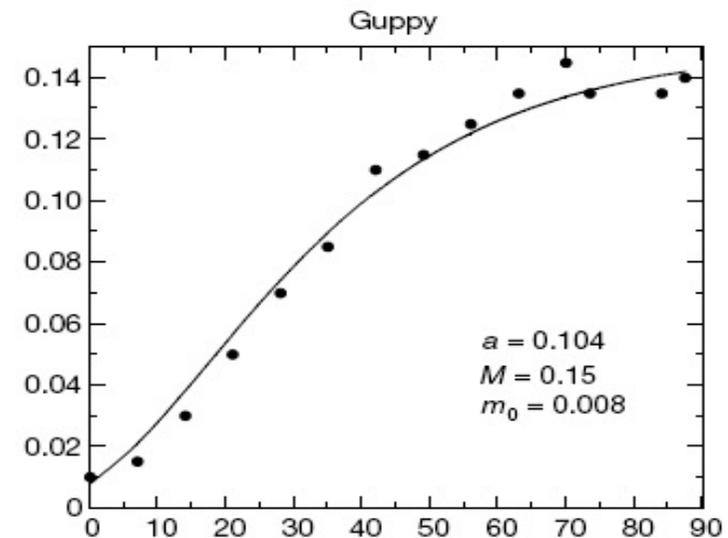
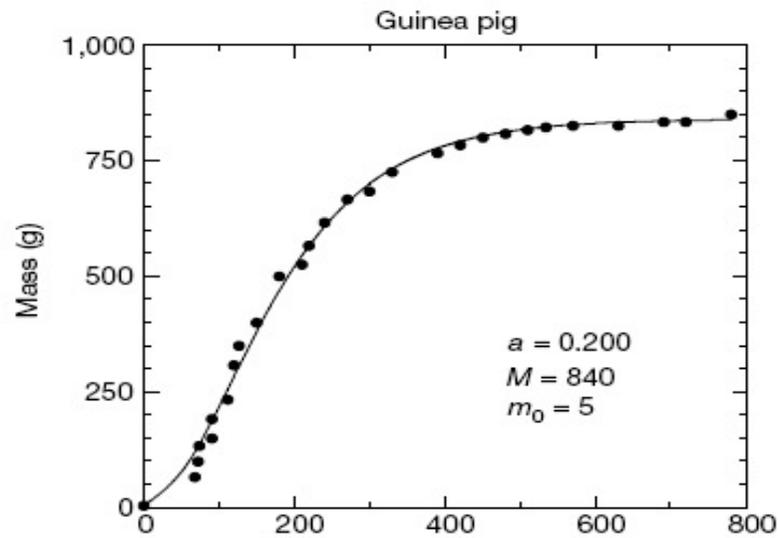
$$\left(\frac{m}{M}\right)^{1/4} = 1 - \left[1 - \left(\frac{m_0}{M}\right)^{1/4}\right] e^{-at/4M^{1/4}}$$

WHERE m_0 = MASS AT BIRTH ($m = m_0$ WHEN $t = 0$)



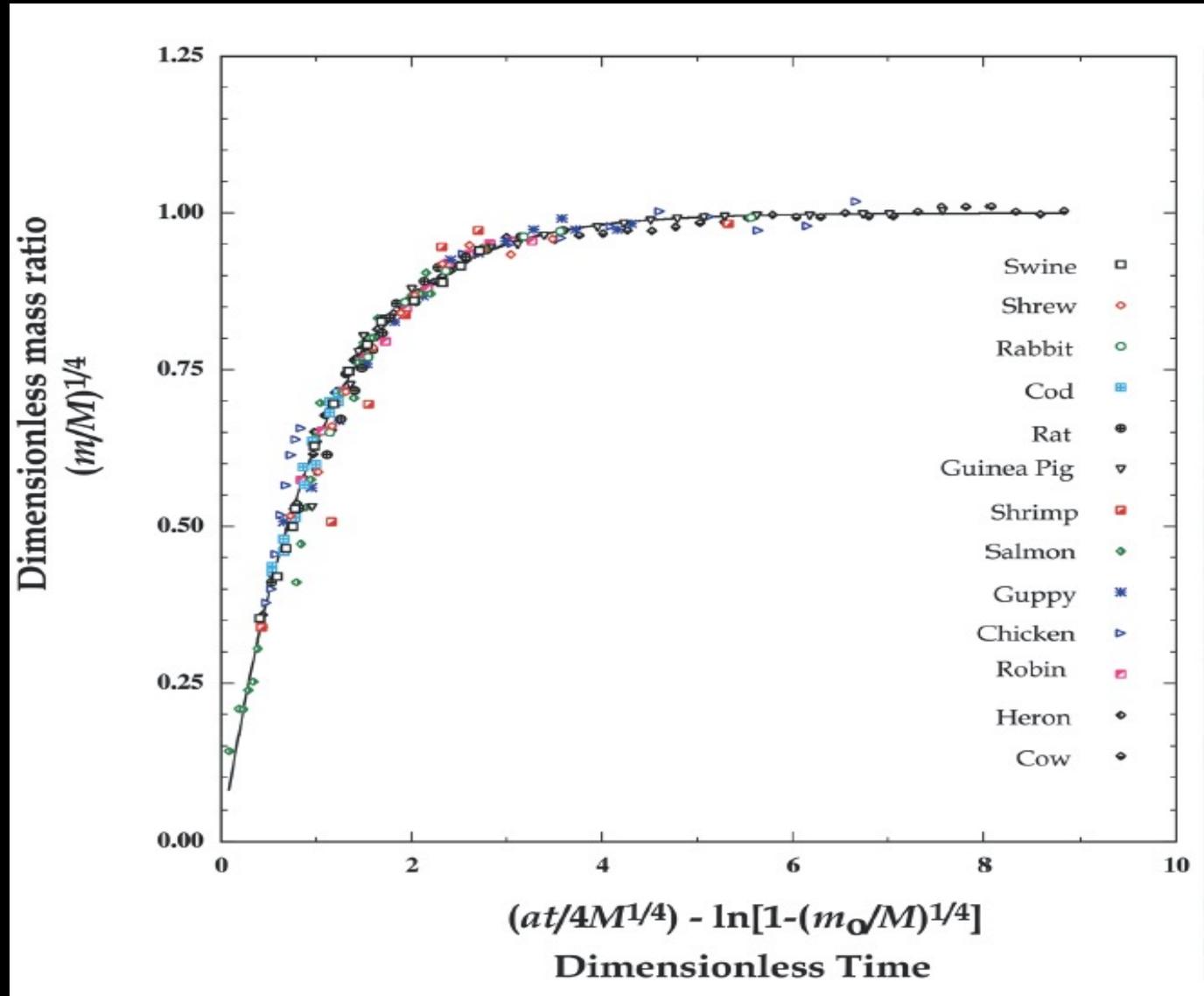
**SUB-LINEAR SCALING
LEADS TO BOUNDED GROWTH**

PREDICTED GROWTH CURVES OF ANIMALS



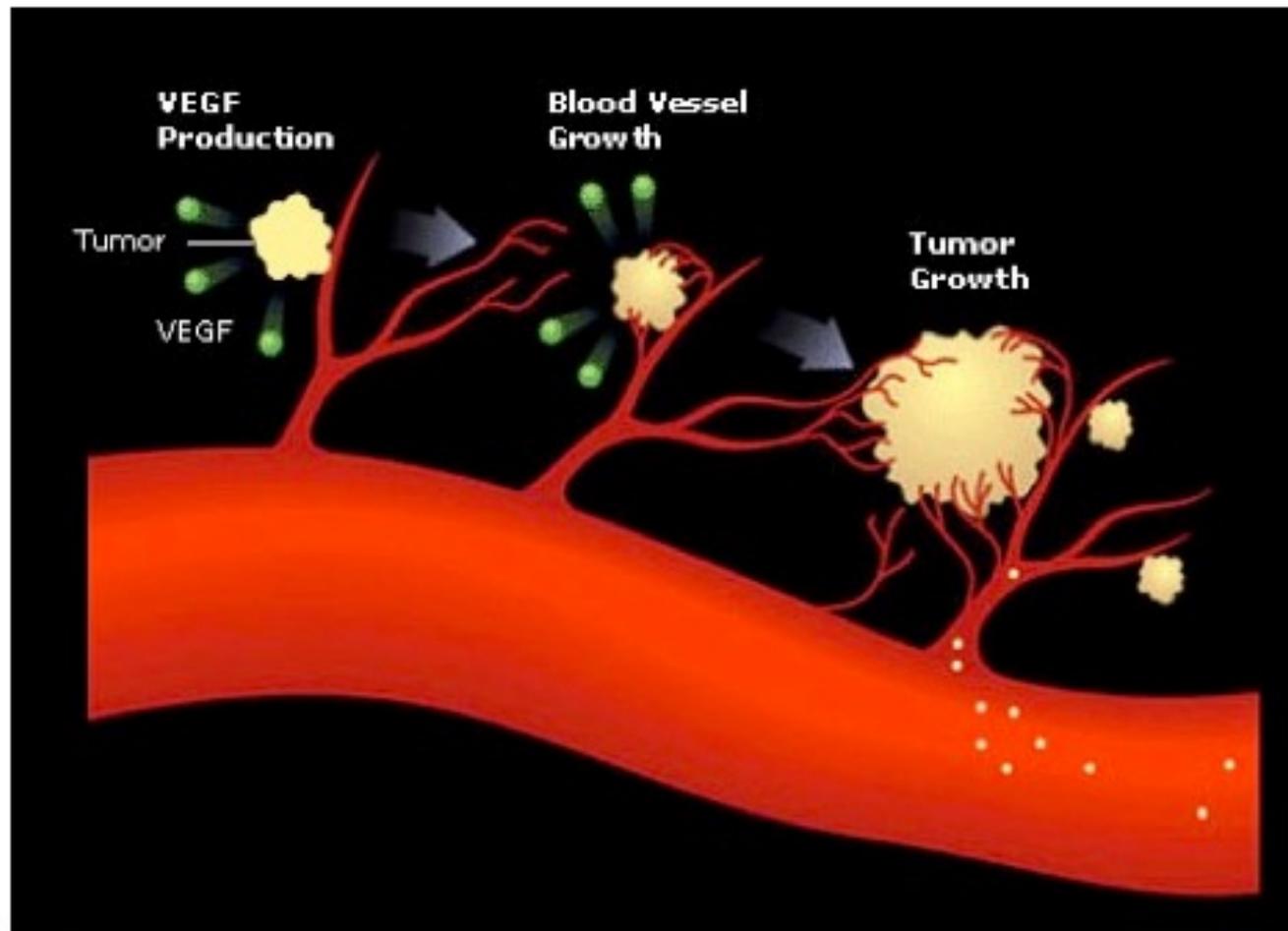
UNIVERSAL COLLAPSED GROWTH CURVE

RESCALED MASS VS. RESCALED AGE

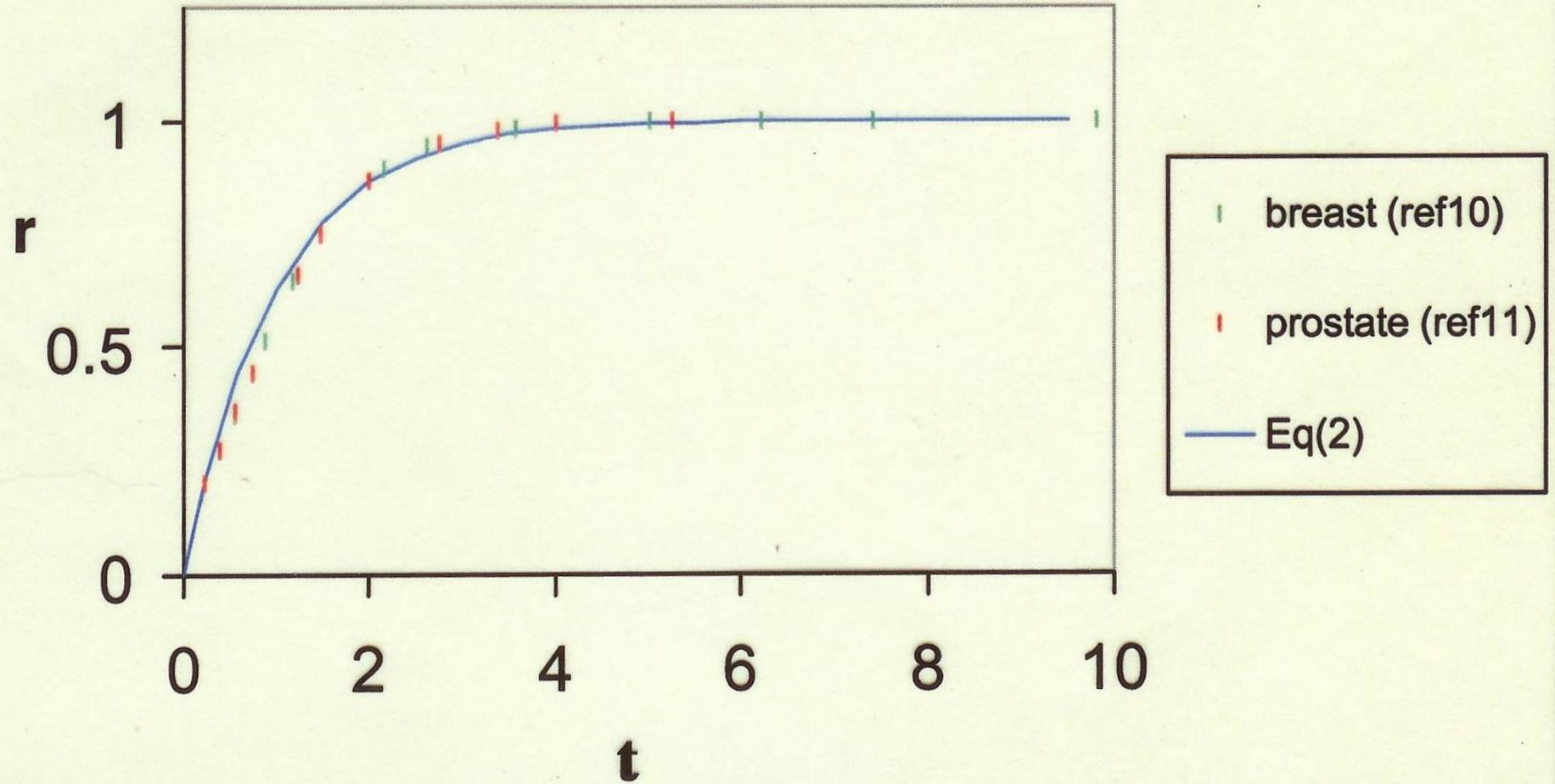


COUPLED NETWORK PROBLEM: TUMORS

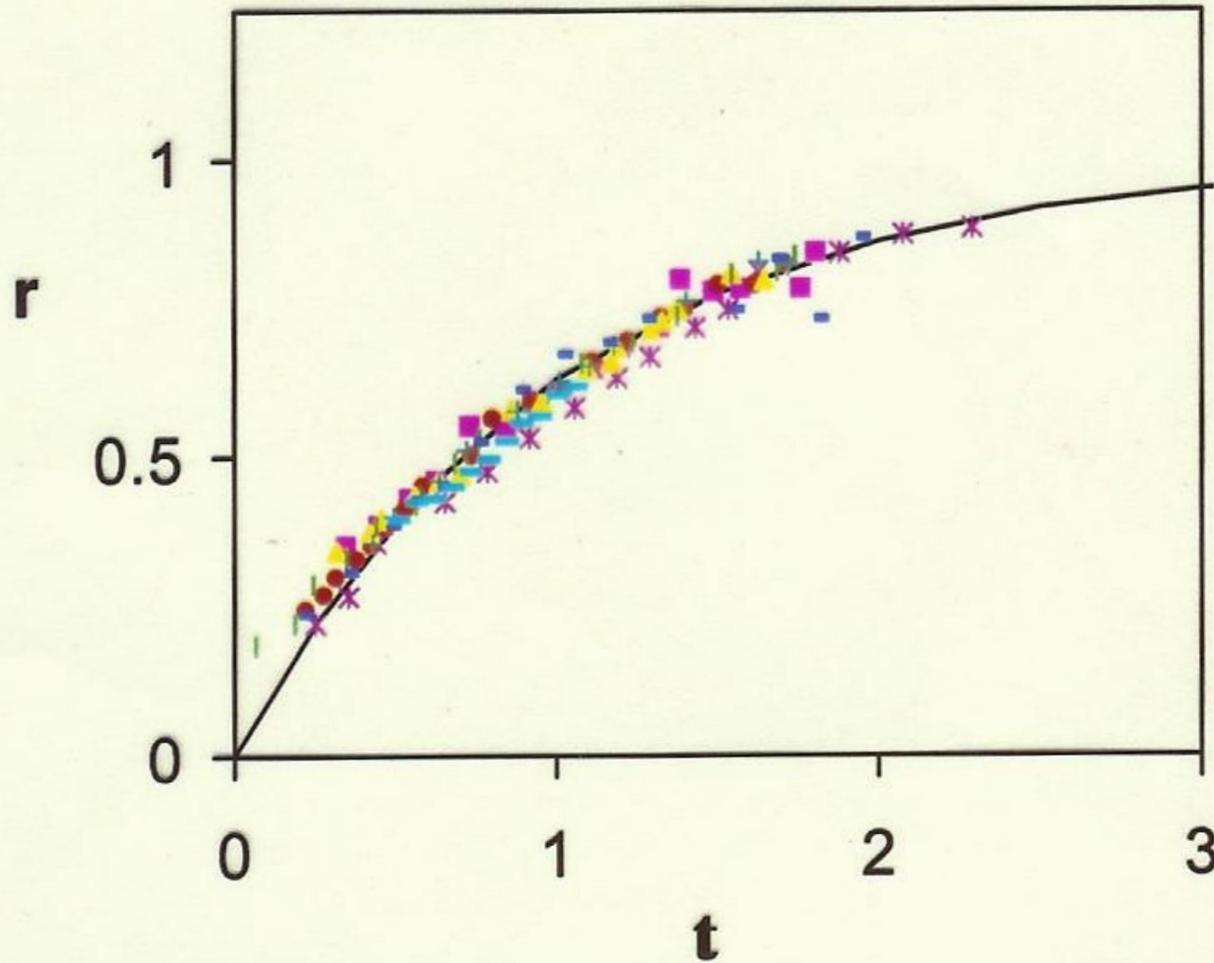
Pre- and post-angiogenesis



'in vivo' data (patients)



'in vivo' data (rodents)



■ Fibro (ref8)

* Walker (ref8)

● KHJJ (ref8)

▲ C3H (ref8)

┆ EMT6 (ref8)

+ NCTC2472 (ref8)

- Osteo (ref8)

- C33 ISS (ref9)

— Eq(2)

BIOLOGY (LIFE)

- a) **DOMINATED BY SYSTEMATIC, PREDICTABLE, NON-LINEAR (UNIVERSAL) SCALING LAWS**
- b) **ECONOMIES OF SCALE (THE BIGGER YOU ARE, THE LESS YOU NEED PER "CAPITA") - SUBLINEAR**
- c) **PACE OF LIFE SYSTEMATICALLY SLOWS WITH INCREASING SIZE**
- d) **GROWTH IS SIGMOIDAL REACHING A STABLE SIZE AT MATURITY**
- e) **FINITE LIFESPAN**

**ARE CITIES (AND COMPANIES)
SCALED VERSIONS OF EACH
OTHER?**

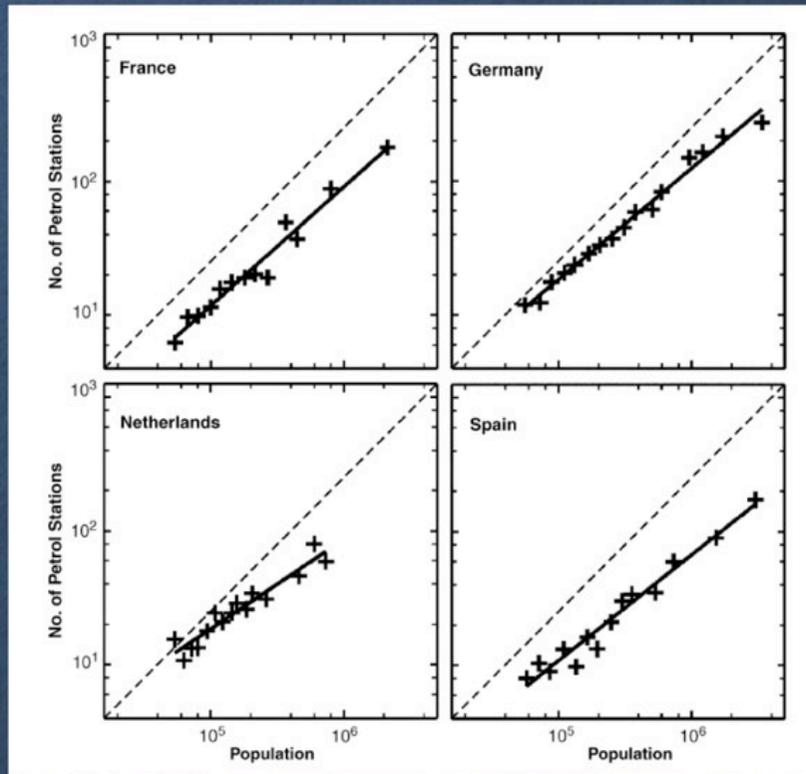
**DO THEY MANIFEST
“UNIVERSALITY”?**

HIDDEN LAWS OF BIOLOGY → HIDDEN LAWS OF CITIES



HIDDEN LAWS OF BIOLOGY → HIDDEN LAWS OF CITIES

NUMBER OF PETROL STATIONS VS. POPULATION

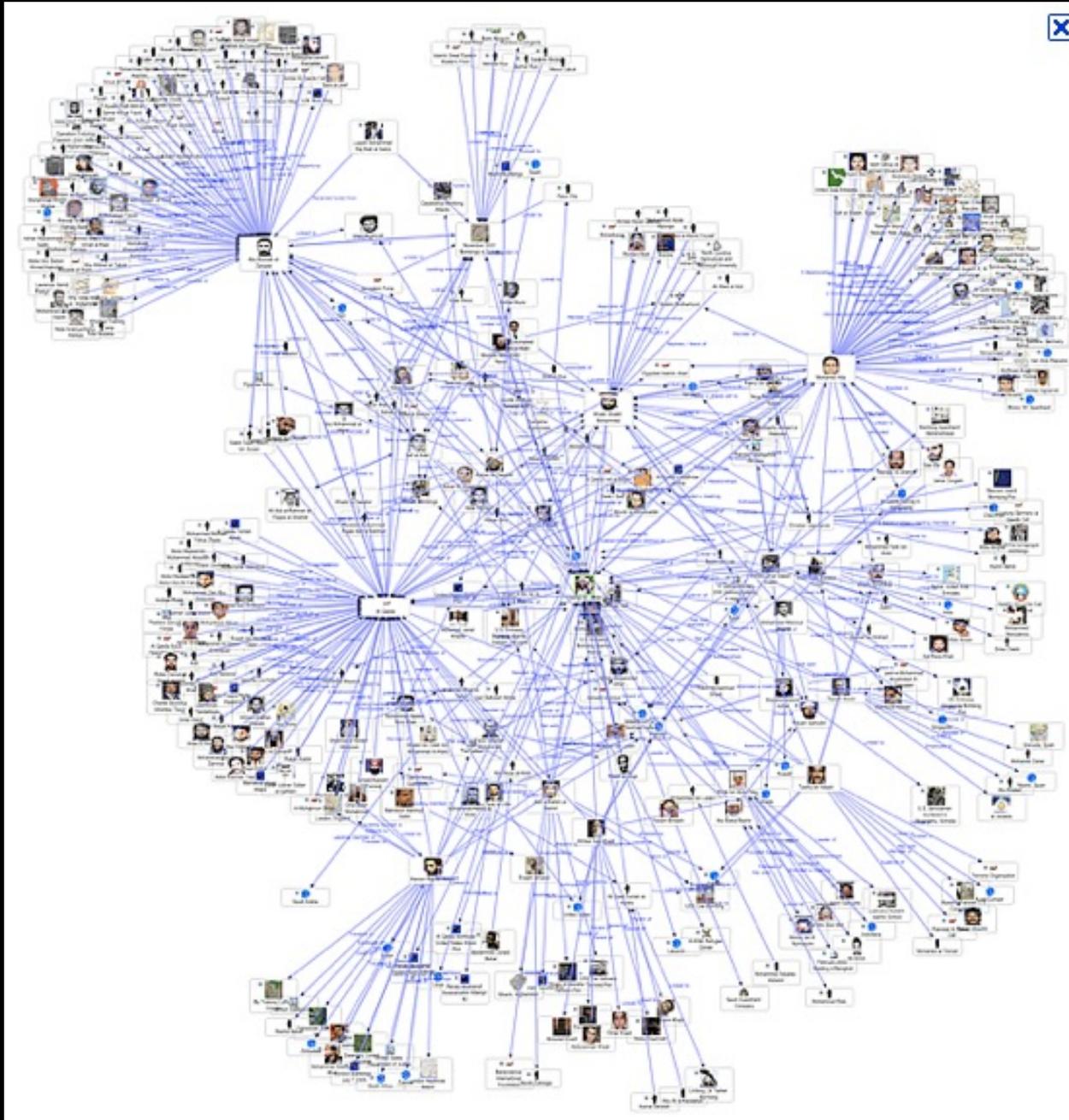


INFRASTRUCTURE

SUB-LINEAR SCALING

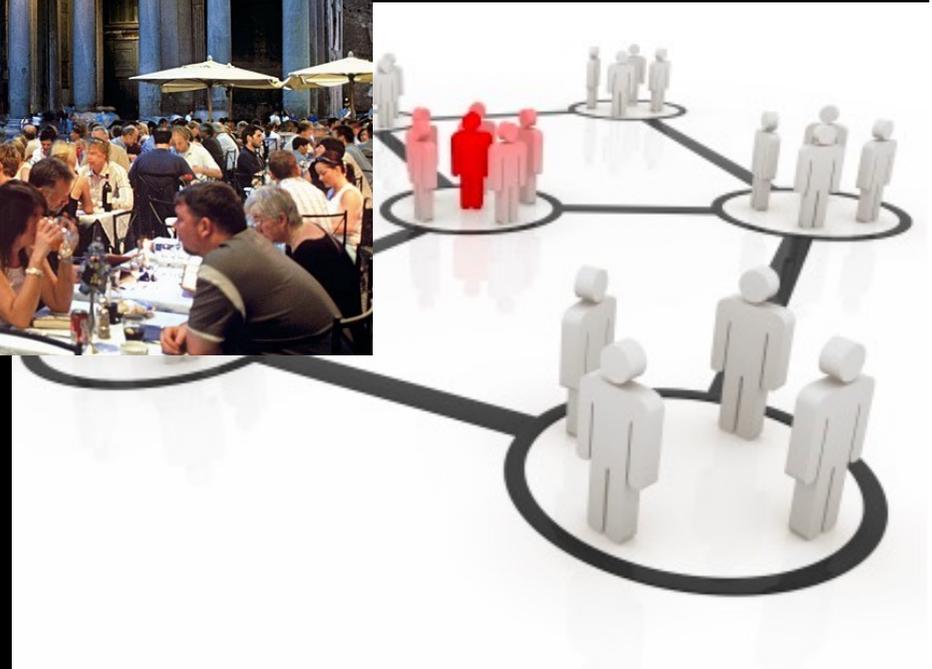
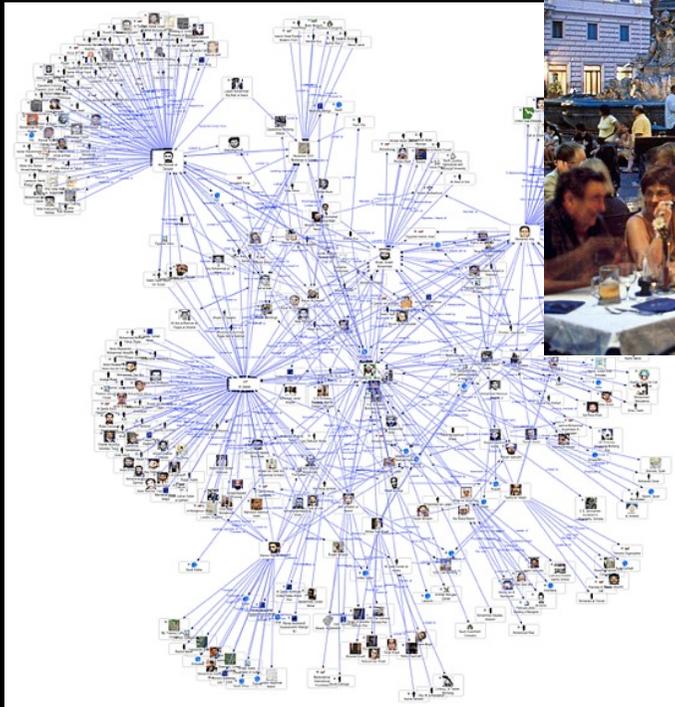
ECONOMY OF SCALE

SOCIAL NETWORKS

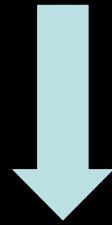


MODULARITY AND *PLACE*



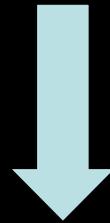


**POSITIVE FEEDBACK MECHANISM IN
SOCIAL NETWORKS**



SUPERLINEAR SCALING

POSITIVE FEEDBACK MECHANISM IN SOCIAL NETWORKS



**SUPERLINEAR SCALING
& INCREASING PACE OF LIFE**

L.M.A. Bettencourt, D. Helbing, C. Kuhnert, J. Lobo, G.B. West PNAS, 2007
L. M. A. Bettencourt & G. B. West *Nature* 2010
L. M. A. Bettencourt *Science* 2017

NETWORK “PRINCIPLES”

i) SOCIO-ECONOMIC SYSTEMS ARE SUSTAINED BY THE TRANSPORT OF ENERGY, RESOURCES AND INFORMATION THROUGH (HIERARCHICAL) BRANCHING NETWORKS IN ORDER TO SUPPLY AND SUSTAIN ALL LOCAL PARTS OF THE SYSTEM (PEOPLE, BUILDINGS, BUSINESSES,...)

ii) NETWORKS ARE SPACE-FILLING

iii) TERMINAL UNITS ARE INVARIANT

iv) EVOLVED TO (JOINTLY) MINIMISE TRAVEL TIME AND DISTANCE AND MAXIMISE SOCIAL INTERACTION VIA EXCHANGE OF INFORMATION TO CREATE “WEALTH” AND “INNOVATE”

v) UNIVERSALITY OF HIERARCHICAL MODULAR STRUCTURES

**WITHIN SOCIO-ECONOMIC ORGANISATIONS
THESE LEAD TO FRACTAL-LIKE STRUCTURES
AND FLOWS**

**AND TO (APPROXIMATE) POWER LAW SCALING
ACROSS ORGANISATIONS:**

$$Y(N) \propto N^b$$

***SOCIO-ECONOMIC QUANTITIES DEPEND ON
“TWO-BODY” INTERACTIONS (INFORMATION
EXCHANGE) AND THEREFORE THE NUMBER
AND DENSITY OF SOCIAL INTERACTIONS:***

$$Y(N) \propto N_{\text{int}}$$

THE CONSTRAINTS AND DYNAMICS OF SOCIAL & INFRASTRUCTURAL NETWORKS (AND THE DATA!) LEAD TO

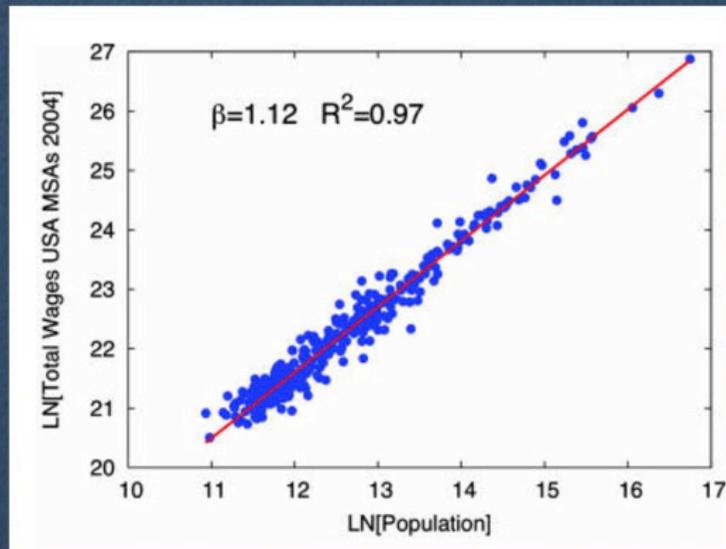
$$N_{\text{int}} \sim N^{1.15}$$

SO, FOR THE AVERAGE INDIVIDUAL, THE NUMBER OF INTERACTIONS $\sim N^{0.15}$

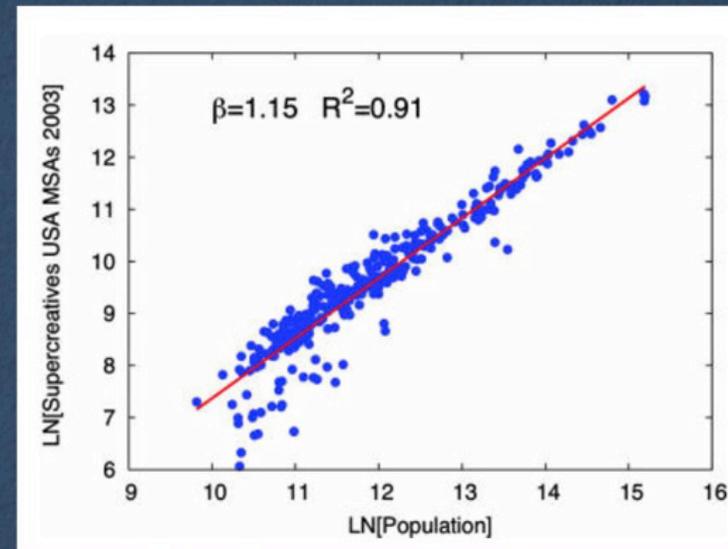
CONSEQUENTLY,

$$Y(N) \propto N_{\text{int}} \propto N^{1.15}$$

SUPER-LINEAR SCALING

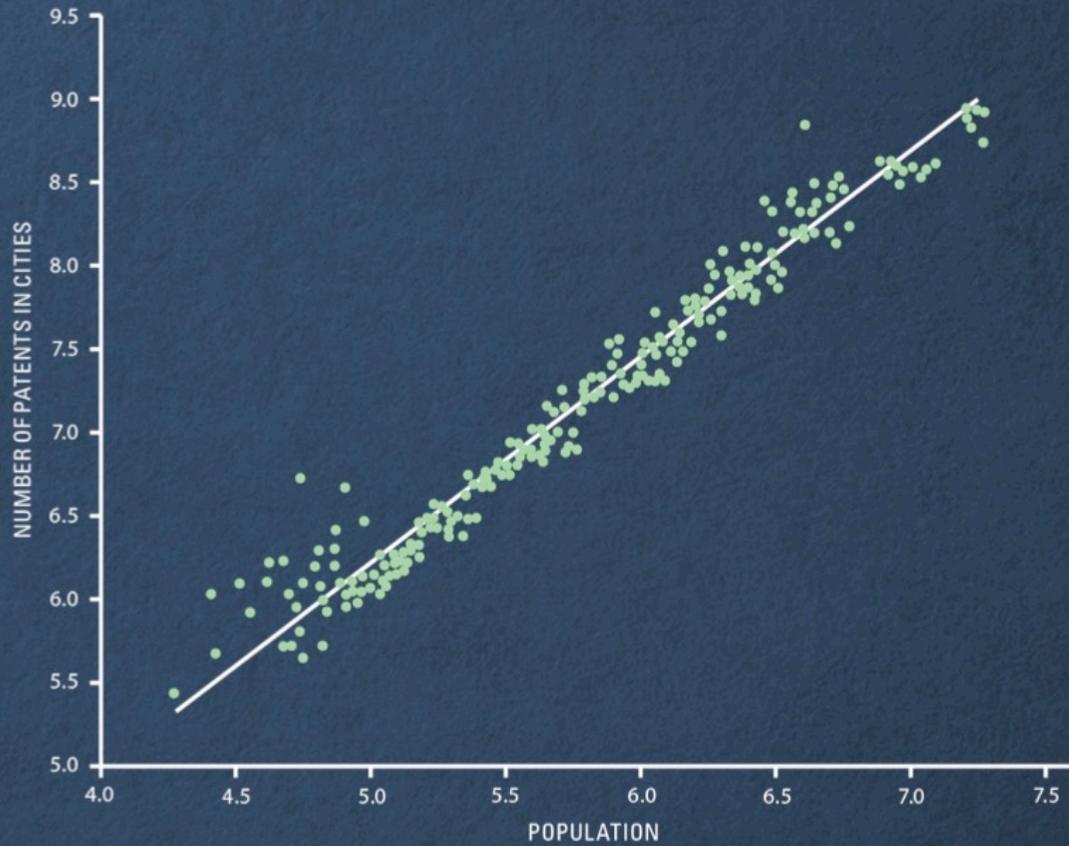


Total wages per MSA in 2004 for the USA vs. metropolitan population.

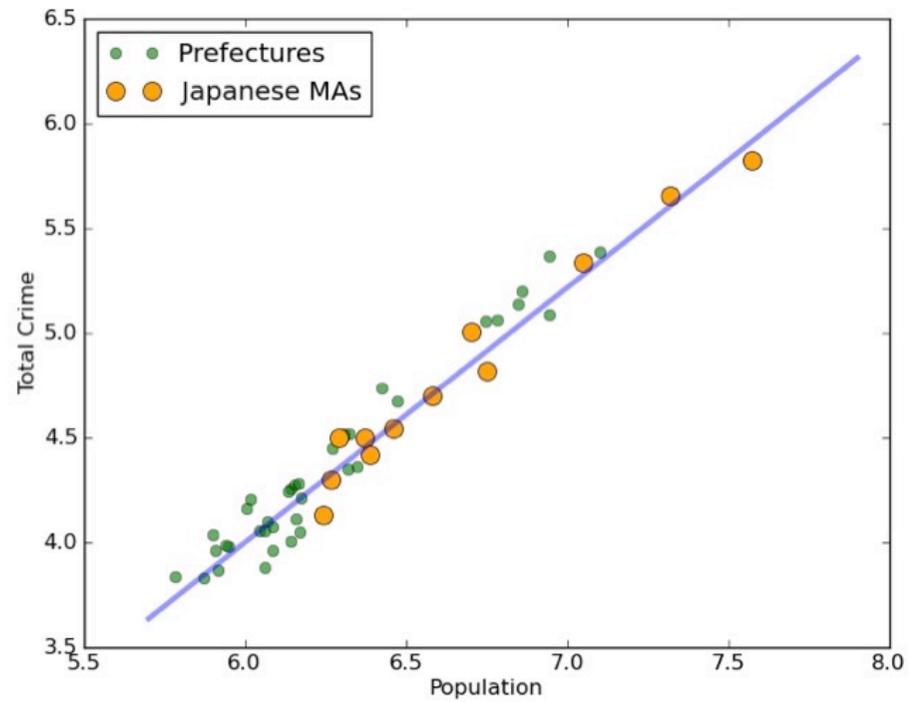


Supercreative employment per MSA in 2003, for the USA vs. metropolitan population.

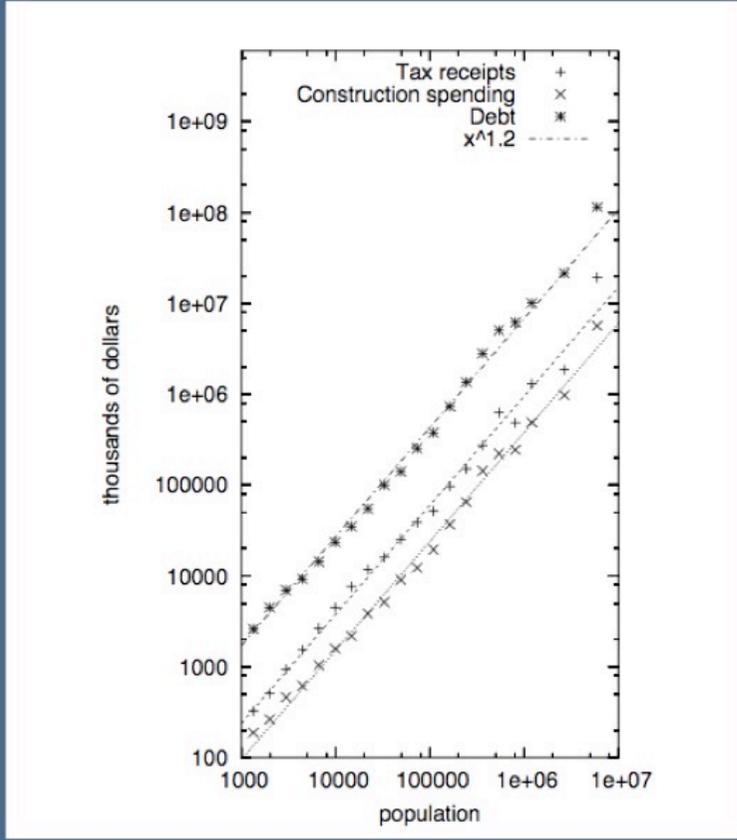
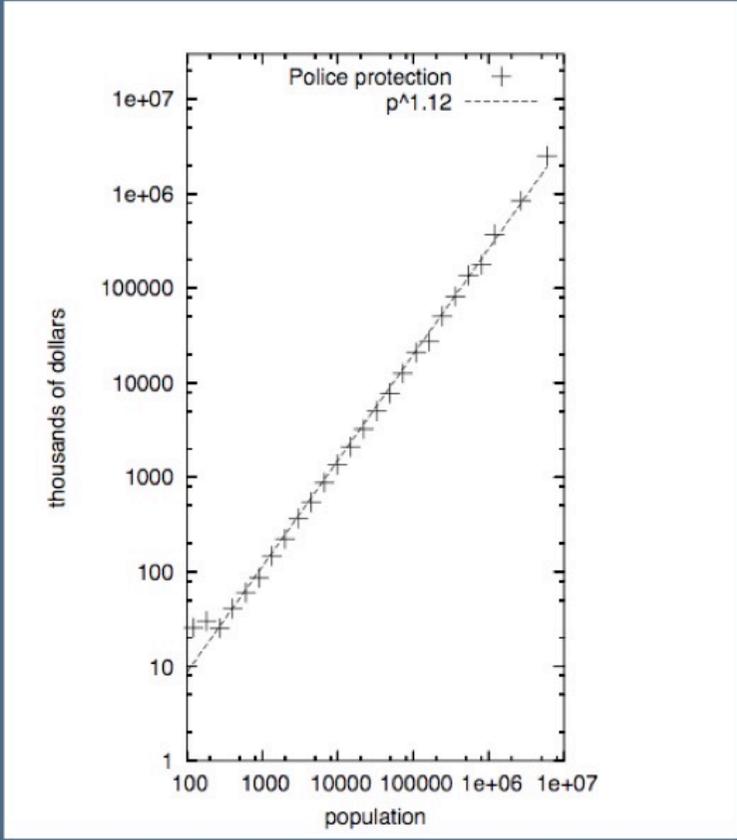
INNOVATION MEASURED BY PATENTS



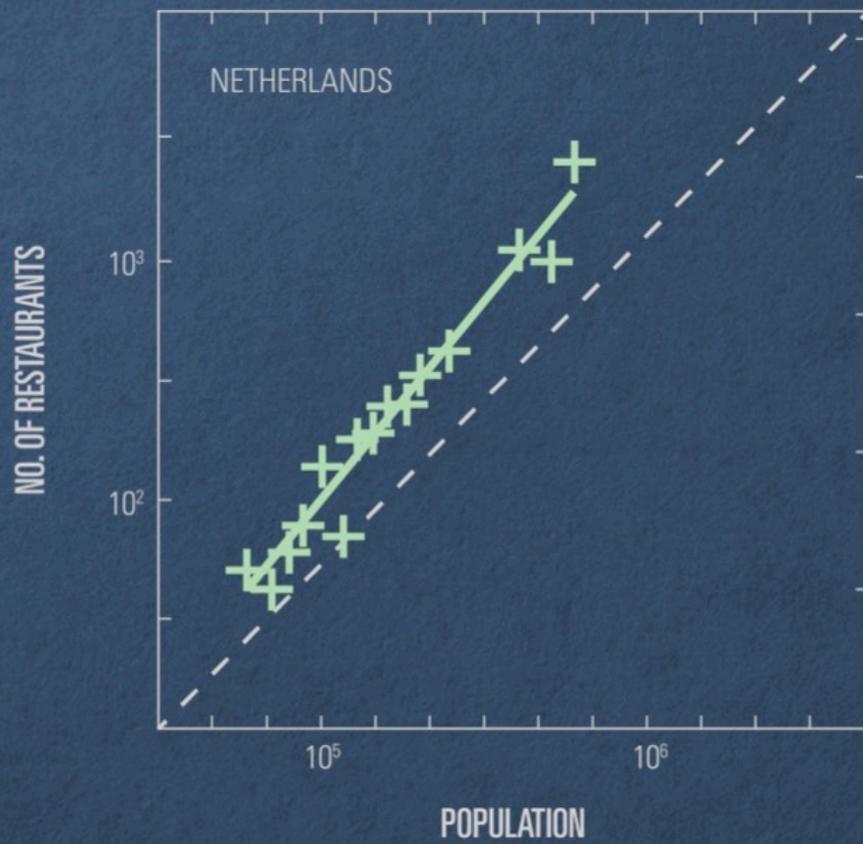
TOTAL CRIME (JAPAN)

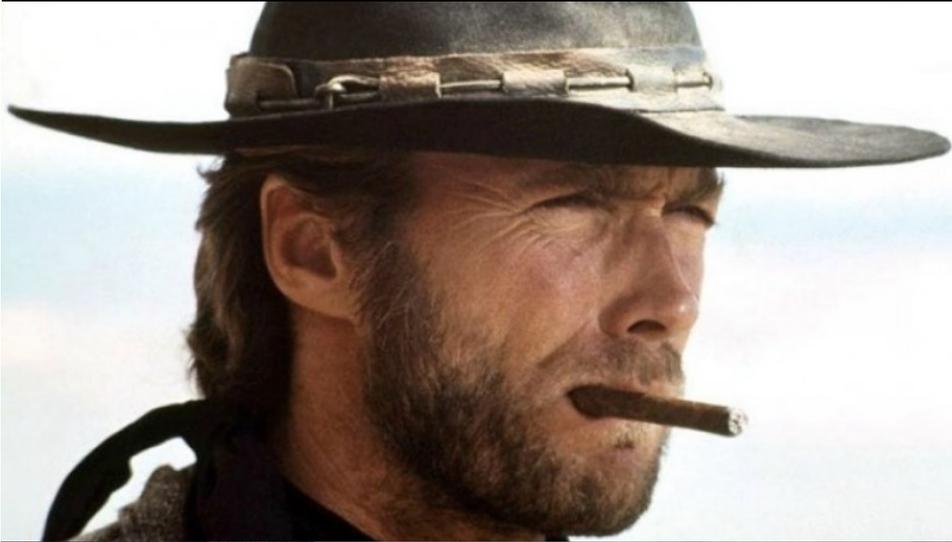


Slope = 1.21 [1.08, 1.35]



RESTAURANTS IN THE NETHERLANDS





**THE GOOD,
THE BAD,
THE UGLY**

**ON AVERAGE DOUBLING THE SIZE OF
A CITY SYSTEMATICALLY**

**ON AVERAGE DOUBLING THE SIZE OF
A CITY SYSTEMATICALLY**

***SAVES APPROXIMATELY 15% ON ALL
INFRASTRUCTURE***

***(ROADS, ELECTRICAL LINES, GAS
STATIONS,.....)***

**ON AVERAGE DOUBLING THE SIZE OF
A CITY SYSTEMATICALLY**

***SAVES APPROXIMATELY 15% ON ALL
INFRASTRUCTURE***

***(ROADS, ELECTRICAL LINES, GAS
STATIONS,.....)***

AND

INCREASES

**INCOME, WEALTH, PATENTS,
COLLEGES, CREATIVE PEOPLE,
POLICE, CRIME, SOCIAL
INTERACTIONS, AIDS, FLU,
AND**

INCREASES

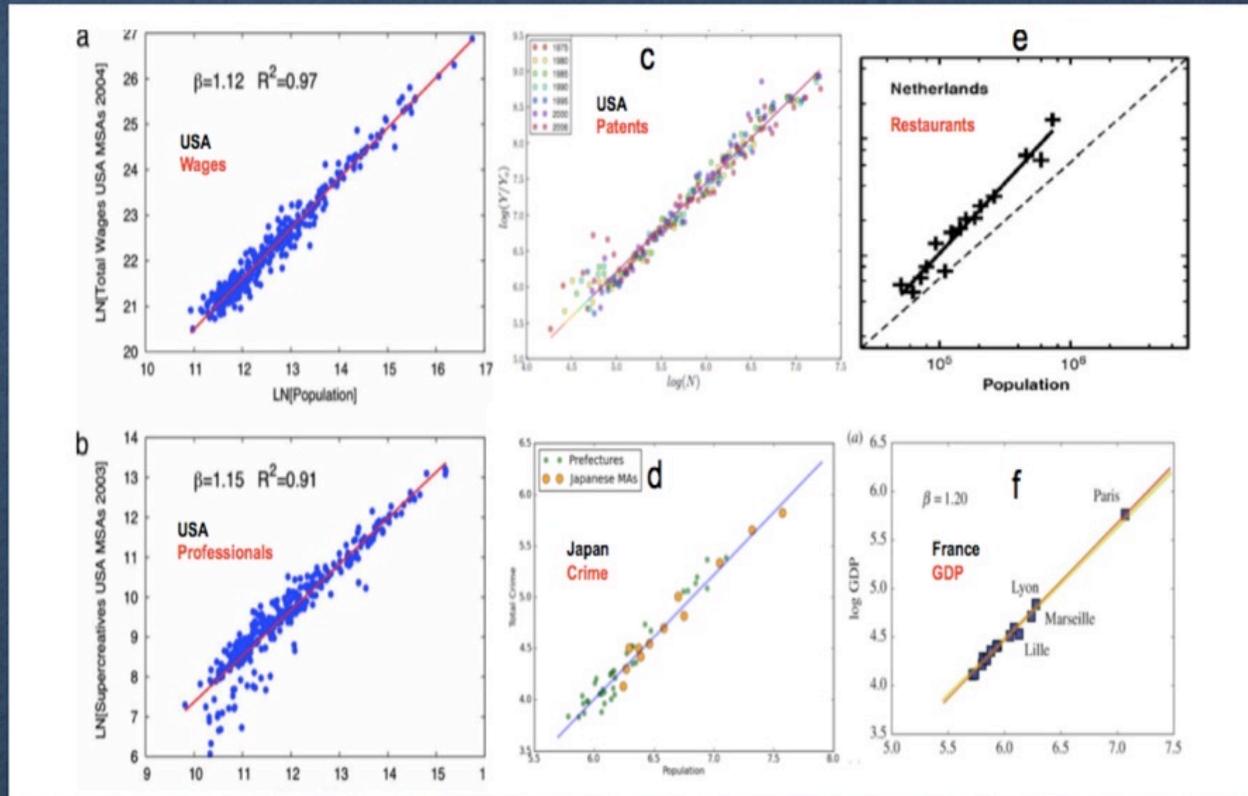
**INCOME, WEALTH, PATENTS,
COLLEGES, CREATIVE PEOPLE,
POLICE, CRIME, SOCIAL
INTERACTIONS, AIDS, FLU,
AND**

COVID-19

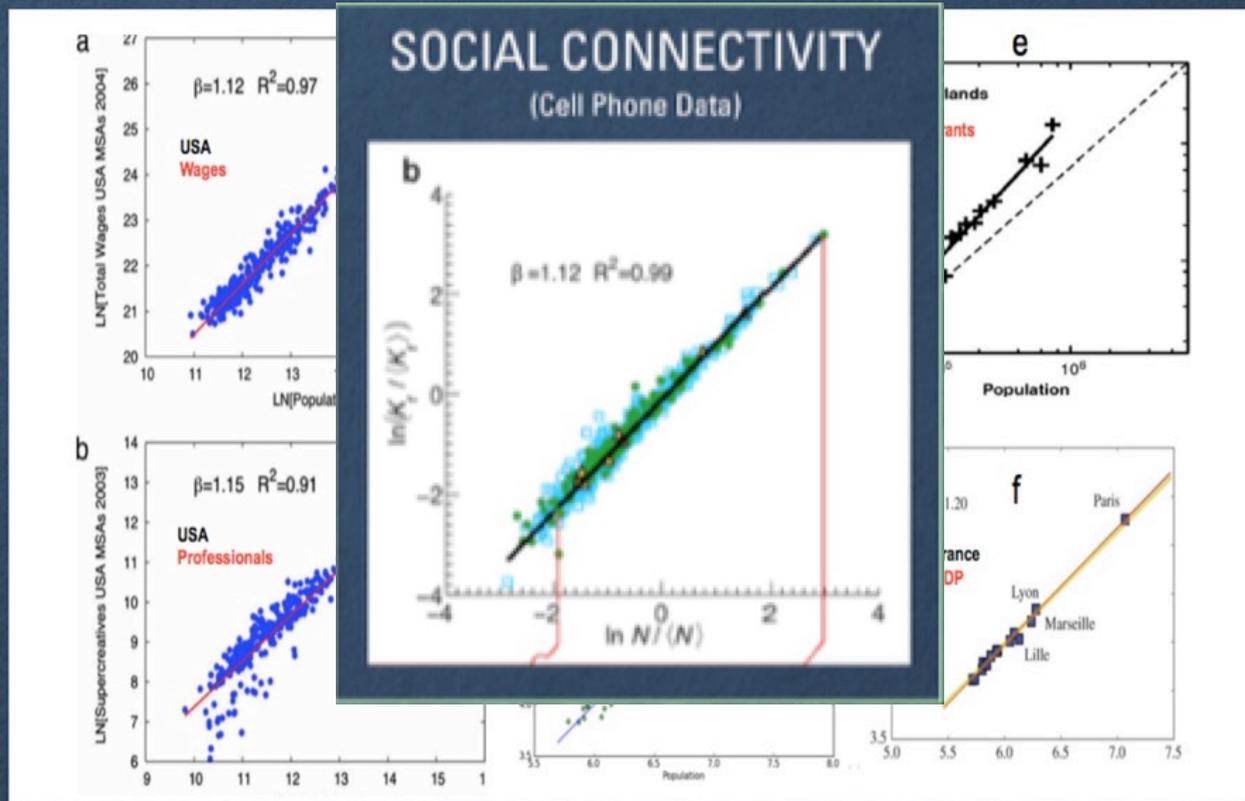
ALL BY ABOUT 15%

***A CITY OF 10 MILLION WILL HAVE DOUBLE
THE NUMBER OF COVID CASES IN HALF
THE TIME A CITY OF 100,000 WILL.....
AND HAVE ~ 200 TIMES AS MANY CASES***

UNIVERSALITY OF URBAN SCALING



UNIVERSALITY OF URBAN SCALING

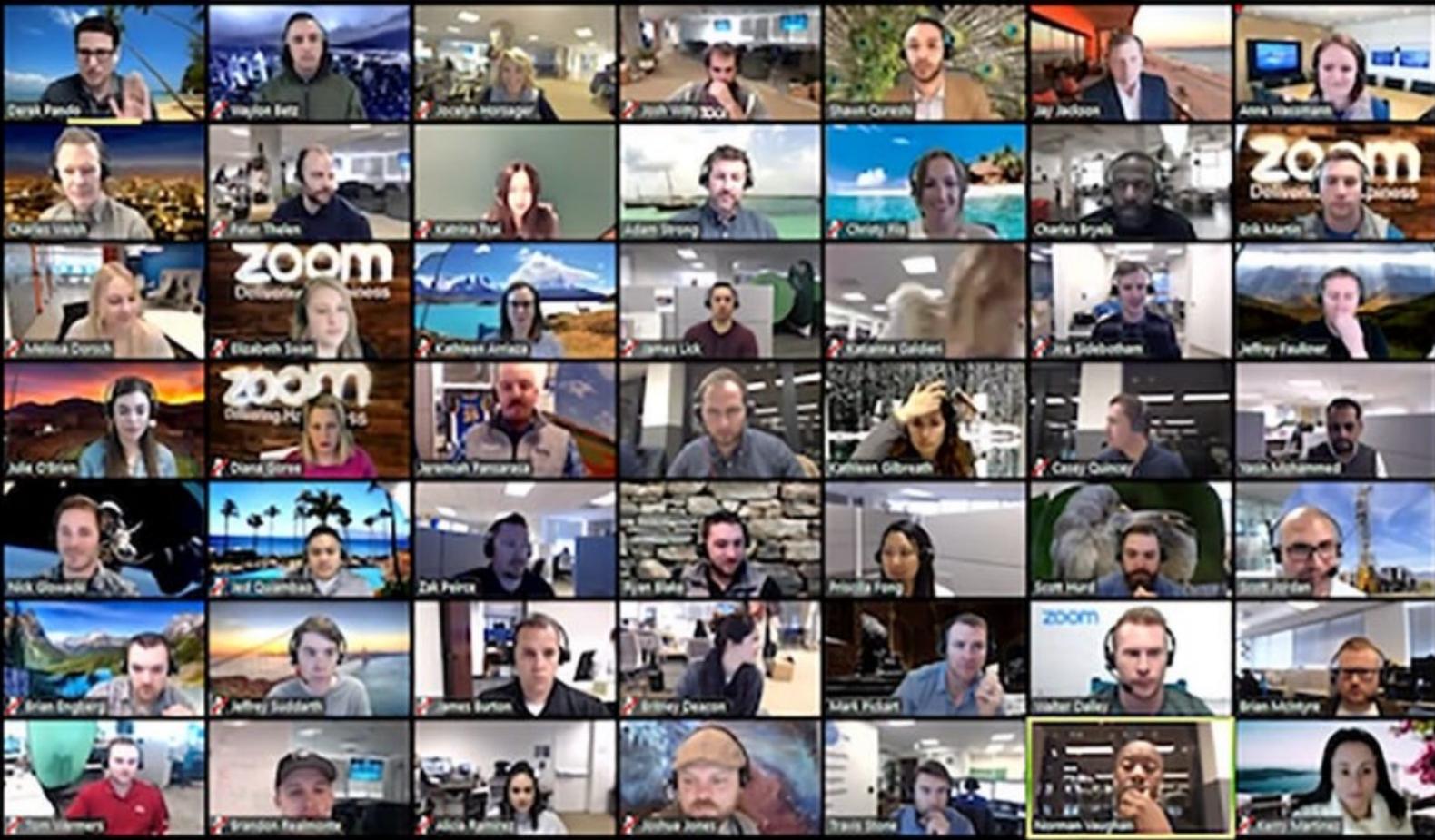


?

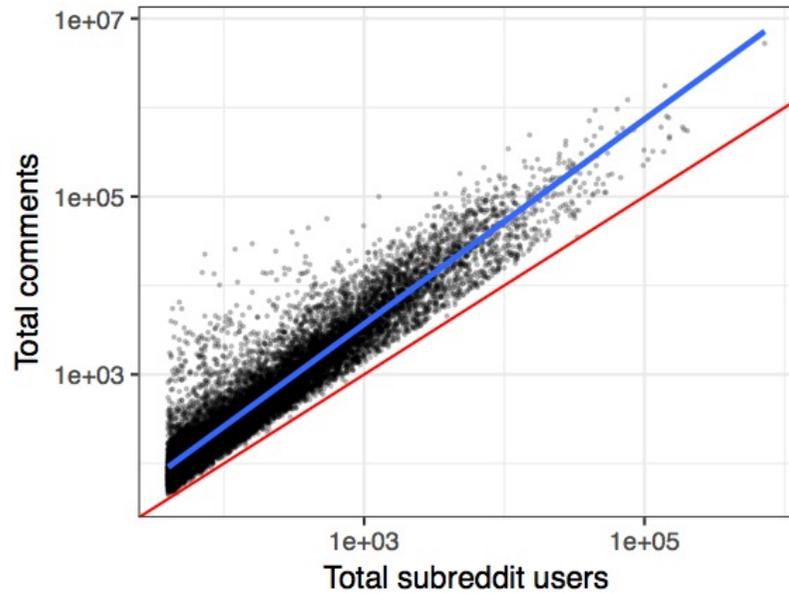
Turn on Original Sound

Total users in this meeting: 32

00:00:29 Speaker View

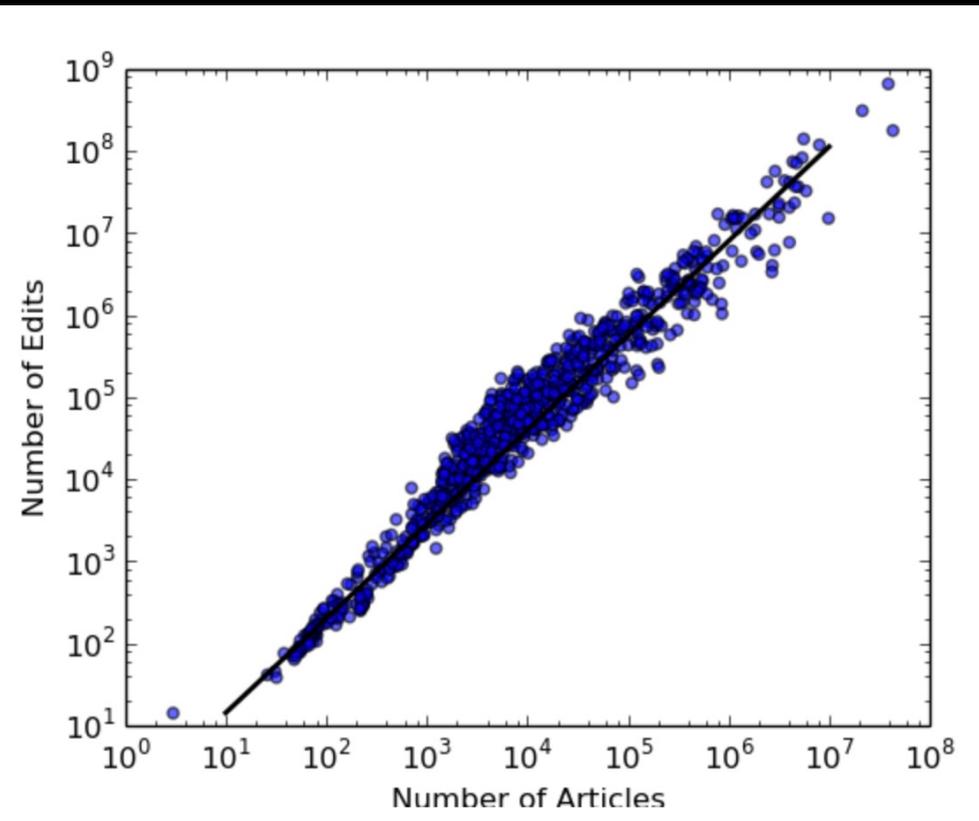


Leave Meeting



SUBREDDIT

BOTH HAVE SLOPE ~ 1.15



WIKIPEDIA

Growth

Incoming “Social Metabolic Rate”

(Resources, Products, Patents, “Energy” or
“Dollar” equivalent)

≈ **Maintenance** (Repair, Replacement,
Sustenance of Infrastructure, People, Institutions,
Companies ...)

+

New Growth (of Infrastructure, People,
Institutions, Companies ...)

$$R = \sum_{i=1}^n Y_i(N) = \sum_{j=1}^N r_j + \frac{d}{dt} \sum_{j=1}^N c_j$$

n = NUMBER OF “DRIVERS” Y_i CONTRIBUTING TO THE CITY “METABOLISM”

r_j = RATE AT WHICH THESE RESOURCES ARE USED BY THE j^{th} INDIVIDUAL (MAINTAIN HIS/HER/ITS LIFE-STYLE, ETC)

c_j = COST OF ADDING A NEW INDIVIDUAL TO THE CITY POPULATION

$$R \approx NR_0 + E_0 \frac{dN}{dt}$$

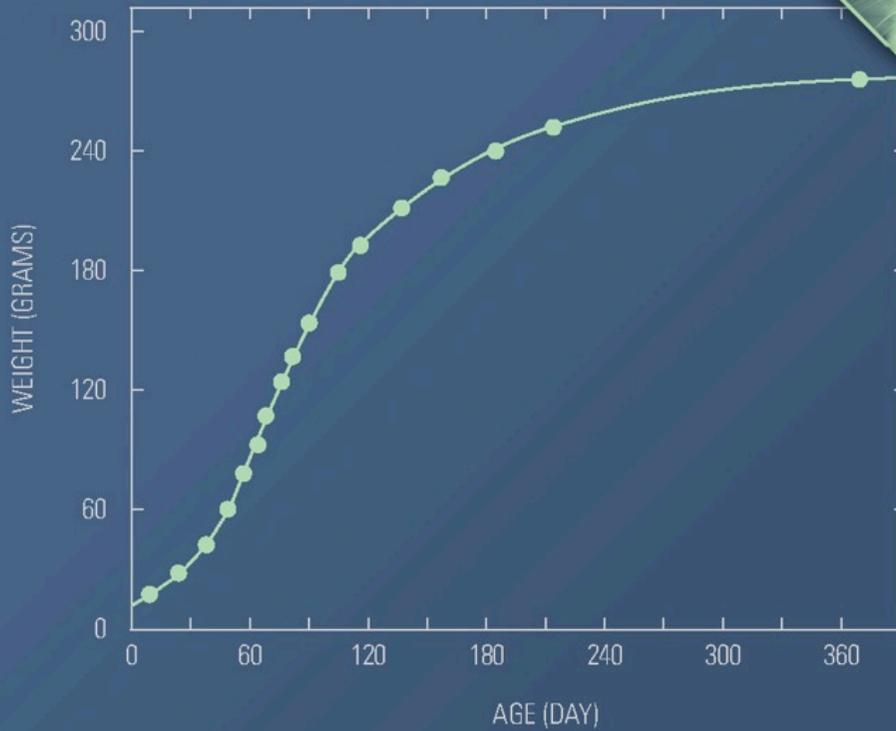
$$\frac{dN}{dt} = \left(\frac{R_1}{E_0} \right) \left[N^\beta - \left(\frac{R_0}{R_1} \right) N \right]$$

SOLUTION:

$$N^{1-\beta} = \frac{R_1}{R_0} + \left[N^{1-\beta}(0) - \frac{R_1}{R_0} \right] e^{-\frac{R_0}{E_0}(1-\beta)t}$$

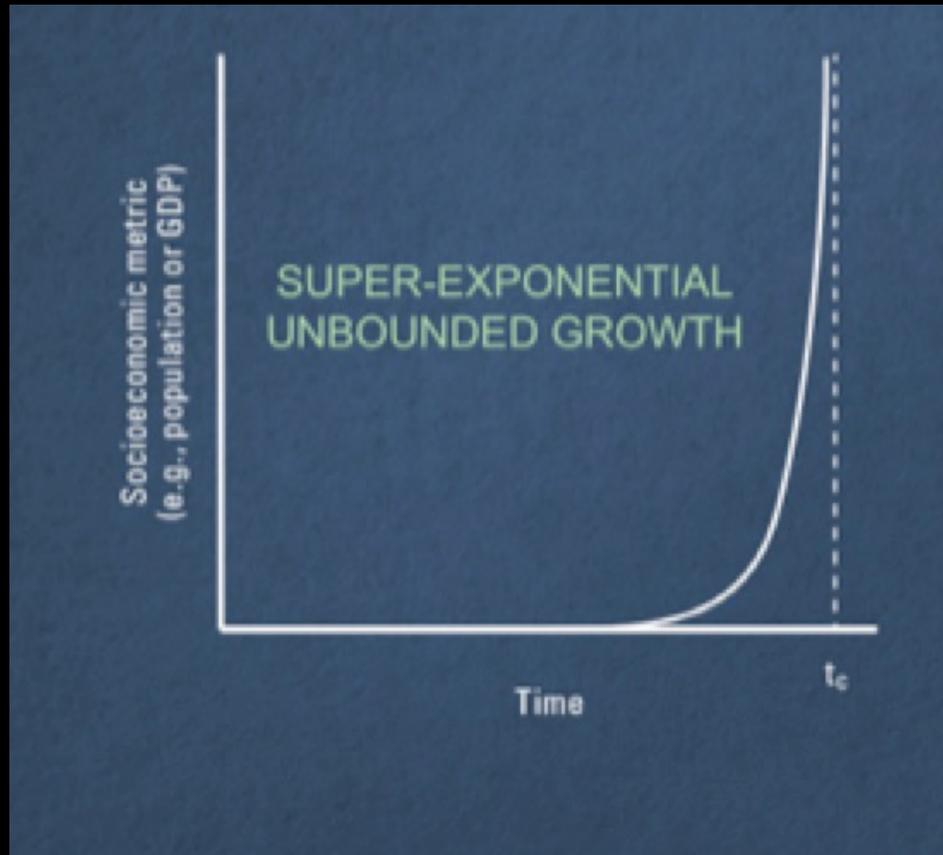
CHARACTER OF SOLUTION SENSITIVE TO $\beta >, =, < 1$

GROWTH CURVE OF RAT

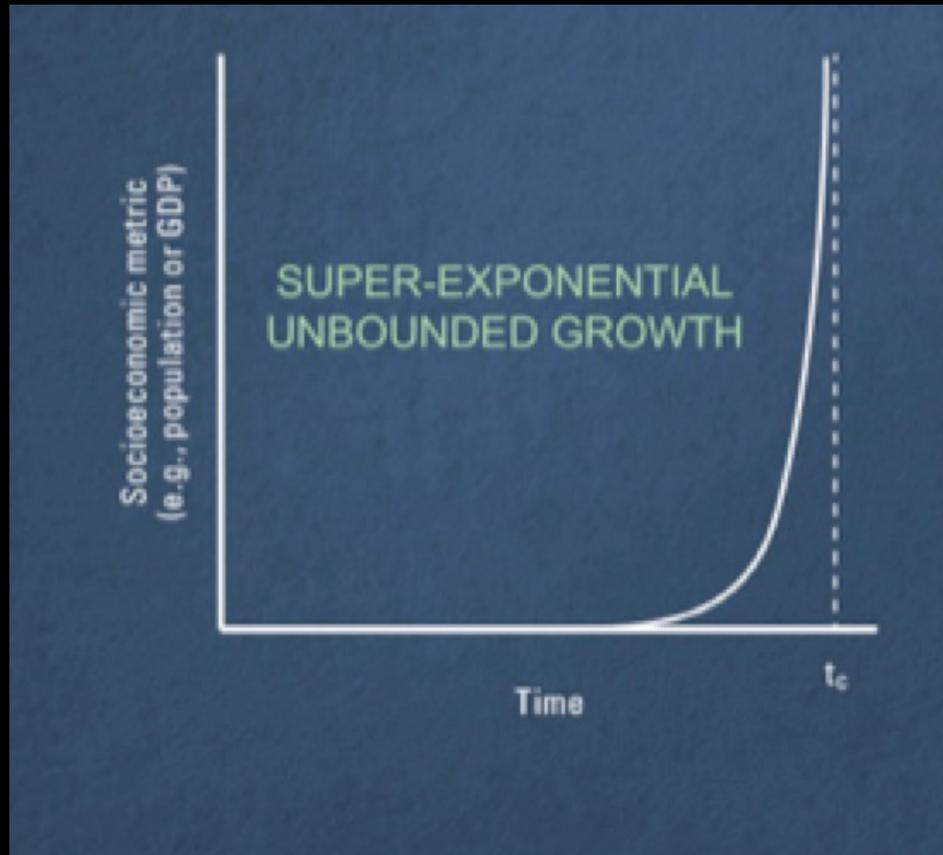


SUB-LINEAR SCALING LEADS
TO BOUNDED GROWTH

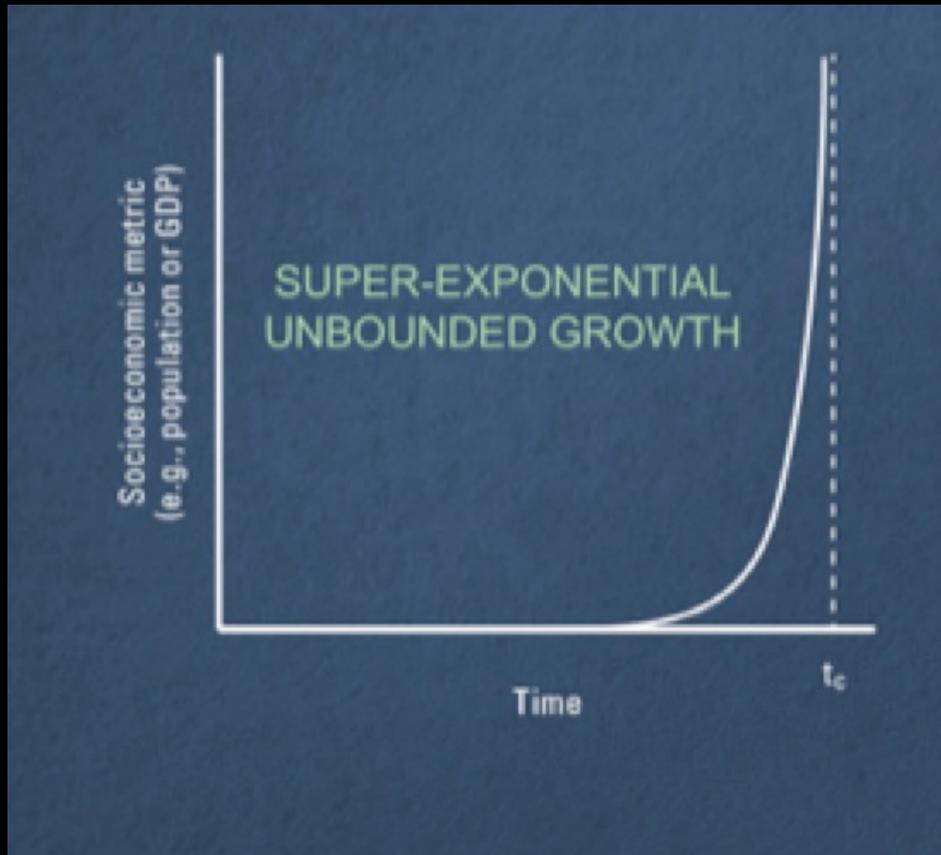
SUPERLINEAR SCALING LEADS TO UNBOUNDED GROWTH



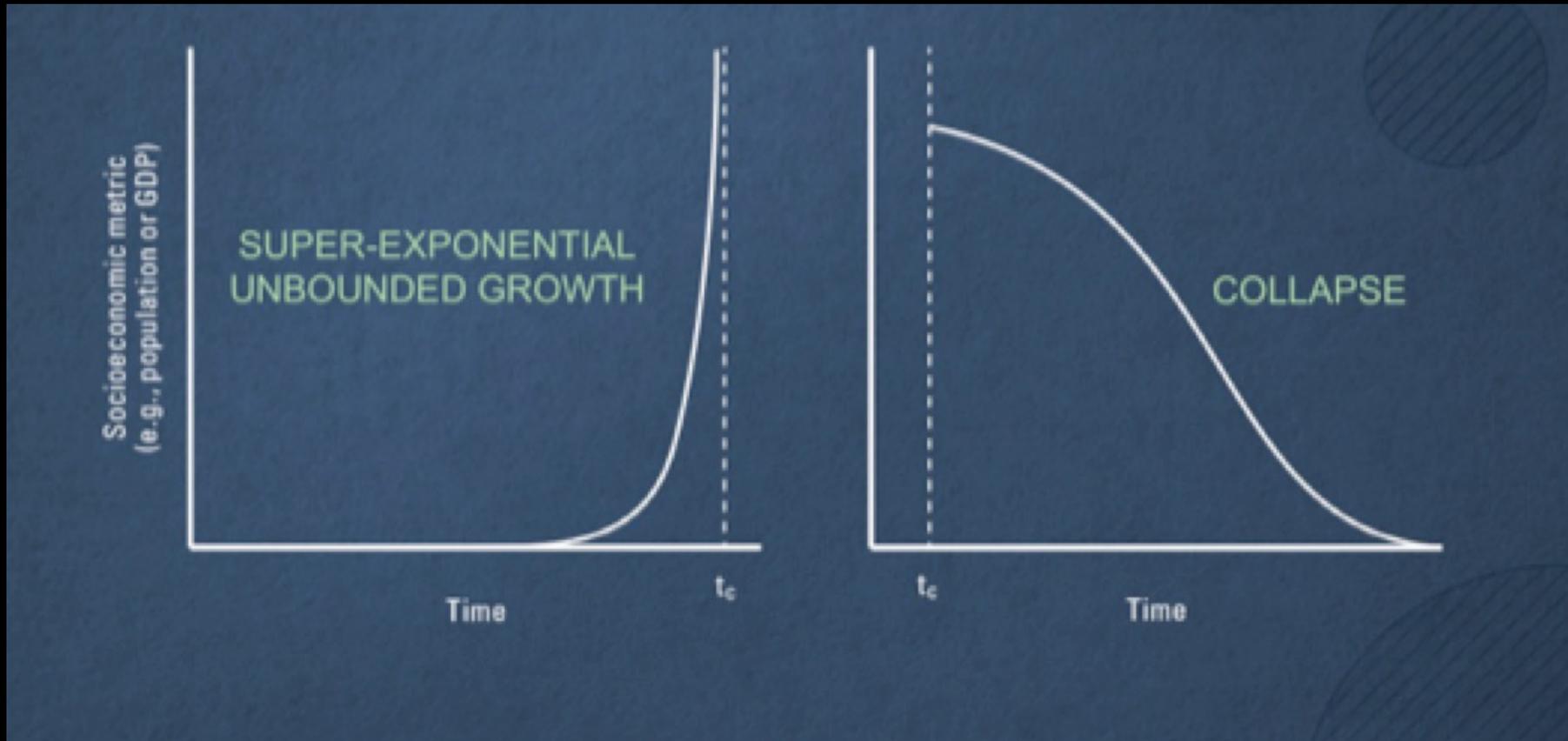
SUPERLINEAR SCALING LEADS TO UNBOUNDED GROWTH BUT ALSO TO A

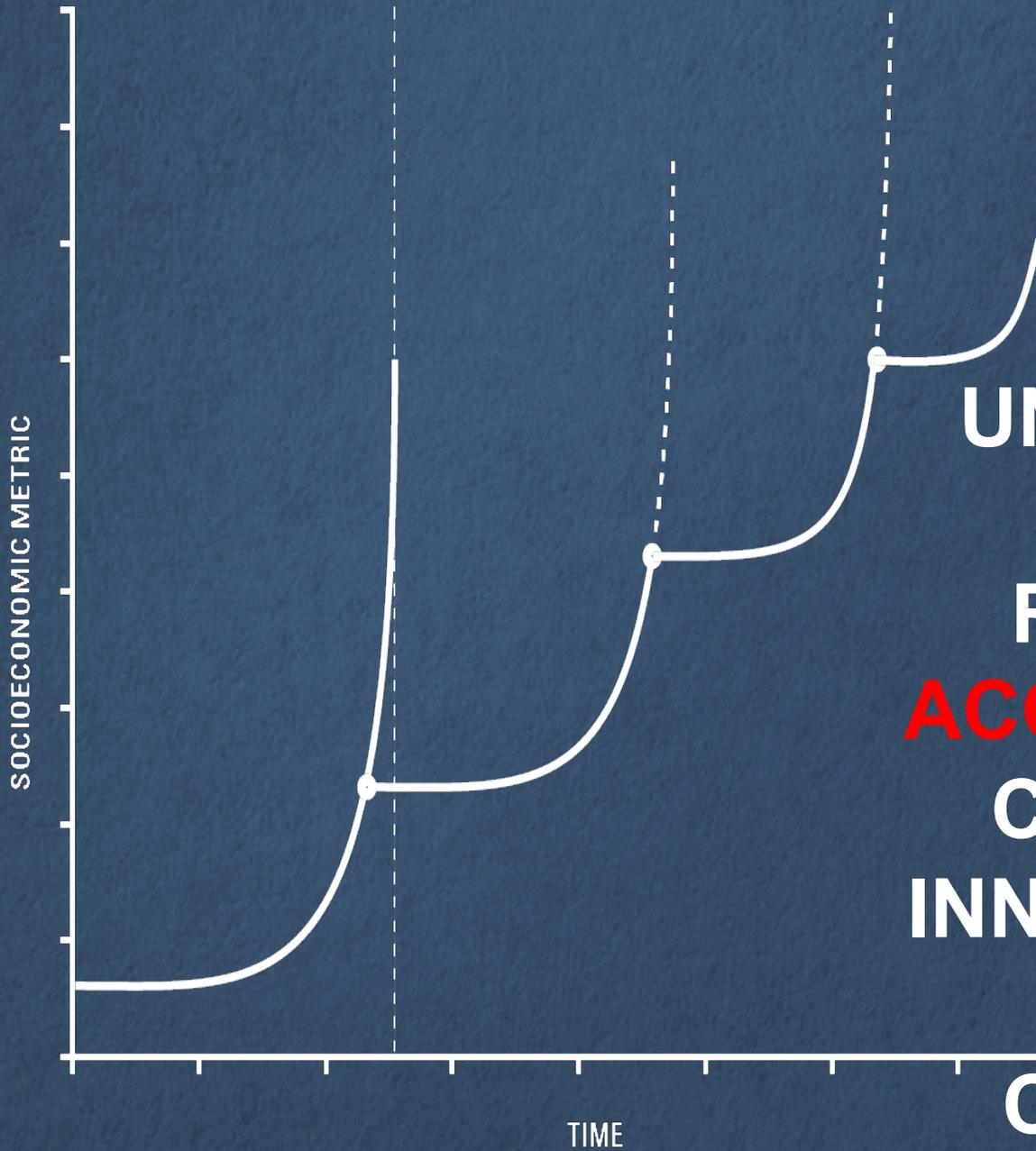


FINITE TIME SINGULARITY

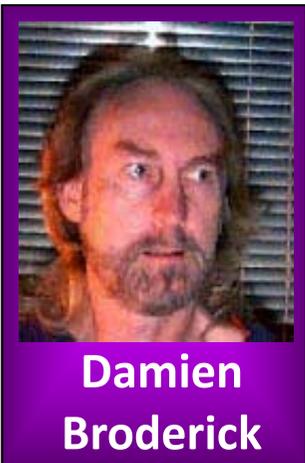


FINITE TIME SINGULARITY

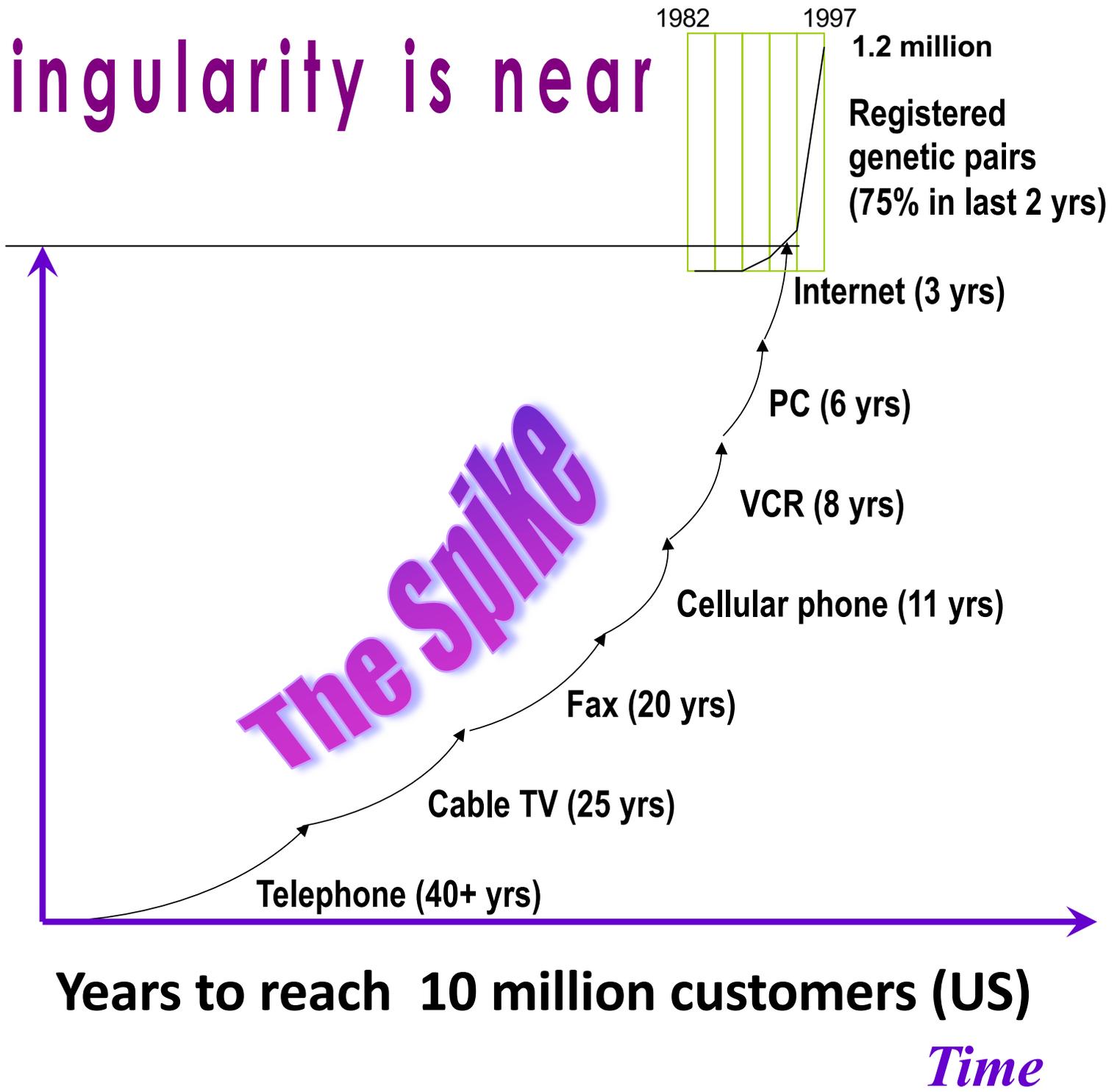




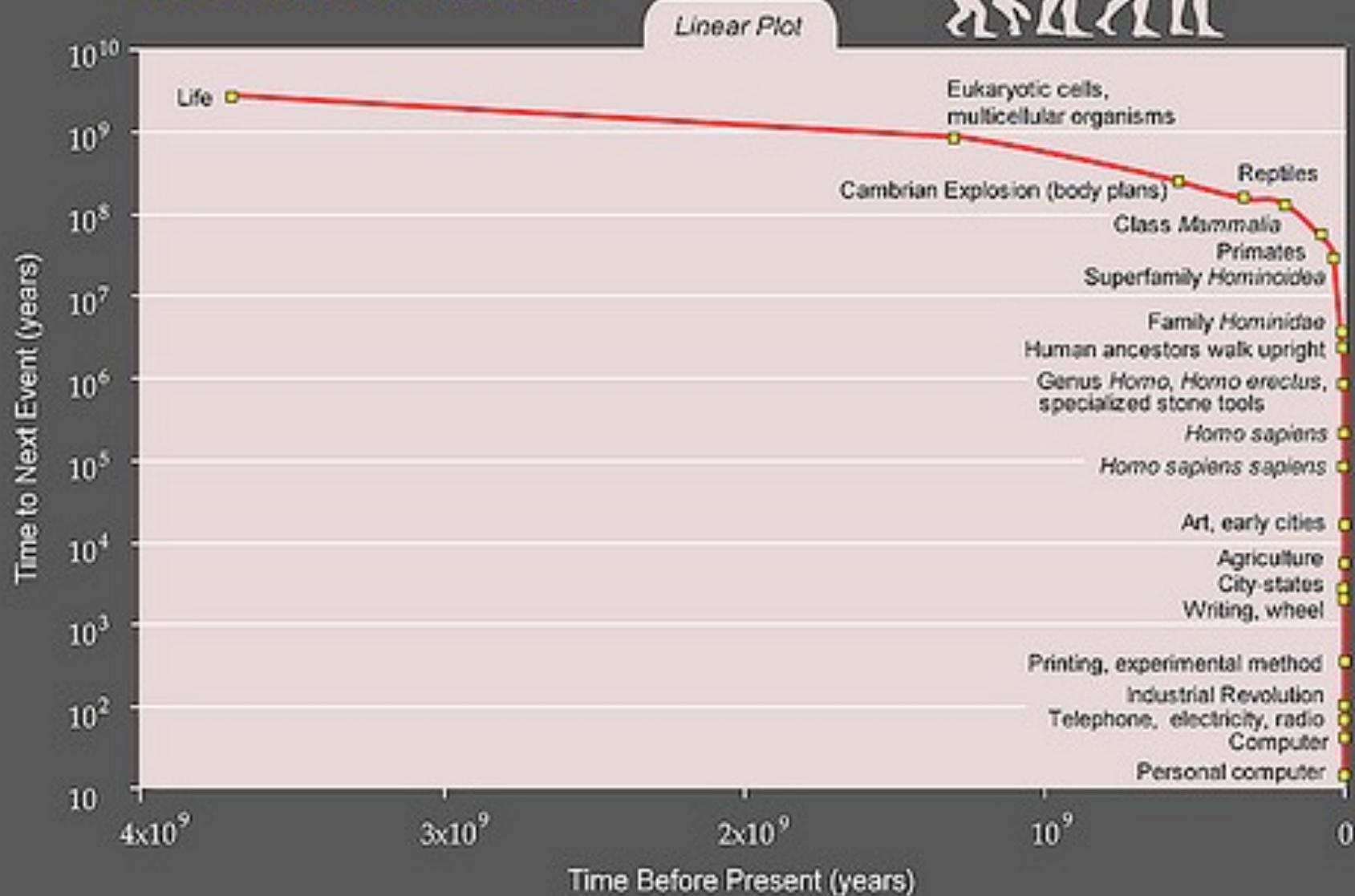
**UNBOUNDED
GROWTH
REQUIRES
ACCELERATING
CYCLES OF
INNOVATION TO
AVOID
COLLAPSE**



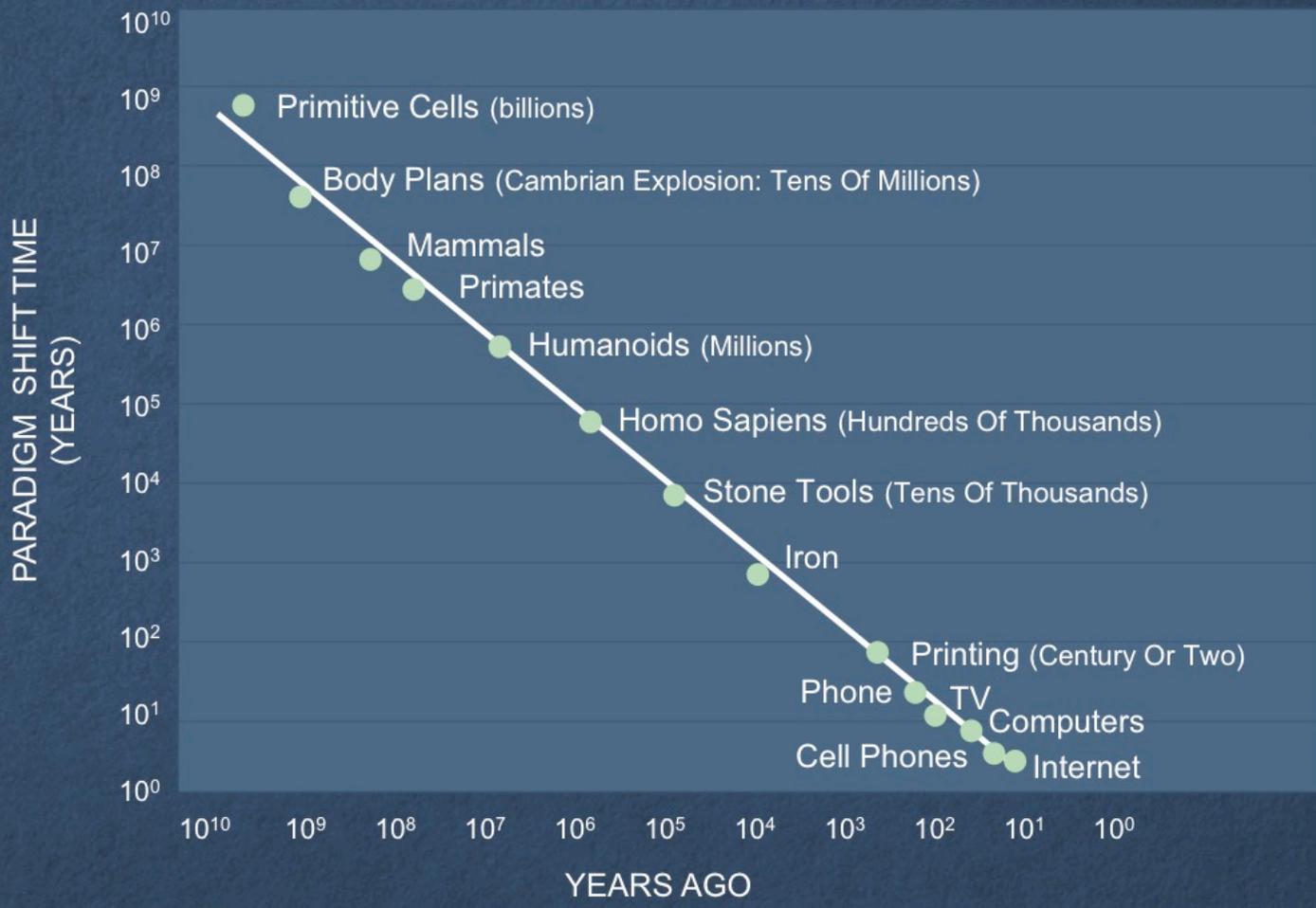
Singularity is near



Countdown to Singularity



SEQUENCE OF SINGULARITIES



**UNBOUNDED GROWTH LEADING TO
“FINITE-TIME SINGULARITY” & COLLAPSE**

**UNLESS INNOVATIONS OCCUR
(SYSTEMATICALLY) FASTER AND FASTER**

**UNBOUNDED GROWTH LEADING TO
“FINITE-TIME SINGULARITY” & COLLAPSE**

**UNLESS INNOVATIONS OCCUR
(SYSTEMATICALLY) FASTER AND FASTER**

**EXAMPLE OF THE ACCELERATING PACE OF
ALL SOCIO-ECONOMIC LIFE!!**

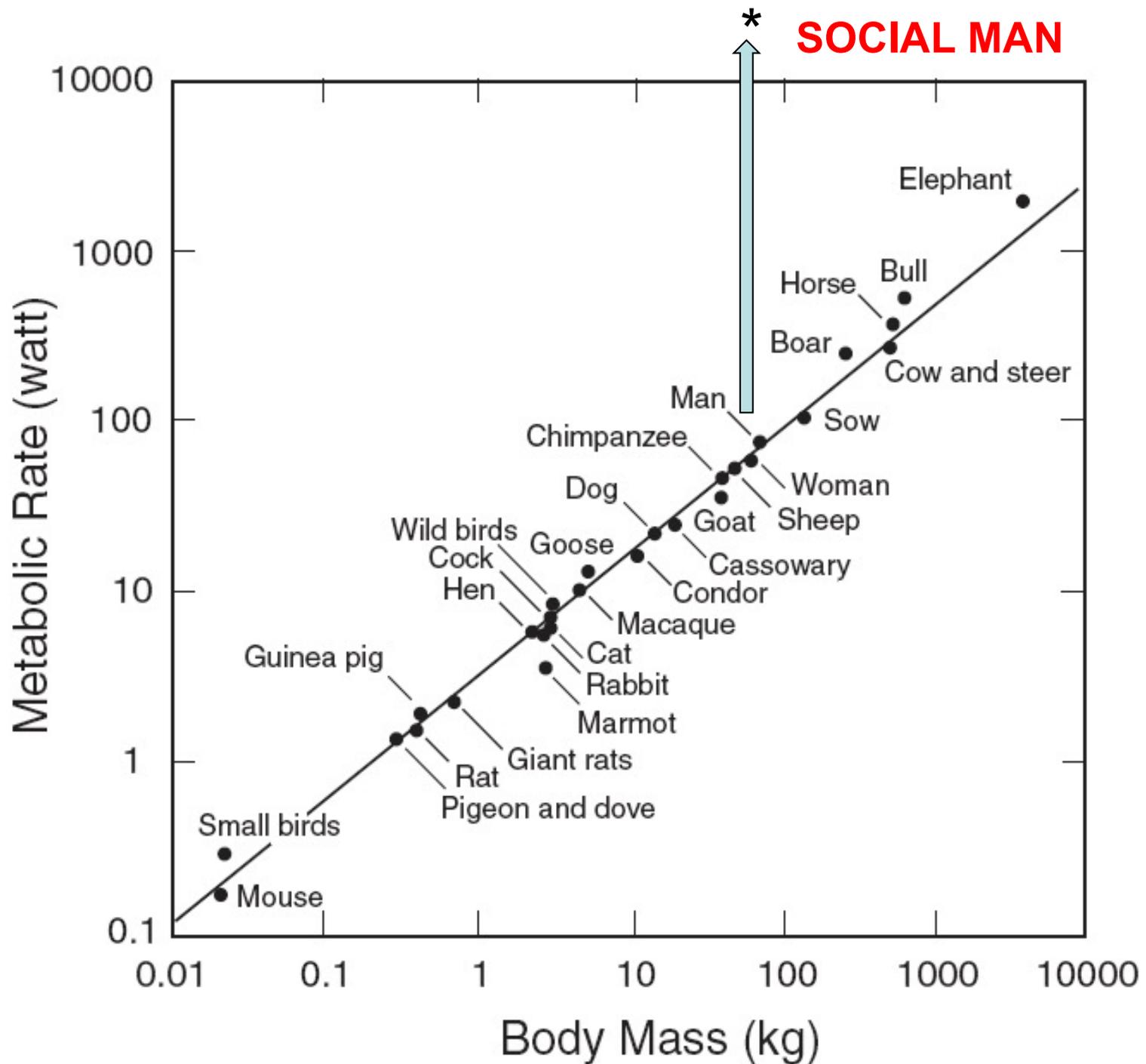
**NEED TO ADAPT FASTER AND FASTER
USING THE SAME BRAIN AND BIOLOGY
WE’VE ALWAYS HAD!**



SUSTAINABLE????

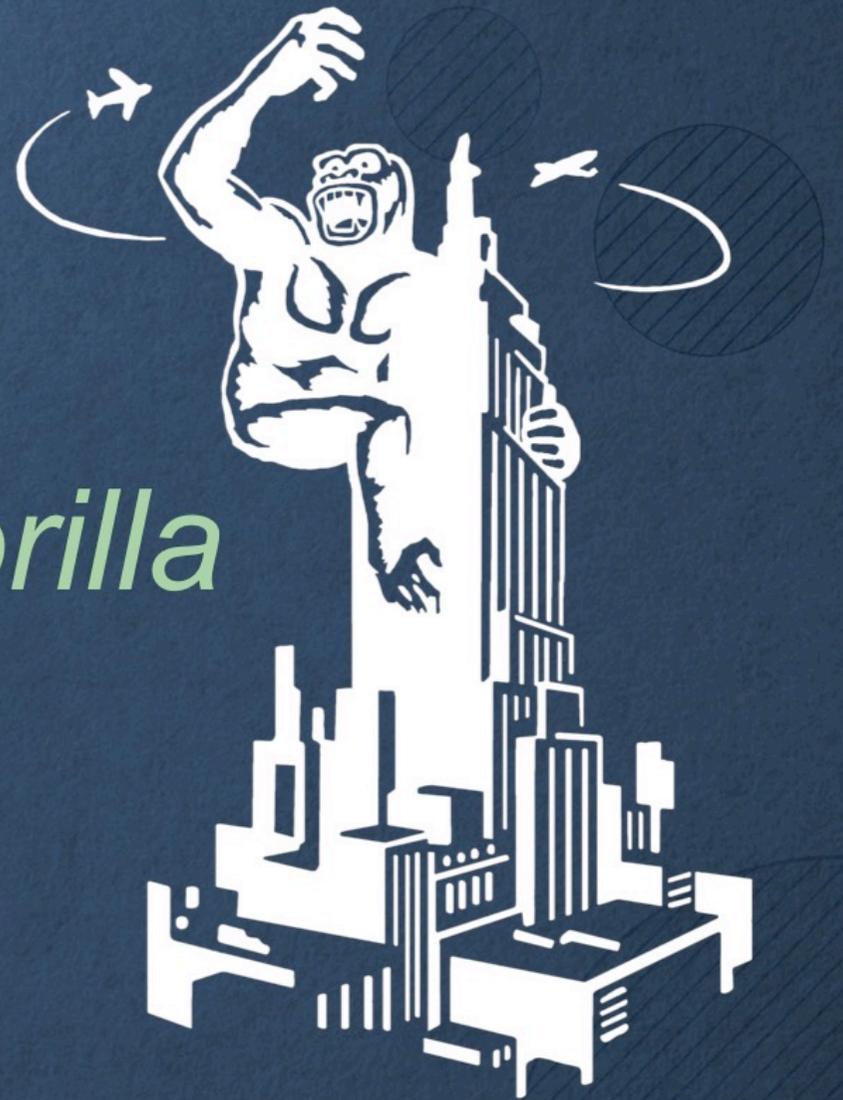
Our “natural” metabolic rate *~90 watts*

Our social metabolic rate *~11,000
watts*



SLOPE = $\frac{3}{4} < 1$; SUB-LINEAR; ECONOMY OF SCALE

We are equivalent to a
30,000 kg Gorilla





12 *Elephants*



THE SINGULARITY IS NEAR!

The ever accelerating progress of technology....gives the appearance of approaching some essential singularity in the history of the race beyond which human affairs, as we know them, could not continue.



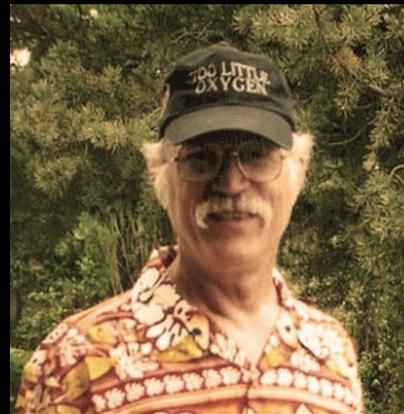
John von
Neumann
(1903 - 1957)



Jim Brown (UNM)



Brian Enquist (U of Arizona)



Woody Woodruff (LANL)



Van Savage (UCLA)



Jamie Gillooly (U of Florida)



Drew Allen (MacQuarie U)



Chen Hou (MissouriTech)



Melanie Moses (UNM)



Alex Herman (Minnesota)



Ric Charnov (UNM)



Chris Kempes (SFI)



Wenyun Zhuo (Stanford)



Luis Bettencourt (Chicago)



Jose Lobo (U of Arizona)



**Debbie Strumsky (U of
Arizona)**



Hyejin Youn (N'western)



**Marcus Hamilton
(U of Texas)**



Madeleine Daepf (MIT)



Markus Schlapfer (ETH Zurich)



Carlo Ratti (MIT)



David Lane (U of Reggio)



**Sander van der Leeuw
(U of Arizona)**



**Denise Pumain (U
of Paris)**



Dirk Helbing (ETH Zurich)

SCALE

The Universal Laws of Growth,
Innovation, Sustainability, and the
Pace of Life, in Organisms, Cities,
Economies, and Companies

Geoffrey
West

GEOFFREY WEST

SCALE DIE
UNIVERSALEN GESETZE
DES LEBENS VON ORGANISMEN,
STÄDTEN UND UNTERNEHMEN

C.H. BECK

...und auf Deutsch: <https://www.chbeck.de/west-scale/product/27896321>