

GBP MC Analysis

Hits Profiles and Estimation of Reconstruction Precision

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Hits Profile

- Following the standalone MC analysis, a hit is defined as

An energy deposition event in which $E_{dep} > 1 \text{ keV}$

- Hits are a 'counting process' - follows Poisson statistics so error in each bin is given by $\sigma = \sqrt{N_{hits}}$
- From GEANT4 data (/nfs/dust/luxe/group/MCProduction/Signal/g4/ptarmigan-v0.8.1/e-laser/phase0/lp/), Hits tree was used to determine hits profile by placing appropriate cuts
- Energies are in GeV and distances in mm
- Bin sizes are assumed to be $100 \mu m$ (200 x 200 cells)

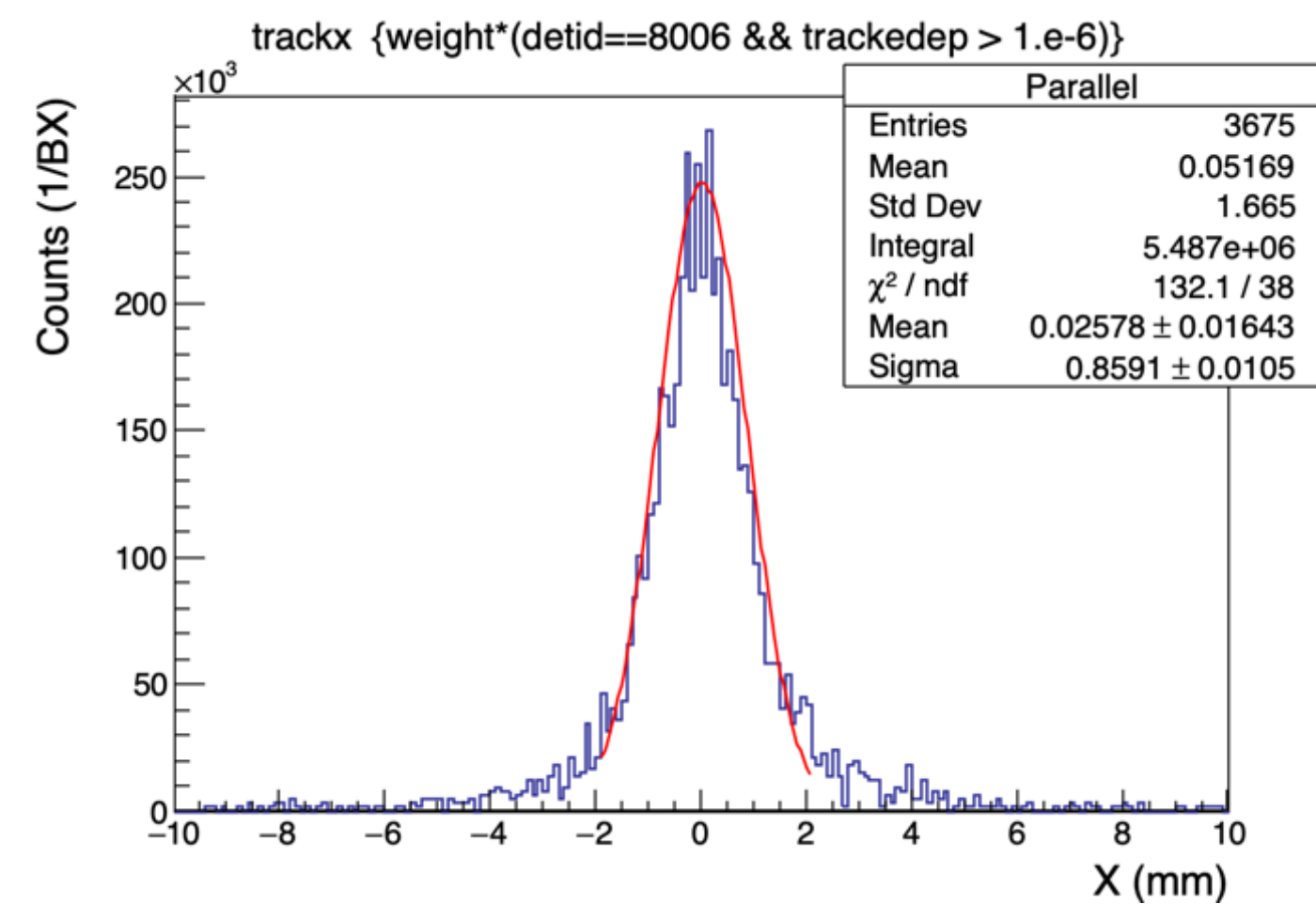
Gaussian Fit

- Gaussian fit applied to central range of distribution - taken to be ± 2.0 mm
- ROOT fit settings:
 - "WL" - weighted log-likelihood; recommended in ROOT documentation for histograms representing counts
 - "R" - fit to sub-range
 - "I" - use integral of bin content rather than value at centre
- Bin errors are more complicated - GEANT4 data uses macroparticles and so is weighted. Use `sumw1()` or `sumw2()`?
- `Sumw1()` determines the error in each bin to be $\sigma = \sqrt{\sum w_i}$ i.e. Sqrt of sum of bin weights
- `Sumw2()` determines the error in quadrature: $\sigma = \sqrt{\sum w_i^2}$
- `Sumw2()` is recommended when performing arithmetic (scaling, adding, subtracting, etc.) histograms to propagate errors correctly
- For our purposes, `sumw1()` is more appropriate

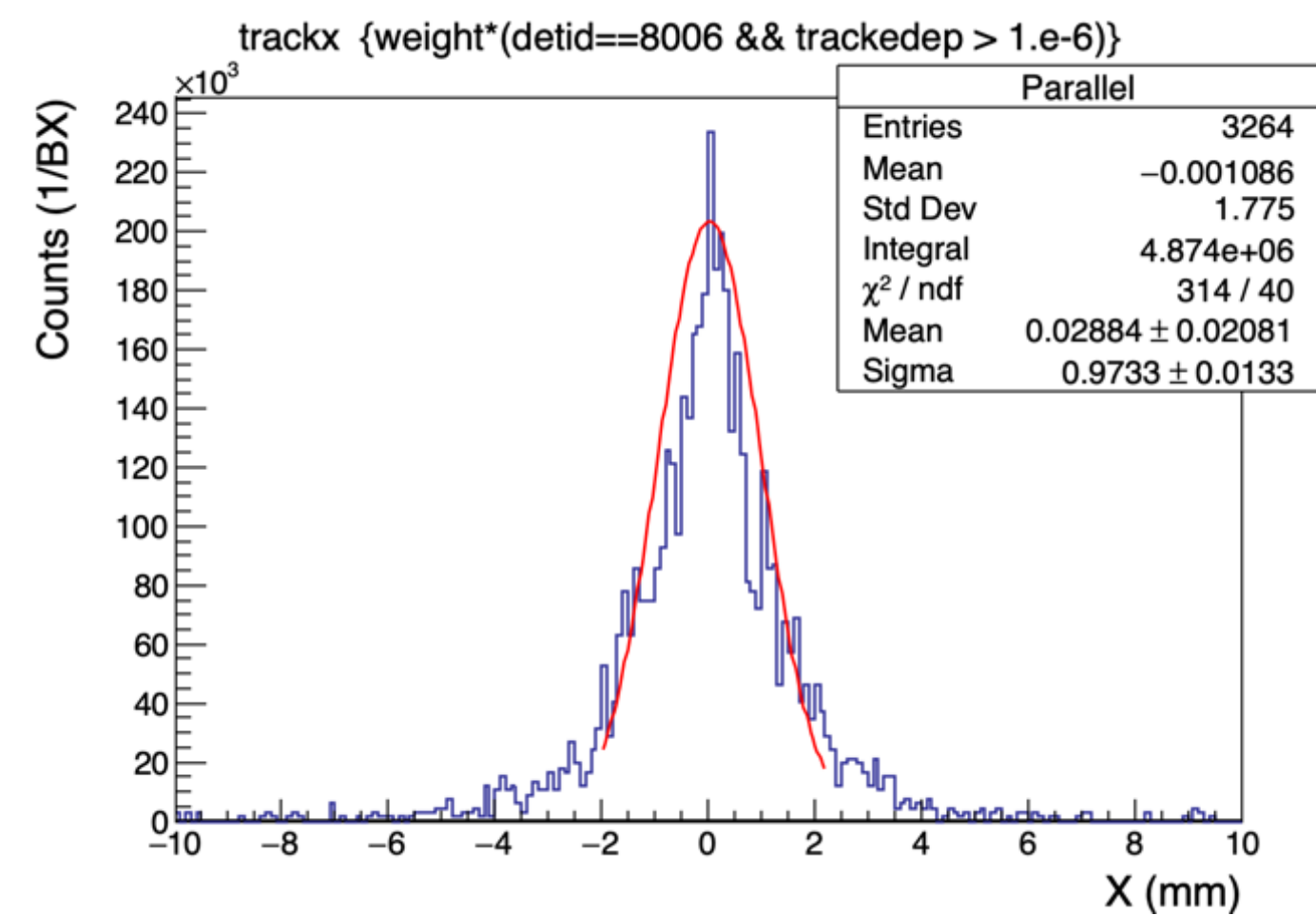
Fit Results

Upstream Profiler - Gaussian

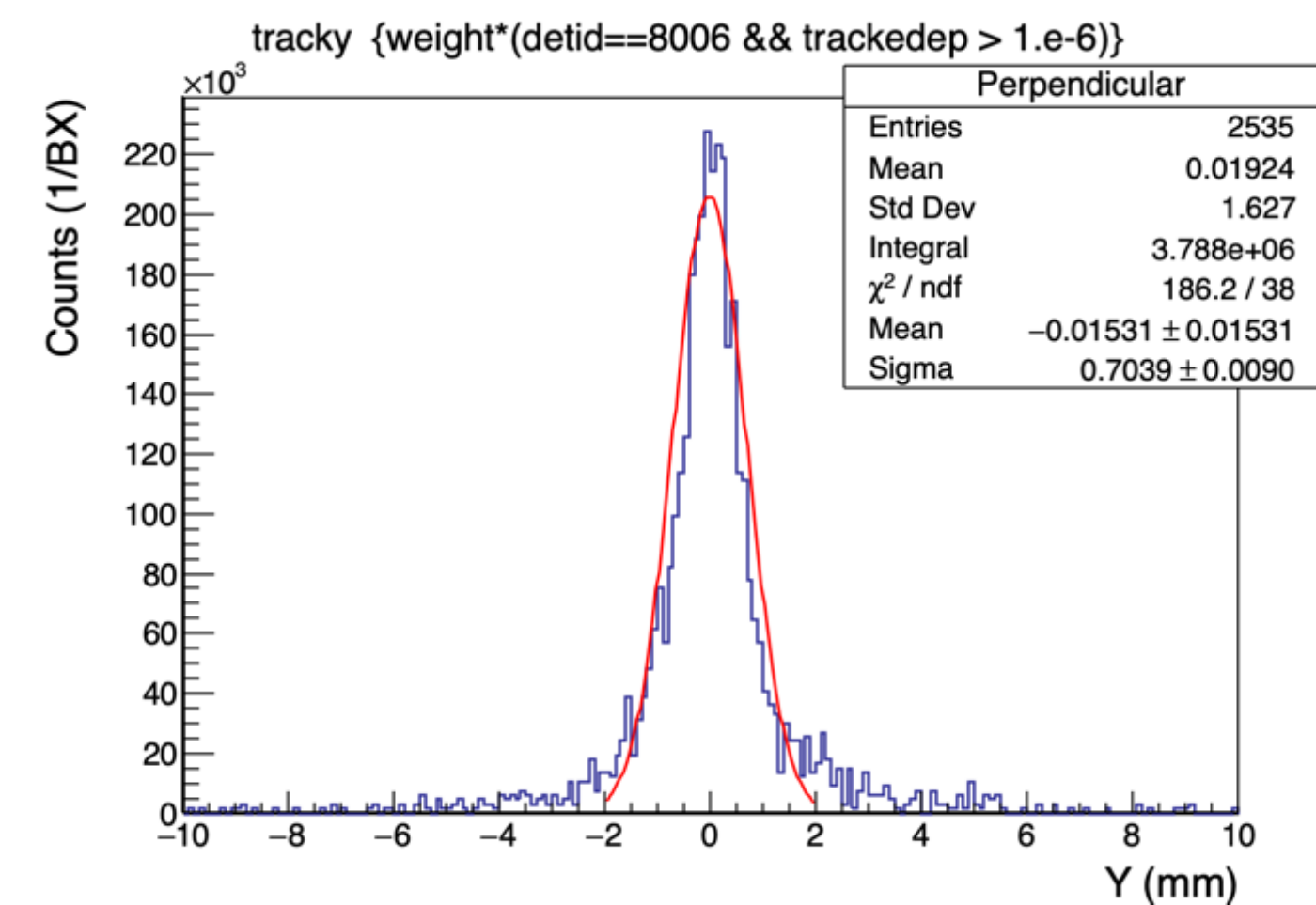
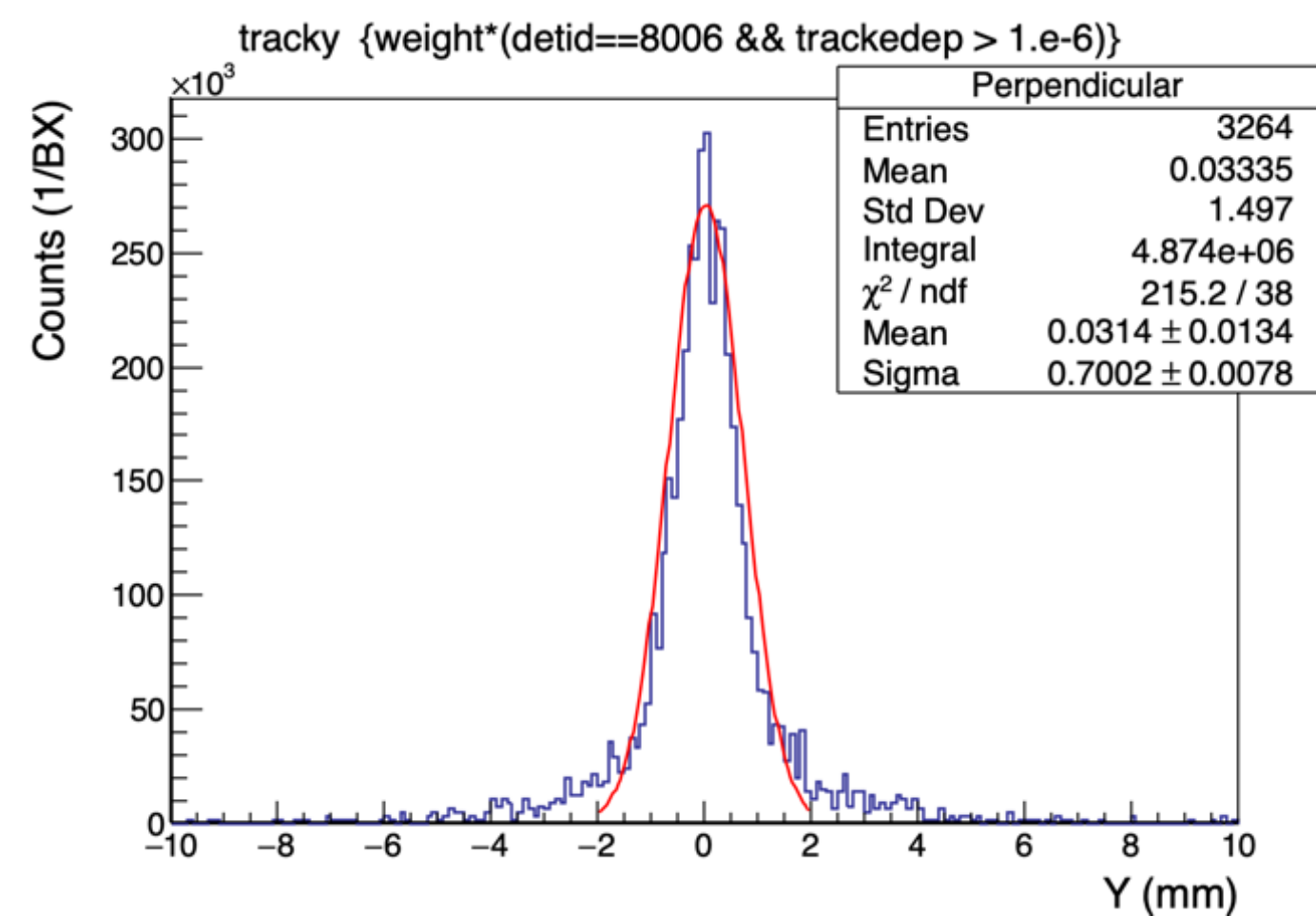
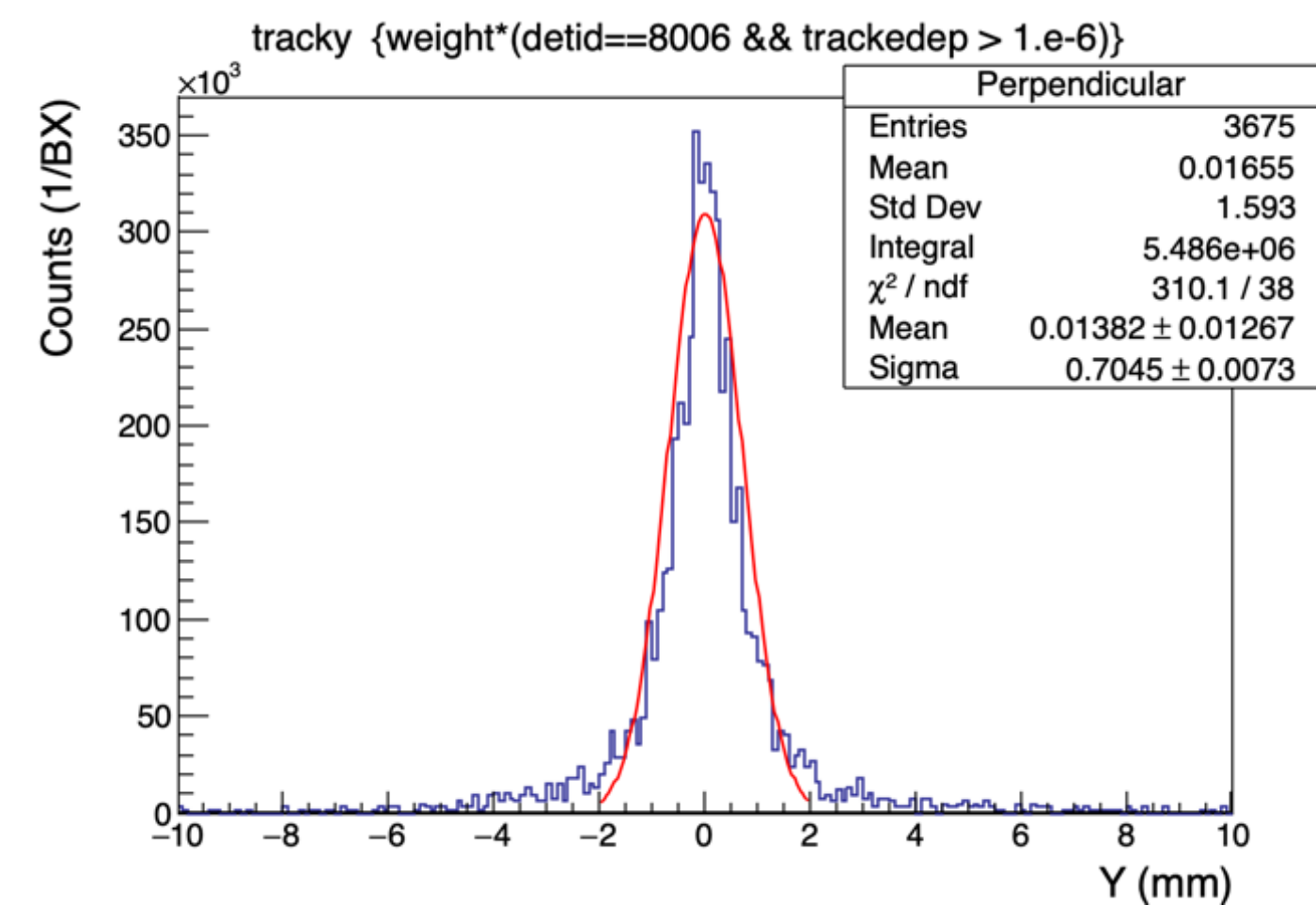
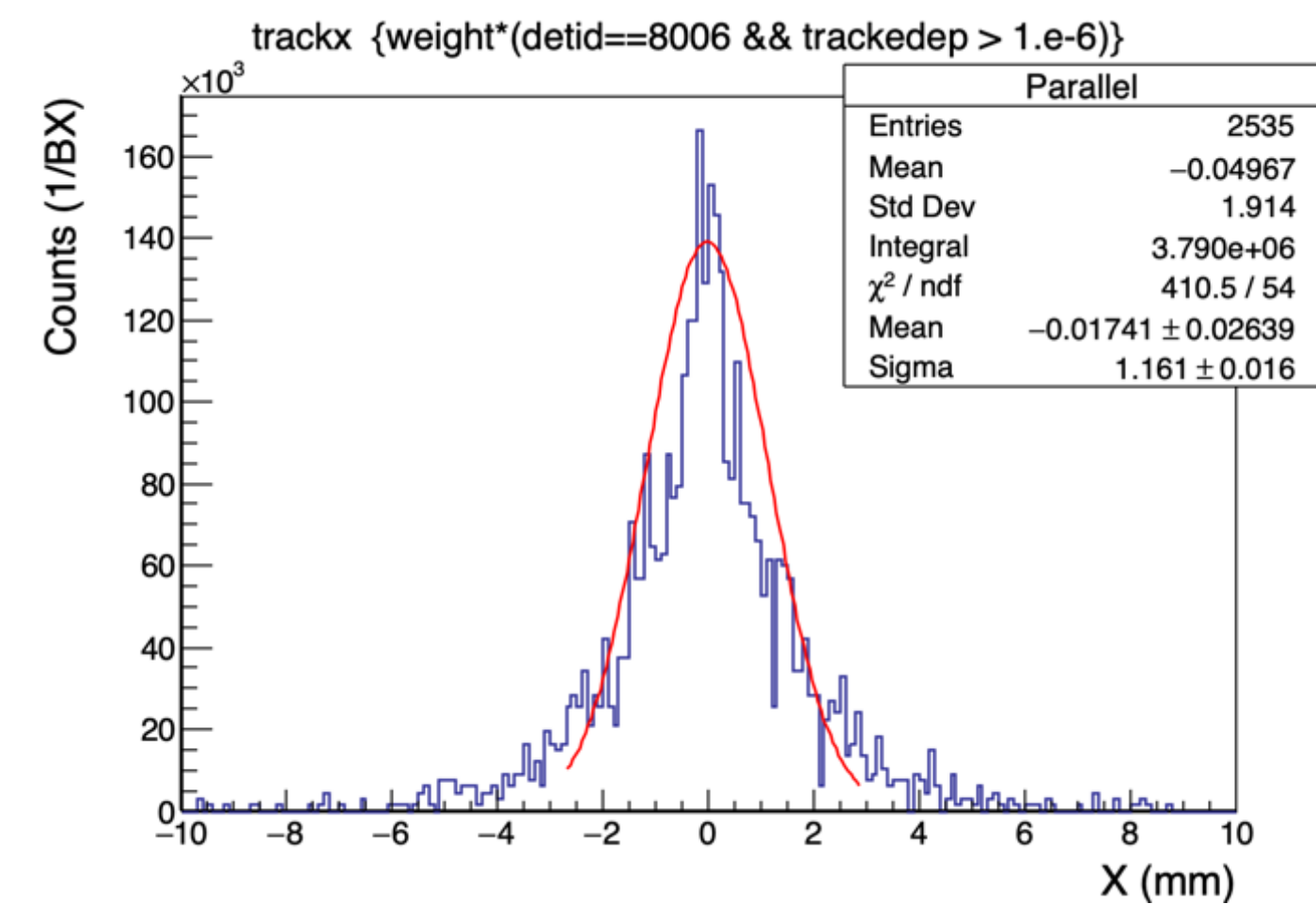
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$$\xi = 7$$



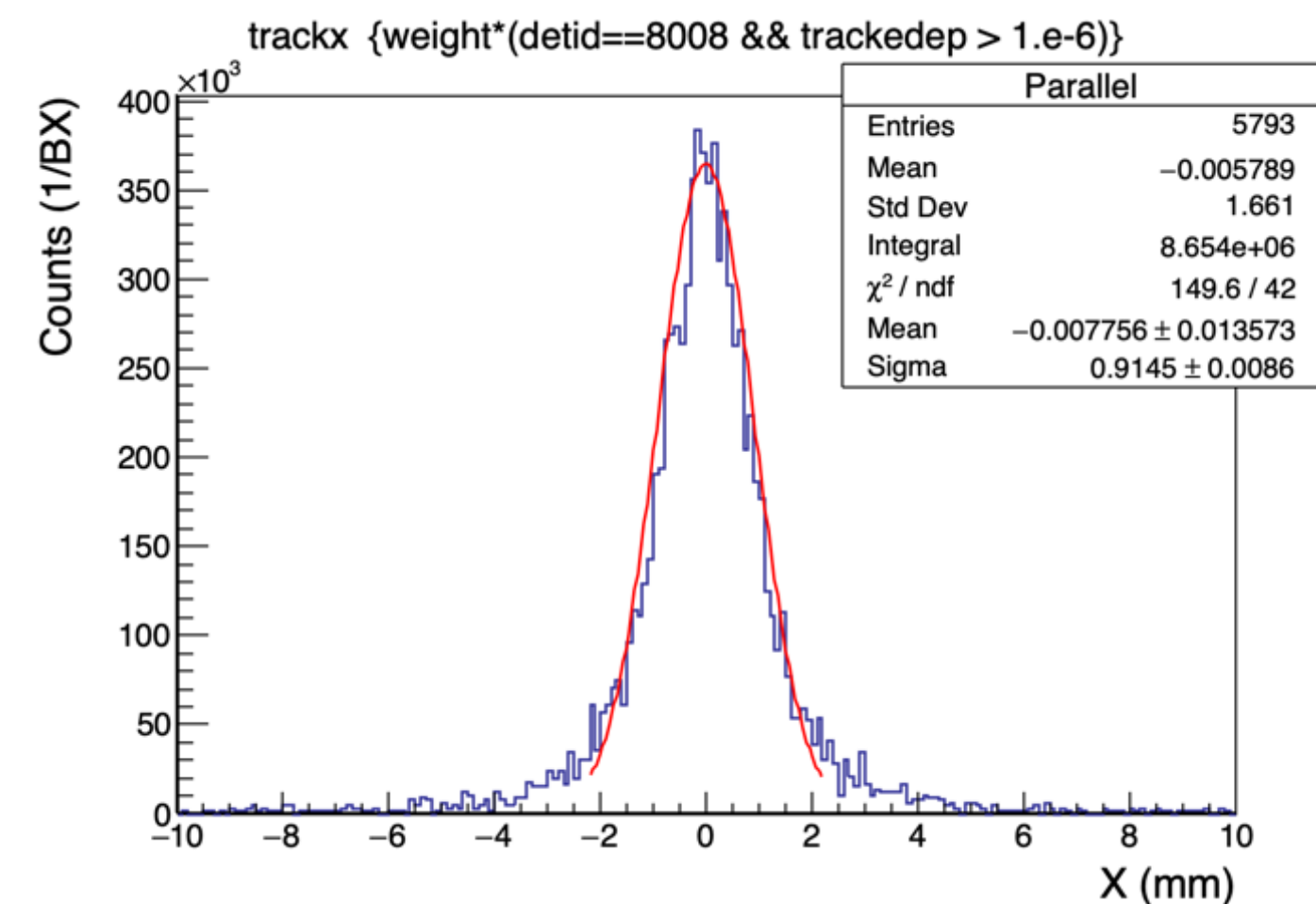
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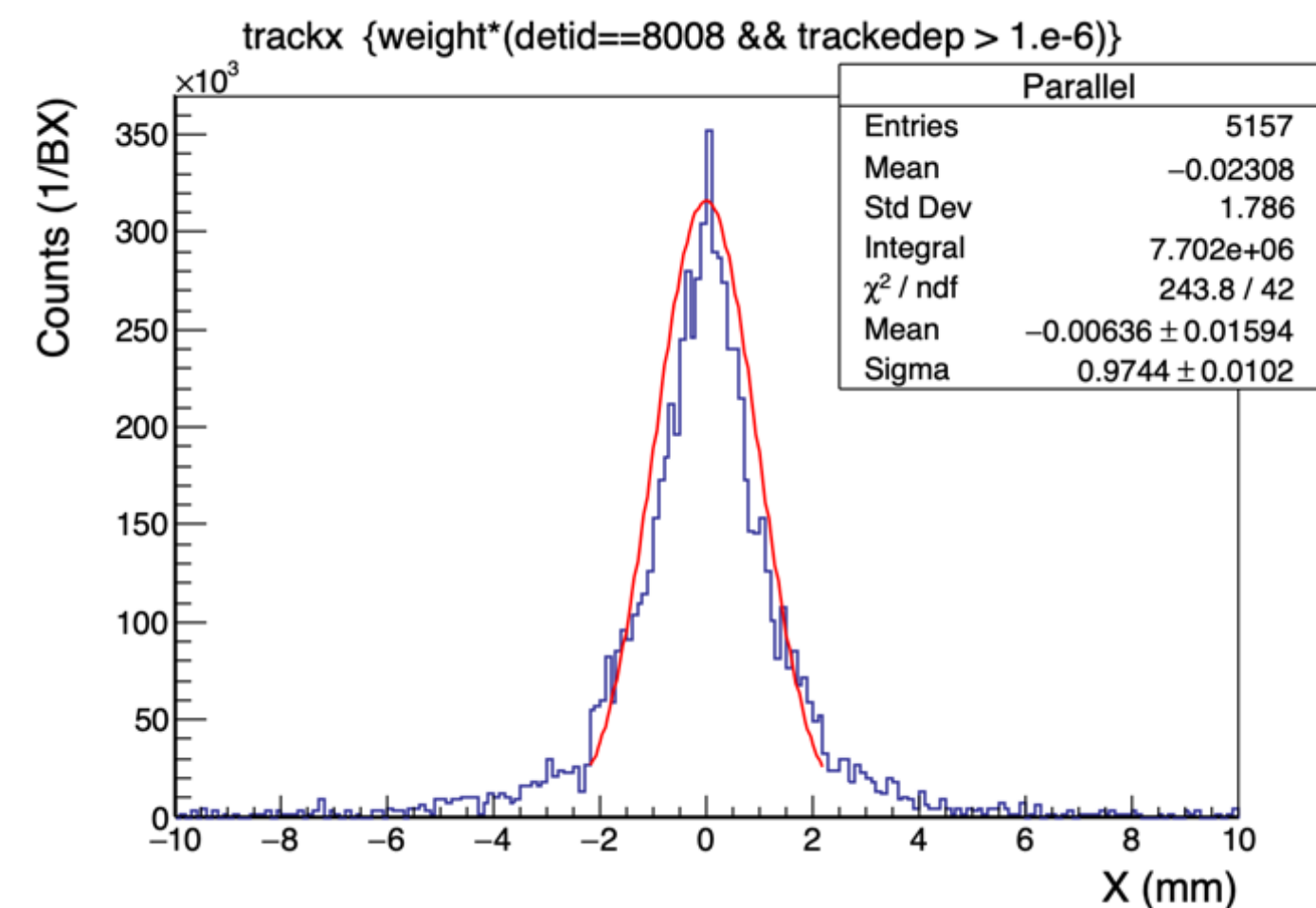
Fit Results

Downstream Profiler - Gaussian

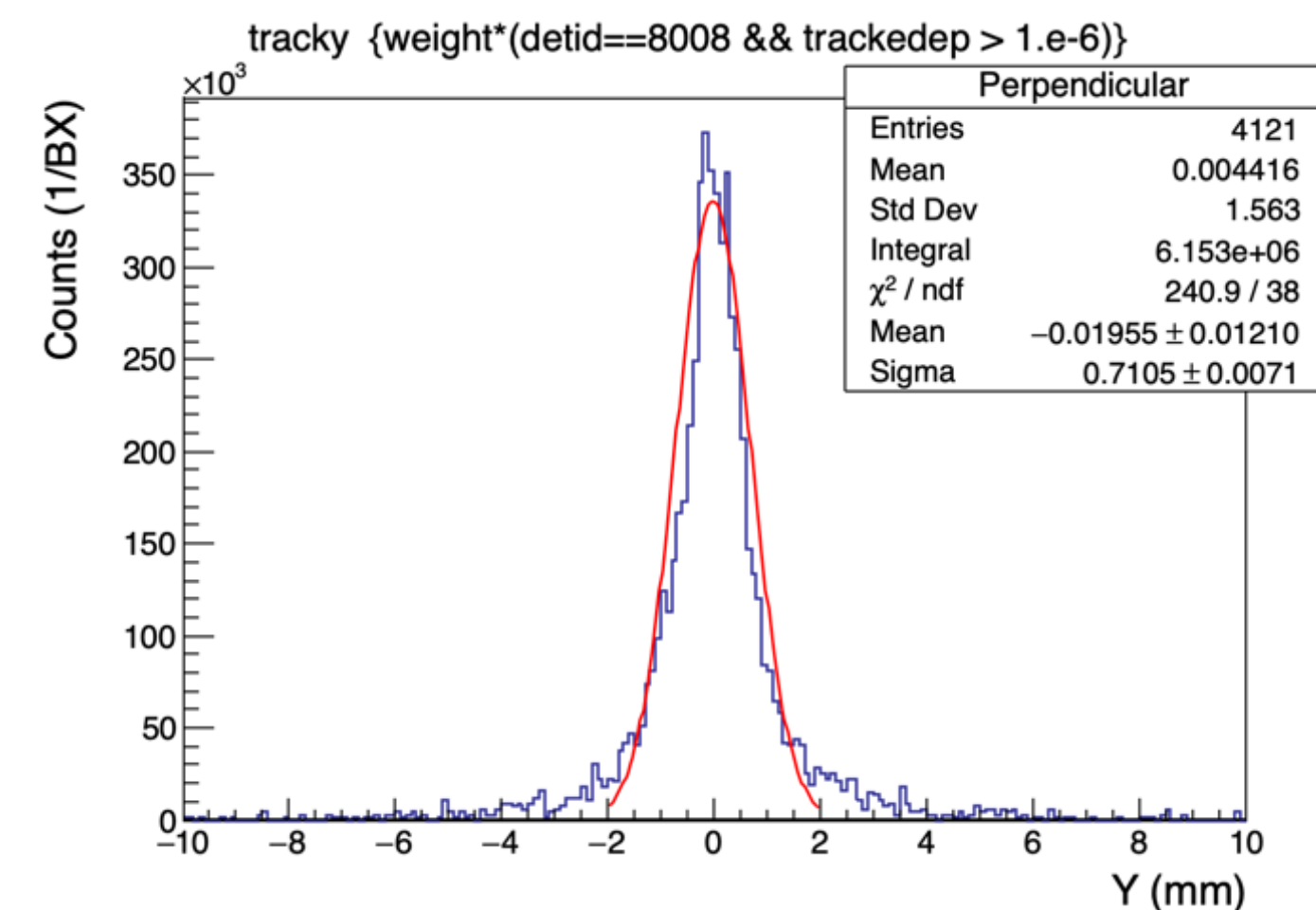
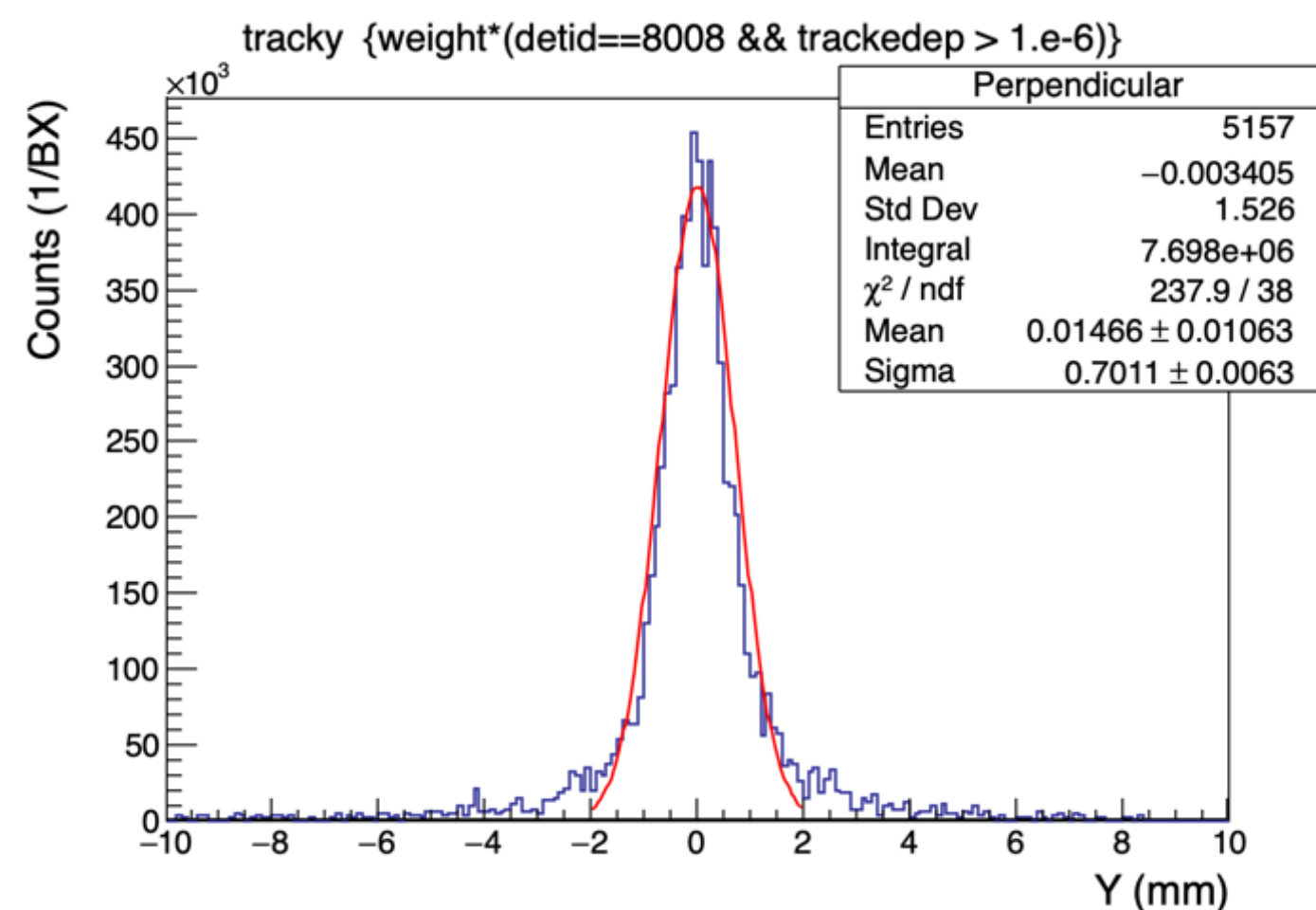
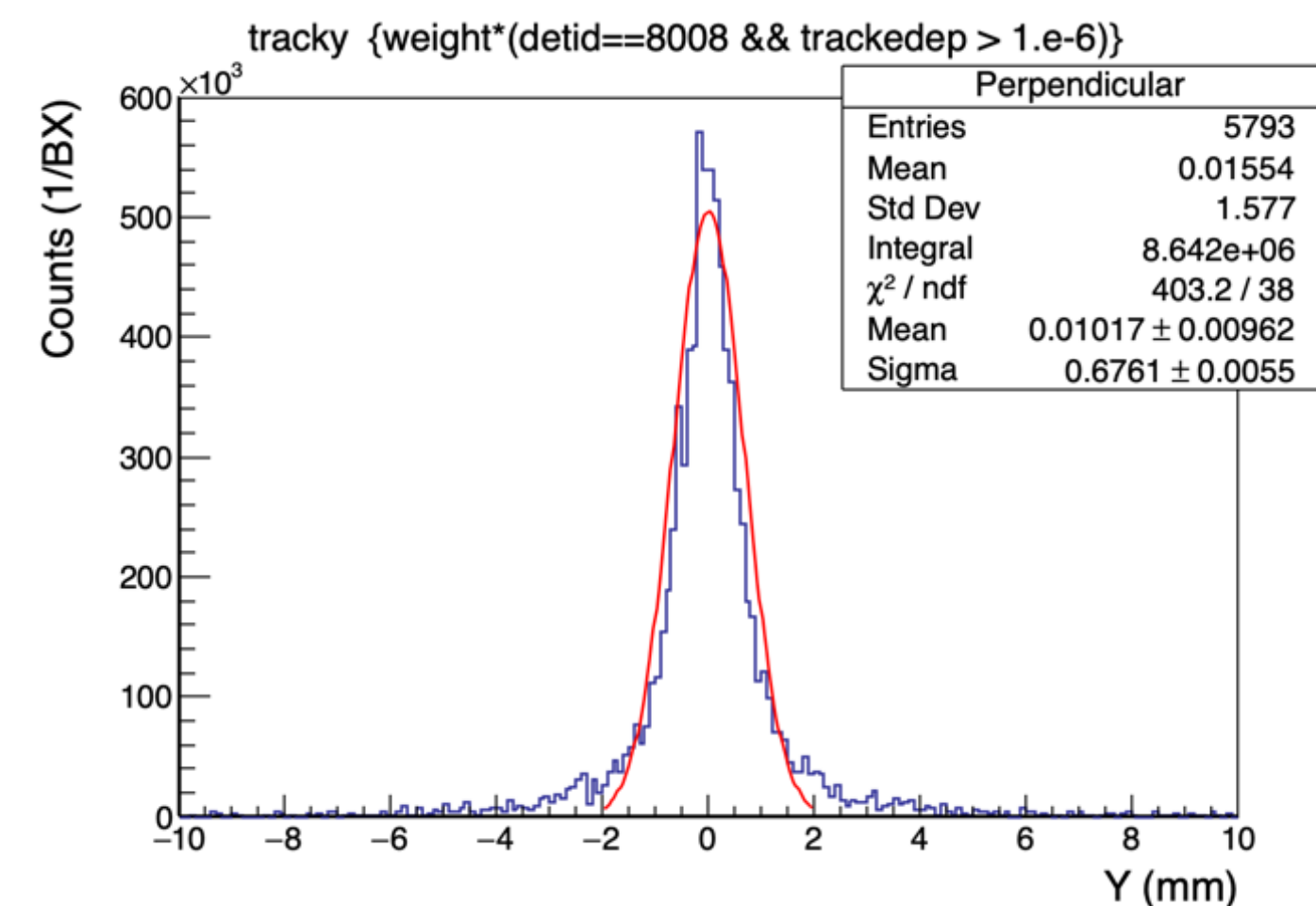
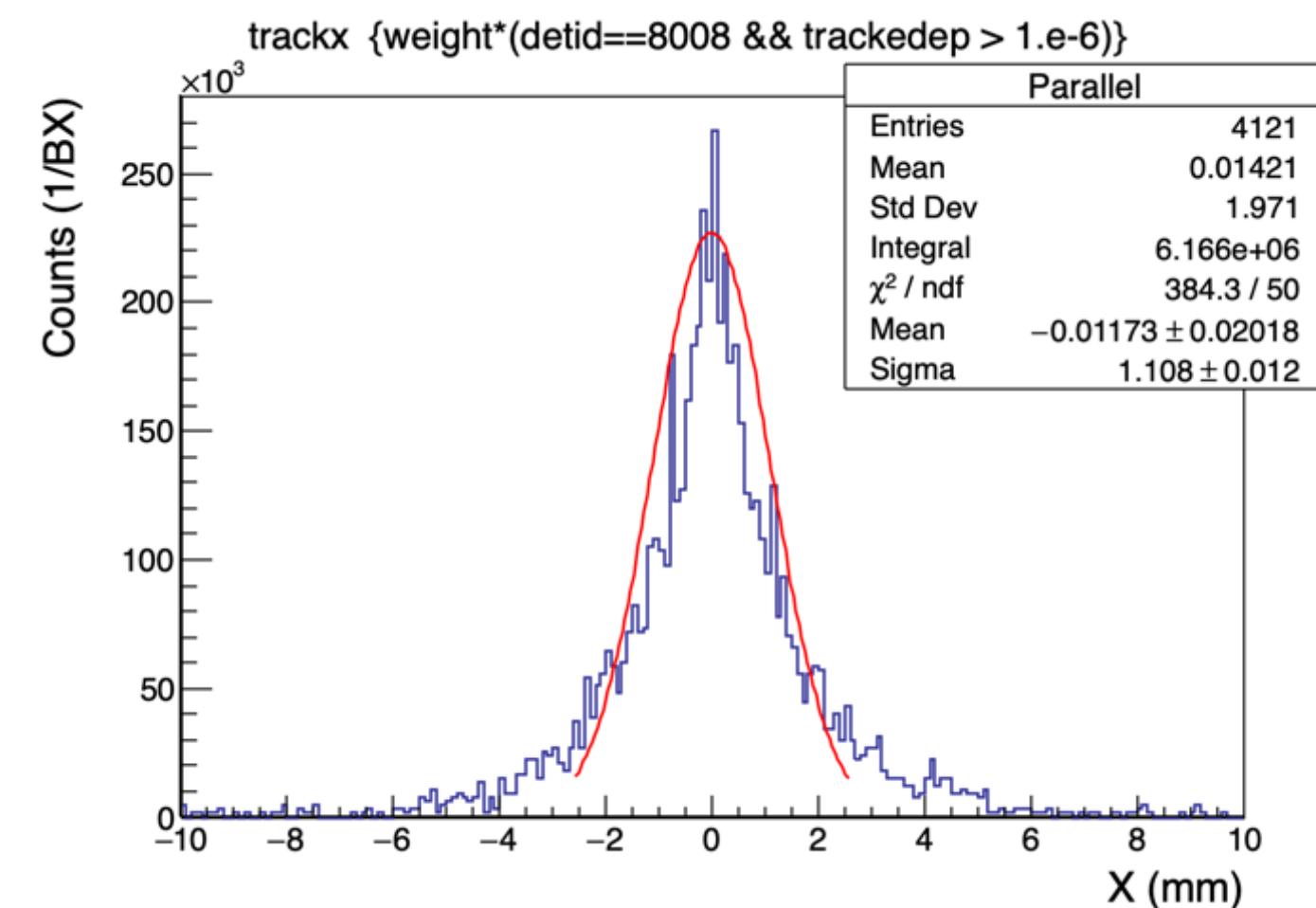
$$\xi = 5$$



$$\xi = 7$$



$$\xi = 10$$



Fit Results

Estimation of Resolution

- An estimate of the resolution can be obtained from the average error in the fitted Gaussian standard deviation (σ)
- Unweighted arithmetic mean:
 - Parallel - $25.0\ \mu m$, $18.6\ \mu m$
 - Perpendicular - $11.6\ \mu m$, $9.1\ \mu m$
- Weighted (by integral) arithmetic mean:
 - Parallel - $23.2\ \mu m$, $18.0\ \mu m$
 - Perpendicular - $11.5\ \mu m$, $12.3\ \mu m$

Estimation of ξ

- From Blackburn 2020 (10.1103/PhysRevAccelBeams.23.064001), model-independent formula for estimating ξ is

$$\bar{\xi}^2 = \frac{1}{\beta^2} 4\sqrt{2} \langle \gamma_i \rangle \langle \gamma_f \rangle (\sigma_{\parallel}^2 - \sigma_{\perp}^2)$$

- Here, σ^2 is the variance of the **energy-weighted** distribution - this should be Gaussian
- GBP measures **number-weighted** distribution
- Current Ptarmigan simulations use LCFA which overestimates low energy (high angle) photons giving profile heavier tails
- Moving to LMA later (more accurate than LCFA) may reduce this effect
- Energy-weighted distribution rather than number-weighted also takes this into account and gives a more reasonable Gaussian shape

Voigt Profile

- Voigt profile is the convolution of a Gaussian and a Lorentzian function

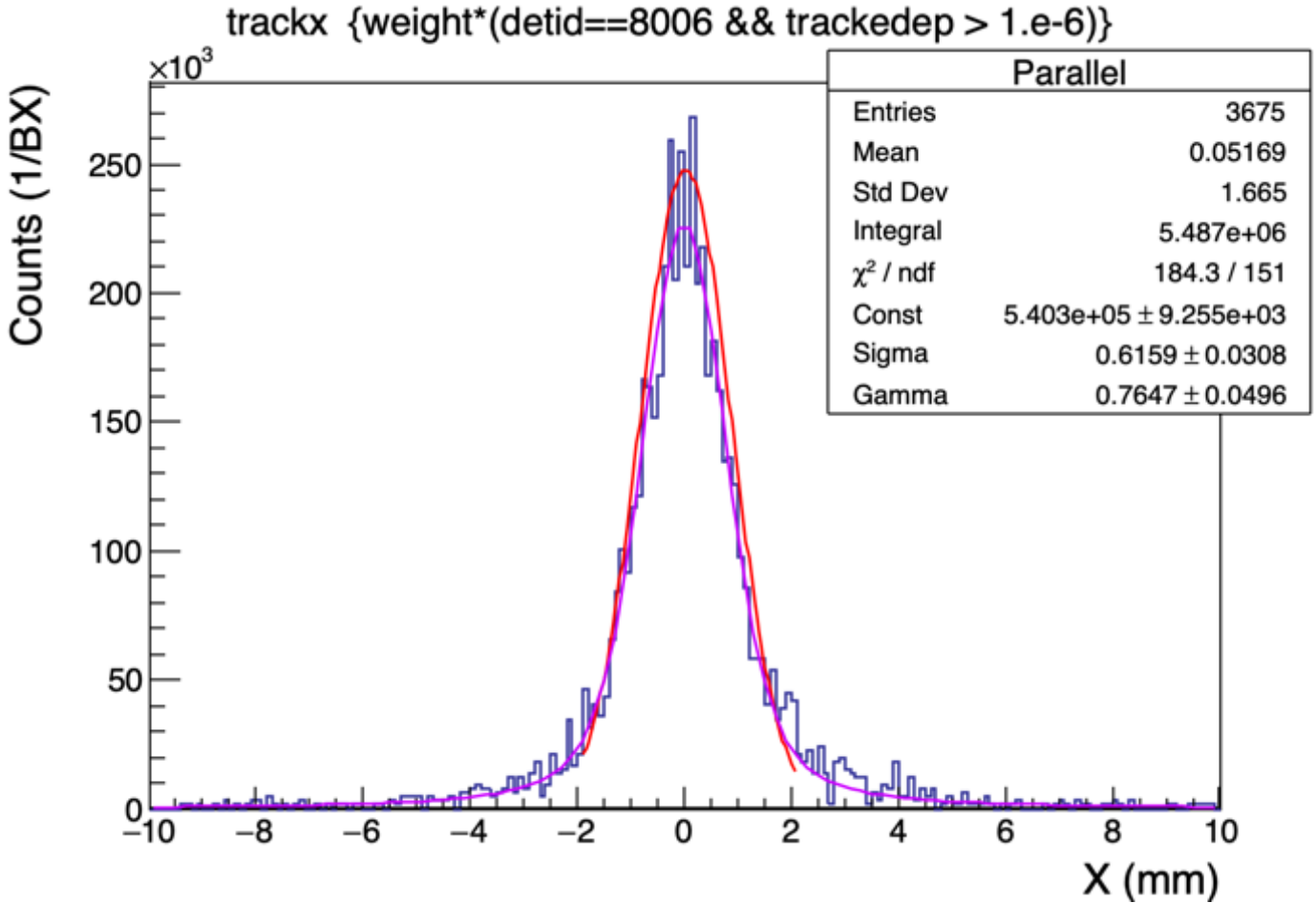
$$V(x; \sigma, \gamma) = \int dt G(t; \sigma) \cdot L(x - t; \gamma)$$

- Definition assumes distributions centred at zero
- ROOT provides an in-built function to evaluate and fit Voigt profiles to histograms
- May provide a way of separating the Gaussian and Lorentzian 'signatures' seen in the profiler results

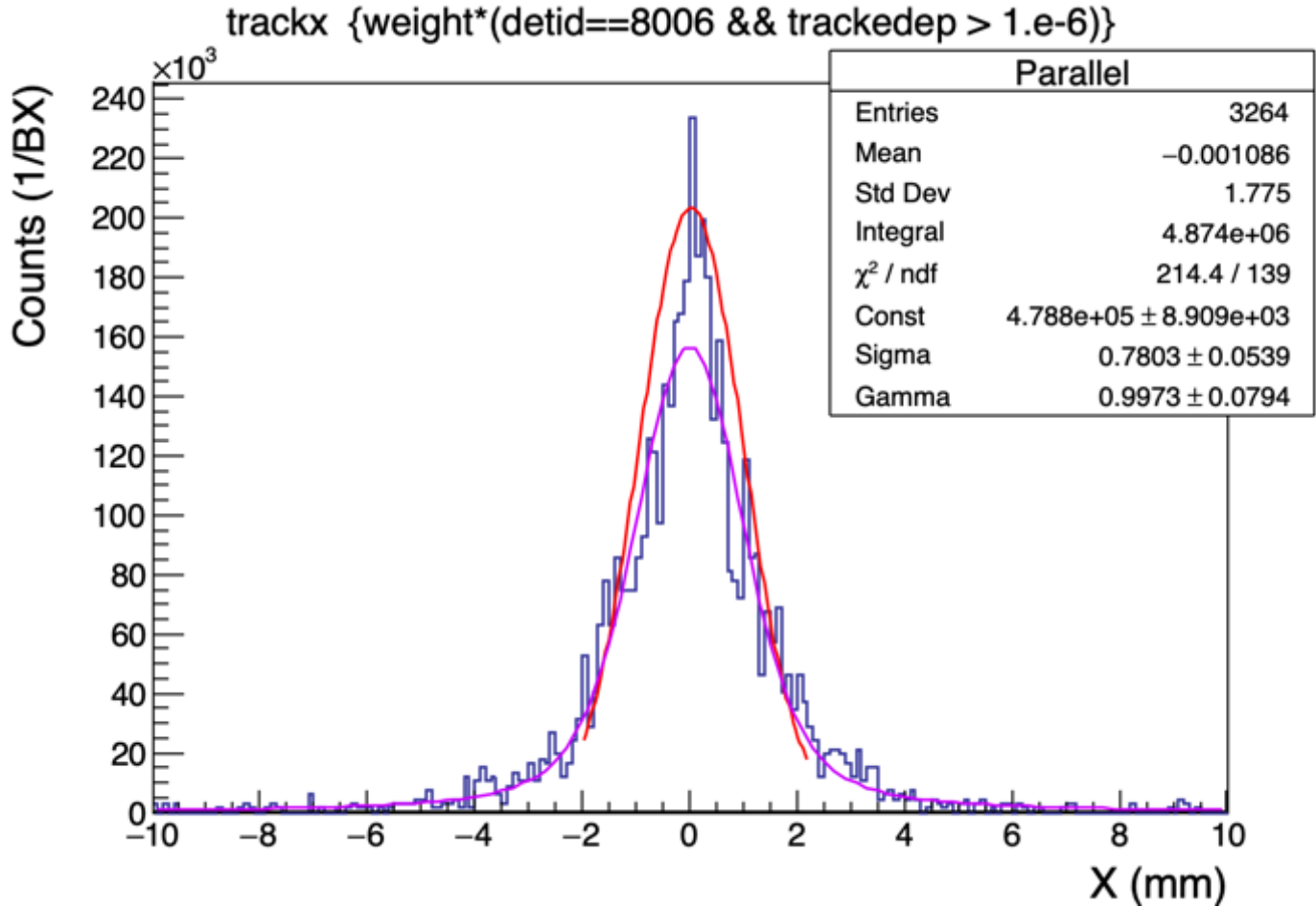
Fit Results

Upstream Profiler - Voigt

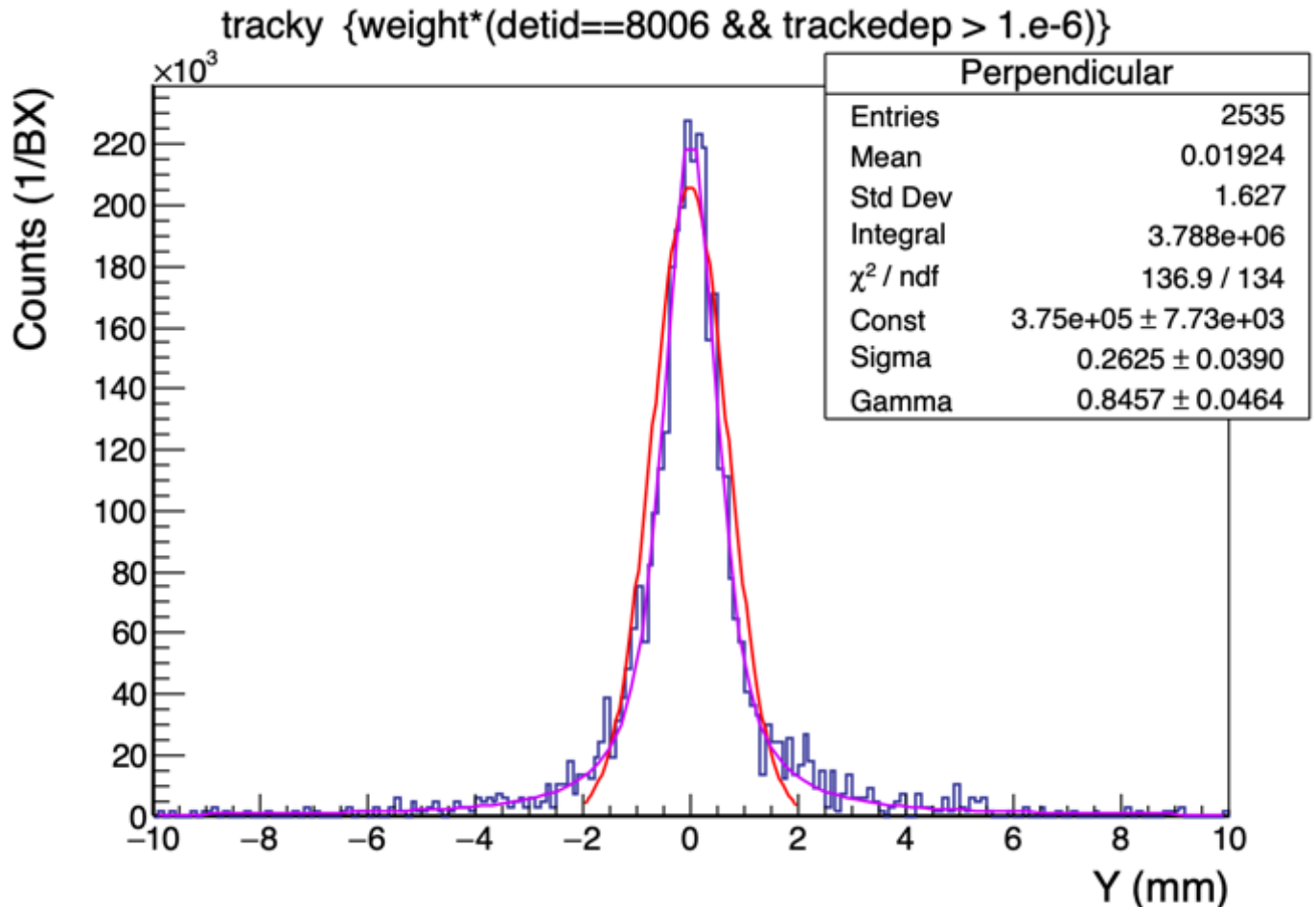
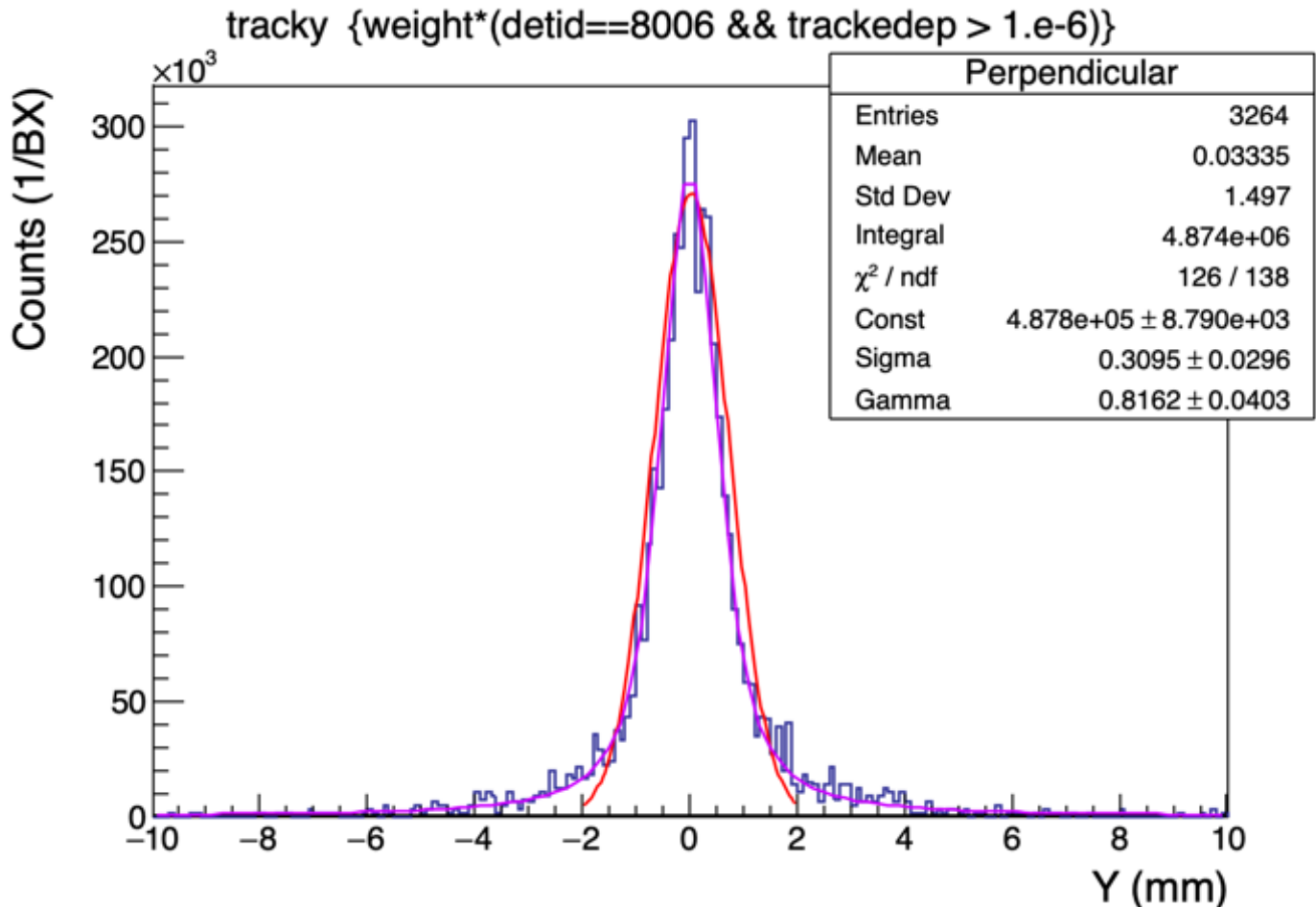
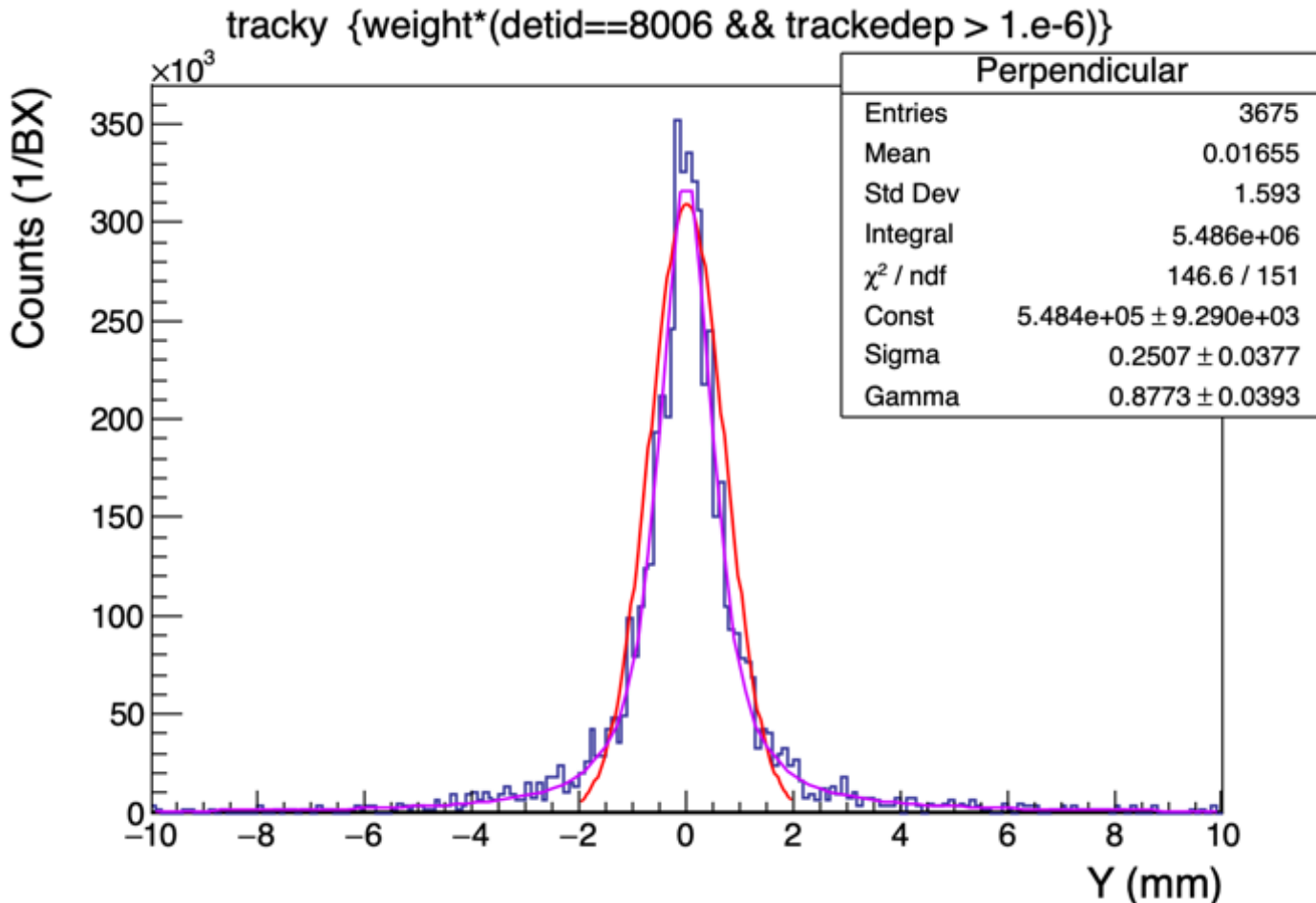
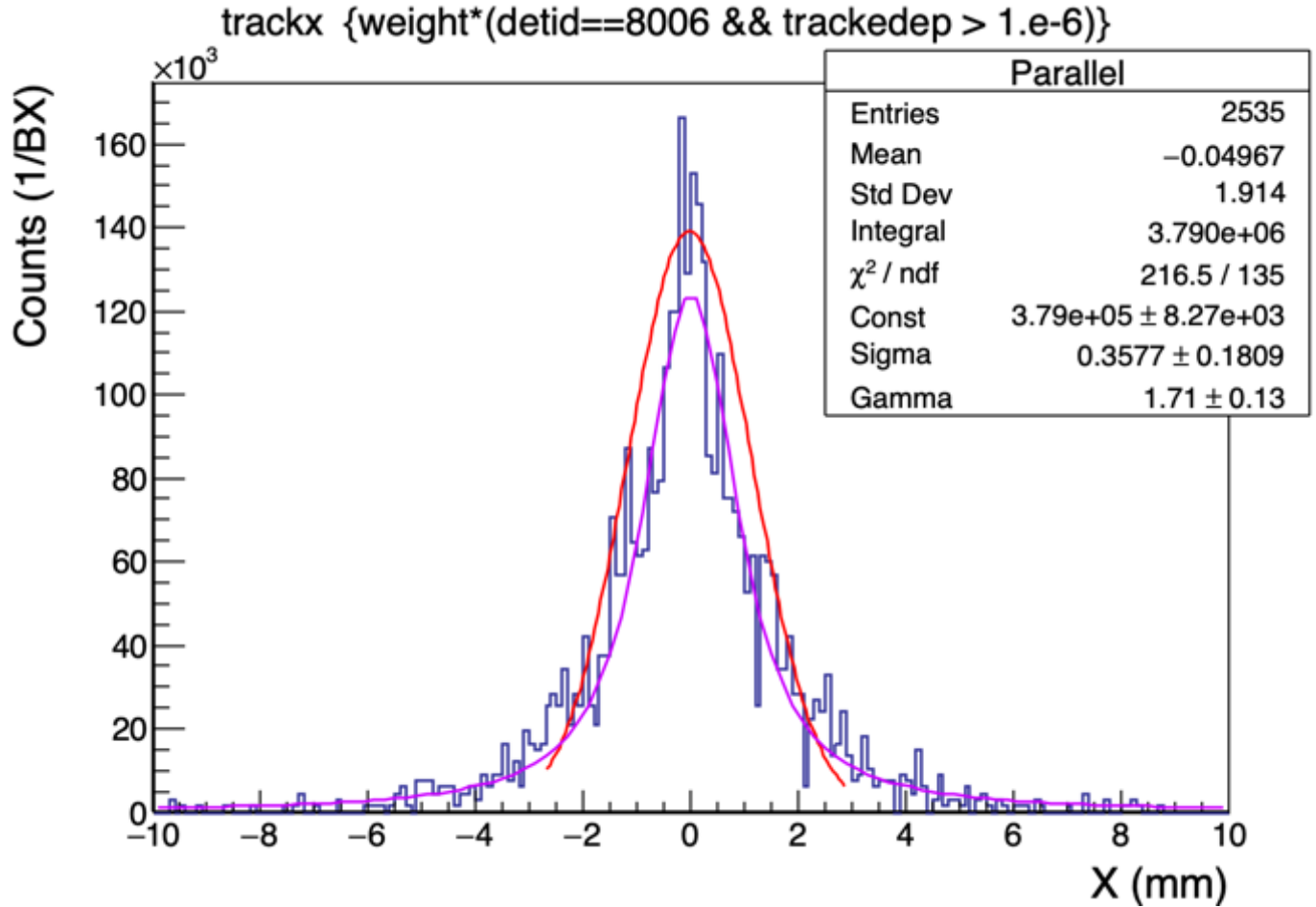
$$\xi = 5$$



$$\xi = 7$$



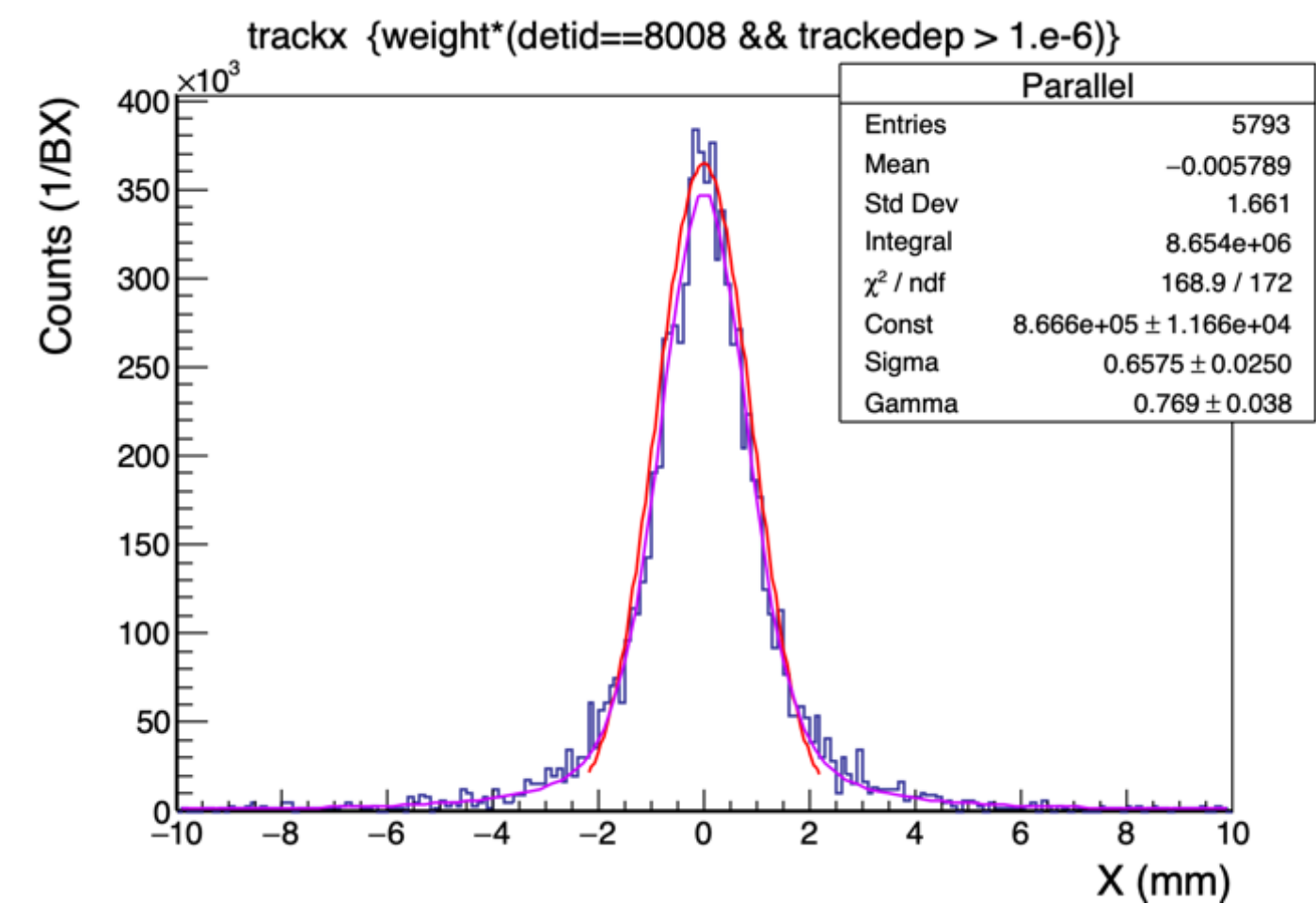
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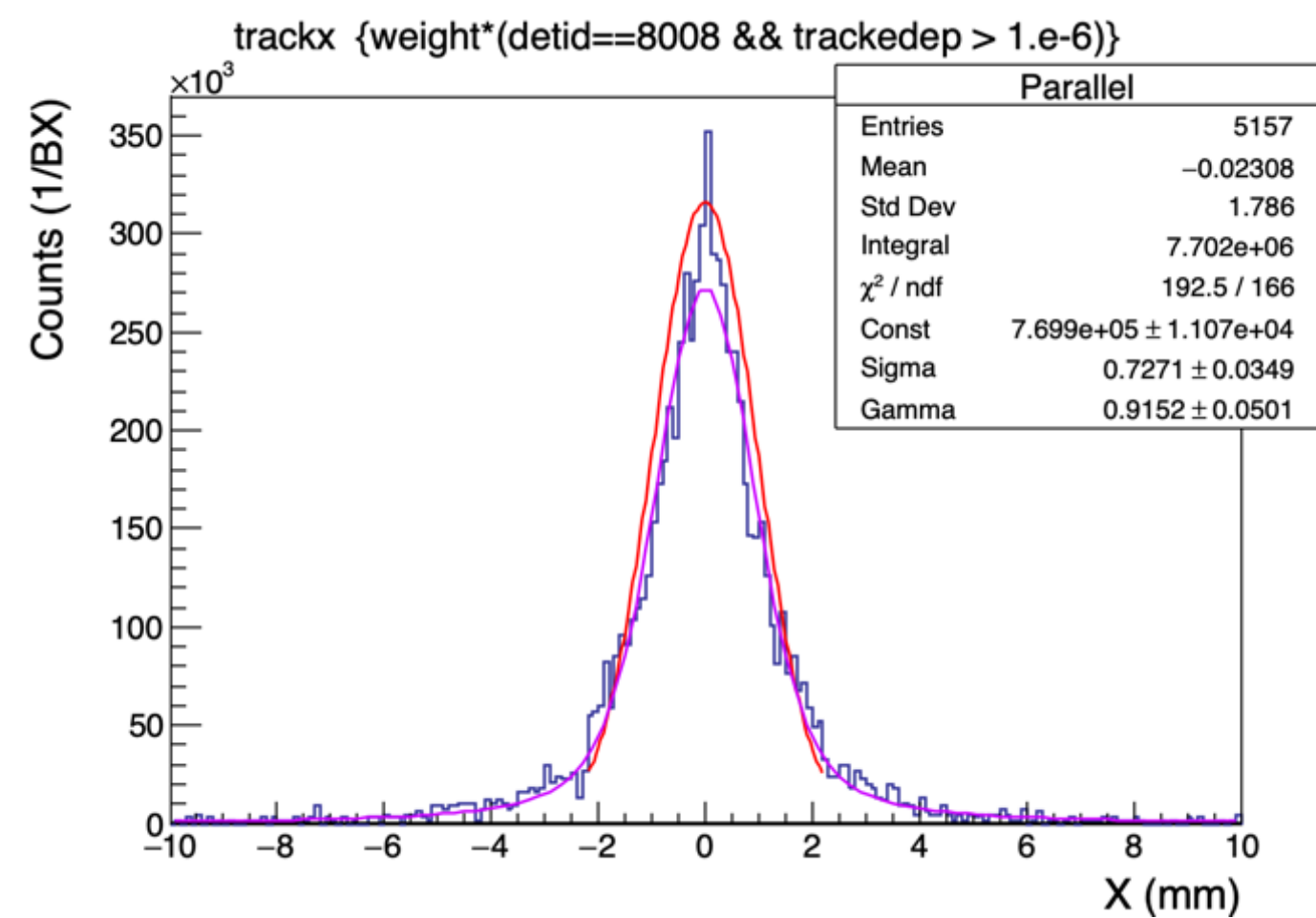
Fit Results

Downstream Profiler - Voigt

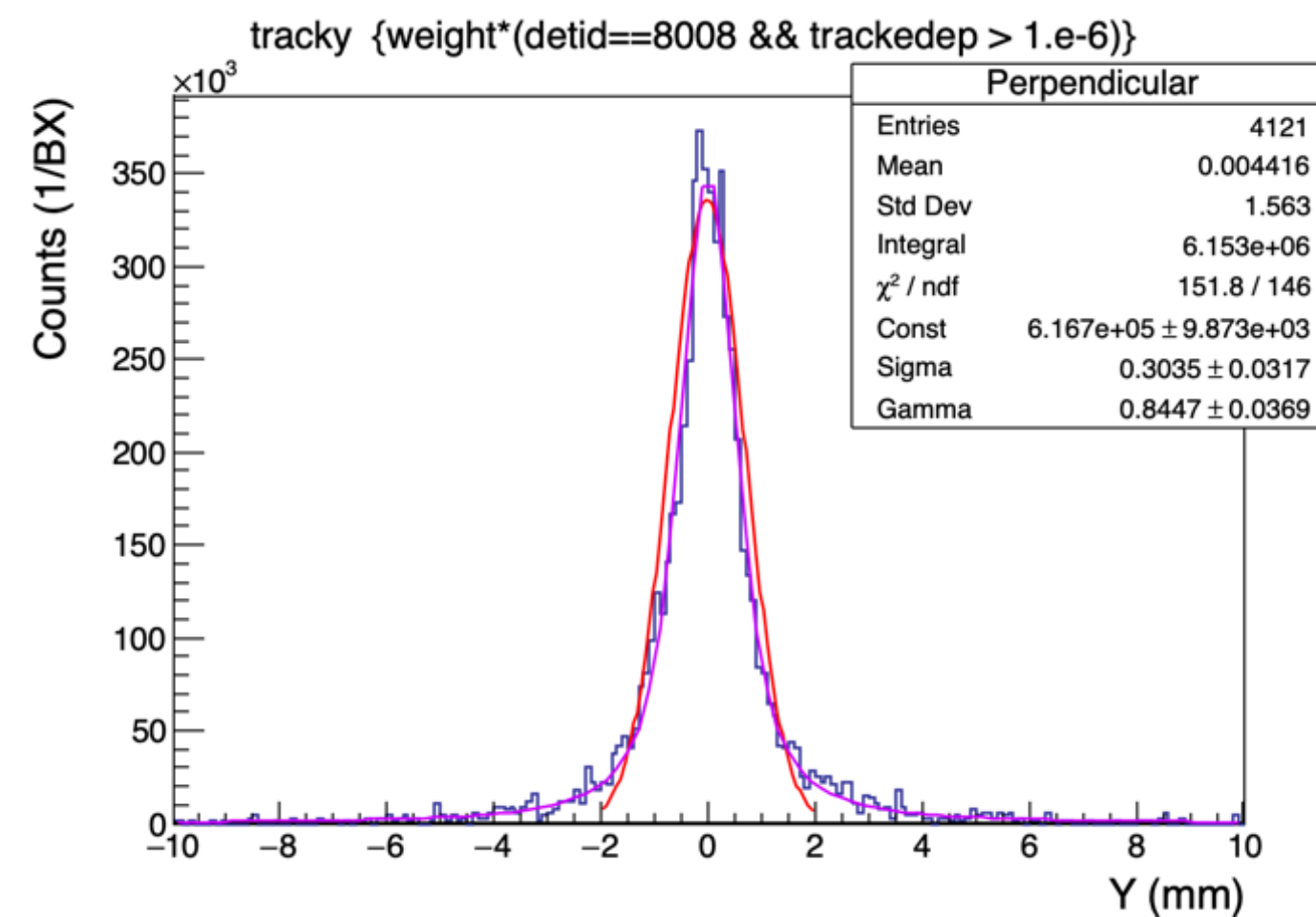
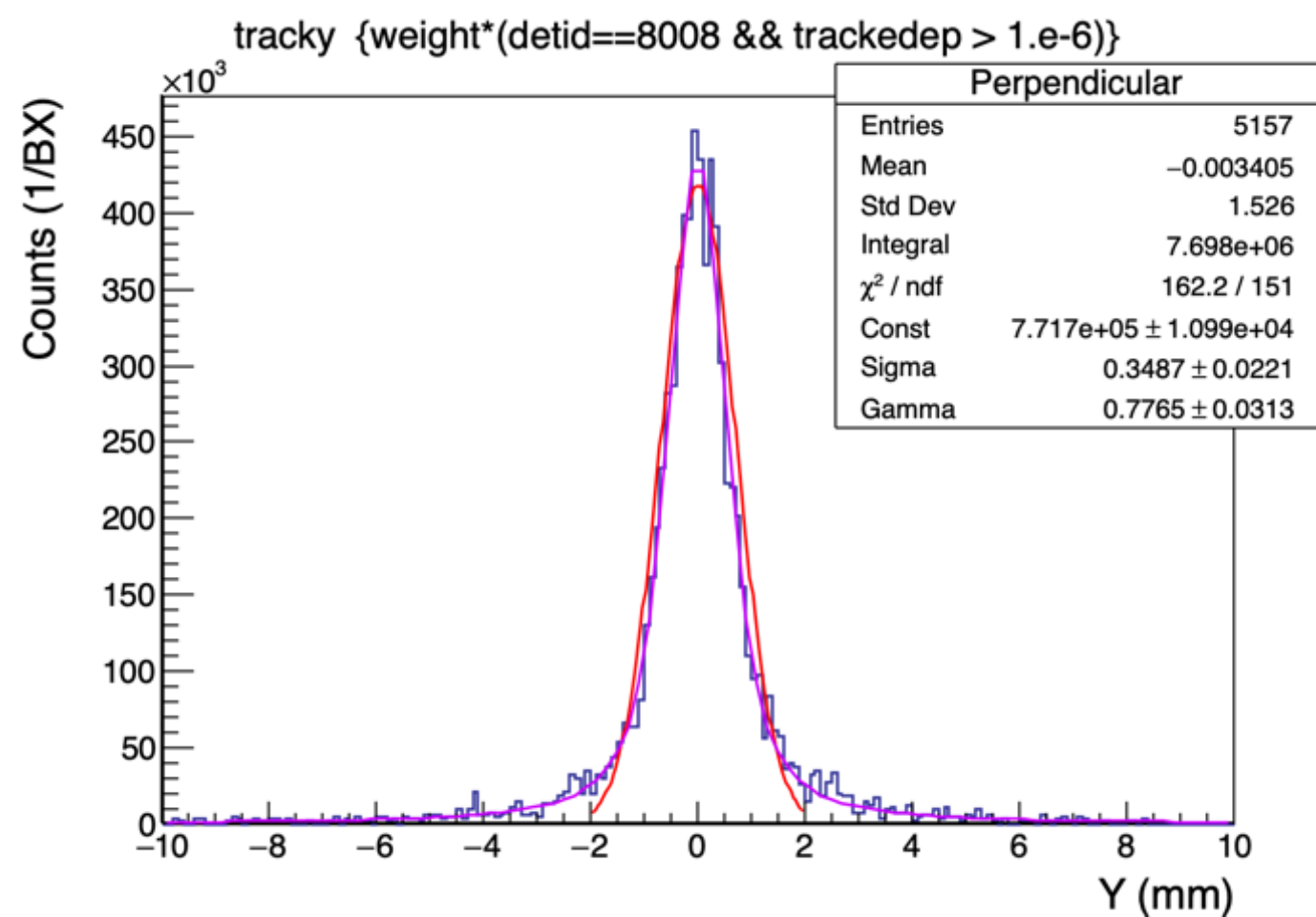
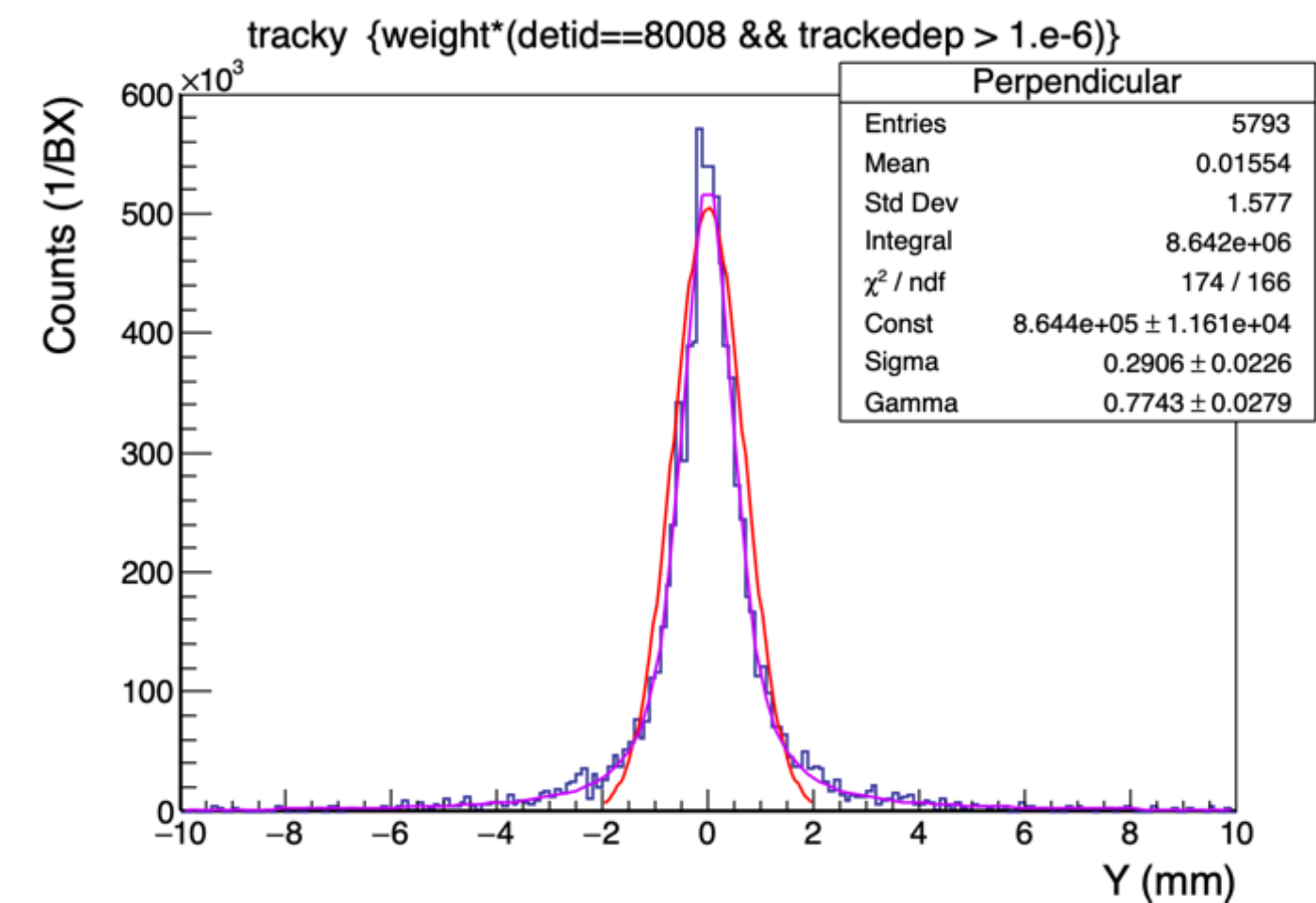
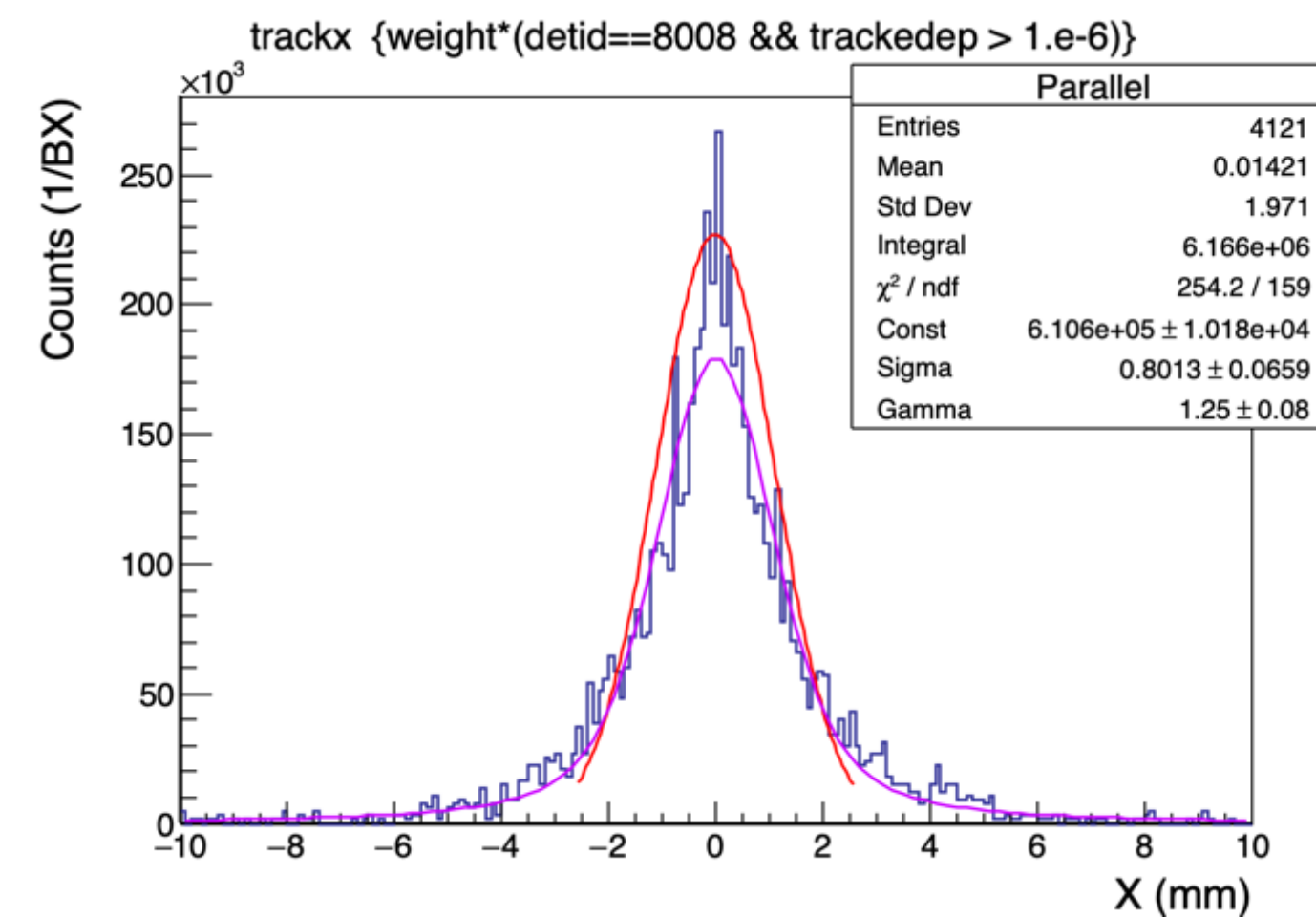
$$\xi = 5$$



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Dose Estimation

- Dose is defined as

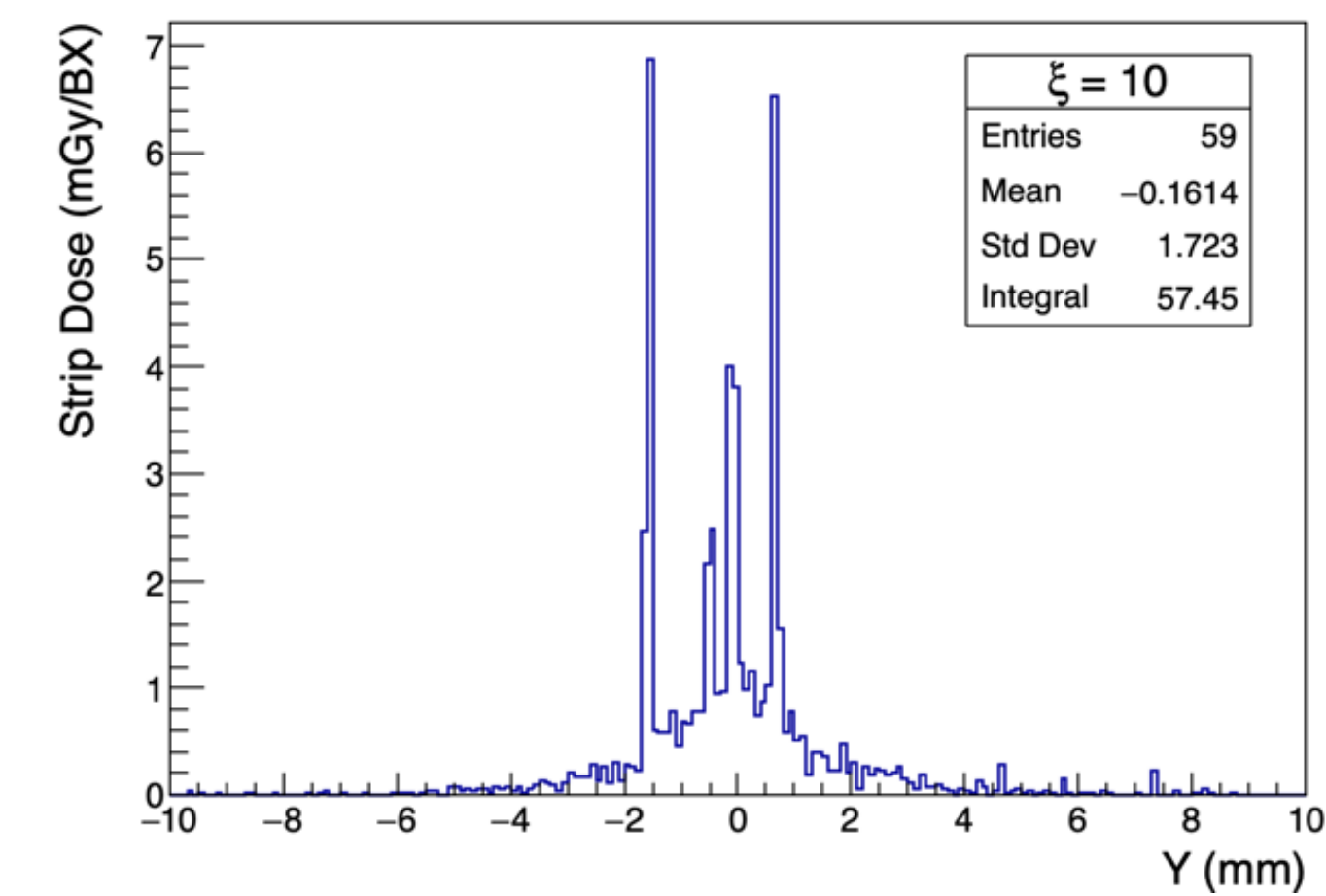
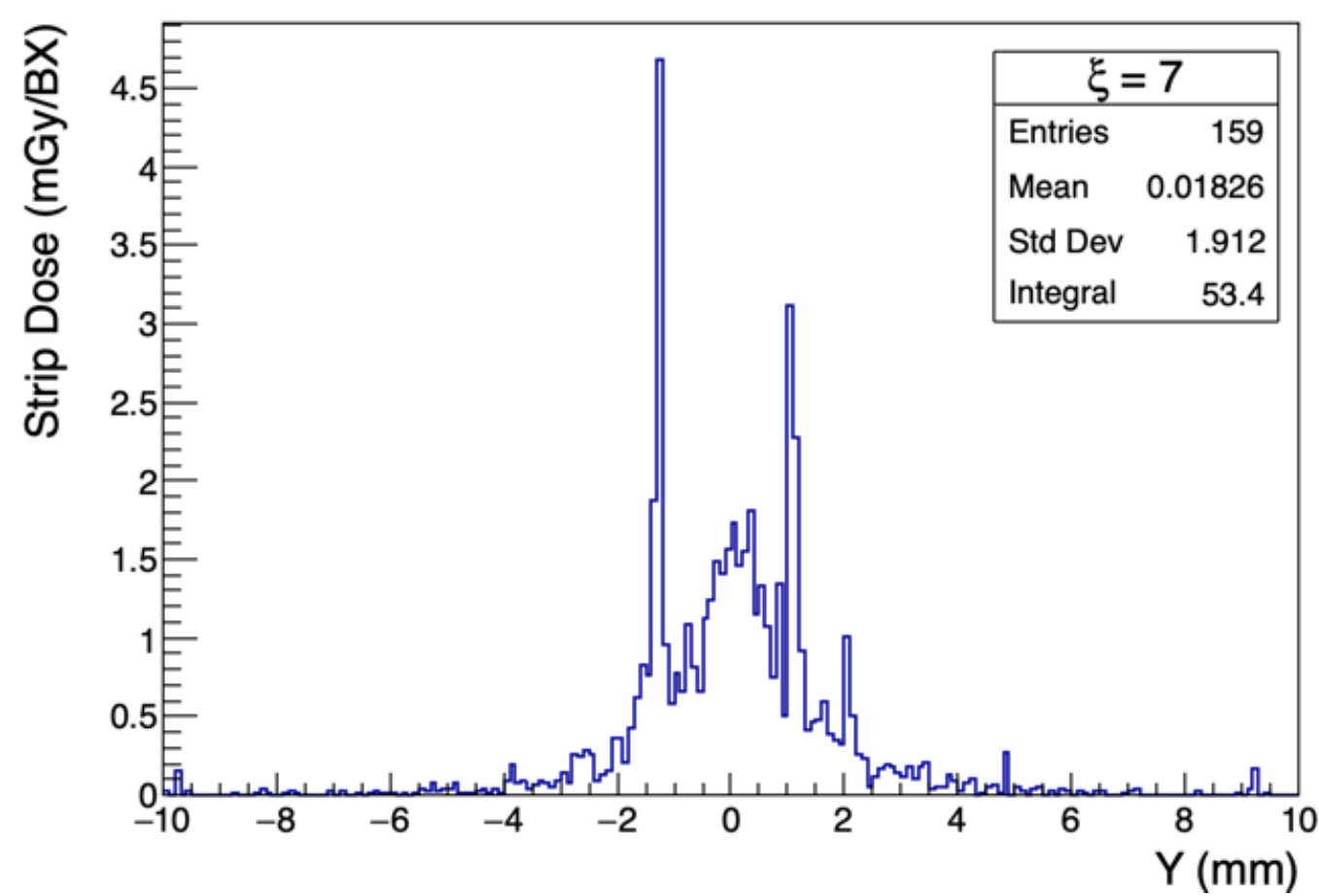
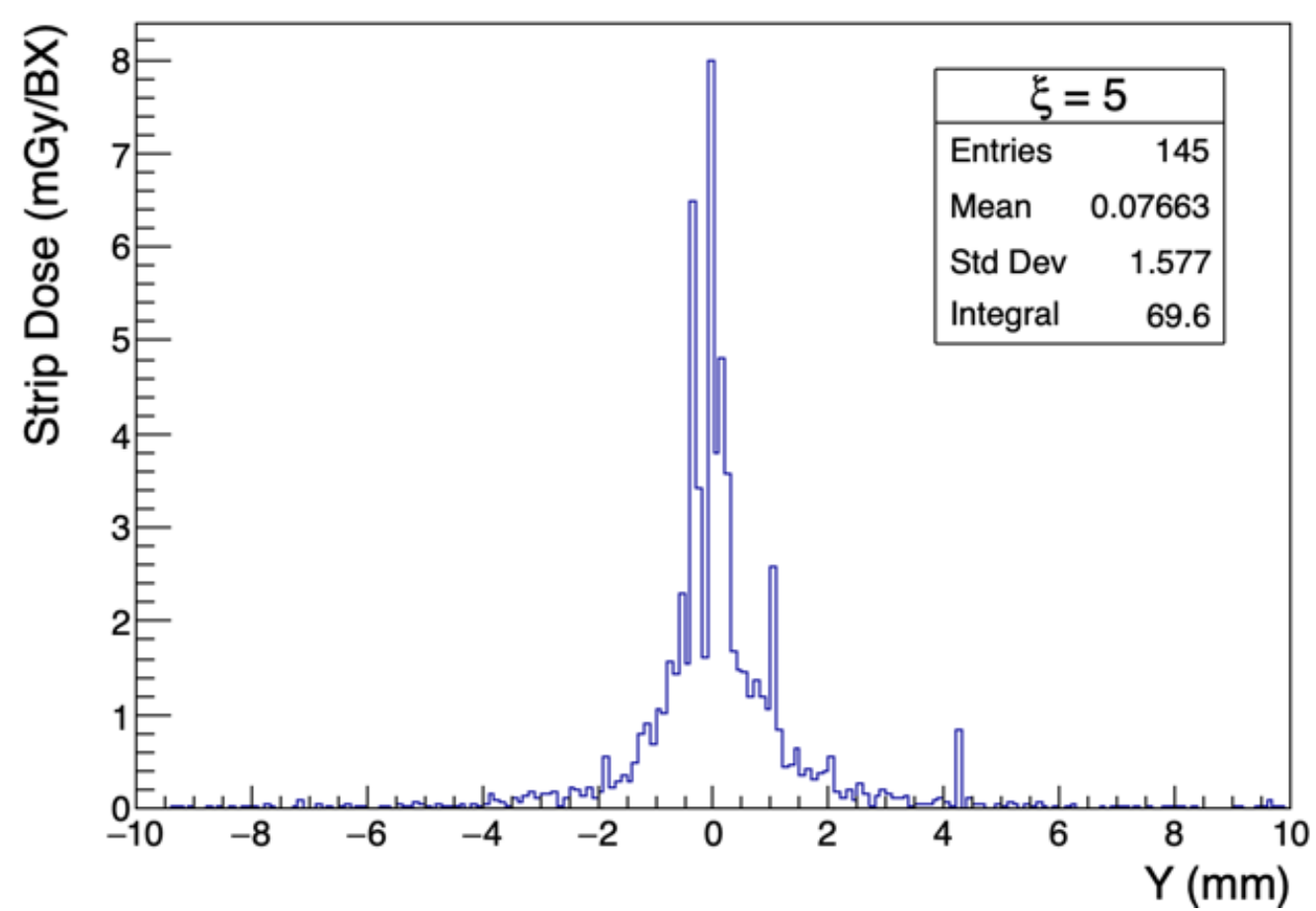
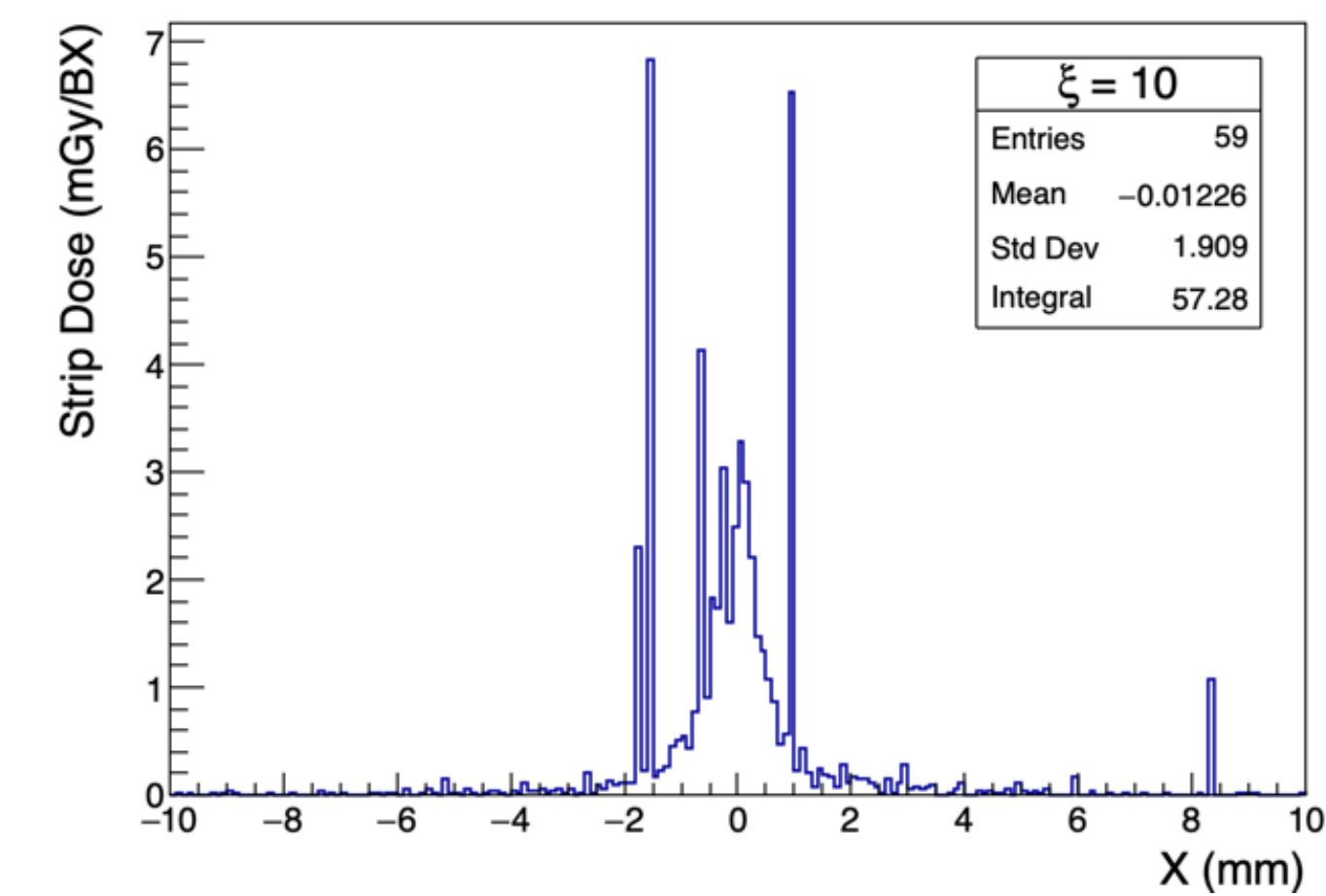
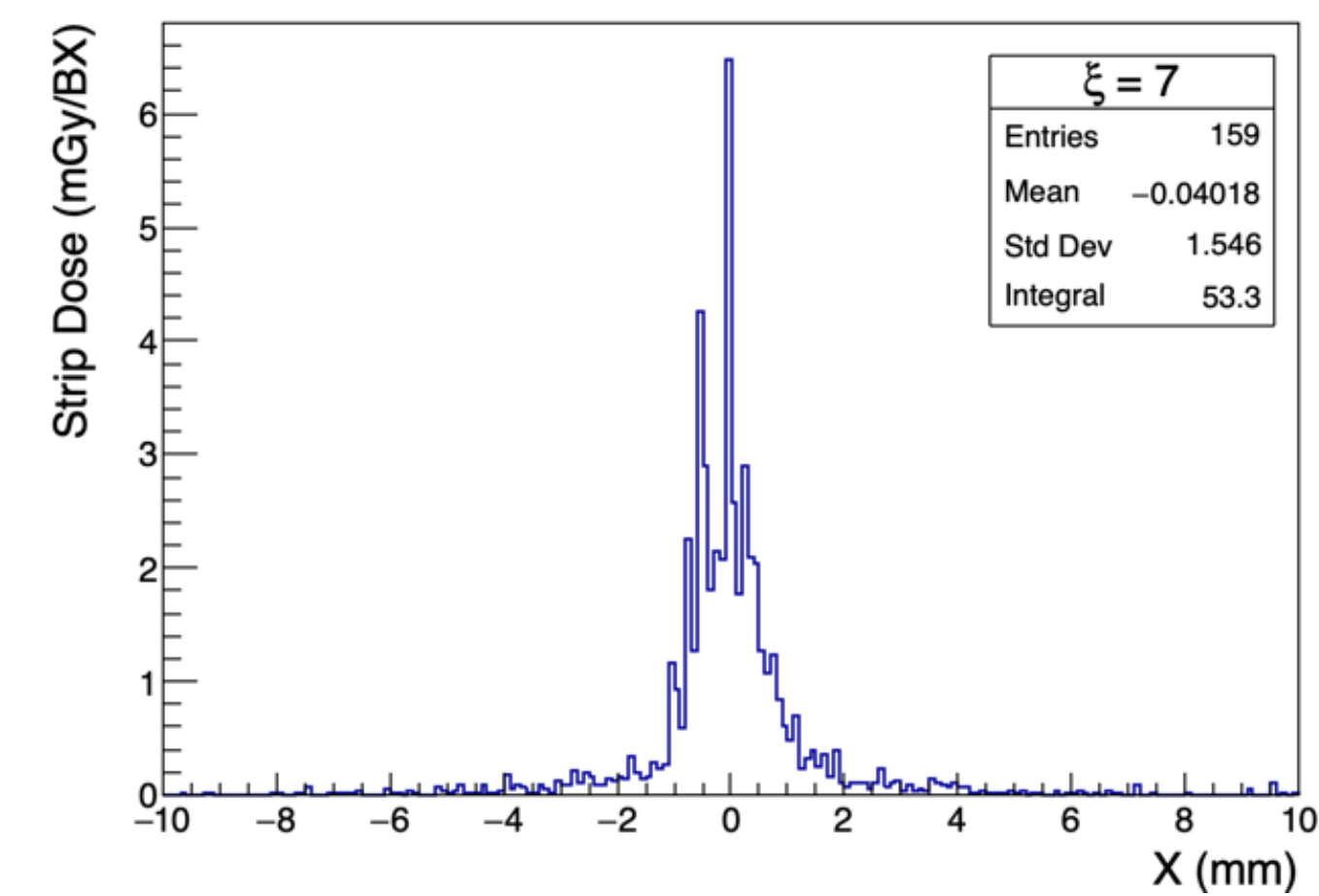
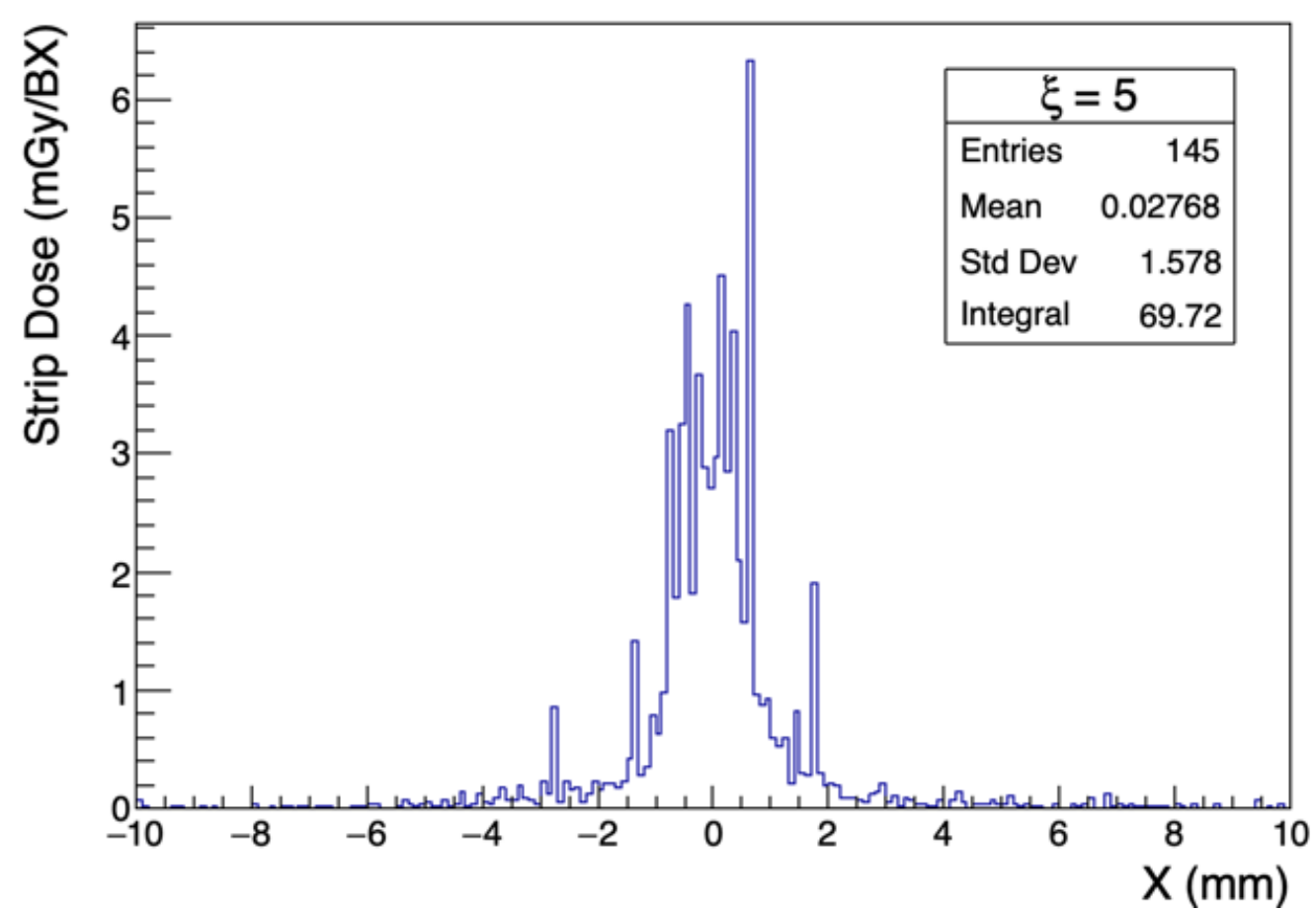
$$D[\text{Gy}] = \frac{\text{Energy Deposited}}{\text{Mass of Absorber}} = 1.60 \times 10^{-7} \cdot \frac{E_{dep}[\text{GeV}]}{\rho[\text{g/cm}^3]V[\text{cm}^3]}$$

- Following Pietro's analysis, two dose quantities of interest:
 - Total (average) dose (dose absorbed by the entire profiler volume)
 - Strip dose (dose absorbed by each strip)
- For total dose, define active area to be a circle which contains $p = 95\%$ of hits:

$$r_{X,Y} = \sigma_{X,Y} \sqrt{-2 \ln(1 - p)}$$

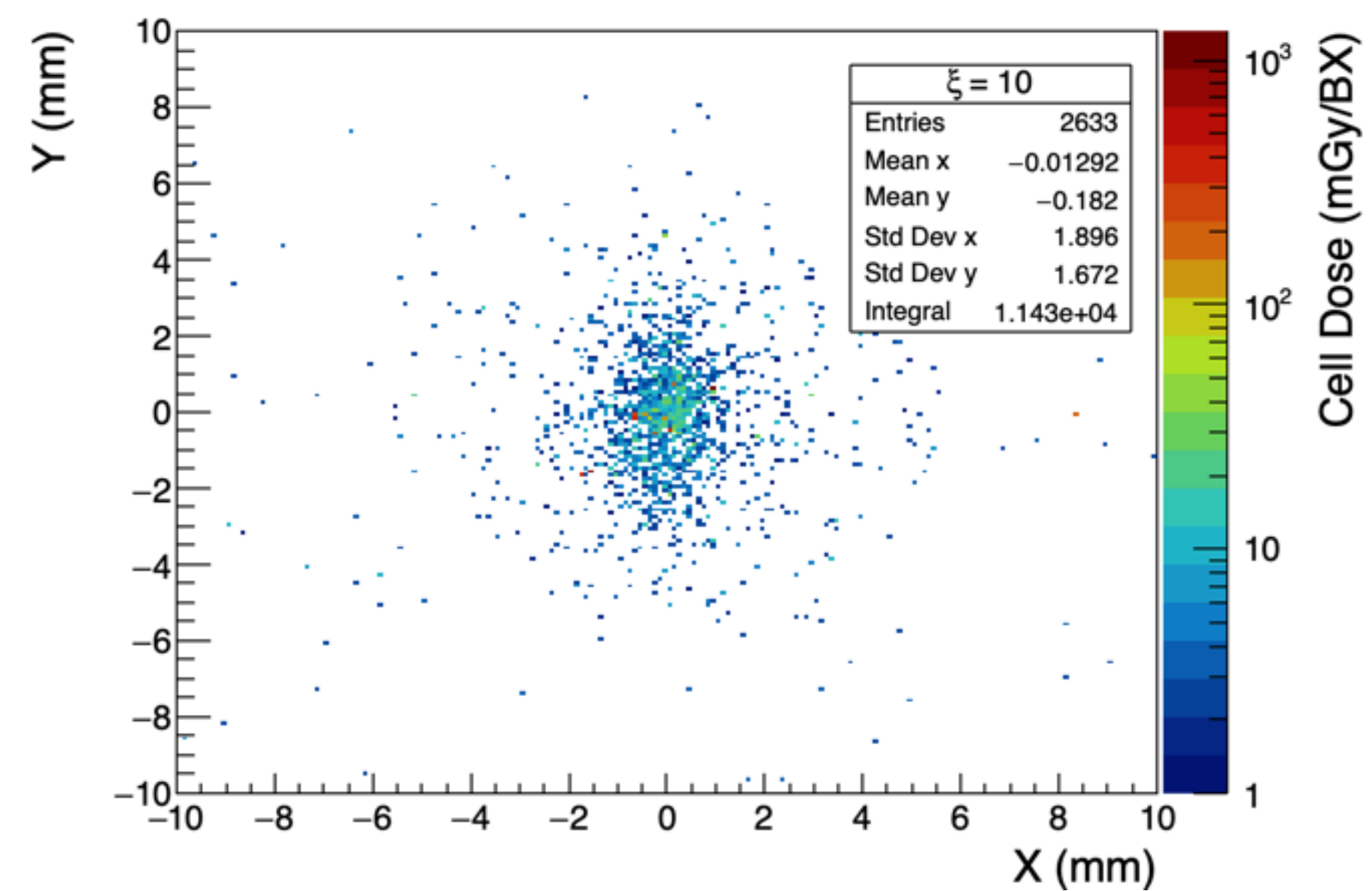
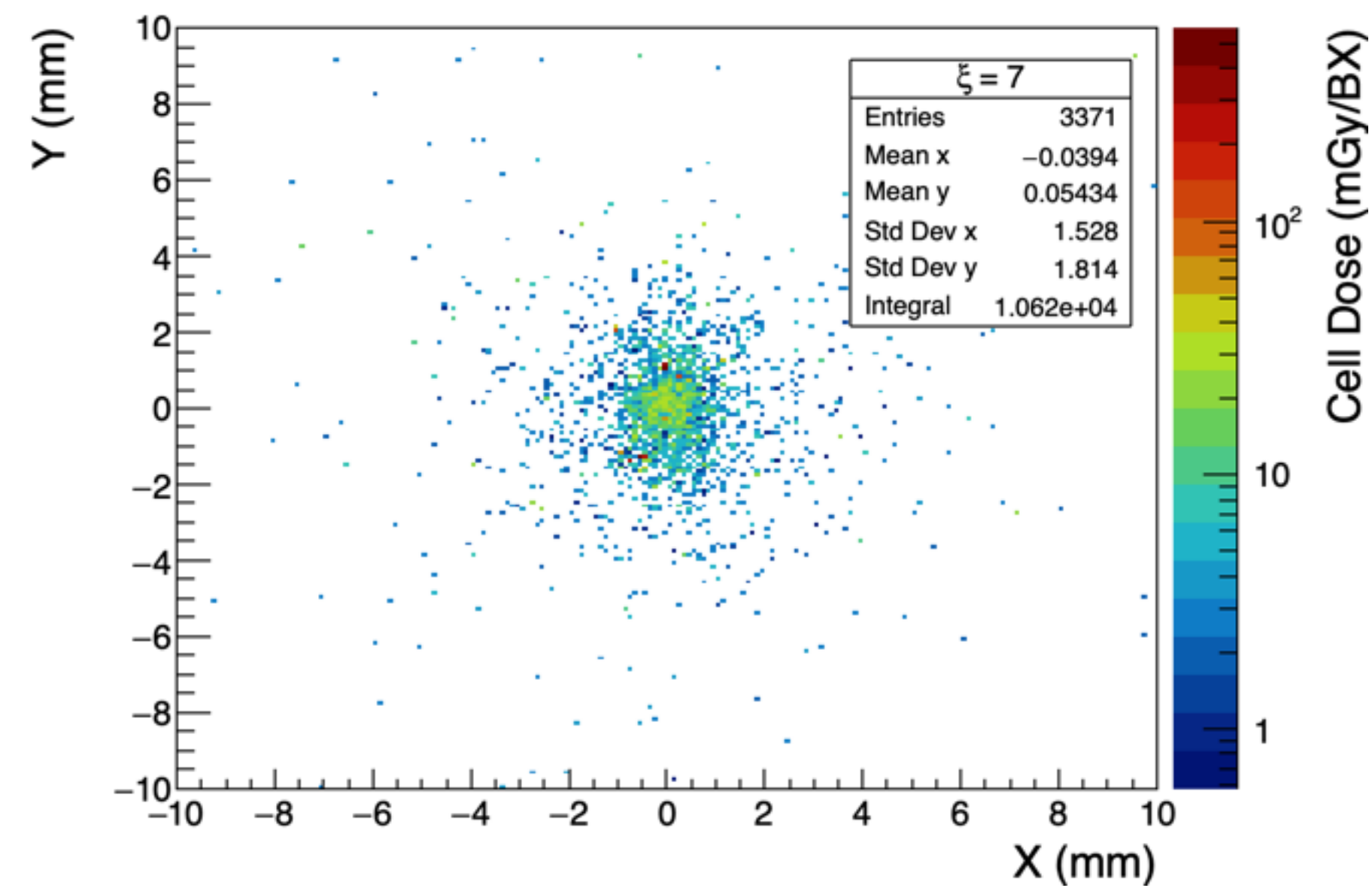
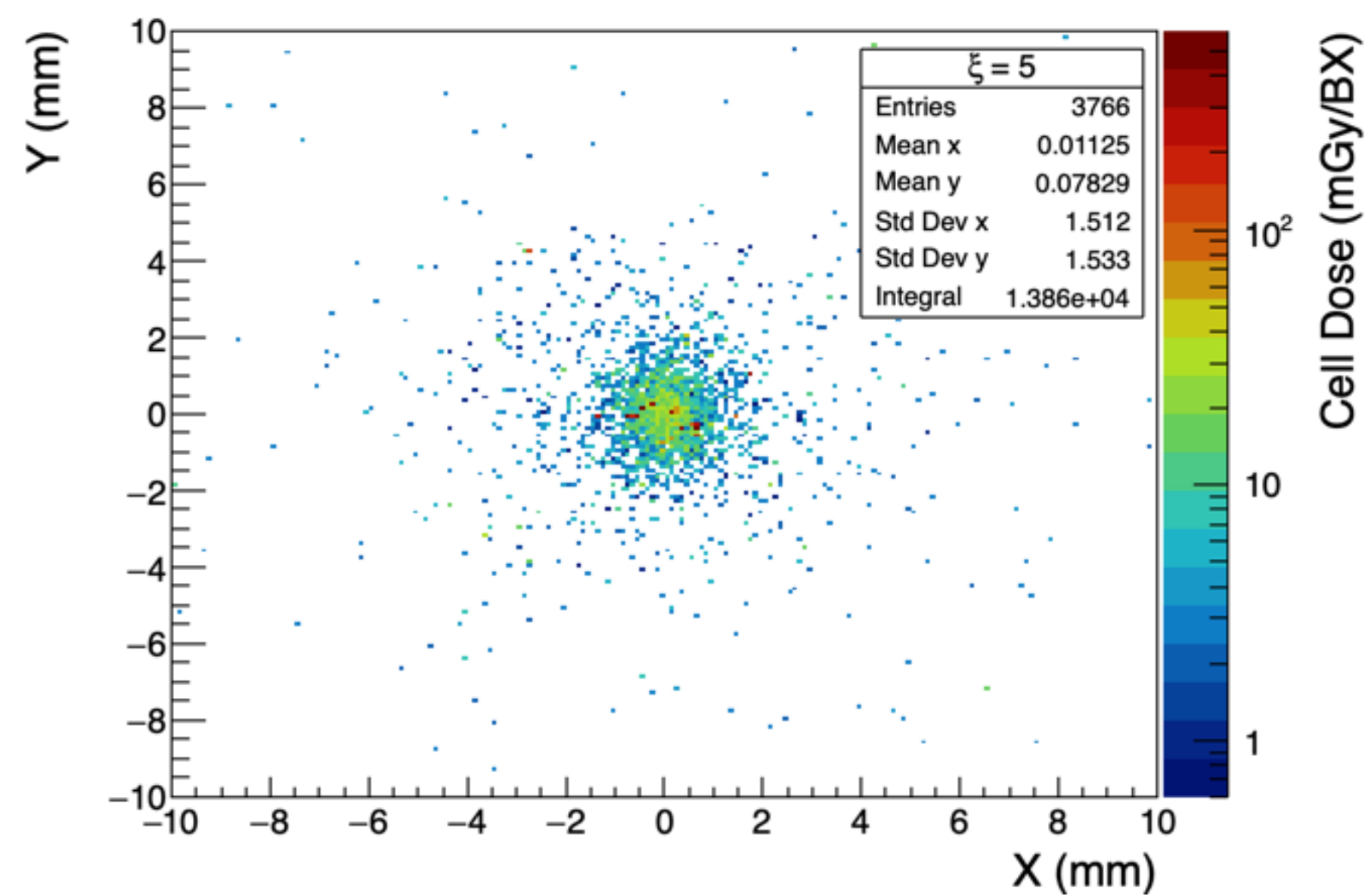
Dose Estimation

Strip Dose - Upstream



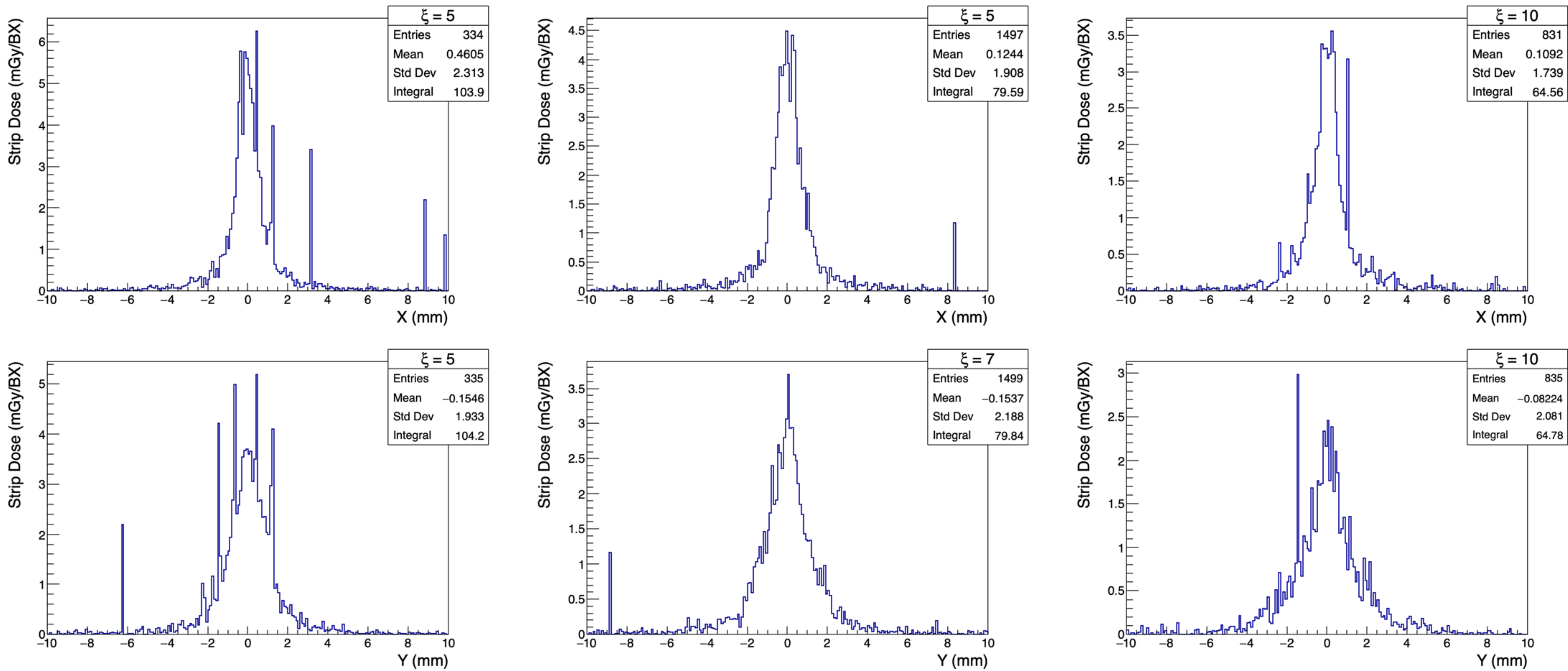
Dose Estimation

Cell Dose - Upstream



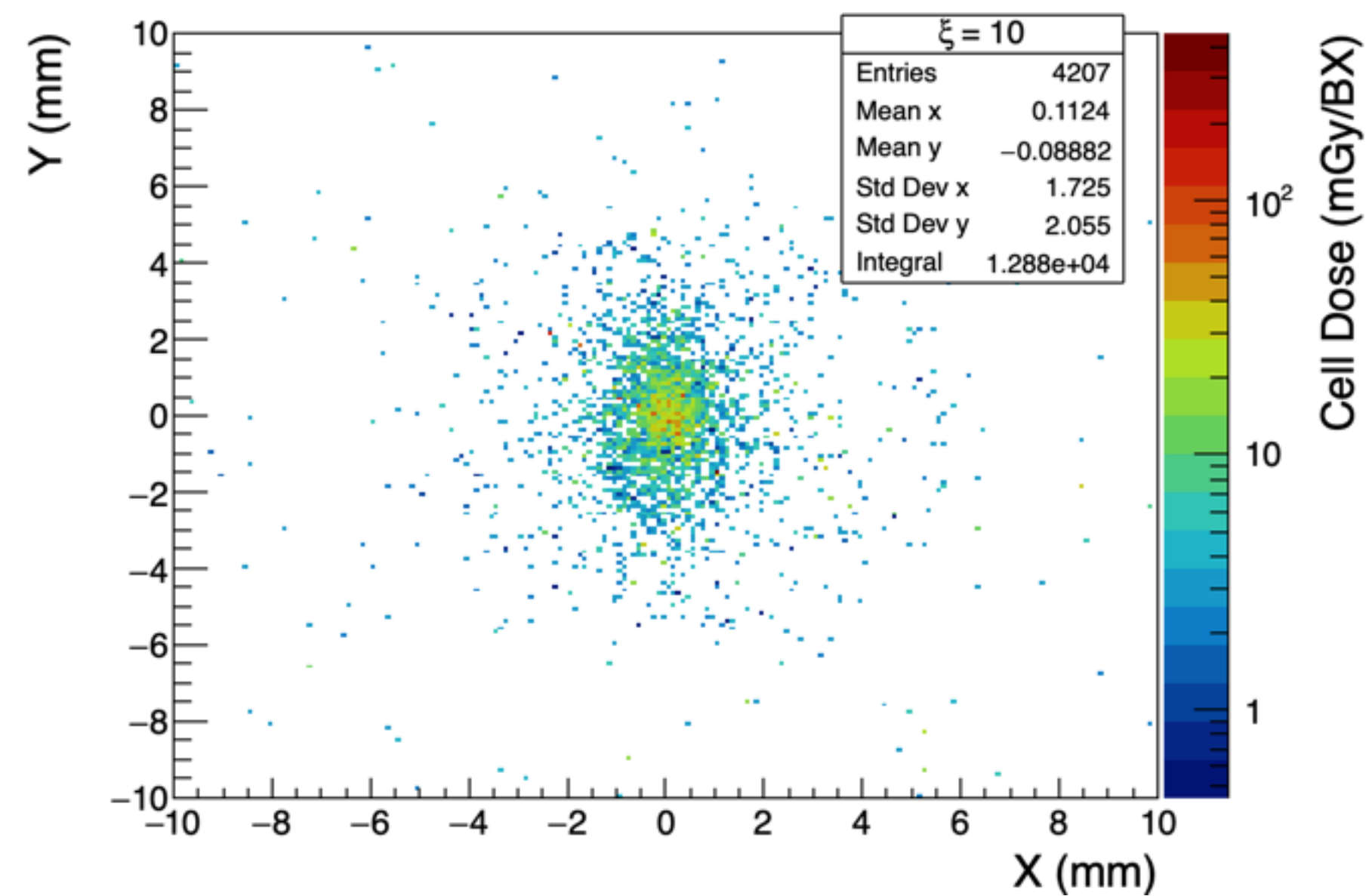
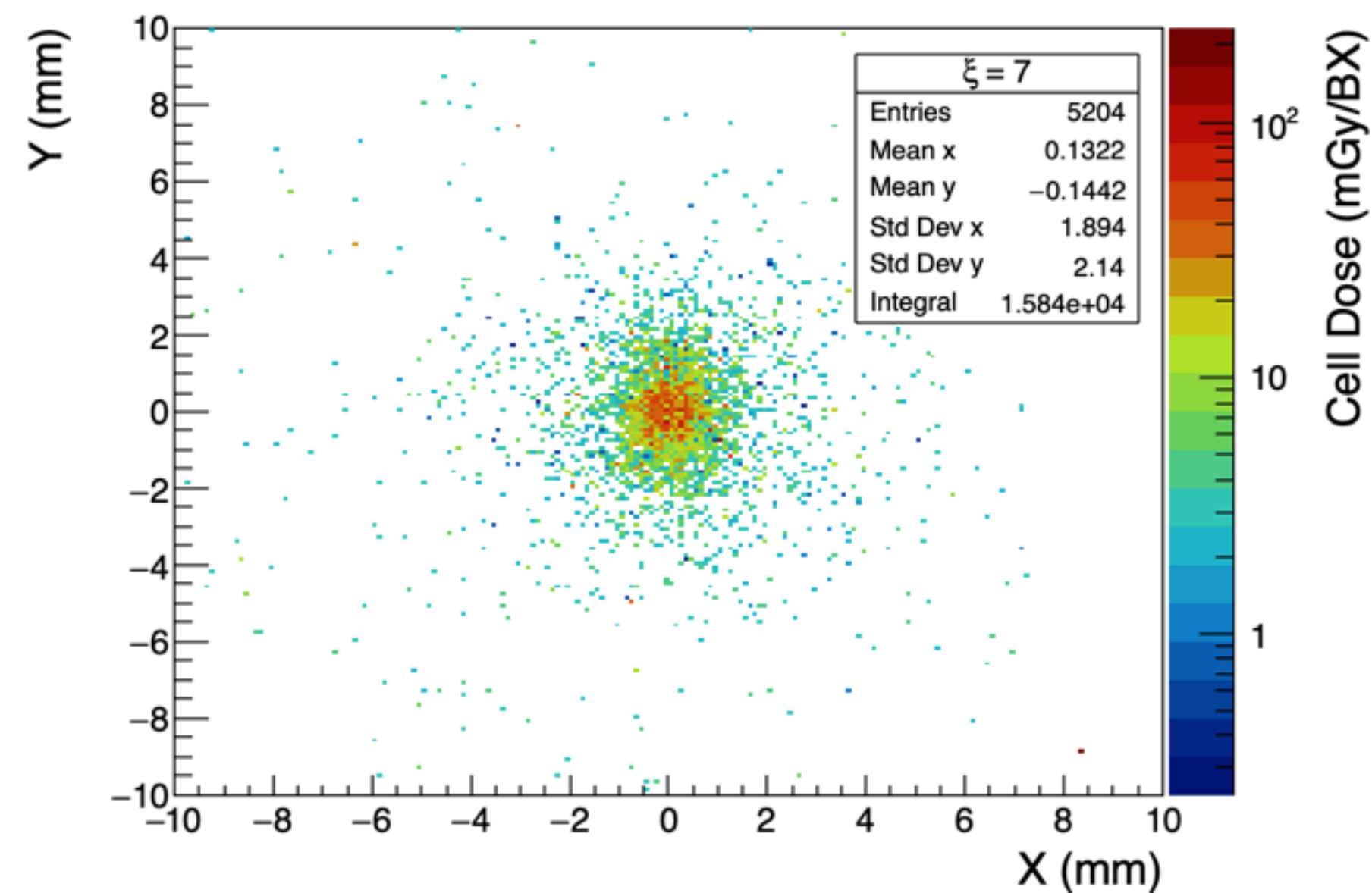
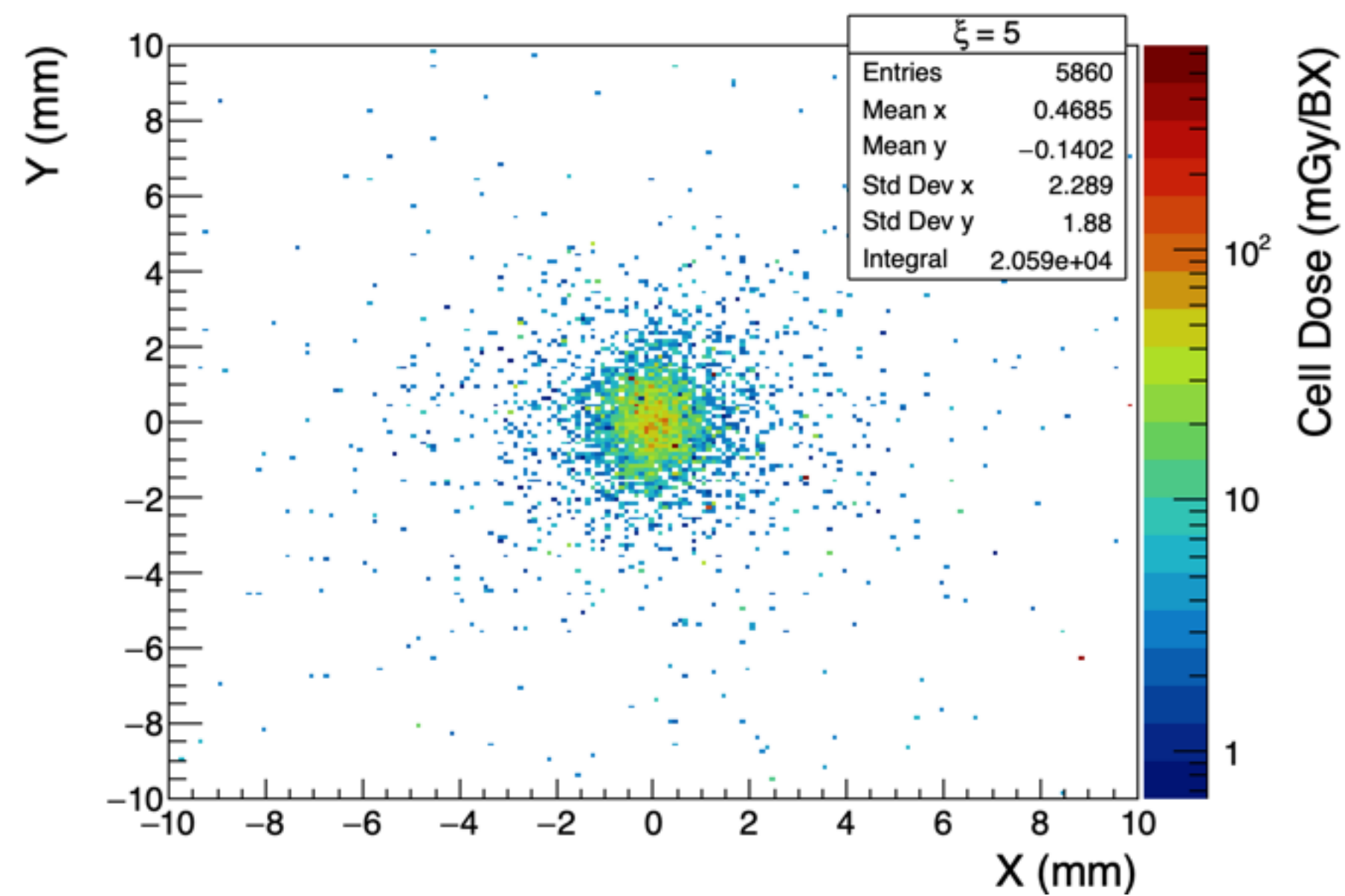
Dose Estimation

Strip Dose - Downstream



Dose Estimation

Cell Dose - Downstream



Dose Estimation

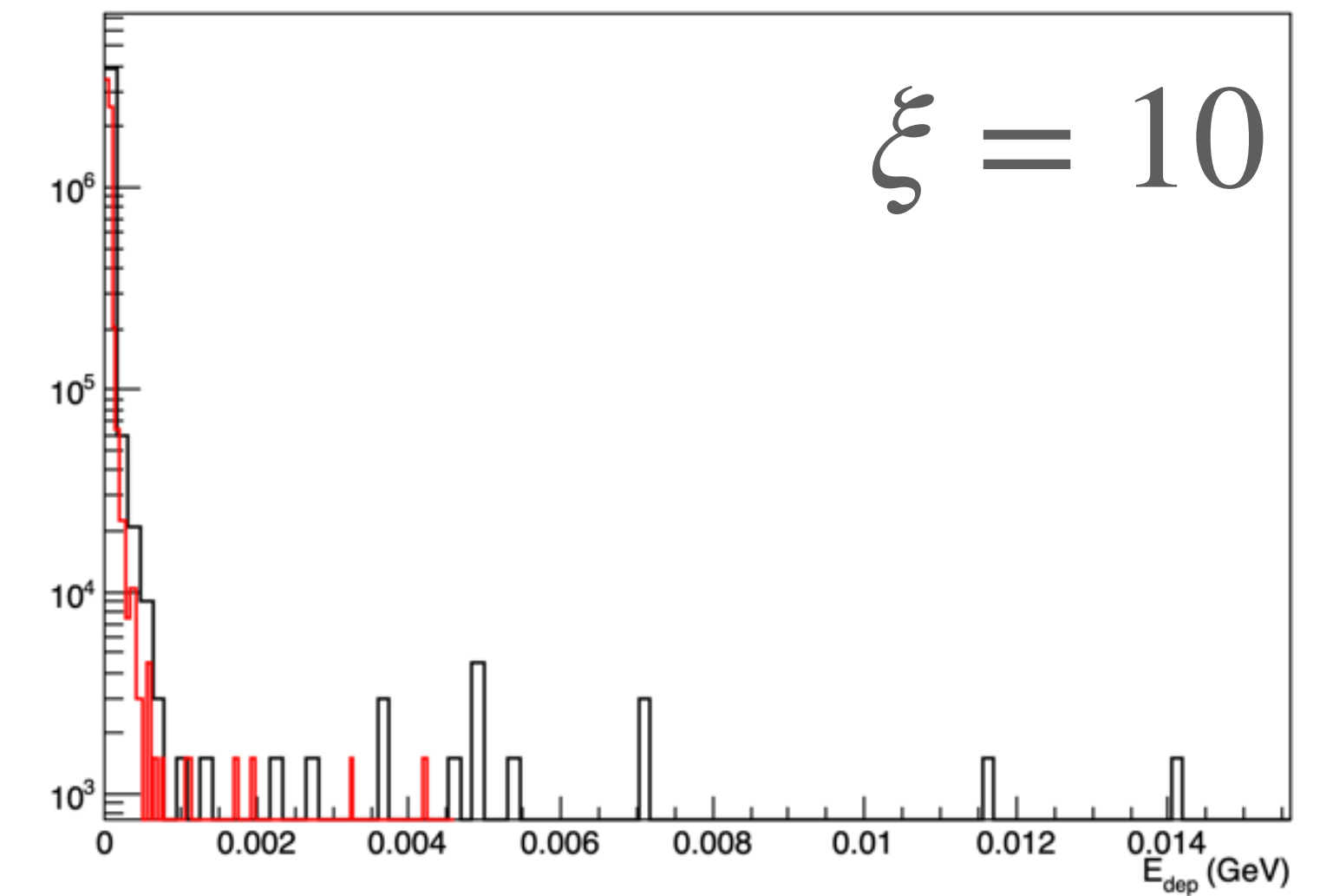
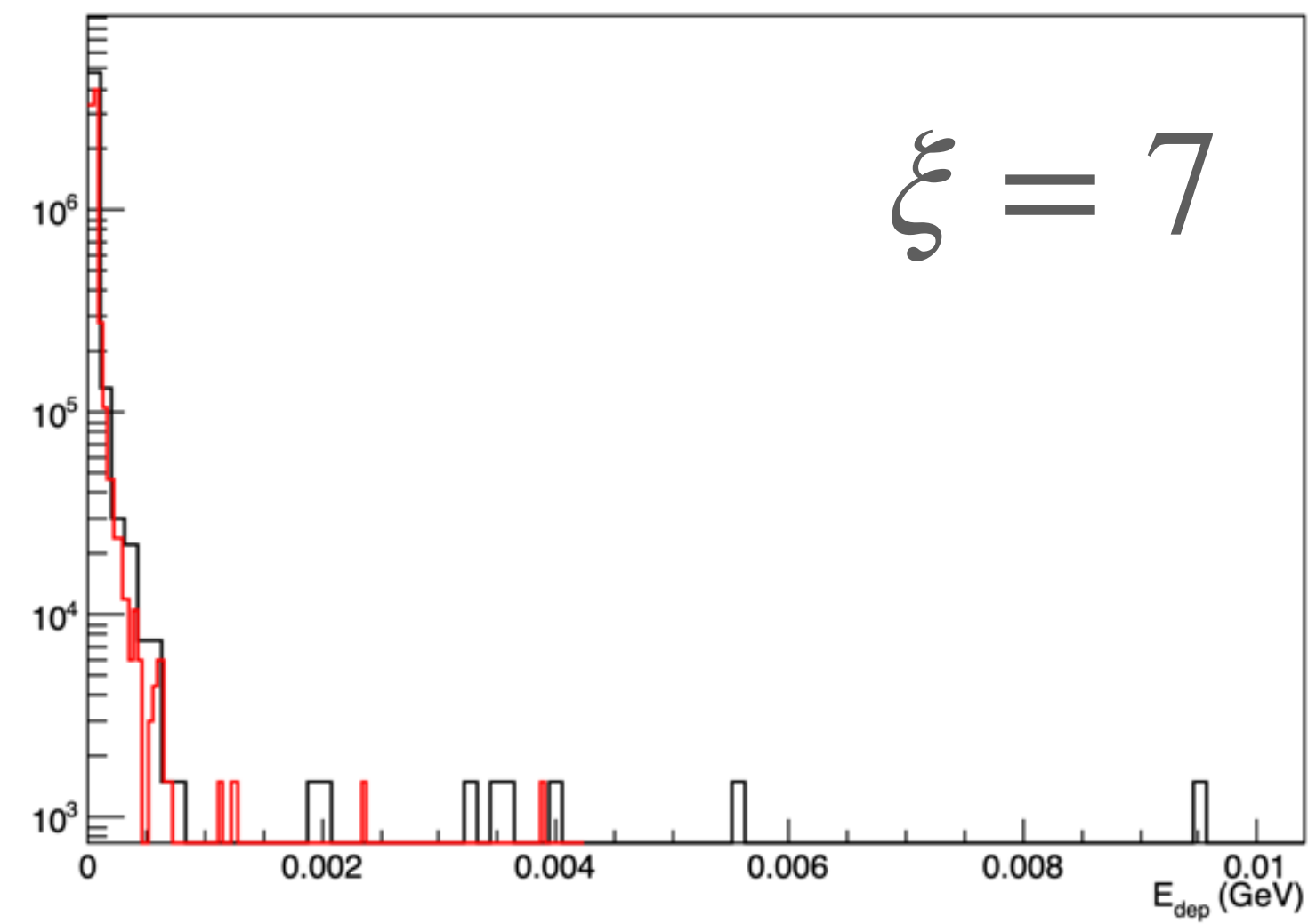
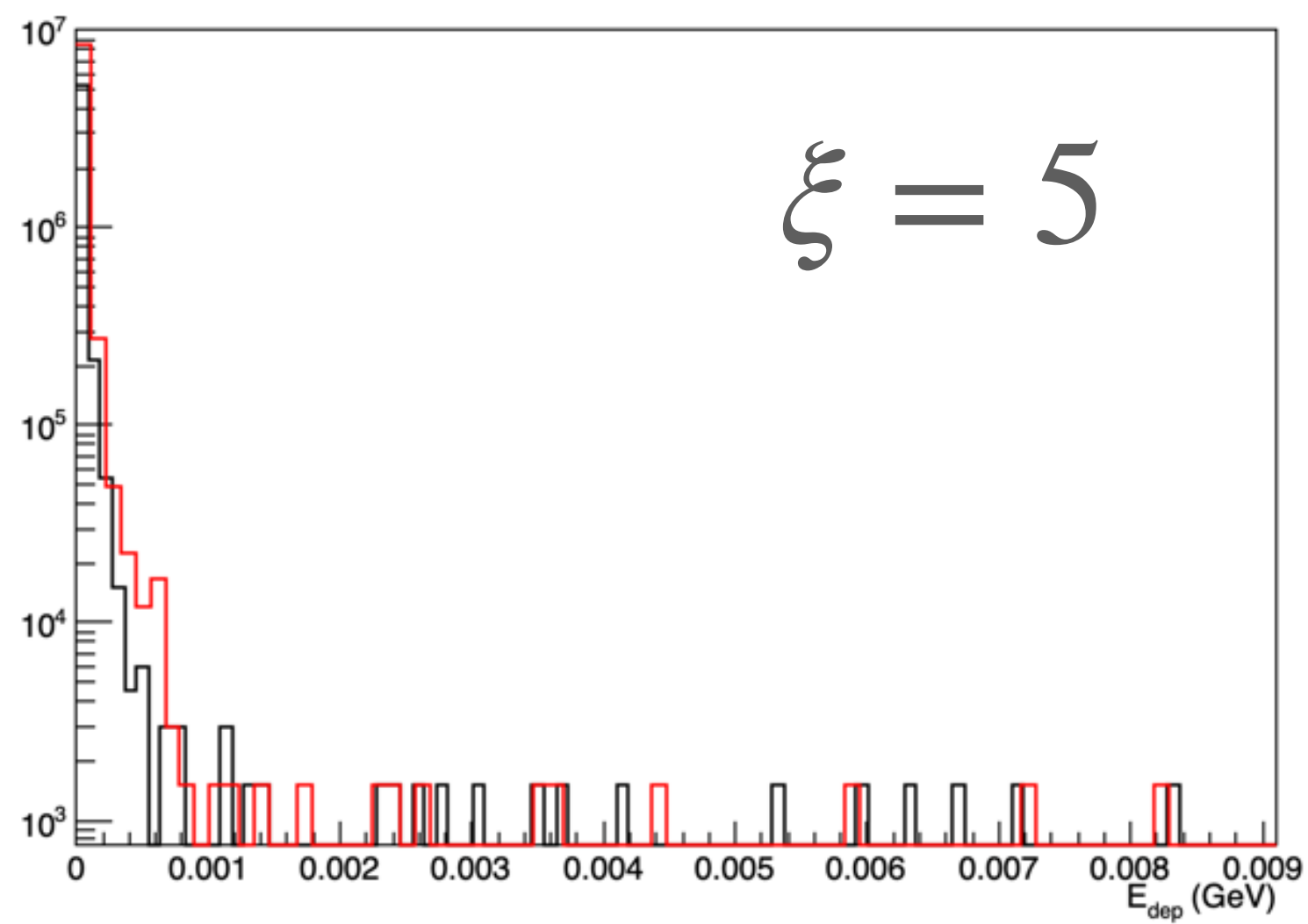
Comparison

Xi	Radius (mm) X Y		Total Energy Deposition (GeV)	Total Dose (mGy)	Peak Energy Deposited (GeV)		Peak Dose (mGy)	
5	2.10	1.72	287.3	0.10	30.7	39.3	6.2	7.9
7	2.38	1.71	204.15	0.06	30.5	23.3	6.1	4.7
10	2.84	1.72	228.26	0.06	33.5	34.0	6.7	6.8
5	2.24	1.65	377.91	0.13	29.2	24.3	5.9	4.9
7	2.39	1.72	295.72	0.09	19.9	17.5	4.0	3.5
10	2.71	1.74	231.03	0.06	14.6	14.8	2.9	3.0

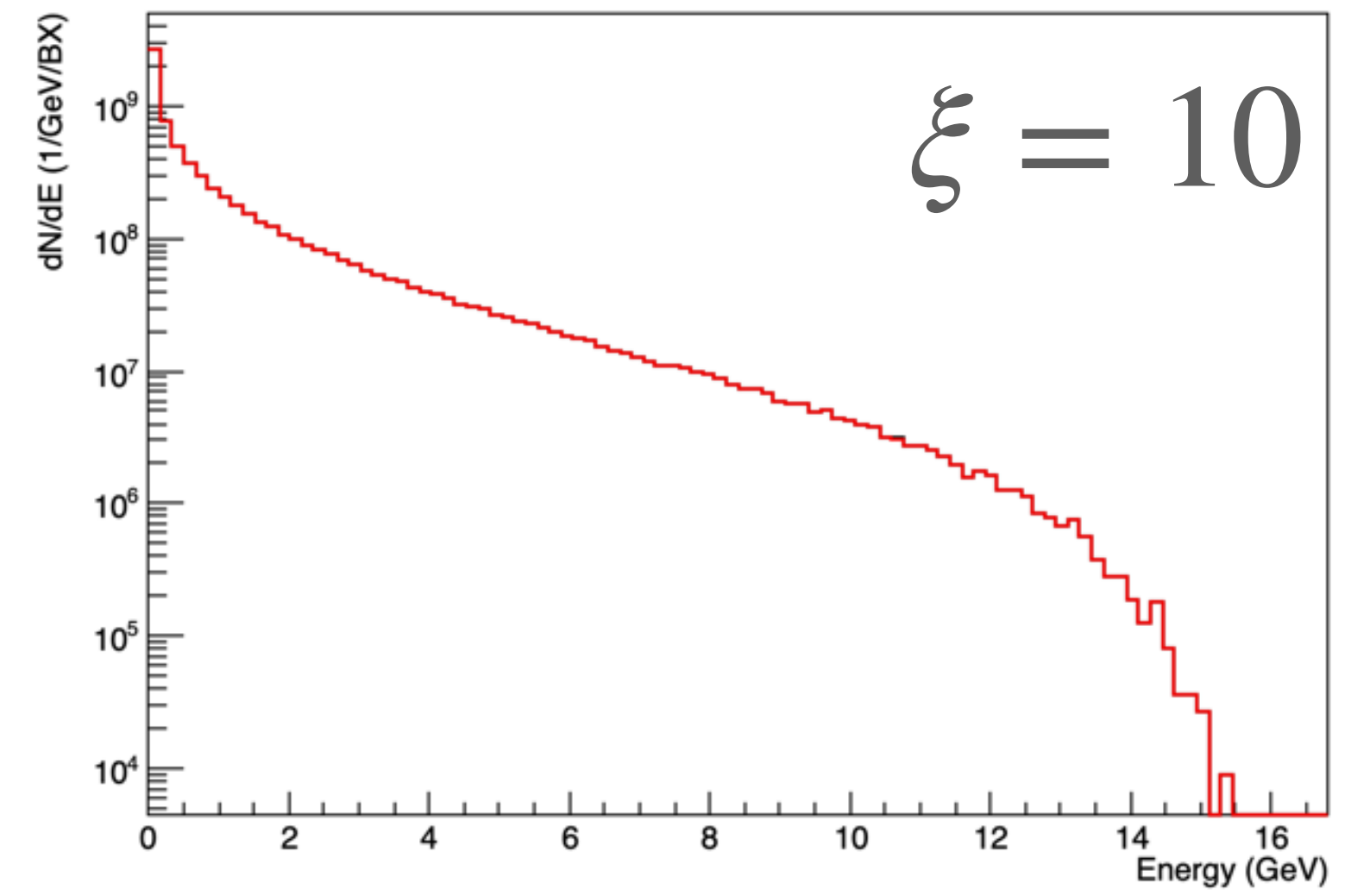
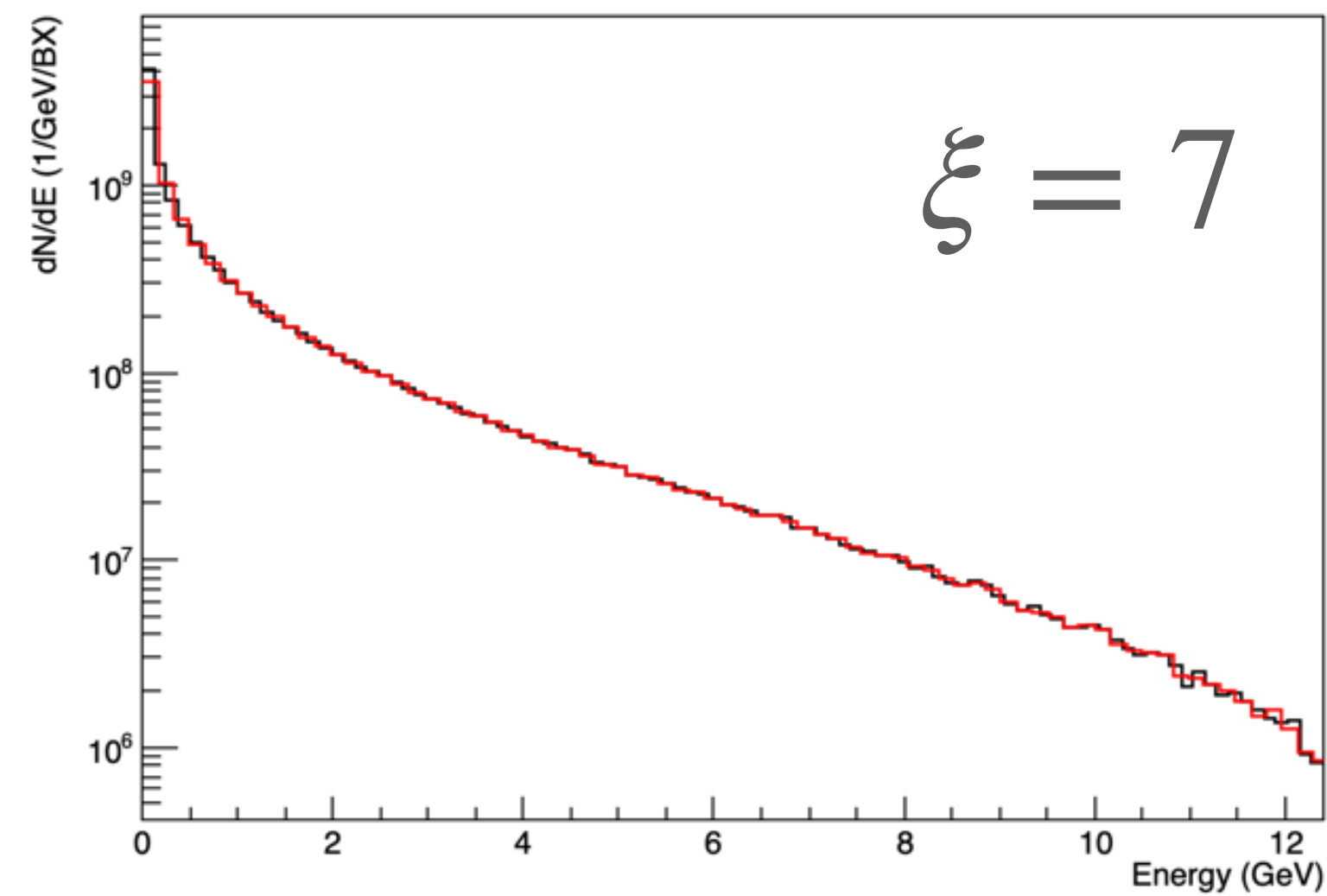
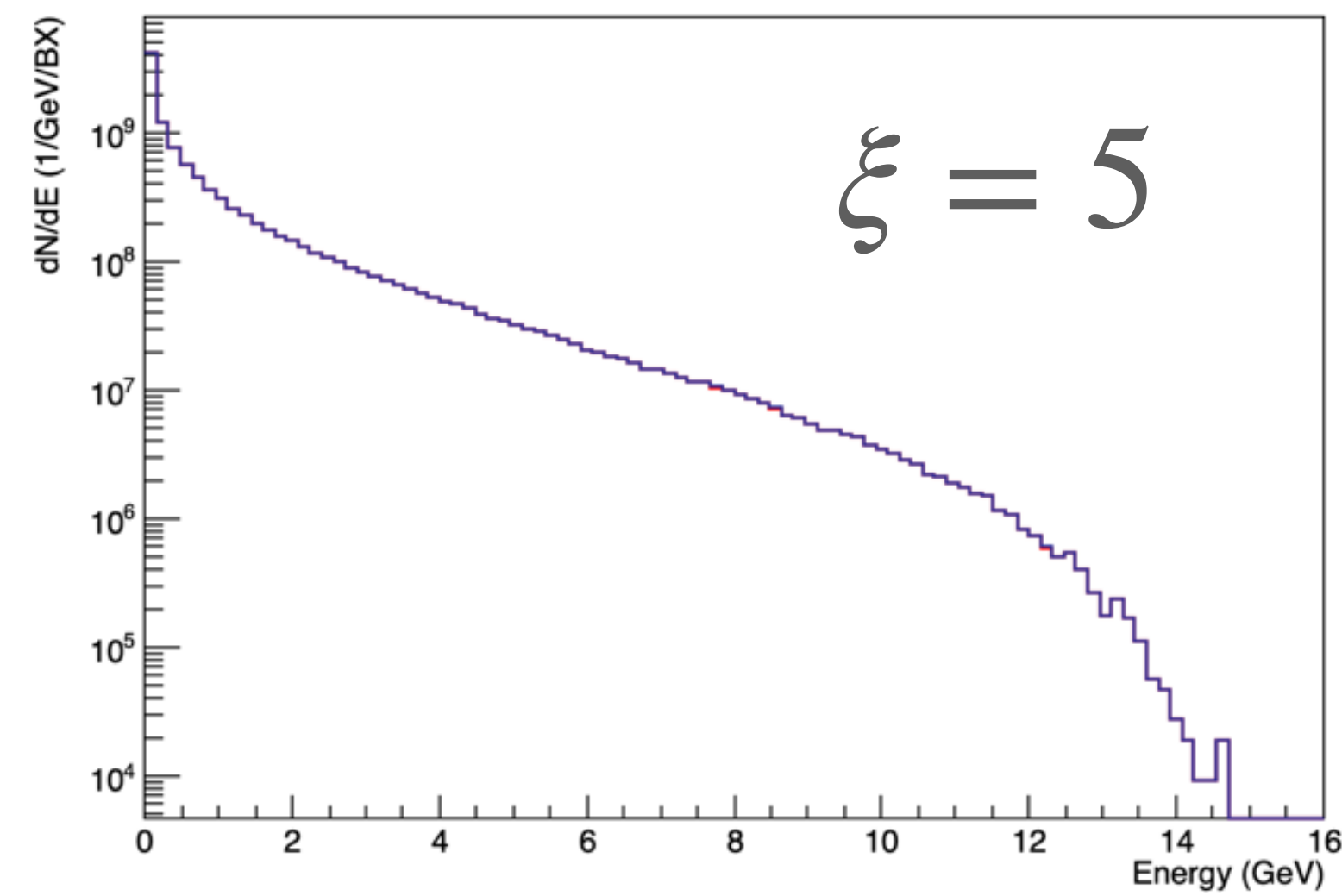
Backup

Dose Estimation

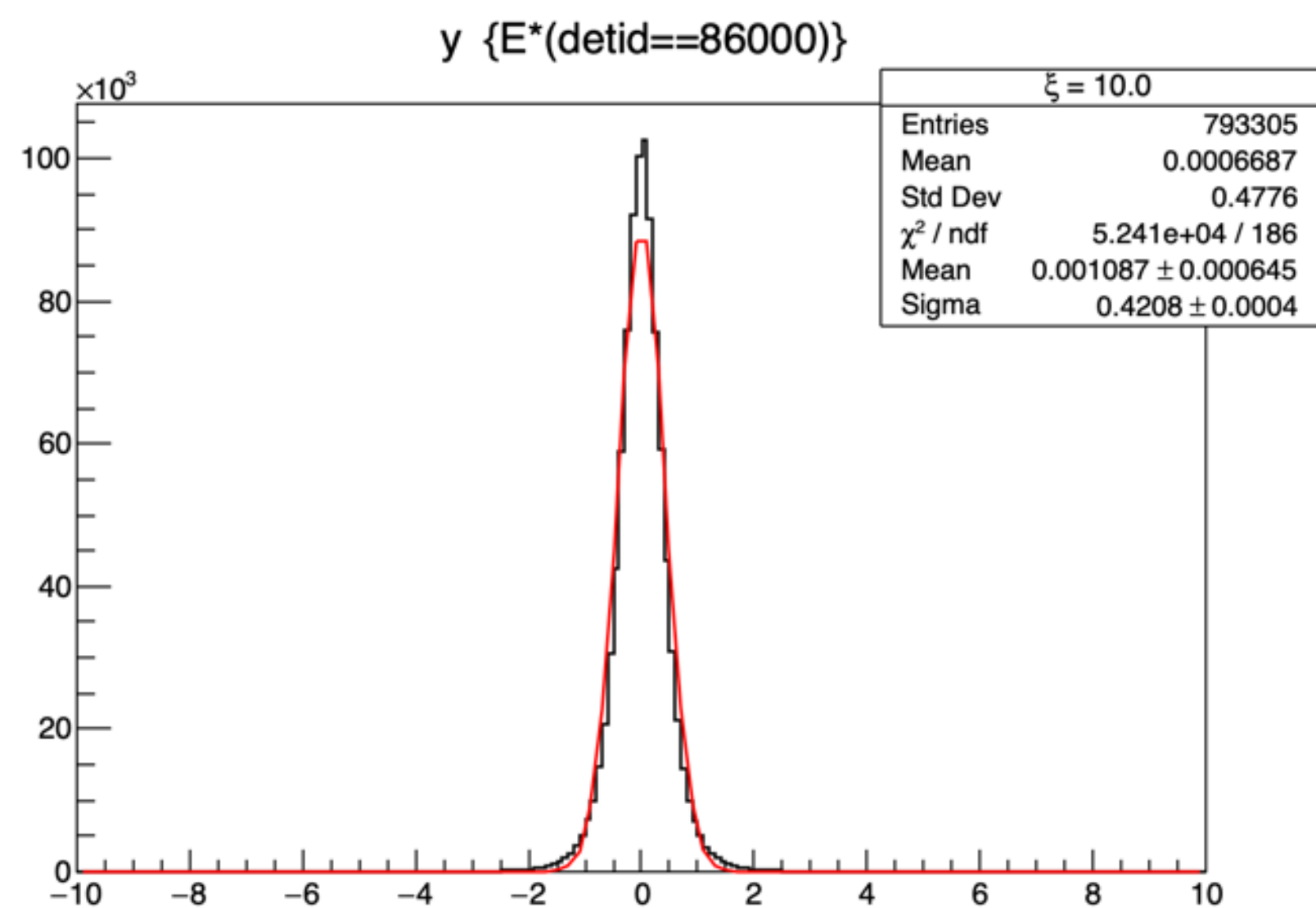
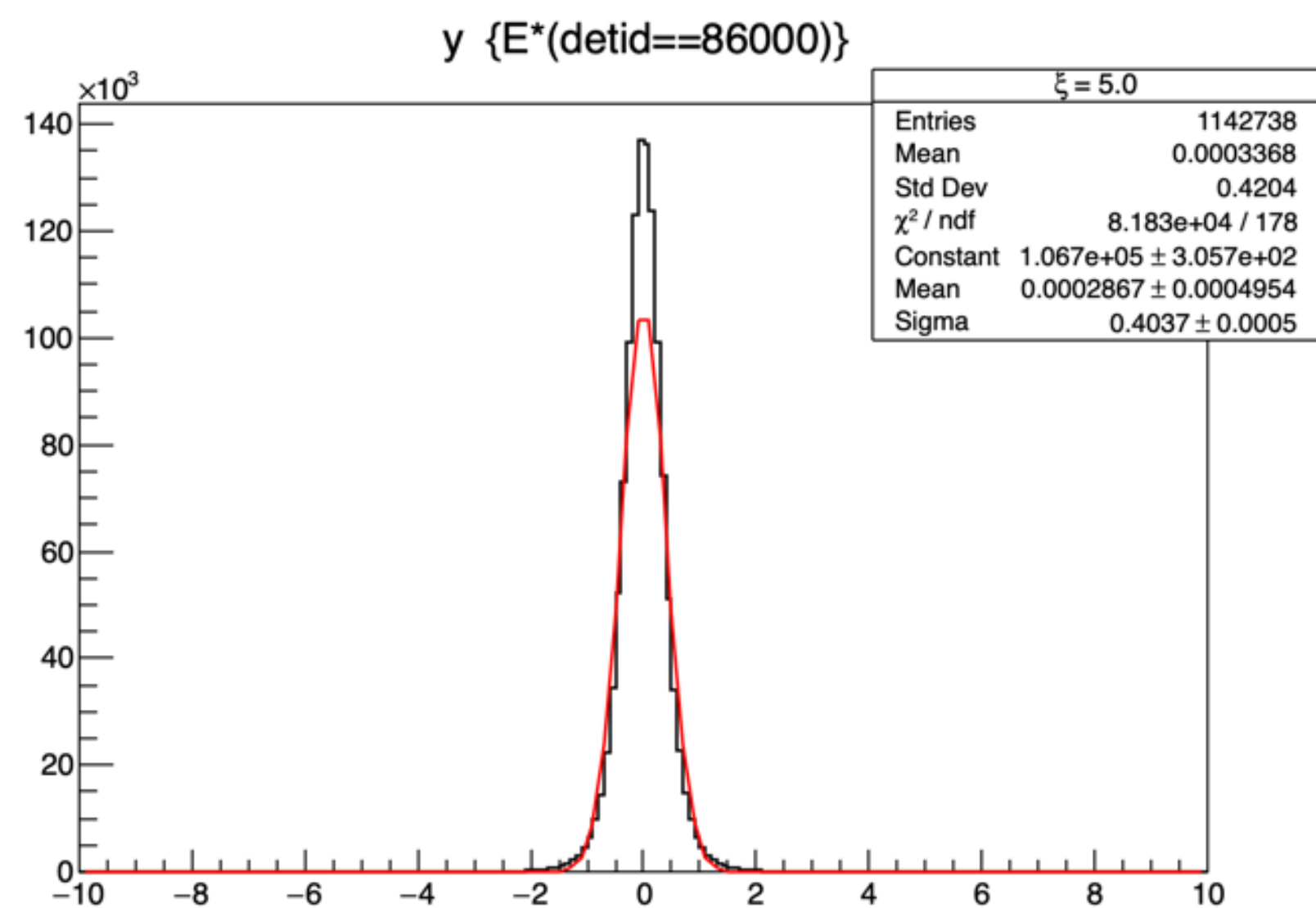
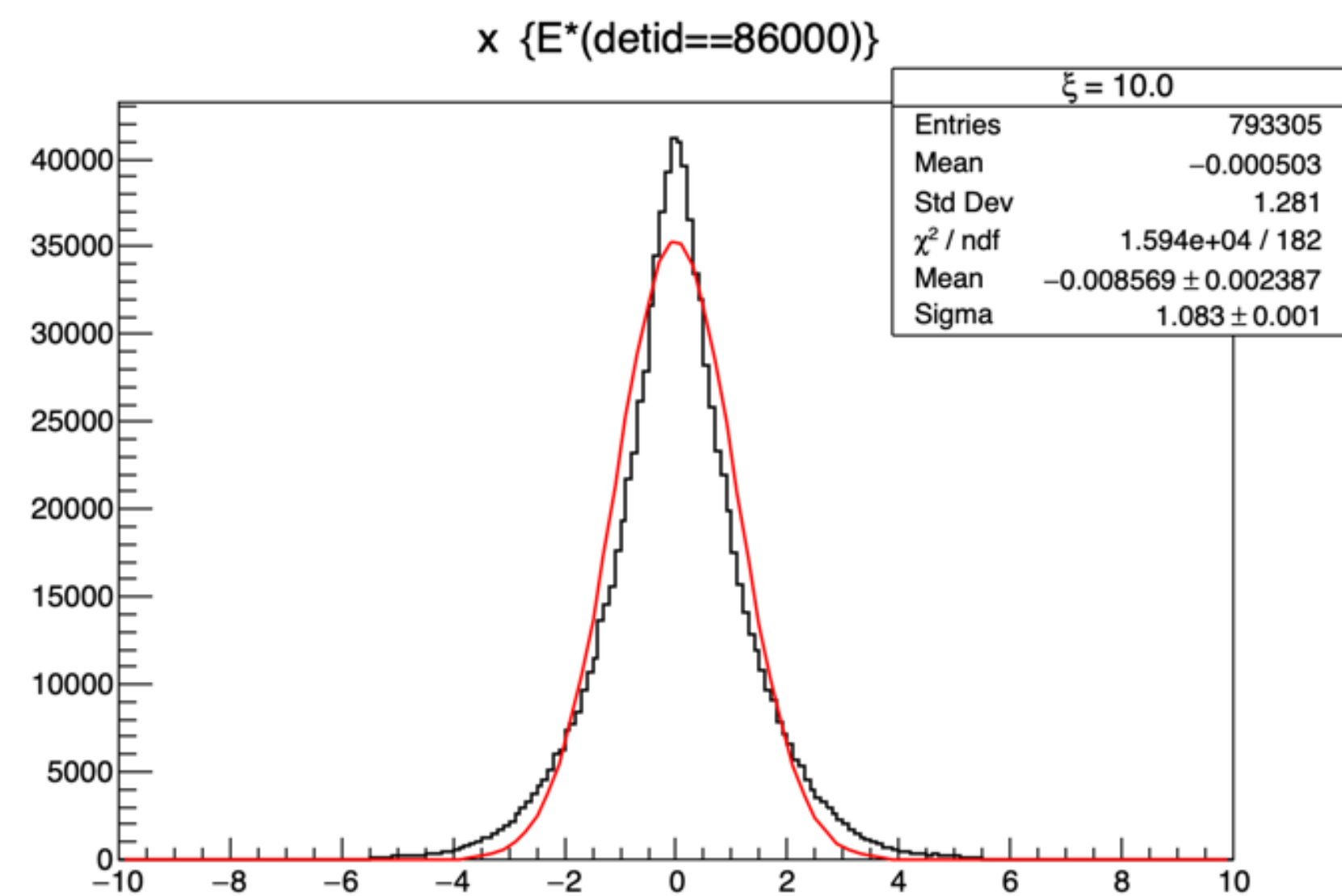
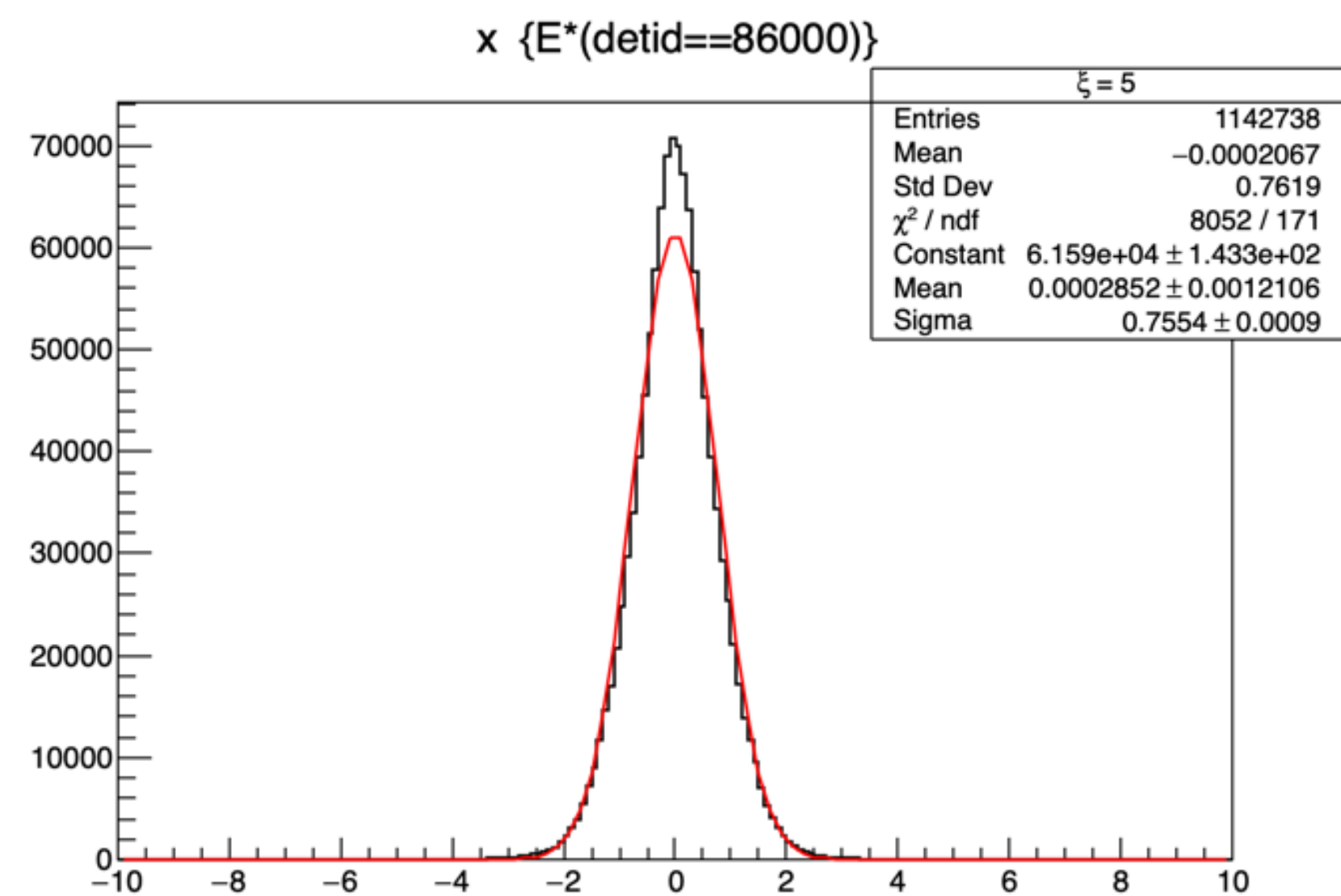
Distribution of Energy Deposition



Photon Spectra



Energy-weighted profiles



Xi reconstruction

Geometrical factor

- The model-independent formula for xi contains the geometrical factor

$$\beta = \sqrt{\frac{P}{Q}} \exp\left(-\frac{\delta^2}{PQ}\right)$$

- $P = 1 + 4\rho^2$ $Q = 1 + 8\rho^2$ $\rho = \frac{r_b}{w_0}$ $\delta = \frac{x_b}{w_0}$
- Impact parameter is zero for MC simulations

