

Resummation

Evolution

Sudakov logarithms in dijet photoproduction at low x

Pieter Tael

Universiteit Antwerpen

2022
workshop

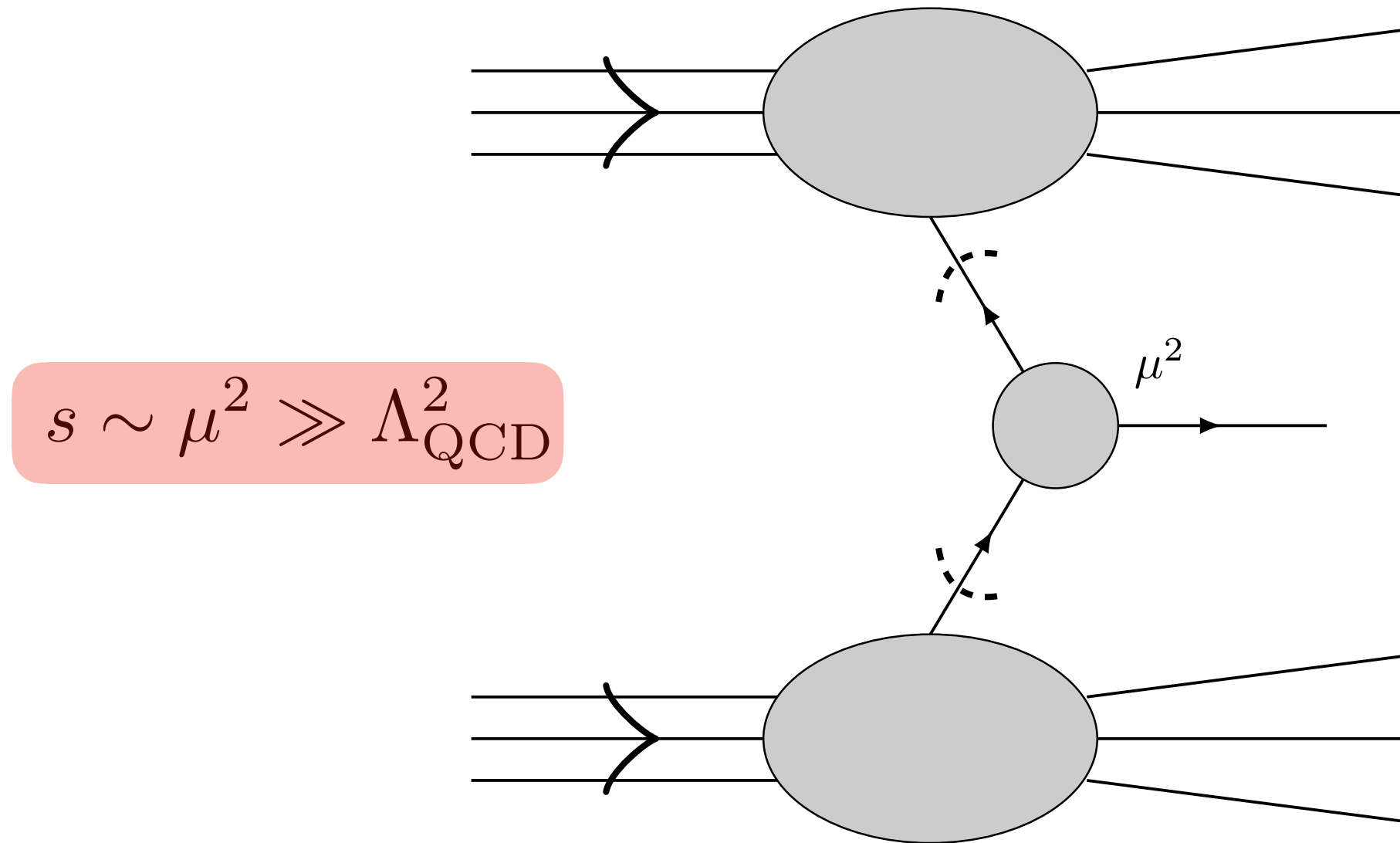
October 31 - November 4, 2022



University of Antwerp
Particle Physics Group



Collinear factorisation

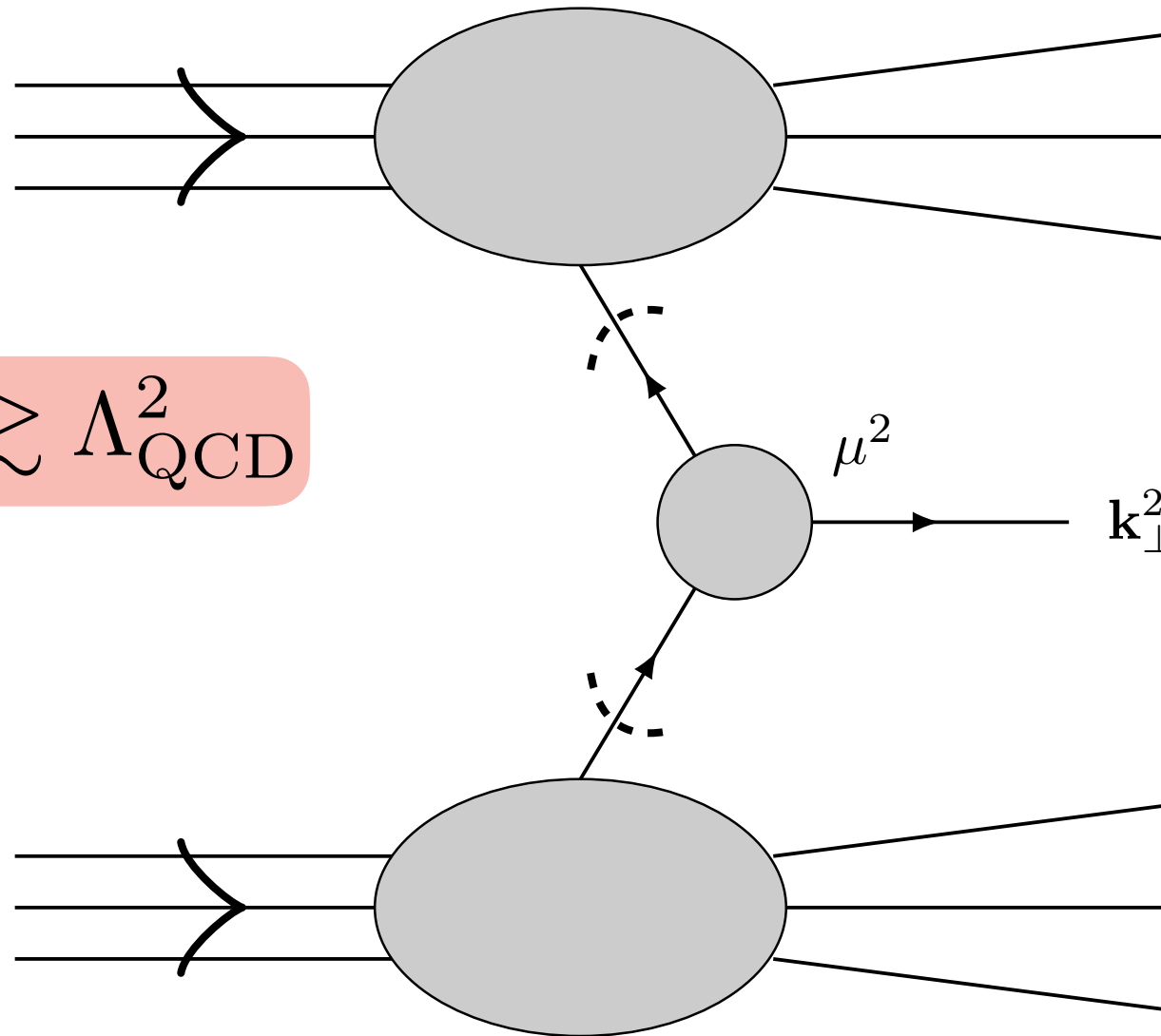


$$\sigma_{\text{coll}} = \hat{\sigma}(\mu^2) \otimes f(x_a, \mu^2) \otimes f(x_b, \mu^2) + \mathcal{O}(\Lambda_{\text{QCD}}/\mu)^n$$

Large logarithms $\ln(\mu^2/\Lambda_{\text{QCD}}^2)$ resummed using DGLAP

Transverse-momentum dependent factorisation

Collinear factorisation needs to be generalised in presence of additional scale $\mu_b^2 \sim \mathbf{k}_\perp^2$



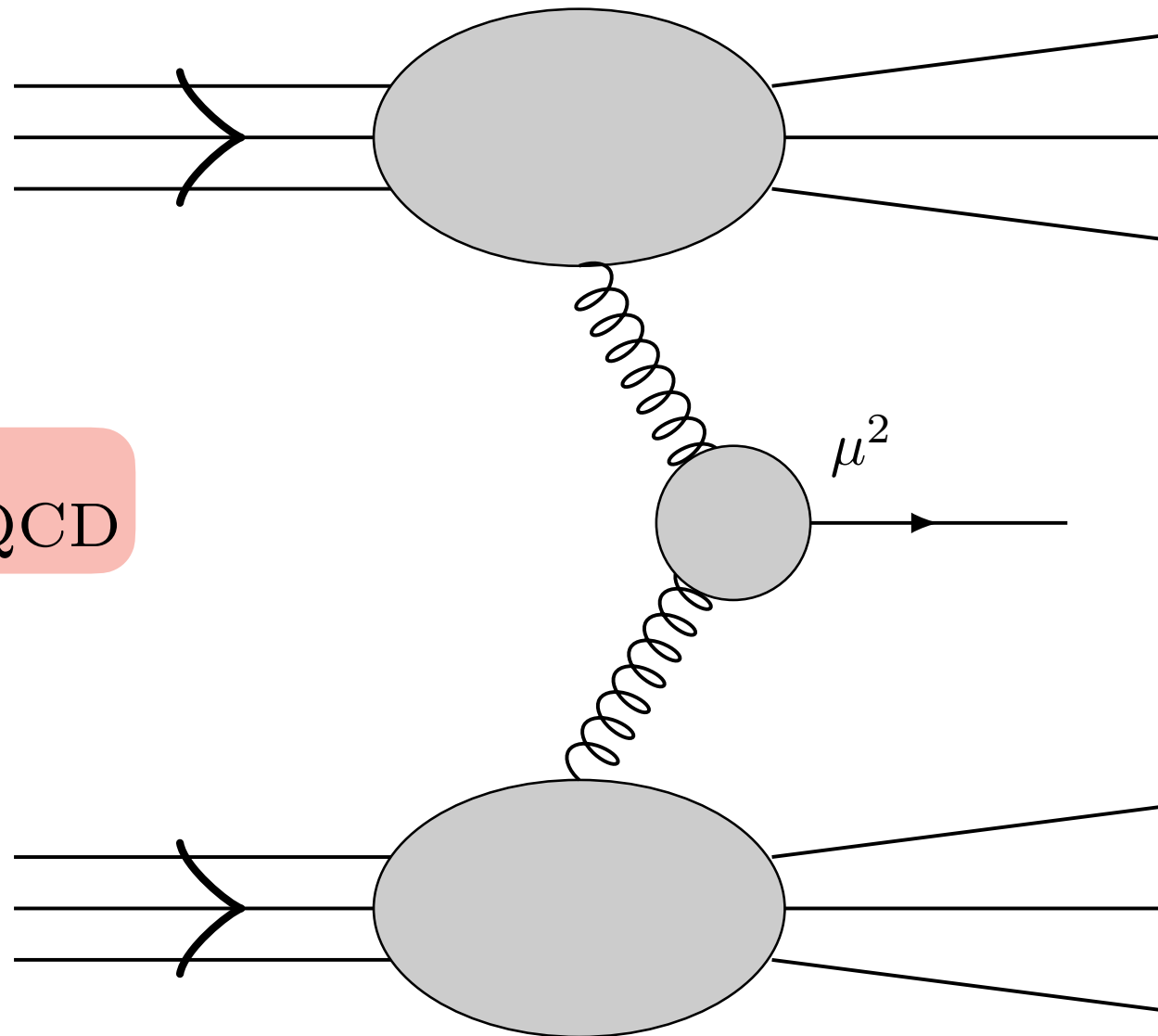
$$s \sim \mu^2 \gg \mathbf{k}_\perp^2 \gtrsim \Lambda_{\text{QCD}}^2$$

$$\sigma_{\text{TMD}} = \hat{\sigma}(\mathbf{k}_\perp^2, \mu^2) \otimes f(x_a, \mathbf{k}_{a\perp}, \mu^2) \otimes f(x_b, \mathbf{k}_{b\perp}, \mu^2) + \mathcal{O}\left(\frac{\Lambda}{\mu}\right)^n$$

Additional Sudakov logarithms $\ln(\mu^2/\mathbf{k}_\perp^2)$
resummed using CSS

Collins, Soper, Sterman ('85-'89)
Collins (2011)
Echevarria, Idilbi, Scimemi (2012)

High-energy factorisation



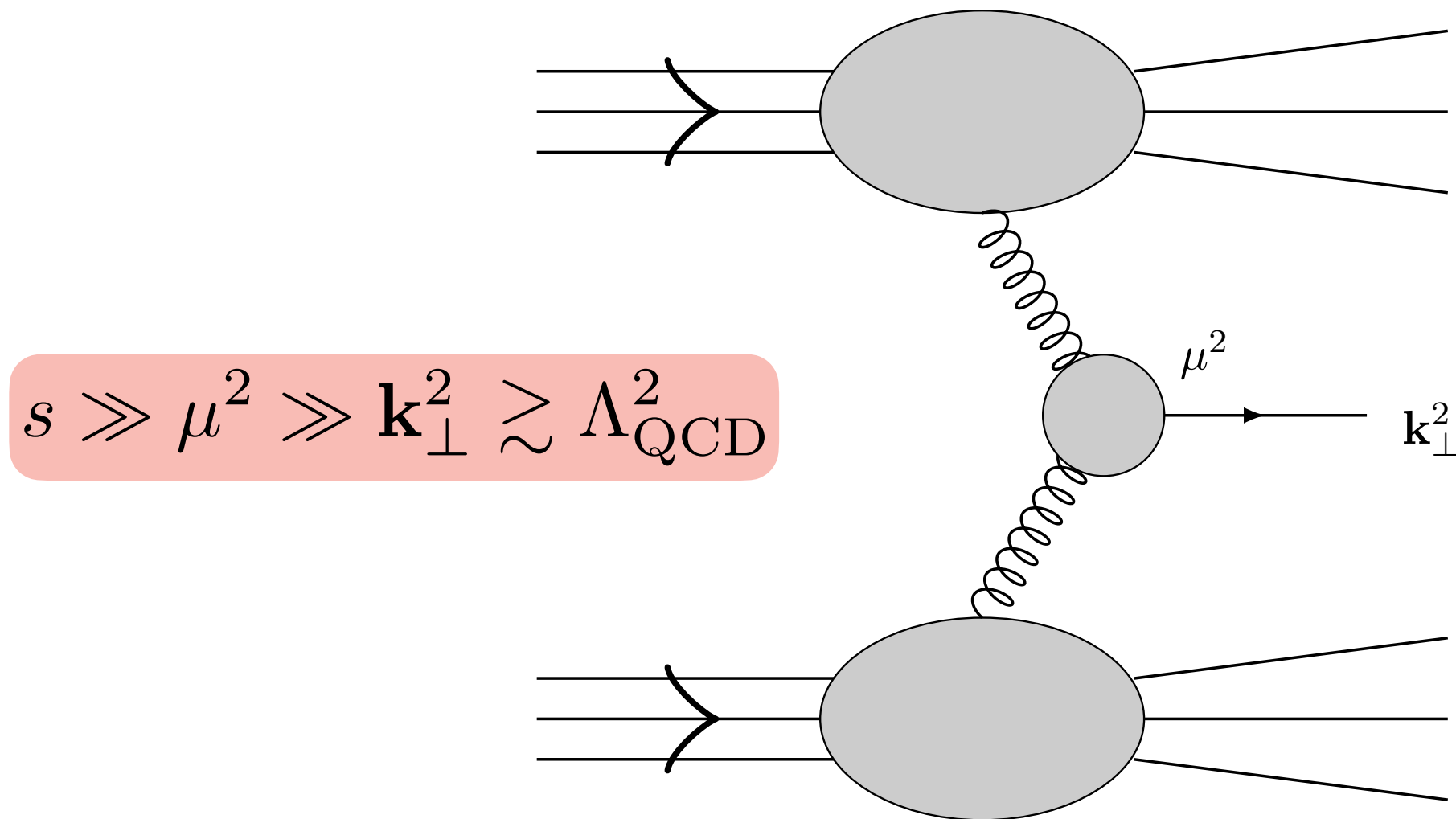
$$s \gg \mu^2 \gg \Lambda_{\text{QCD}}^2$$

$$\sigma_{\text{HEF}} = \hat{\sigma}\left(\frac{k_a^2}{\mu^2}, \frac{k_b^2}{\mu^2}, \mu^2\right) \otimes \mathcal{G}(x_a, \mathbf{k}_{a\perp}, \mu^2) \otimes \mathcal{G}(x_b, \mathbf{k}_{b\perp}, \mu^2) + \mathcal{O}\left(\frac{\Lambda}{\mu}\right)^n$$

Additional logarithms $\ln(s/\mu^2) \sim \ln(1/x)$ resummed using BFKL

Catani, Ciafaloni, Hautmann ('90-'94)

Combining low-x and Sudakov resummation



Simultaneous resummation of $\ln(1/x)$ and $\ln(\mu^2/\mathbf{k}_\perp^2)$?

Many approaches and implementations:

SW: Balitsky, Tarasov (2015)

HEF: Deak, Hautmann, Jung, Kutak, van Hameren, Sapeta, Hentschinski (2016-2021)

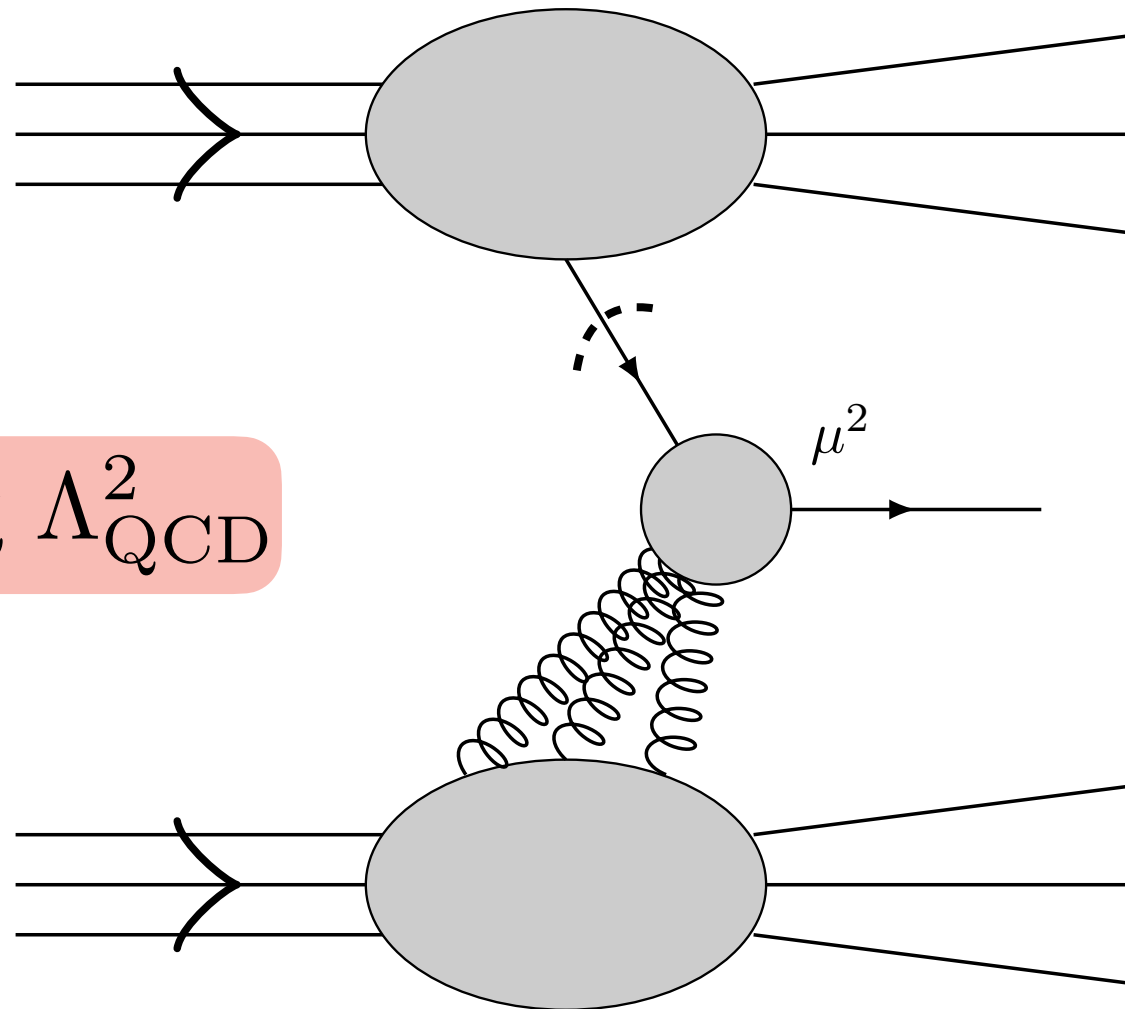
BFKL: Nefedov (2021)

PB: Hautmann, Hentschinski, Keersmaekers, Kusina, Kutak, Lelek (2022)

CGC: Mueller, Xiao, Yuan (2011); Xiao, Yuan, Zhou (2017); Stasto, Wei, Xiao, Yuan (2018);

PT, Altinoluk, Beuf, Marquet (2022); Caucal, Salazar, Schenke, Venugopalan (2022)

Why (not) the Colour Glass Condensate?



$$s \gg \mu^2 \gtrsim Q_s^2 \gtrsim \Lambda_{\text{QCD}}^2$$

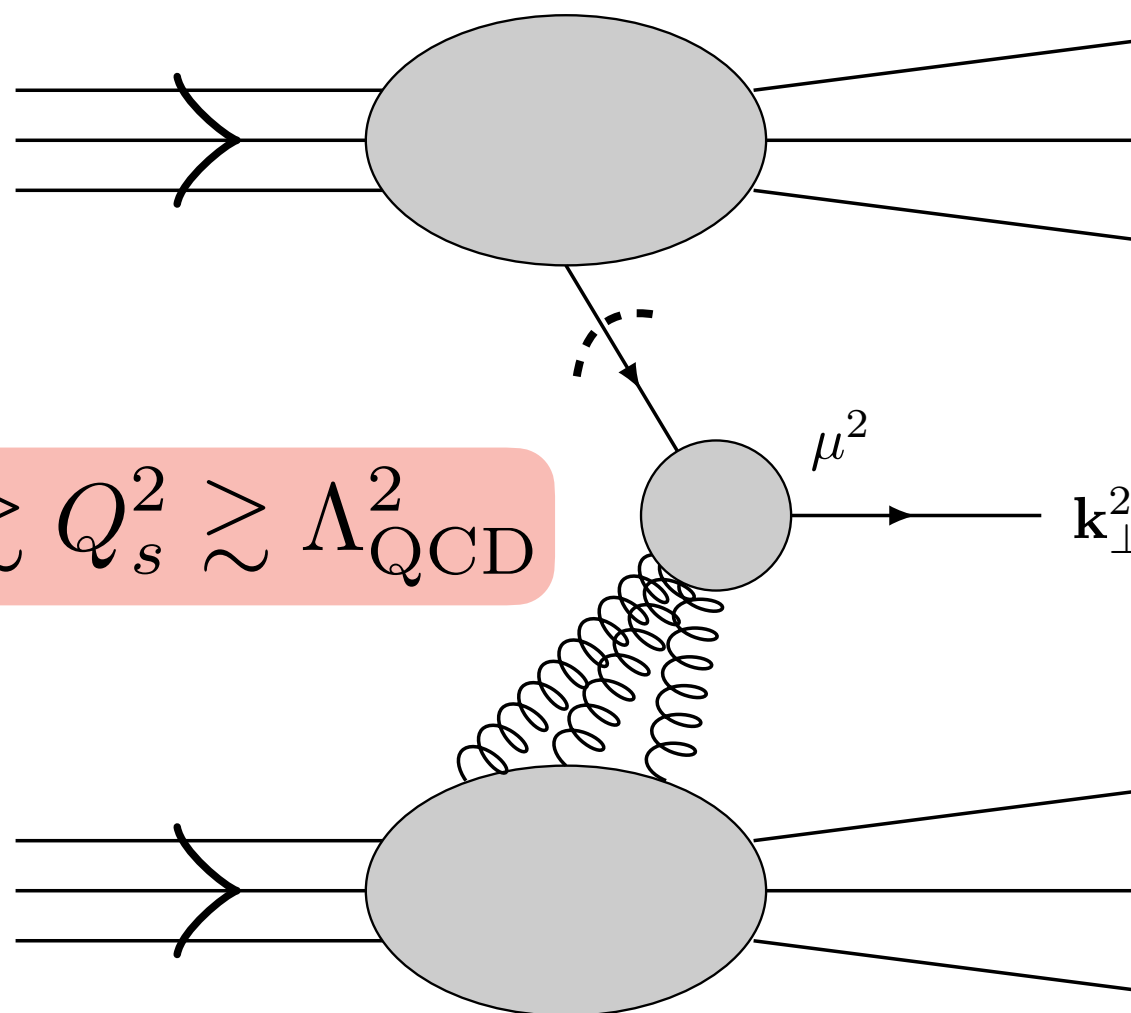
Saturation scale $Q_s^2(A, x) \simeq \frac{A^{1/3}}{x^{0.3}}$, e.g. $Q_s^2 \simeq 35 \text{ GeV}^2$ for lead at $x = 10^{-3}$

All-twist framework, all hadronic operators $\sim Q_s^2/\mu^2$ included

$$\sigma_{\text{CGC}} \neq \hat{\sigma} \otimes \mathcal{G}$$

Mueller, McLerran, Venugopalan, Jalilian-Marian,
Kovner, Leonidov, Iancu, Weigert (1990-2001)

CGC in the TMD limit



$$s \gg \mu^2 \gg \mathbf{k}_\perp^2 \gtrsim Q_s^2 \gtrsim \Lambda_{\text{QCD}}^2$$

$$\sigma_{\text{CGC, TMD}} = \hat{\sigma}(\mathbf{k}_\perp^2, \mu_b^2) \otimes f(x_a, \mu^2) \otimes f(x_b, \mathbf{k}_\perp, \mu^2) + \mathcal{O}(Q_s^2/\mu^2) + \mathcal{O}(\alpha_s^n)$$

Dominguez, Marquet, Xiao, Yuan (2011)

CGC in the TMD limit

$$\Gamma^{\mu\nu}(x, \mathbf{k}) = \frac{2}{p_A^-} \int \frac{d\xi^+ d^2\xi}{(2\pi)^3} e^{i\xi^+ k^-} e^{-i\xi \mathbf{k}} \langle p_A | \text{Tr } F^{-\mu}(0) \mathcal{U}(0, \xi^+, \xi) F^{-\nu}(\xi^+, \xi) | p_A \rangle$$

(Gluon) TMDs are process-dependent through gauge links / Wilson lines

$$\Gamma^{\mu\nu}(x, \mathbf{k}) = -\frac{g_T^{\mu\nu}}{2} \mathcal{F}_{\text{WW}}(x, \mathbf{k}) + \left(\frac{k_T^\mu k_T^\nu}{\mathbf{k}^2} + \frac{g_T^{\mu\nu}}{2} \right) \mathcal{H}_{\text{WW}}(x, \mathbf{k})$$

Contribution from linearly polarised gluons even in unpolarised hadron

Full Wilson-line and spin structure not included in k_t -factorisation

$$\begin{aligned} \mathcal{F}_i(x, \mathbf{k}_\perp) &= \mathcal{G}(x, \mathbf{k}_\perp) + \mathcal{O}(Q_s^2/\mathbf{k}_\perp^2) \\ \mathcal{H}_i(x, \mathbf{k}_\perp) &= \mathcal{G}(x, \mathbf{k}_\perp) + \mathcal{O}(Q_s^2/\mathbf{k}_\perp^2) \end{aligned}$$

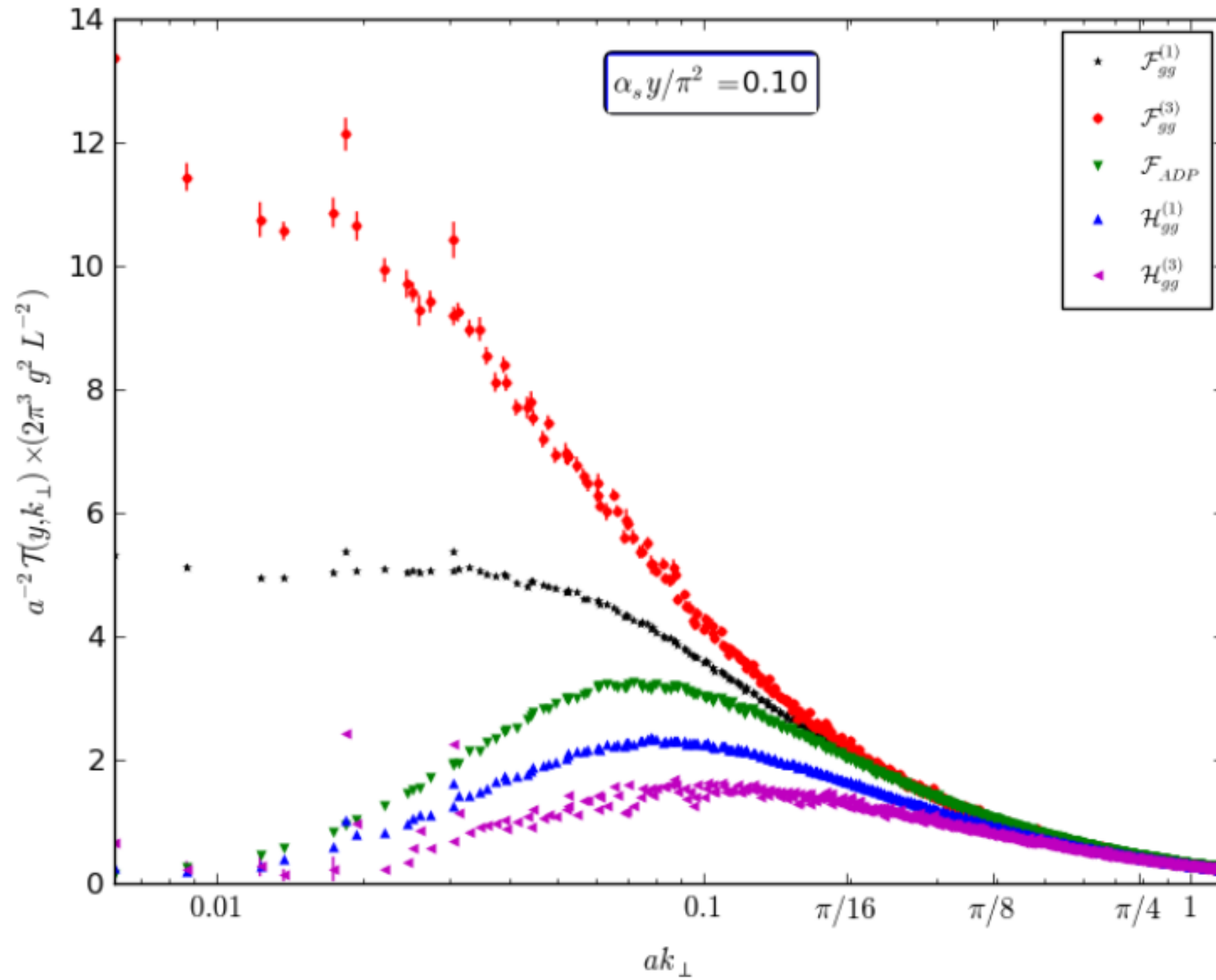
Unintegrated PDF

Unpolarised gluon TMD with gauge structure i

/
Linearly polarised gluon TMD with gauge structure i

Kotko, Kutak, Marquet, Petreska, Sapeta, van Hameren (2015)
Altinoluk, Boussarie, Kotko (2019)

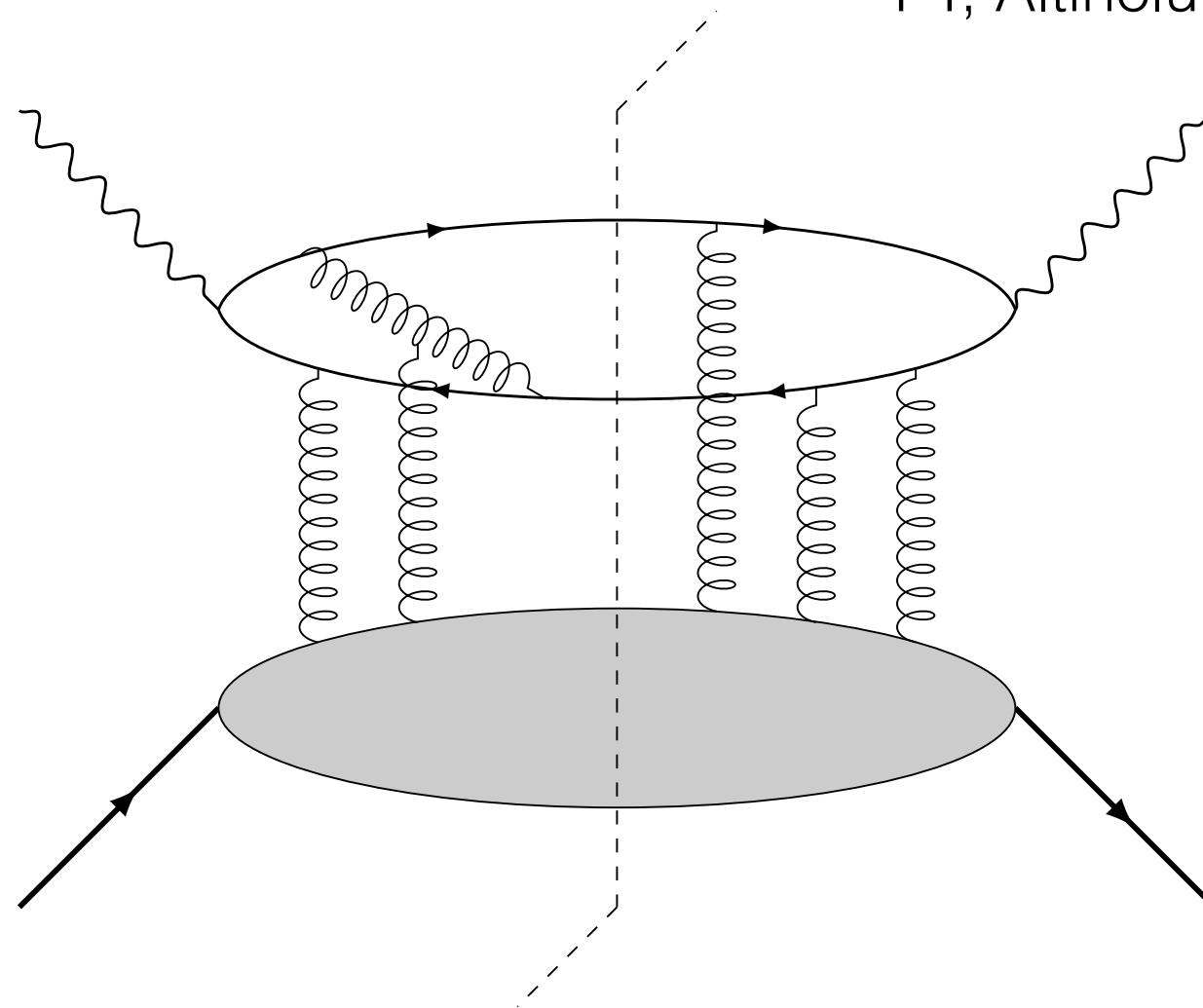
CGC in the TMD limit



Marquet, Roiesnel, PT (2018)

Dijet photoproduction at NLO in the CGC

PT, Altinoluk, Beuf, Marquet (2022)



Framework: dipole formulation of CGC, light-cone perturbation theory

$$_f \langle (\mathbf{q})[\vec{p}_1]_{s_1}; (\bar{\mathbf{q}})[\vec{p}_2]_{s_2} | \hat{F} - 1 | (\gamma)[\vec{q}]_{\lambda} \rangle_i$$

$$= \langle (\mathbf{q})[\vec{p}_1]_{s_1}; (\bar{\mathbf{q}})[\vec{p}_2]_{s_2} | \mathcal{U}(+\infty, 0)(\hat{F} - 1)\mathcal{U}(0, -\infty) | (\gamma)[\vec{q}]_{\lambda} \rangle$$

LCPT: Bjorken, Kogut, Soper (1971)

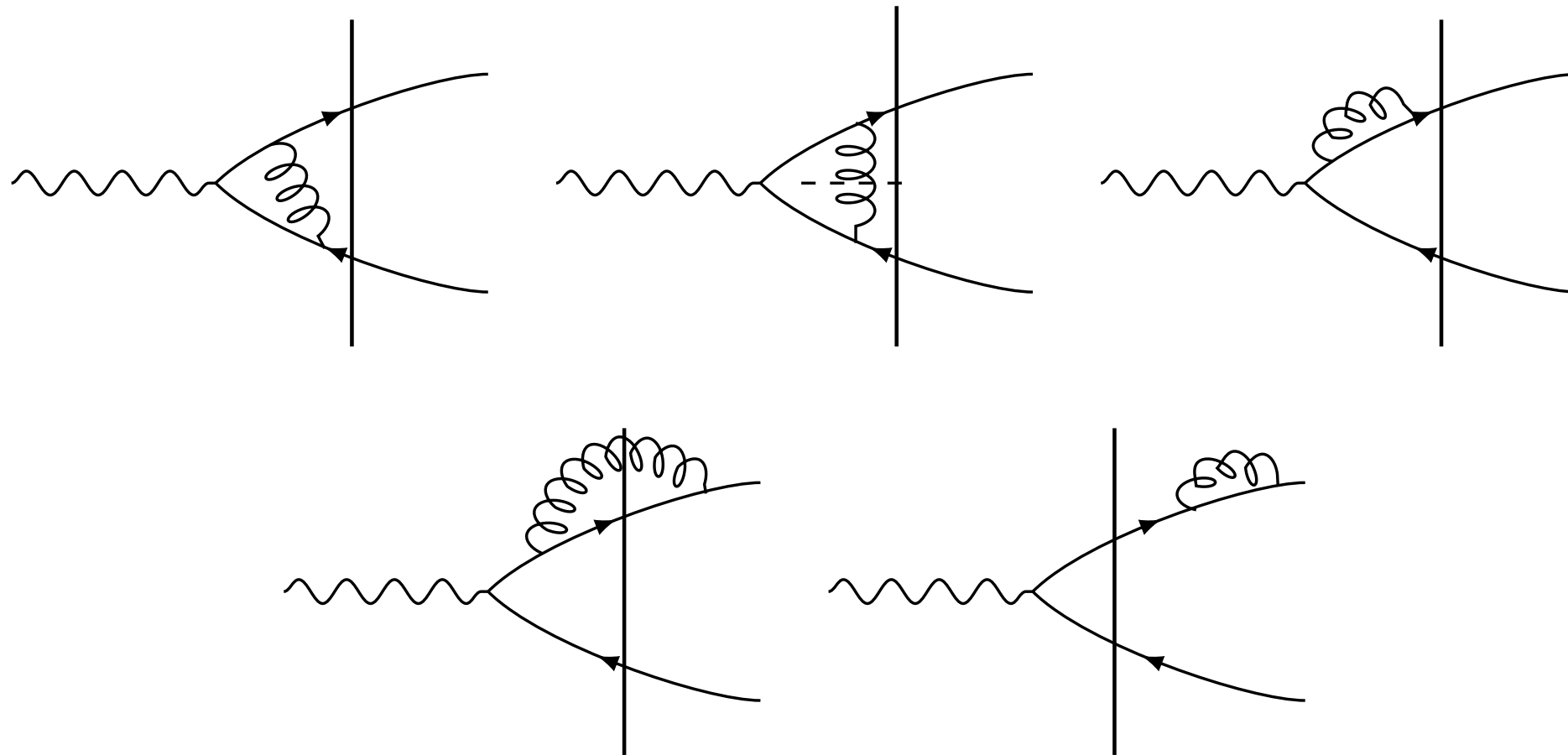
Inclusive DIS: Beuf (2016-2017)

DIS: Caucal, Salazar, Venugopalan (2022)

Dihadron: Bergabo, Jalilian-Marian (2022)

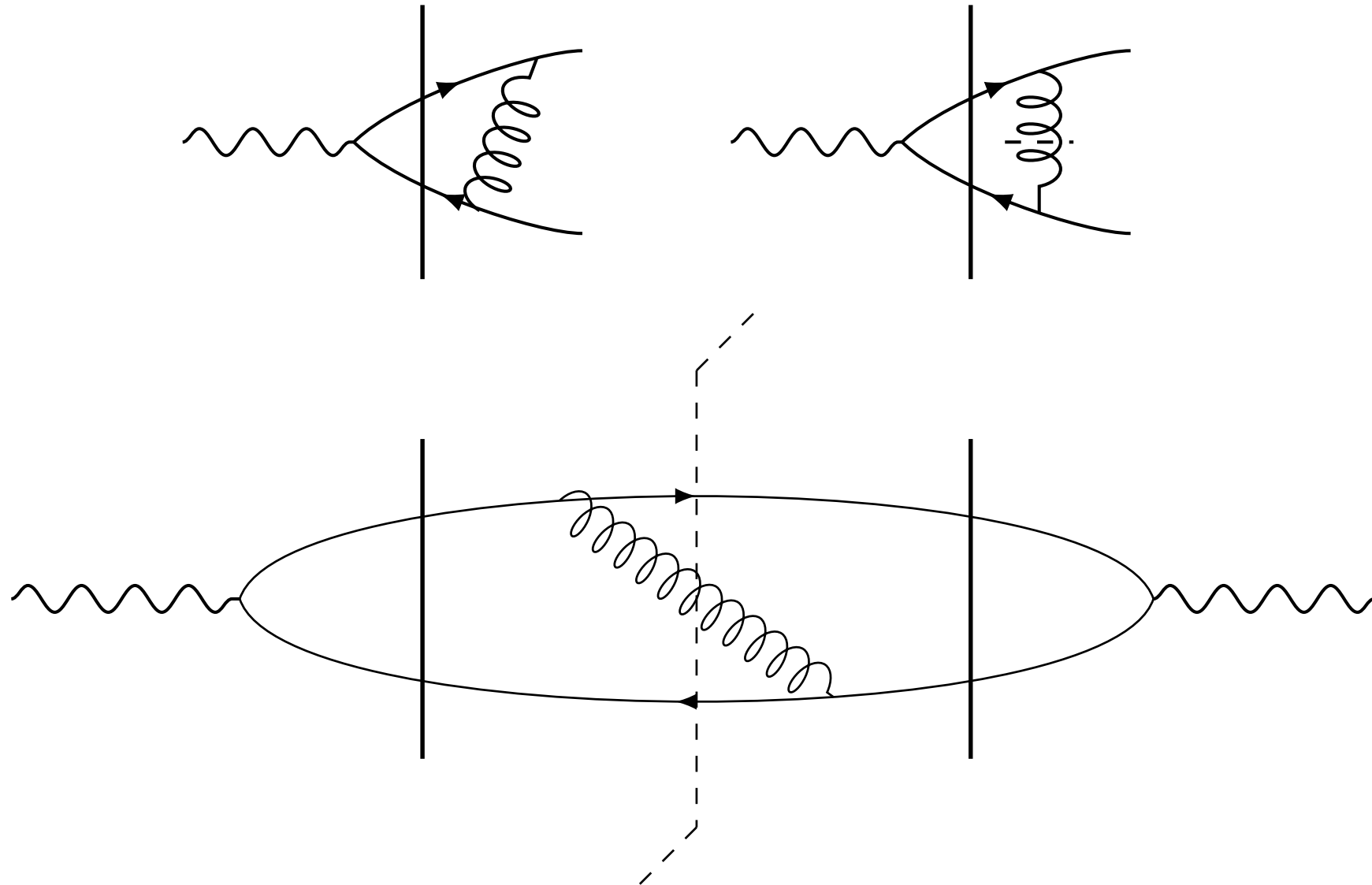
Diffraction: Emilie Li (REF)

UV divergences



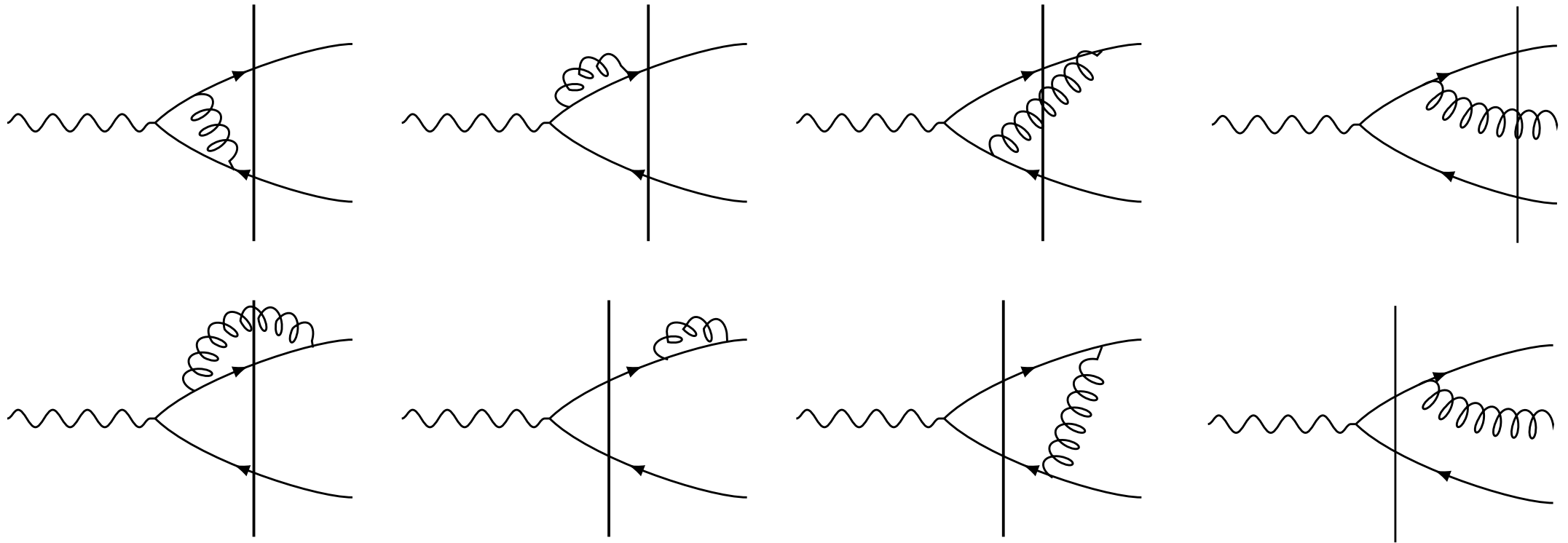
$\mathbf{k}_{\perp} \rightarrow \infty$ in loops, regulated with dimensional regularisation,
no leftover logarithms

Soft divergences



$(k^+, \mathbf{k}_\perp) \rightarrow 0$ in final state, regulated with dimensional regularisation,
no leftover logarithms

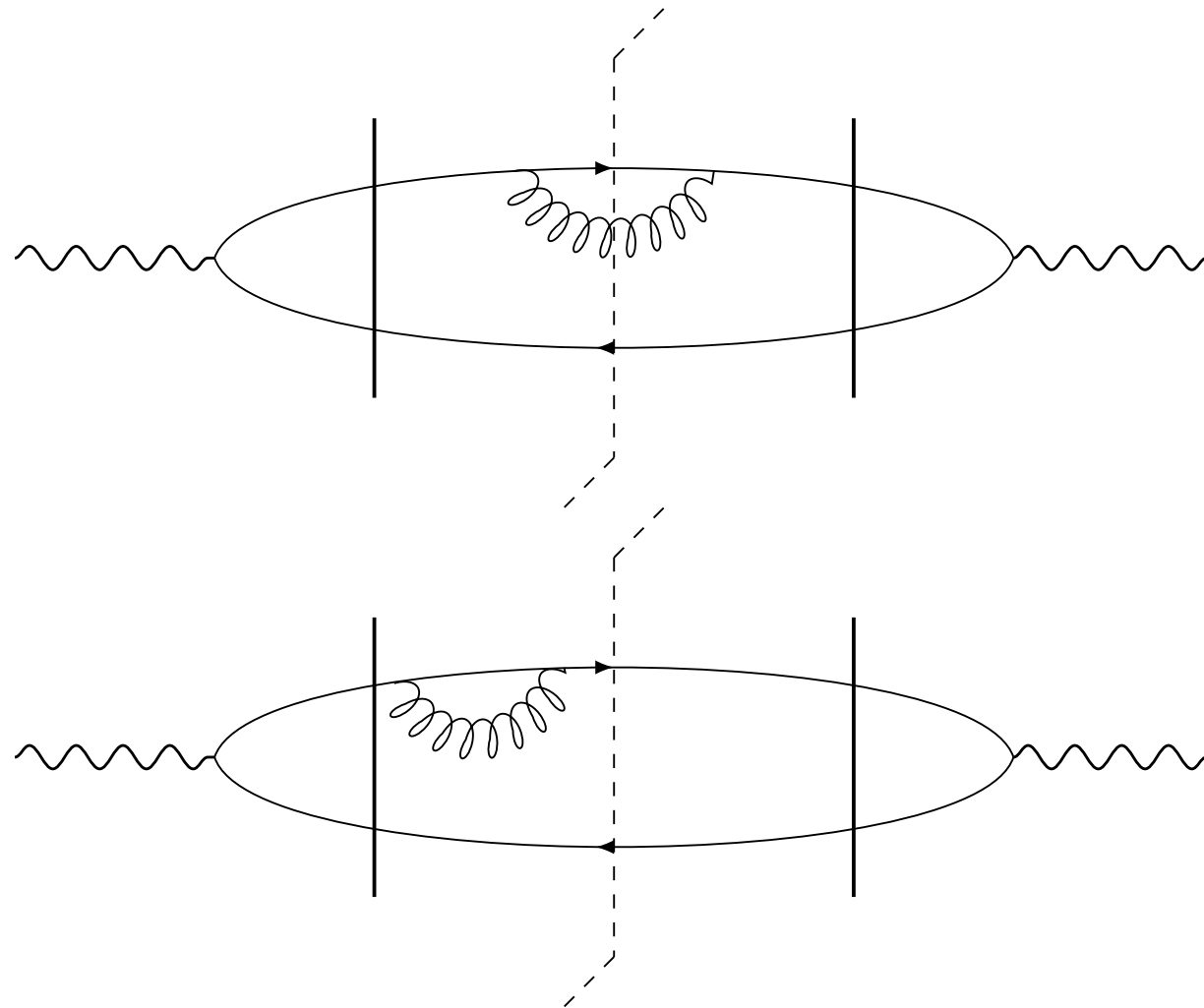
Rapidity divergences



$k^+ \rightarrow 0$, regulated with cutoff $k_{\min}^+$, 'renormalisation scale' k_f^+ ,
absorbed into JIMWLK evolution of LO cross section

$$\begin{aligned} d\sigma_{\text{NLO}} = & \int_{k_{\min}^+}^{k_f^+} \frac{dp_3^+}{p_3^+} \hat{H}_{\text{JIMWLK}} d\sigma_{\text{LO}} \\ & + \int_{k_{\min}^+}^{+\infty} \frac{dp_3^+}{p_3^+} \left[d\tilde{\sigma}_{\text{NLO}} - \theta(k_f^+ - p_3^+) \hat{H}_{\text{JIMWLK}} d\sigma_{\text{LO}} \right] \end{aligned}$$

Collinear-soft divergences

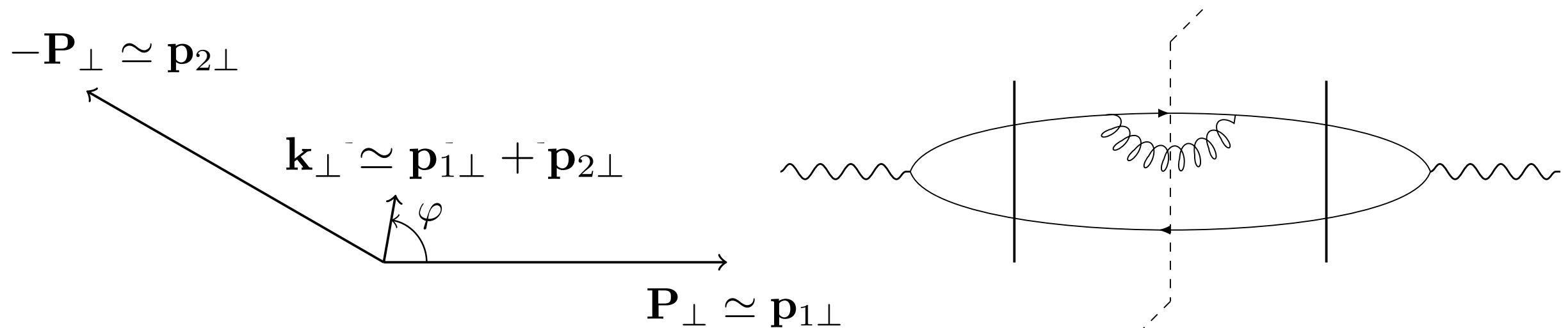


Mix of dimensional regularisation and cutoff method

Collinear divergences cancel between inside-jet radiation and self-energy

Leftover soft divergences cancel between radiation in-and outside the jet

Back-to-back limit: Sudakov logarithms



Remnants of soft-collinear generate Sudakov double log with wrong sign!

$$d\sigma_{\text{NLO}}^{\text{TMD}} = d\sigma_{\text{LO}}^{\text{TMD}} \times \frac{\alpha_s N_c}{4\pi} \ln \left(\frac{\mathbf{P}_\perp^2 (\mathbf{b} - \mathbf{b}')^2}{c_0^2} \right)^2 \quad \begin{array}{l} \mathbf{P}_\perp^2 \sim \mu^2 \\ (\mathbf{b} - \mathbf{b}')^2 \sim 1/\mathbf{k}_\perp^2 \end{array}$$

... but in our framework hard to distinguish soft $(k^+, \mathbf{k}_\perp) \rightarrow 0$ and rapidity $k^+ \rightarrow 0$ divergences

oversubtraction of high-energy logs via JIMWLK?

Kinematically consistent low-x resummation

JIMWLK evolution along p^+ in interval $k_{\min}^+ \rightarrow k_f^+$

‘Naive’ approach: strong ordering in p^+ only, implicitly assumes $s \rightarrow \infty$

More realistic approach calls for additional ordering in p^- , and additional renormalisation scale k_f^-

Implementing this ordering in final-state diagrams with suitable choice

$$k_f^+ = \frac{p_{j1}^+ p_{j2}^+}{q^+} \text{ and } k_f^- = \frac{\mathbf{P}_\perp^2}{2k_f^+} \text{ exactly compensates for wrong sign!}$$

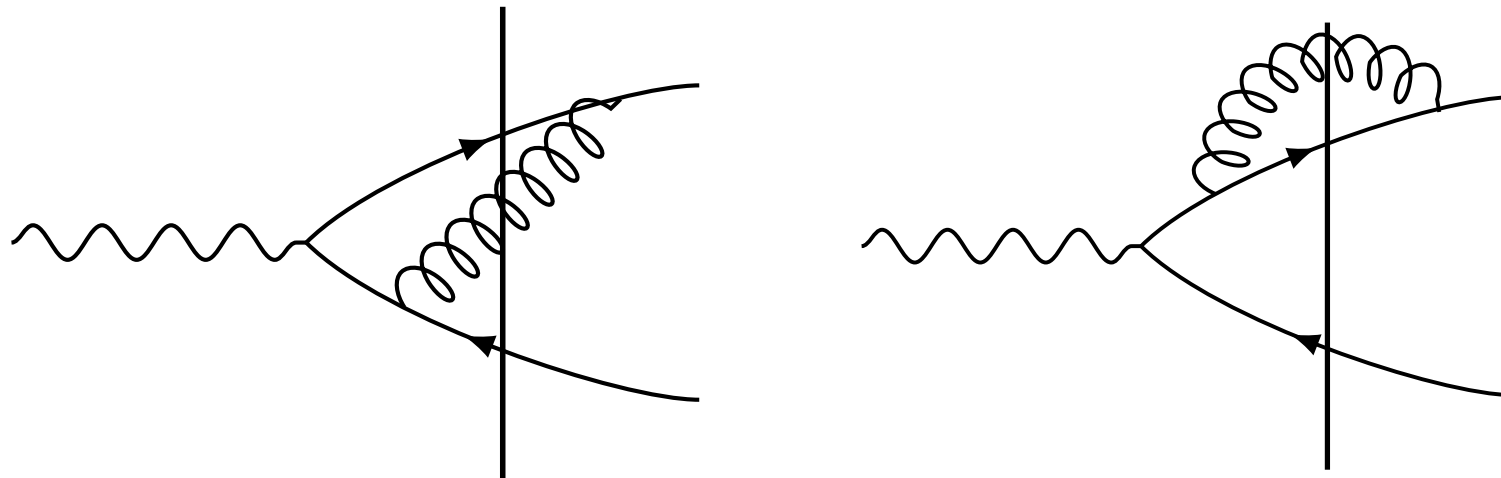
We end up with expected:

$$d\sigma_{\text{NLO}}^{\text{TMD}} = d\sigma_{\text{LO}}^{\text{TMD}} \times -\frac{\alpha_s N_c}{4\pi} \ln \left(\frac{\mathbf{P}_\perp^2 (\mathbf{b} - \mathbf{b}')^2}{c_0^2} \right)^2$$

Beyond large- N_c and double log: see Farid Salazar’s talk tomorrow

Ciafaloni ('88); Andersson, Gustafson, Samuelsson ('96); Kwiecinski, Martin, Sutton ('96); Salam ('98); Motyka, Stasto (2009); Kutak, Golec-Biernat, Jadach (2011); Beuf (2014); Iancu, Madrigal, Mueller, Soyez, Triantafyllopoulos (2019); Hatta, Iancu (2016); Nefedov (2022)

Breaking of TMD factorisation (?)



$$d\sigma_{\text{NLO}}^{\text{TMD}} = d\sigma_{\text{LO}}^{\text{TMD}} \times -\frac{\alpha_s N_c}{4\pi} \ln \left(\frac{\mathbf{P}_{\perp}^2 (\mathbf{b} - \mathbf{b}')^2}{c_0^2} \right)^2 + \text{fact. breaking}$$

At this point, we need rigorous power-counting à la SCET (Varun Vaidya's talk)

Outlook

Computed full NLO dijet photoproduction cross section in CGC

Recover correct Sudakov logs in TMD limit provided kinematical improved JIMWLK

Argued that k_t -factorisation needs extension when $\mu^2 \gg \mathbf{k}_\perp^2 \sim Q_s^2$
... but then TMD factorisation is seemingly broken beyond LO

Thanks for your attention !