



HERAPDF2.0 Jets and estimation of $\alpha_s(M_Z)$ @ NNLO

EPJ C 82, 243 (2022)
arXiv:2112.01120

K. Wichmann @REF22

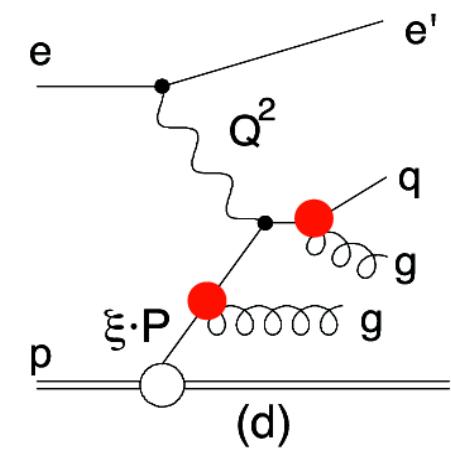
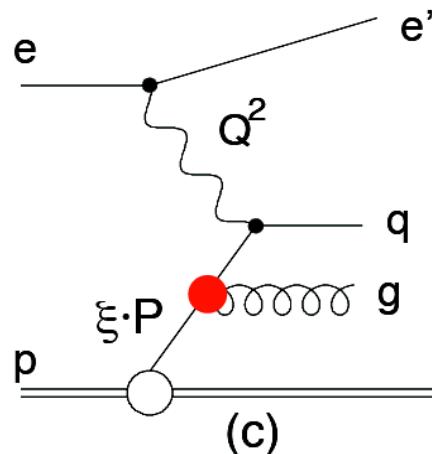
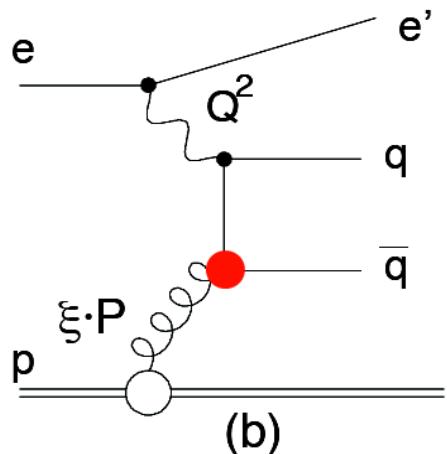
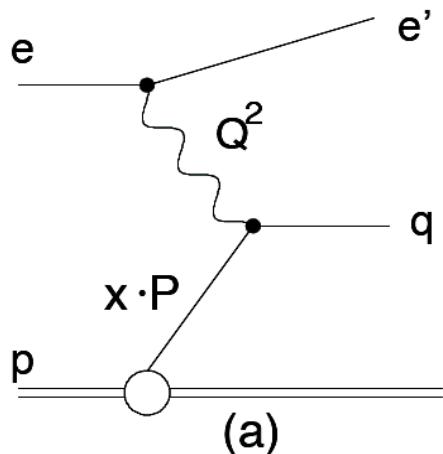


Jets produced @ DESY for over 40 years

At HERA direct information on gluon and $\alpha_s(M_Z)$ comes from jet production

→ Possible simultaneous determination of parton densities and $\alpha_s(M_Z)$

Jets at HERA



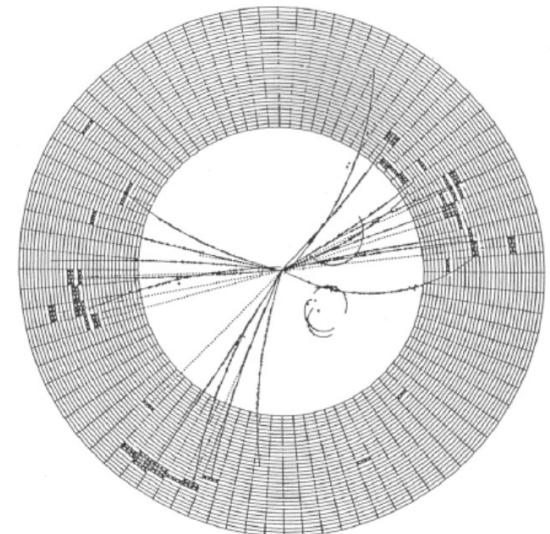
elweak coupling

$\propto \alpha_s$

dijets

$\propto \alpha_s^2$
trijets

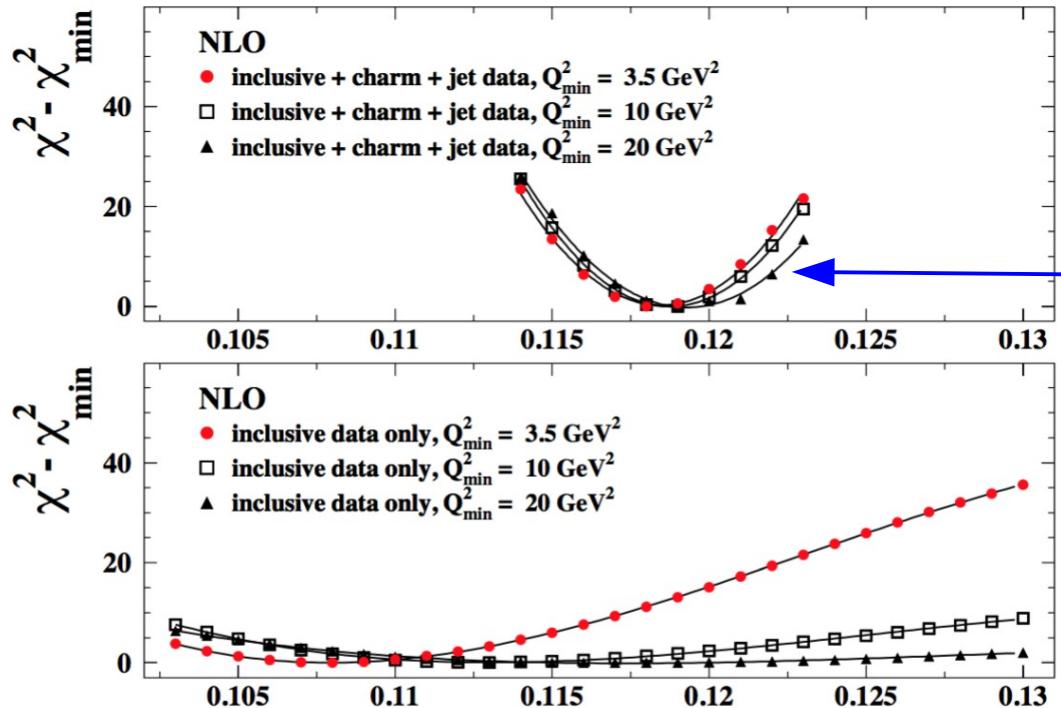
Jets at PETRA, 1979



*** SUMS (GeV) *** PTOT 35.768 PTRANS 29.954 PLONG 15.788 CHARGE -2
TOTAL CLUSTER ENERGY 15.169 PHOTON ENERGY 4.893 NR OF PHOTONS 11

Why study jets @ HERA?

H1 and ZEUS



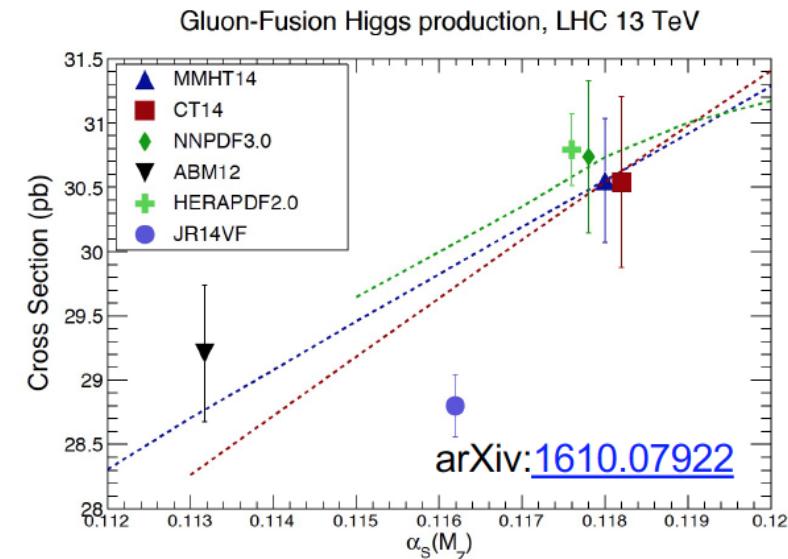
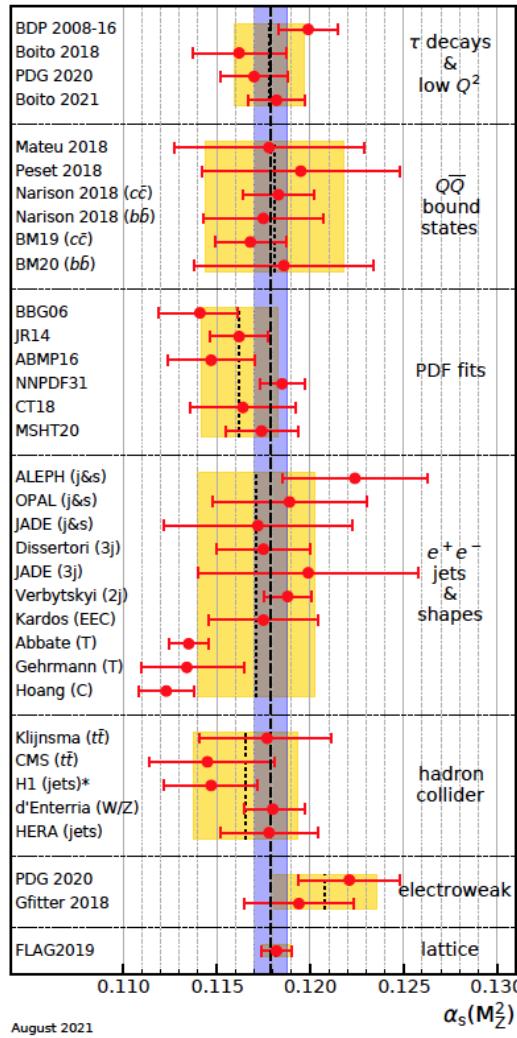
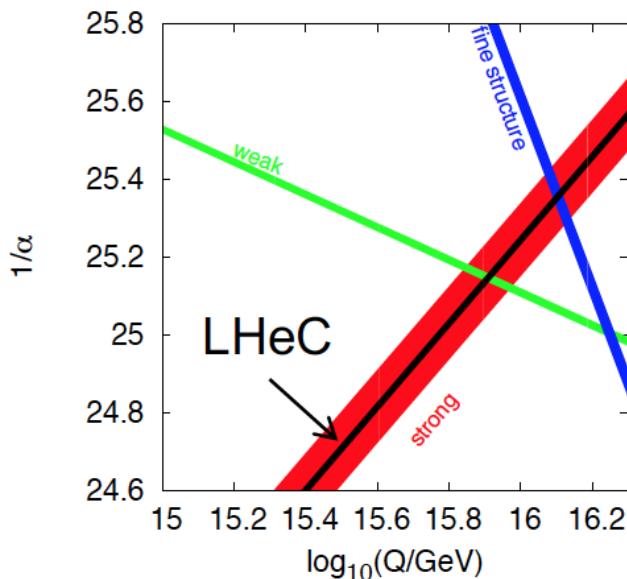
- HERA inclusive data carry little information on $\alpha_s(M_Z)$
- Jet data sensitive to $\alpha_s(M_Z)$



New NNLO calculations for HERA ep jet production available now

- Implemented in FastNLO and APPLEGRID → fast cross section calculation possible
- EPJ C 82, 243 (2022) arXiv:2112.01120
- Possible simultaneous determination of PDFs and $\alpha_s(M_Z)$ at NNLO

motivation and impact at LHC



- α_s is least known coupling constant;
needed to constrain GUT scenarios; cross section predictions, including Higgs;
...
- what is true α_s central value and uncertainty?
new precise determinations have important role to play

HERAPDF2.0 parameterisation

$$xf(x) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} \left(1 + E_{u_v} x^2 \right),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- Additional constrains
 - A_{u_v}, A_{d_v}, A_g : constrained by the quark-number sum rules and momentum sum rule
 - $B_{\bar{U}} = B_{\bar{D}}$
 - $x\bar{s} = \boxed{f_s} x\bar{D}$ at starting scale, $f_s = 0.4$

Updates in the procedure

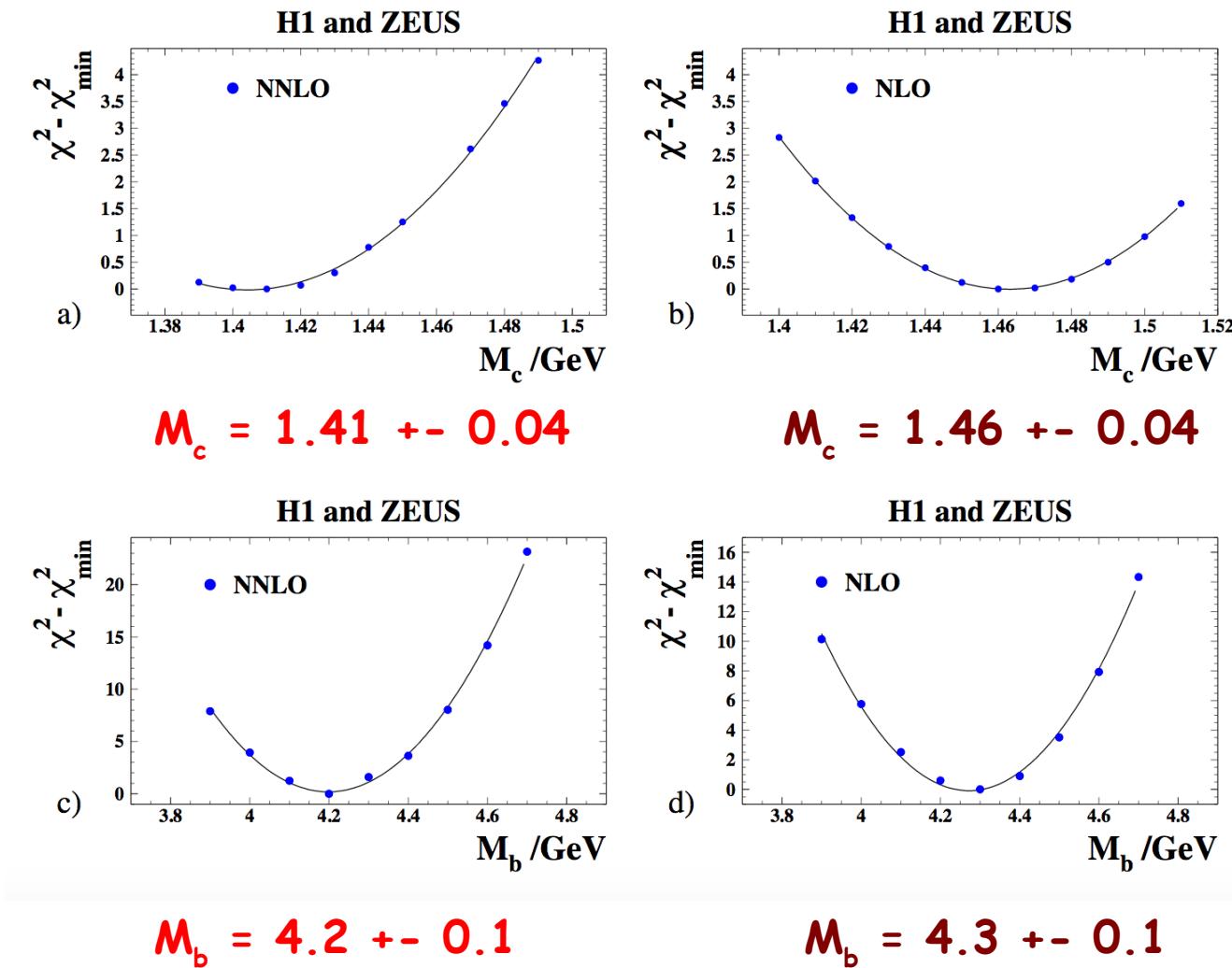
- scale choice changes:
- factorisation: $\mu F^2 = (Q^2 + pt^2)$
- cf. $\mu F^2 = Q^2$ in previous NLO analysis; updated since not a good choice for low Q^2 jet data; change makes almost no difference for high Q^2 jets
- renormalisation: $\mu R^2 = (Q^2 + pt^2)$
- cf. $\mu R^2 = (Q^2 + pt^2)/2$ in previous NLO analysis
- NNLO fit with $\mu R^2 = (Q^2 + pt^2)$ gives $\Delta \chi^2 = -15$ cf. $\mu R^2 = (Q^2 + pt^2)/2$ and vice versa for NLO fit
- scale uncertainties treated as completely correlated between bins and datasets

† pt denotes pt^{jet} in the case of inclusive jet cross sections and $\langle pt \rangle$ for dijets

- improved treatment of hadronisation uncertainties; NOW included together with exp. systematics; treated as $\frac{1}{2}$ correlated, $\frac{1}{2}$ uncorrelated between bins and datasets
- (small) uncertainties on theory predictions included

Estimation of charm & beauty masses

- new HERA combined charm and beauty data: EPJ C78 (2018), 473
 → updated estimation of M_c and M_b
 → Heavy Quark (HQ) coefficient functions evaluated using Thorne-Roberts Optimised Variable Flavour Number Scheme



HERA jet data used in PDF fit

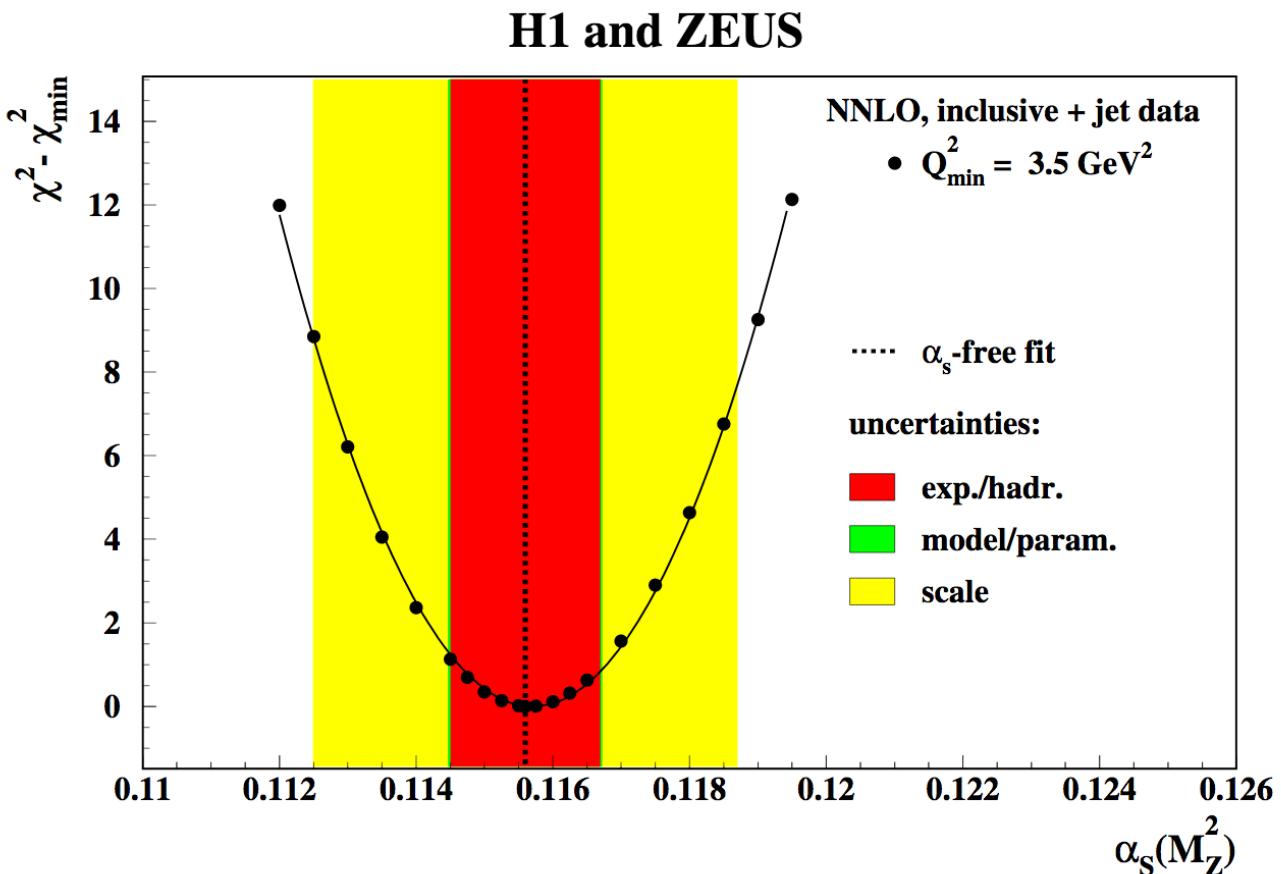
- Inclusive jets and dijets included
- Trijets from HERAPDF2Jets NLO excluded → no NNLO predictions
- H1 low Q^2 data added - particularly sensitive to $\alpha_s(M_Z)$
- Some data points excluded due theory limitations
 - Data at low scale $\mu = (pt_2 + Q_2) < 10 \text{ GeV} \rightarrow$ scale variations are large (~25% NLO and ~10% NNLO)
 - 6 ZEUS Dijet data points at low pt for which predictions are not truly NNLO

| Data set | taken from to | $Q^2[\text{GeV}^2]$ range from to | $\mathcal{L} \text{ pb}^{-1}$ | e^+ / e^- | $\sqrt{s} \text{ GeV}$ | Normalised | All points | Used points |
|--|---------------------------|-----------------------------------|-------------------------------|-----------------|------------------------|------------|------------|-------------|
| H1 HERA I normalised jets | 1999 – 2000 | 150 15000 | 65.4 | $e^+ p$ | 319 | yes | 24 | 24 |
| H1 HERA I jets at low Q^2 | 1999 – 2000 | 5 100 | 43.5 | $e^+ p$ | 319 | no | 28 | 20 |
| H1 normalised inclusive jets at high Q^2 | 2003 – 2007 | 150 15000 | 351 | $e^+ p / e^- p$ | 319 | yes | 30 | 30 |
| H1 normalised dijets at high Q^2 | 2003 – 2007 | 150 15000 | 351 | $e^+ p / e^- p$ | 319 | yes | 24 | 24 |
| H1 normalised inclusive jets at low Q^2 | 2005 – 2007 | 5.5 80 | 290 | $e^+ p / e^- p$ | 319 | yes | 48 | 37 |
| H1 normalised dijets at low Q^2 | 2005 – 2007 | 5.5 80 | 290 | $e^+ p / e^- p$ | 319 | yes | 48 | 37 |
| ZEUS inclusive jets | 1996 – 1997 | 125 10000 | 38.6 | $e^+ p$ | 301 | no | 30 | 30 |
| ZEUS dijets | 1998 – 2000 & 2004 – 2007 | 125 20000 | 374 | $e^+ p / e^- p$ | 318 | no | 22 | 16 |

- Possibilities for PDF fit with jet data
 - With fixed $\alpha_s(M_Z)$
 - With free $\alpha_s(M_Z)$ or doing $\alpha_s(M_Z)$ scan → $\alpha_s(M_Z)$ value

α_s @ NNLO from HERA jets

- $\alpha_s(M_Z)$ determined with experimental, model, param. and hadr. uncertainties
- In fits with free $\alpha_s(M_Z)$ scale uncertainty important → calculated as 100% correlated between bins and data sets



$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \quad {}^{+0.0001}_{-0.0002} \text{ (model + parameterisation)}$$

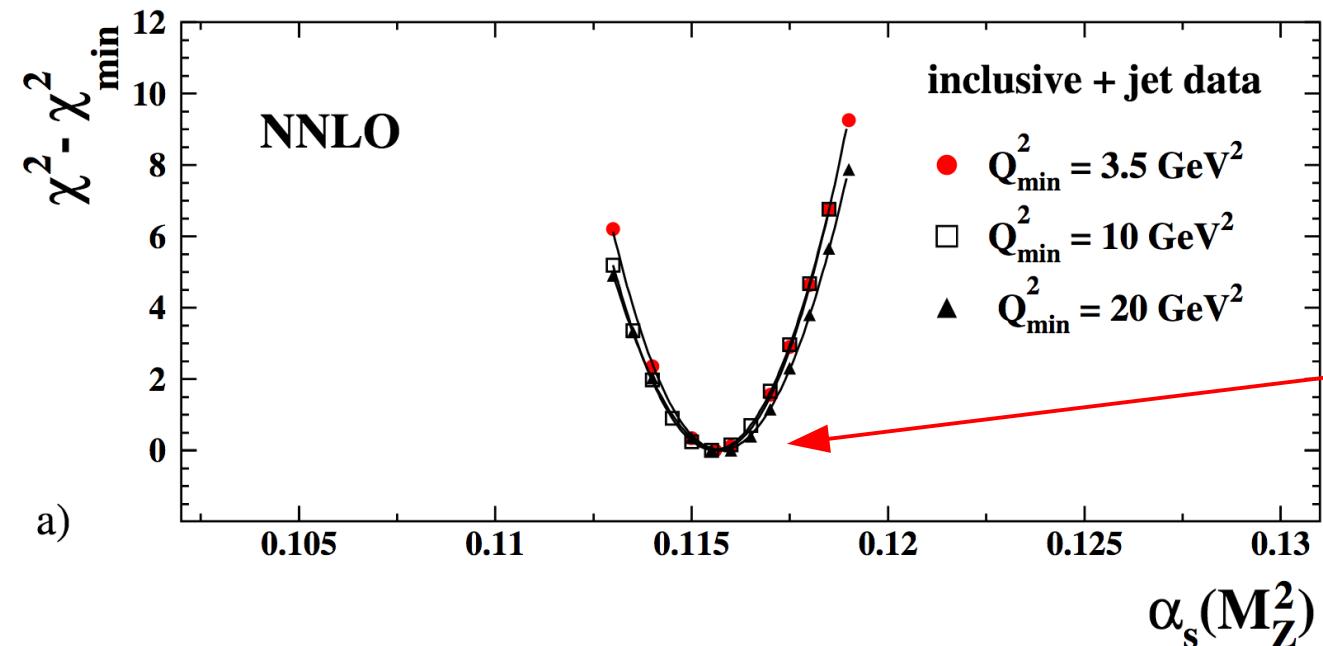
± 0.0029 (scale)

Checking robustness of results

- HERA data at low x and Q^2 may be subject to need for $\ln(1/x)$ resummation or higher twist effects (eg arXiv:1506.06042, 1710.05935)

→ χ^2 scans performed with harder Q^2 cuts

H1 and ZEUS



Q^2 cuts do not result in any significant change to the value of $\alpha_s(M_Z)$

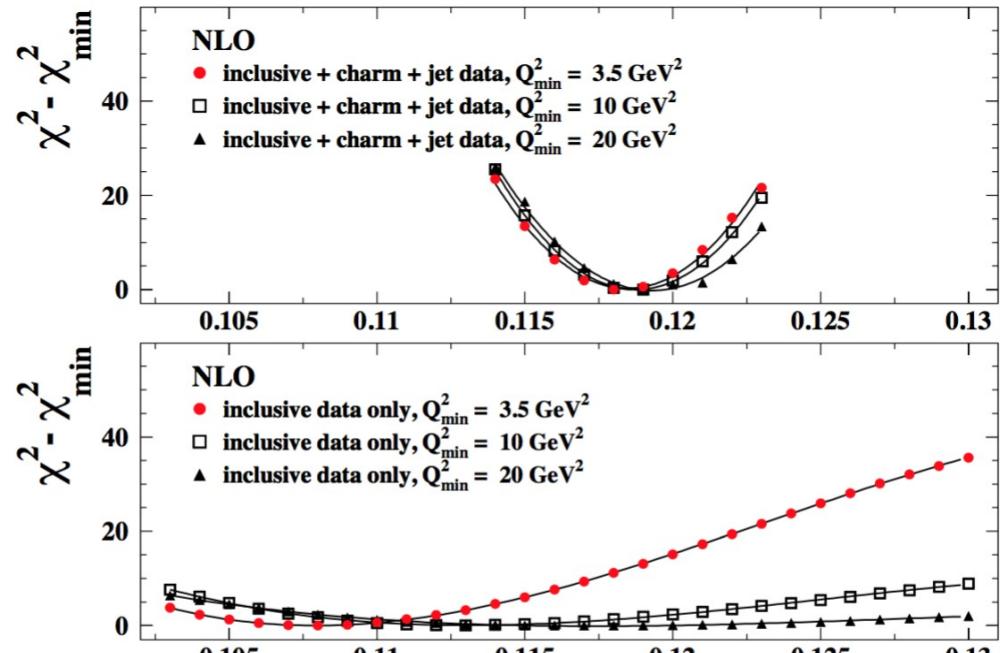
a)

- Alternative parameterisations checked
 - No negative gluon term and no NG but additional Dg parameter
→ both give the same result
 - consistent with nominal

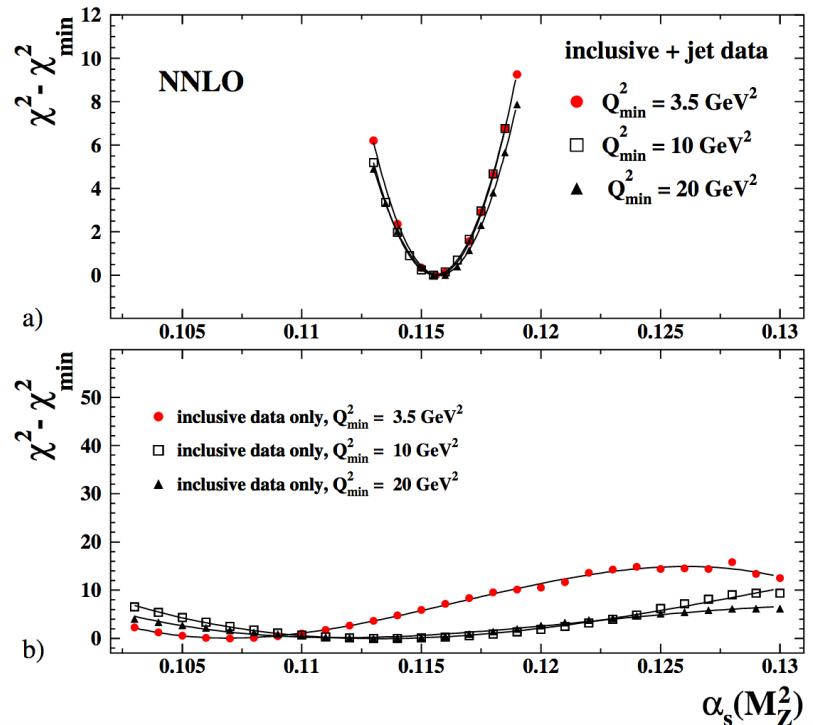
$$\alpha_s(M_Z^2) = 0.1151 \pm 0.0010 \text{ (exp)}$$

Completing NLO picture

H1 and ZEUS



H1 and ZEUS



- Similar behavior and level of precision at NLO and NNLO
- However direct comparison of 2015 and 2022 results not possible
→ different scale choice and slightly different jet data sets
- After unifying (details in backup)

$$\alpha_s(M_Z) = 0.1186 \pm 0.0014 \text{ (exp) NLO}$$

$$\alpha_s(M_Z) = 0.1144 \pm 0.0013 \text{ (exp) NNLO}$$

Comparison to other HERAPDF2.0 fits

- For previous NLO results scale uncertainty applied as 50% correlated and 50% uncorrelated between bins and data sets (due to inclusion of HQ and trijet data)
- Using the previous procedure at NNLO:

NNLO

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \quad {}^{+0.0001}_{-0.0002} \text{ (model + parameterisation)}$$

$$\pm 0.0022$$

HERAPDF2.0Jets NLO

$$\begin{aligned} \alpha_s(M_Z^2) = & 0.1183 \pm 0.0009 \text{(exp)} \pm 0.0005 \text{(model/parameterisation)} \\ & \pm 0.0012 \text{(hadronisation)} \quad {}^{+0.0037}_{-0.0030} \text{(scale)} . \end{aligned}$$

Scale uncertainties reduced
→ as expected for NNLO calculations

comparison to other HERA DIS results

1. H1 NNLO jet study using fixed PDFs, includes H1 inclusive-jet and di-jet:

| | | |
|---------|--------------|---|
| H1 jets | $\mu > 2m_b$ | 0.1170 (9) _{exp} (7) _{had} (5) _{PDF} (4) _{PDFα_s} (2) _{PDFset} (38) _{scale} |
|---------|--------------|---|

with similar breakup of uncertainties and similar μ , new HERA result:

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 (\text{exp+had+PDF})^{+0.0001}_{-0.0002} (\text{model + parameterisation}) \pm 0.0029 (\text{scale})$$

H1 also provided a **PDF+ α_s** fit
to H1 inclusive and jet data

| |
|---|
| 0.1147 (11) _{exp, NP, PDF} (2) _{mod} (3) _{par} (23) _{scale} |
|---|

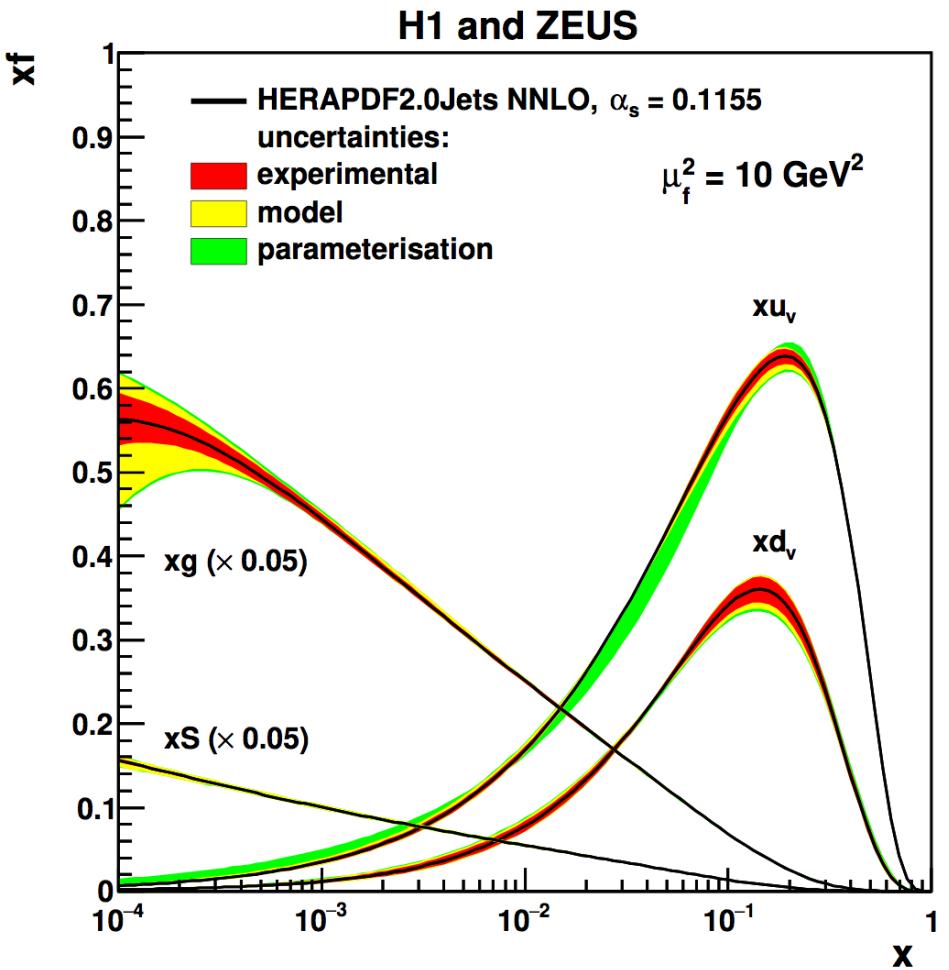
analysis required $Q^2 > 10\text{GeV}^2$; NEW HERA result re-evaluated with this cut (rather than $>3.5\text{GeV}^2$), is:

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 (\text{exp}) \pm 0.0002 (\text{model + parameterisation}) \pm 0.0021 (\text{scale})$$

2. NNLOJet+APPLfast using fixed PDFs, includes H1+ZEUS inclusive-jet:

| | | |
|---------------------|--------------|---|
| HERA inclusive jets | $\mu > 2m_b$ | 0.1171 (9) _{exp} (5) _{had} (4) _{PDF} (3) _{PDFα_s} (2) _{PDFset} (33) _{scale} |
|---------------------|--------------|---|

Fit with fixed $\alpha_s = 0.1155$



◆ Experimental uncertainties:

- Hessian method
- Conventional $\Delta\chi^2 = 1 \rightarrow 68\% \text{ CL}$

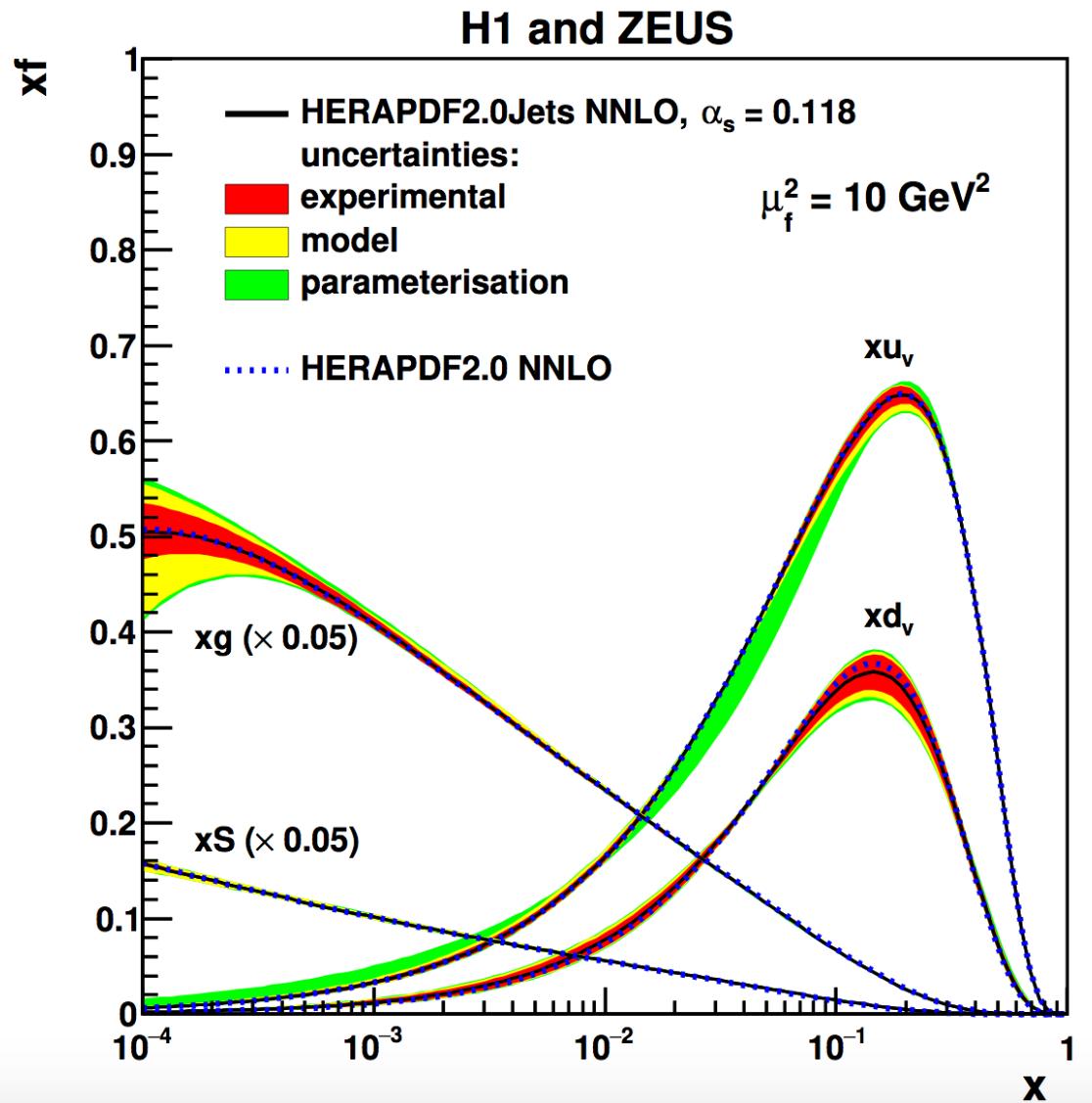
| Parameter | Central value | Downwards variation | Upwards variation |
|-----------------------------|---------------|---------------------|-------------------|
| $Q_{\min}^2 [\text{GeV}^2]$ | 3.5 | 2.5 | 5.0 |
| f_s | 0.4 | 0.3 | 0.5 |
| $M_c [\text{GeV}]$ | 1.41 | 1.37* | 1.45 |
| $M_b [\text{GeV}]$ | 4.20 | 4.10 | 4.30 |
| $\mu_{f0}^2 [\text{GeV}^2]$ | 1.9 | 1.6 | 2.2* |

Adding D and E parameters to each PDF

- ◆ Parametrisation uncertainties
 - largest deviation
- ◆ Model uncertainties
 - all variations added in quadrature

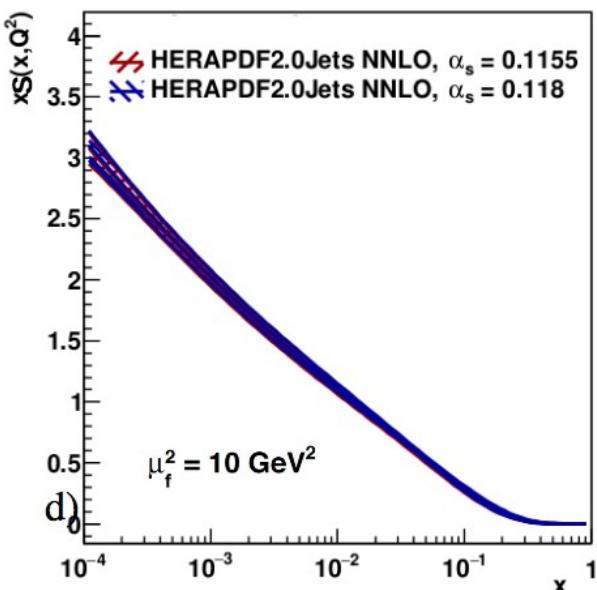
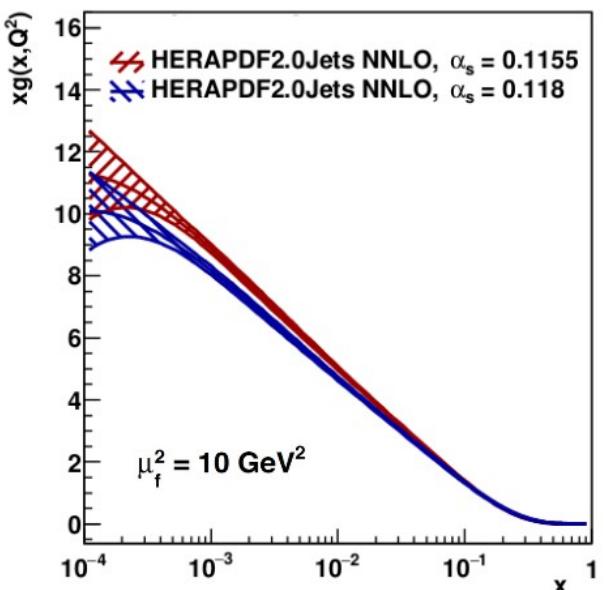
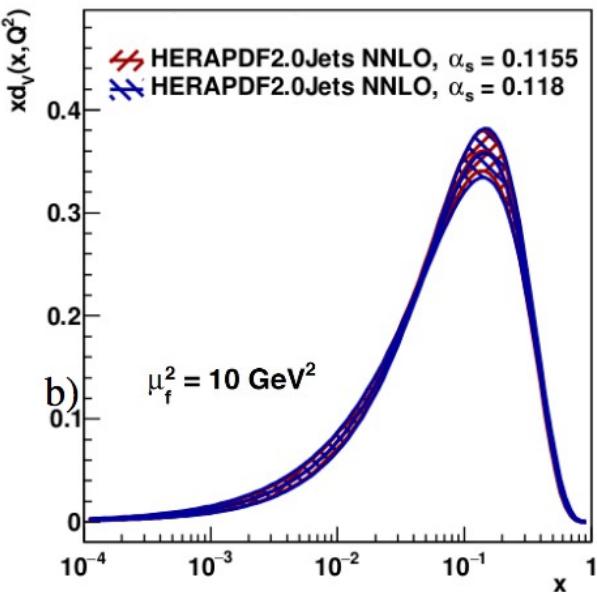
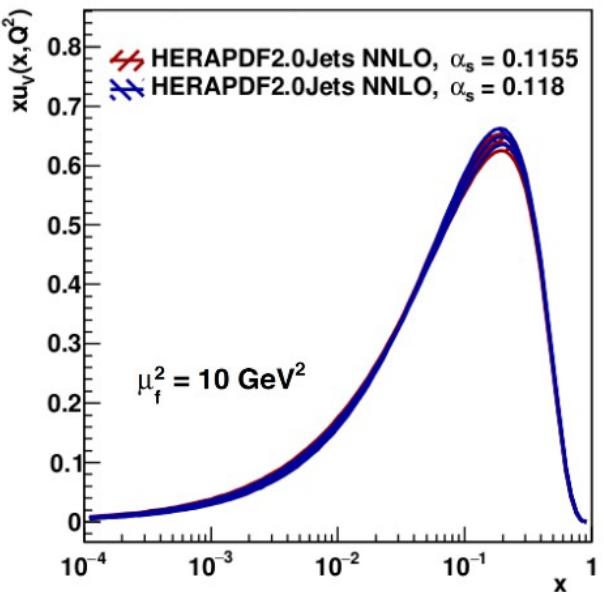
Fit with fixed $\alpha_s = 0.118$

How does it compare to HERAPDF2.0? Well!

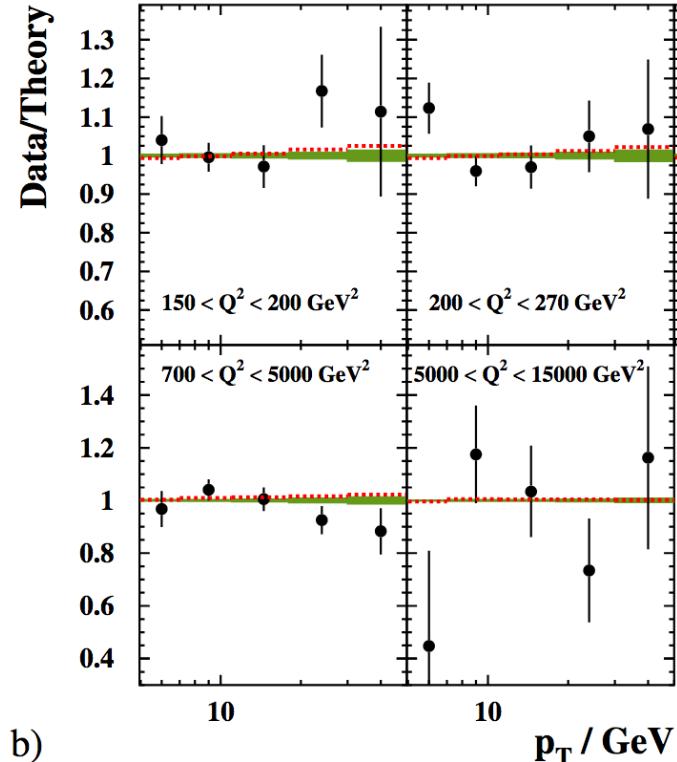


... and how it compares to $\alpha_s = 0.1155$

H1 and ZEUS



H1 and ZEUS



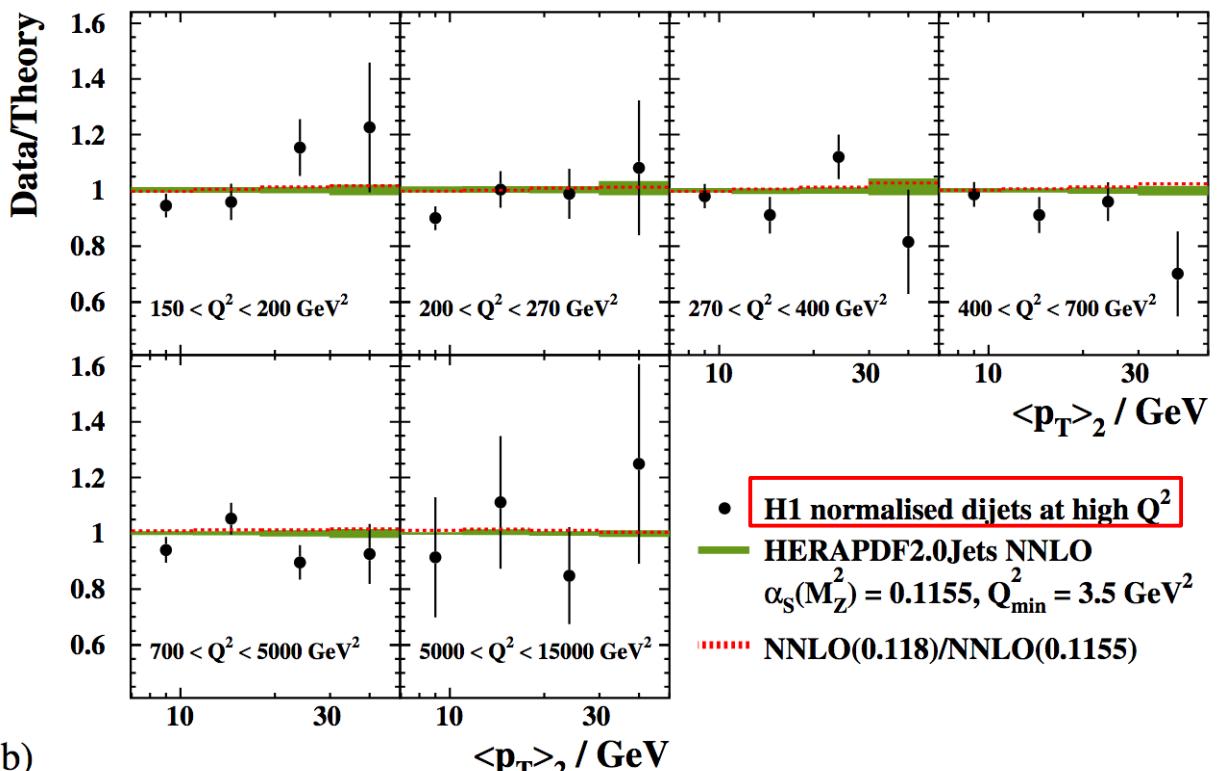
b)

• H1 norm. inclusive jets at high Q^2

— HERAPDF2.0Jets NNLO
 $\alpha_S(M_Z^2) = 0.1155, Q_{\min}^2 = 3.5 \text{ GeV}^2$
··· NNLO(0.118)/NNLO(0.1155)

Comparison of theory predictions to H1 HERA II normalised jets @ high Q^2
→ good agreement for all data used in PDF fits

H1 and ZEUS



b)

• H1 normalised dijets at high Q^2

— HERAPDF2.0Jets NNLO
 $\alpha_S(M_Z^2) = 0.1155, Q_{\min}^2 = 3.5 \text{ GeV}^2$
··· NNLO(0.118)/NNLO(0.1155)

Message to take away

- HERAPDF2.0 family completed
→ NNLO fit including jet data performed
- Two new PDF sets
→ HERAPDF2.0Jets NNLO $\alpha_s(M_Z) = 0.118 \rightarrow \text{PDG}$
→ HERAPDF2.0Jets NNLO $\alpha_s(M_Z) = 0.1155 \rightarrow \text{value favored by our fit}$
- Jet data allow us to constrain $\alpha_s(M_Z)$

$$\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \quad {}^{+0.0001}_{-0.0002} \text{ (model + parameterisation)} \quad \pm 0.0029 \text{ (scale)}$$

- Comparing to NLO at the same footing

NNLO $\alpha_s(M_Z^2) = 0.1156 \pm 0.0011 \text{ (exp)} \quad {}^{+0.0001}_{-0.0002} \text{ (model + parameterisation)}$
±0.0022

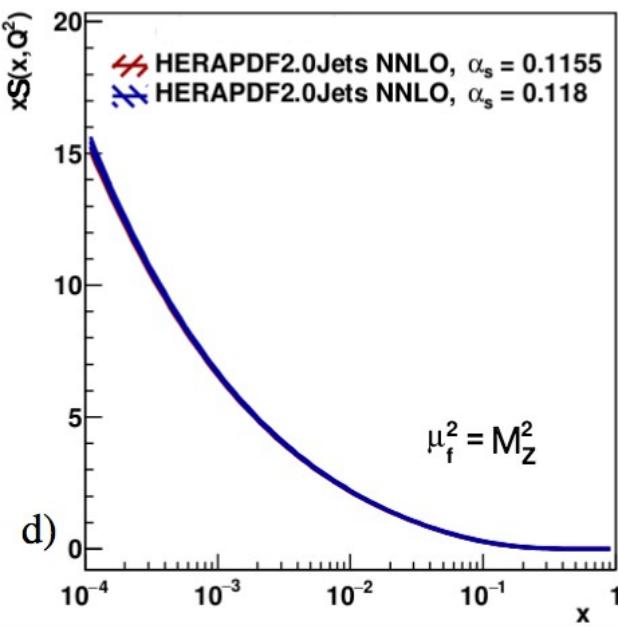
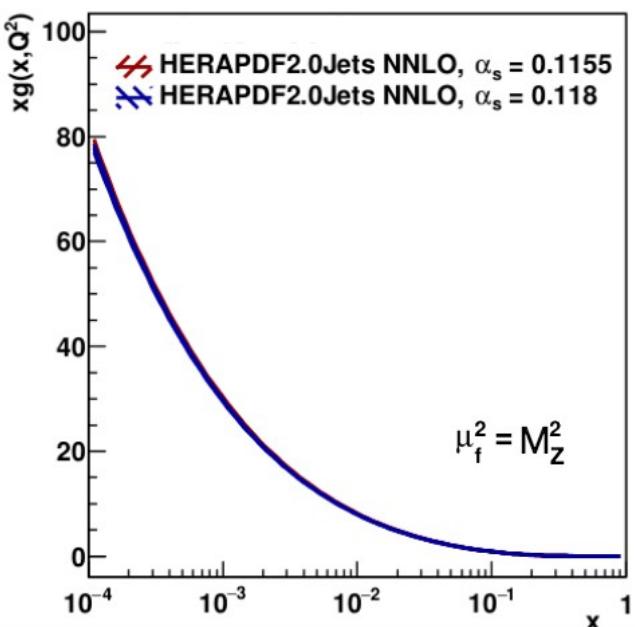
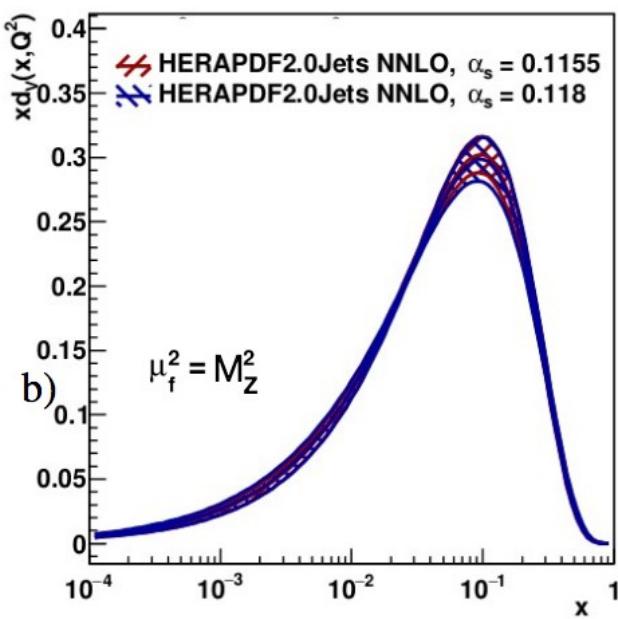
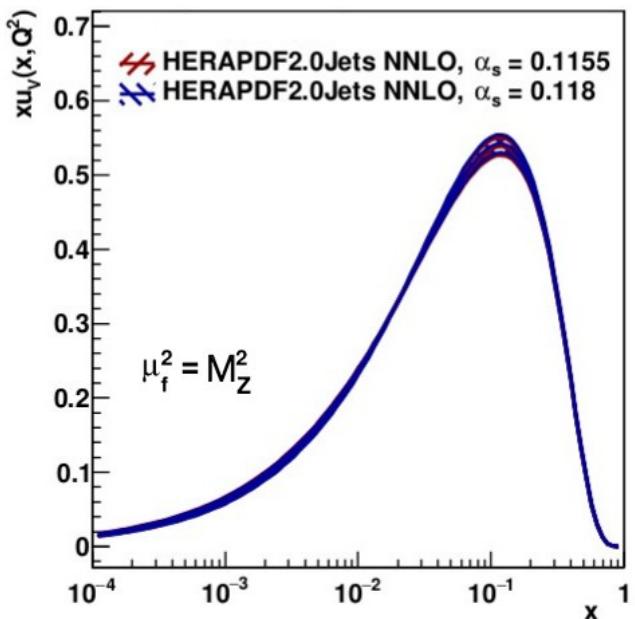
NLO $\alpha_s(M_Z^2) = 0.1183 \pm 0.0009 \text{ (exp)} \pm 0.0005 \text{ (model/parameterisation)}$
 $\pm 0.0012 \text{ (hadronisation)} \quad {}^{+0.0037}_{-0.0030} \text{ (scale)} .$

Systematic shift downwards at NNLO and reduction of scale uncertainty

Additional slides

... and how it compares to $\alpha_s = 0.1155$

H1 and ZEUS



Some remarks on NLO to NNLO comparison- (not in the paper)

Our present NNLO result using $\frac{1}{2}$ correlated and $\frac{1}{2}$ uncorrelated scale uncertainty

$$\alpha_s(M_Z) = 0.1156 \pm 0.0011(\text{exp})^{+0.0001}_{-0.0002} (\text{model+parametrisation} \pm 0.0022(\text{scale}))$$

where “exp” denotes the experimental uncertainty which is taken as the fit uncertainty, including the contribution from hadronisation uncertainties.

Maybe compared with the NLO result

$$\alpha_s(M_Z) = 0.1183 \pm 0.0008(\text{exp}) \pm 0.0012(\text{had})^{+0.0003}_{-0.0005} (\text{mod/param})^{+0.0037}_{-0.003} (\text{scale})$$

BUT

- the choice of scale was different;
- the NLO result did not include the recently published H1 low- Q^2 inclusive and dijet data [28];
- the NLO result did not include the newly published low p_T points from the H1 high- Q^2 inclusive data;
- the NNLO result does not include trijet data;
- the NNLO result does not include the low p_T points from the ZEUS dijet data;
- the NNLO analysis imposes a stronger kinematic cut $\mu > 10 \text{ GeV}$
- the treatment of hadronisation uncertainty differs.

All these changes with respect to the NLO analysis had to be made to create a consistent environment for a fit at NNLO. at the same time, an NLO fit cannot be done under exactly the same conditions as the NNLO fit since the H1 low Q^2 data cannot be well fitted at NLO. However, an NLO and an NNLO fit can be done under the common conditions:

(from A. Cooper-Sarkar, alpha-s 2022 workshop)

An NLO and an NNLO fit can be done under the common conditions:

- choice of scale, $\mu_f^2 = \mu_r^2 = Q^2 + p_T^2$;
- exclusion of the H1 low- Q^2 inclusive and dijet data;
- exclusion of the low- p_T points from the H1 high- Q^2 inclusive jet data;
- exclusion of trijet data;
- exclusion of low- p_T points from the ZEUS dijet data;
- exclusion of data with $\mu < 10$ GeV
- hadronisation uncertainties treated as correlated systematic uncertainties as done in the NNLO analysis.

The values of $\alpha_s(M_Z)$ obtained for these conditions are:

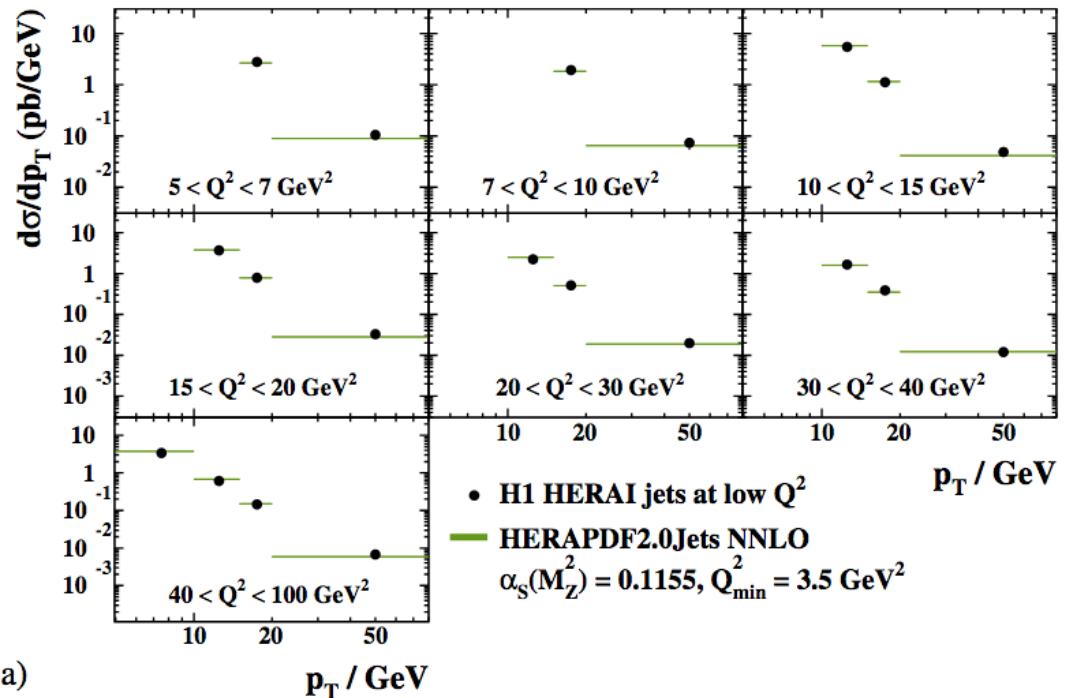
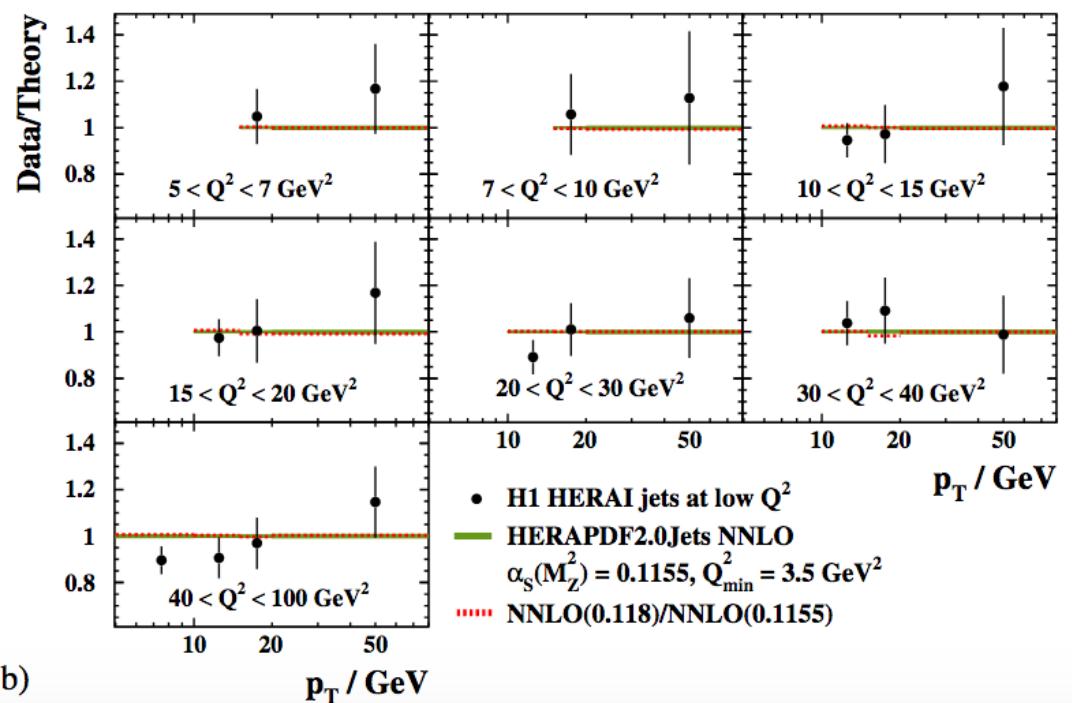
0.1186 ± 0.0014 (exp) NLO and 0.1144 ± 0.0013 (exp) NNLO.

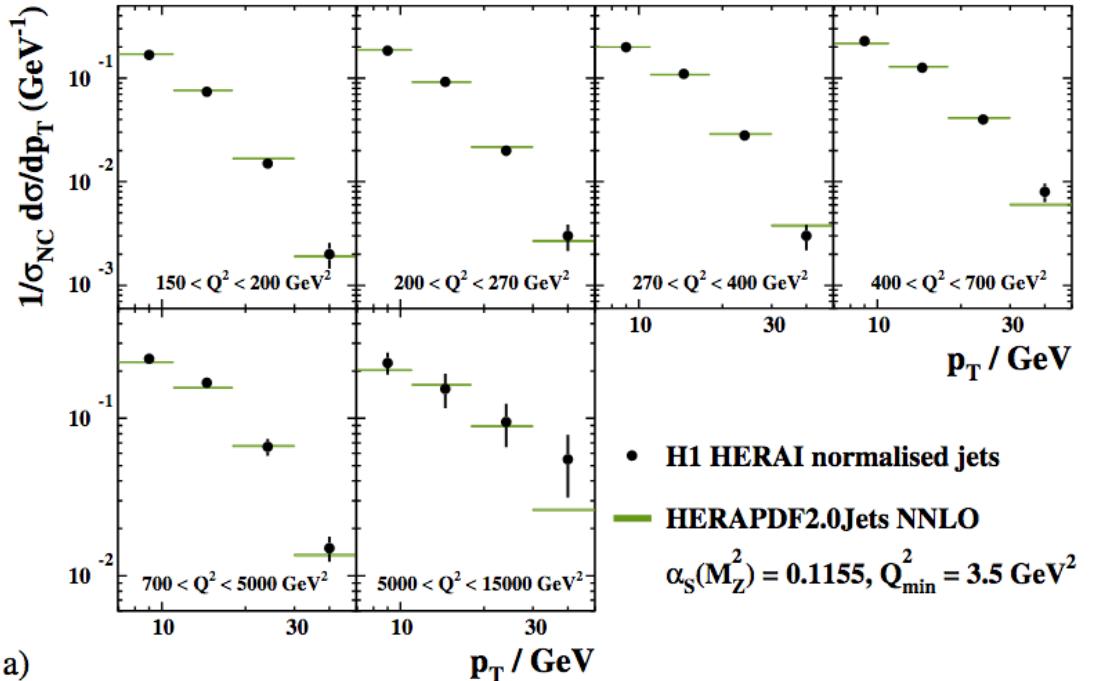
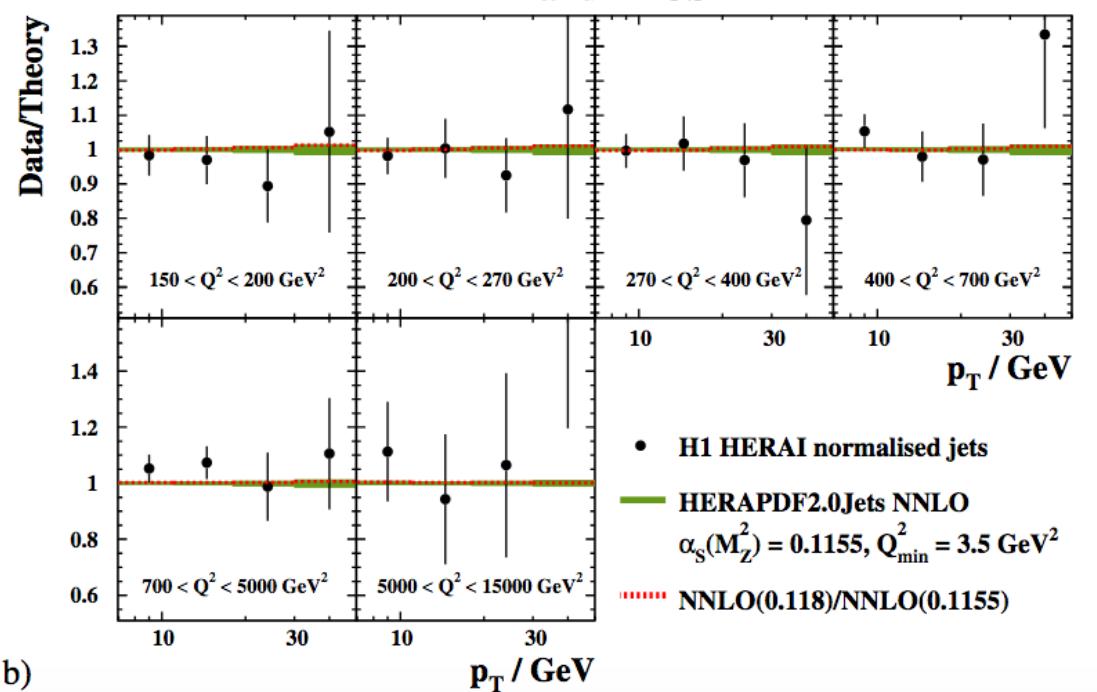
The change of the NNLO value from the preferred value of 0.1156 is mostly due to the exclusion of the H1 low Q^2 data and the low- p_T points at high Q^2 .

What do we mean when we say the H1 low Q^2 jets cannot be well fitted at NLO?

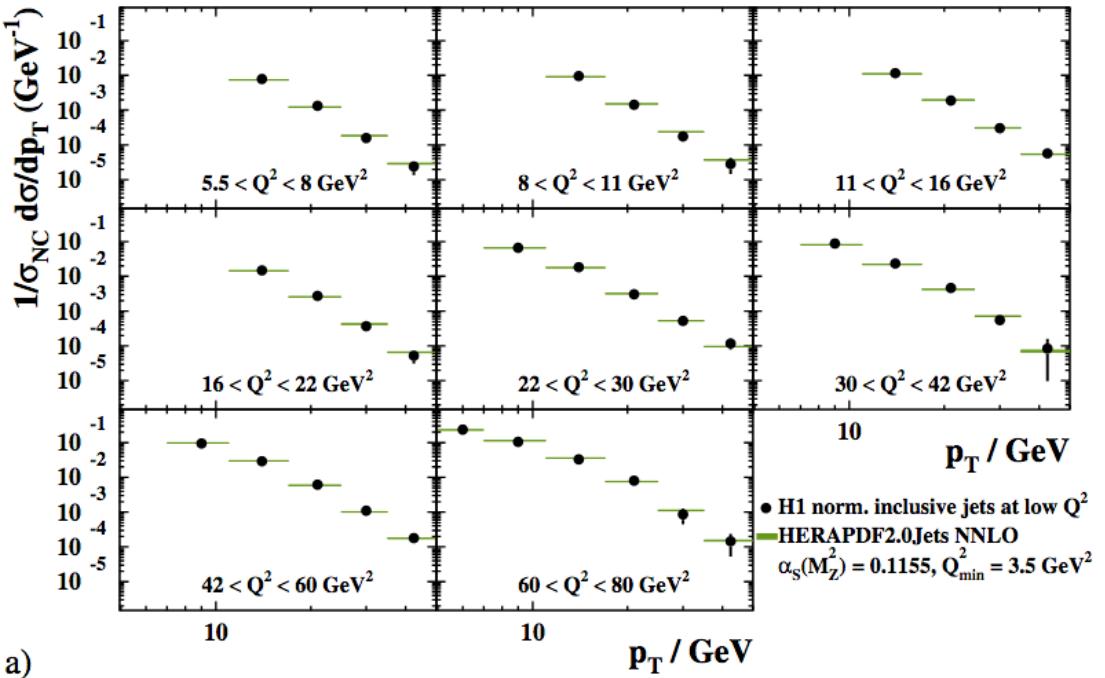
Simply this, that at NNLO the increase in overall χ^2 of the fit when the 74 data pts of these data are added is ~ 80 (exact value depends on $\alpha_s(M_Z)$ and on scale choice)

Whereas at NLO the increase in overall χ^2 of the fit when the 74 data pts of these data are added is ~ 180 .

H1 and ZEUS**H1 and ZEUS**

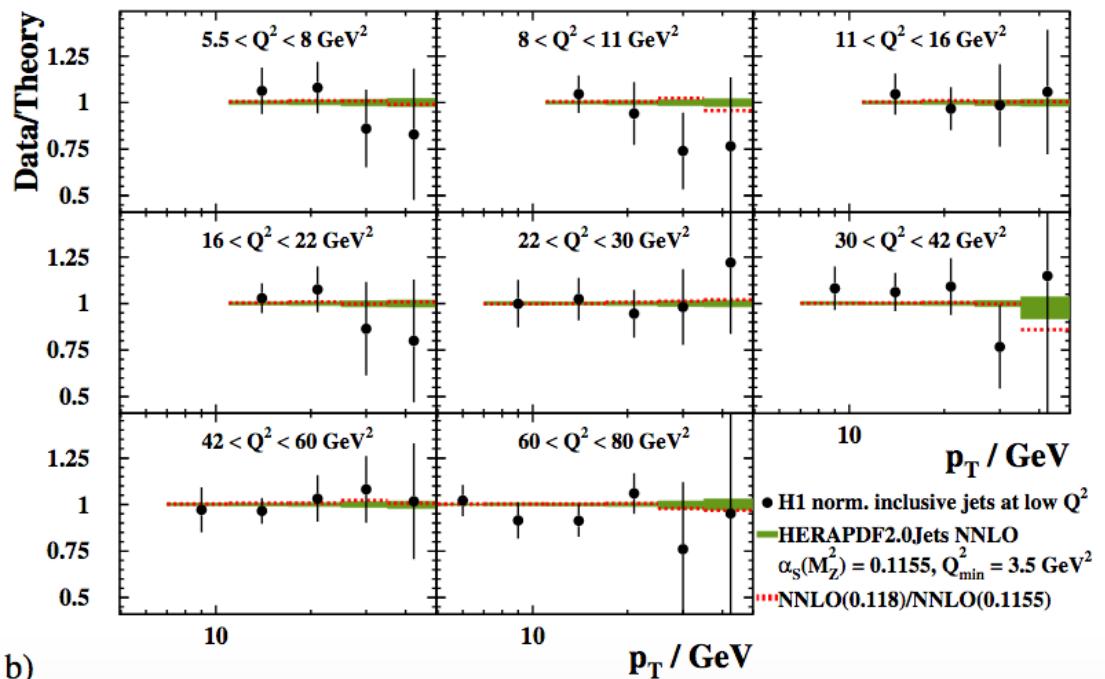
H1 and ZEUS**H1 and ZEUS**

H1 and ZEUS

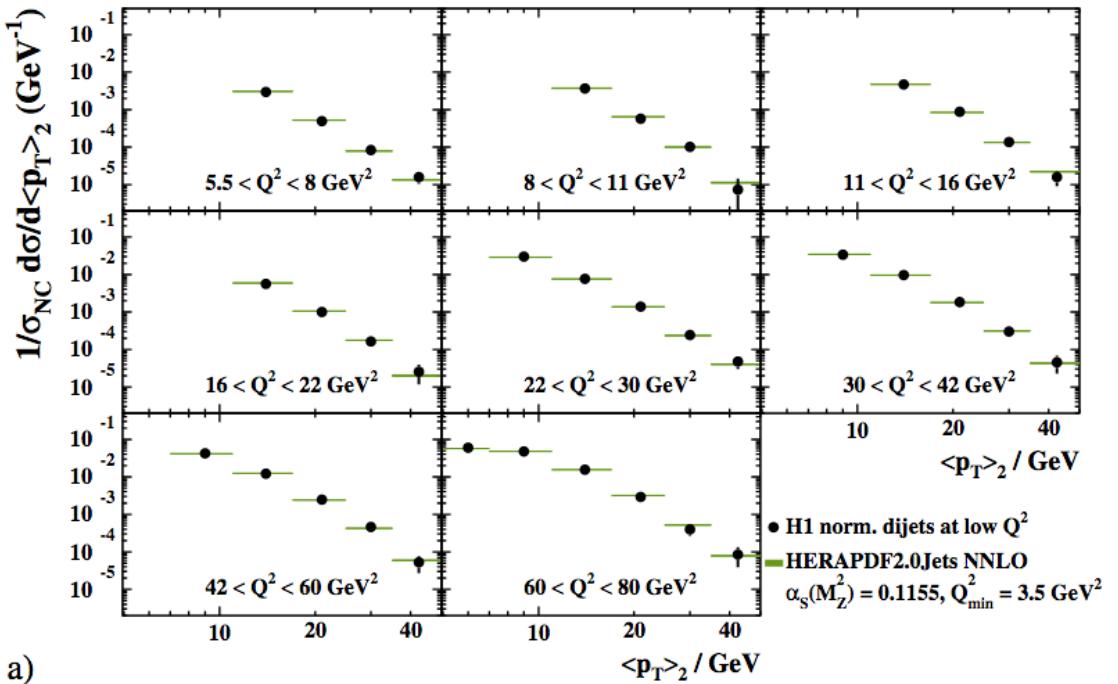


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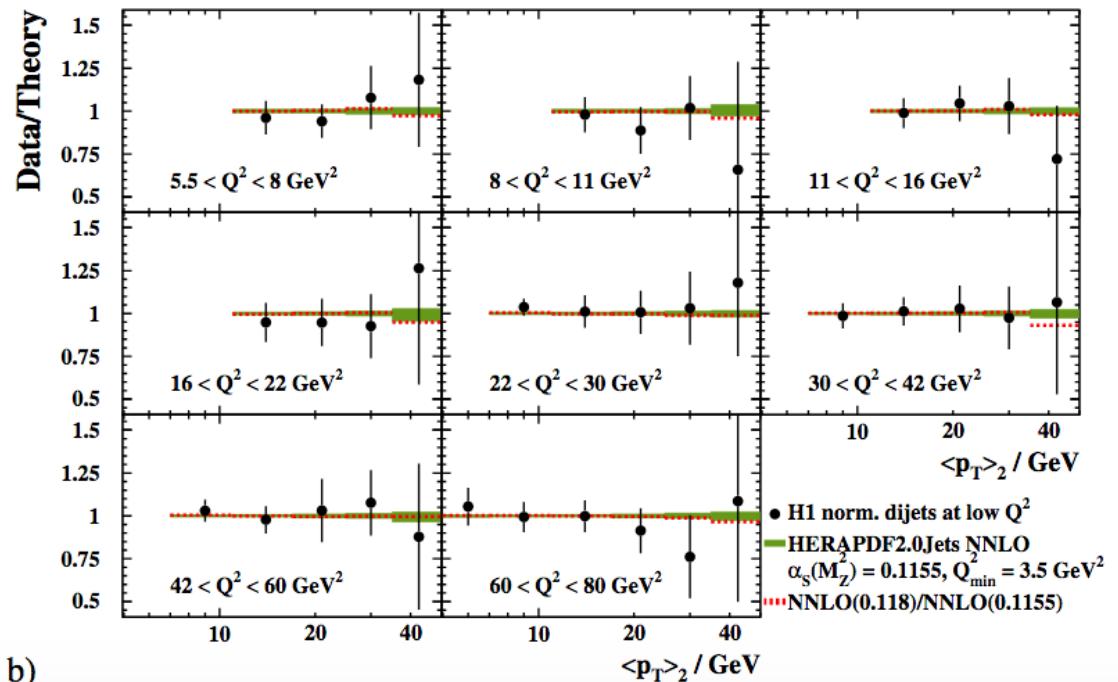
H1 and ZEUS



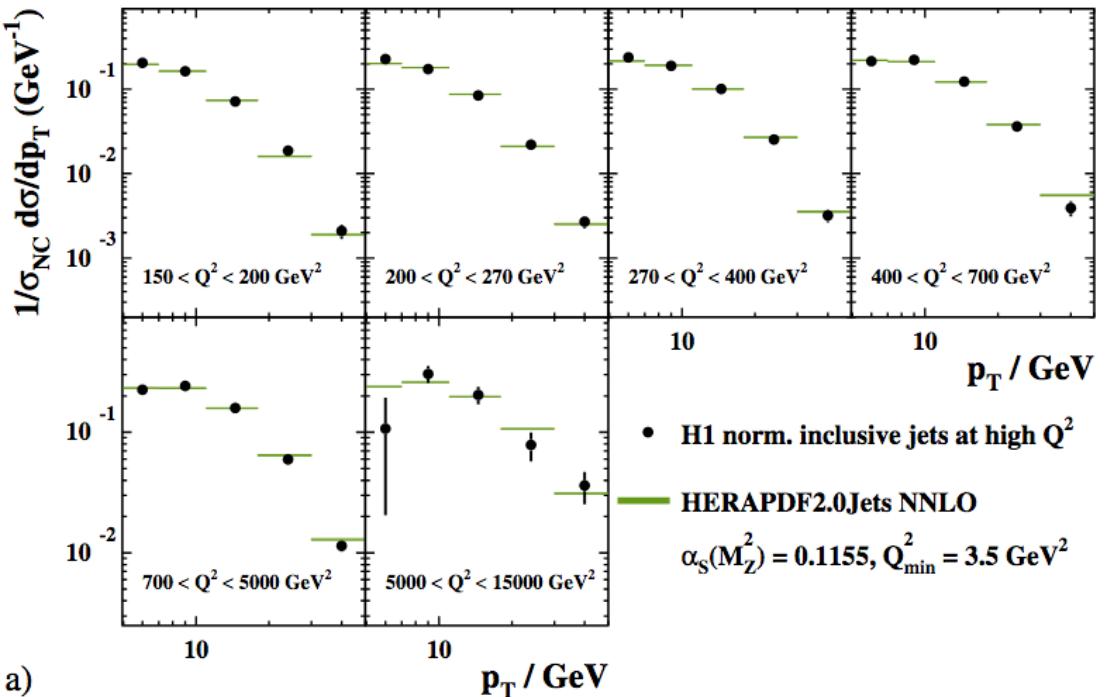
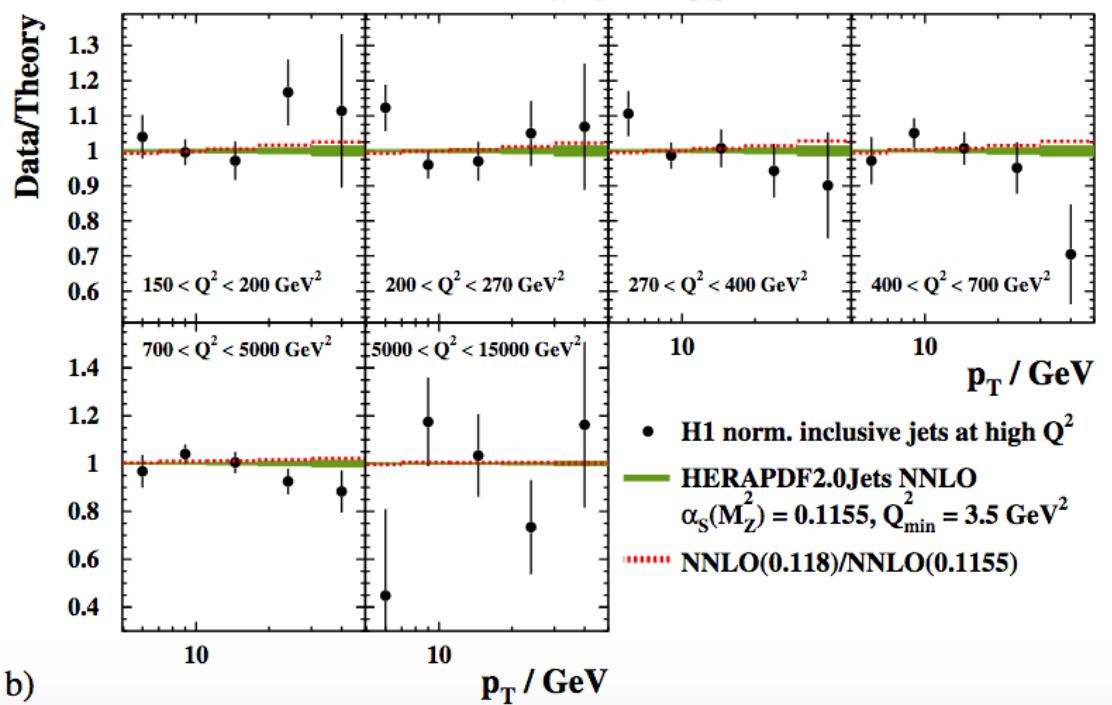
b)

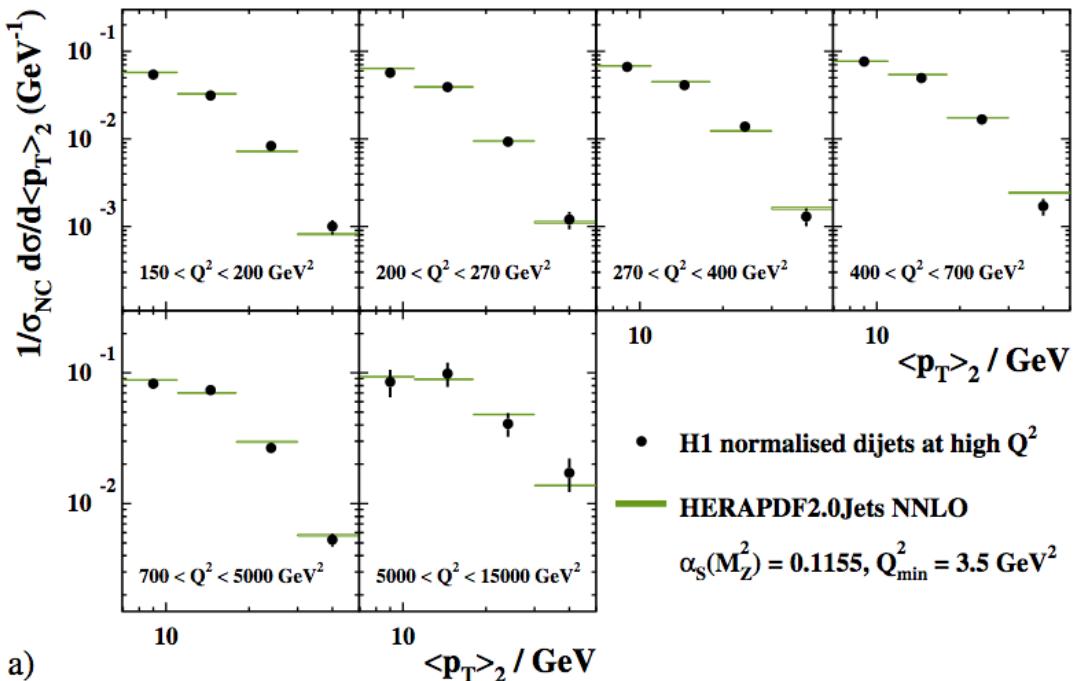
H1 and ZEUS

a)

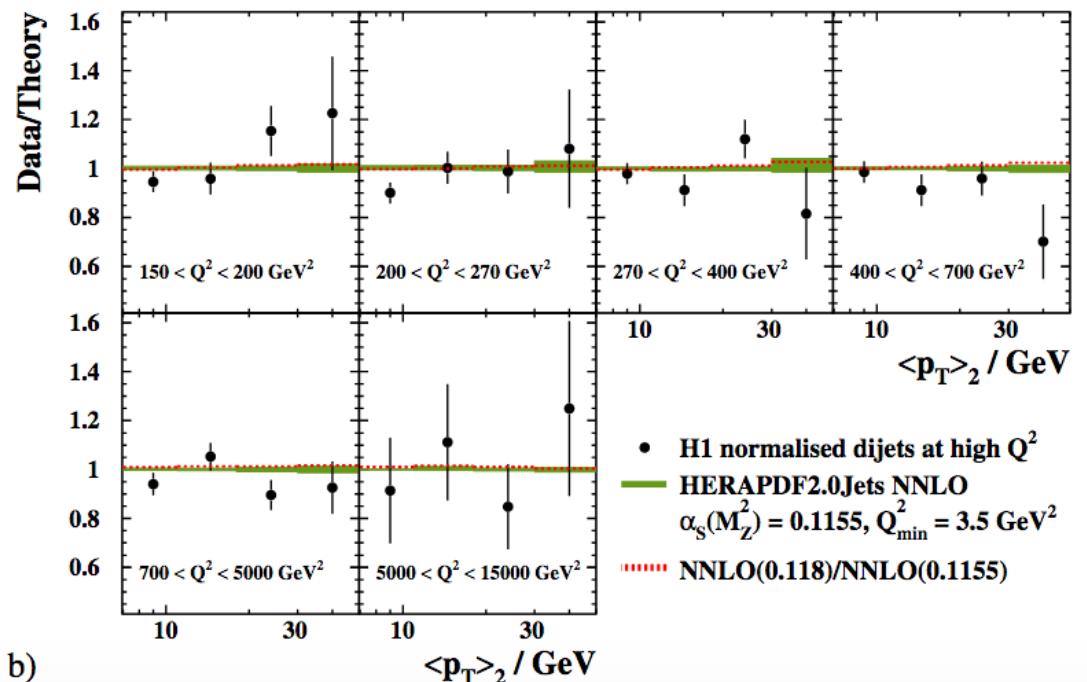
H1 and ZEUS

b)

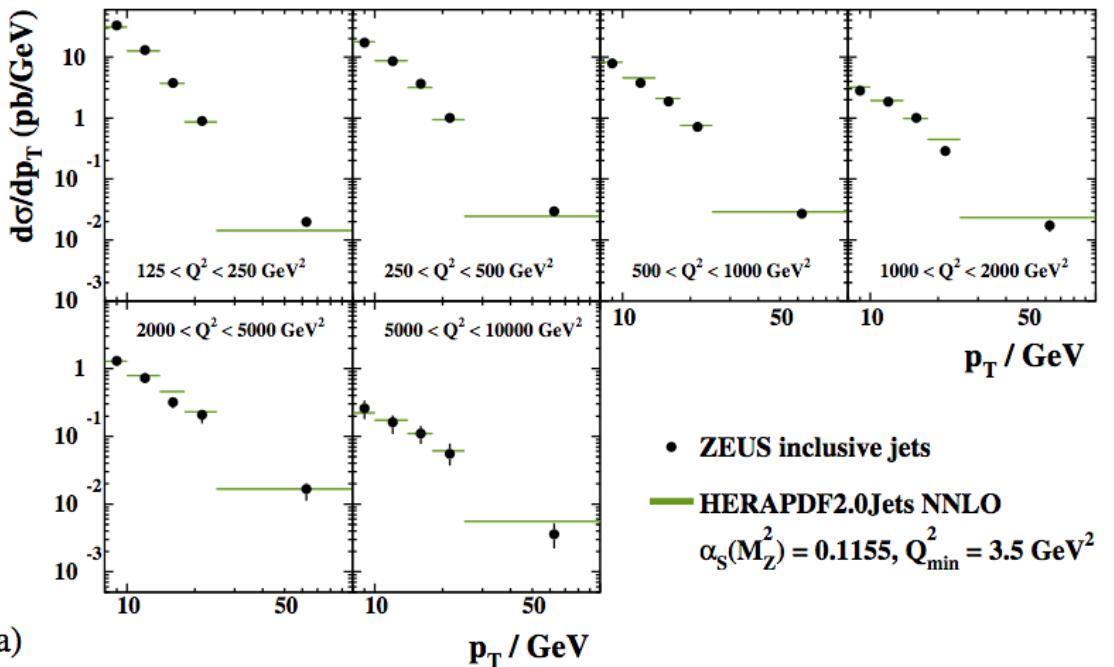
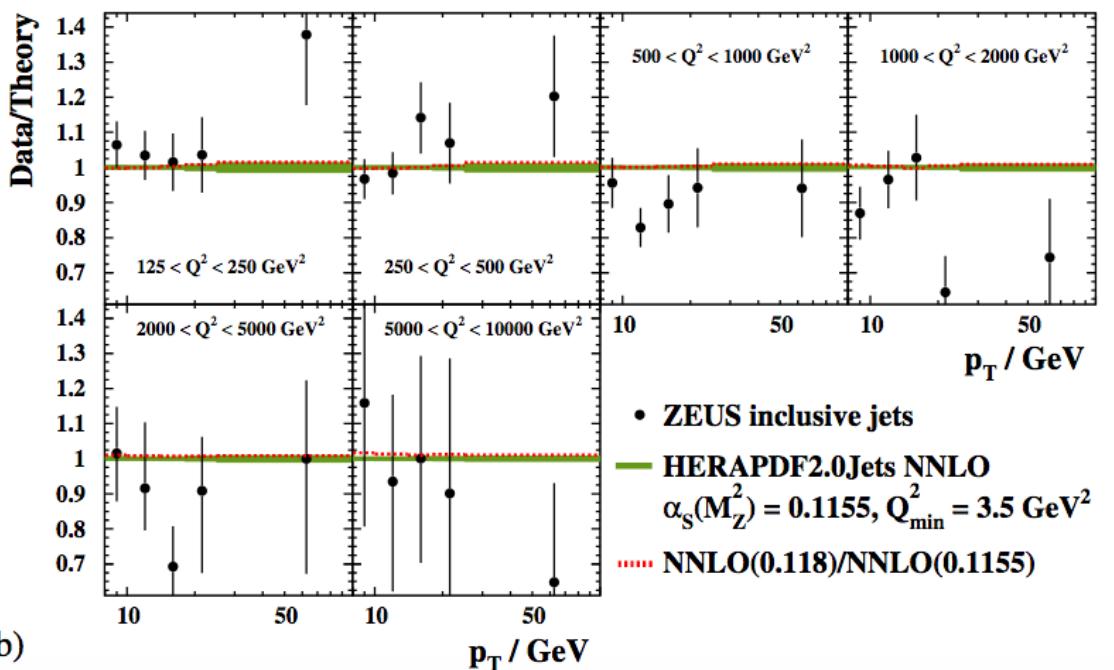
H1 and ZEUS**H1 and ZEUS**

H1 and ZEUS

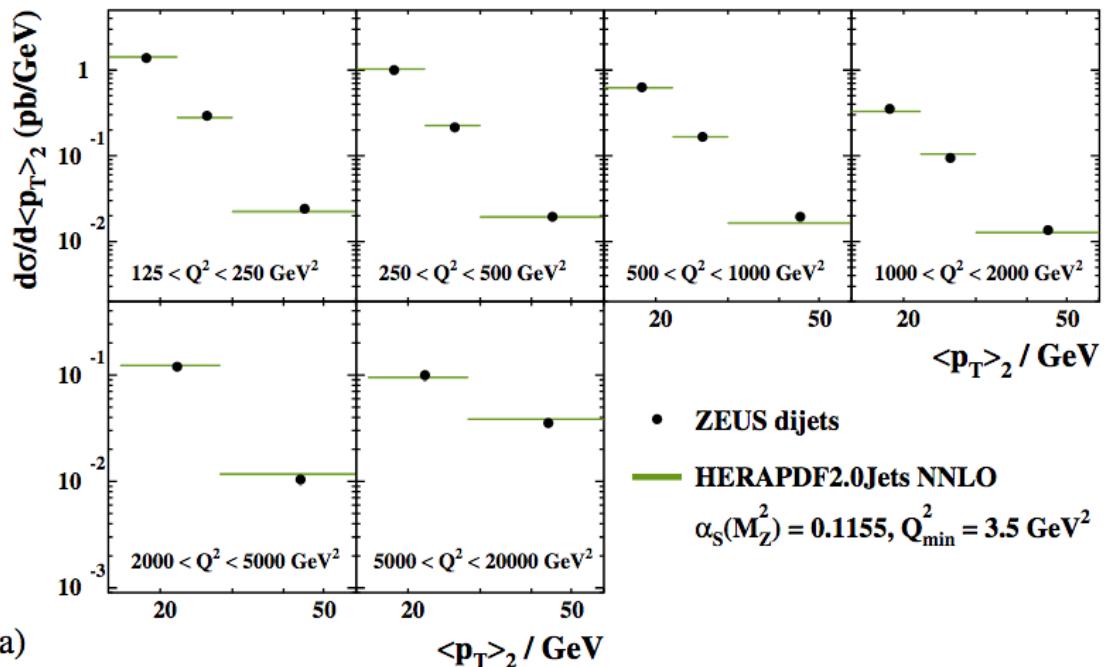
a)

H1 and ZEUS

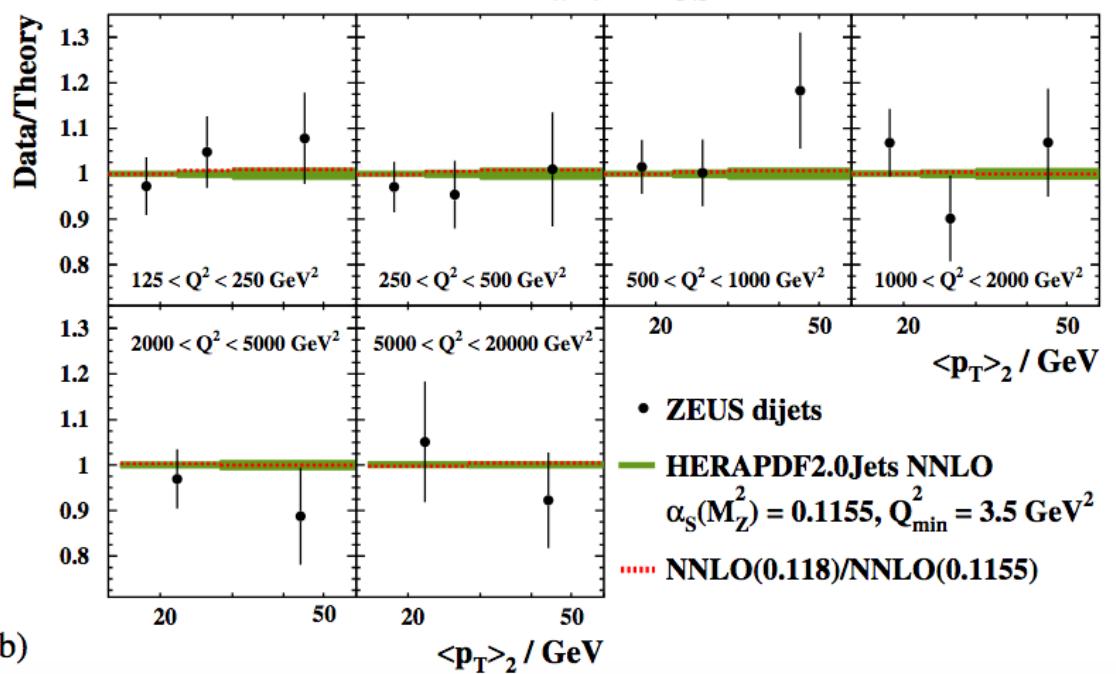
b)

H1 and ZEUS**H1 and ZEUS**

H1 and ZEUS

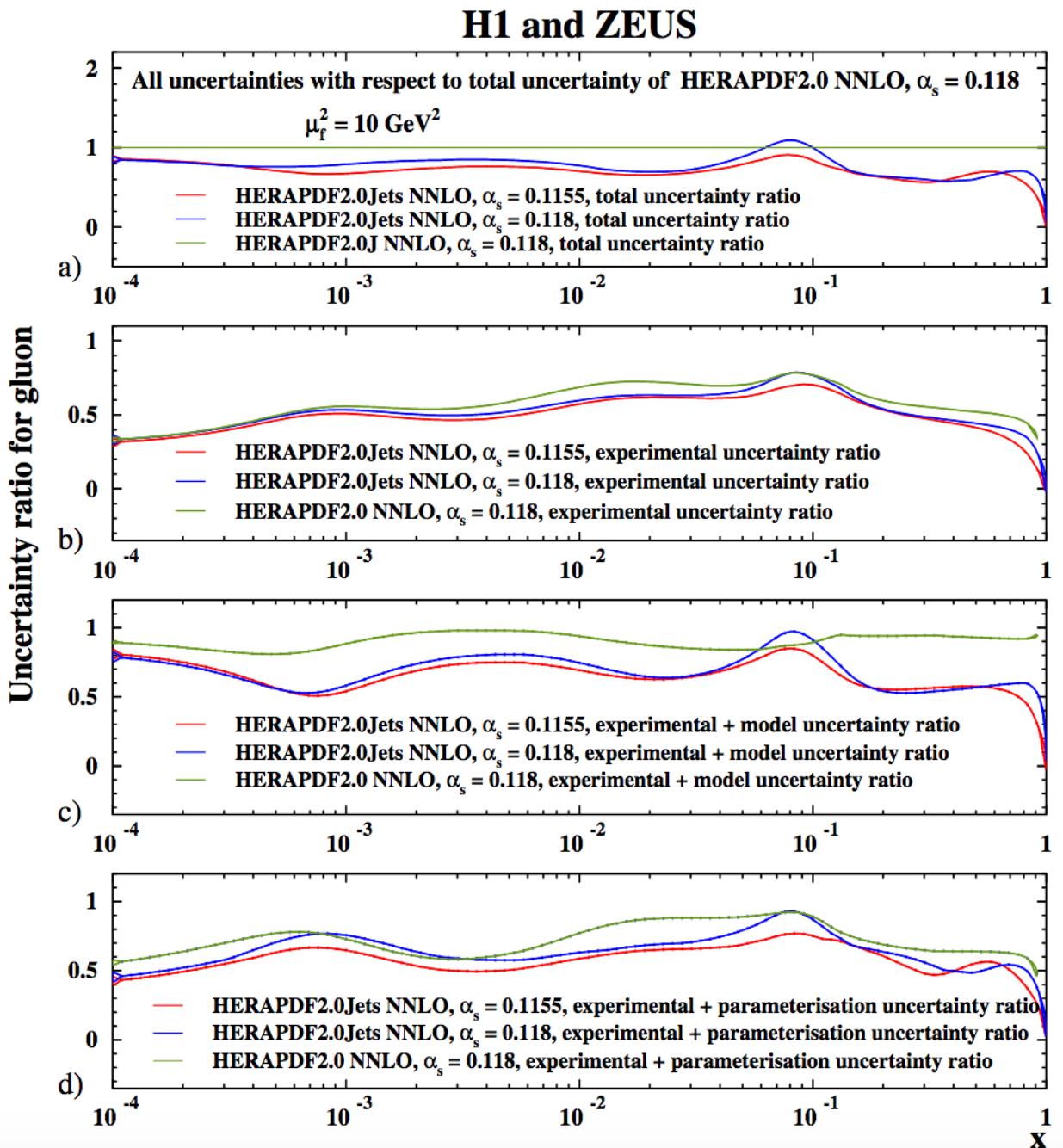


H1 and ZEUS



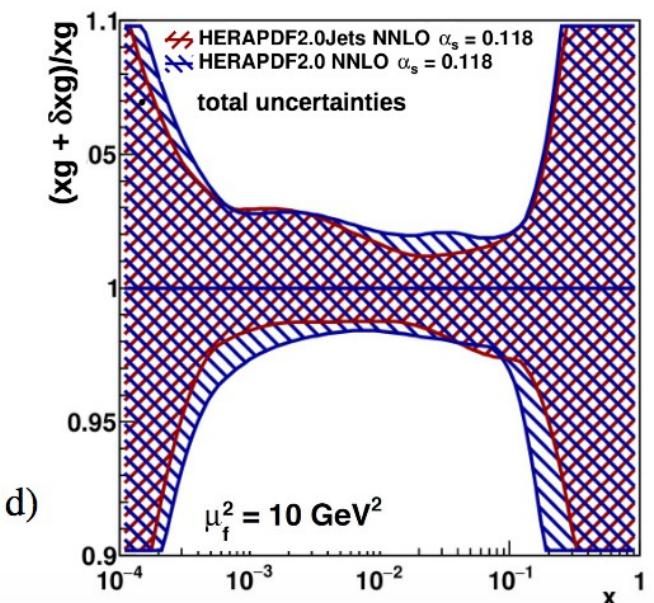
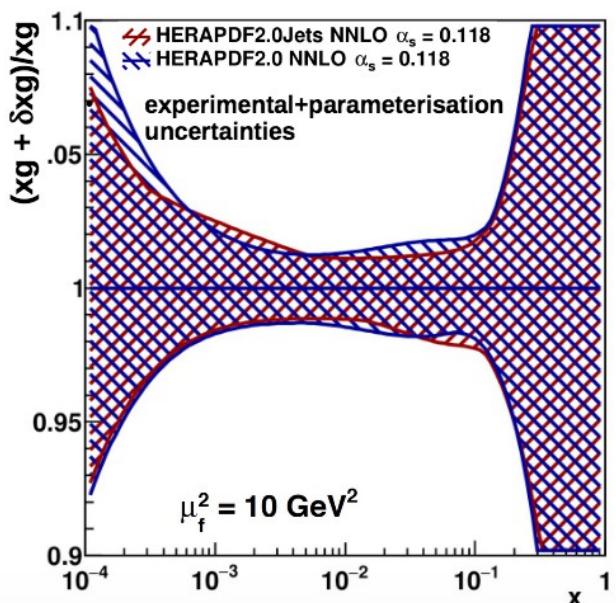
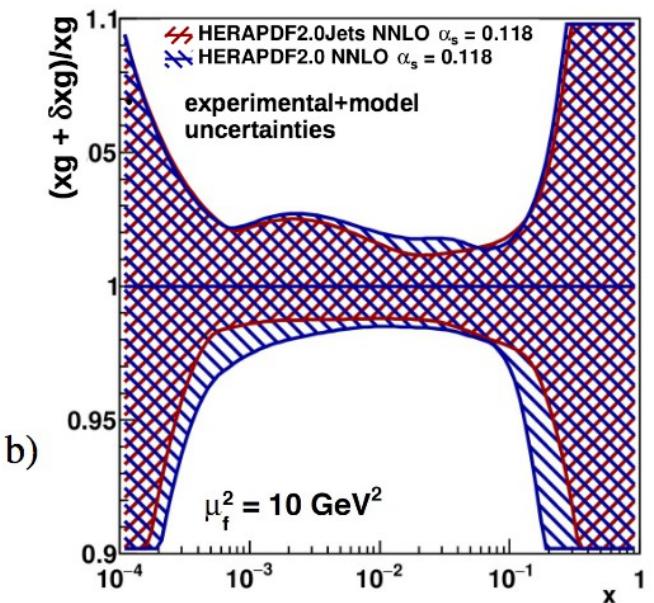
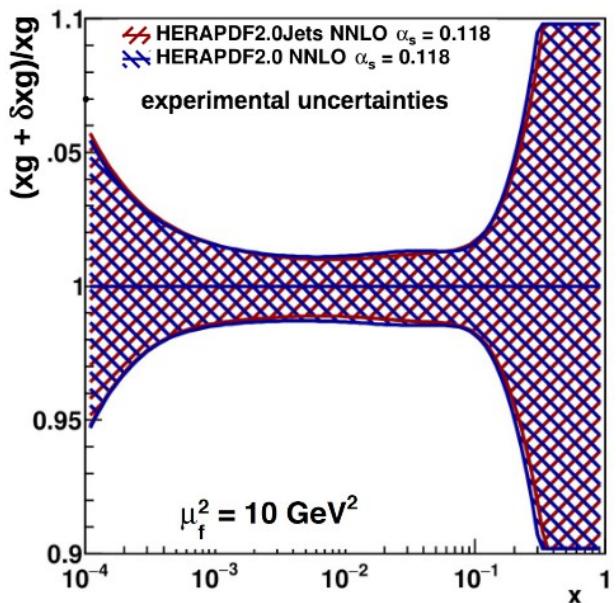
Uncertainties

- Reduction of low- x gluon ($x < 10^{-3}$) uncertainties due to reduced model/param uncertainties in variations of M_c and μ_f^2
- Reduction of high- x gluon ($x > 10^{-3}$) uncertainties due to reduced model/param/exp uncertainties
- The same for other scales



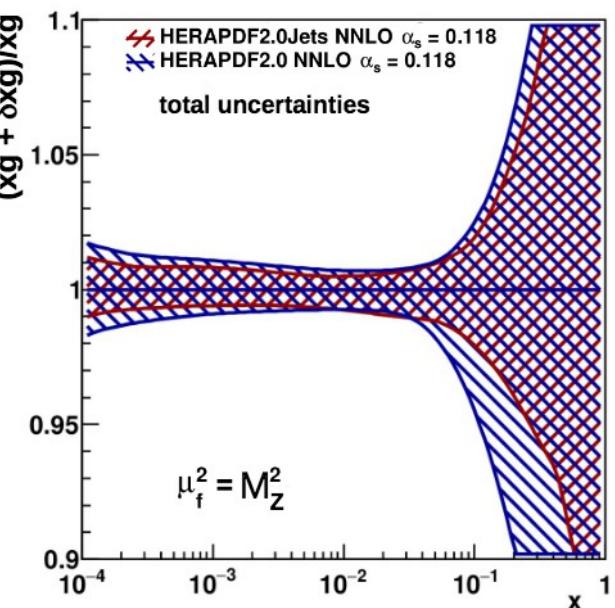
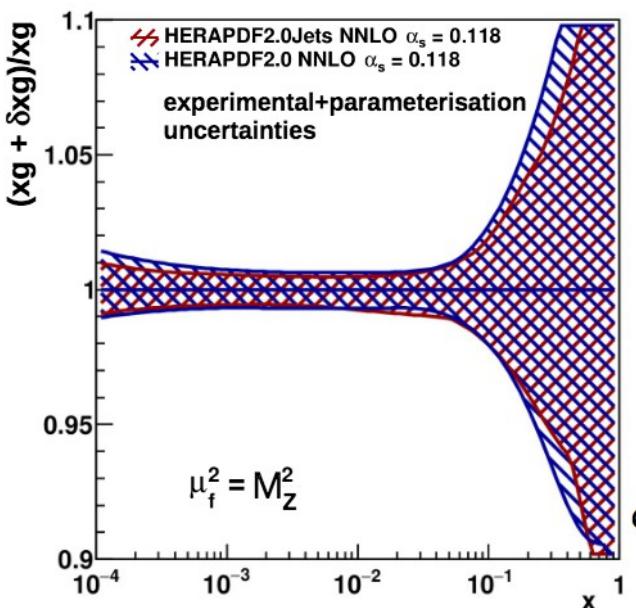
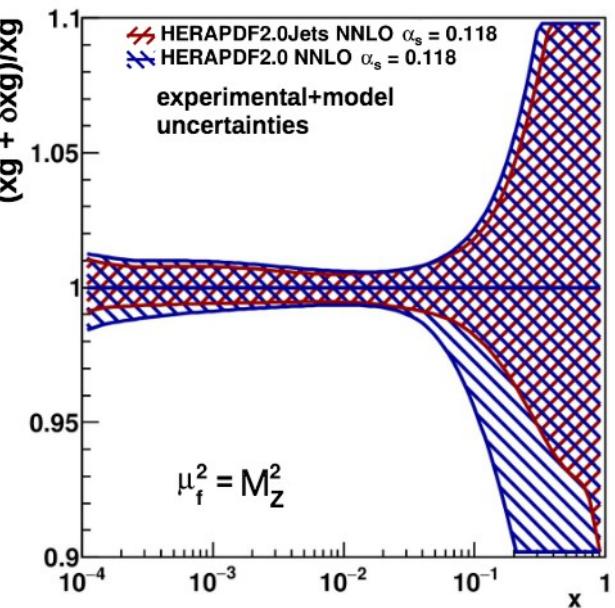
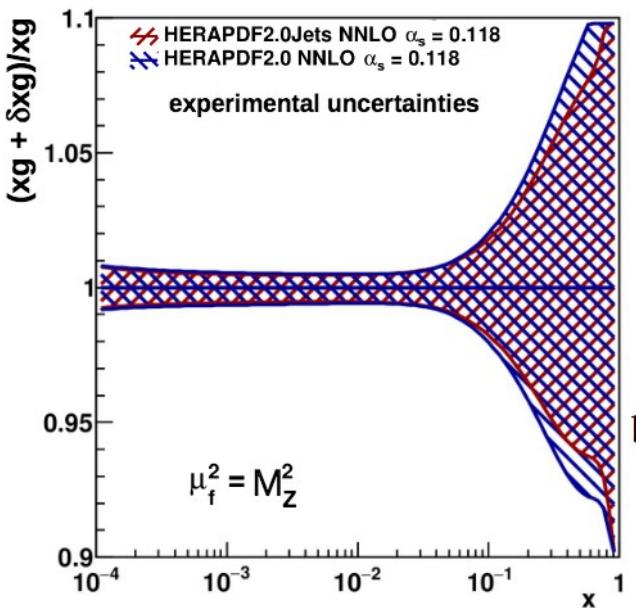
Uncertainties

H1 and ZEUS



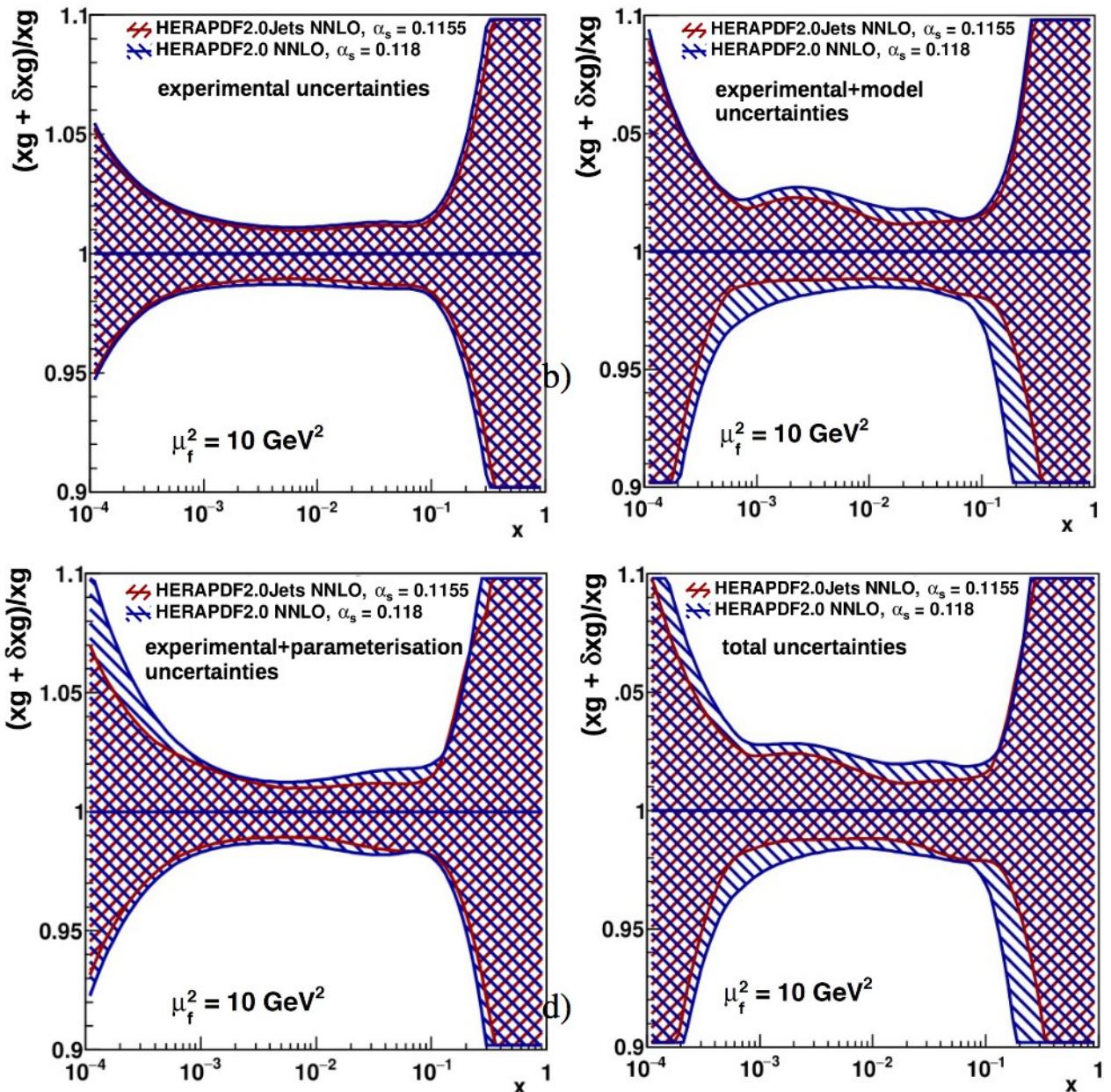
Uncertainties

H1 and ZEUS



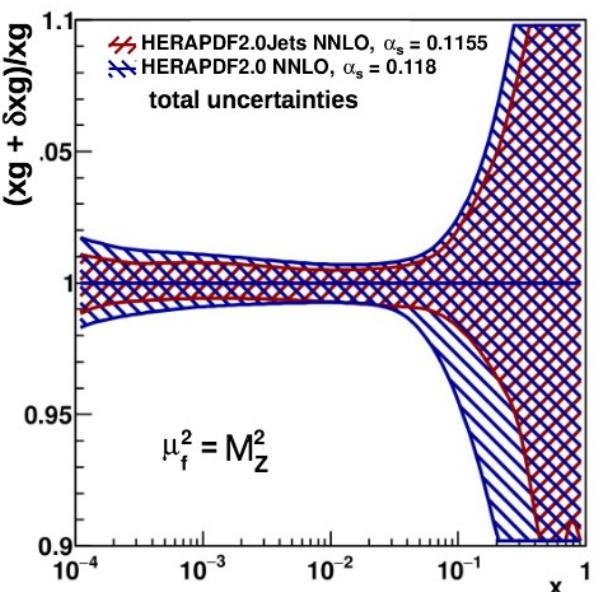
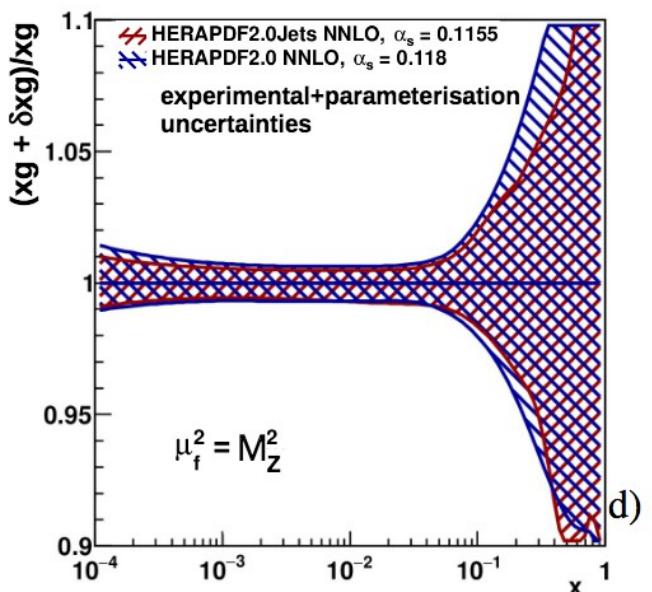
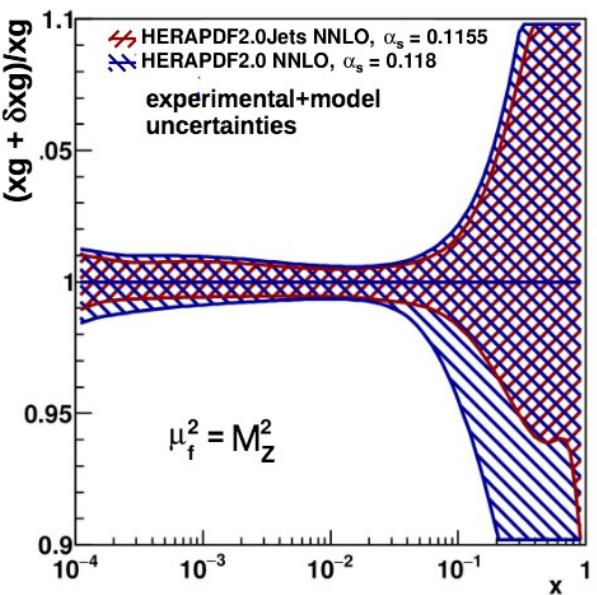
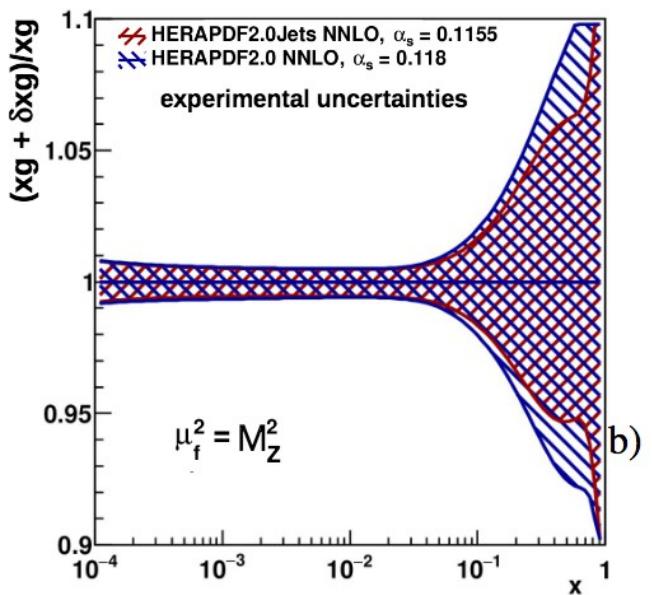
Uncertainties

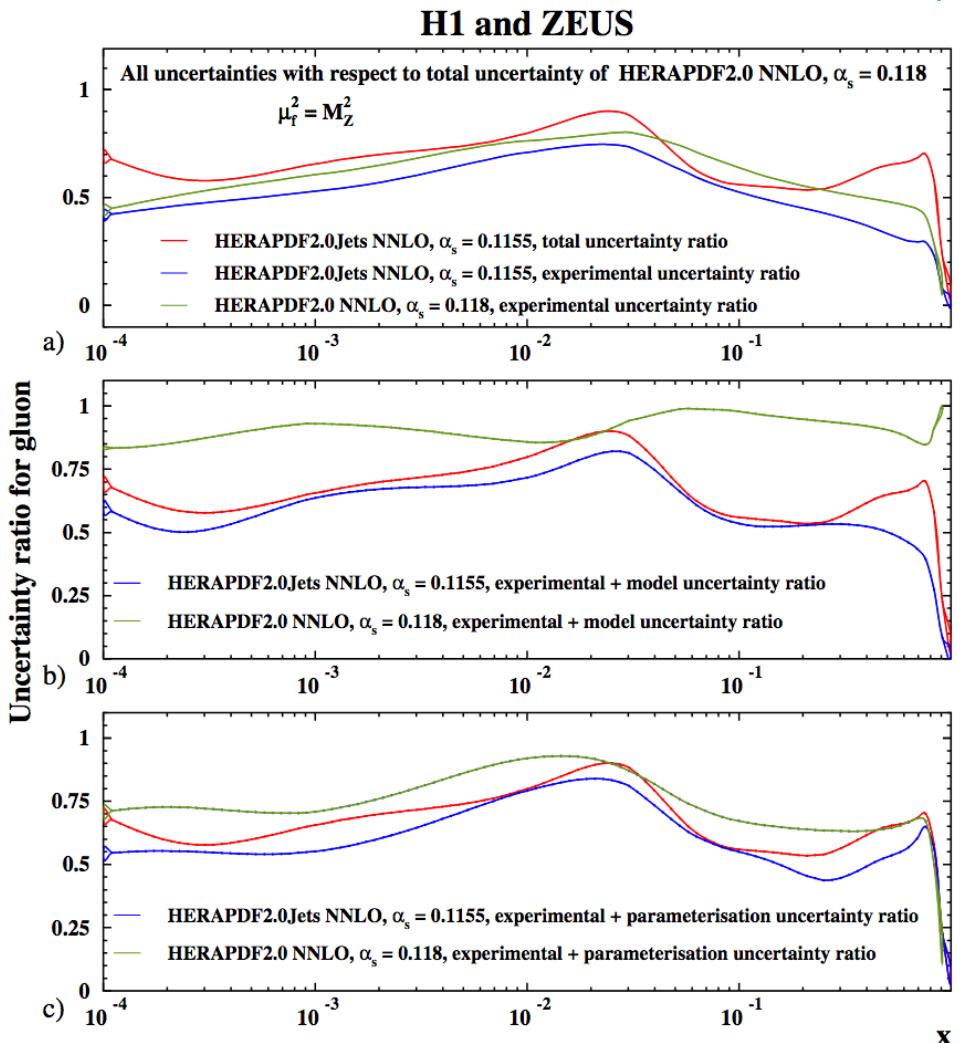
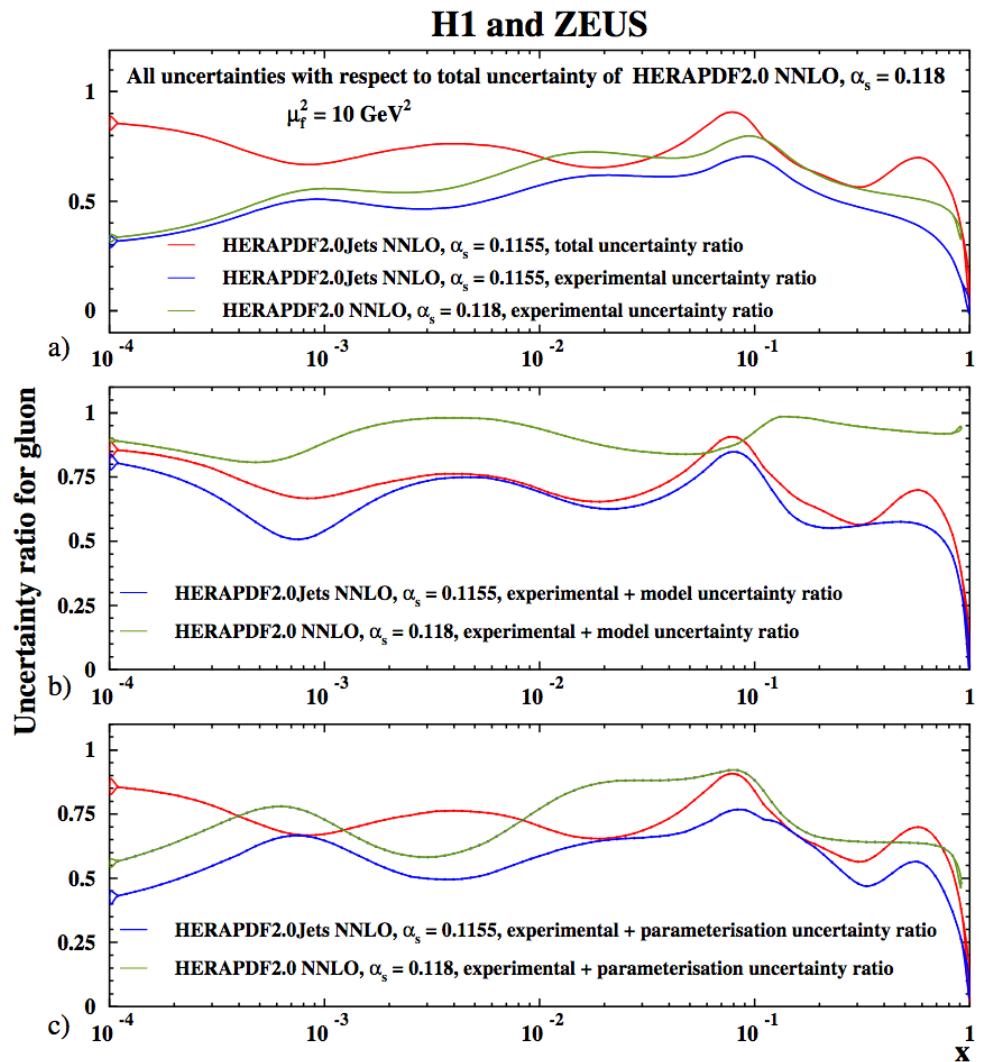
H1 and ZEUS

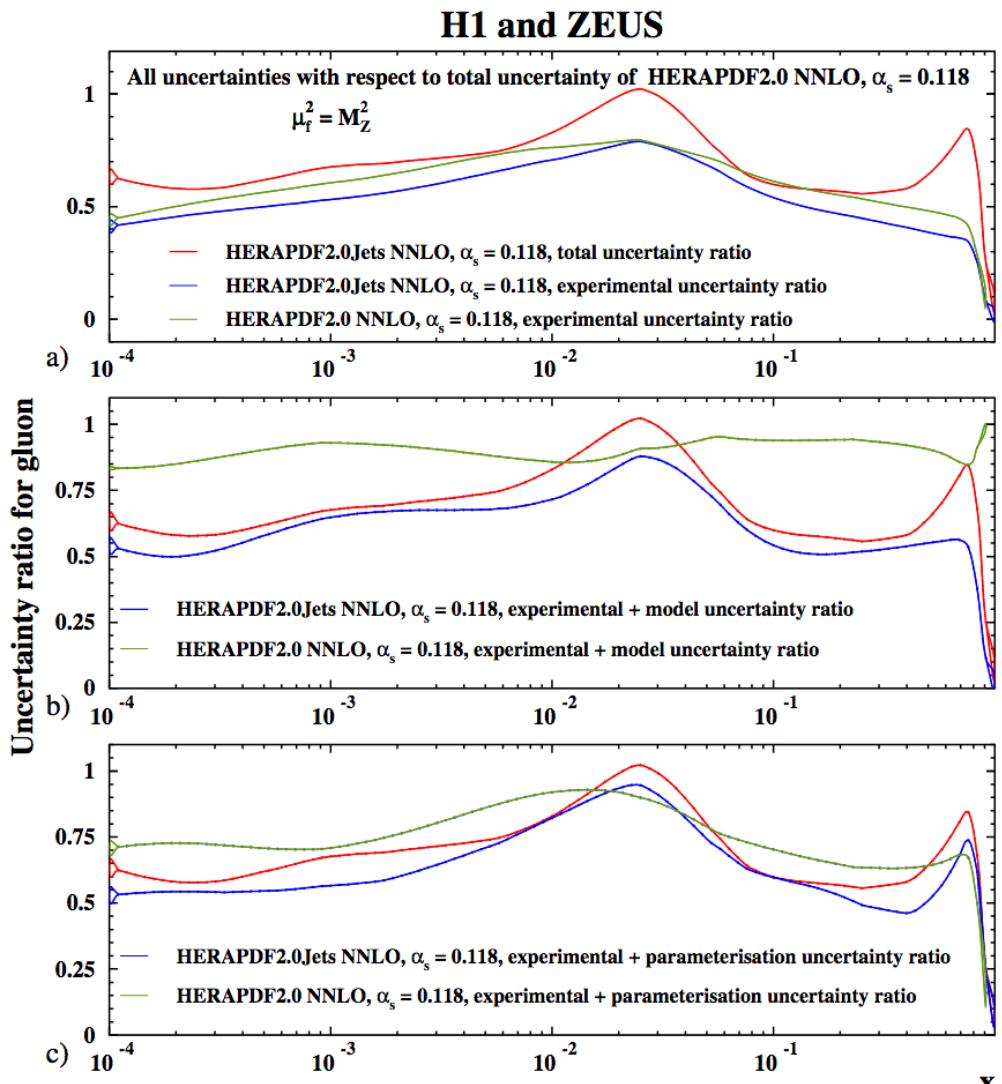
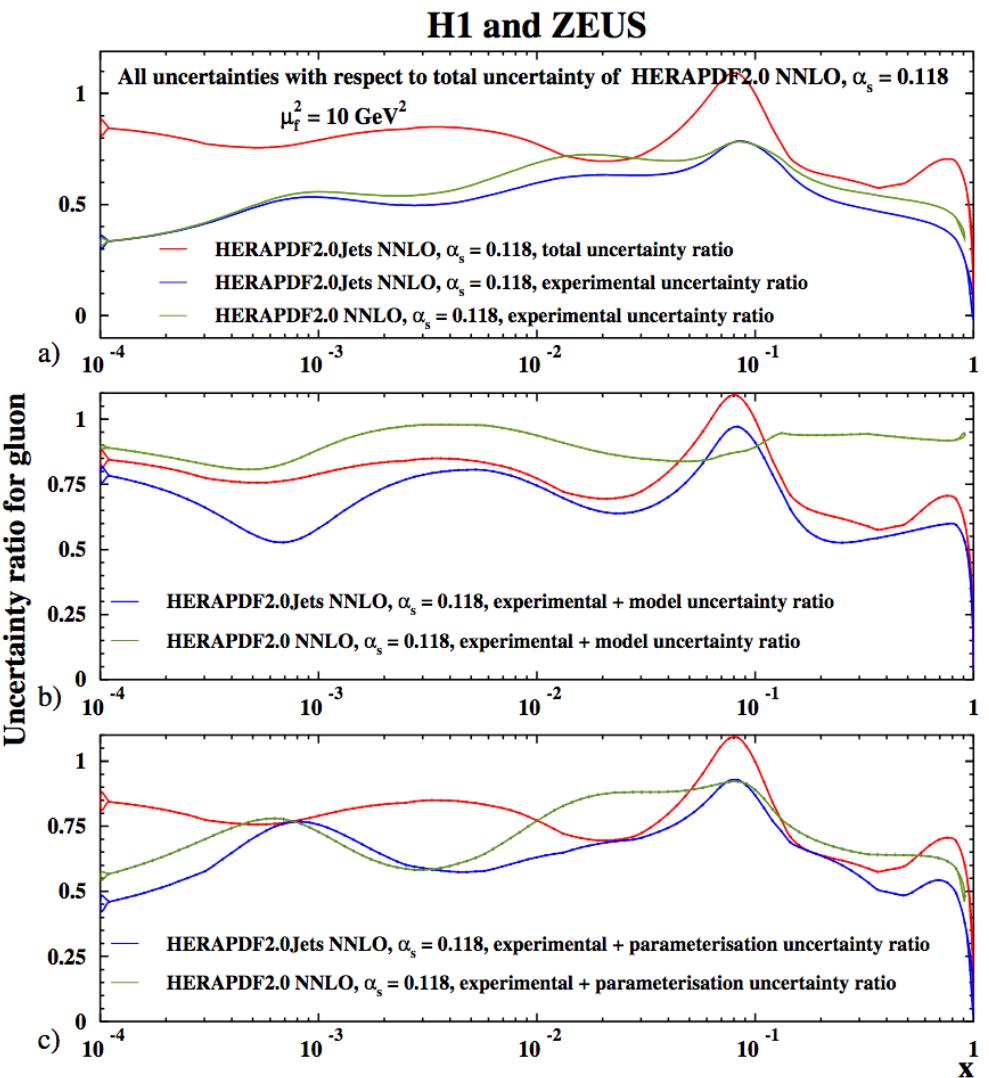


Uncertainties

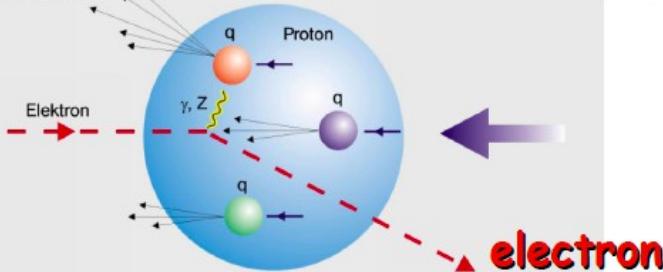
H1 and ZEUS







HERA combined inclusive DIS



HERA combined DIS data are
core of every modern PDF
extraction

- 2927 data points combined to 1307
- impressive precision

HERAPDF approach uses
ONLY HERA data in
global QCD fit

