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THE ROYAL SOCIETY

Collider Events on a Quantum Computer

Simon Williams

Resummation, Evolution, Factorization
2022

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- Quantum Computing - The Power of the Qubit
- Why are we interested in High Energy Physics?
- The Parton Shower
 - Discretising QCD
- Collider Events on a Quantum Computer

G. Gustafson, S. Prestel, M. Spannowsky and S. Williams, Collider Events on a Quantum Computer, [arXiv:2207.10694](https://arxiv.org/abs/2207.10694)



LUND
UNIVERSITY



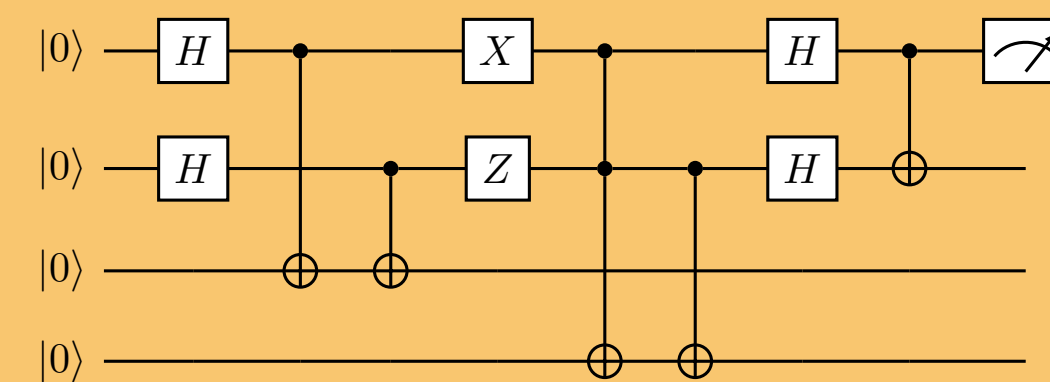
Quantum Computing - The Power of the Qubit!



“Nature is quantum [...] so if you want to simulate it, you need a quantum computer”
- Richard Feynman (1982)

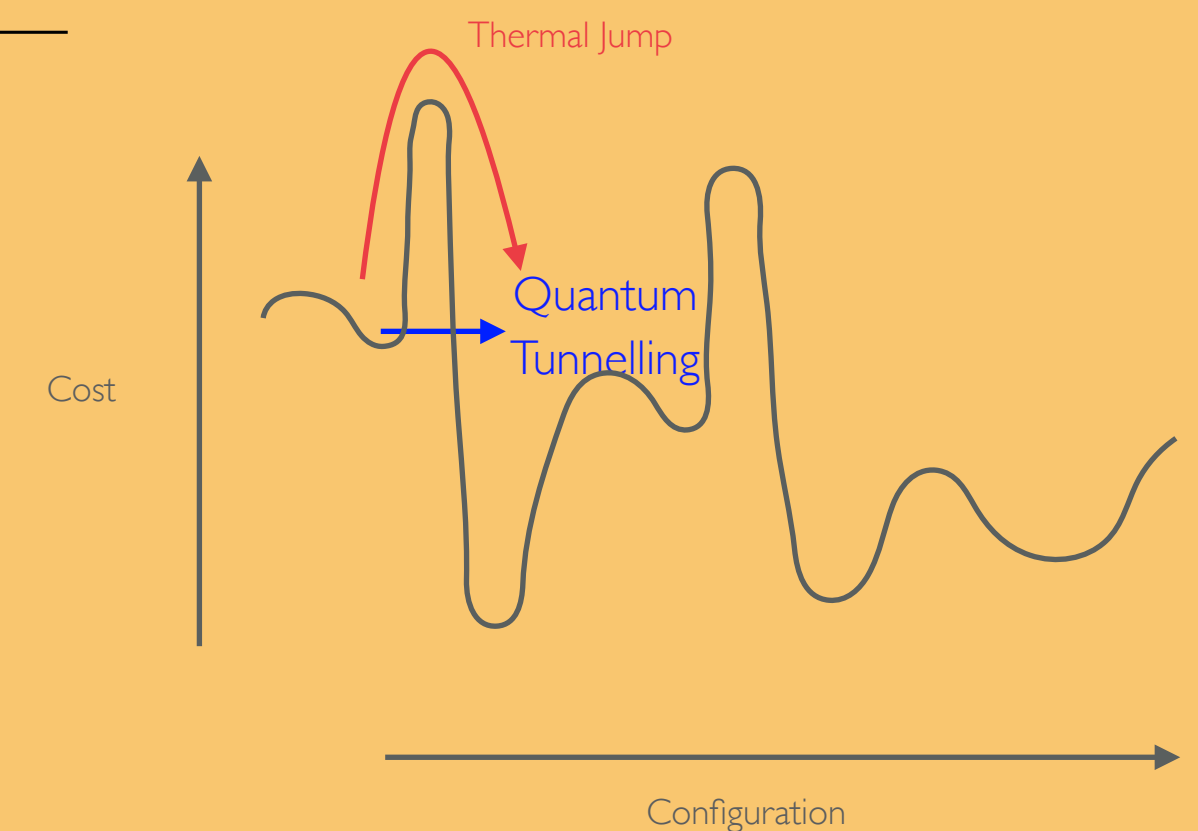
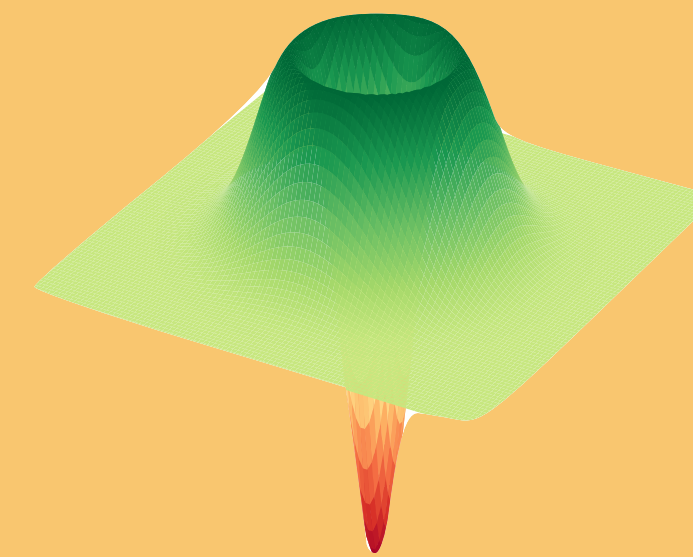
Quantum Computing has had a lot of successes since - most recently with Shor and Deutsch winning the Breakthrough Prize and the 2022 Nobel Prize going to Quantum Information

Types of Quantum Device:



Gate Quantum Computing

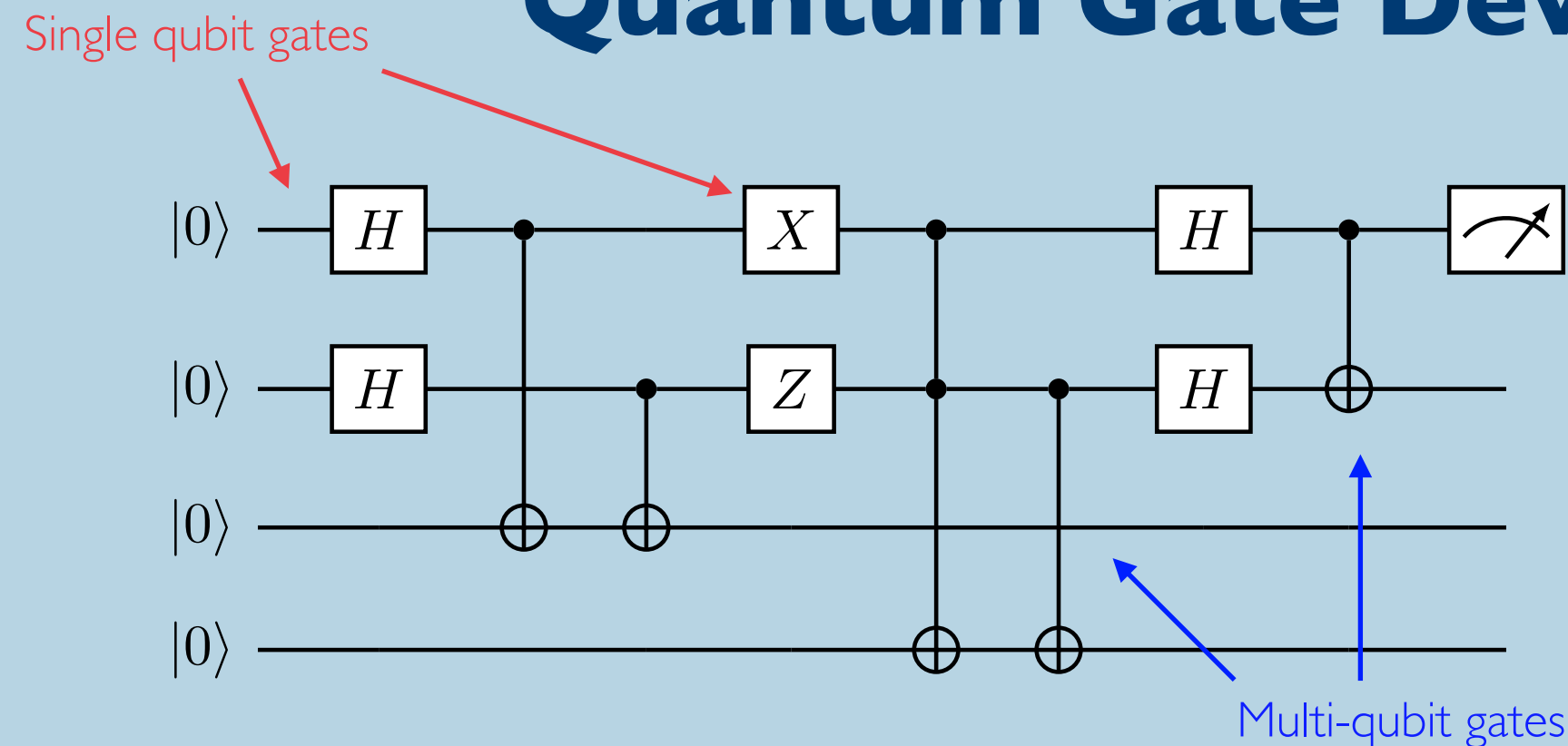
Quantum Annealing



Photonic Devices

Types of Quantum Computing Devices

Quantum Gate Devices



Qubit model:

Qubit is the quantum analogue of the classical bit, not restricted only to $|0\rangle$ and $|1\rangle$

$$|\psi\rangle = \cos \frac{\theta}{2} |0\rangle + e^{i\phi} \sin \frac{\theta}{2} |1\rangle$$

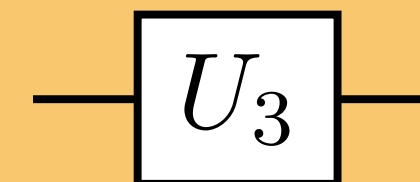
Advantages:

- Highly controllable qubits
- Universal computation

Disadvantages:

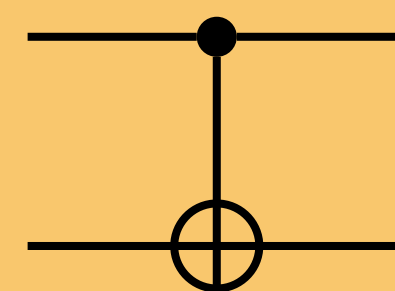
- Small number of qubits, not very fault tolerant

Single qubit gates:



$$U_3 |0\rangle \rightarrow \cos \frac{\theta}{2} |0\rangle + e^{i\phi} \sin \frac{\theta}{2} |1\rangle$$

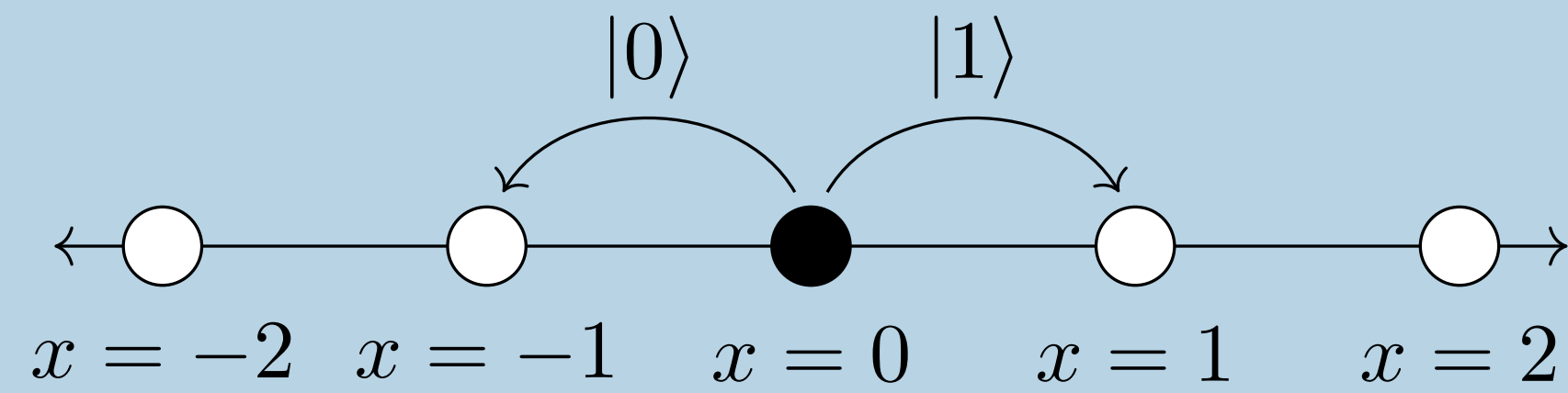
Multi-qubit gates:



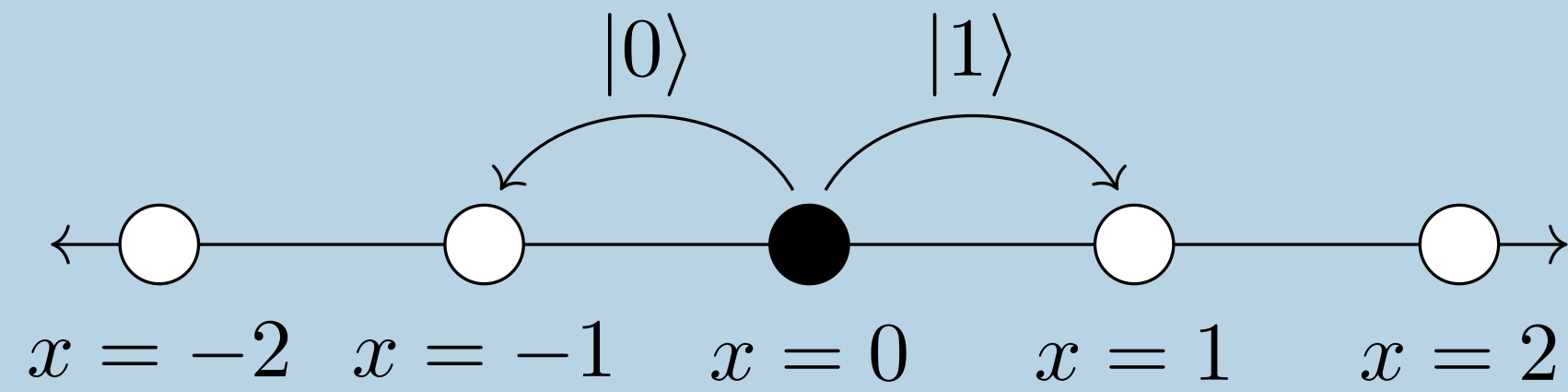
$$\begin{aligned} \text{CNOT } |00\rangle &\rightarrow |00\rangle, \text{CNOT } |10\rangle \rightarrow |11\rangle, \\ \text{CNOT } |01\rangle &\rightarrow |01\rangle, \text{CNOT } |11\rangle \rightarrow |10\rangle \end{aligned}$$

Quantum Computing - The Quantum Walk

Quantum Computing - The Quantum Walk

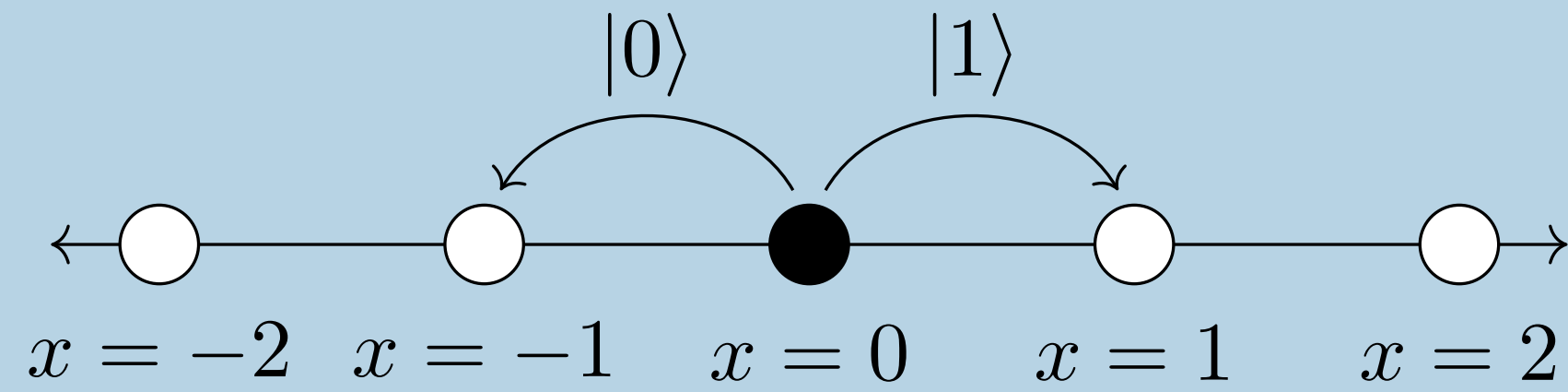


Quantum Computing - The Quantum Walk



$$\left. \begin{array}{l} \mathcal{H}_P = \{ |i\rangle : i \in \mathbb{Z} \} \\ \mathcal{H}_C = \{ |0\rangle, |1\rangle \} \end{array} \right\} \mathcal{H} = \mathcal{H}_C \otimes \mathcal{H}_P$$

Quantum Computing - The Quantum Walk

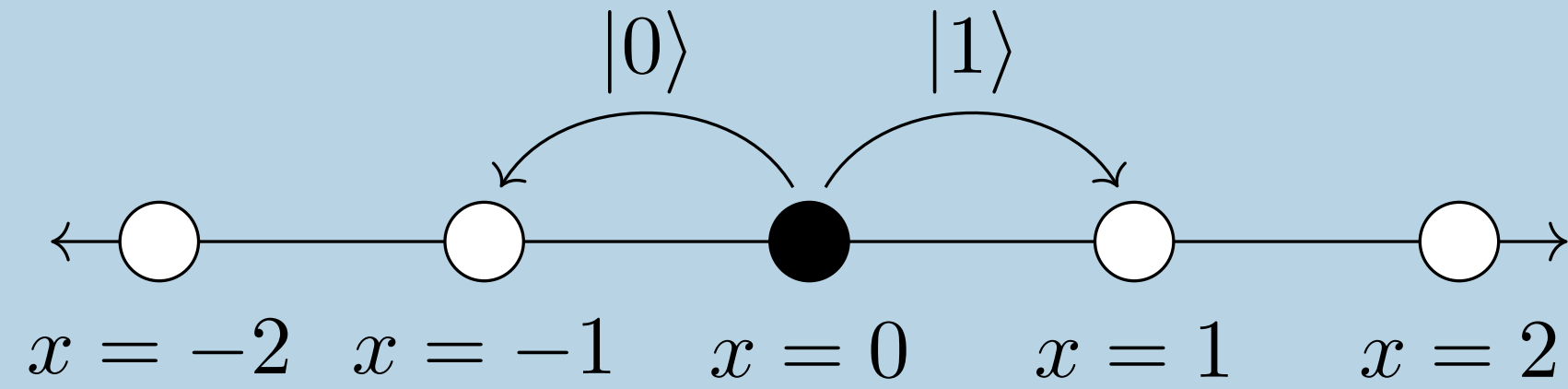


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Unitary
Transformation:

$$U = S \cdot (C \otimes I)$$

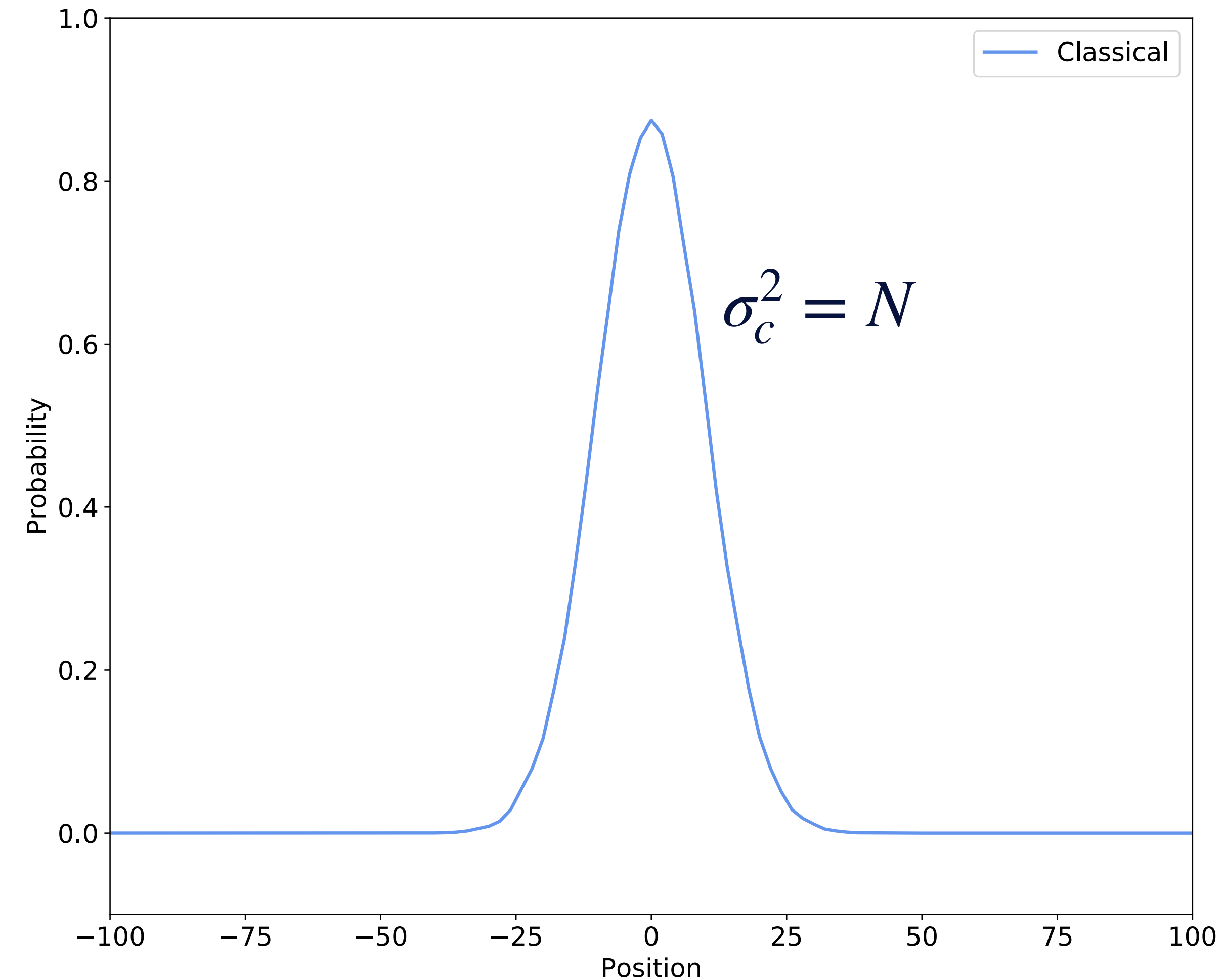
Quantum Computing - The Quantum Walk



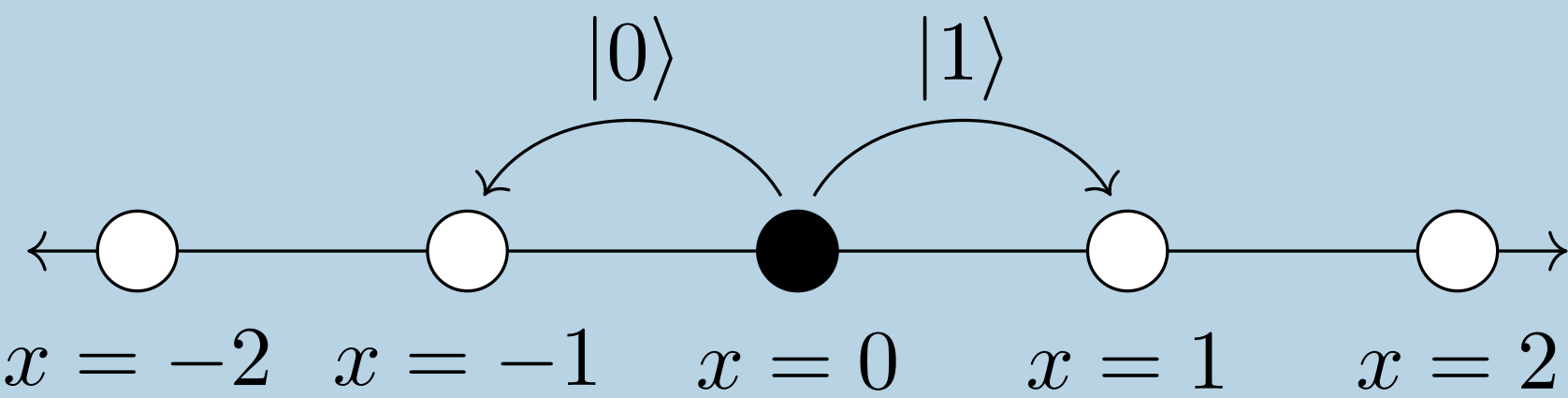
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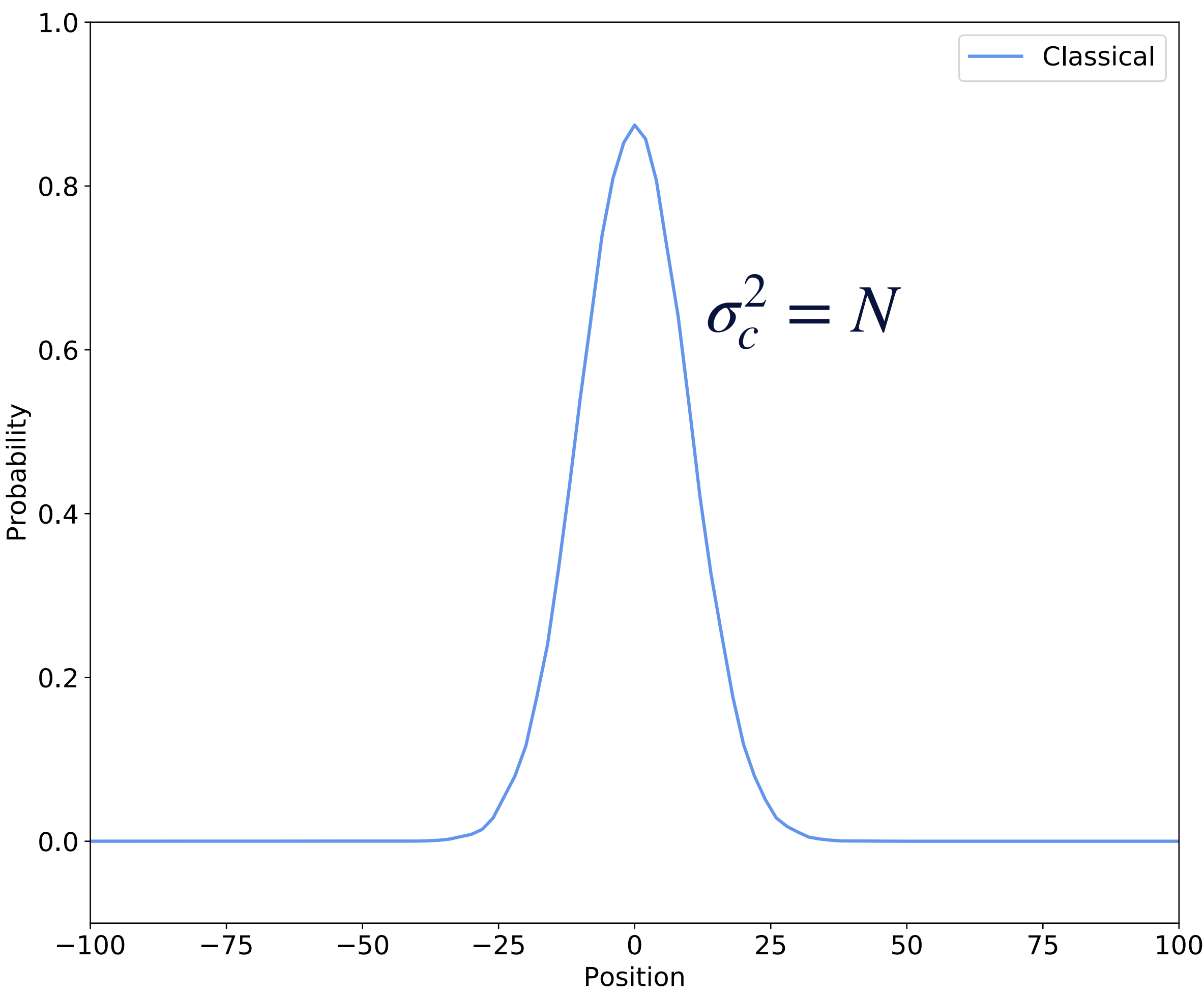
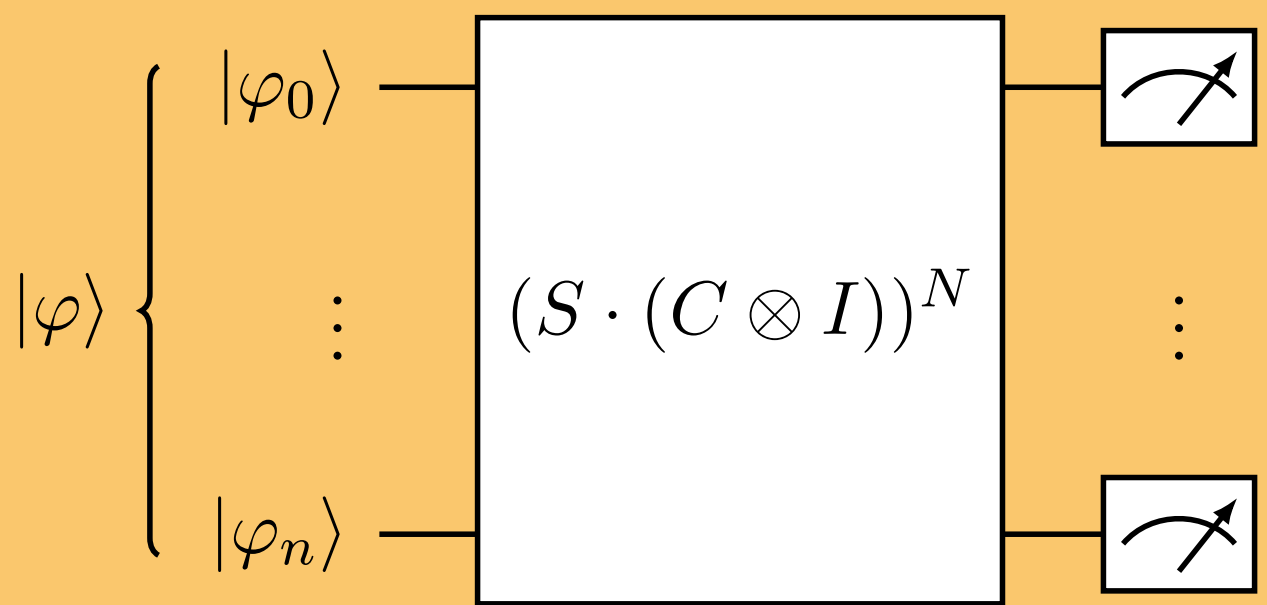
Quantum Computing - The Quantum Walk



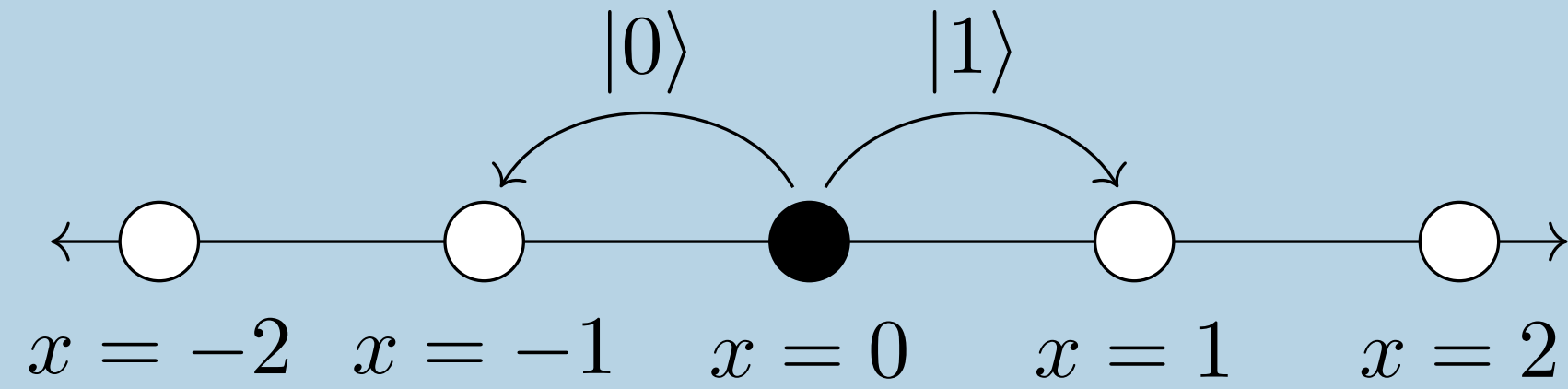
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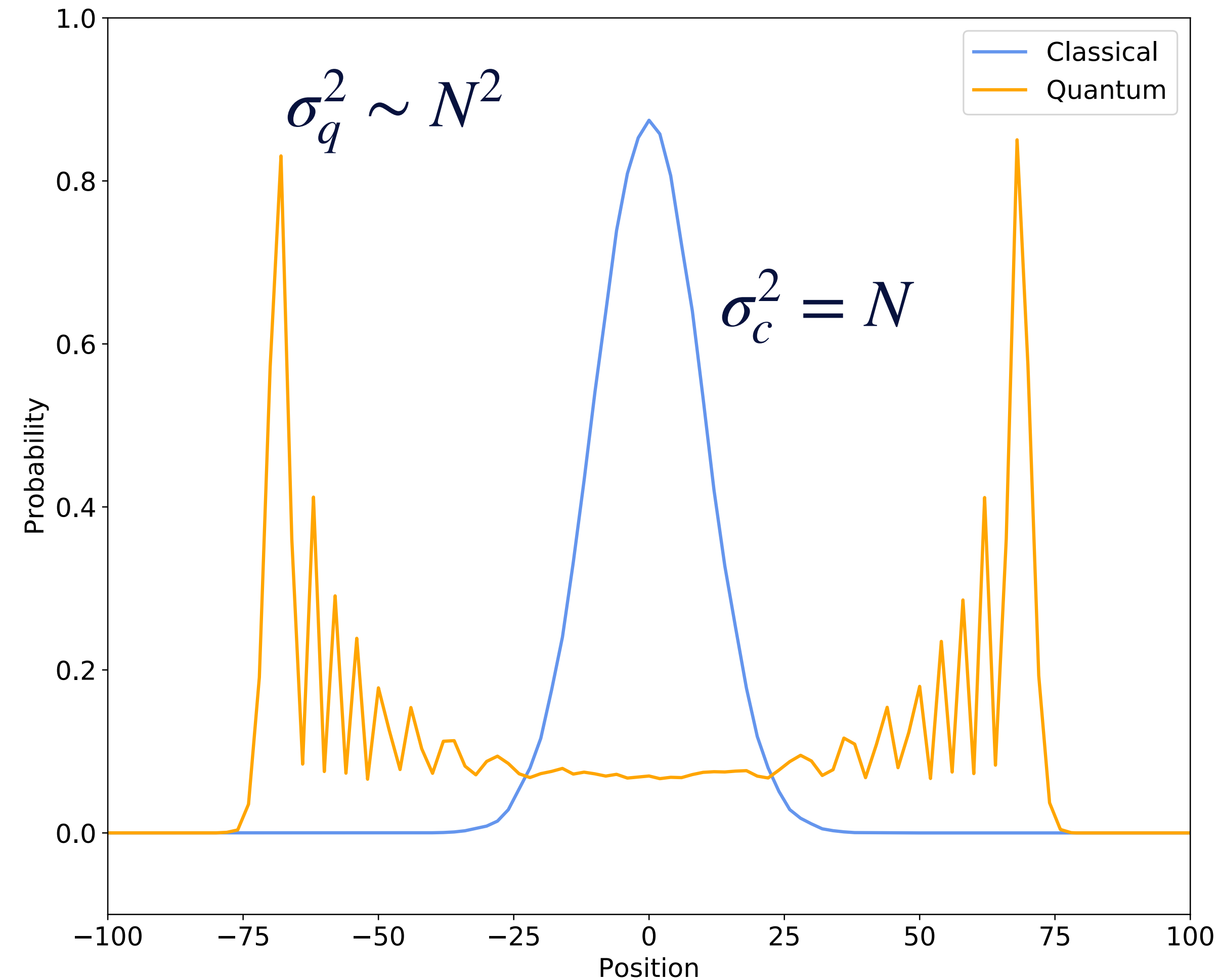
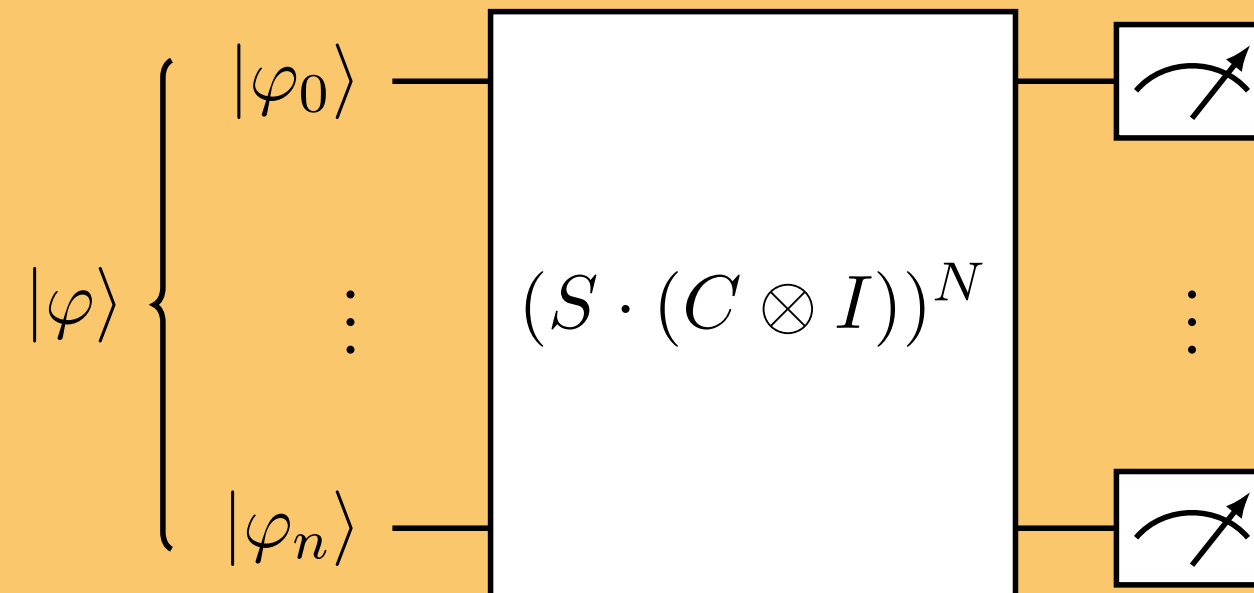
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Unitary Transformation:

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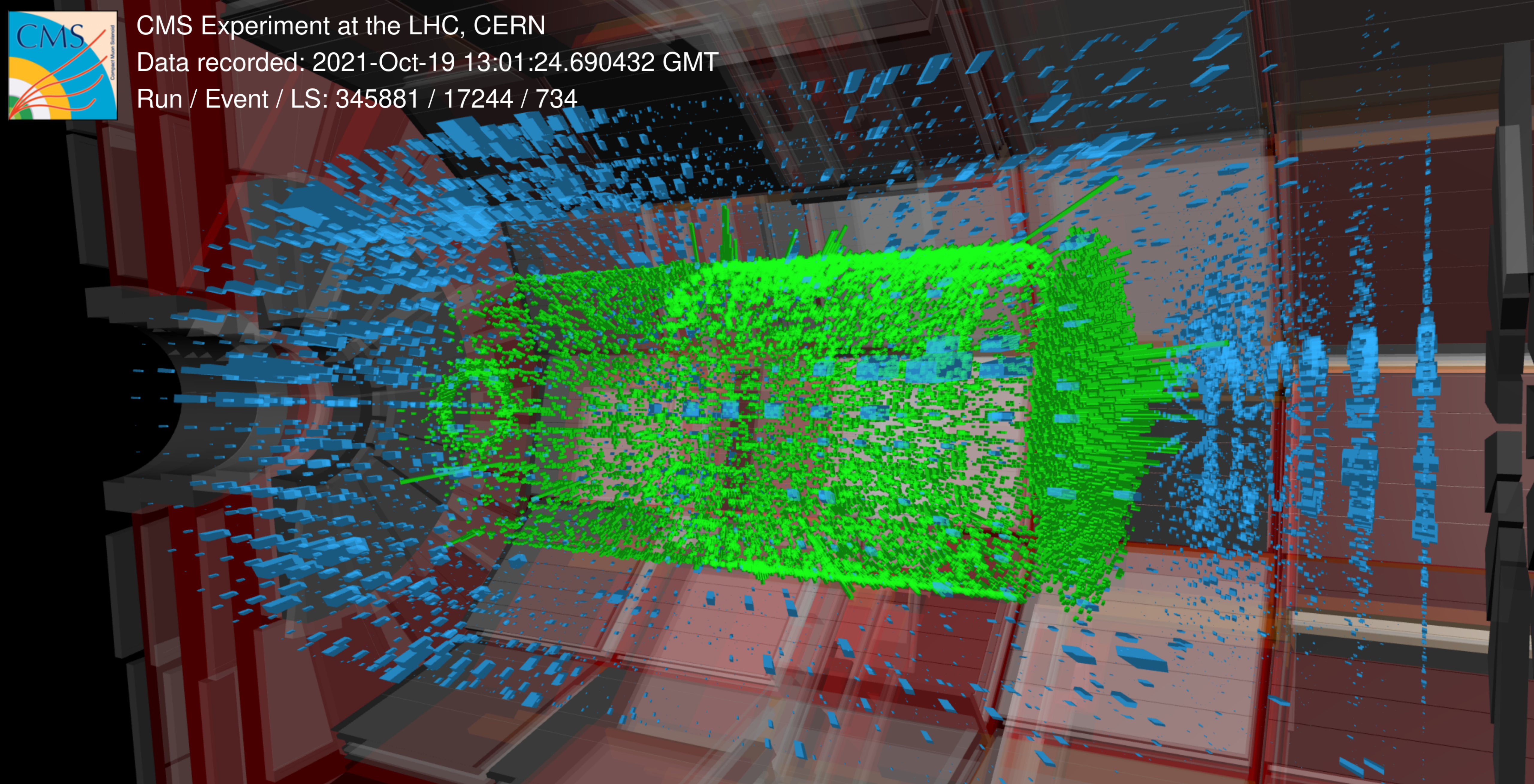
The Power of the Qubit! - Why are we interested in HEP?



CMS Experiment at the LHC, CERN

Data recorded: 2021-Oct-19 13:01:24.690432 GMT

Run / Event / LS: 345881 / 17244 / 734

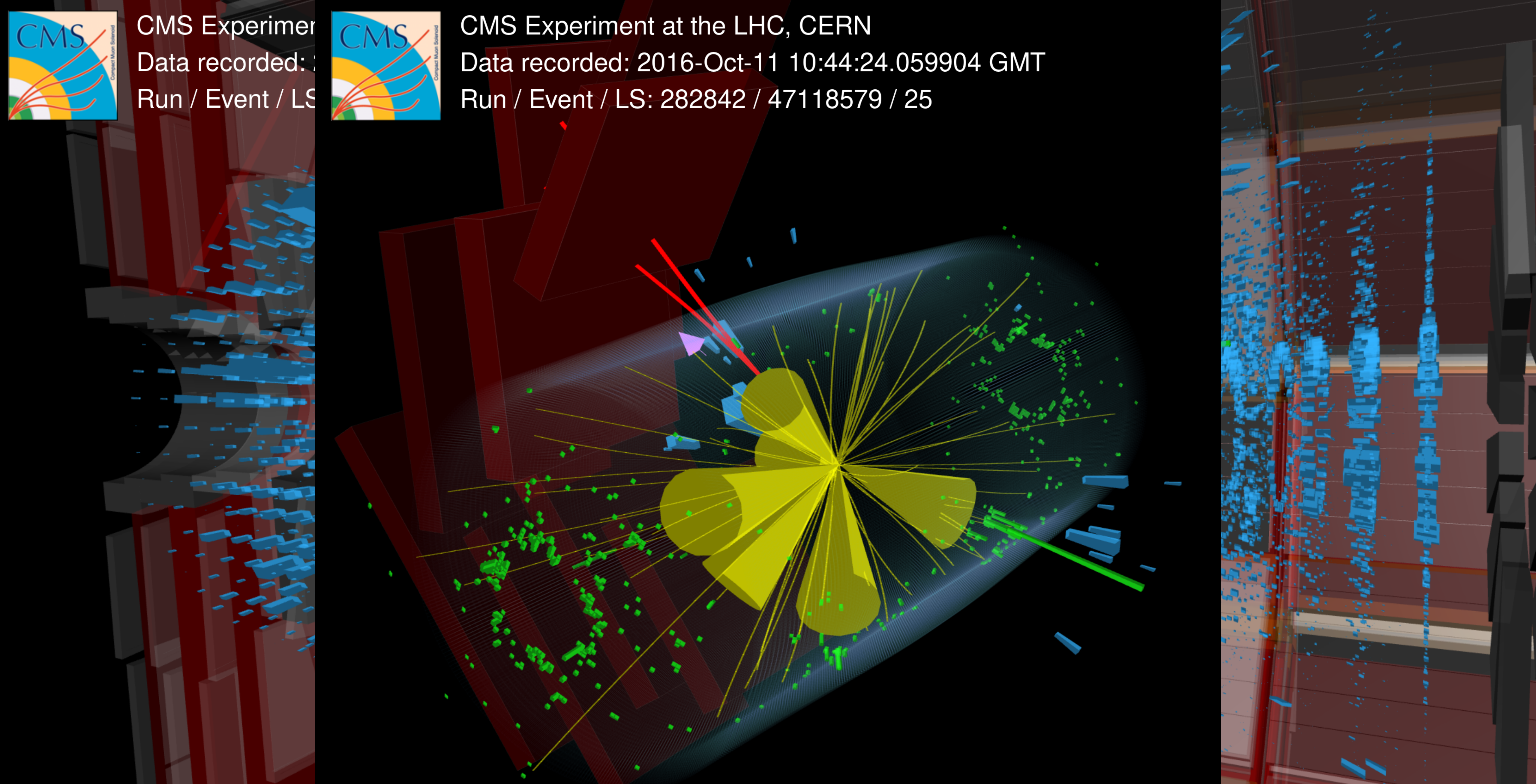




CMS Experiment
Data recorded:
Run / Event / LS

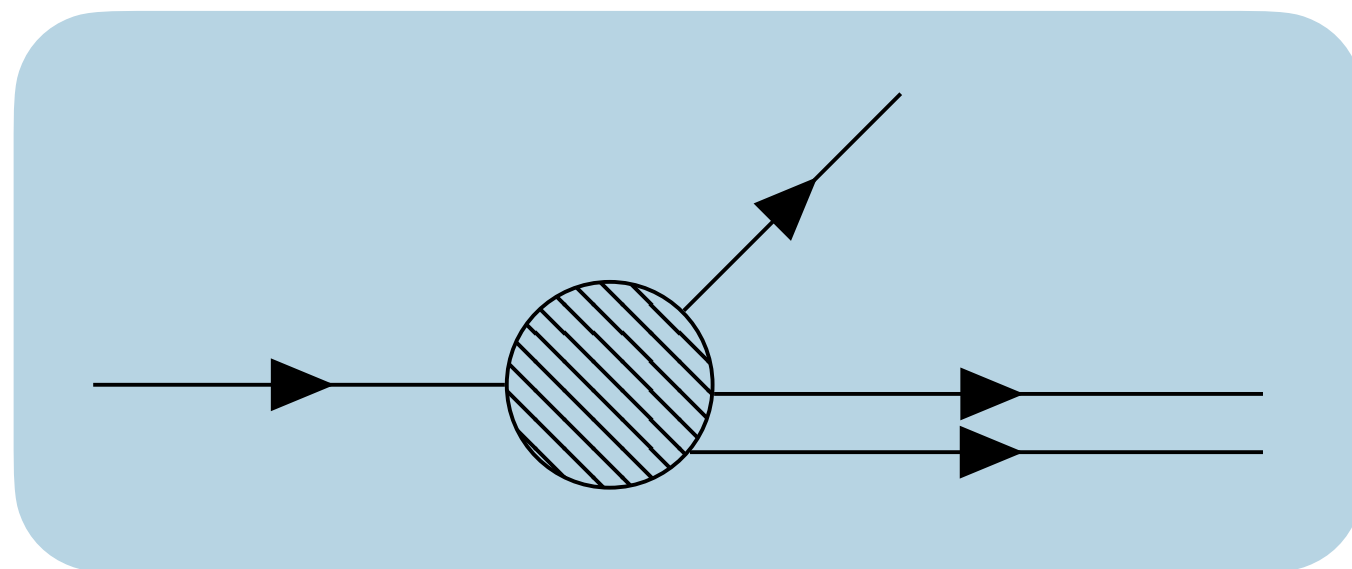
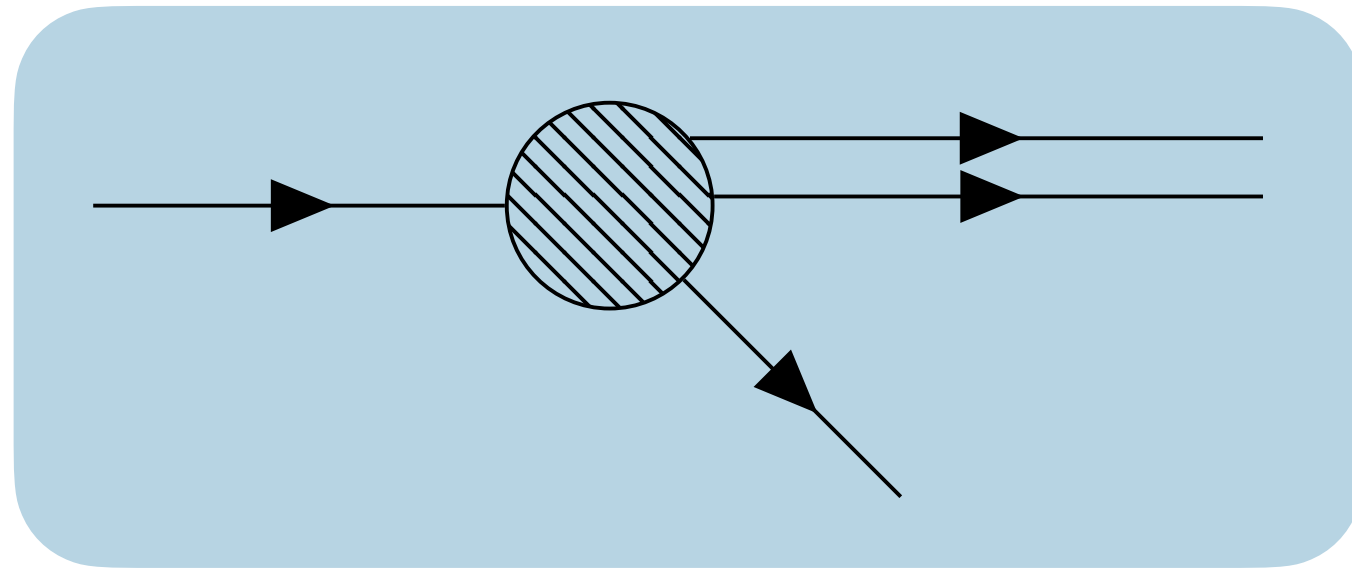


CMS Experiment at the LHC, CERN
Data recorded: 2016-Oct-11 10:44:24.059904 GMT
Run / Event / LS: 282842 / 47118579 / 25



The Power of the Qubit! - Why are we interested in HEP?

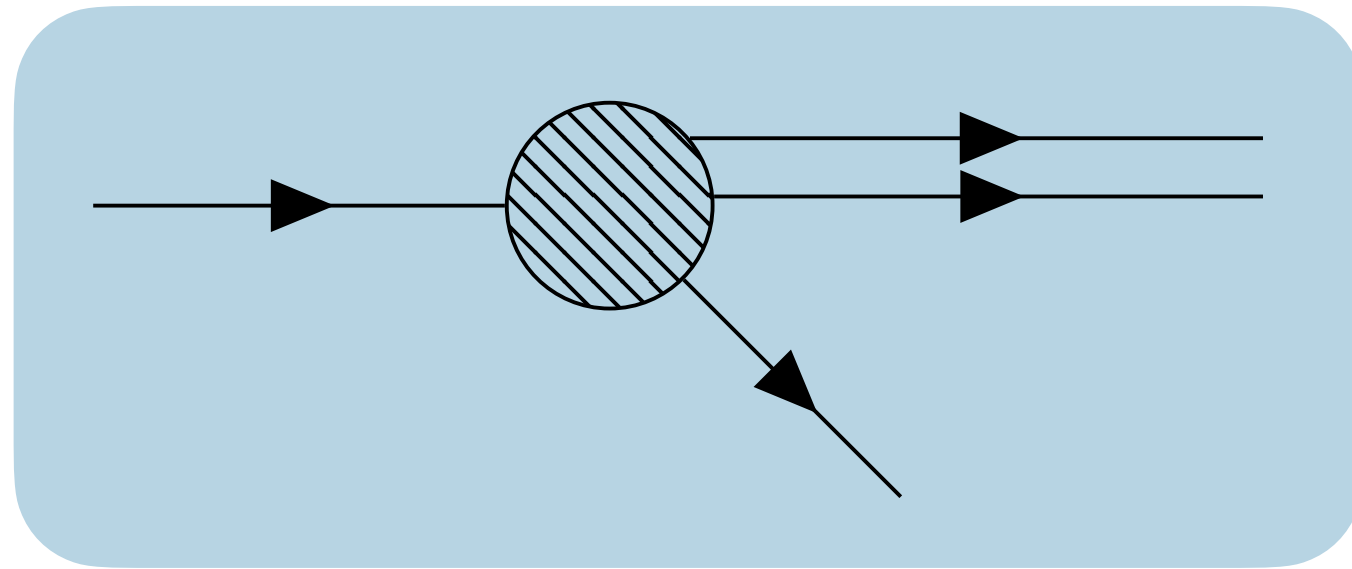
Parton Density Functions



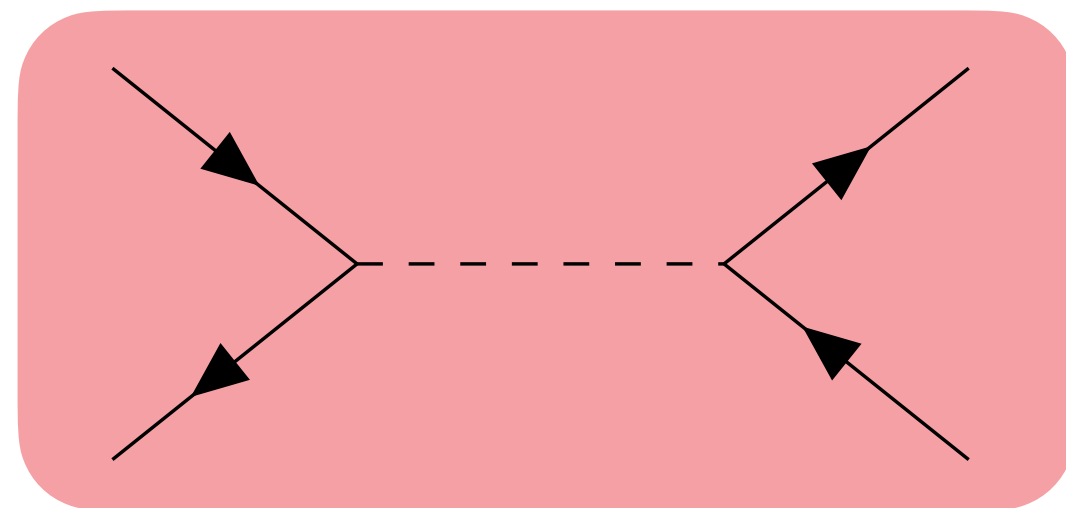
[Phys. Rev. D 103, 034027](#)

The Power of the Qubit! - Why are we interested in HEP?

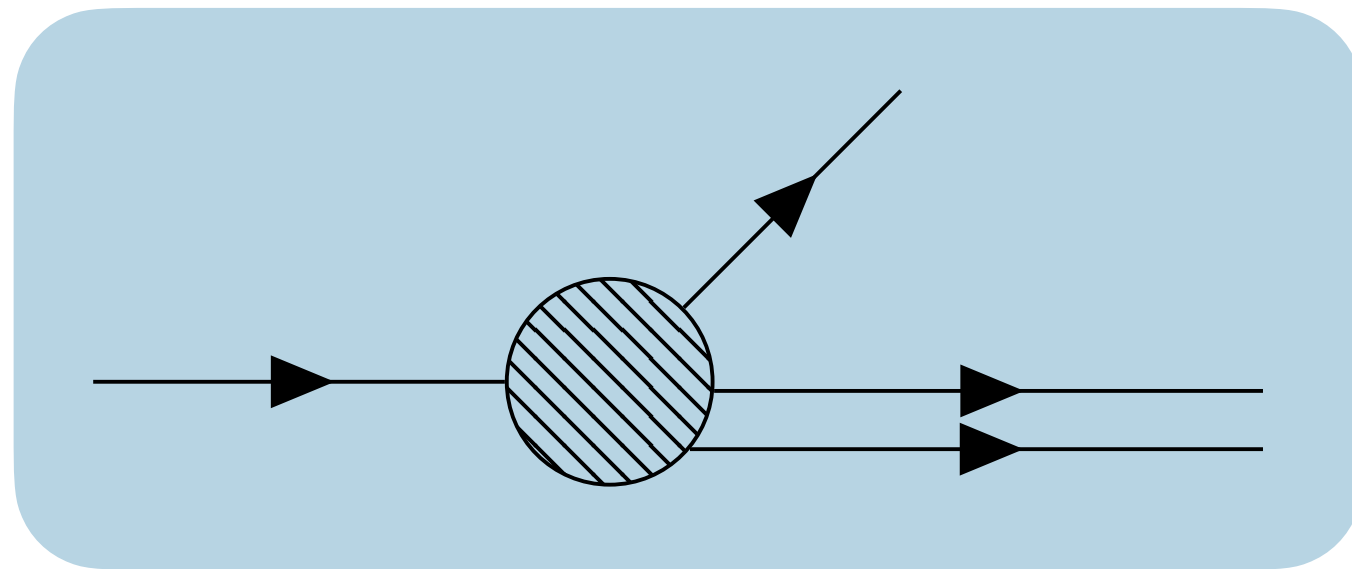
Parton Density Functions



Hard Process



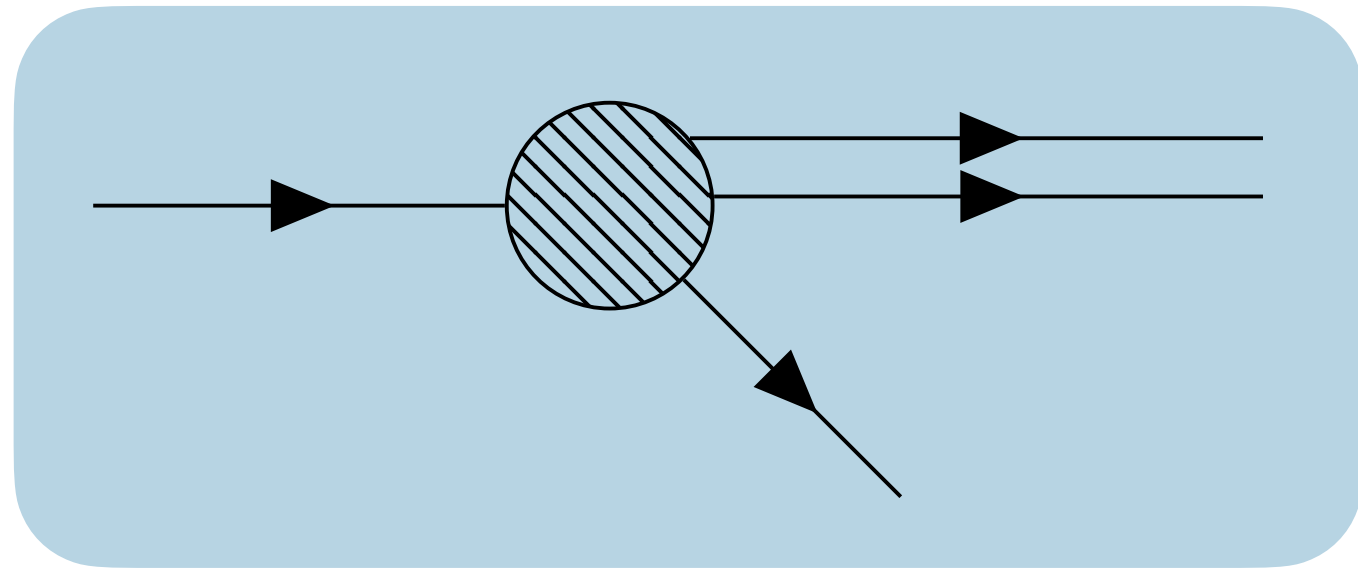
[Phys. Rev. D 103, 076020](#)



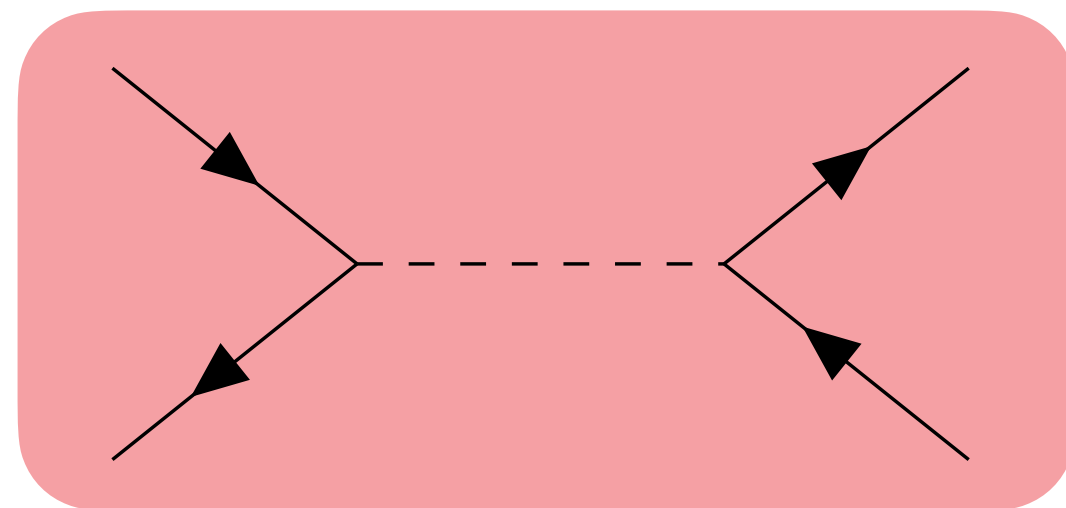
[Phys. Rev. D 103, 034027](#)

The Power of the Qubit! - Why are we interested in HEP?

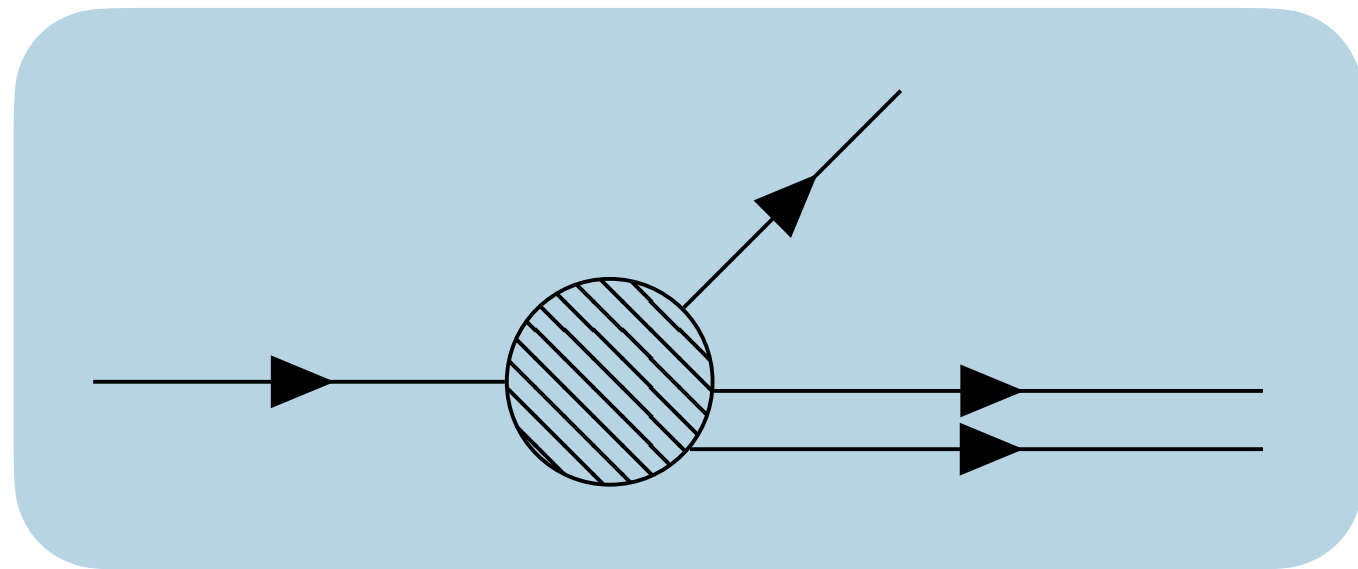
Parton Density Functions



Hard Process

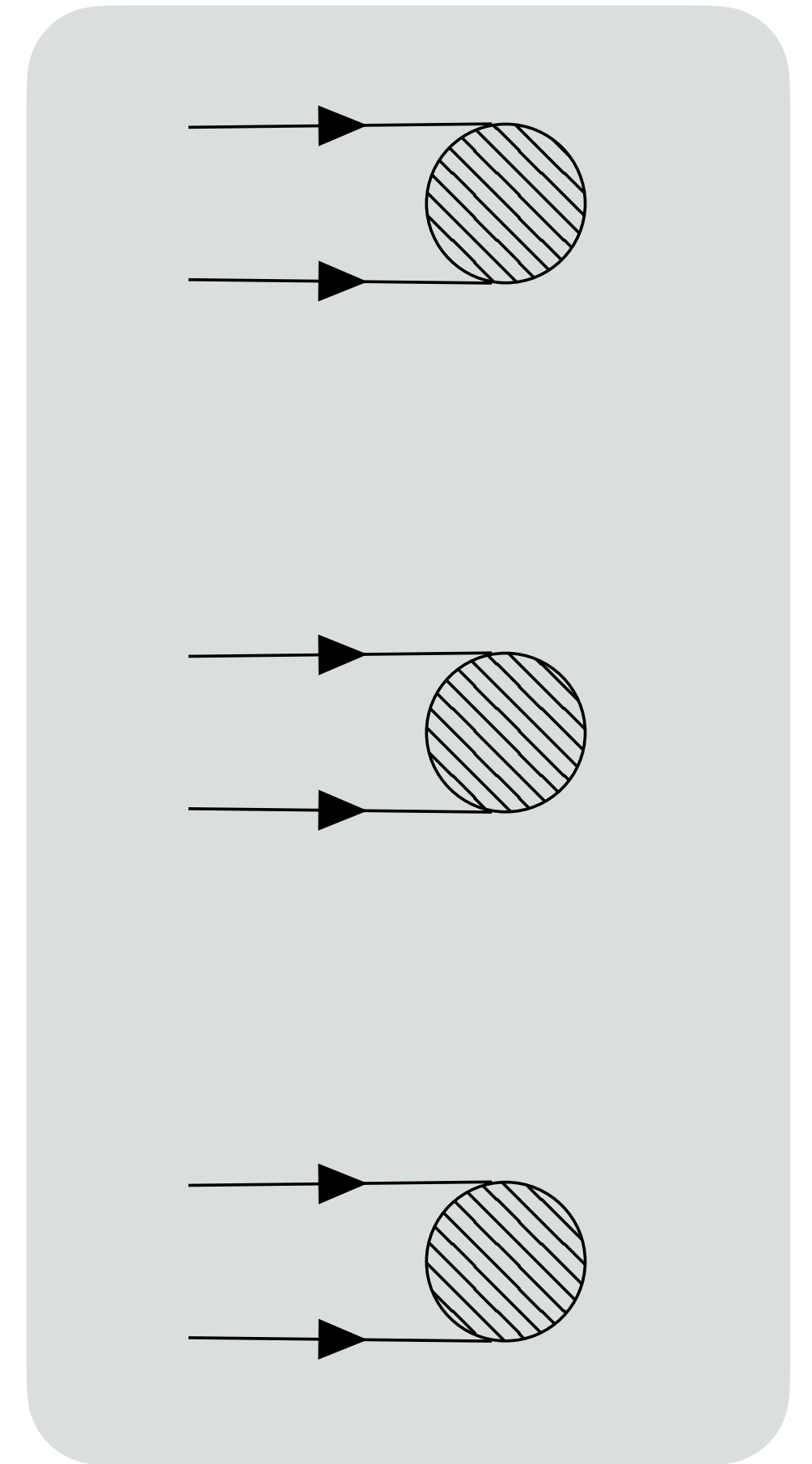


[Phys. Rev. D 103, 076020](#)



[Phys. Rev. D 103, 034027](#)

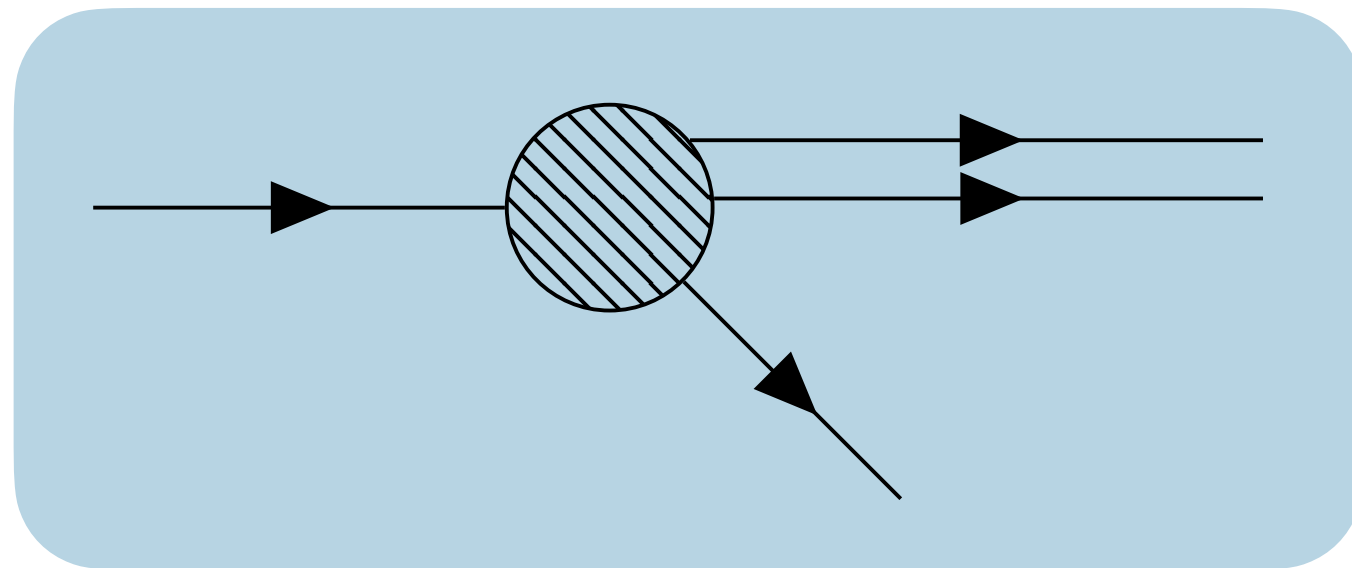
Hadronisation



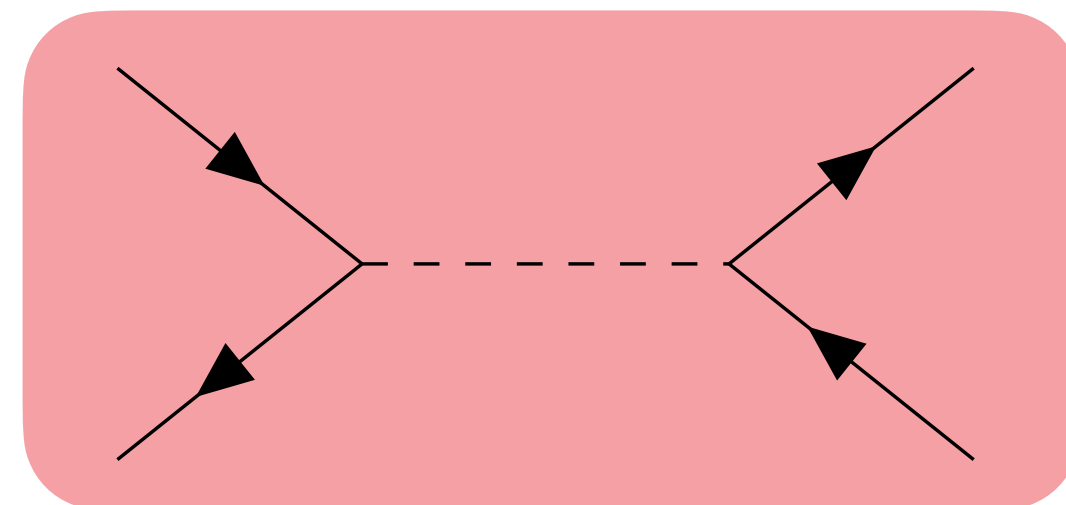
[arXiv:2207.10694](#)

The Power of the Qubit! - Why are we interested in HEP?

Parton Density Functions



Hard Process



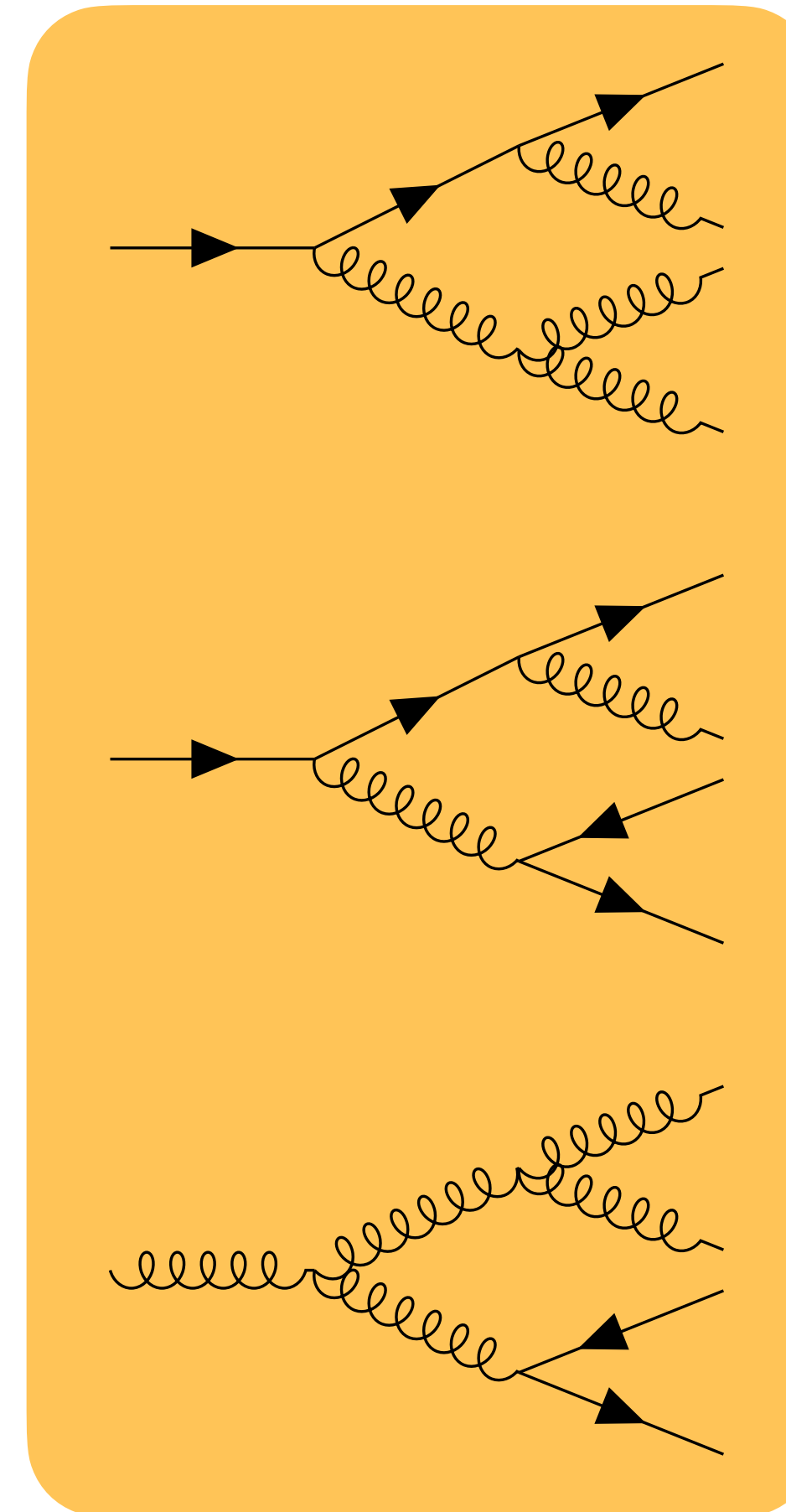
[Phys. Rev. D 103, 076020](#)

[Phys. Rev. D 106, 056002](#)

[Phys. Rev. D 103, 034027](#)

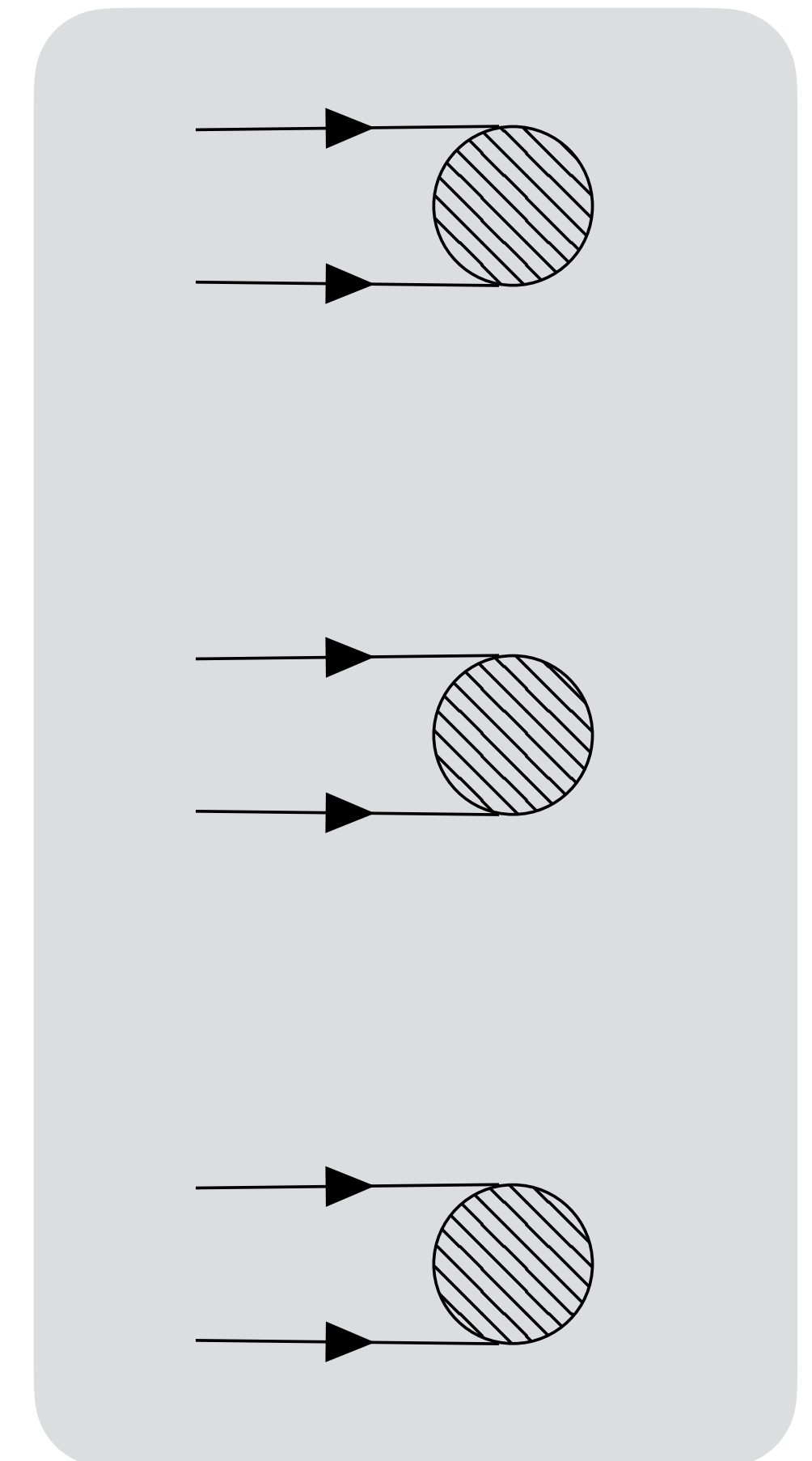
[Phys. Rev. Lett. 126, 062001](#)

Parton Shower



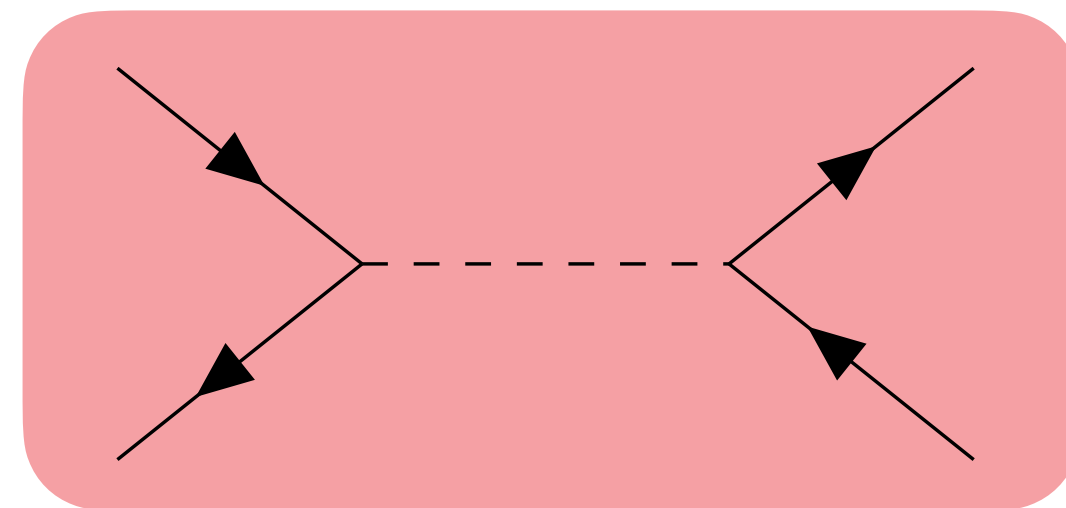
[arXiv:2207.10694](#)

Hadronisation



The Power of the Qubit! - Why are we interested in HEP?

Hard Process

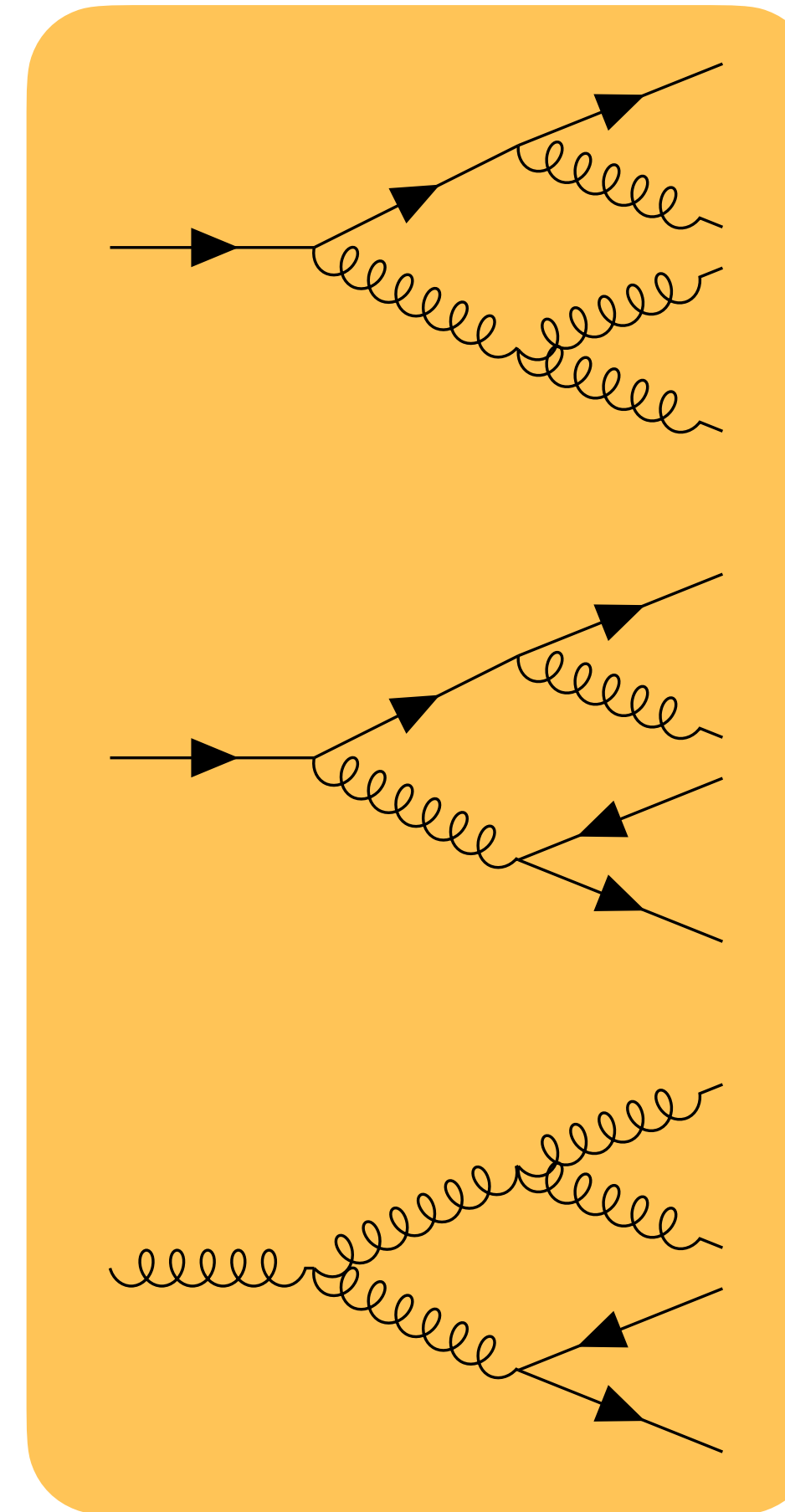


[Phys. Rev. D 103, 076020](#)

[Phys. Rev. D 106, 056002](#)

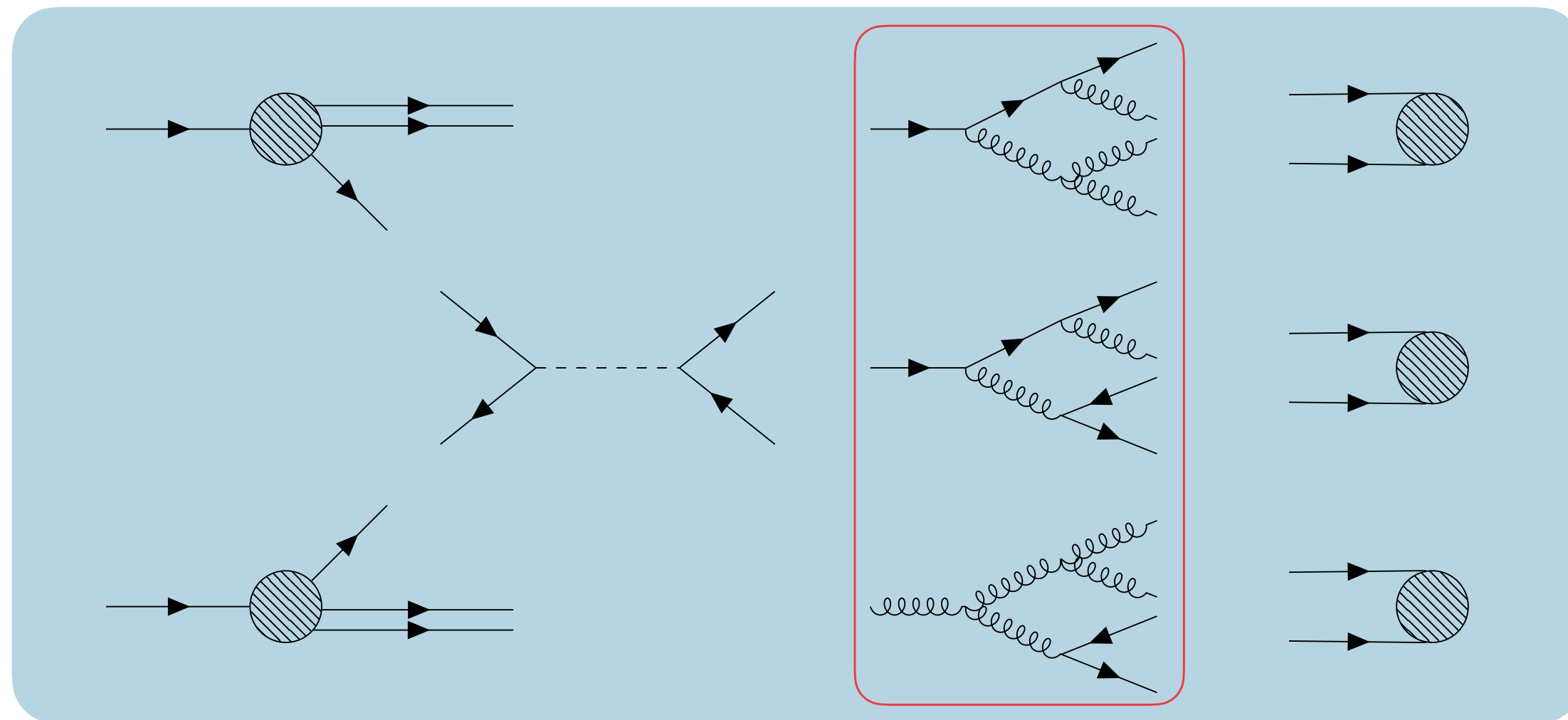
[Phys. Rev. Lett. 126, 062001](#)

Parton Shower

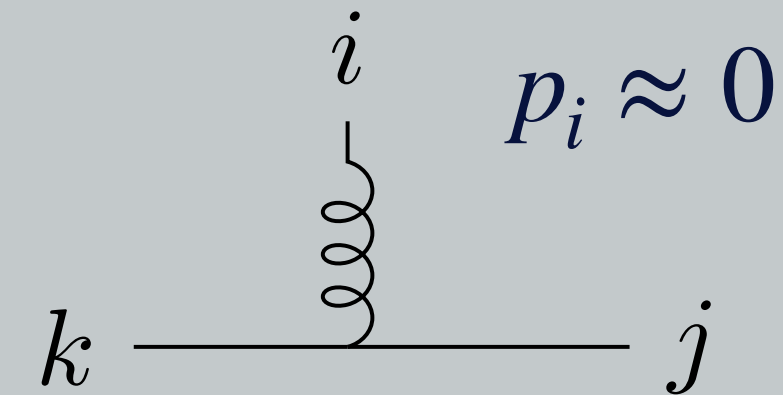


[arXiv:2207.10694](#)

The Parton Shower



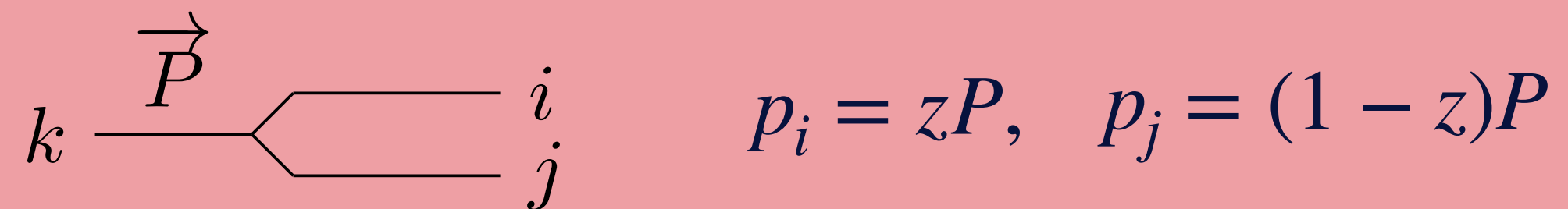
Soft mode:



Interference effects only allow for partial factorisation

Leading contributions to the decay rate in the collinear limit are included in the soft limit

Collinear mode:



Successive decay steps factorise into independent quasi-classical steps

In this limit, the decay from high energy to low energy proceeds as a **colour-dipole cascade**.

This interpretation allows for straightforward interference patterns and momentum conservation

The Parton Shower - The Veto Algorithm

The choice of the variables ξ and t is known as the **phase space parameterisation**

Non-Emission Probability

$$\Delta(t_n, t) = \exp \left(- \int_t^{t_n} dt d\xi \frac{d\phi}{2\pi} C \frac{\alpha_s}{2\pi} \frac{2s_{ik}(t, \xi)}{s_{ij}(t, \xi) s_{jk}(t, \xi)} \right)$$

$$\mathcal{F}_n(\Phi_n, t_n, t_c; O) = \Delta(t_n, t_c) O(\Phi_n)$$

Master Equation

$$+ \int_{t_c}^{t_n} dt d\xi \frac{d\phi}{2\pi} C \frac{\alpha_s}{2\pi} \frac{2s_{ik}(t, \xi)}{s_{ij}(t, \xi) s_{jk}(t, \xi)} \Delta(t_n, t) \mathcal{F}_n(\Phi_{n+1}, t, t_c; O)$$

Inclusive Decay Probability

$$d\mathcal{P}(q(p_I)\bar{q}(p_K) \rightarrow q(p_i)g(p_j)\bar{q}(p_k)) \simeq \frac{ds_{ij}}{s_{IK}} \frac{ds_{jk}}{s_{IK}} C \frac{\alpha_s}{2\pi} \frac{2s_{IK}}{s_{ij}s_{jk}}$$

Current interpretations of the veto algorithm treat the phase space variables ξ and t as **continuous**

Collider Events on a Quantum Computer

Gösta Gustafson,^a Stefan Prestel,^a Michael Spannowsky,^b Simon Williams^c

^a*Department of Astronomy and Theoretical Physics, Lund University, S-223 62 Lund, Sweden*

^b*Institute for Particle Physics Phenomenology, Department of Physics, Durham University, Durham DH1 3LE, U.K.*

^c*High Energy Physics Group, Blackett Laboratory, Imperial College, Prince Consort Road, London, SW7 2AZ, United Kingdom*

ABSTRACT: High-quality simulated data is crucial for particle physics discoveries. Therefore, Parton shower algorithms are a major building block of the data synthesis in event generator programs. However, the core algorithms used to generate parton showers have barely changed since the 1980s. With quantum computers' rapid and continuous development, dedicated algorithms are required to exploit the potential that quantum computers provide to address problems in high-energy physics. This paper presents a novel approach to synthesising parton showers using the Discrete QCD method. The algorithm benefits from an elegant quantum walk implementation which can be embedded into the classical toolchain. We use the `ibm_algiers` device to sample parton shower configurations and generate data that we compare against measurements taken at the ALEPH, DELPHI and OPAL experiments. This is the first time a Noisy Intermediate-Scale Quantum (NISQ) device has been used to simulate realistic high-energy particle collision events.

Discrete QCD - Abstracting the Parton Shower Method

I. Parameterise phase space in terms of gluon transverse momentum and rapidity:

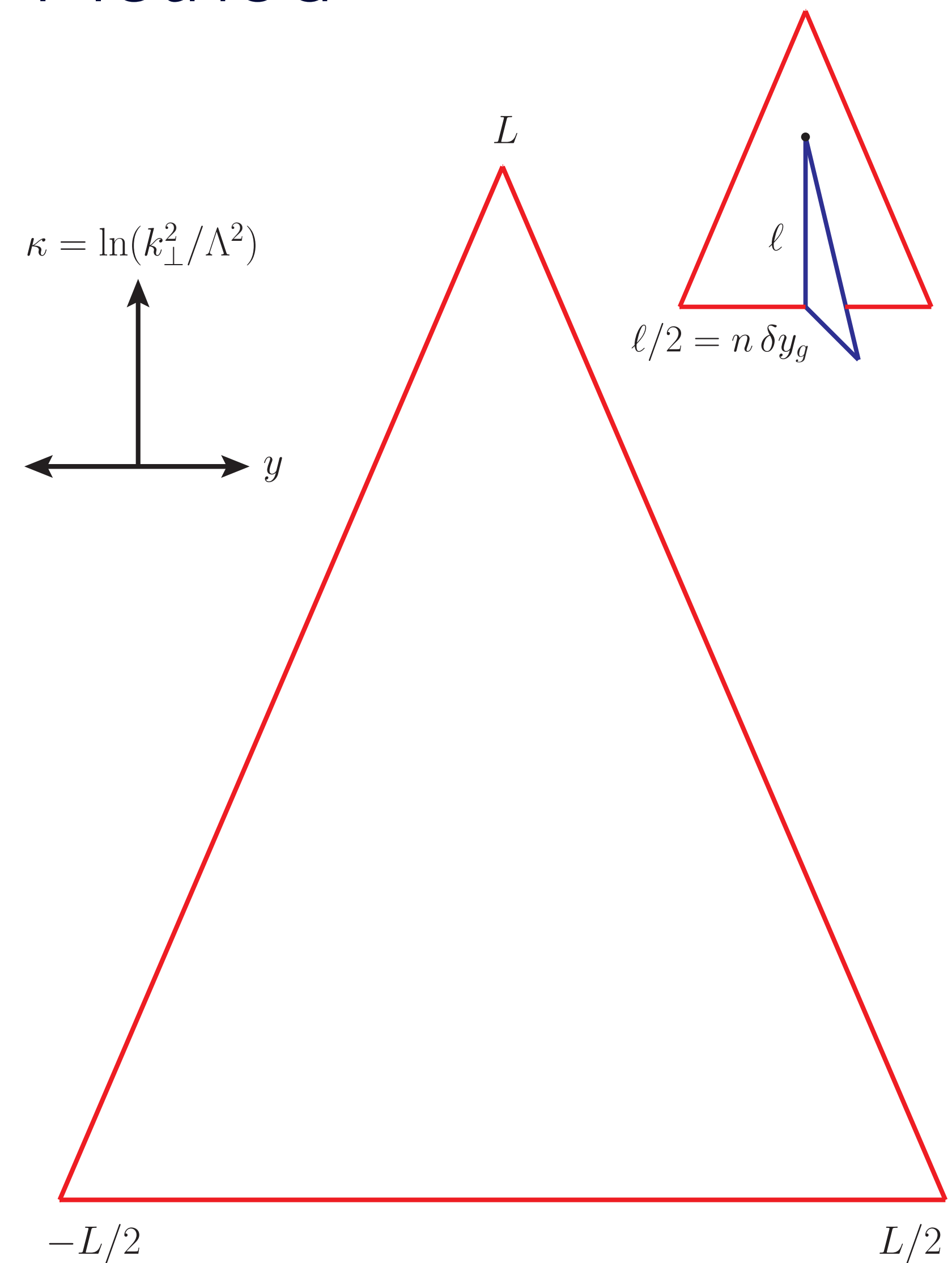
$$k_{\perp}^2 = \frac{s_{ij}s_{jk}}{s_{IK}} \quad \text{and} \quad y = \frac{1}{2} \ln \left(\frac{s_{ij}}{s_{jk}} \right)$$

which leads to the inclusive probability:

$$d\mathcal{P} (q(p_I)\bar{q}(p_K) \rightarrow q(p_i)g(p_j)\bar{q}(p_k)) \simeq \frac{C\alpha_s}{\pi} d\kappa dy$$

where $\kappa = \ln \left(\frac{k_{\perp}^2}{\Lambda^2} \right)$ and Λ is an arbitrary mass scale

Due to the colour charge of emitted gluons, the rapidity span for subsequent dipole decays is increased. This is interpreted as **“folding out”**



Discrete QCD - Abstracting the Parton Shower Method

2. Neglect $g \rightarrow q\bar{q}$ splittings and examine transverse-momentum-dependent running coupling

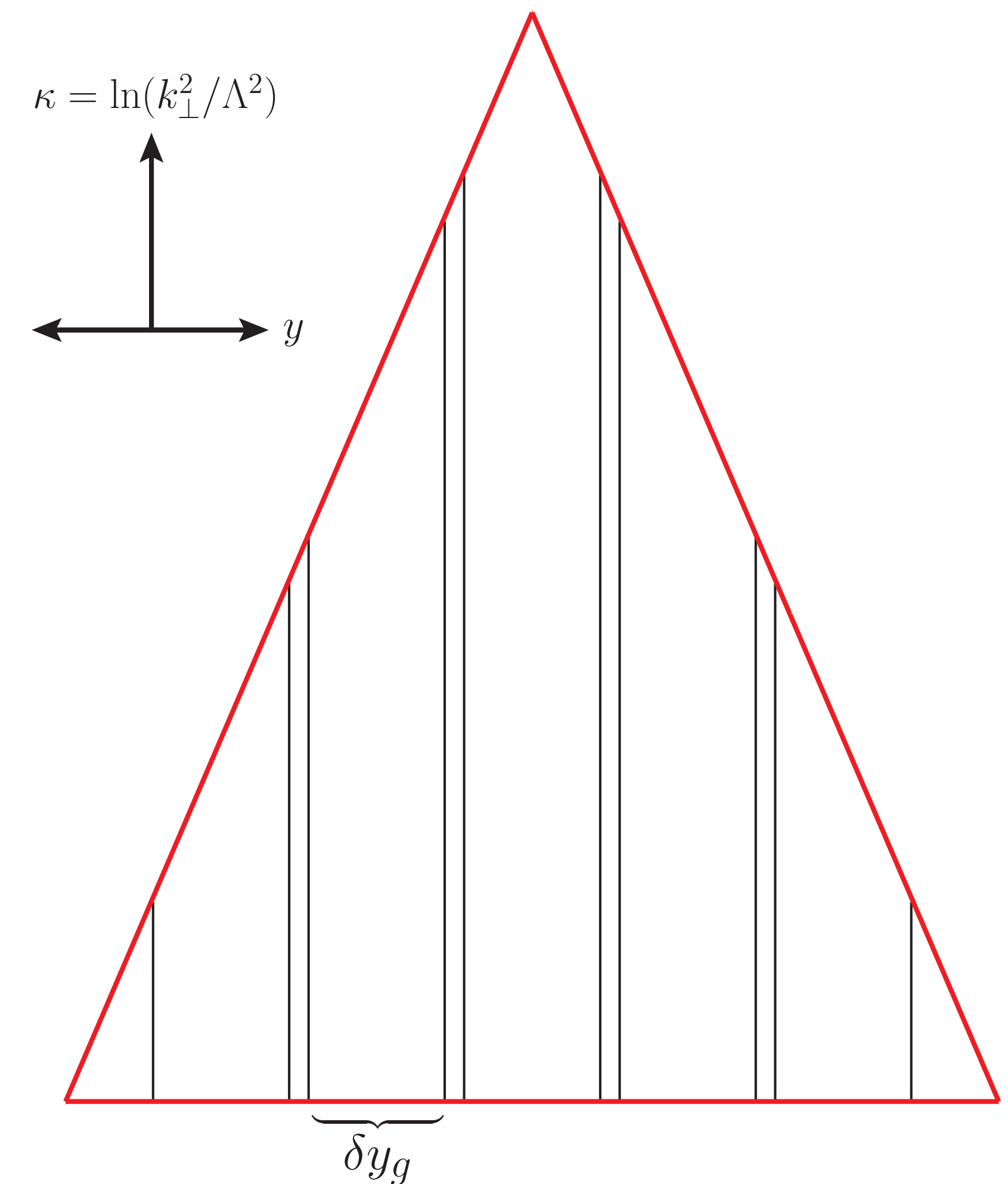
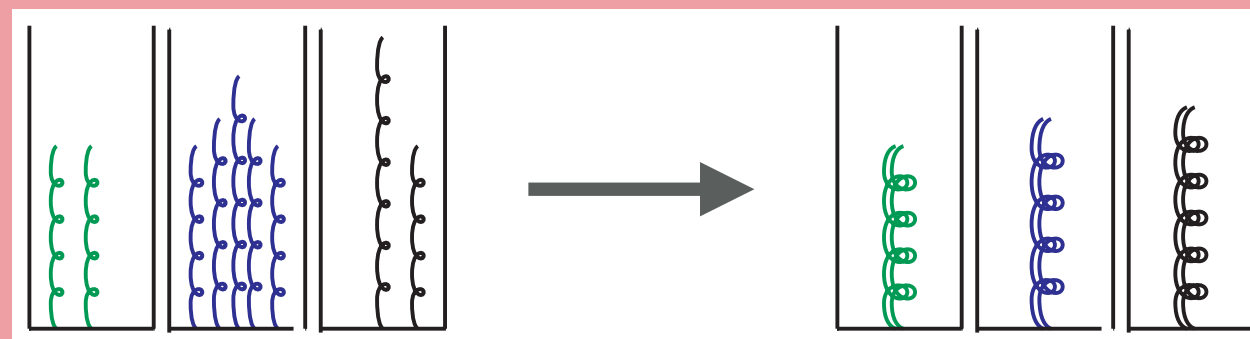
$$\alpha_s(k_\perp^2) = \frac{12\pi}{33 - 2n_f} \frac{1}{\ln(k_\perp^2/\Lambda_{\text{QCD}}^2)}$$

leads to the inclusive probability

$$d\mathcal{P}(q(p_I)\bar{q}(p_K) \rightarrow q(p_i)g(p_j)\bar{q}(p_k)) \simeq \frac{d\kappa}{\kappa} \frac{dy}{\delta y_g} \quad \text{with} \quad \delta y_g = \frac{11}{6}$$

Interpreting the running coupling renormalisation group as a gain-loss equation:

Gluons within δy_g act coherently as one effective gluon



Discrete QCD - Abstracting the Parton Shower Method

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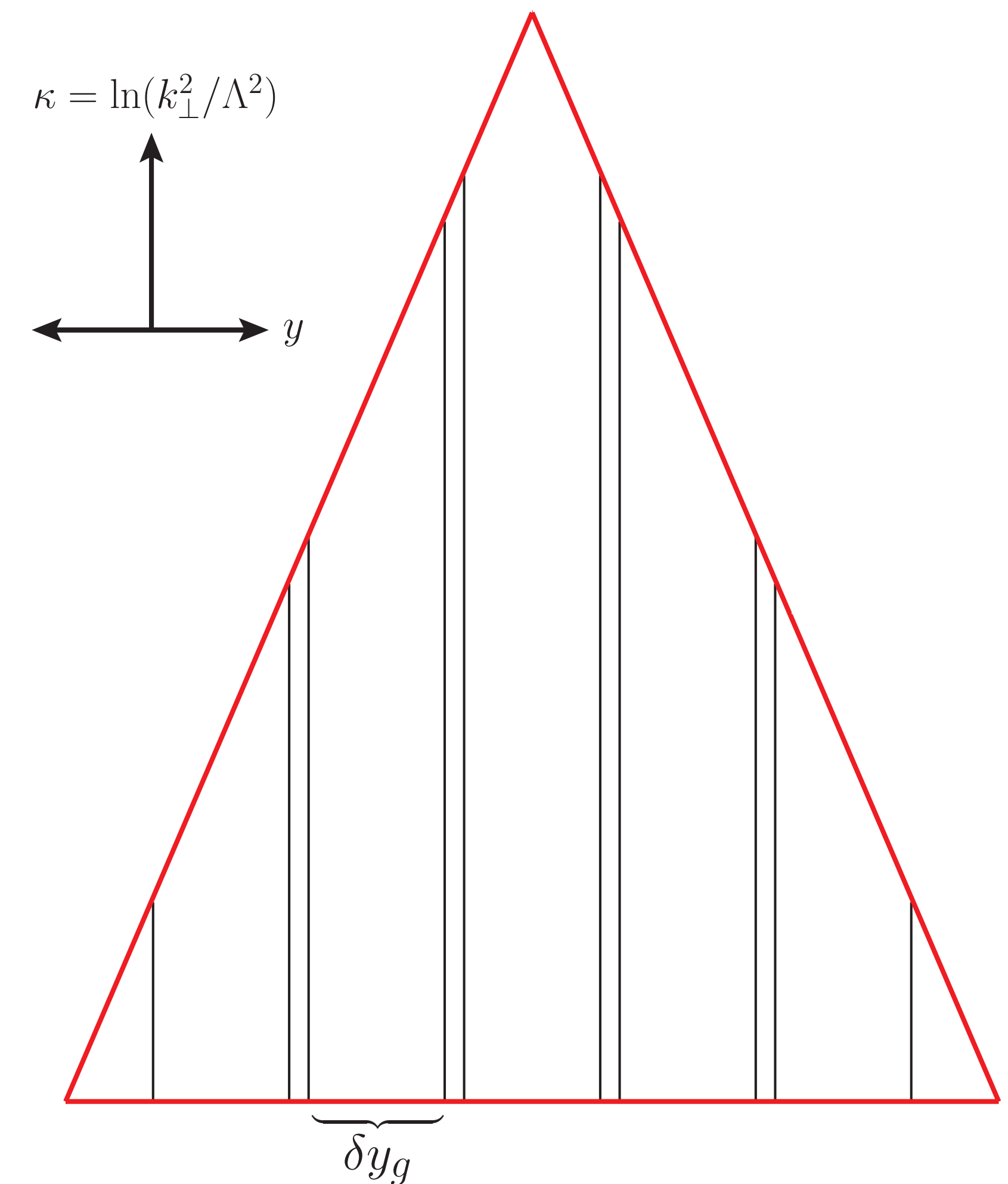
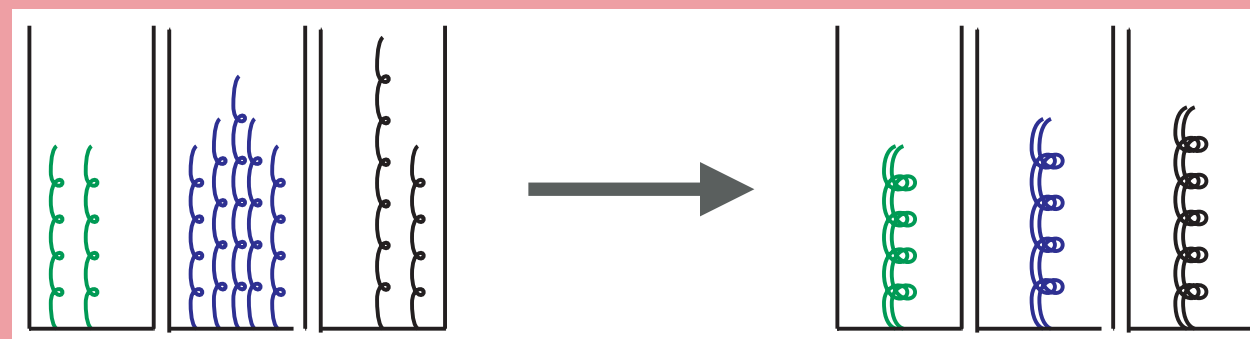
$$\alpha_s(k_\perp^2) = \frac{12\pi}{33 - 2n_f} \frac{1}{\ln(k_\perp^2 / \Lambda_{\text{QCD}}^2)} = \frac{\text{const.}}{\kappa}$$

leads to the inclusive probability

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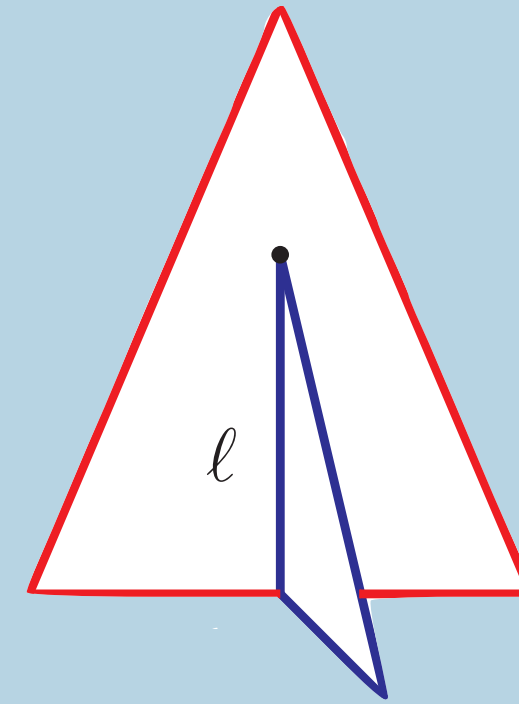
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Discrete QCD - Abstracting the Parton Shower Method

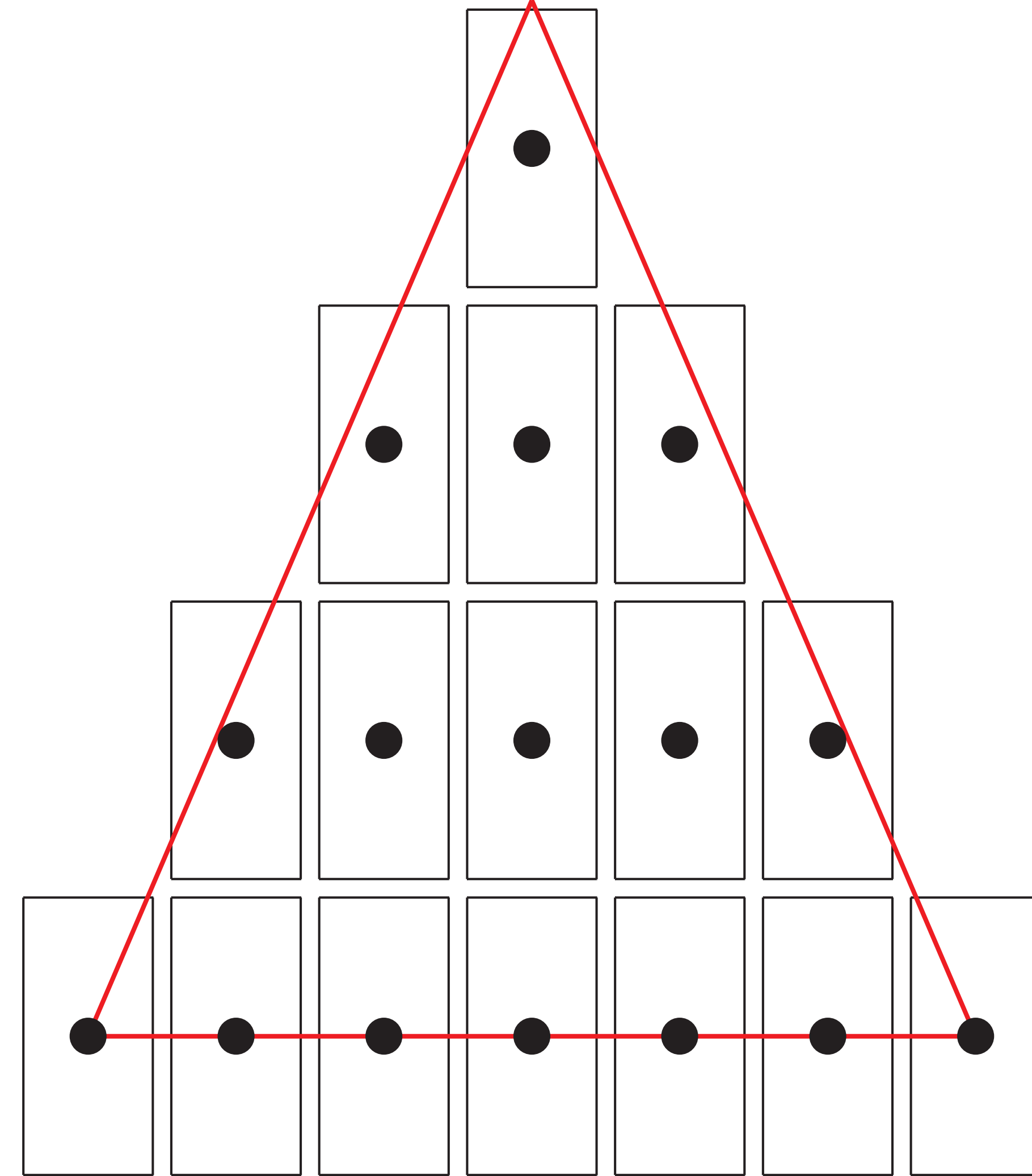
Folding out extends the baseline of the triangle to positive y by $\frac{l}{2}$, where l is the height at which to emit effective gluons



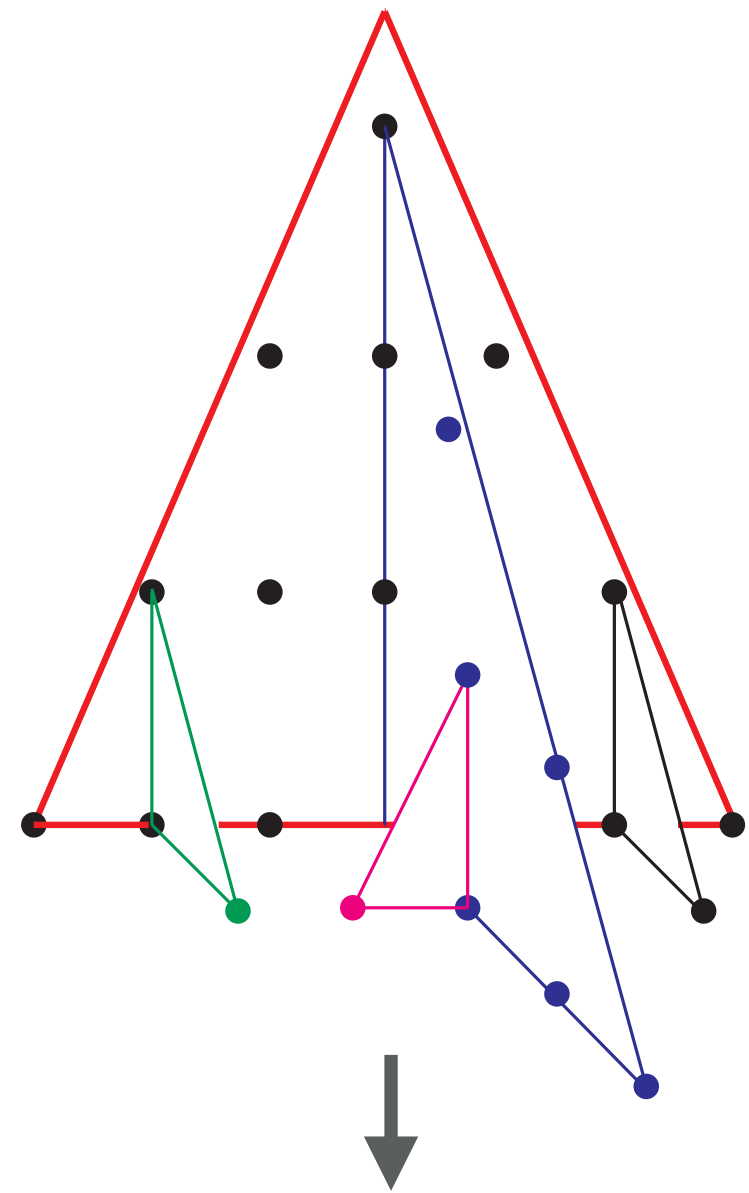
A consequence of folding is that the κ axis is quantised into multiples of $2\delta y_g$

Each rapidity slice can be treated independently of any other slice. The exclusive rate probability takes the simple form:

$$\frac{d\kappa}{\kappa} \exp \left(- \int_{\kappa}^{\kappa_{max}} \frac{d\bar{\kappa}}{\bar{\kappa}} \right) = \frac{d\kappa}{\kappa_{max}}$$

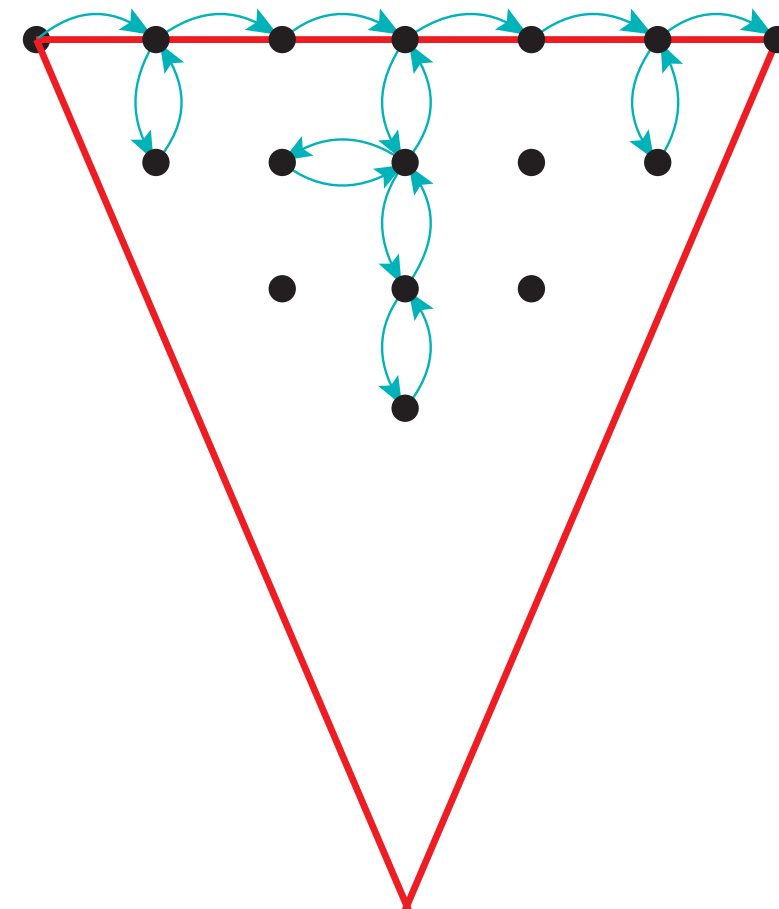
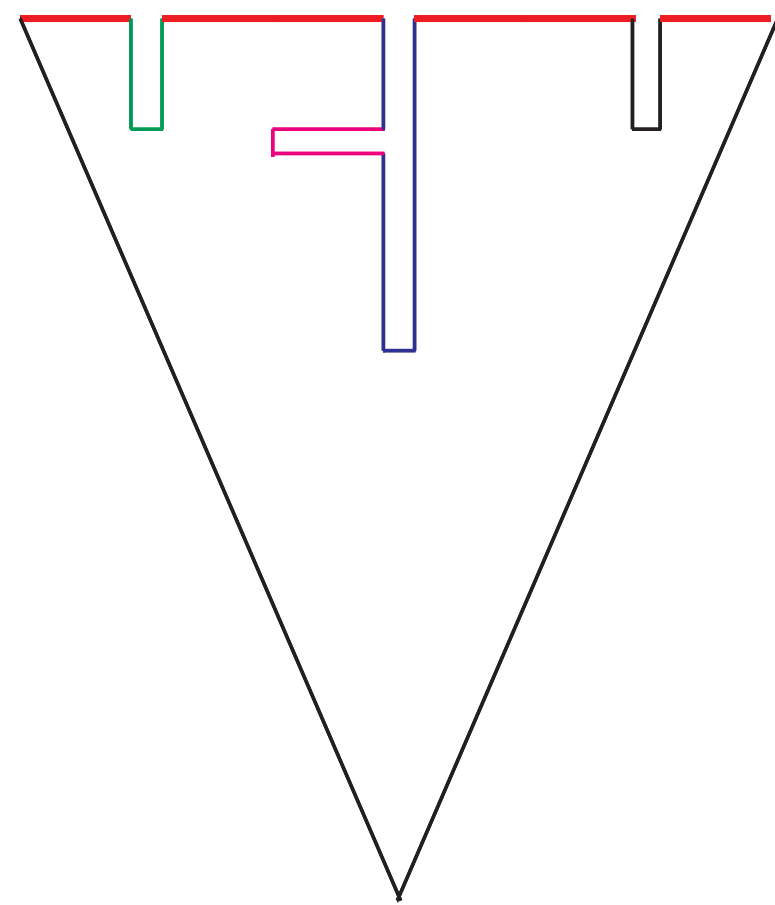


Discrete QCD as a Quantum Walk

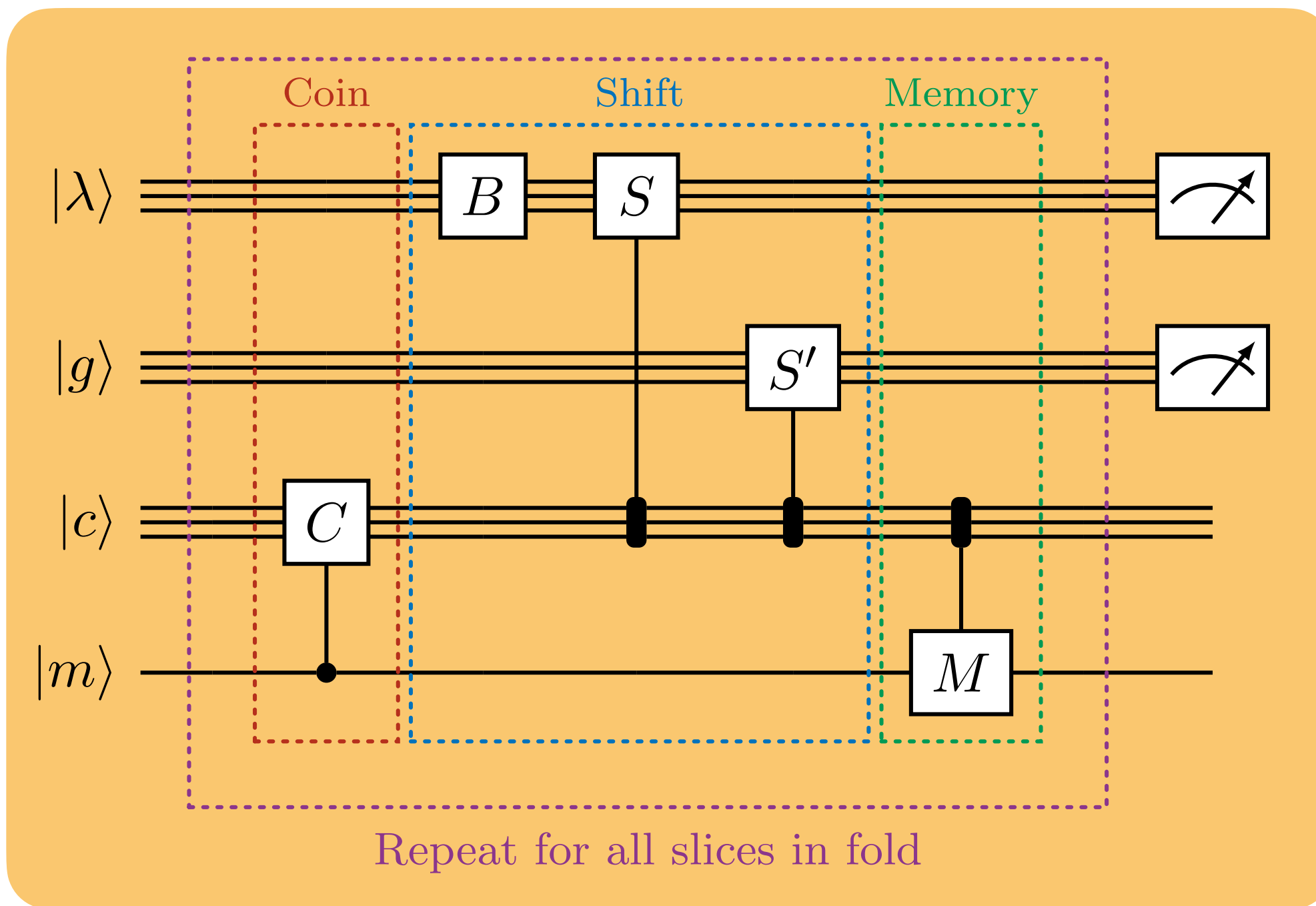


The **baseline** of the grove structure contains all kinematics information

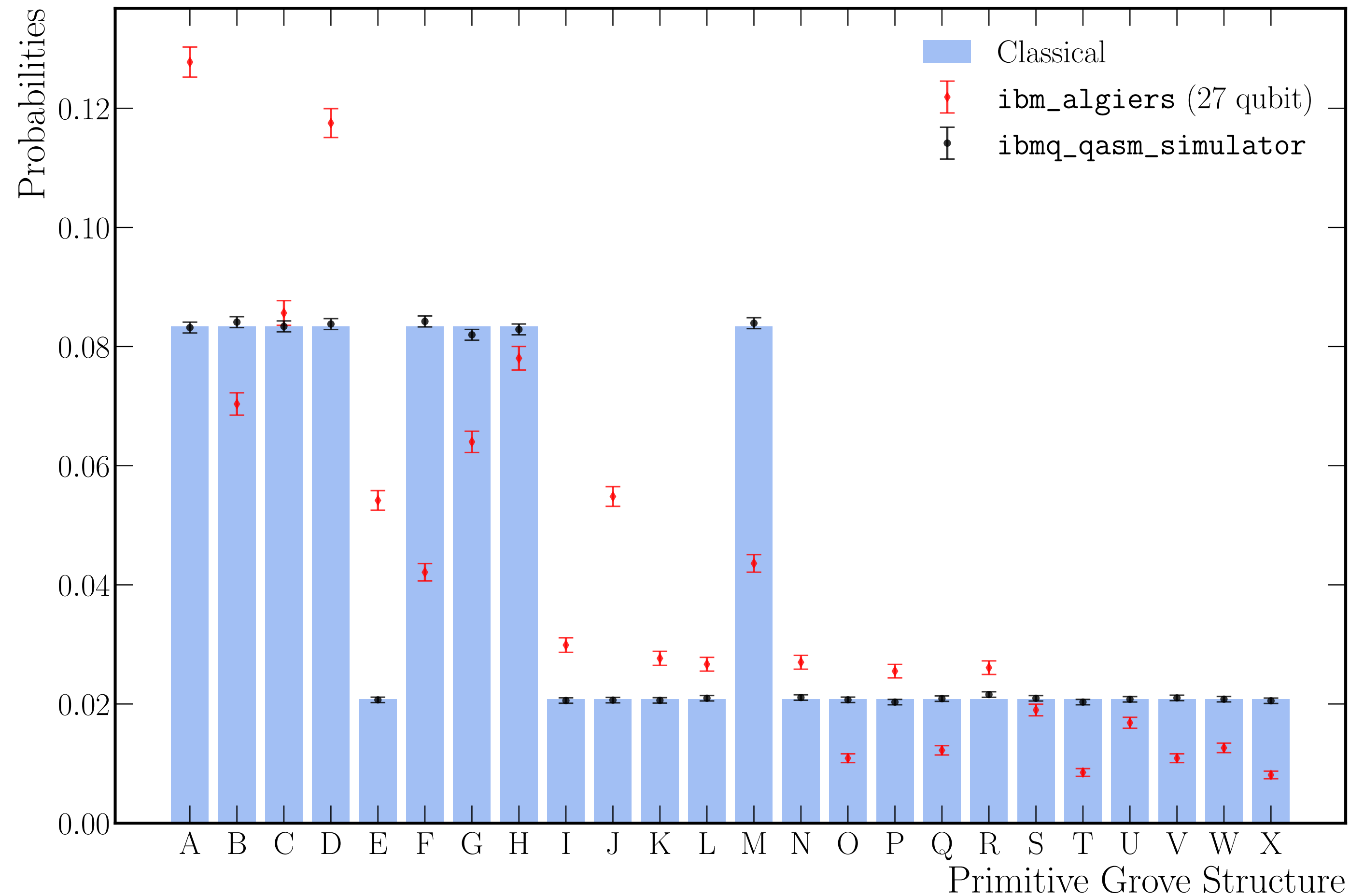
For LEP data there are **24 unique grove structures** for $\Lambda_{\text{QCD}} \in [0.1, 1] \text{ GeV}$



The Discrete-QCD dipole cascade can therefore be implemented as a simple **Quantum Walk**



Discrete QCD as a Quantum Walk - Raw Grove Simulation



The algorithm has been run on the **IBM Falcon 5.1 Ir chip**

The figure shows the uncorrected performance of the **ibm_algiers** device compared to a simulator

The 24 grove structures are generated for a $E_{CM} = 91.2$ GeV, corresponding to typical collisions at LEP.

Main source of error from CNOT errors from large amount of SWAPs

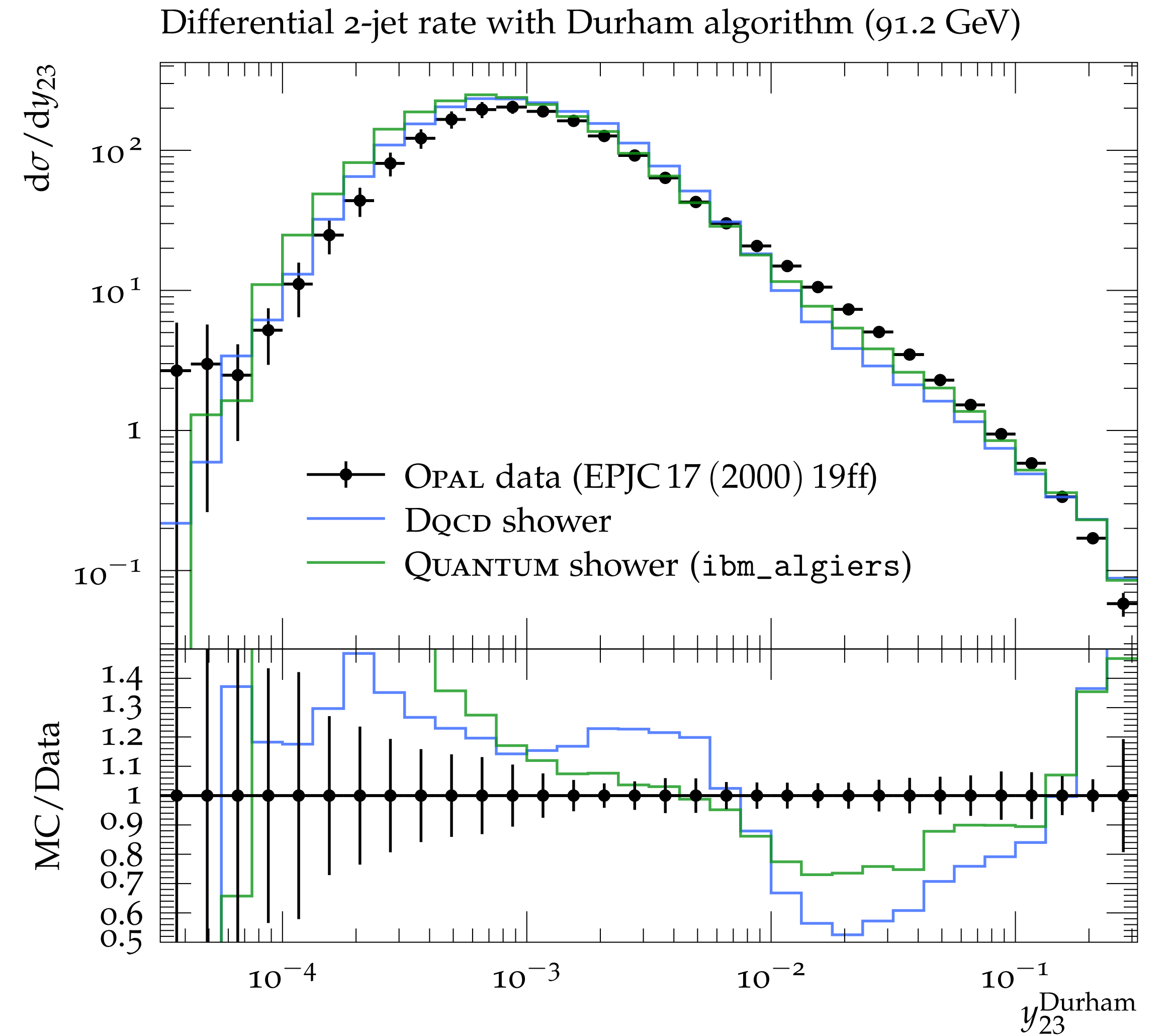
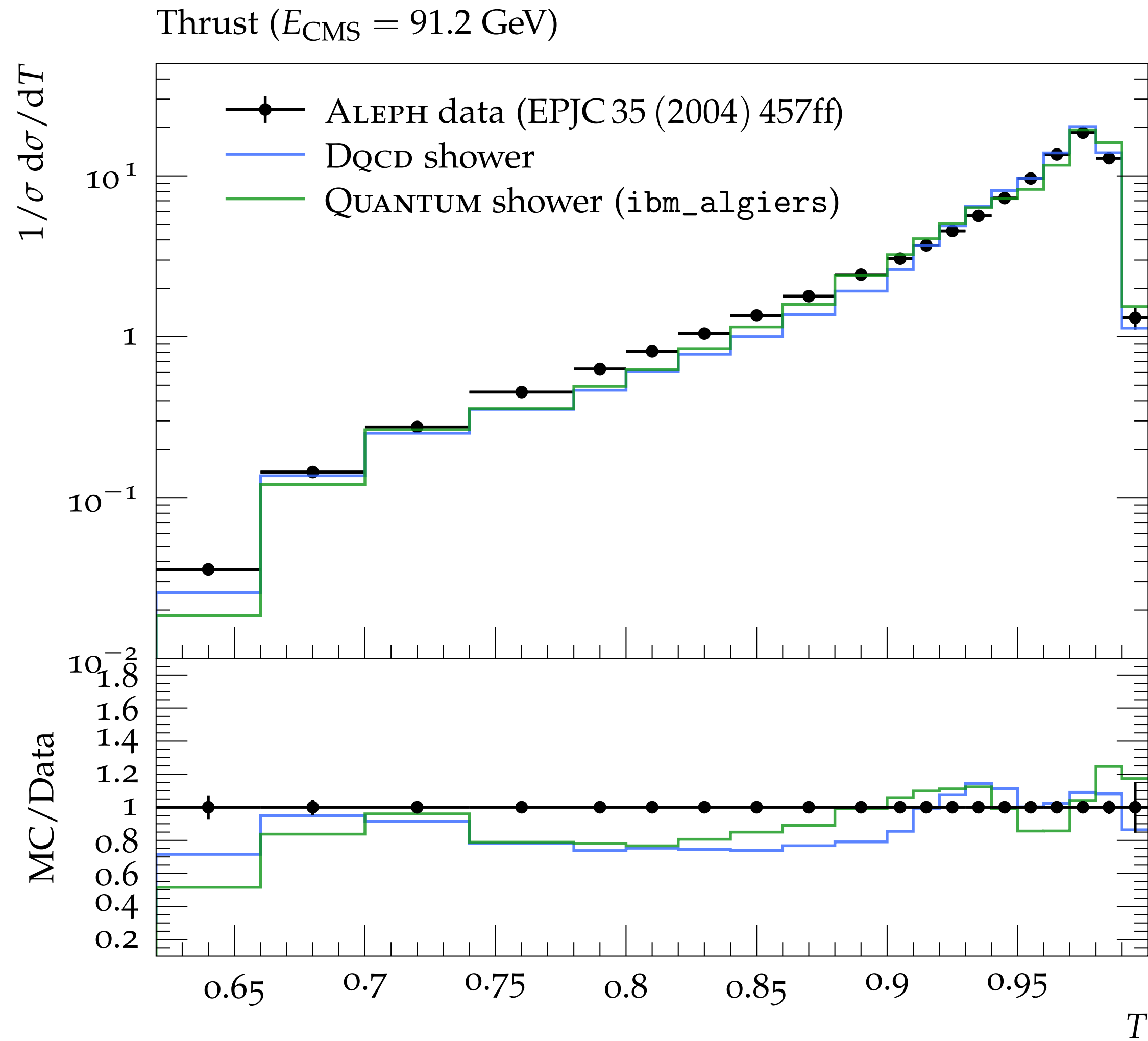
Generating Scattering Events from Groves

Once the grove structure has been selected, event data can be synthesised in the following steps using the baseline:

1. Create the highest κ effective gluons first (i.e. go from top to bottom in phase space)
2. For each effective gluon j that has been emitted from a dipole IK , read off the values s_{ij} , s_{jk} and s_{IK} from the grove
3. Generate a uniformly distributed azimuthal decay angle ϕ , and then employ momentum mapping (here we have used [Phys. Rev. D 85, 014013 \(2012\), 1108.6172](#)) to produce post-branching momenta

This has been done using the ibm_cloud 27 qubit device ibm_algiers, with 20,000 shots on the device. A comparison with a like-for-like classical parton shower algorithm has been made.

Collider Events on a Quantum Computer



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Summary

High Energy Physics is on the edge of a **computational frontier**, the High Luminosity Large Hadron Collider and FCC will provide **unprecedented amounts of data**

Quantum Computing offers an impressive and powerful tool to **combat computational bottlenecks**, both for theoretical and experimental purposes

The **first realistic simulation** of a **high energy collision** has been presented using a compact **quantum walk** implementation, allowing for the algorithm to be run on a **NISQ device**

Future Work: A dedicated research effort is required to fully evaluate the **potential** of **quantum computing** applications in **HEP**

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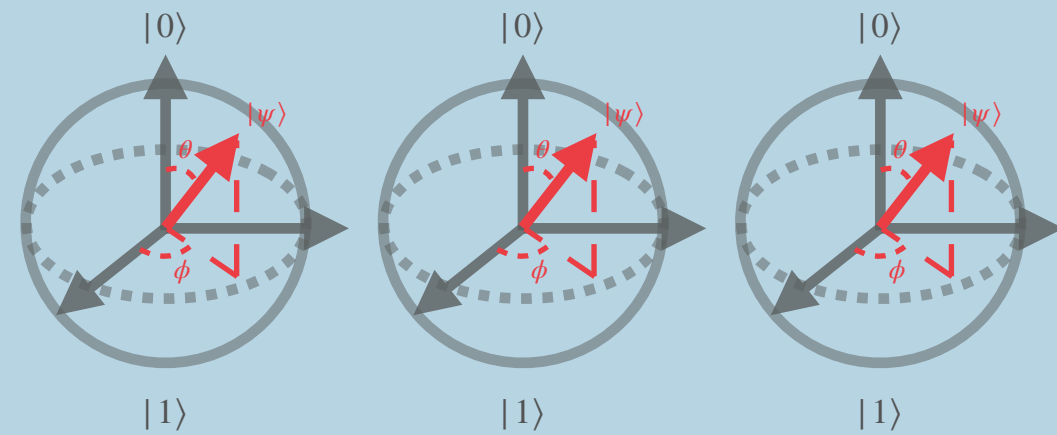
Backup Slides

Simon Williams

Resummation, Evolution, Factorization
2022

The Future of Quantum Computing

More qubits?



A lot of emphasis on more qubits, but without fault tolerance, large qubit devices become **impractical**

Be better architects?

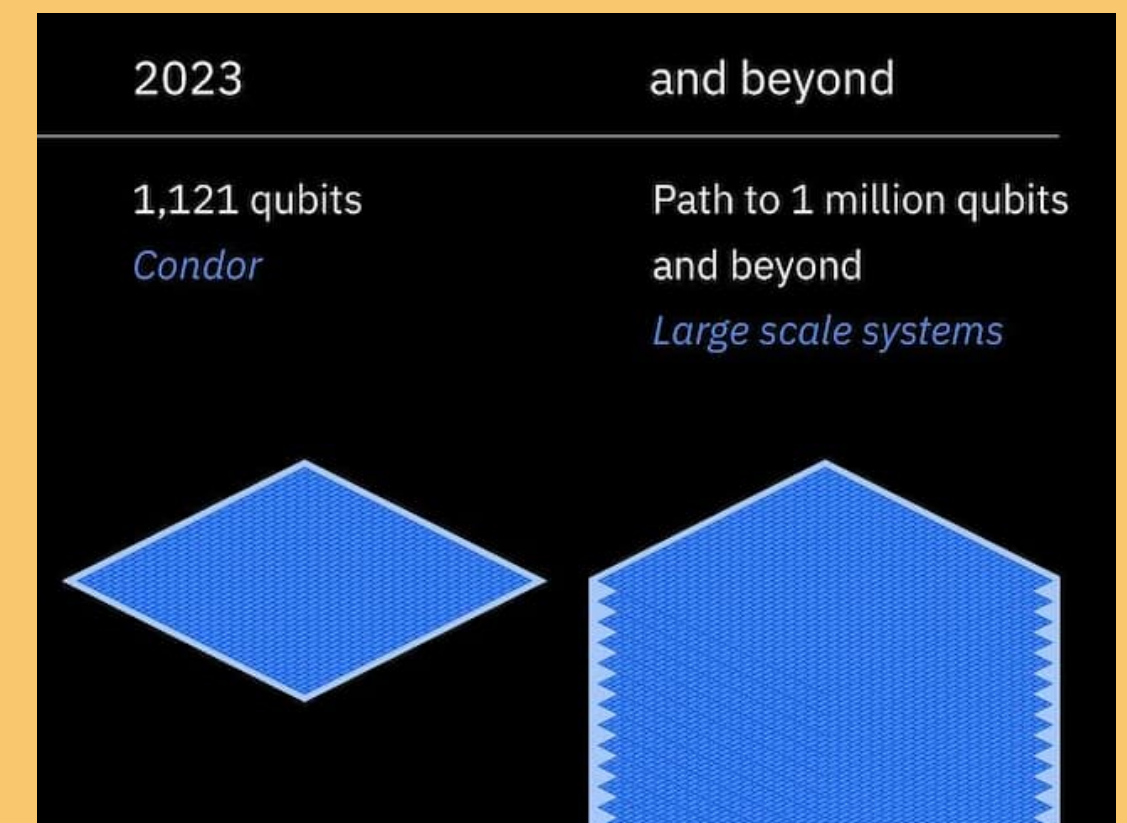
Realistic algorithms are already being created for NISQ devices. Efficient architectures allow for **practical algorithms** on NISQ devices.

Better technology?

New technology could be the answer - will new qubit hardware be more **fault tolerant?**

IBM Roadmap

On track to deliver
1000 qubits by 2023



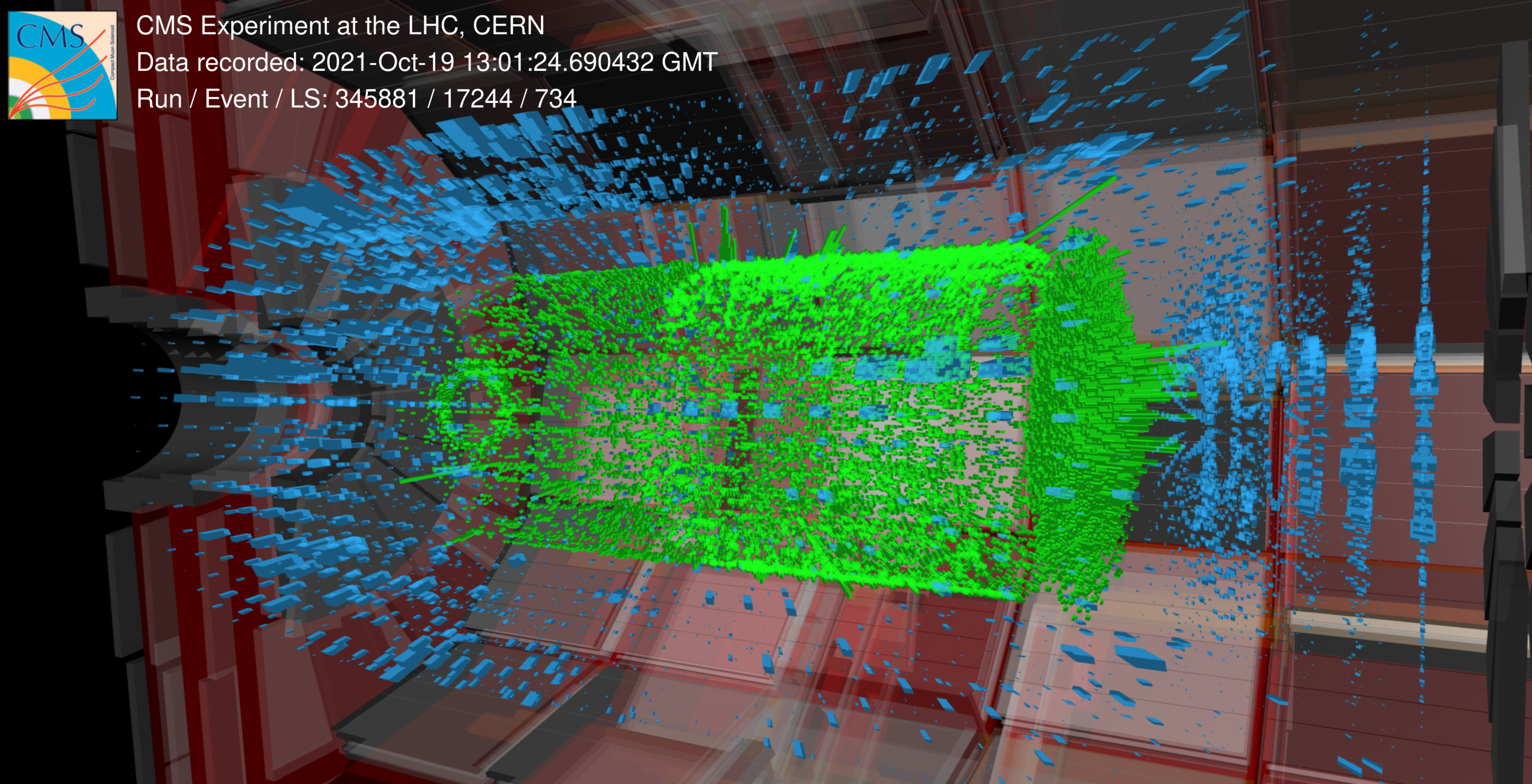
The Power of the Qubit! - Why are we interested in HEP?



CMS Experiment at the LHC, CERN

Data recorded: 2021-Oct-19 13:01:24.690432 GMT

Run / Event / LS: 345881 / 17244 / 734

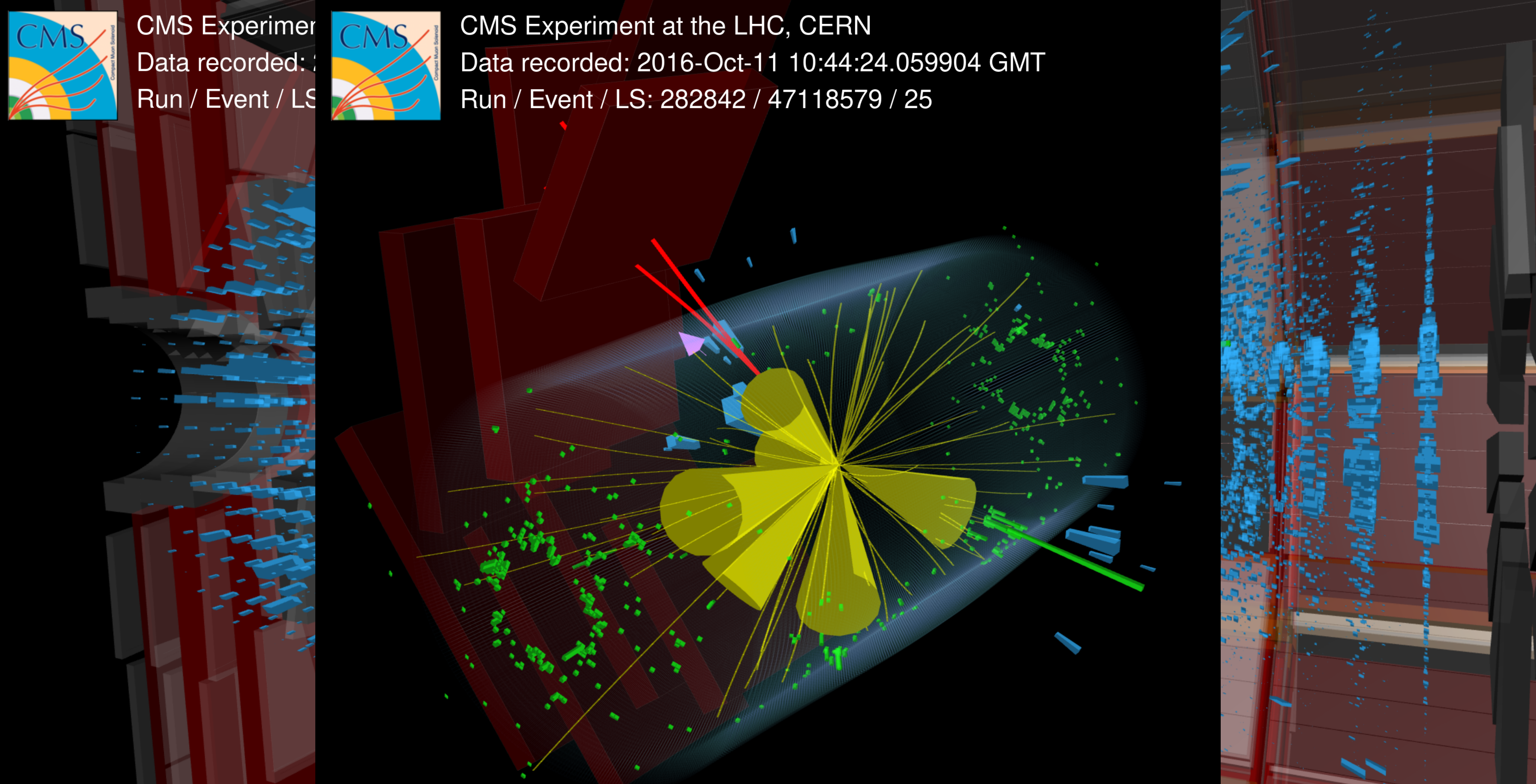




CMS Experiment
Data recorded:
Run / Event / LS

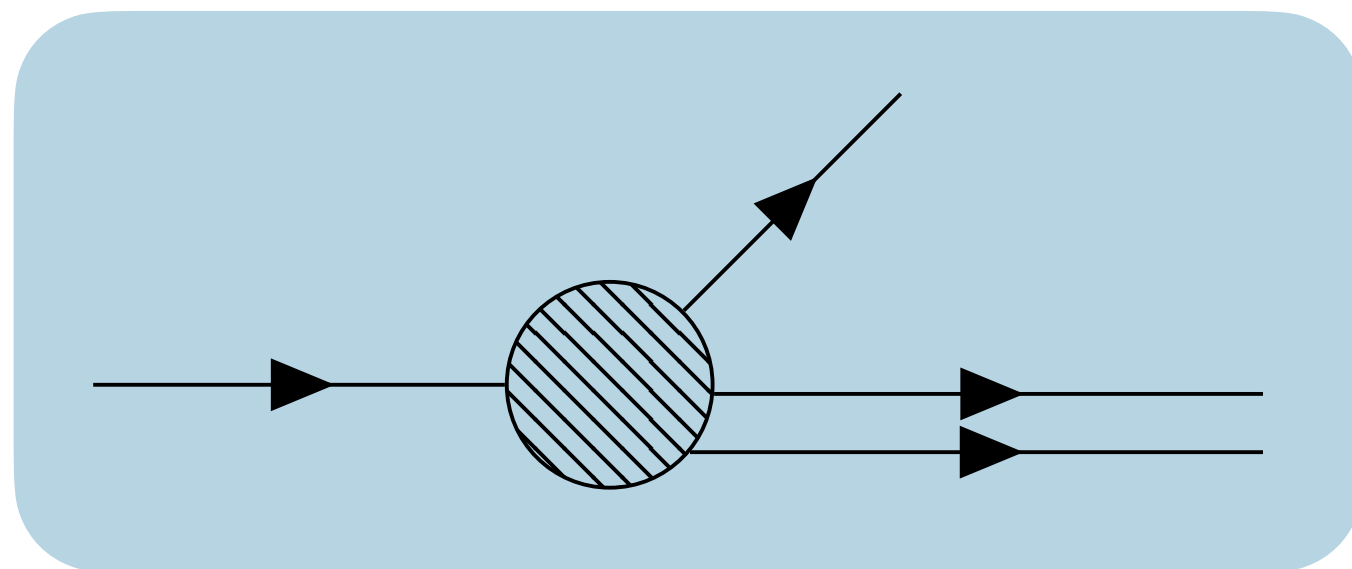
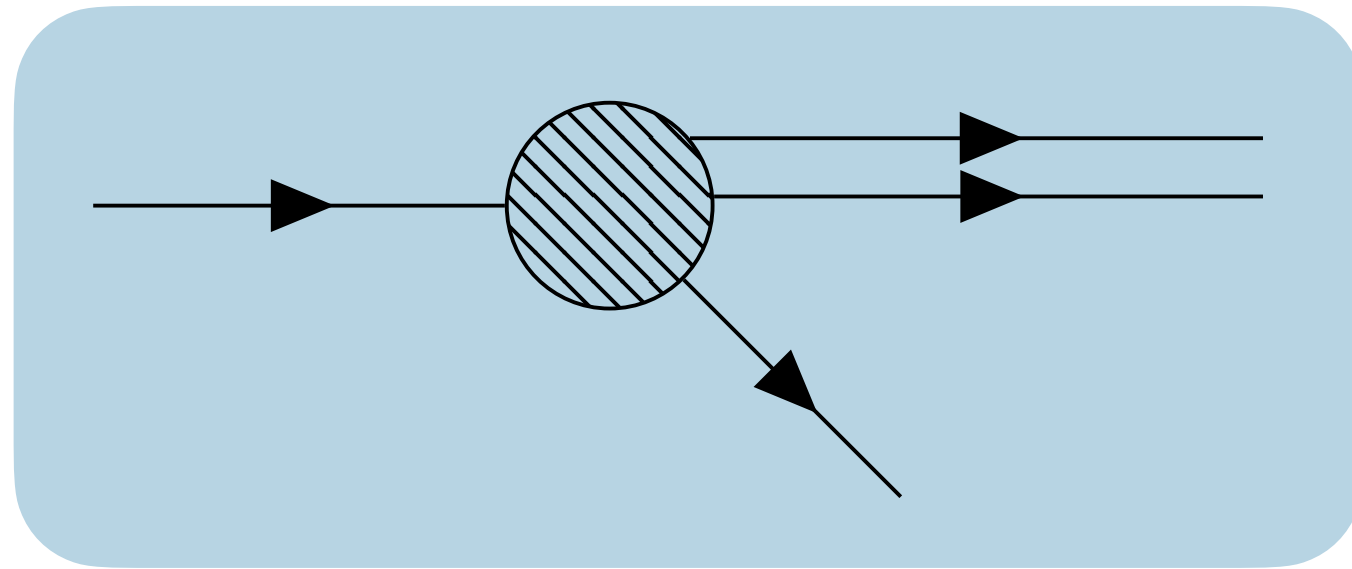


CMS Experiment at the LHC, CERN
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Run / Event / LS: 282842 / 47118579 / 25



The Power of the Qubit! - Why are we interested in HEP?

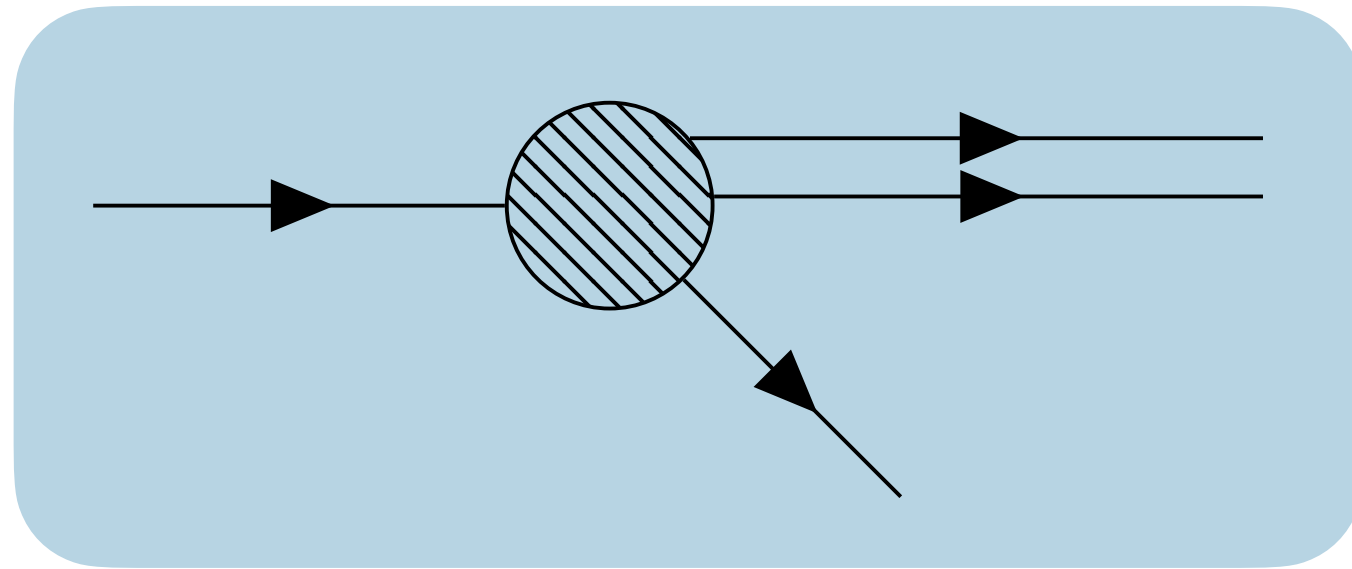
Parton Density Functions



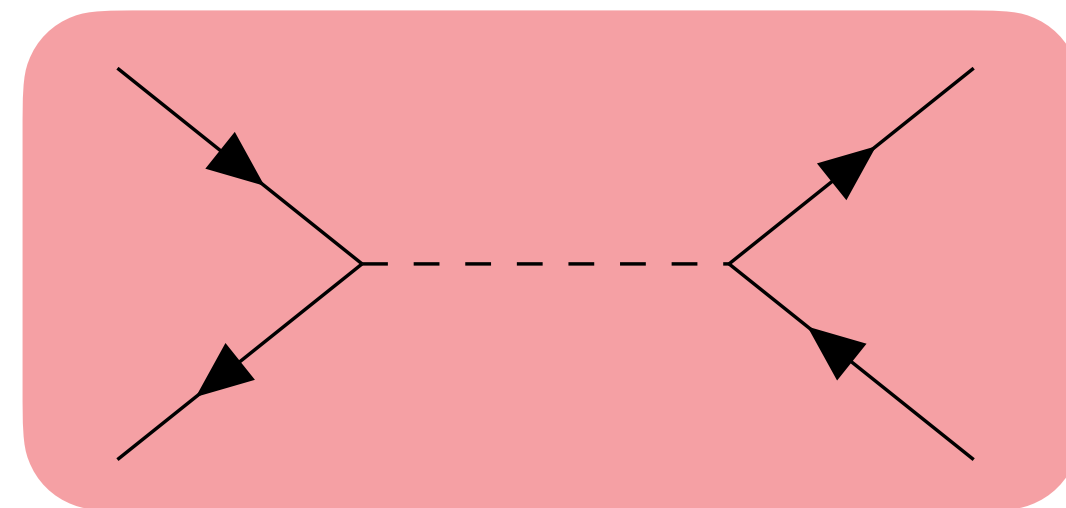
[Phys. Rev. D 103, 034027](#)

The Power of the Qubit! - Why are we interested in HEP?

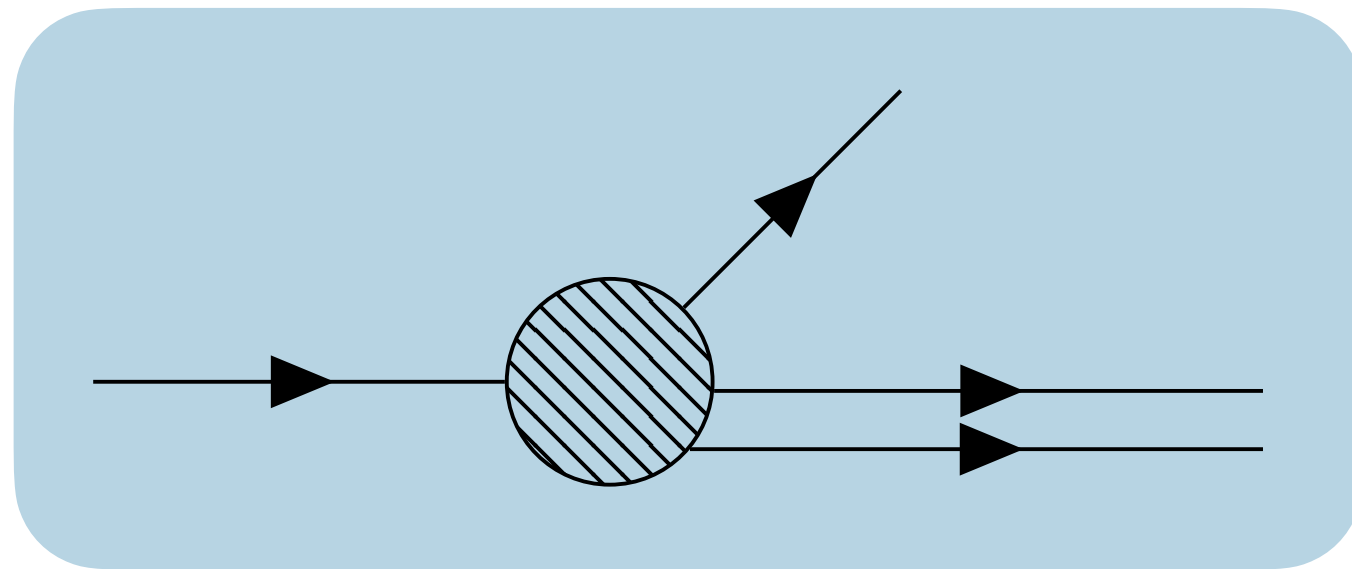
Parton Density Functions



Hard Process



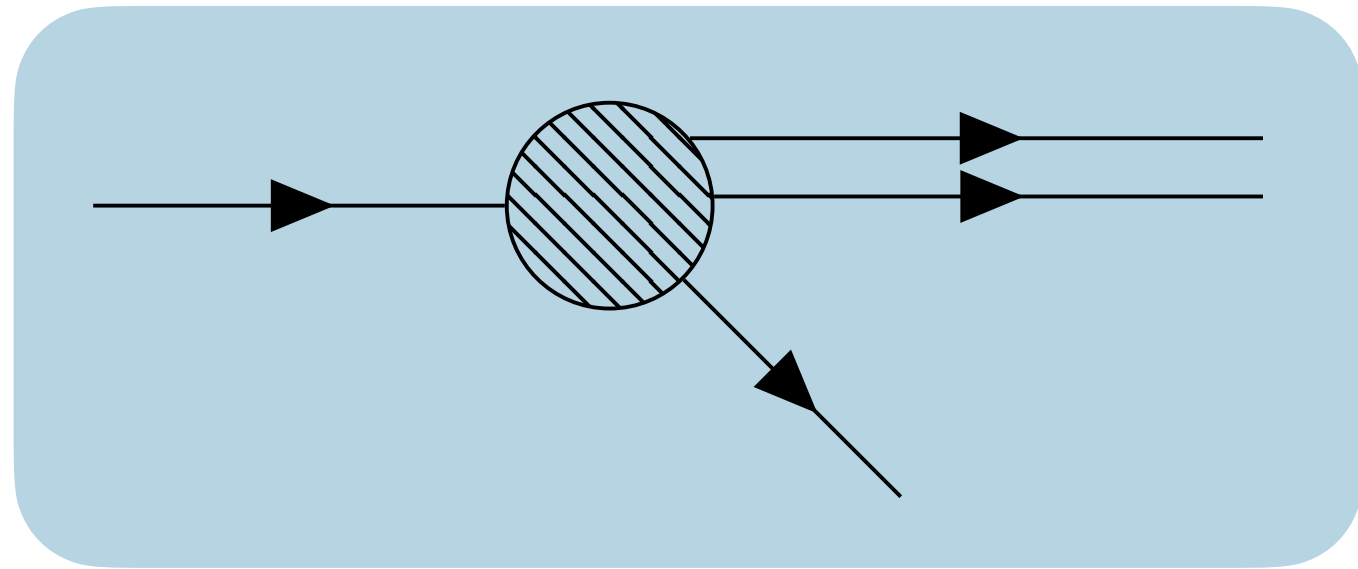
[Phys. Rev. D 103, 076020](#)



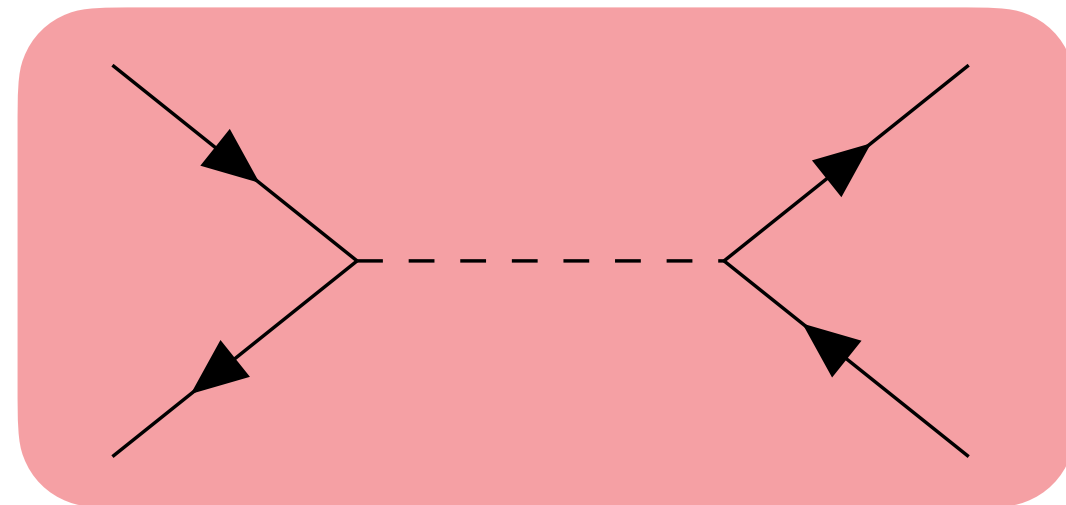
[Phys. Rev. D 103, 034027](#)

The Power of the Qubit! - Why are we interested in HEP?

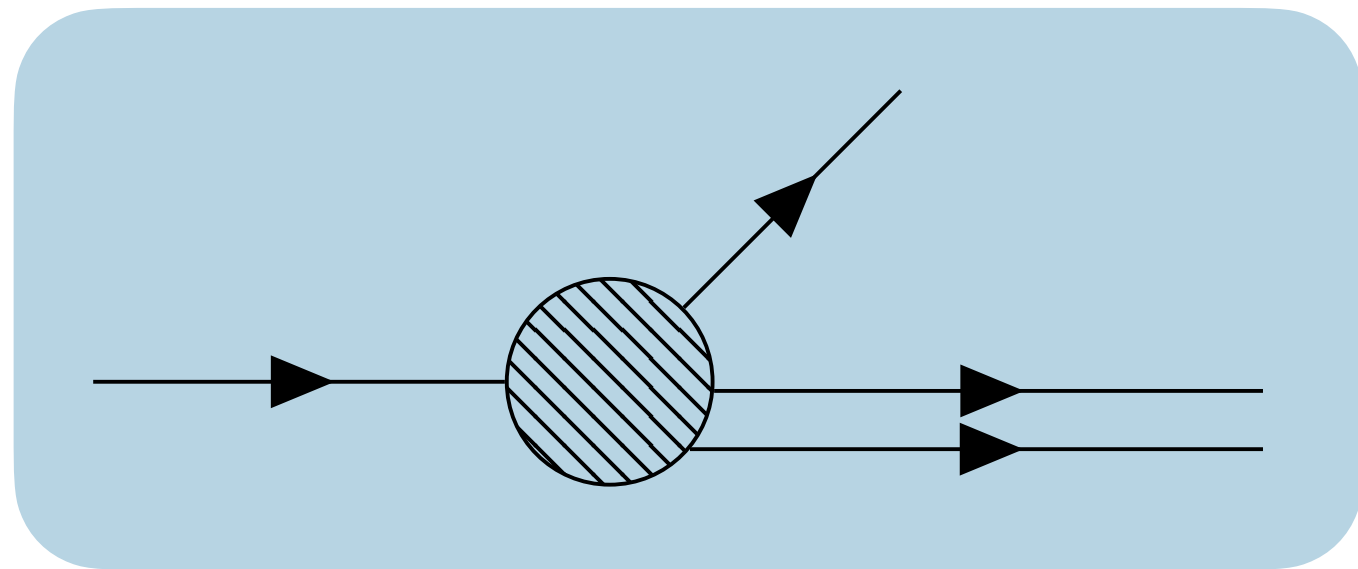
Parton Density Functions



Hard Process

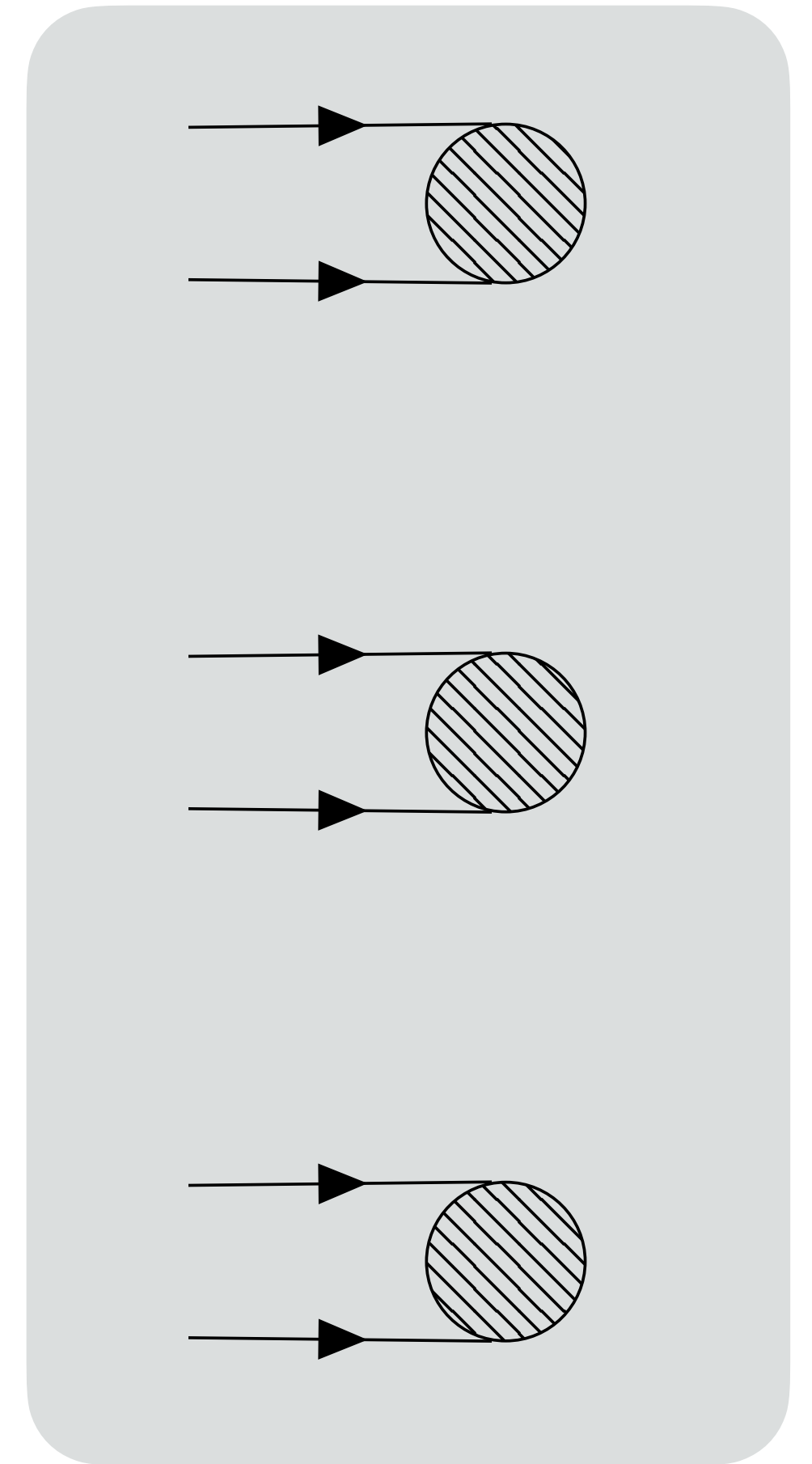


[Phys. Rev. D 103, 076020](#)



[Phys. Rev. D 103, 034027](#)

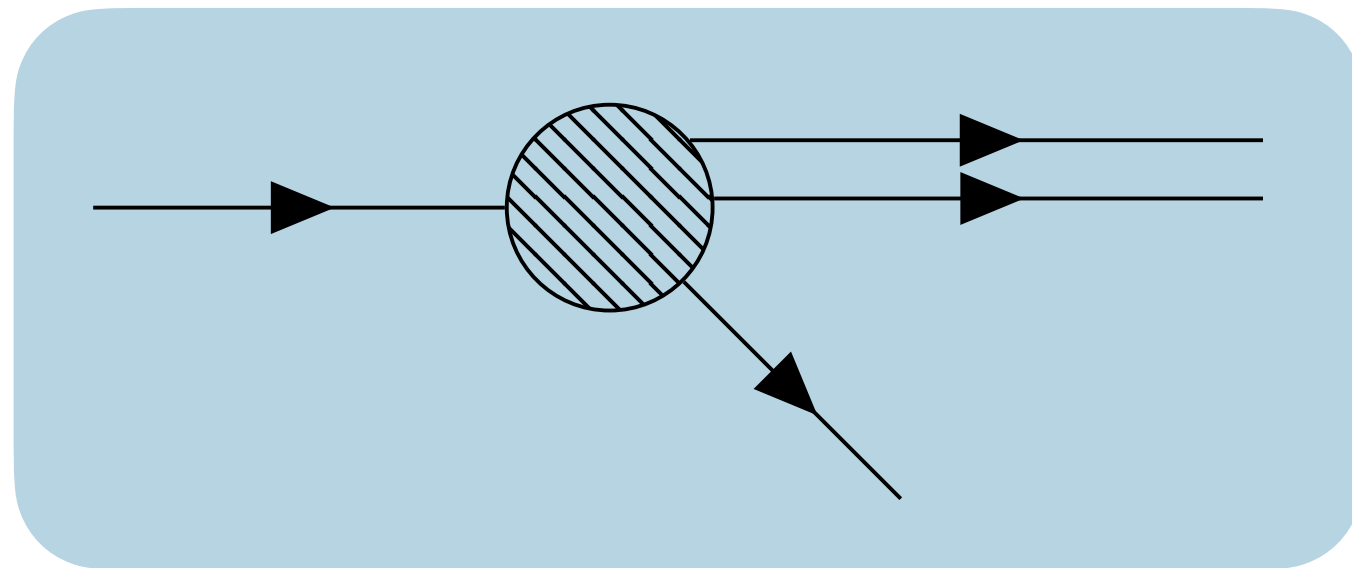
Hadronisation



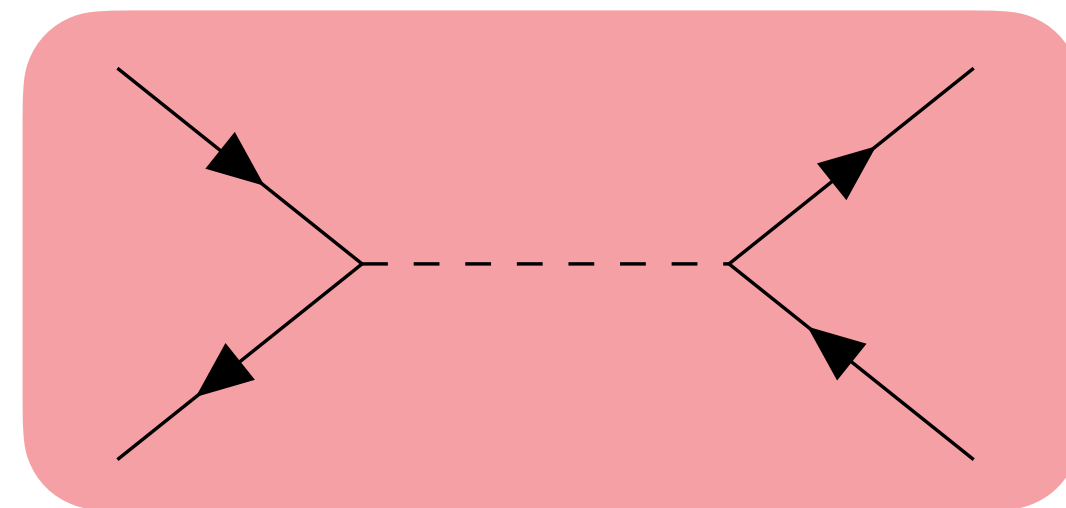
[arXiv:2207.10694](#)

The Power of the Qubit! - Why are we interested in HEP?

Parton Density Functions



Hard Process



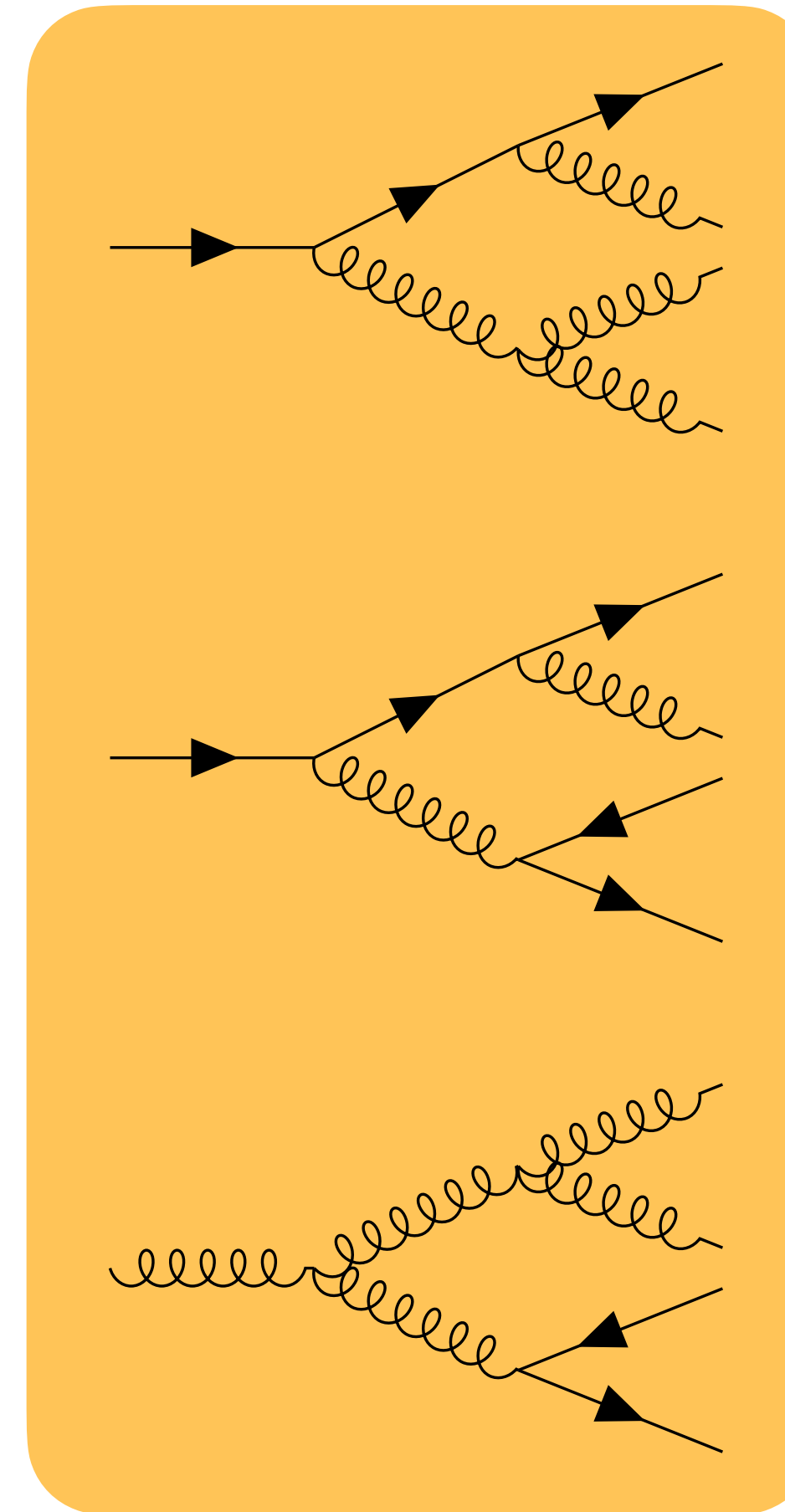
[Phys. Rev. D 103, 076020](#)

[Phys. Rev. D 106, 056002](#)

[Phys. Rev. D 103, 034027](#)

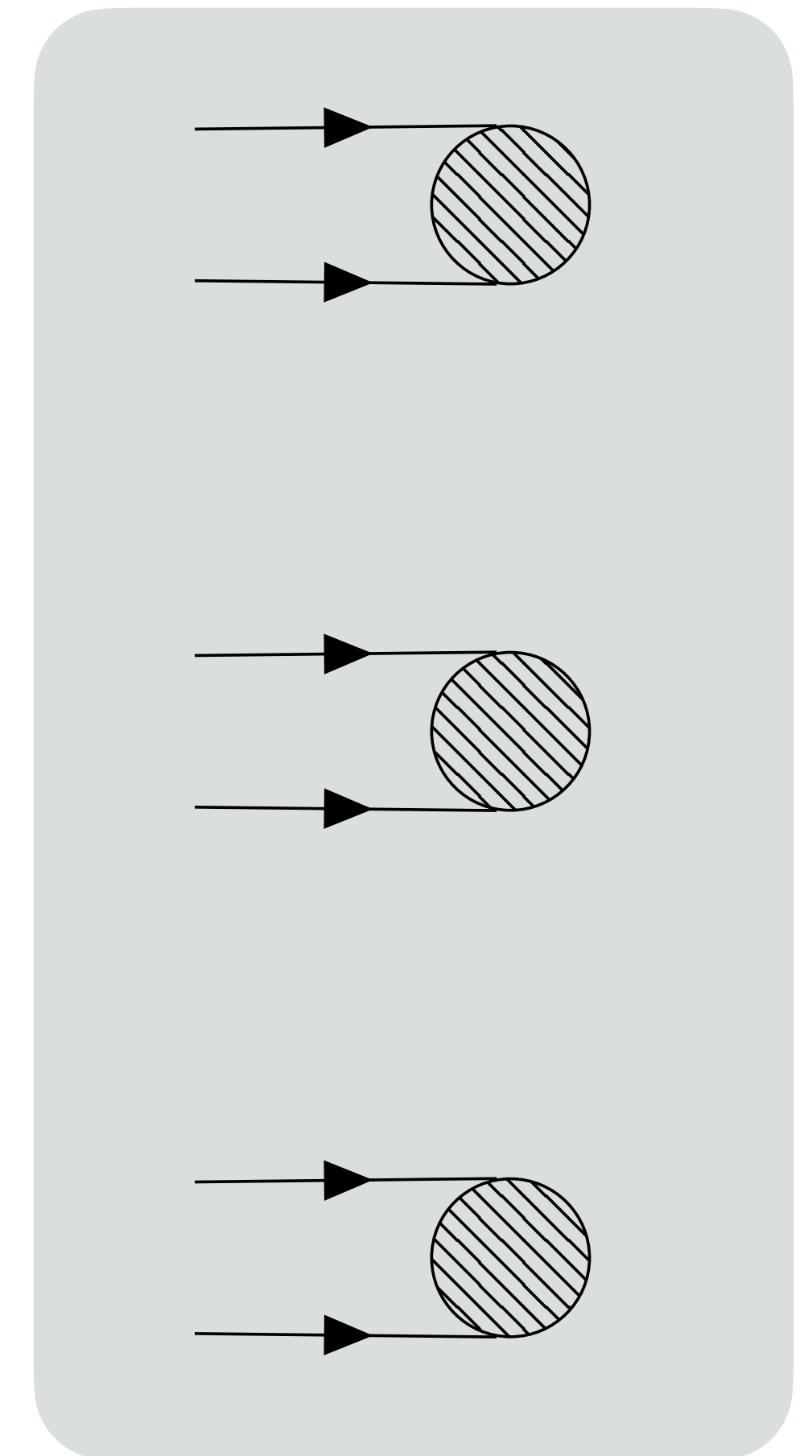
[Phys. Rev. Lett. 126, 062001](#)

Parton Shower



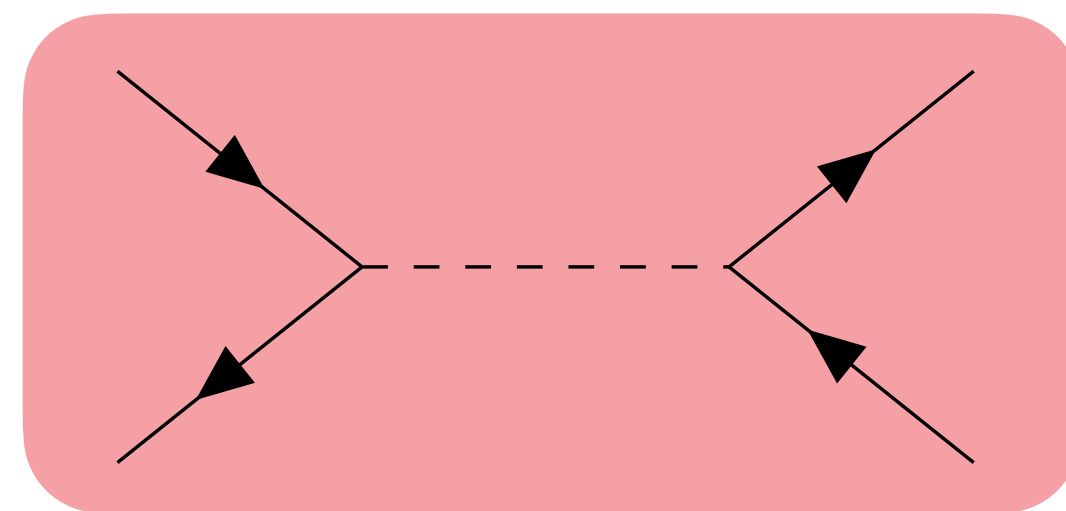
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Hadronisation



The Power of the Qubit! - Why are we interested in HEP?

Hard Process

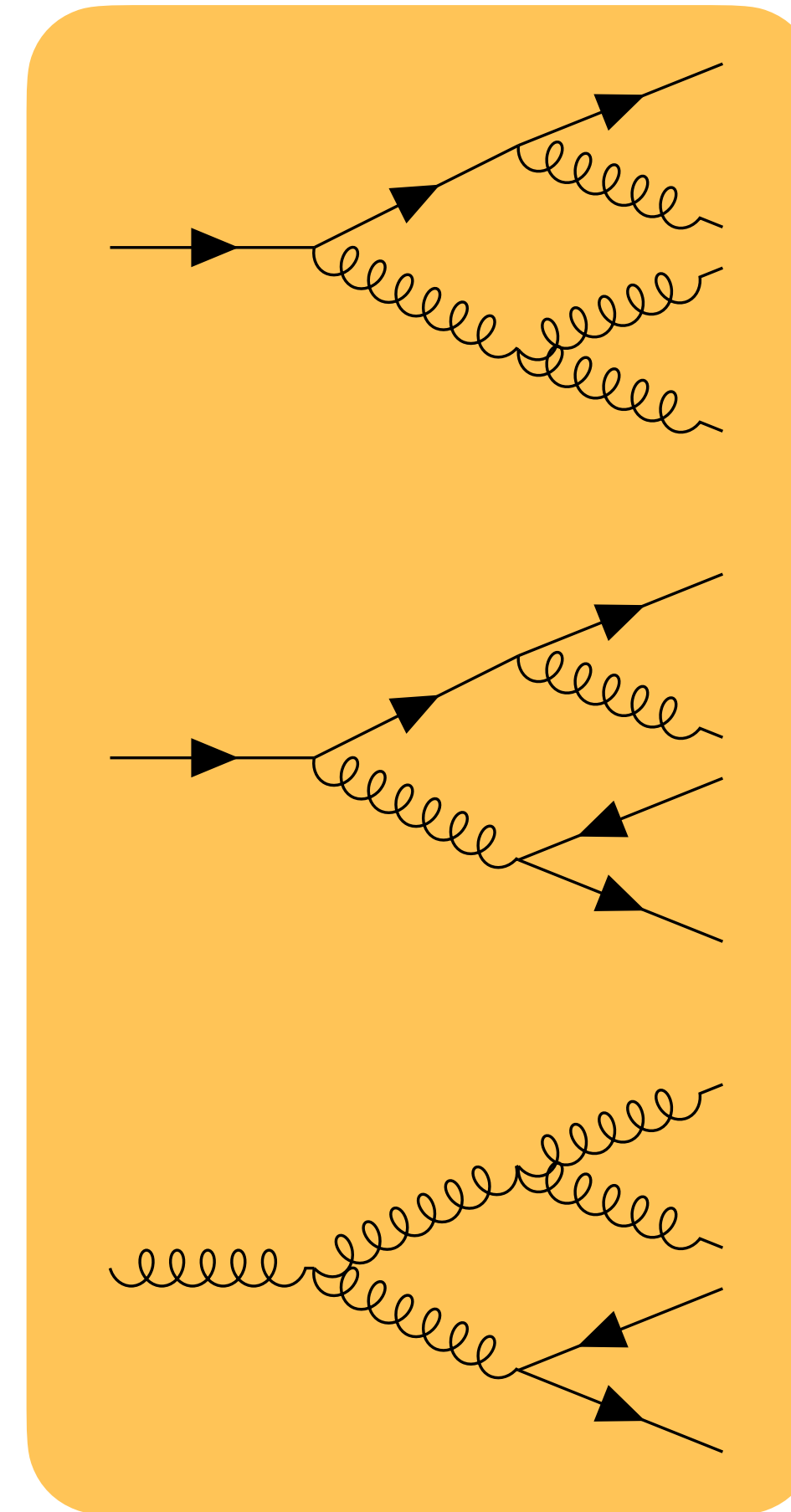


[Phys. Rev. D 103, 076020](#)

[Phys. Rev. D 106, 056002](#)

[Phys. Rev. Lett. 126, 062001](#)

Parton Shower



[arXiv:2207.10694](#)

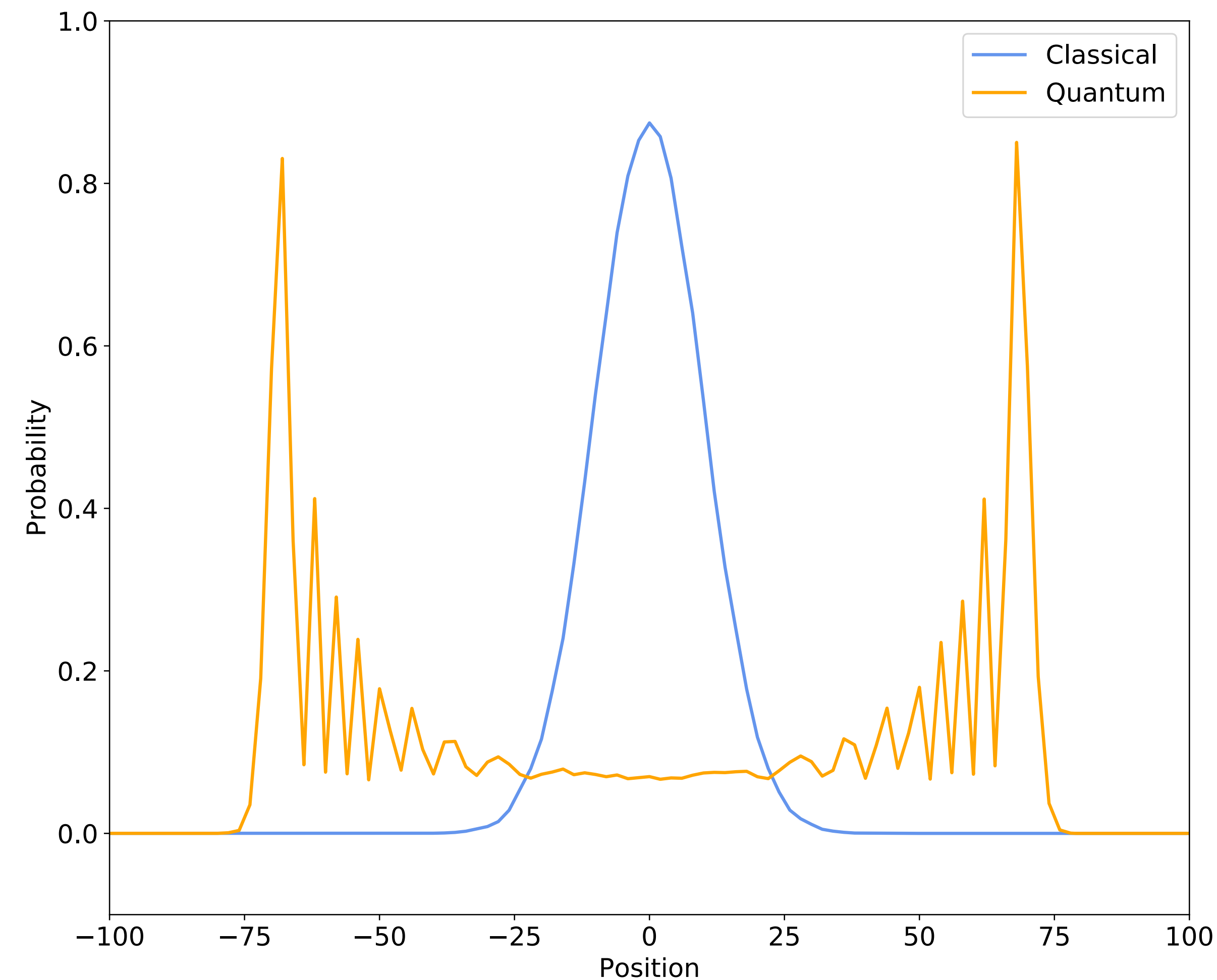
Speed up via Quantum Walks

Quantum Walks have long be conjectured to achieved at least **quadratic speed up**

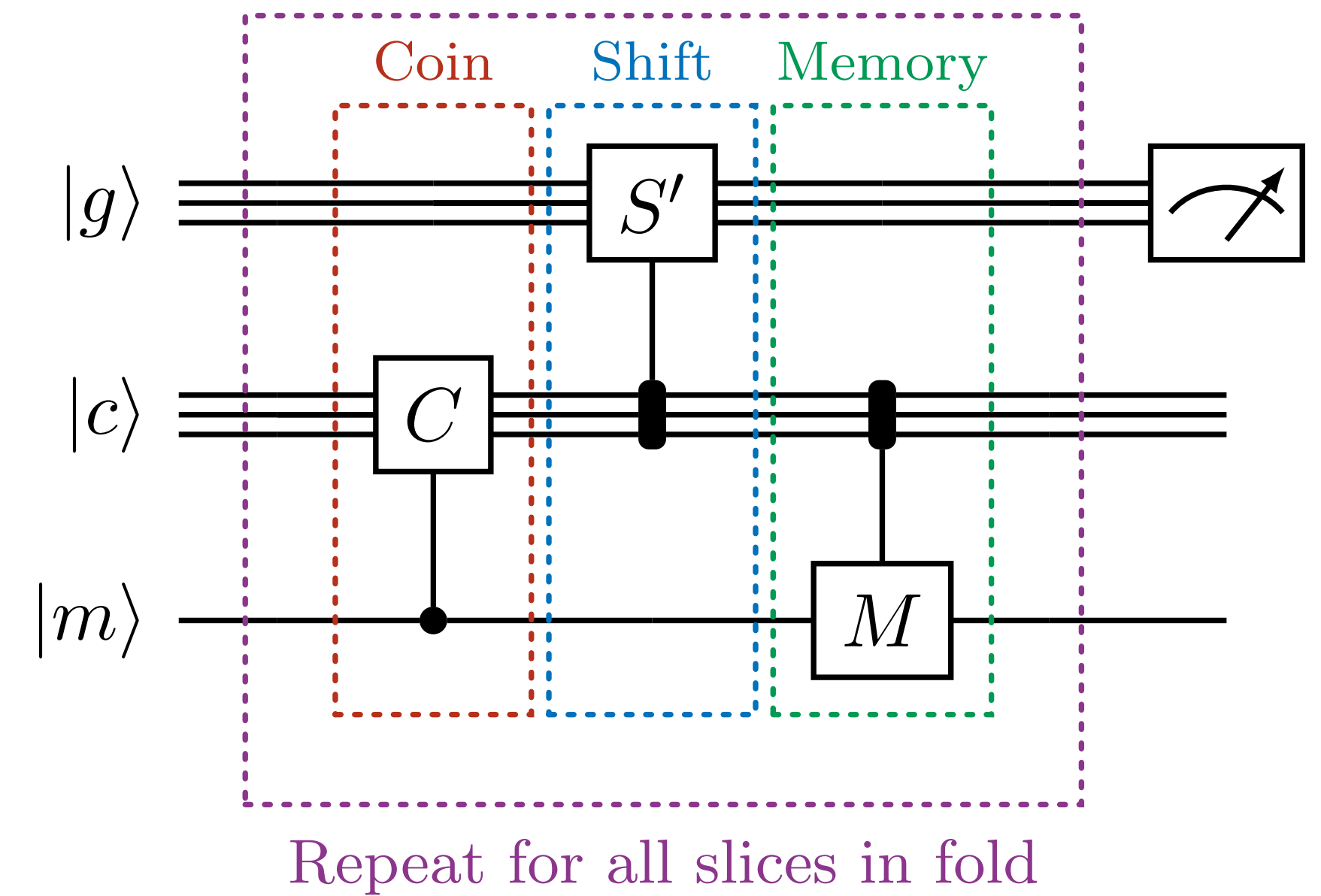
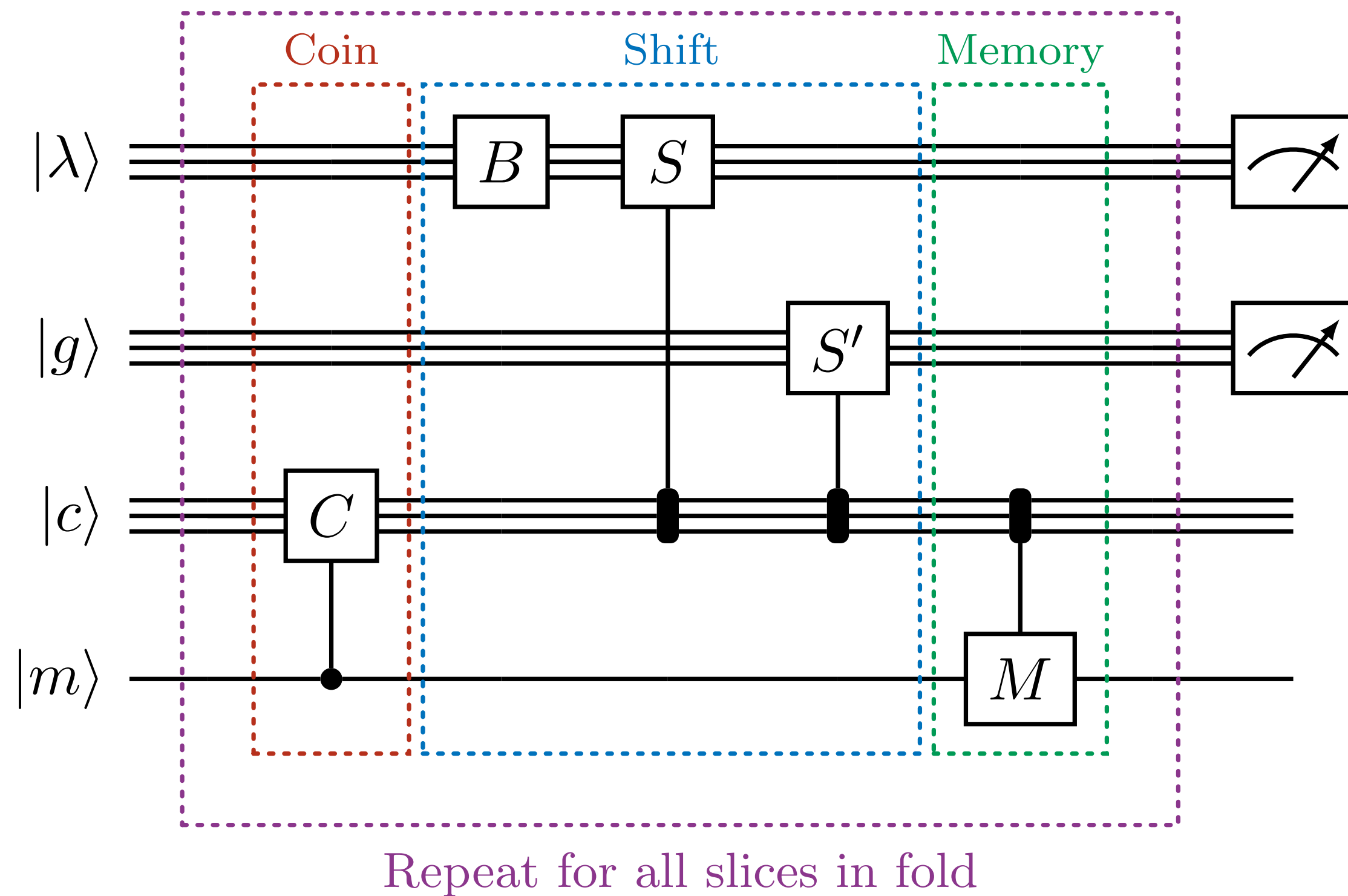
Szegedy Quantum Walks have been proven to achieve quadratic speed up for **Markov Chain Monte Carlo**

This has been proven under the condition that the MCMC algorithm is **reversible and ergodic**

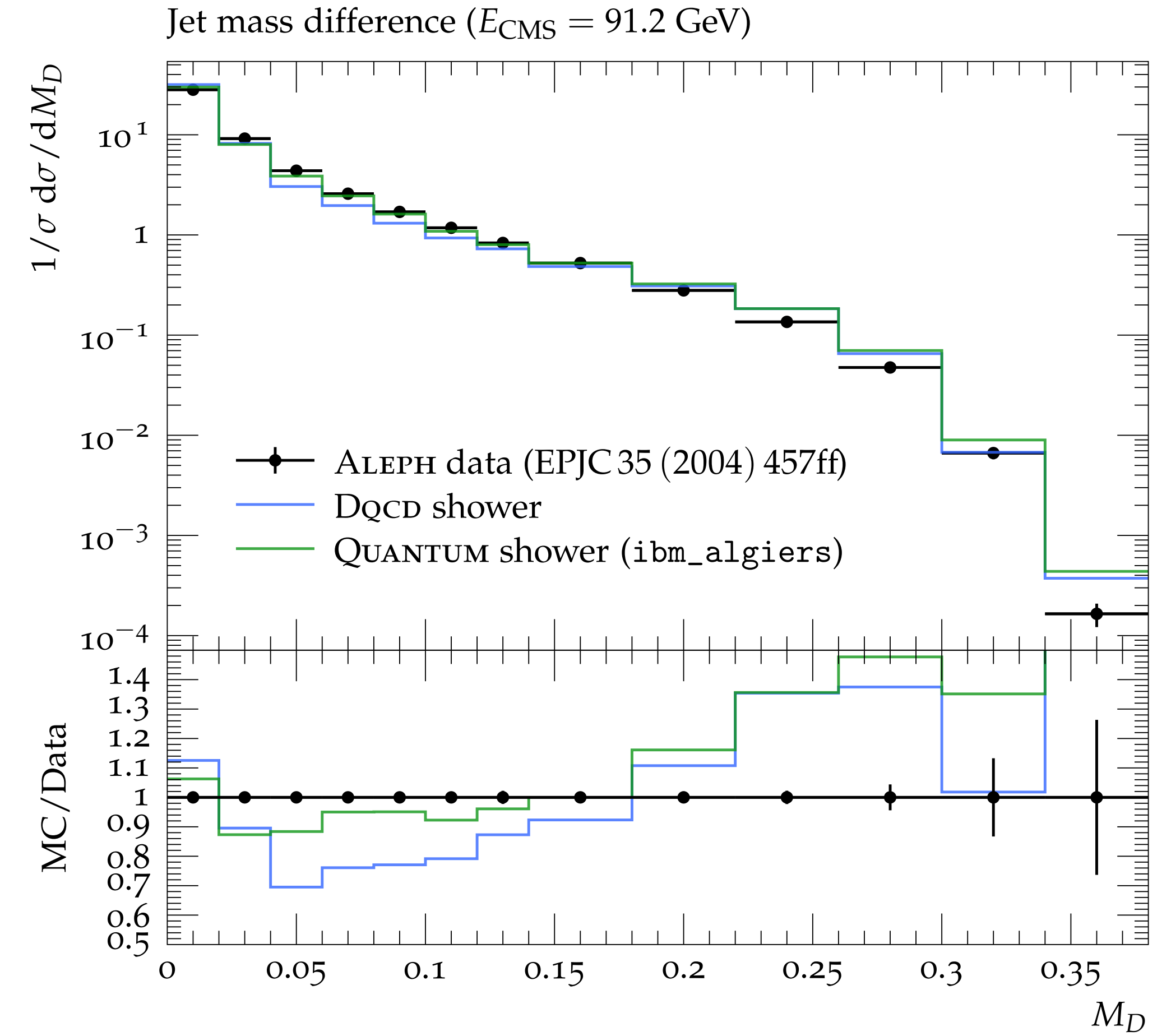
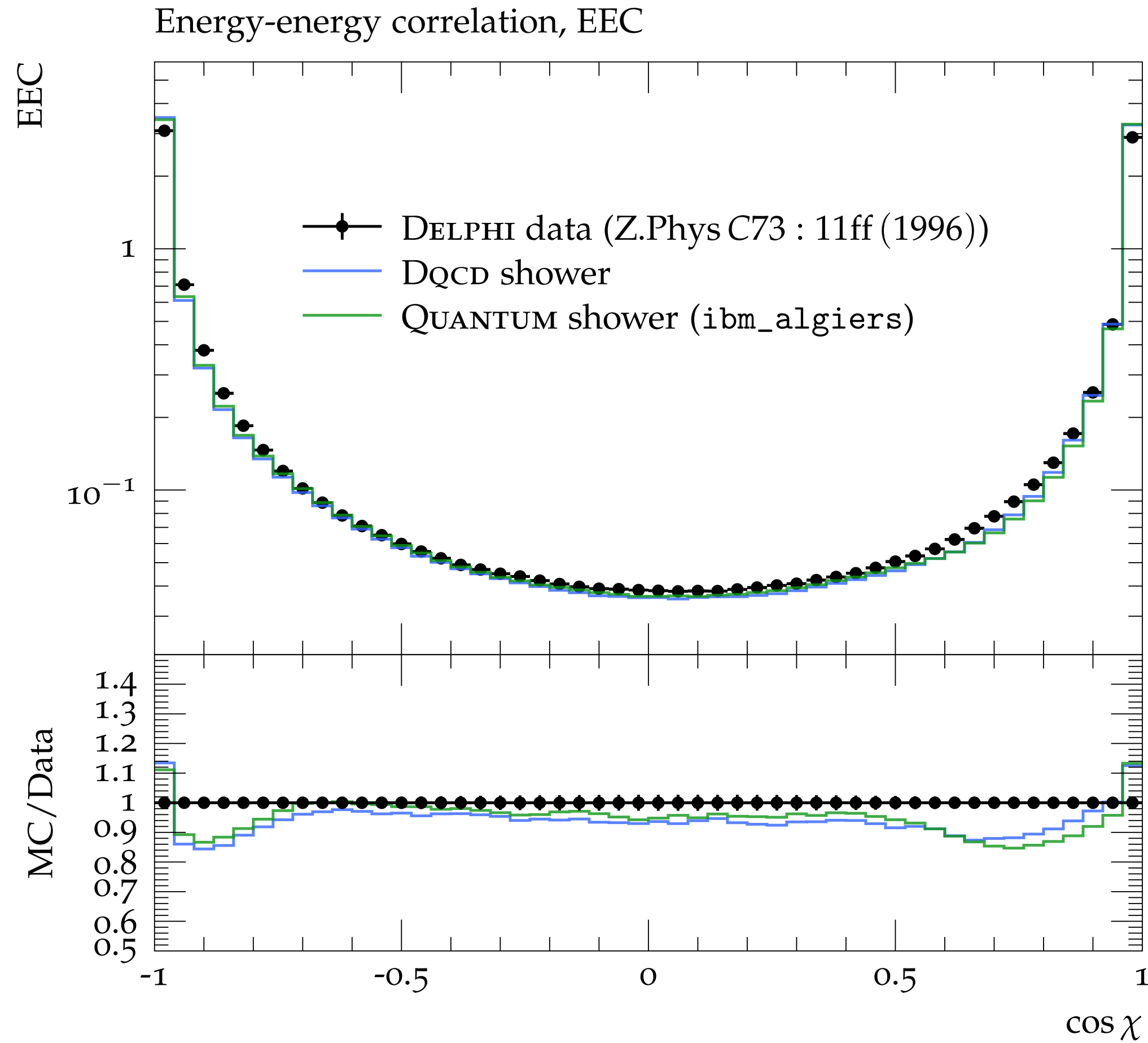
Work is ongoing to prove this is true for all QWs, but latest upper limits are on par with classical RW



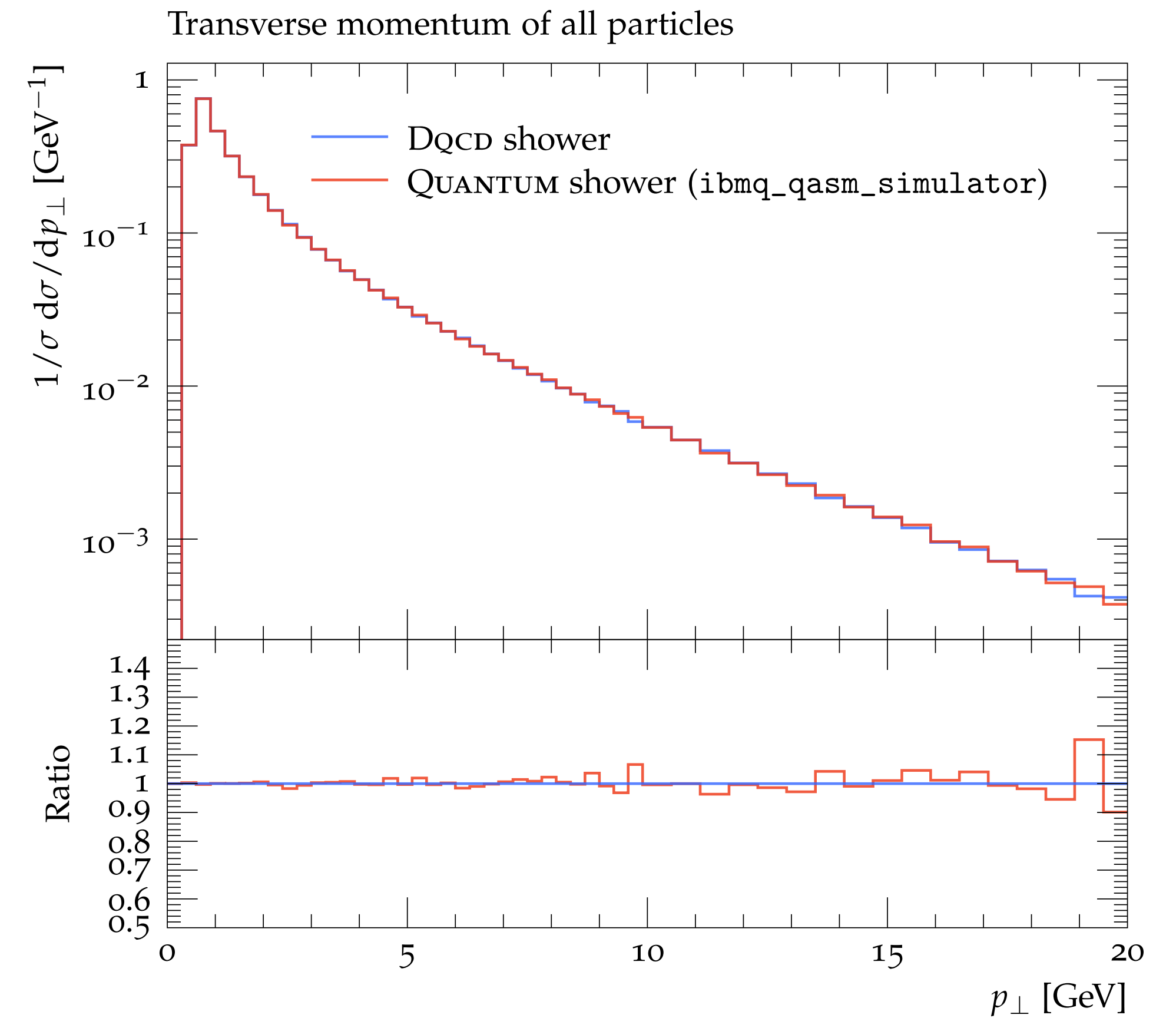
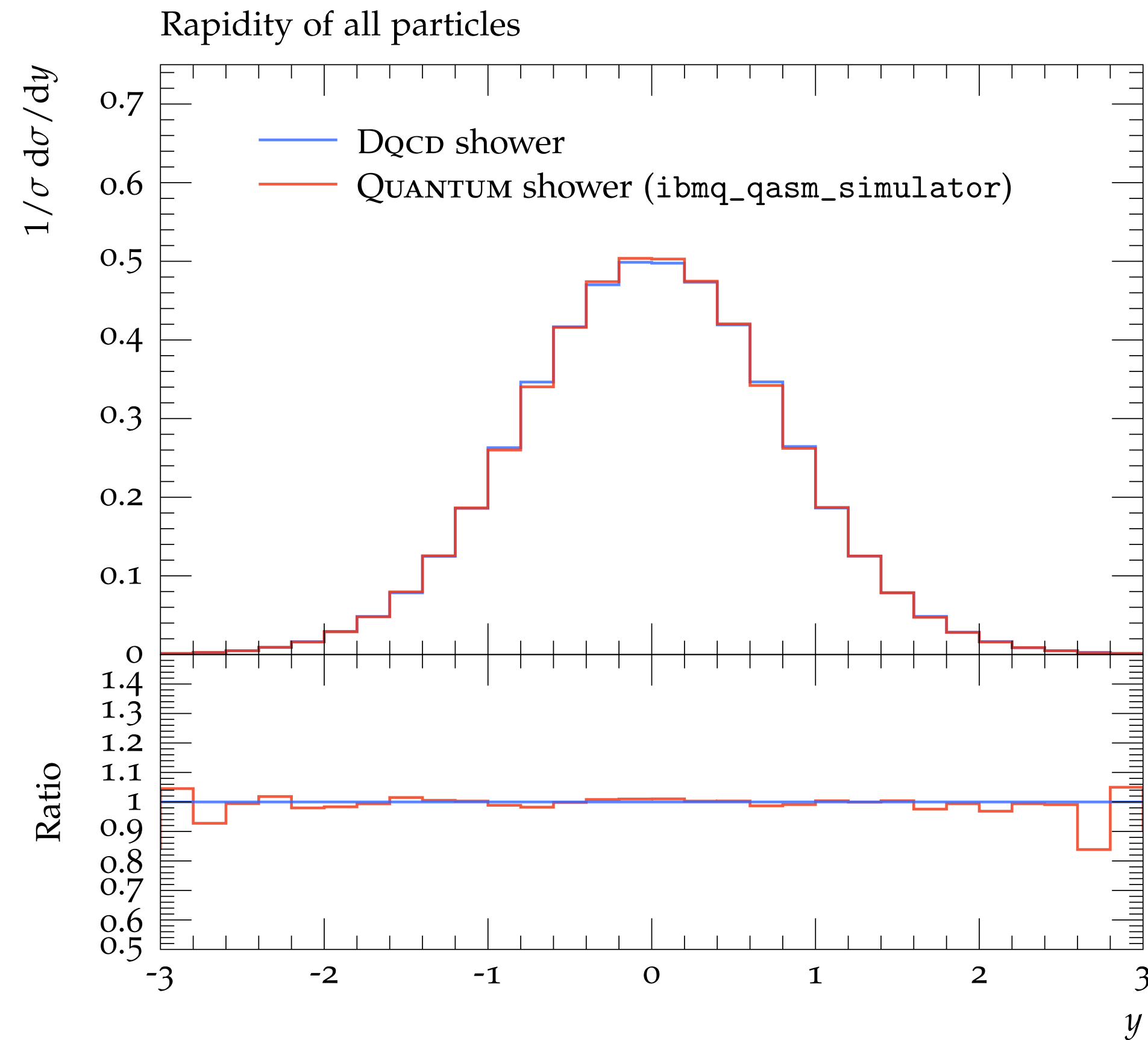
Collider Events on a Quantum Computer



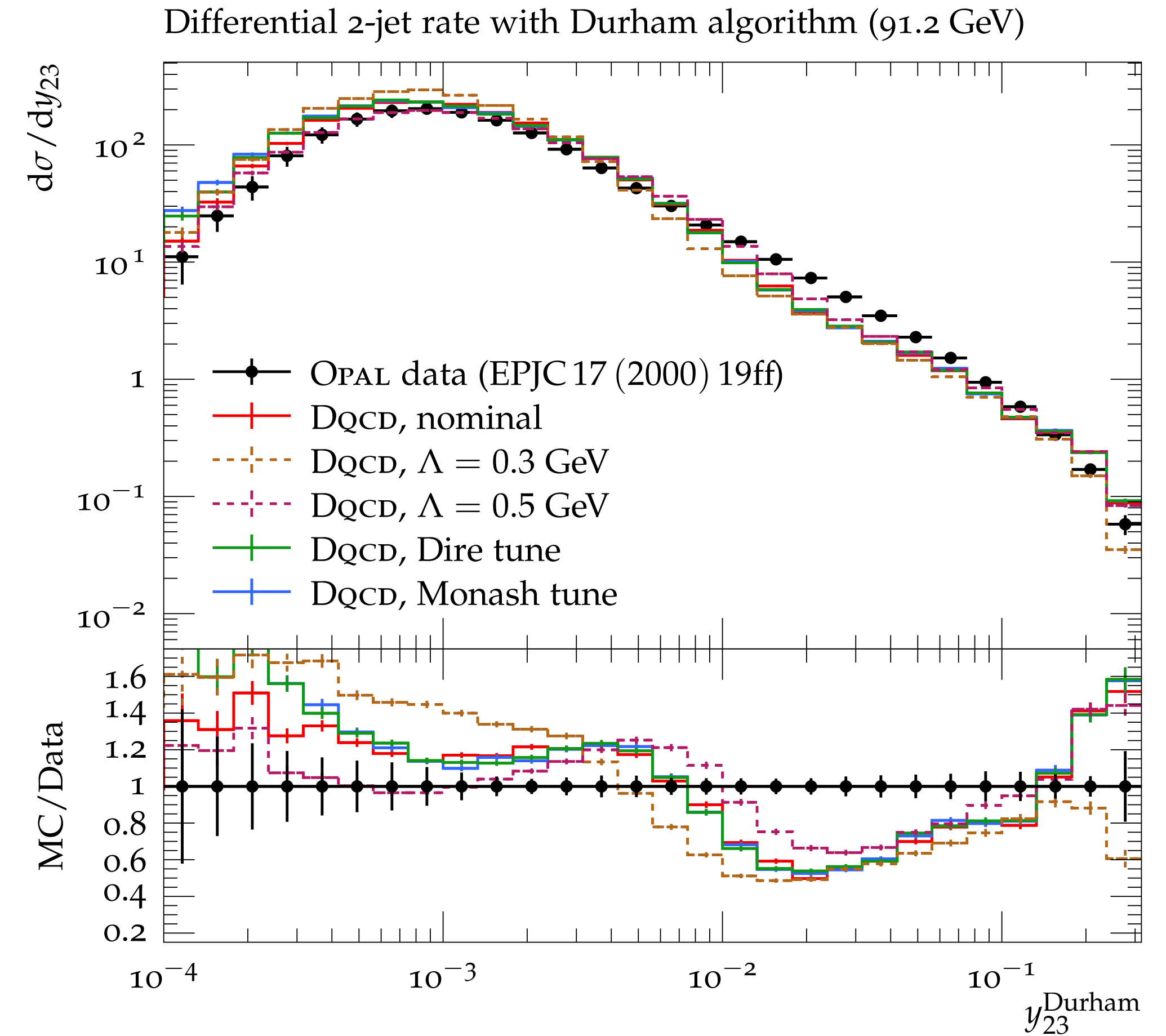
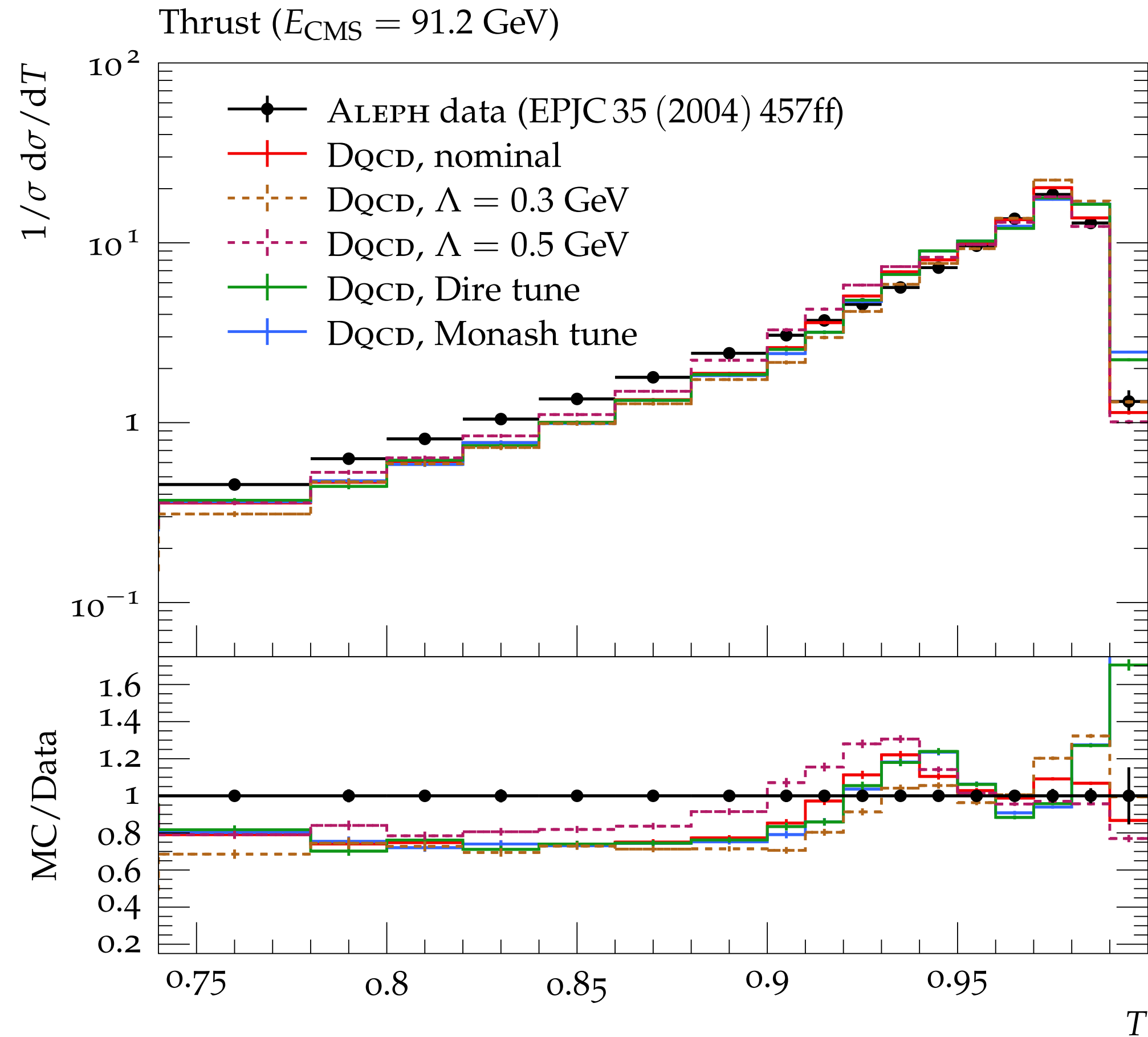
Collider Events on a Quantum Computer



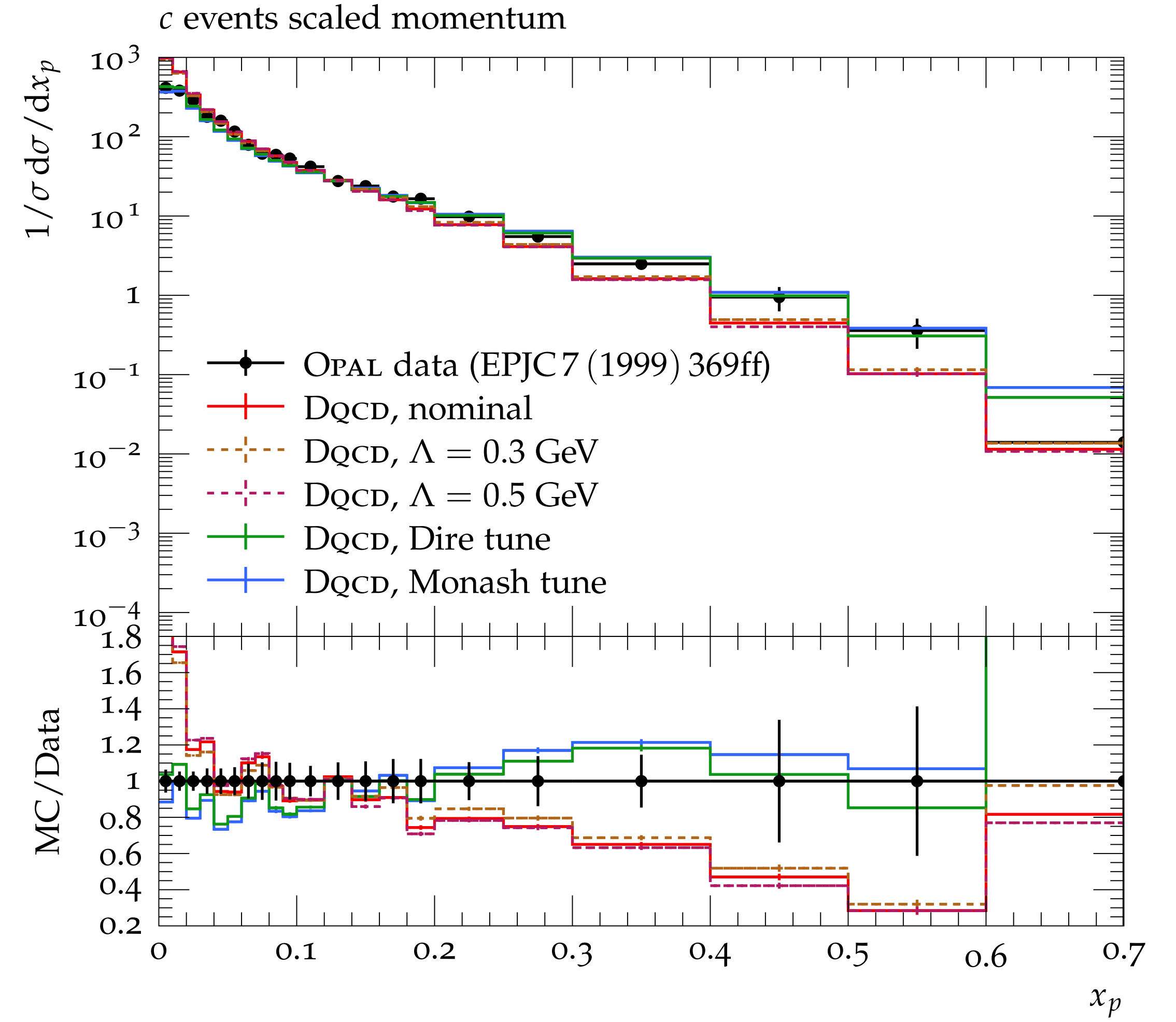
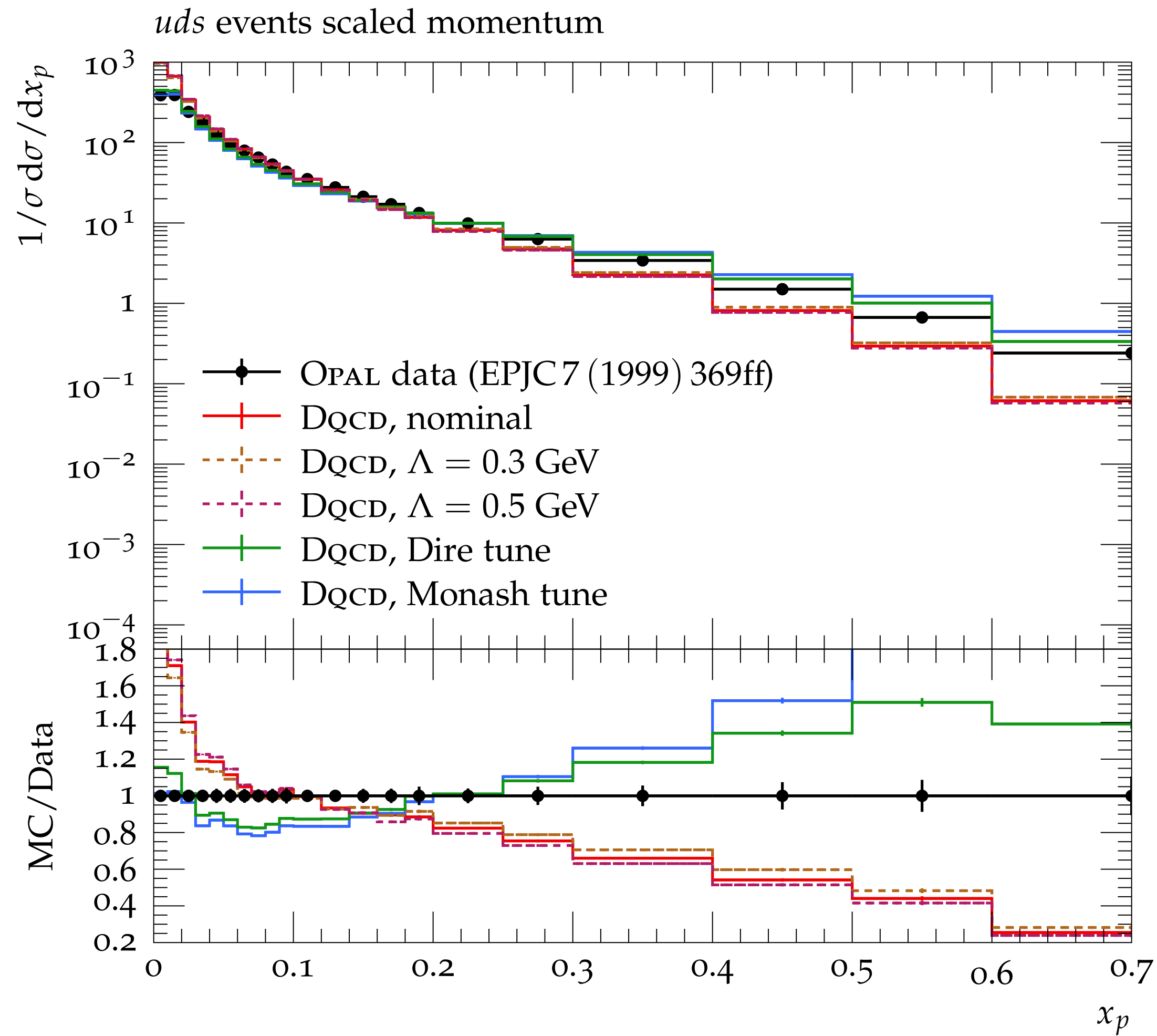
Collider Events on a Quantum Computer



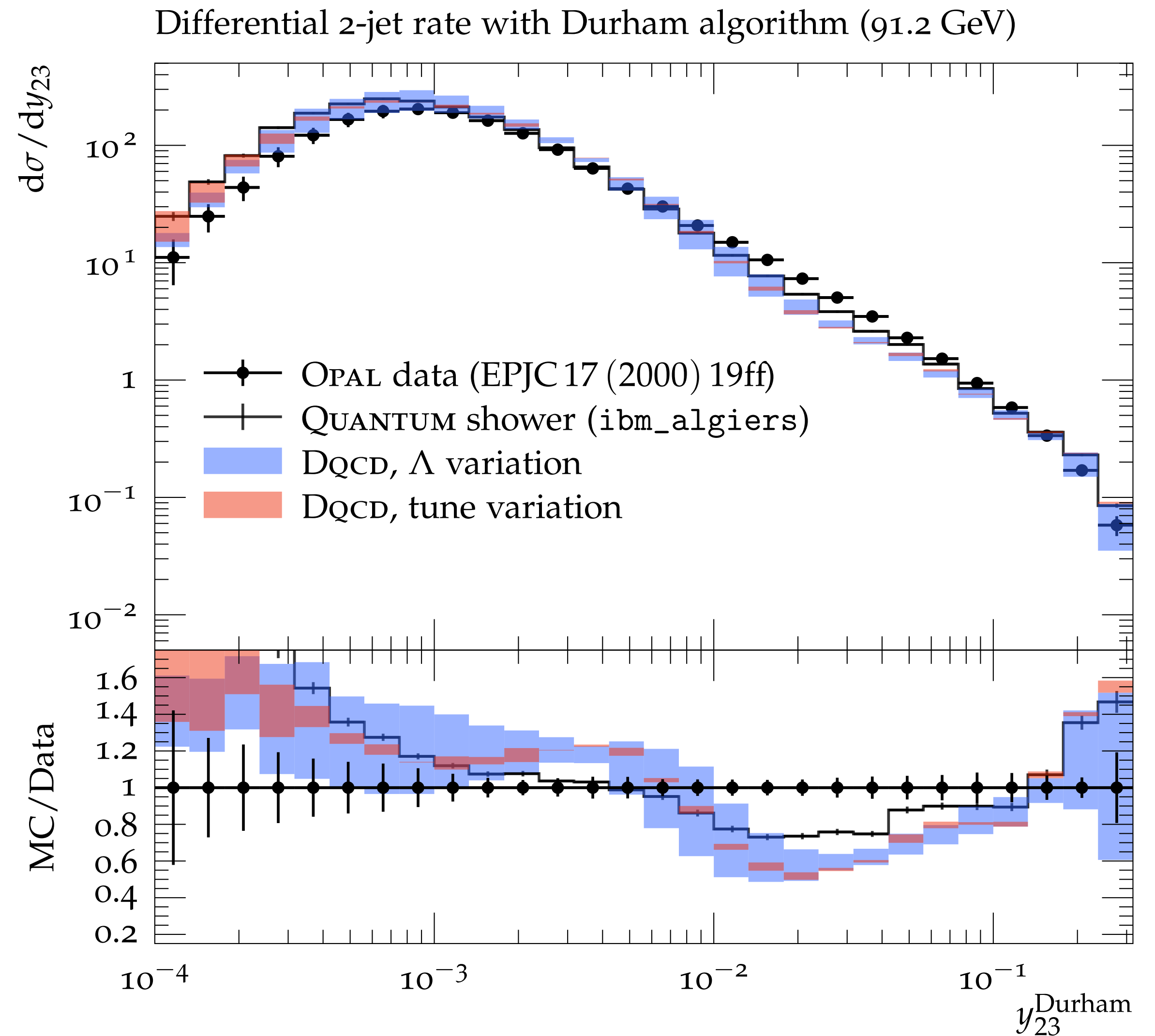
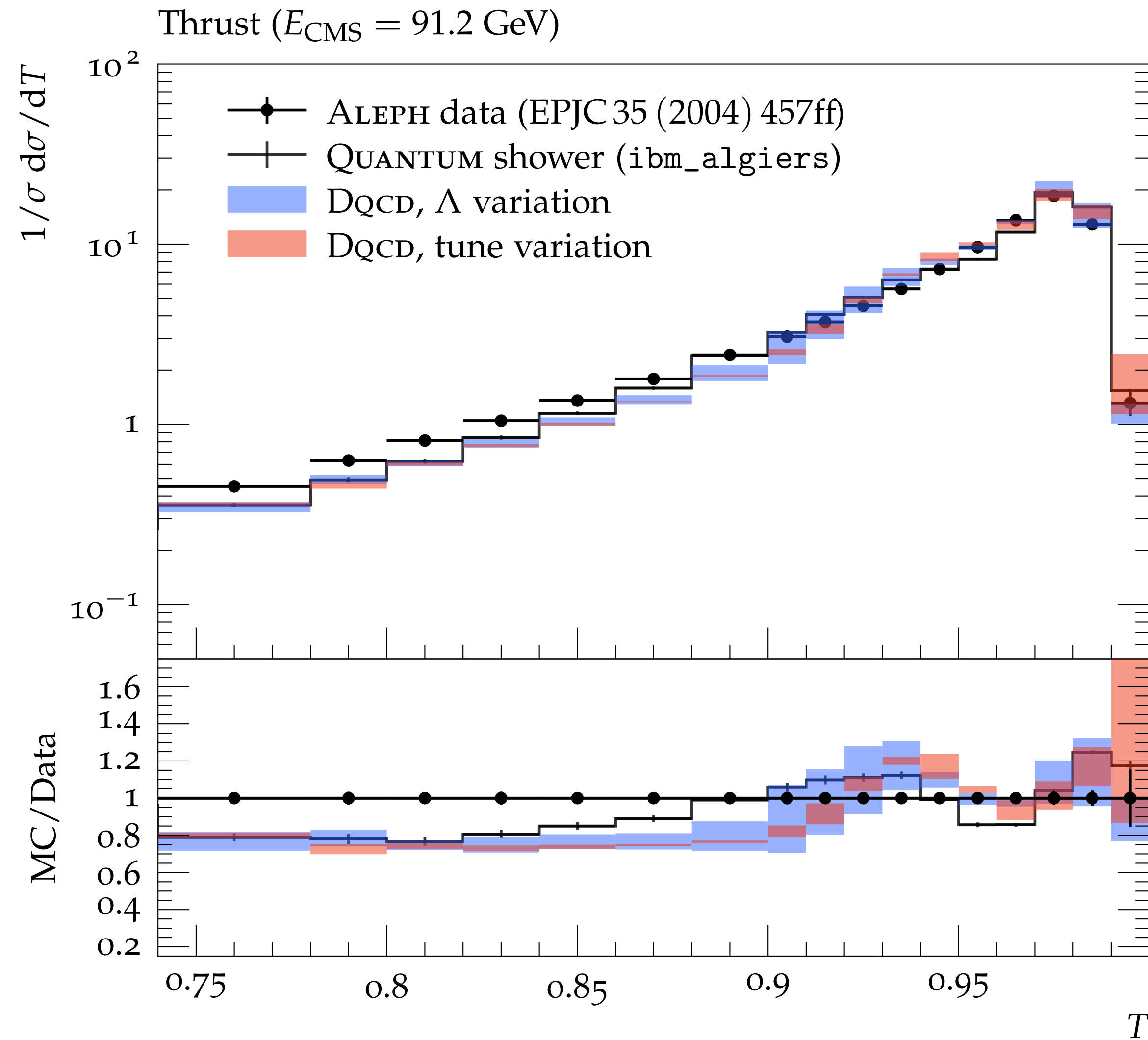
Collider Events on a Quantum Computer



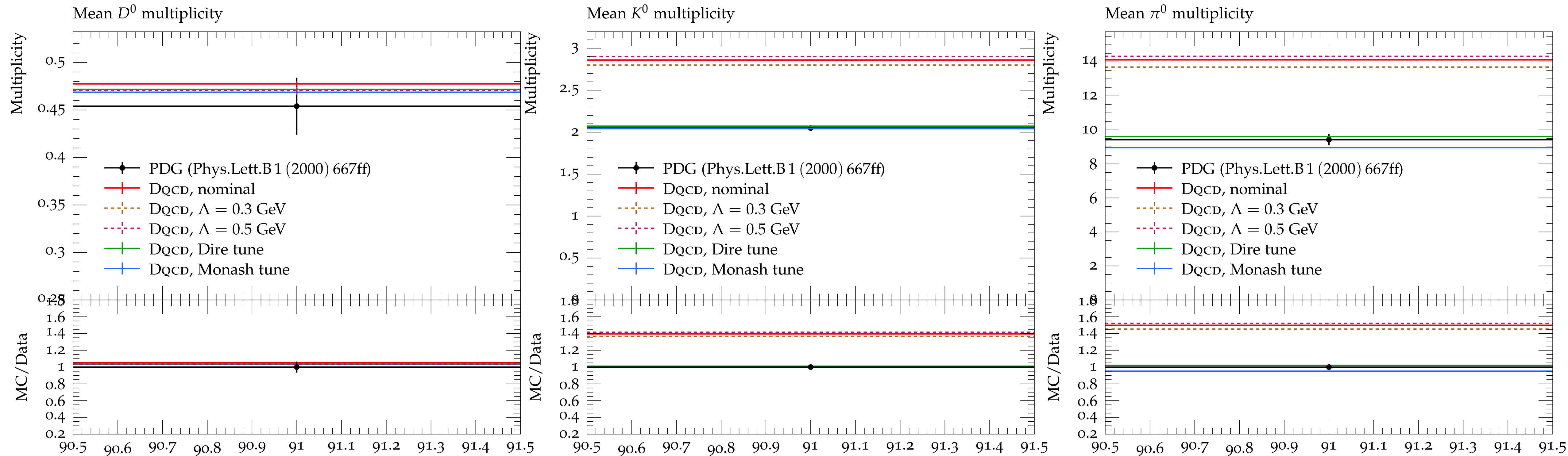
Collider Events on a Quantum Computer



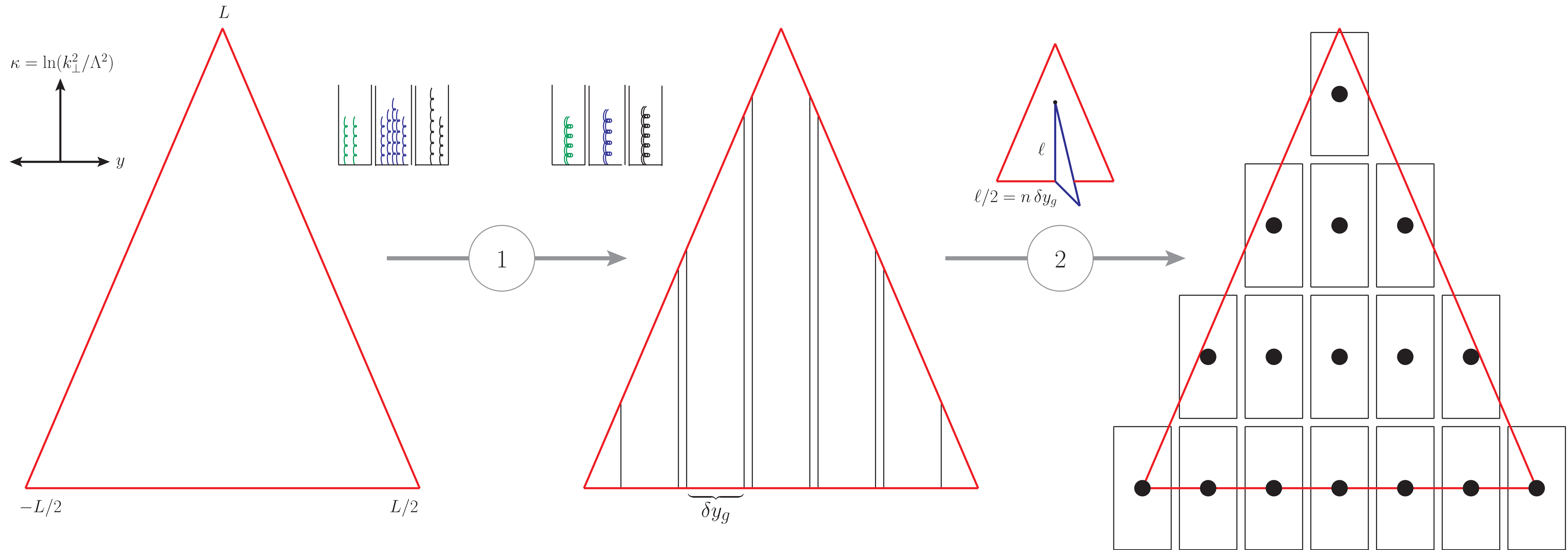
Collider Events on a Quantum Computer



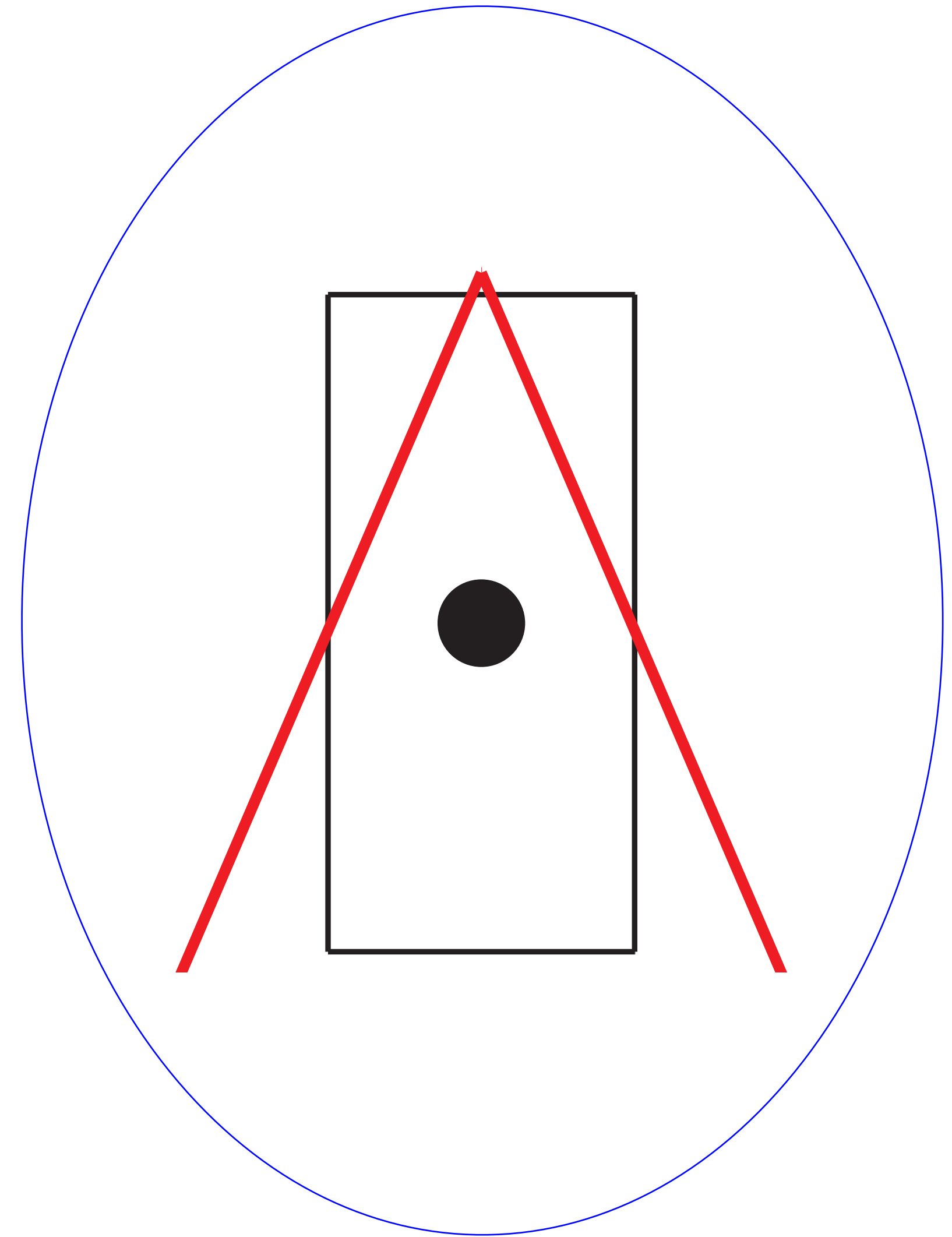
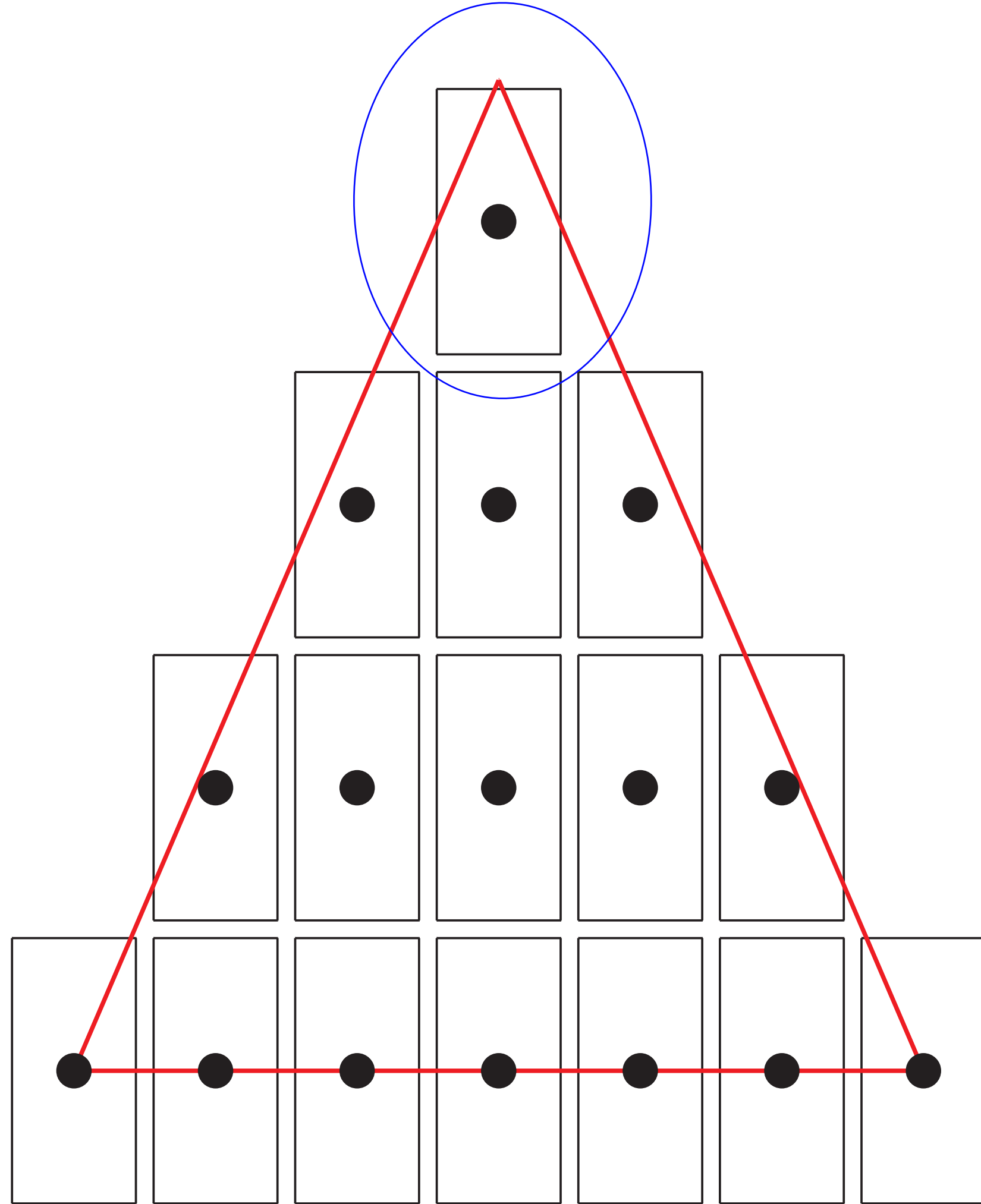
Collider Events on a Quantum Computer



Collider Events on a Quantum Computer



Collider Events on a Quantum Computer



Looking to the Future of Quantum Computers

