

# Towards a Data-driven Digital Twin of a Free Electron Laser



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# Hoffmann Lab: Helmholtz AI Young Investigator Group

## AI for Photon Science



[photon-ai-research.github.io](https://photon-ai-research.github.io)

### Digital twins of future laser-driven particle accelerators

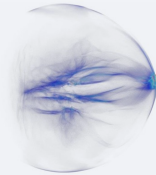
Surrogate modeling

ML-driven optimizer

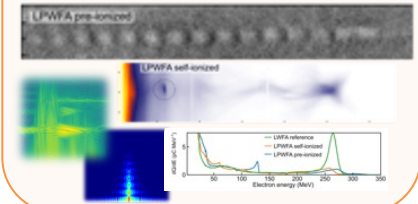
Inverse Problems

**Theory:**  
laser-plasma acceleration

$$\begin{aligned}\nabla \cdot \mathbf{D} &= \rho \\ \nabla \cdot \mathbf{B} &= 0 \\ \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{H} &= \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}\end{aligned}$$



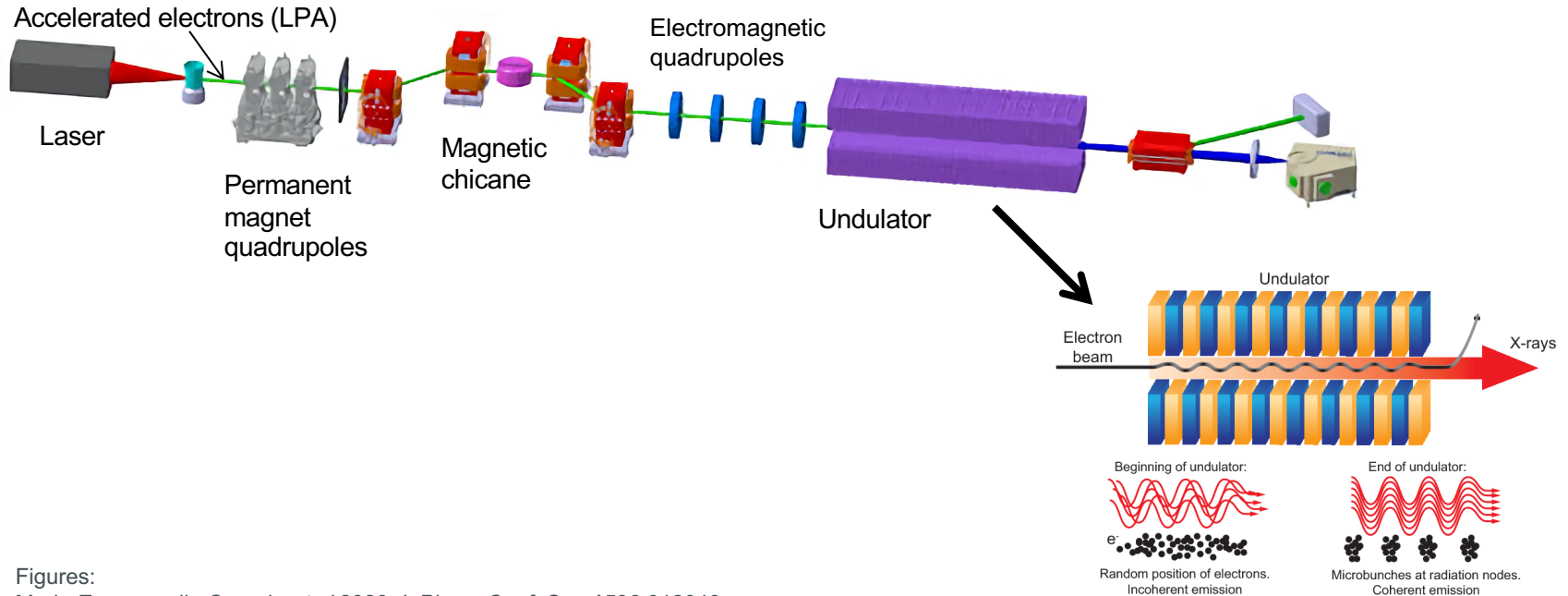
**Experimental Data**



Closing the loop between theory and experiment by researching data-driven digital twinning techniques

# Free Electron Laser

Source of directional coherent X-rays with a short bandwidth and a high photon pulse.



Figures:  
Marie-Emmanuelle Couprie *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012040  
Nilsson, D. (2013). *Zone Plates for Hard X-Ray Free-Electron Lasers*.

# Digital Twin of a Free Electron Laser

## Motivation

- Unveil correlation LPA-parameters to FEL radiation

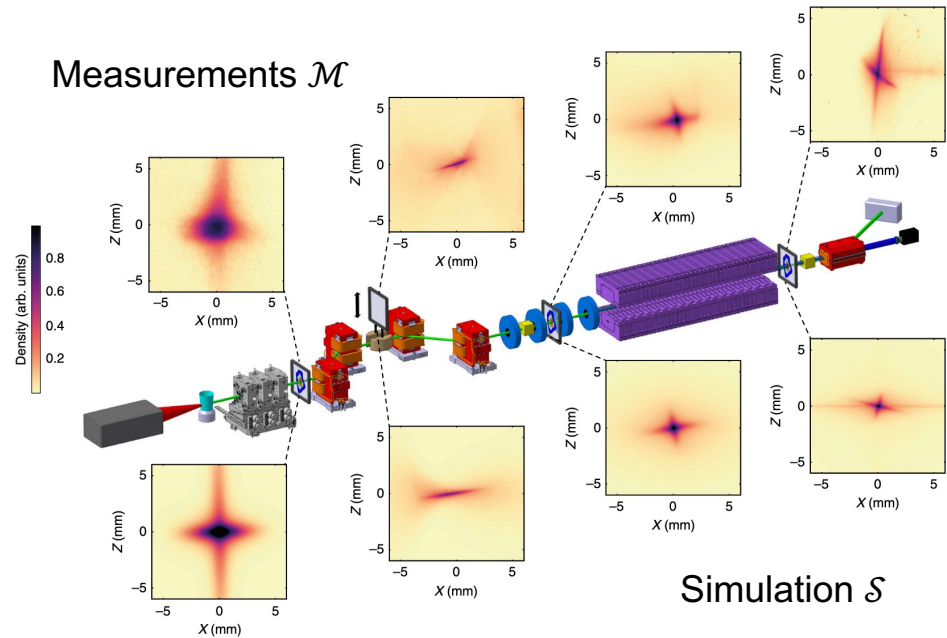


Figure:  
André, T., et al. "Control of laser plasma accelerated electrons for light sources."  
*Nature communications* 9.1 (2018): 1-11.

# Digital Twin of a Free Electron Laser

## Motivation

- Unveil correlation LPA-parameters to FEL radiation
- Fast and full inversion of the whole beamline from FEL radiation until LPA parameters

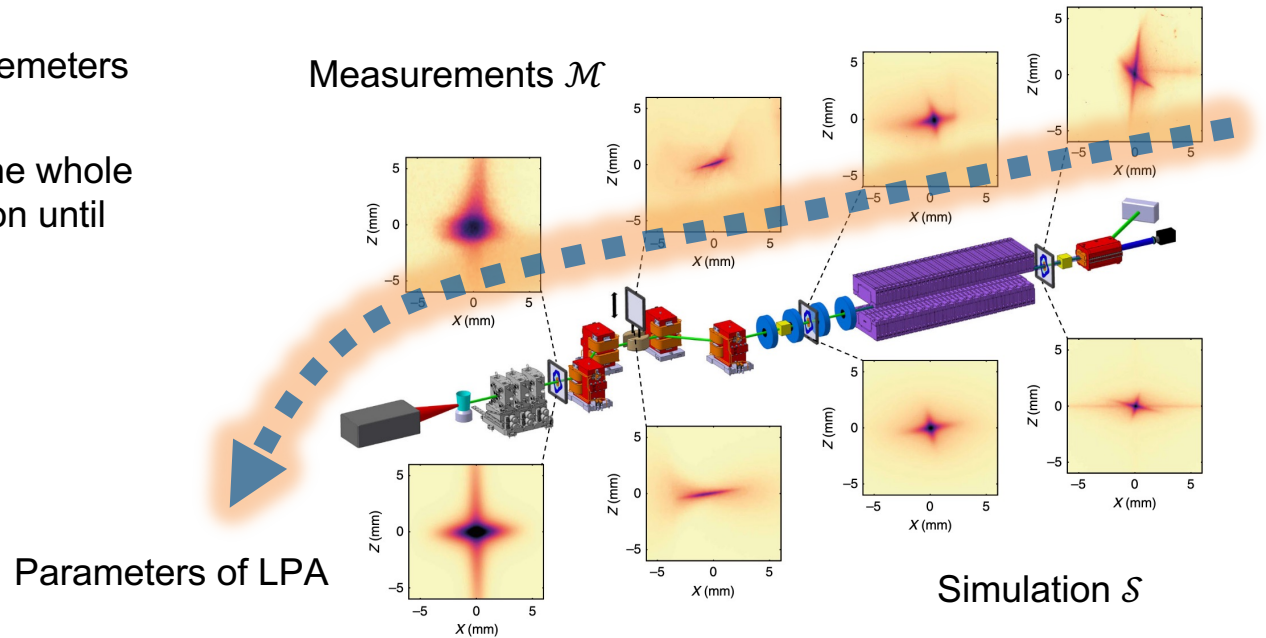


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# Digital Twin of a Free Electron Laser

## Inverse Problem

Surrogate Modeling

ML-driven optimizer

Inverse Problem

**Inverse problem**  
extract the simulation parameters from  
diagnostic measurements

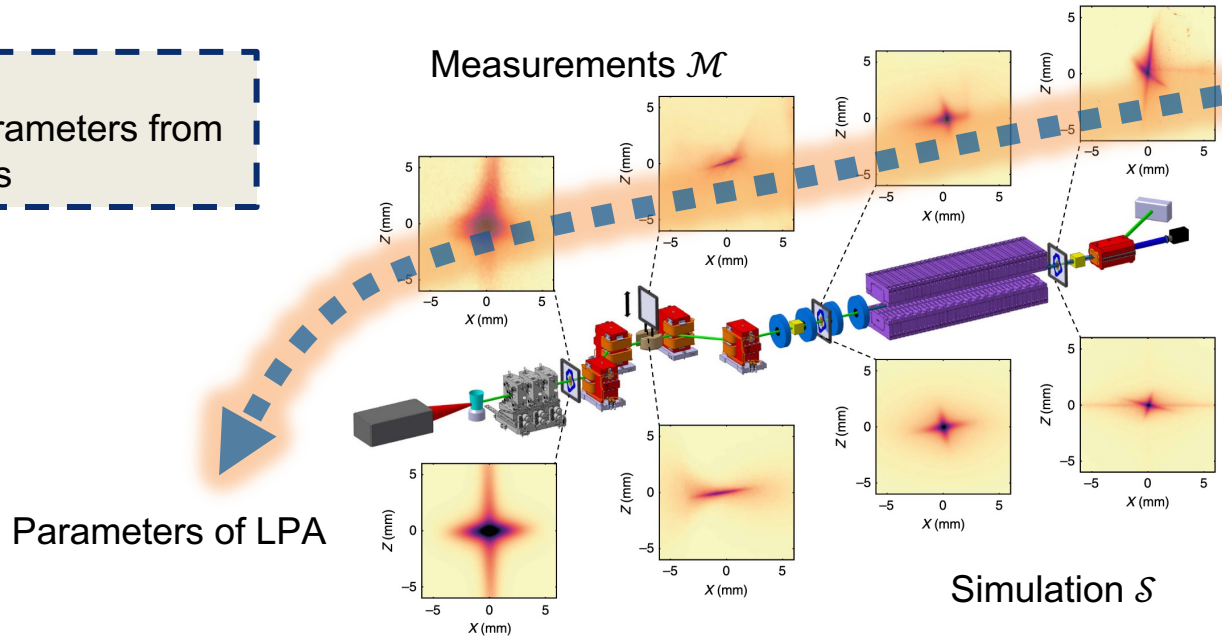


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# Digital Twin of a Free Electron Laser

## Inverse Problem

Surrogate Modeling

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Inverse Problem

### Inverse problem

extract the simulation parameters from diagnostic measurements

$$\mathbf{p}_{LPA}^* = \operatorname{argmin}_{\mathbf{p}_{LPA}} \operatorname{dist}(\mathcal{M}, \mathcal{S}(\mathbf{p}_{LPA}))$$

Parameters of LPA

$\mathbf{p}_{LPA}^*$

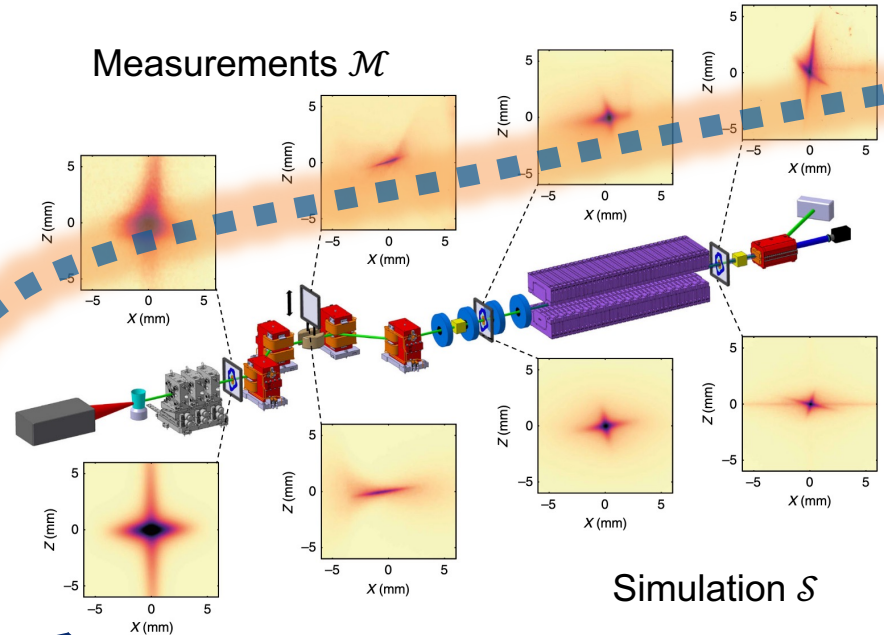


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*Nature communications* 9.1 (2018): 1-11.

# Solution to Inverse Problem

## Optimizer

Surrogate modeling

ML-driven optimizer

Inverse Problem

Optimization problem:

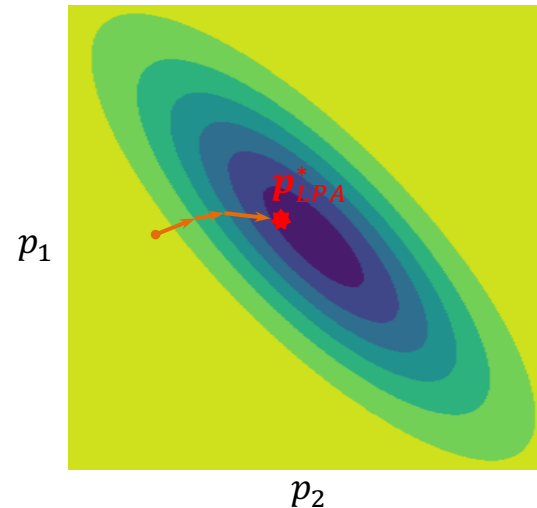
$$\mathbf{p}_{LPA}^* = \operatorname{argmin}_{\mathbf{p}_{LPA}} \operatorname{dist}(\mathcal{M}, \mathcal{S}(\mathbf{p}_{LPA}))$$

Each step of optimizer requires computation of  $\mathcal{S}(\mathbf{p}_{LPA})$



ML-based Surrogate Model  $\tilde{\mathcal{S}}$   
for fast forward pass

Gradient Descend





# Surrogate Modeling

Surrogate modeling

ML-driven optimizer

Inverse Problem

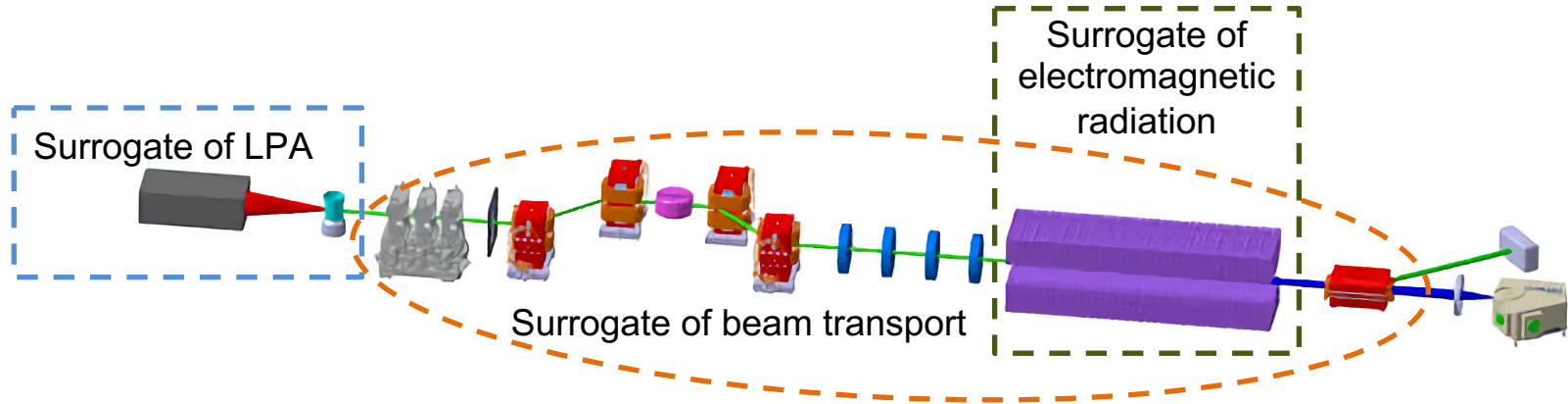


Figure:  
Marie-Emmanuelle Couprie *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012040

# Surrogate Modeling

Surrogate modeling

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Inverse Problem

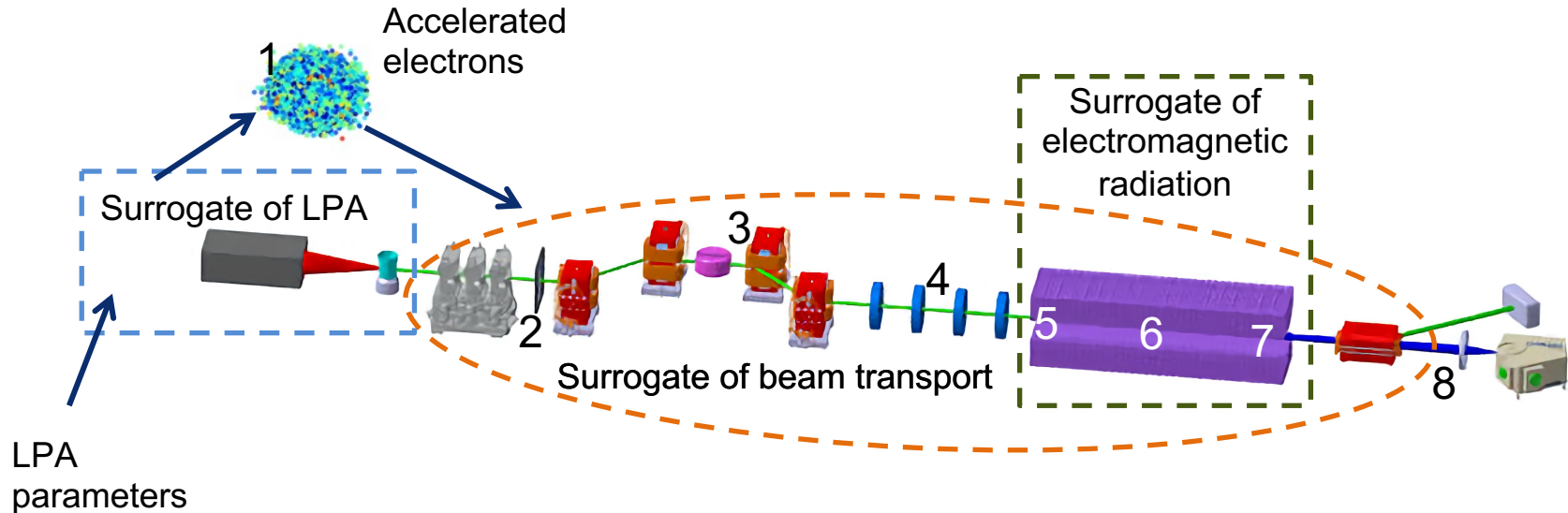


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Marie-Emmanuelle Couprie *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012040

# Surrogate Model of Electron Beam Transport

Surrogate modeling

ML-driven optimizer

Inverse Problem

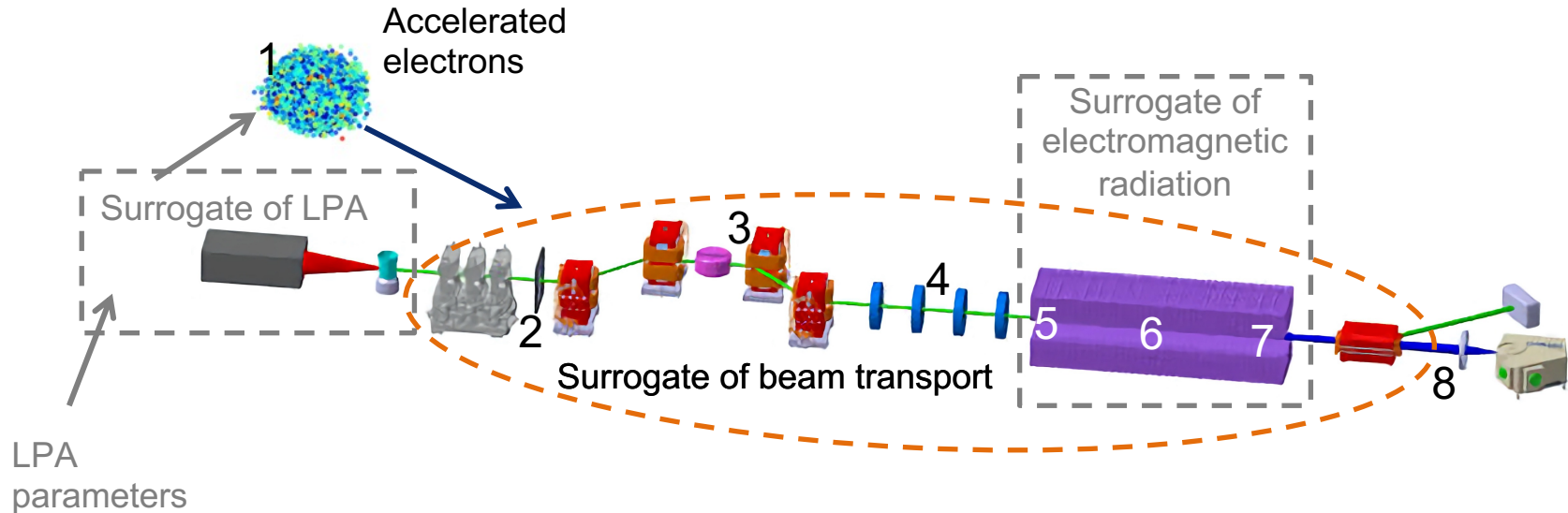


Figure:  
Marie-Emmanuelle Couprie *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012040

# Surrogate Model of Electron Beam Transport

## Given:

parameters of accelerated electron beam after LPA – emittance and beta

## Approximate:

phase space representation of electron beam at defined positions in the transport line

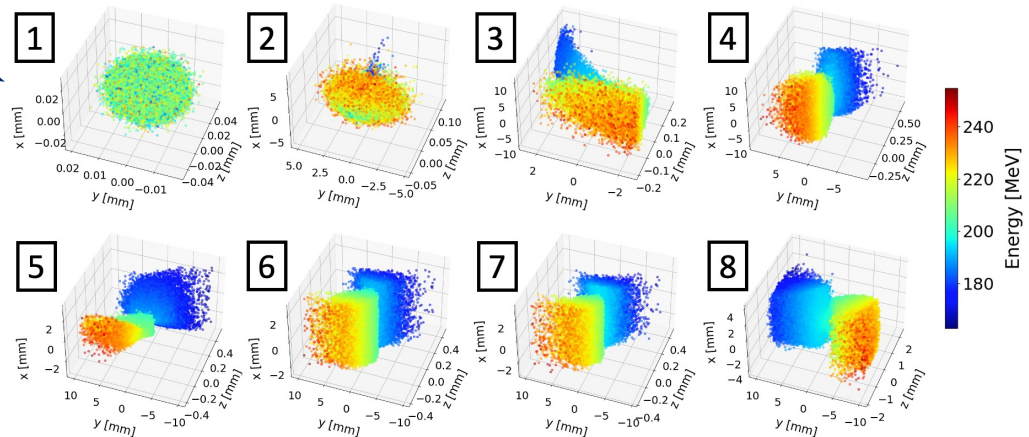
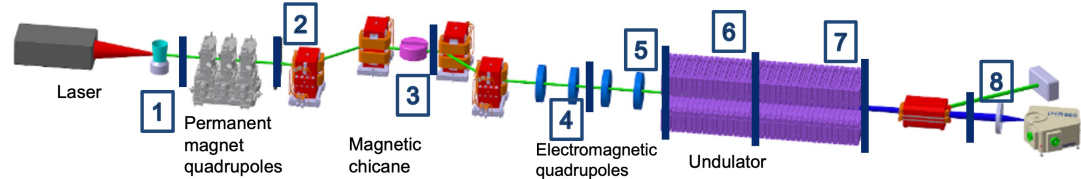
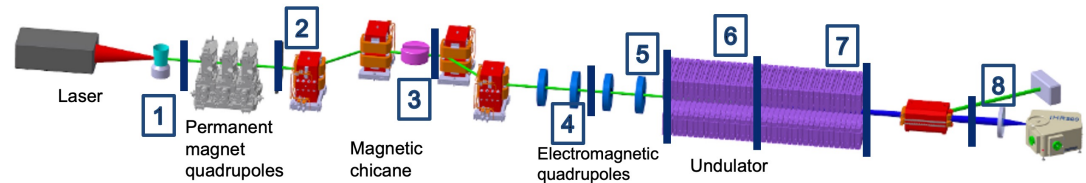


Figure:

Marie-Emmanuelle Couprie *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012040

# Surrogate Model of Electron Beam Transport



## Challenge

- Tracking of each particle is not required
  - Electron cloud is given by a distribution of electrons
- => Flexible sampling from any electron cloud

Phase space representation is processed as point cloud

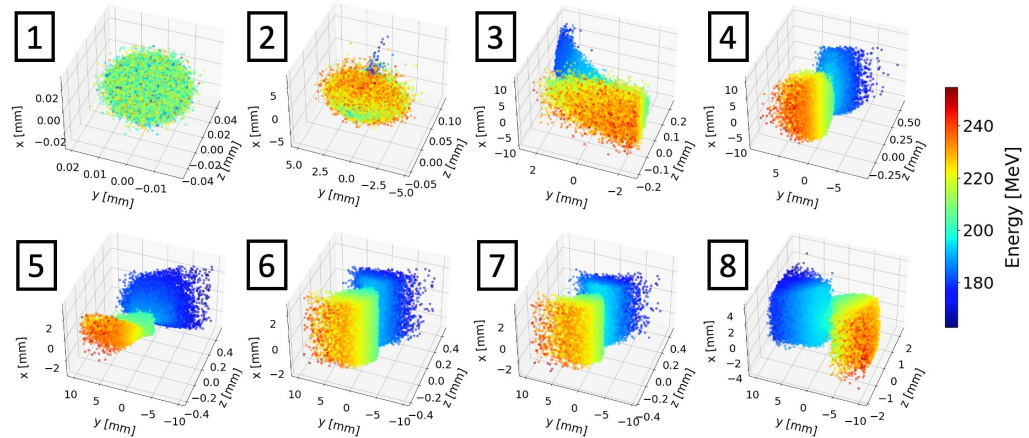


Figure:

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# Surrogate Model of Electron Beam Transport

## Generative Model: Normalizing Flows

### Goal

Take samples from **a normal distribution** and transform them into **distribution of electrons**

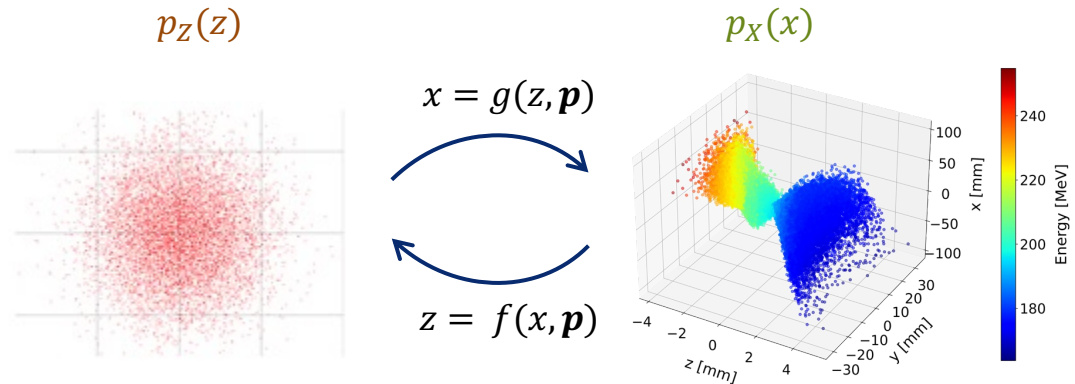
### Approach

$f$  is **invertible neural network**

$g = f^{-1}$  is differentiable

Change of variable formula

$$p_X(x) = p_Z(f(x)) \left| \det \frac{\partial f(x)}{\partial x^T} \right|$$

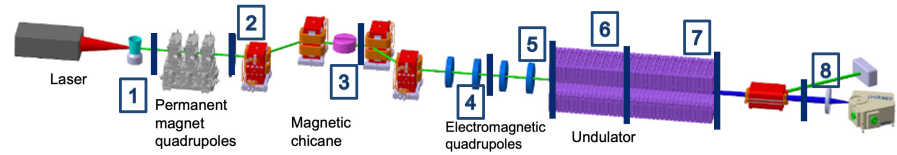
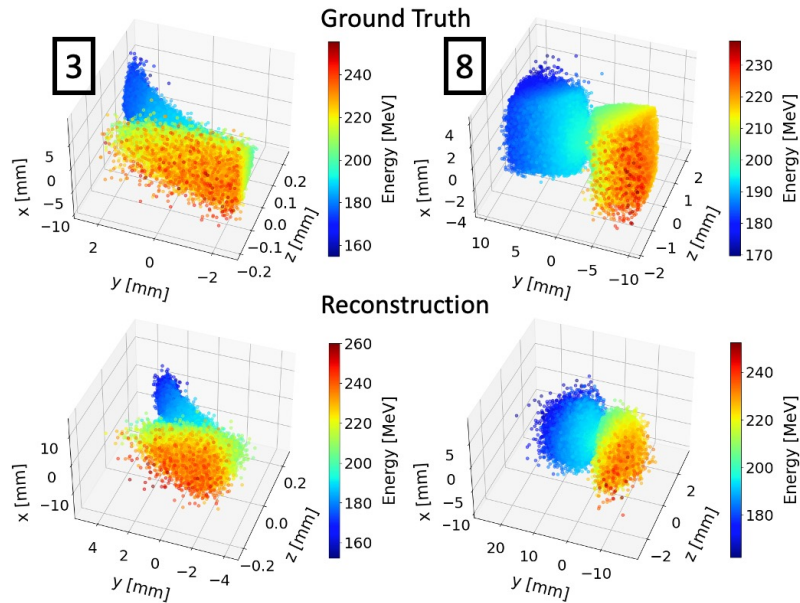


$p$  – parameters of an initial electron bunch

Ardizzone, Lynton, et al. "Guided image generation with conditional invertible neural networks." *arXiv preprint arXiv:1907.02392* (2019).

# Surrogate Model of Electron Beam Transport

## Results: Testing Data



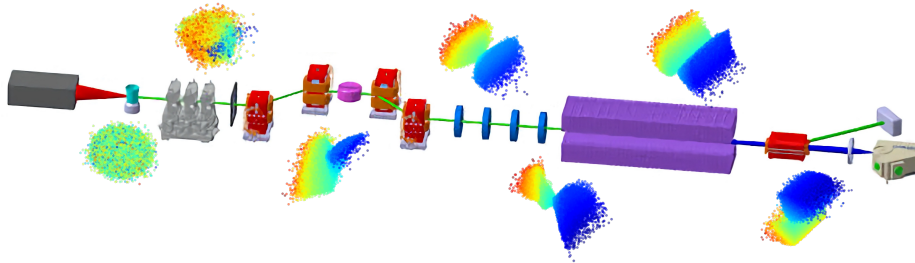
- Model is able to recognize different screens and reconstruct a shape of distribution
- Flexible inference w.r.t. number of electrons
- Easy to adjust to another setting of a beamline (only new training data required)

Figure:  
Marie-Emmanuelle Couprie *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012040

# Summary

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Digital Twin is foundation for autonomous operation/tuning of accelerators and beamlines



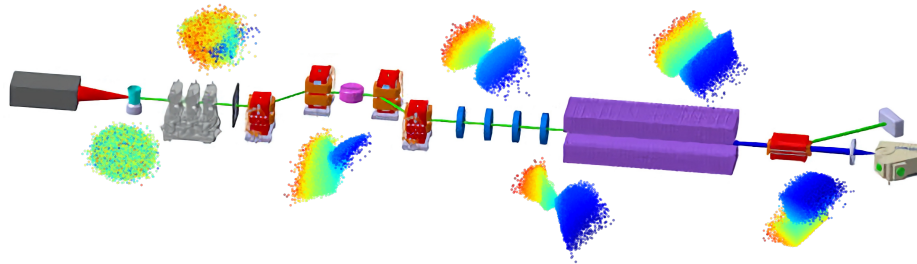
Surrogate model is able to produce electron clouds along a beamline



# Summary

Digital Twin is foundation for autonomous operation/tuning of accelerators and beamlines

Surrogate modeling    ML-driven optimizer    Inverse Problems



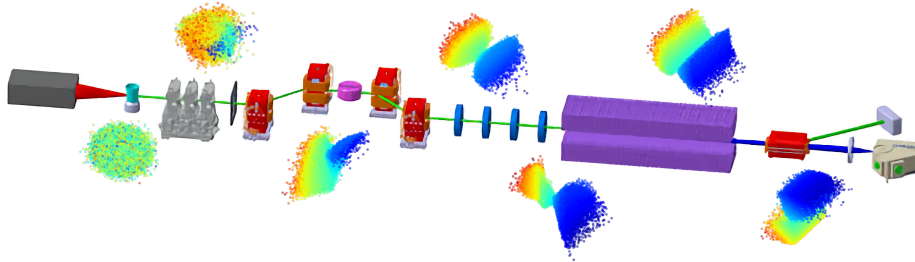
Surrogate model is able to produce electron clouds along a beamline

Electron clouds can be mapped to experimental data by integration of another surrogate models and an optimizer

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Digital Twin is foundation for autonomous operation/tuning of accelerators and beamlines

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Surrogate model is able to produce electron clouds along a beamline

Electron clouds can be mapped to experimental data by integration of another surrogate models and an optimizer

Simple development of further surrogate models based on normalizing flows to solve inverse problems:

library NF4IP

<https://github.com/Photon-AI-Research/NF4IP>

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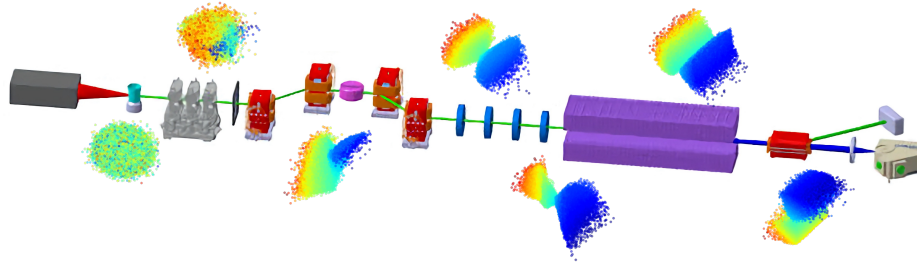
*Thank you for your attention!*

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