A kT-dependent sea-quark distribution for CASCADE

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Based on results obtained with F. Hautmann and H. Jung

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- particularly suitable for dynamics at small \boldsymbol{x}
- provides unintegrated gluon density $\mathcal{A}(x,k_t,\mu^2)$
 - $\ + \$ CCFM parametrization of valence quark distribution
- but no sea quark distribution

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Process of interest at LHC: forward Drell-Yan production (\gamma^*,\,Z,\,W)
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- couples by seaquark to gluon density
- probe proton at very small x, up to $3\cdot 10^{-6}$
- investigate small x dynamics: BFKL, saturation,



. . .

Forward DY production



- leading order: $q\bar{q} \rightarrow Z$
- quark q: valence quark of proton 1
- anti-quark \bar{q} : sea quark, couples to gluon evolution of proton 2
- CASCADE with unintegrated gluon: sea quark by $qg^* \rightarrow Zq$ [Ball, Marzani, '09]
- collinear divergence: inclusive Z requires cut-off or finite quark mass



Collinear factorization (DGLAP):

- coll. divergency \equiv non-perturbative contributions to partonic process
- universal: factorize and subtract into seaquark distribution

Goal of this study: do the same, but within the context of CCFM:

universal unintegrated sea quark density

gluon splitting: CCFM versus DGLAP versus BFKL



- **DGLAP:** emssion ordered in k_T , evolution in transverse scale Q^2
- splitting function:

$$P_{gg}(z) = 2C_A \left[\frac{1-z}{z} + \frac{z}{1-z} + z(1-z) \right]$$

- k_T of gluon neglected against collinear component xp
- integrated gluon distribution $g(x,\mu)$
- no k_T dependence for partonic cross-section $gq \rightarrow Zq$

gluon splitting: CCFM versus DGLAP versus BFKL



- BFKL: reggeized gluon formalism, emission ordered in longitudinal momenta
- k_T dependent splitting kernel

$$\frac{1}{(\boldsymbol{q}-\boldsymbol{k})^2}\frac{1}{x}x^{-\bar{\alpha}_s\ln(\boldsymbol{q}^2/\lambda^2)}$$

- keep k_T dependence for partonic cross-section and unintegrated gluon density $\mathcal{F}(x,\mu^2,k^2)$
- neglect 'small' against 'large' longitudinal momenta; for DGLAP: $z \to 0$, miss $z \to 1$ region and finite terms

reggeized gluon formalism \rightarrow effective couplings \rightarrow gauge invariant off-shell continuation ($k^2 \neq 0$) of collinear partonic cross-section $\hat{\sigma}(k_T)$

• Higher accuracy in kinematics: LO k_T catches important $N^m LO$ collinear effects in small x region

gluon splitting: CCFM versus DGLAP versus BFKL



- **CCFM** : based on color coherence \rightarrow angular ordered emssion
- splitting kernel contains both enhanced parats ($z \rightarrow 0, 1)$ of DGLAP splitting
- small x: for inclusives observables (allow for $z \rightarrow 0$) \equiv BFKL $\Rightarrow k_T$ dependence!
- $z \rightarrow 1$ region treated correclty \rightarrow essential for exclusive events (Monte-Carlo!), correct DGLAP limit
- defines (as BFKL) unintegrated gluon density $\mathcal{A}(x, \pmb{k}^2, \bar{q})$

 $\hat{\sigma}(k_T)$ defined as for BFKL (effective reggeized gluon couplings)

- $\bullet\,$ no longer restricted to very small x
- take care: collinear and soft divergencies!

Factorization of collinear divergency: quark-gluon splitting



• DGLAP: contains naturally splitting function $P_{qg}(z) = Tr(z^2 + (1-z)^2)$

• no k_T dependence for seaquark distribution $q(x,\mu^2)=P_{qg}(z)\otimes g(x/z,\mu^2)$ and partonic cross-section $\sigma_{q\bar{q}\to Z}$

$$\hat{\sigma}_{q\bar{q}\to Z}(\nu=\hat{s}) = \underbrace{\sqrt{2}G_F M_Z^2(V_q^2 + A_q 2)}_{\text{Z-coupling}} \times \frac{\pi}{N_c} \delta(\nu - M_Z^2)$$

- reggeized quarks (analogy to BFKL): arises in the limit of high center of mass energies of the $qg^* \rightarrow Zq$ process
- gauge invariant definition of q_T dependent partonic process $q\bar{q}^* \rightarrow Z$ (with off-shell quark!)

$$\hat{\sigma}_{q\bar{q}^* \to Z}(\nu, \boldsymbol{q}^2) = \underbrace{\sqrt{2}G_F M_Z^2(V_q^2 + A_q 2)}_{N_c} \times \frac{\pi}{N_c} \delta(\nu - M_Z^2 - \boldsymbol{q}^2)$$

• splitting: $z \rightarrow 0$; correct for strict h.e. limit

kT-dep. quark-gluon splitting function

 $[\mathsf{Catani},\,\mathsf{Hautmann}\,\,'94\,]$: high energy resummation within collinear factorization

$$P_{qg}\left(z,\frac{k^{2}}{q^{2}}\right) = T_{R}\left(\frac{q^{2}}{q^{2}+z(1-z)k^{2}}\right)^{2} \left[P_{qg}(z) + 4z^{2}(1-z)^{2}\frac{k^{2}}{q^{2}}\right]$$

- $k^2 \rightarrow 0$: DGLAP splitting, $z \rightarrow 0$: reggeized quark splitting
- k_T -dependent splitting function is universal \rightarrow can use it to define q_T dependent sea-quark density

$$\mathcal{A}^{\text{seaquark}}(x, \boldsymbol{q}^2, \mu^2) := \int_x^1 dz \int_0^{\boldsymbol{q}^2/z} \frac{d\boldsymbol{k}^2}{q^2} P_{qg}\left(z, \frac{\boldsymbol{k}^2}{q^2}\right) \mathcal{A}_{\text{CCFM}}^{\text{gluon}}(x/z, \boldsymbol{k}^2, \boldsymbol{q}^2/z)$$

 $zx. \mathbf{q}$

Forward DY



Catani-Hautmann: exact k_T -dependence of gluon, integrate over $q^2 \longrightarrow$ no q_T -dependence for $\hat{\sigma}$

here: keep explicit $q_T\text{-dependence}$ for partonic proces $q\bar{q}^* \to Z$

 \rightarrow more accurate kinematics : p_T of Z ...

analyze $qg^* \rightarrow Zq$ (in k_T -fact.) [Ball, Marzani, '09]; find

$$\hat{\sigma}_{qg^* \to Zq}(\nu, \boldsymbol{k}^2) = \int_x^1 \frac{dz}{z} \int \frac{d\boldsymbol{q}^2}{\boldsymbol{q}^2} \hat{\sigma}_{q\bar{q}^* \to Z} P_{qg}(z, \frac{\boldsymbol{k}^2}{\boldsymbol{q}^2}) + \text{remainder}$$

- remainder subleading in high energy $(\hat{s}_{qg^*} \rightarrow \infty)$ and collinear limit
- $\hat{\sigma}_{q\bar{q}^*\to Z}$ agrees with the reggeized quark result, but difference in delta-function of $\hat{\sigma}_{q\bar{q}^*\to Z}$

$$\delta(
u - M_Z^2 - \boldsymbol{q}^2) \leftrightarrow \delta(
u - M_Z^2 - \frac{\boldsymbol{q}^2}{1 - z} - z\boldsymbol{k}^2)$$

• in general: more accurate but not exact kinematics, here: can absorb by redefinition of q_T

Extension: central DY



- $g^*g^* \to q\bar{q}Z$ by [Deak, Schwennsen, '08] and [Baranov, Lipatov, Zotov, '08]
- need massive quarks or cut-off for inclusive production: collinear singularity
- can factorize now with splitting function, requires $\hat{\sigma}_{q^*\bar{q}^*\to Z}$

• extraction from $\hat{\sigma}_{g^*g^* \rightarrow Zq\bar{q}}$ possible but difficult • reggeized quark formalism yields

$$\hat{\sigma}_{q^*\bar{q}^*\to Z}(\boldsymbol{q}_1, \boldsymbol{q}_2) = g_{q\bar{q}Z}^2 \frac{\pi}{N_c} \left[\frac{M_Z^2 + \boldsymbol{q}_1^2 + \boldsymbol{q}_2^2}{\nu} \right] \delta \left[\nu - M_Z^2 - (\boldsymbol{q}_1 + \boldsymbol{q}_2)^2 \right]$$

splitting function requires in addition angular averaging

Conclusion and outlook

- Defined q_T dependent seaquark density with correct collinear and high energy limit and correct h.e. resummed gluon-quark splitting
- Partonic cross-sections (off-shell continuation of collinear X-sec.)
 - (a) extraction from higher order calculation
 - (b) direct: reggeized quark formalism
- explicit: forward and central DY

NOW:

• Numerical implementation into CASCADE is in progress: acuracy of the approximation?

FUTURE:

- Analyze further splittings (gluon quark, quark quark)
- soft gluon resummation (?)
- Further process: forward jets