

# Azimuthal correlations in dijet events at NLO with the parton branching method

CPHI-2022

**Aron Mees van Kampen**

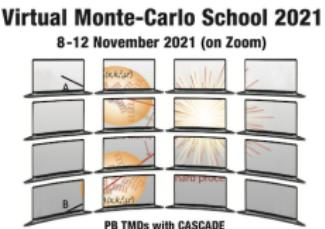
on behalf of  
the CASCADE developer team  
& participants of the Monte Carlo school: PB TMDs with CASCADE

University of Antwerp, Belgium

February 24, 2022



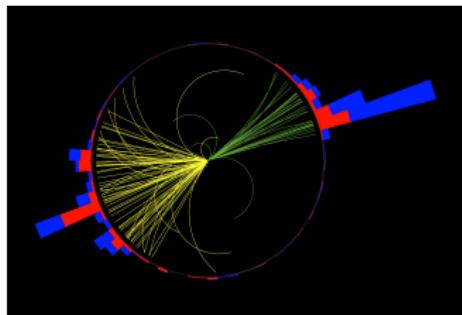
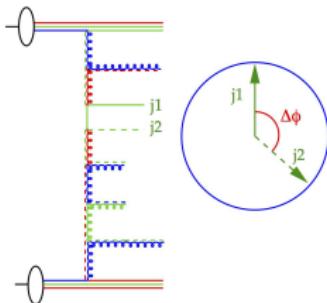
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# Introduction

Azimuthal correlation of dijets at the LHC:  $\Delta\phi_{12}$  Abdulhamid et al. [Eur.Phys.J.C 82 (2022) 1, 36]

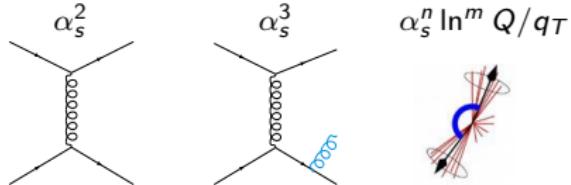
- PP collisions @13 TeV
- High  $p_T$  of leading jet(s):  $p_T^{\text{leading}} > 200 \text{ GeV}$
- fixed order calculation not sufficient



CMS figure of jets in back-to-back  $\Delta\phi$  region

Calculation of  $\Delta\phi_{12}$ :

- ① LO: only 2 jets ( $\Delta\phi = \pi$ )
- ② NLO: middle  $\Delta\phi$  region
- ③ Resummation approach ( $\Delta\phi \rightarrow \pi$ )



Resummation in CSS manner by Sun, Yuan, Yuan [Phys. Rev. D 92, 094007 (2015)]  
Possible factorization breaking effects towards  $\Delta\phi \rightarrow \pi$

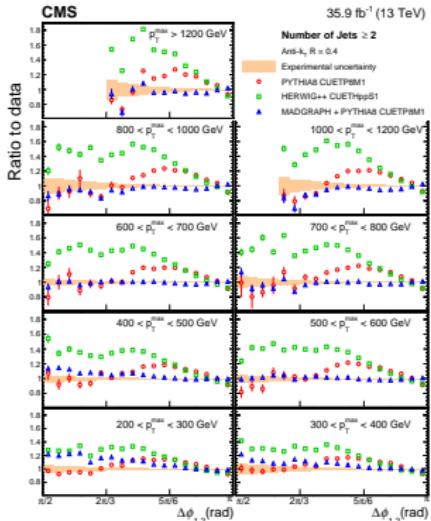
# $\Delta\phi_{12}$ with high $p_T$ dijets using Parton Branching

General purpose event generators results

Tunes needed!

Deviations up to 50% in medium  $\Delta\phi$   
& up to 10% in  $\Delta\phi \rightarrow \pi$  region

Experimental uncertainty smaller than  
theoretical deviations



CMS coll. [Eur. Phys. J. C 78 (2018) 566]

**Parton branching** formalism for TMD evolution very suitable!

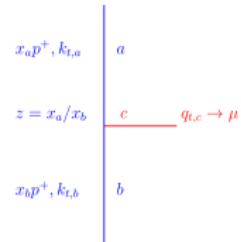
- Initial parton radiation: moves  $\delta(\Delta\phi_{12} - \pi)$ -peak
- Resums large logarithms
- Matching to NLO matrix elements

# The Parton Branching (PB) method

Hautmann et al. [JHEP 01 (2018) 070]

The **parton branching (PB) method** provides evolution equations for TMDs  $\tilde{A}_a(x, k_t^2, \mu^2)$ :

$$\begin{aligned} \tilde{A}_a(x, k_t^2, \mu^2) &= \Delta_a(\mu^2, \mu_0^2) \tilde{A}_a(x, k_{t,0}^2, \mu_0^2) + \\ &+ \sum_b \left[ \int \frac{d^2 \mu'}{\pi \mu'^2} \int_x^{z_M(\mu')} dz \Theta(\mu^2 - \mu'^2) \Theta(\mu'^2 - \mu_0^2) \right. \\ &\times \left. \frac{\Delta_a(\mu^2, \mu_0^2)}{\Delta_a(\mu'^2, \mu_0^2)} P_{ab}^{(R)}(\alpha_s(q_t), z) \tilde{A}_b\left(\frac{x}{z}, \underbrace{k_{t,b} - q_{t,c}}_{k_{t,a}}, \mu'^2\right) \right] \end{aligned}$$



Non-perturbative distribution  $\tilde{A}_a(x, k_{t,0}^2, \mu_0^2)$  includes intrinsic  $k_t$ :

$$f_a(x, \mu_0) e^{-k_t^2/2\sigma^2}$$

- Angular ordering:  $\mu' = q_t/(1-z)$  in  $z_M$ ,  $k_{t,a}$  and  $\alpha_s$

Hautmann, MvK et al. [Nucl.Phys.B 949 (2019) 114795]

- DGLAP splitting functions  $P_{ab}(\alpha_s, z)$  ( $P_{ab}^{(R)}$  are real emission probabilities)
- Sudakov form factor (non-resolvable / no-emission probability):

$$\Delta_a^{(PB)}(Q^2, q_0^2) = \exp \left\{ - \int_{q_0^2}^{Q^2} \frac{dq_t^2}{q_t^2} \left[ \frac{1}{2} \ln \left( \frac{Q^2}{q_t^2} \right) k_a(\alpha_s(q_t^2)) - d_a(\alpha_s(q_t^2)) \right] \right\}$$

resummation up to at least NLL accuracy!

# The Parton Branching (PB) method

Integration of the PB evolution equation over transverse momentum gives

$$\begin{aligned}\tilde{f}_a(x, \mu^2) &= \Delta_a(\mu^2, \mu_0^2) \tilde{f}_a(x, \mu_0^2) + \sum_b \int_{\mu_0^2}^{\mu^2} \frac{d\mu'^2}{\mu'^2} \int_x^1 dz \\ &\quad \times \Theta(z_M(\mu') - z) \frac{\Delta_a(\mu^2, \mu_0^2)}{\Delta_a(\mu'^2, \mu_0^2)} P_{ab}^{(R)}\left(z, \alpha_s(q_t)\right) \tilde{f}_b\left(\frac{x}{z}, \mu'^2\right).\end{aligned}$$

Coincide with **CMW for coherent branching** (Catani-Marchesini-Webber, [Nucl. Phys. B349 (1991) 635]) by using:

- dynamical resolution scale  $z_M(\mu') = 1 - q_0/\mu'$
- $\alpha_s(q_t^2)$

Recover **DGLAP** in limits (Hautmann et al. [JHEP 1801 (2018) 070]):

- $z_M(\mu') \rightarrow 1$
- $\alpha_s(q_t) \rightarrow \alpha_s(\mu')$

PB TMD sets fitted to data, available in TMDLIB

N.A. Abdulov, MvK et al. [Eur.Phys.J.C 81 (2021) 8, 752]

Set 1: PB-NLO-HERAII-2018-set1 has  $\alpha_s(\mu')$

Set 2: PB-NLO-HERAII-2018-set2 has  $\alpha_s(q_t)$

# Matching PB evolution to NLO matrix elements

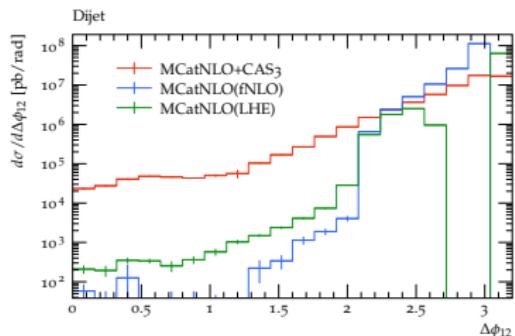
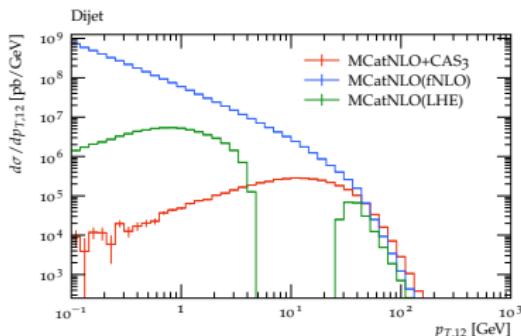
## Matching NLO from MADGRAPH\_AMC@NLO with PB

A. Bermudez Martinez et al. [Phys. Rev. D 100, 074027 (2019)]

- PB-TMDs and TMD shower implemented in CASCADE3

S. Baranov et al. [Eur.Phys.J.C 81 (2021) 5, 425]

- Avoid double counting: HERWIG6 subtraction terms (angular ordered shower)
- Associate  $k_t$  to partons in the hard process according to the TMD
- Two modes for parton shower: PB and CCFM shower

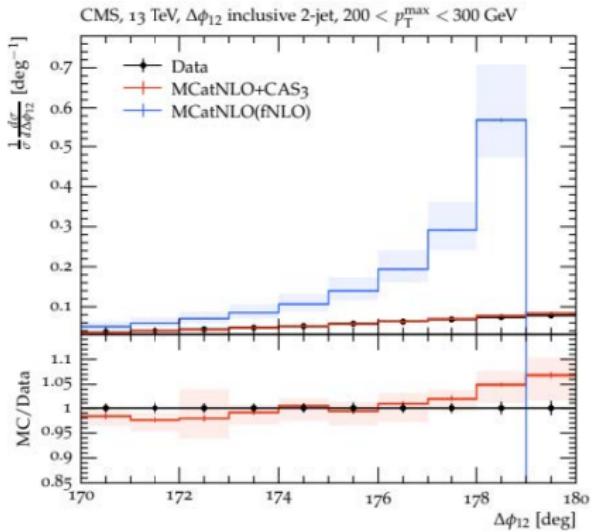


DY  $p_T$  results see next talk by A. Lelek

Now apply this method to dijets

## Results: fixed order NLO versus NLO+PB

- fNLO: no subtraction terms
- CAS3: include subtraction terms, TMD



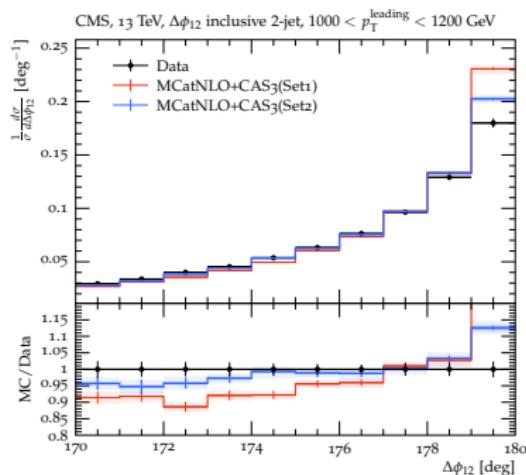
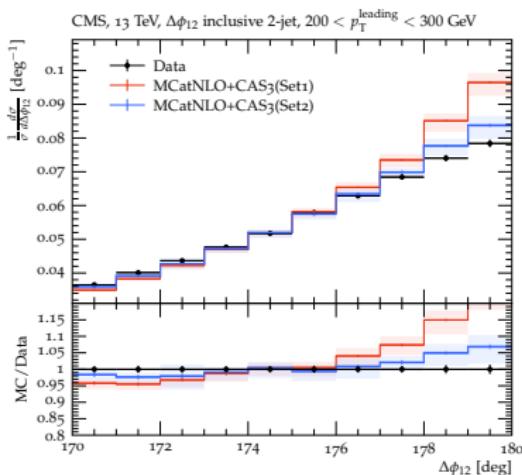
Q. Wang, REF workshop 2021

# Results: back-to-back region $\Delta\phi \in [170, 180]^\circ$

In the back-to-back region, both perturbative and non-perturbative effects.

$p_T^{\text{leading}} > 200$  GeV: perturbative effects dominate.

- MC@NLO matched to PB-TMD-set1:  $\alpha_s(\mu)$
- MC@NLO matched to PB-TMD-set2:  $\alpha_s(q_T)$

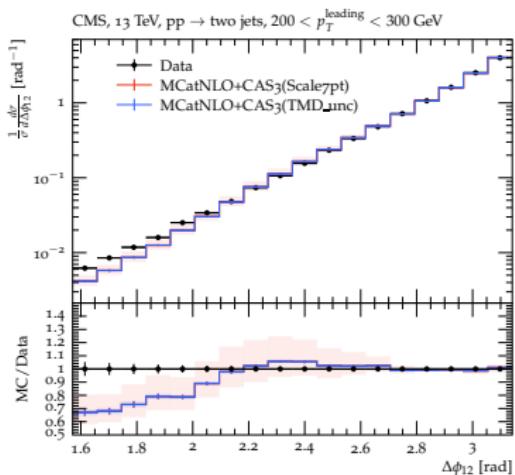
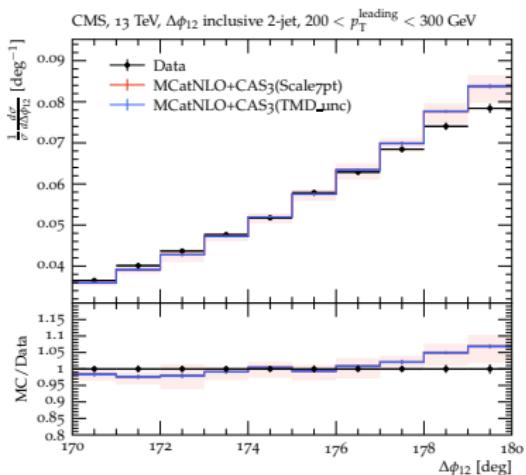


- TMD important in the back-to-back region
- ISR not important for inclusive 2-jet calculation

Azimuthal separation in nearly back-to-back jet topologies in inclusive 2- and 3-jet events in pp collisions at 13 TeV [Eur.Phys.J. C79 (2019) no.9, 773]

## Results: theoretical uncertainties

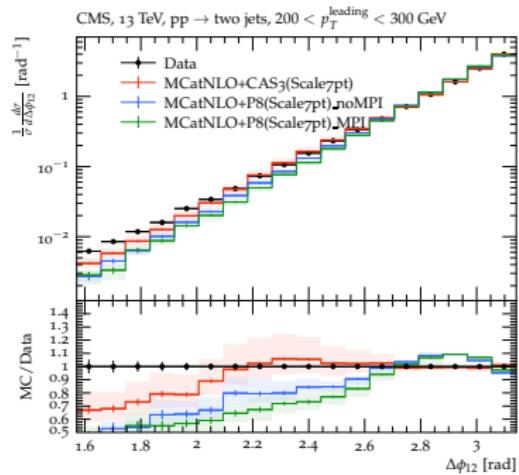
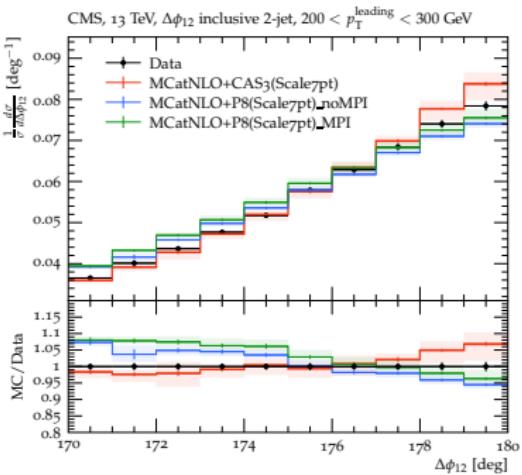
- Scale uncertainties:  $\mu_R$  and  $\mu_F$ ; 7-point scale variations
- TMD uncertainties: uncertainty from fit to data



Azimuthal correlations for inclusive 2-jet, 3-jet, and 4-jet events in pp collisions at 13 TeV  
Eur.Phys.J. C78 (2018) no.7, 566

# Results: comparison PB-TMD with PYTHIA8

- Madgraph\_aMC@NLO with PYTHIA8
- Check results with and without MPI
- Tune in PYTHIA needed, not needed for PB!



- PB uncertainties: TMD + scale uncertainties
- Pythia uncertainties:  $\mu_{R,F}$  in ME +  $\mu_R$  variation in PS

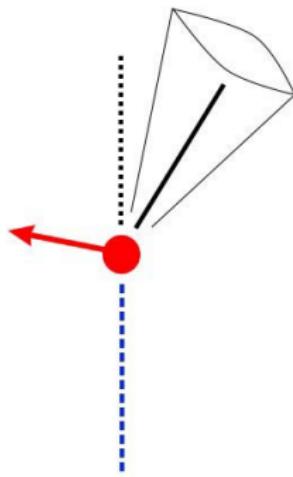
# TMD multi-jet merging

TMD merging is a **new** LO multi-jet merging algorithm

A. Bermudez Martinez et al. [Phys.Lett.B 822 (2021) 136700].

## Steps of TMD merging

- ① Matrix elements for n-jet production
- ② Reweighting the strong coupling according to the parton shower:  $\alpha_s(Q) \rightarrow \alpha_s(Q) \cdot \frac{\alpha_s(q_T)}{\alpha_s(Q)}$
- ③ Apply forward PB evolution to incoming partons with condition  $k_t^2 \leq \mu_{min}^2$
- ④ TMD parton showering of the events
- ⑤ Apply MLM merging procedure  
M. L. Mangano [NPB 632 (2002) 343–362]  
Compare hard partonic event with showered event  
and avoid double counting



This mainly increases accuracy at large  $p_T$  and small  $\Delta\phi$  regions

# TMD multi-jet merging

Dijet with soft radiation:



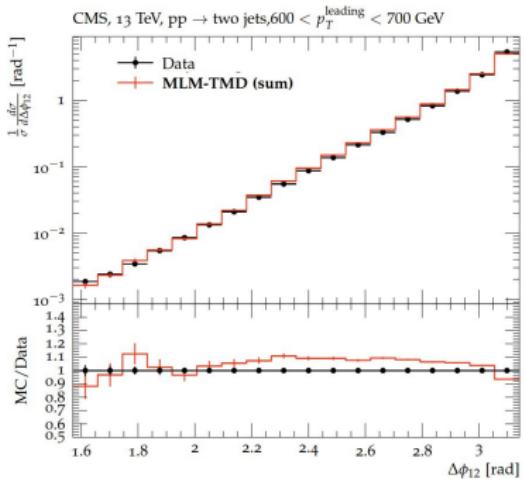
Dijet + 1 jet + additional radiation:



Dijet + 2 jets + additional radiation:



## Preliminary result



To be continued...

# Conclusions

The PB approach for TMDs takes into account both perturbative and non-perturbative effects.

- Perturbative: soft gluon emissions ( $z \rightarrow 1$ ) and all transverse momenta ( $q_\perp$ ) from branchings in the QCD evolution
- Non-perturbative: intrinsic transverse momentum, subject to perturbative evolution

In high  $p_T$  dijets perturbative effects dominate, even at  $\Delta\phi_{12} \sim \pi$ .

## Parton branching TMDs matched to NLO matrix elements

- Good description of dijet azimuthal back-to-back region
- No tuning needed
- Small TMD uncertainties
- TMD evolution important at back-to-back region
- PB-TMD-set1 significantly different from PB-TMD-set2:  $\alpha_s(q_t)$
- Multi-jet TMD merging increases accuracy at small  $\Delta\phi$

## Back-up slides

Inclusive & exclusive observable calculations with PB

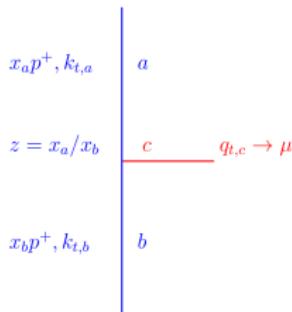
The PB method is implemented in event generator CASCADE3 Eur. Phys. J. C 81, 425 (2021) [arXiv:2101.10221v1]

- Two modes for hard scattering events (LHE input): on-shell and off-shell
  - Associate  $k_t$  to partons in the hard process according to the TMD
  - Two modes for parton shower: PB and CCFM shower

**TMD parton shower** based on PB by constructing the *backward Sudakov*:

$$\Delta_{bw}(x, k_t, \mu_i, \mu_{i-1}) = \exp \left\{ - \sum_b \int_{\mu_{i-1}^2}^{\mu_i^2} \frac{d\mu'^2}{\mu'^2} \int_x^{zM} dz P_{ab}^{(R)} \frac{\tilde{\mathcal{A}}_b(x/z, k'_t, \mu')}{\tilde{\mathcal{A}}_a(x, k_t, \mu')} \right\}.$$

This is the no-branching probability in the TMD parton shower.



- In each splitting

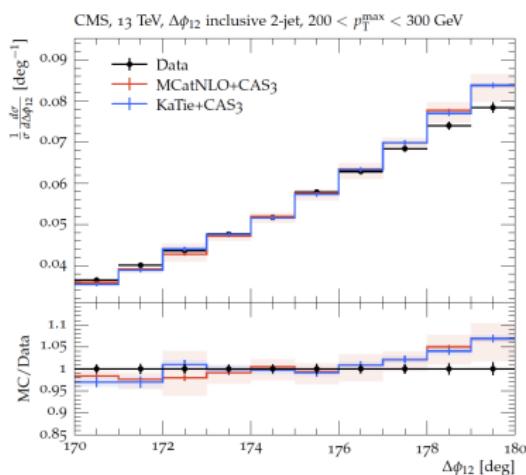
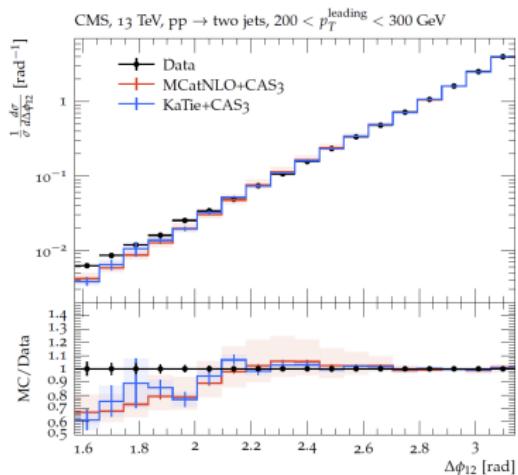
$$\begin{aligned}k_{t,b} &= k_{t,a} + q_{t,c} \\&= k_{t,a} + (1 - z)\mu\end{aligned}$$

- Total transverse momentum:

$$k_t = k_{t,0} + \sum_c q_{t,c}$$

# Results: on-shell versus off-shell matrix elements

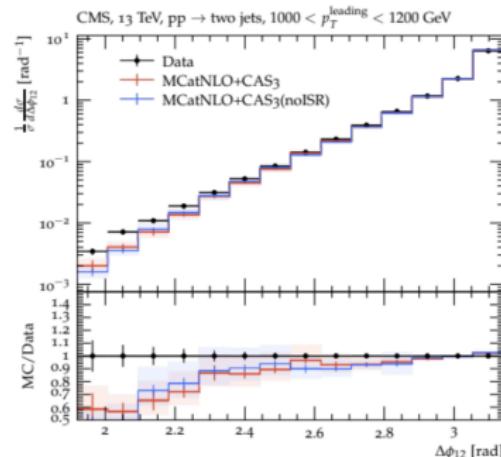
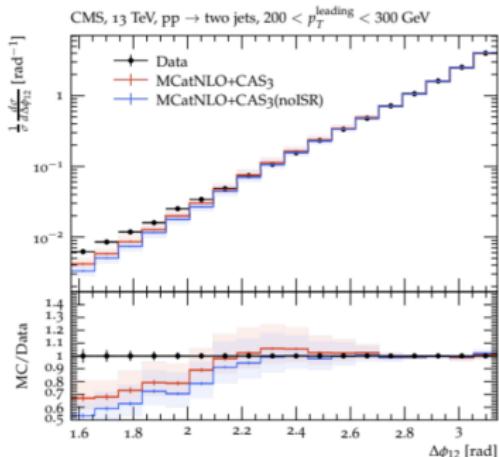
KATIE calculates LO matrix elements with off-shell partons. Compare with PB-TMD with MC@NLO.



- at high  $\Delta\phi$ : off-shellness / TMD more important than higher orders of  $\alpha_s$  in calculation
- at smaller  $\Delta\phi$ : relatively good description with off-shellness / TMD

# Effects of TMD and parton shower

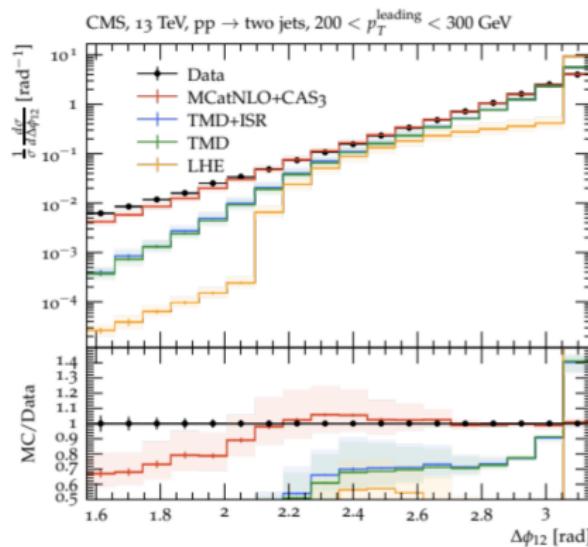
- Study effect of
  - TMD,
  - initial state TMD shower



- TMD is very important in back-to-back region as well as in small  $\Delta\phi$
- ISR does not play a big role since we look at 2 leading jets.

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