

So, is this “dark matter”
in the room with us right now?



$(g - 2)_\mu$ and SUSY: ILC and CLIC Physics Opportunities

Sven Heinemeyer, IFT (CSIC, Madrid)

Hamburg, 10/2022

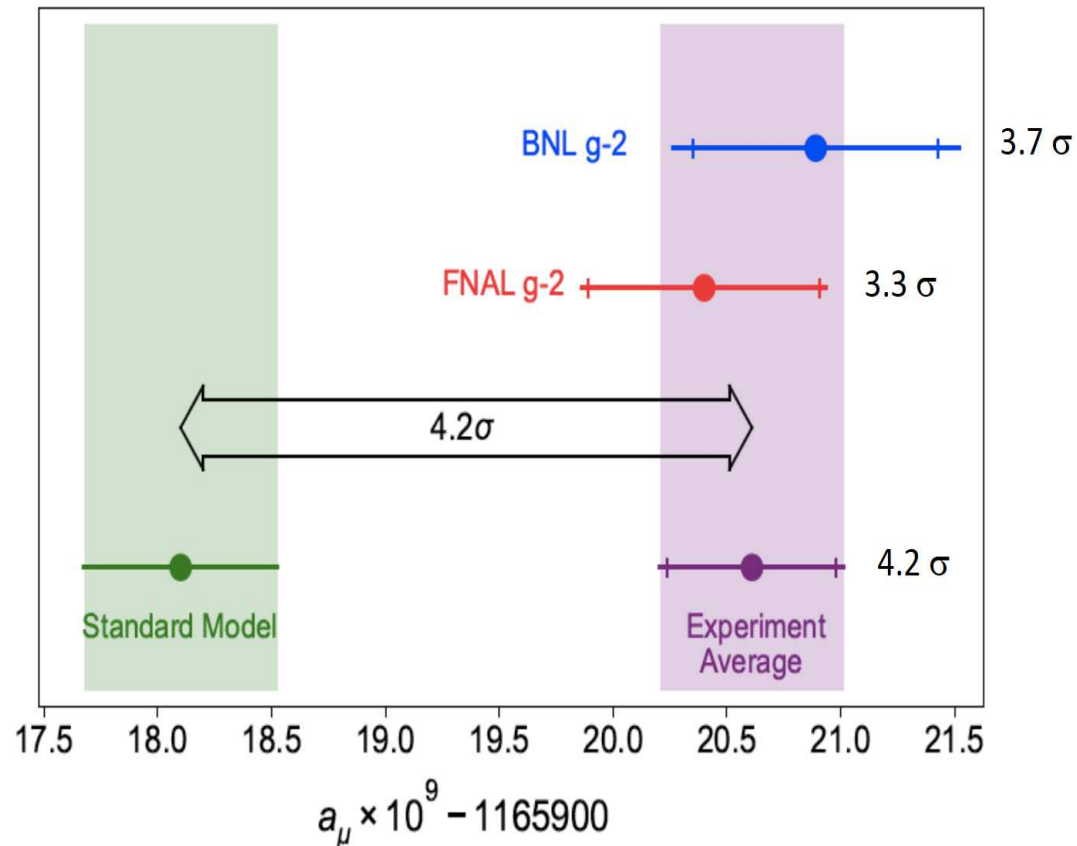
with M. Chakraborti, I. Saha, C. Schappacher

- Introduction
- Prospects for Direct Detection experiments
- ILC and CLIC physics opportunities
- Conclusions

1. Introduction

The anomalous magnetic moment of the muon: $a_\mu \equiv (g - 2)_\mu/2$

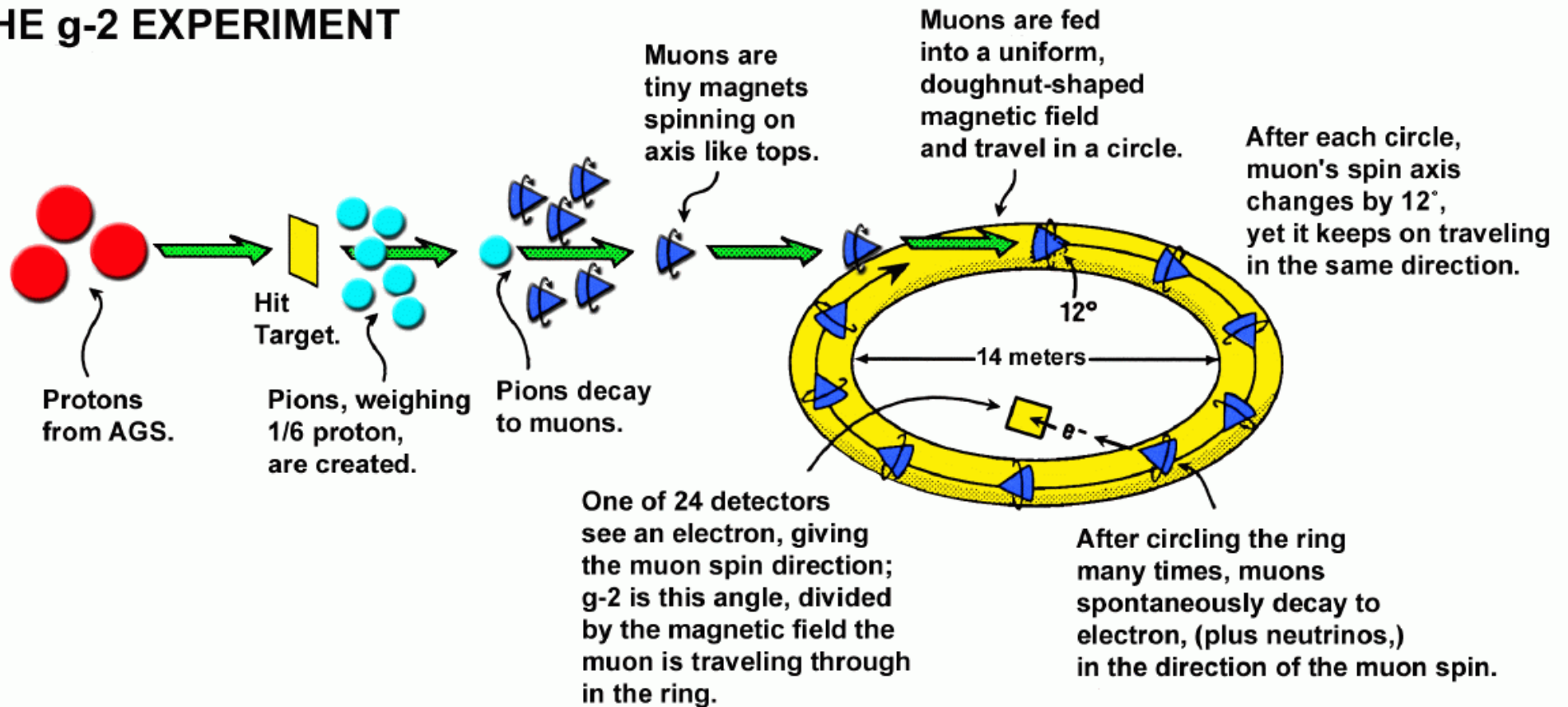
Overview about the current **experimental** and **SM (theory)** result:



$$a_\mu^{\text{exp}} - a_\mu^{\text{theo,SM}} \approx (25.1 \pm 5.9) \times 10^{-10} : 4.2 \sigma$$

The $(g - 2)_\mu$ experiment:

LIFE OF A MUON: THE g-2 EXPERIMENT

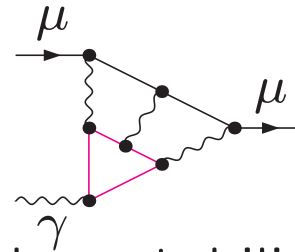


Coupling of muon to magnetic field : $\mu - \mu - \gamma$ coupling

$$\bar{u}(p') \left[\gamma^\mu F_1(q^2) + \frac{i}{2m_\mu} \sigma^{\mu\nu} q_\nu F_2(q^2) \right] u(p) A_\mu \quad F_2(0) = a_\mu$$

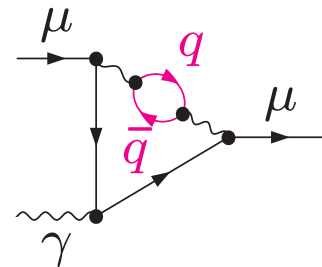
Theory of $(g - 2)_\mu$:

- the **light-by-light** contribution:



2002: sign error discovered; since then stabilized
2021: confirmed by LQCD

- the **hadronic vacuum** contribution:



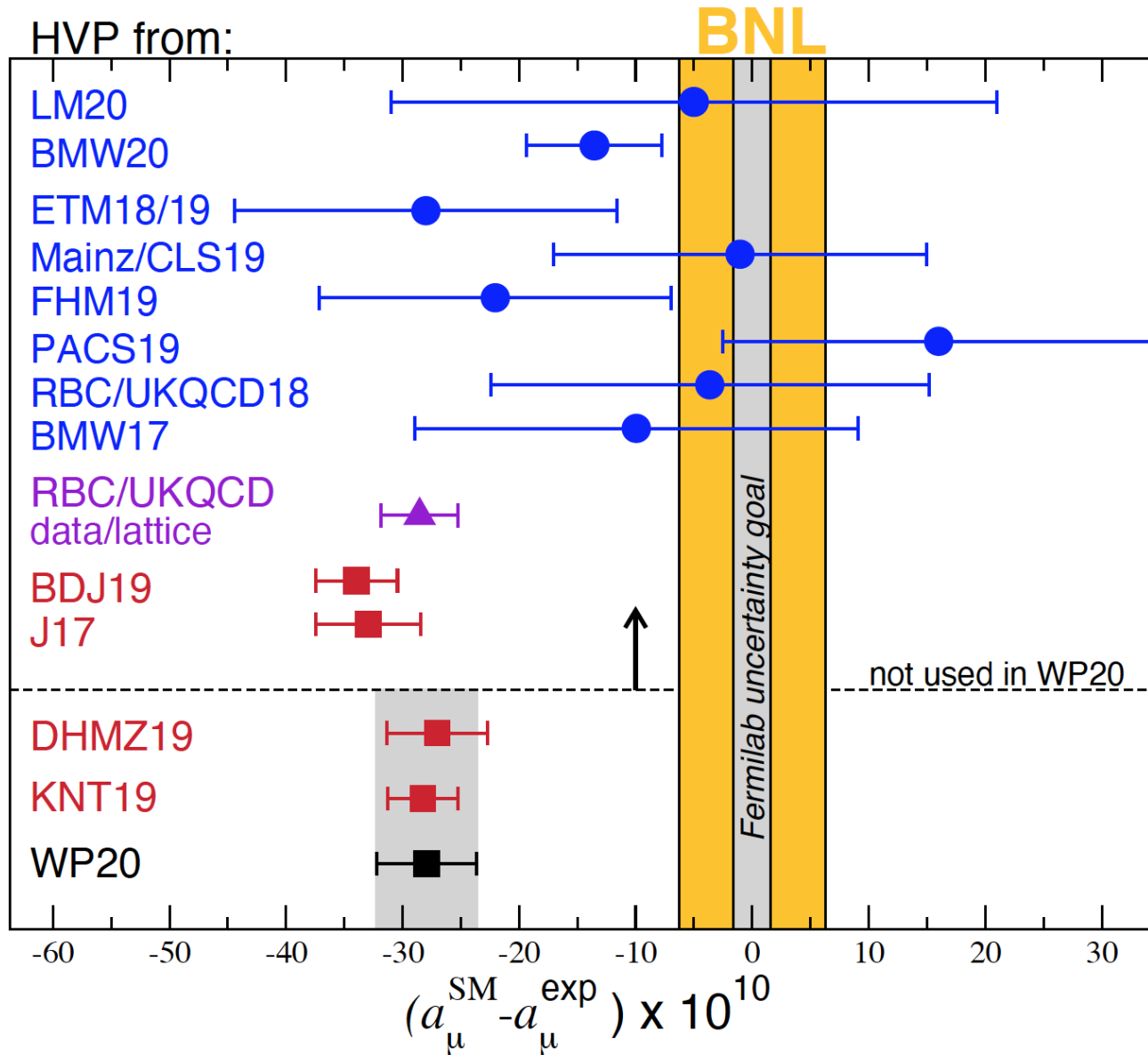
'direct' e^+e^- data:

from **CMD-II**, **SND**, **KLOE**, **BaBar** (radiative return)
 \Rightarrow agree relatively well (also with old e^+e^- data)
 \Rightarrow **tension with LQCD results**

τ data:

tended to be closer to experimental result
inclusion of γ - ρ mixing: agreement with e^+e^- [F. Jegerlehner, R. Szafron '10]
 \Rightarrow still under discussion ... \Rightarrow **effectively not used anymore**

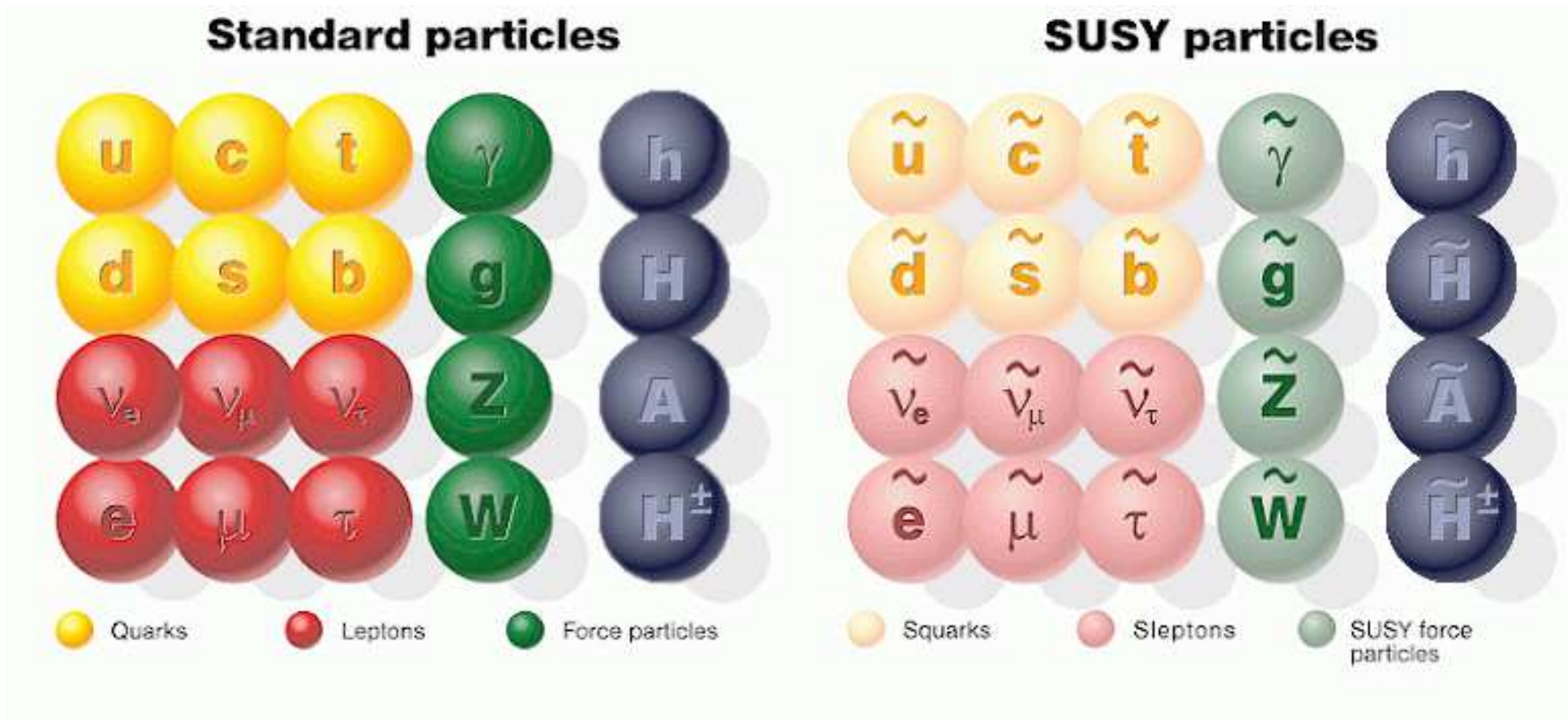
HVP summary:



⇒ BMW20: difference to experimental data $\sim 1.5\sigma$

The MSSM

Superpartners for Standard Model particles



⇒ large uncolored / EW sector

Neutralinos and charginos:

Higgsinos and electroweak gauginos mix

charged:

$$\tilde{W}^+, \tilde{h}_u^+ \rightarrow \tilde{\chi}_1^+, \tilde{\chi}_2^+, \quad \tilde{W}^-, \tilde{h}_d^- \rightarrow \tilde{\chi}_1^-, \tilde{\chi}_2^-$$

Diagonalization of the mass matrix:

$$\mathbf{X} = \begin{pmatrix} M_2 & \sqrt{2} \sin \beta M_W \\ \sqrt{2} \cos \beta M_W & \mu \end{pmatrix},$$

$$\mathbf{M}_{\tilde{\chi}^\pm} = \mathbf{V}^* \mathbf{X}^\top \mathbf{U}^\dagger = \begin{pmatrix} m_{\tilde{\chi}_1^\pm} & 0 \\ 0 & m_{\tilde{\chi}_2^\pm} \end{pmatrix}$$

⇒ charginos: mass eigenstates

mass matrix given in terms of M_2 , μ , $\tan \beta$

neutral:

$$\underbrace{\tilde{\gamma}, \tilde{Z}, \tilde{h}_u^0, \tilde{h}_d^0}_{\tilde{W}^0, \tilde{B}^0} \rightarrow \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$$

Diagonalization of mass matrix:

$$\mathbf{Y} = \begin{pmatrix} M_1 & 0 & -M_Z s_W \cos \beta & M_Z s_W \sin \beta \\ 0 & M_2 & M_Z c_W \cos \beta & -M_Z c_W \sin \beta \\ -M_Z s_W \cos \beta & M_Z c_W \cos \beta & 0 & -\mu \\ M_Z s_W \sin \beta & -M_Z c_W \sin \beta & -\mu & 0 \end{pmatrix},$$

$$\mathbf{M}_{\tilde{\chi}^0} = \mathbf{N}^* \mathbf{Y} \mathbf{N}^\dagger = \text{diag}(m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_4^0})$$

⇒ neutralinos: mass eigenstates

mass matrix given in terms of M_1 , M_2 , μ , $\tan \beta$

⇒ only one additional parameter

⇒ MSSM predicts mass relations between neutralinos and charginos

Scalar lepton sector of the MSSM

Charged slepton mass matrices

$$\mathbf{M}_{\tilde{l}}^2 = \begin{pmatrix} M_{\tilde{l}_L}^2 + m_l^2 + DT_{l_1} & m_l X_l \\ m_l X_l & M_{\tilde{l}_R}^2 + m_l^2 + DT_{l_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{l}}} \begin{pmatrix} m_{\tilde{l}_1}^2 & 0 \\ 0 & m_{\tilde{l}_2}^2 \end{pmatrix}$$

with

$$X_l = A_l - \mu \tan \beta$$

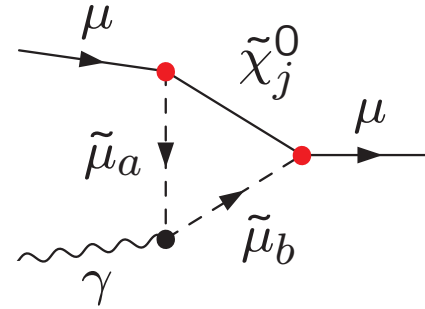
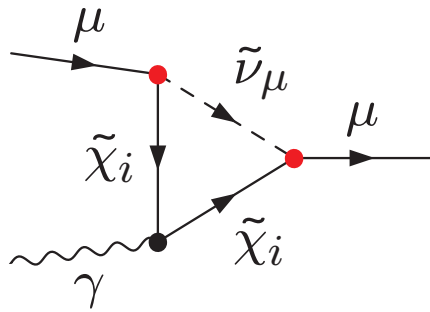
Sneutrino mass

$$m_{\tilde{\nu}_l}^2 = M_{\tilde{l}_L}^2 + DT_{\nu}$$

Simplifying assumption: $M_{\tilde{l}_L}$ and $M_{\tilde{l}_R}$ identical for all three generations

SUSY can easily explain the deviation in a_μ :

Feynman diagrams for MSSM 1L corrections:



- Diagrams with chargino/sneutrino exchange
- Diagrams with neutralino/smuon exchange

Enhancement factor as compared to SM:

$$\mu - \tilde{\chi}_i^\pm - \tilde{\nu}_\mu : \sim m_\mu \tan \beta$$

$$\mu - \tilde{\chi}_j^0 - \tilde{\mu}_a : \sim m_\mu \tan \beta$$

$$\text{SM, EW 1L: } \frac{\alpha}{\pi} \frac{m_\mu^2}{M_W^2}$$

$$\text{MSSM, 1L: } \frac{\alpha}{\pi} \frac{m_\mu^2}{M_{\text{SUSY}}^2} \times \tan \beta$$

SUSY corrections at 1L:

$$a_{\mu}^{\text{SUSY,1L}} \approx 13 \times 10^{-10} \left(\frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 \tan \beta \text{ sign}(\mu)$$

$M_{\text{SUSY}} (= m_{\tilde{\mu}} = m_{\tilde{\nu}} = m_{\tilde{\chi}})$: generic SUSY mass scale

$$a_{\mu}^{\text{SUSY,1L}} = (-100 \dots + 100) \times 10^{-10}$$
$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} \approx (25.1 \pm 5.9) \times 10^{-10}$$

⇒ SUSY could easily explain the “discrepancy”

⇒ a_{μ} can provide **upper limits on the EW masses**

(by requiring agreement at the 95% C.L.)

SUSY corrections at 1L:

$$a_{\mu}^{\text{SUSY},1\text{L}} \approx 13 \times 10^{-10} \left(\frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 \tan \beta \text{ sign}(\mu)$$

$M_{\text{SUSY}} (= m_{\tilde{\mu}} = m_{\tilde{\nu}} = m_{\tilde{\chi}})$: generic SUSY mass scale

$$a_{\mu}^{\text{SUSY},1\text{L}} = (-100 \dots + 100) \times 10^{-10}$$
$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} \approx (25.1 \pm 5.9) \times 10^{-10}$$

⇒ SUSY could easily explain the “discrepancy”

⇒ a_{μ} can provide **upper limits on the EW masses**

(by requiring agreement at the 95% C.L.)

If SUSY exists, it should fix $(g - 2)_{\mu}$!

⇒ there must be light EW SUSY particles!

The general idea:

[M. Chakraborti, S.H., I. Saha '20, '21]

- scan the relevant EW SUSY parameter space
 - impose all relevant experimental constraints:
 - $(g - 2)_\mu$
 - Dark Matter relic density
 - Dark Matter direct detection
 - LHC searches for EW particles
 - Dark Matter relic density requires a mechanism to reduce the density in the early universe
 - bino/wino DM with chargino co-annihilation
 - bino DM with slepton co-annihilation
 - higgsino DM
 - wino DM
 - obtain lower and upper limits on the various EW particle masses
- ⇒ evaluate prospects for e^+e^- colliders!

$(g - 2)_\mu$ constraint: (GM2Calc)

$$\begin{aligned} \text{old: } \Delta a_\mu^{\text{old}} &= (28.0 \pm 7.4) \times 10^{-10} \\ \text{new: } \Delta a_\mu^{\text{new}} &= (25.1 \pm 5.9) \times 10^{-10} \end{aligned}$$

\Rightarrow some results for $\Delta a_\mu^{\text{new}} (\equiv \Delta a_\mu)$
some results only available for $\Delta a_\mu^{\text{old}}$

Note: $\Delta a_\mu^{\text{old}} - 2\sigma^{\text{old}} \approx \Delta a_\mu^{\text{new}} - 2\sigma^{\text{new}}$

\Rightarrow upper limits on SUSY masses are not expected to change

Dark Matter relic density: MicrOmegas

$$\begin{aligned} \Omega_{\text{CDM}} h^2 &= 0.120 \pm 0.001 \\ \text{or } \Omega_{\text{CDM}} h^2 &\leq 0.122 \end{aligned}$$

(as taken from [*Planck '18*])

Dark Matter direct detection: MicrOmegas

limit on spin independent scattering cross section (Xenon1T)

[*Xenon collab. '18*]

Results for (nearly) all SUSY scenarios

A) bino/wino DM with chargino co-annihilation

relic DM density 100% fulfilled

$$\Rightarrow m_{(N)\text{LSP}} \lesssim 650(700) \text{ GeV for new (and old) } (g-2)_\mu$$

B/C) bino DM with slepton co-annihilation

relic DM density 100% fulfilled

$$\Rightarrow m_{(N)\text{LSP}} \lesssim 650(700) \text{ GeV for new (and old) } (g-2)_\mu$$

D) higgsino DM: $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_2^0} \sim m_{\tilde{\chi}_1^\pm} \sim \mu$

relic DM density as upper limit (otherwise $m_{\tilde{\chi}_1^0} \sim 1 \text{ TeV}$)

$$\Rightarrow m_{(N)\text{LSP}} \lesssim 500 \text{ GeV}$$

E) wino DM: $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_1^\pm} \sim M_2$

relic DM density as upper limit (otherwise $m_{\tilde{\chi}_1^0} \sim 3 \text{ TeV}$)

$$\Rightarrow m_{(N)\text{LSP}} \lesssim 600 \text{ GeV}$$

\Rightarrow predictions for future experiments?!

2. Prospects for Direct Detection Experiments



A) Bino/wino DM with chargino co-annihilation

Parameter scan:

$$100 \text{ GeV} \leq M_1 \leq 1 \text{ TeV} ,$$

$$M_1 \leq M_2 \leq 1.1M_1 ,$$

$$1.1M_1 \leq \mu \leq 10M_1 ,$$

$$5 \leq \tan \beta \leq 60 ,$$

$$100 \text{ GeV} \leq m_{\tilde{L}} \leq 1 \text{ TeV} ,$$

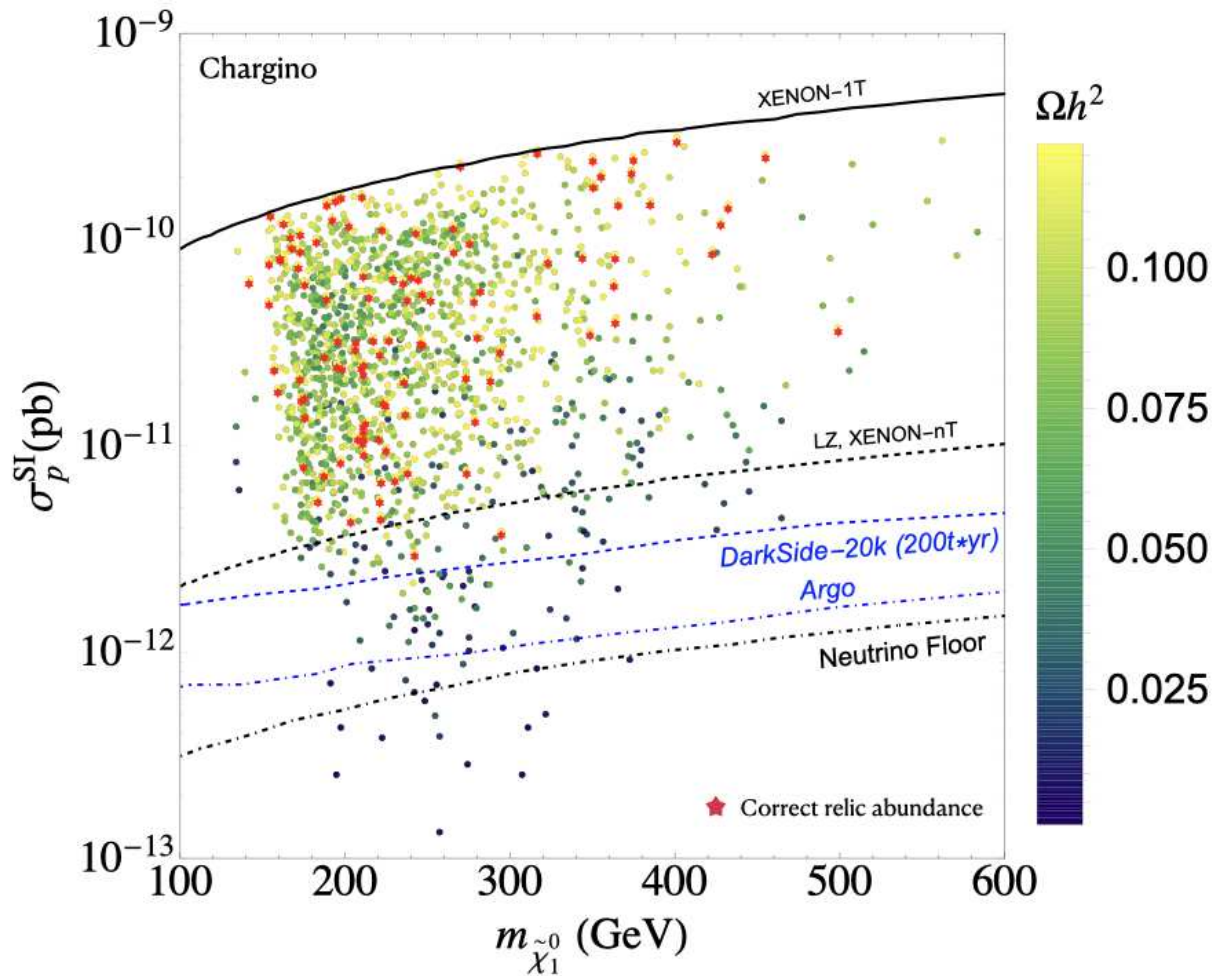
$$m_{\tilde{R}} = m_{\tilde{L}} .$$

(latter condition only to make the analysis simpler, no relevant effect)

relic DM density can be 100% fulfilled

$$\Rightarrow m_{(N)\text{LSP}} \lesssim 650(700) \text{ GeV}$$

Results in the $m_{\tilde{\chi}_1^0} - \sigma_p^{\text{SI}}$ plane: [M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ large part covered by XENON-nT/LZ

⇒ but can go below even the neutrino floor

B/C) Bino DM with slepton co-annihilation

Parameter scan:

$$100 \text{ GeV} \leq M_1 \leq 1 \text{ TeV} ,$$

$$M_1 \leq M_2 \leq 10M_1 ,$$

$$1.1M_1 \leq \mu \leq 10M_1 ,$$

$$5 \leq \tan \beta \leq 60 ,$$

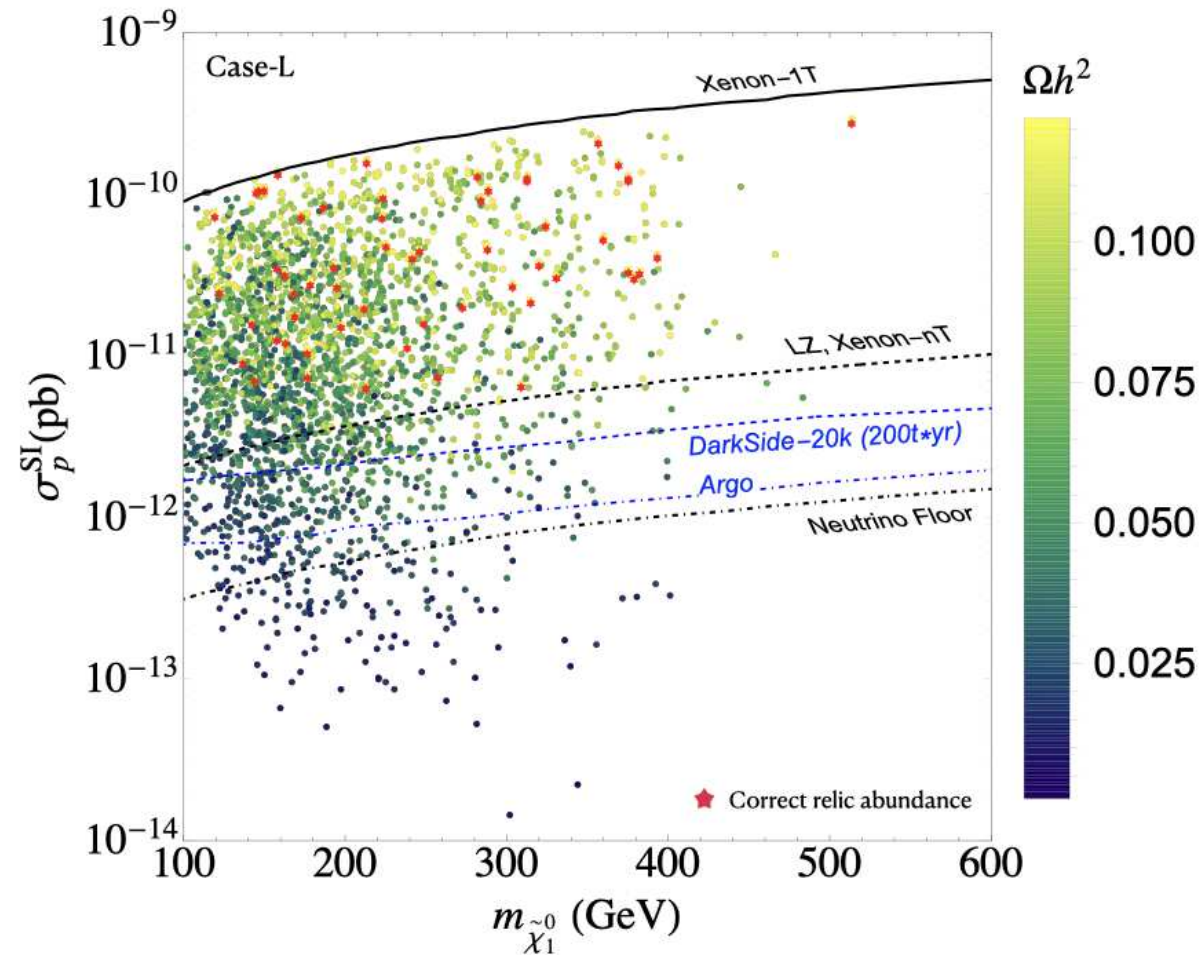
$$\text{Case-L: } M_1 \leq m_{\tilde{L}} \leq 1.2M_1, \quad M_1 \leq m_{\tilde{R}} \leq 10M_1 .$$

$$\text{Case-R: } M_1 \leq m_{\tilde{R}} \leq 1.2M_1, \quad M_1 \leq m_{\tilde{L}} \leq 10M_1 .$$

relic DM density can be 100% fulfilled

$$\Rightarrow m_{(N)\text{LSP}} \lesssim 650(700) \text{ GeV}$$

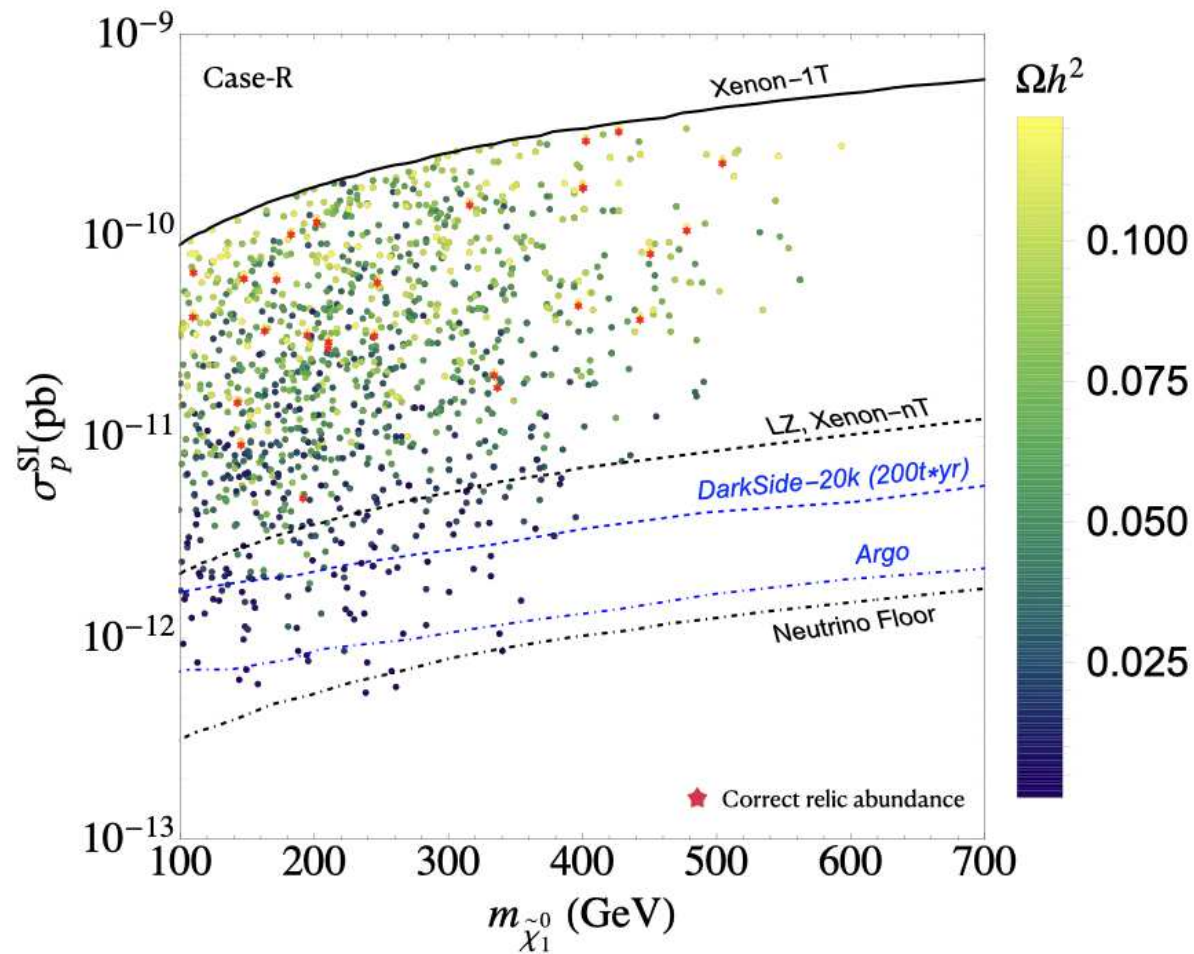
Case-L: results in the $m_{\tilde{\chi}_1^0} - \sigma_p^{\text{SI}}$ plane: [M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ large part covered by XENON-nT/LZ

⇒ but can go below even the neutrino floor

Case-R: results in the $m_{\tilde{\chi}_1^0} - \sigma_p^{\text{SI}}$ plane: [M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ large part covered by XENON-nT/LZ

⇒ but can go below even the neutrino floor

D) Higgsino DM

Parameter scan:

$$100 \text{ GeV} \leq \mu \leq 1.2 \text{ TeV} ,$$

$$1.1\mu \leq M_1 \leq 10\mu ,$$

$$1.1M_2 \leq \mu \leq 10\mu ,$$

$$5 \leq \tan \beta \leq 60 ,$$

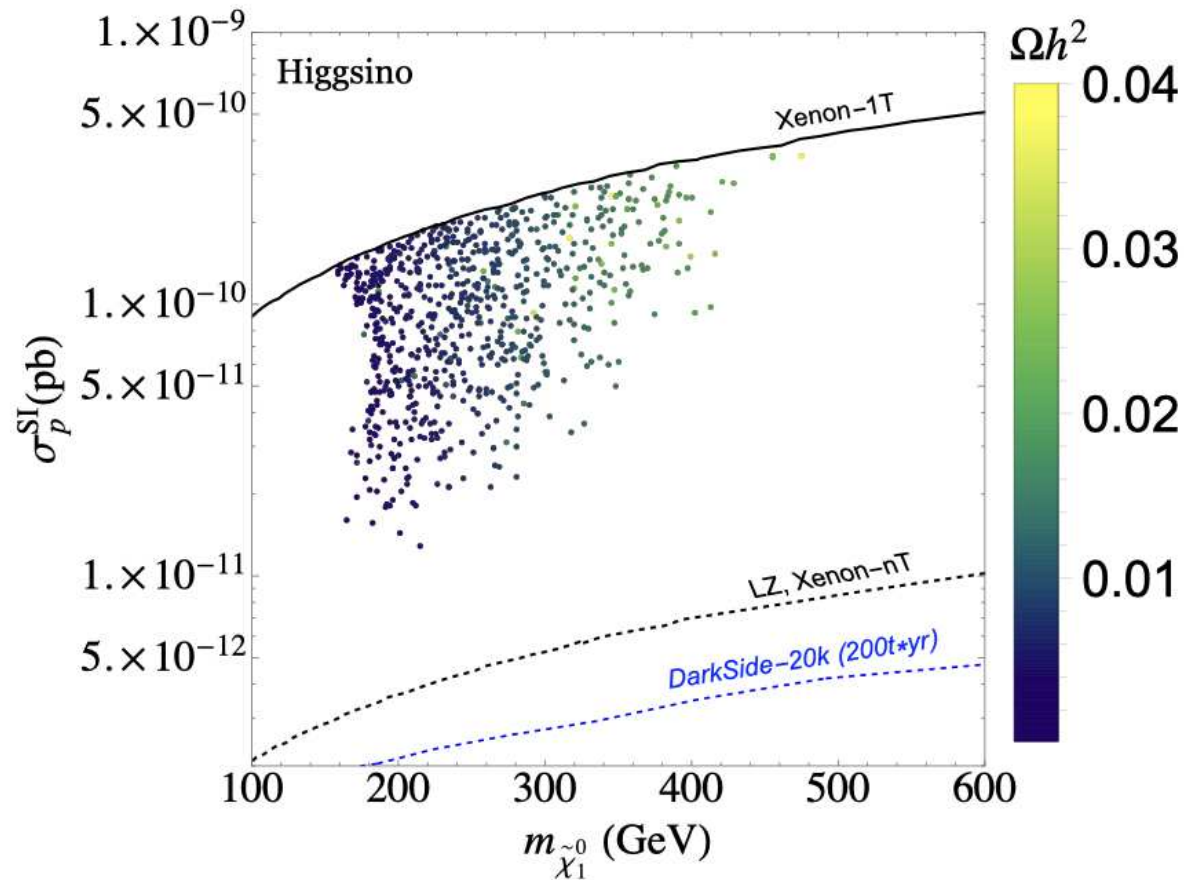
$$100 \text{ GeV} \leq m_{\tilde{L}}, m_{\tilde{R}} \leq 2 \text{ TeV} ,$$

$$\Rightarrow m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_2^0} \sim m_{\tilde{\chi}_1^\pm} \sim \mu$$

Full DM relic density reached only for $m_{\tilde{\chi}_1^0} \sim 1 \text{ TeV}$

\Rightarrow incompatible with $(g-2)_\mu$

$\Rightarrow m_{(N)\text{LSP}} \lesssim 500 \text{ GeV}$



⇒ everything covered by XENON-nT/LZ

⇒ Direct Detection experiments cover the full parameter space

E) Wino DM

Parameter scan:

$$100 \text{ GeV} \leq M_2 \leq 1.5 \text{ TeV} ,$$

$$1.1M_2 \leq M_1 \leq 10M_2 ,$$

$$1.1M_2 \leq \mu \leq 10M_2 ,$$

$$5 \leq \tan \beta \leq 60 ,$$

$$100 \text{ GeV} \leq m_{\tilde{L}}, m_{\tilde{R}} \leq 2 \text{ TeV} ,$$

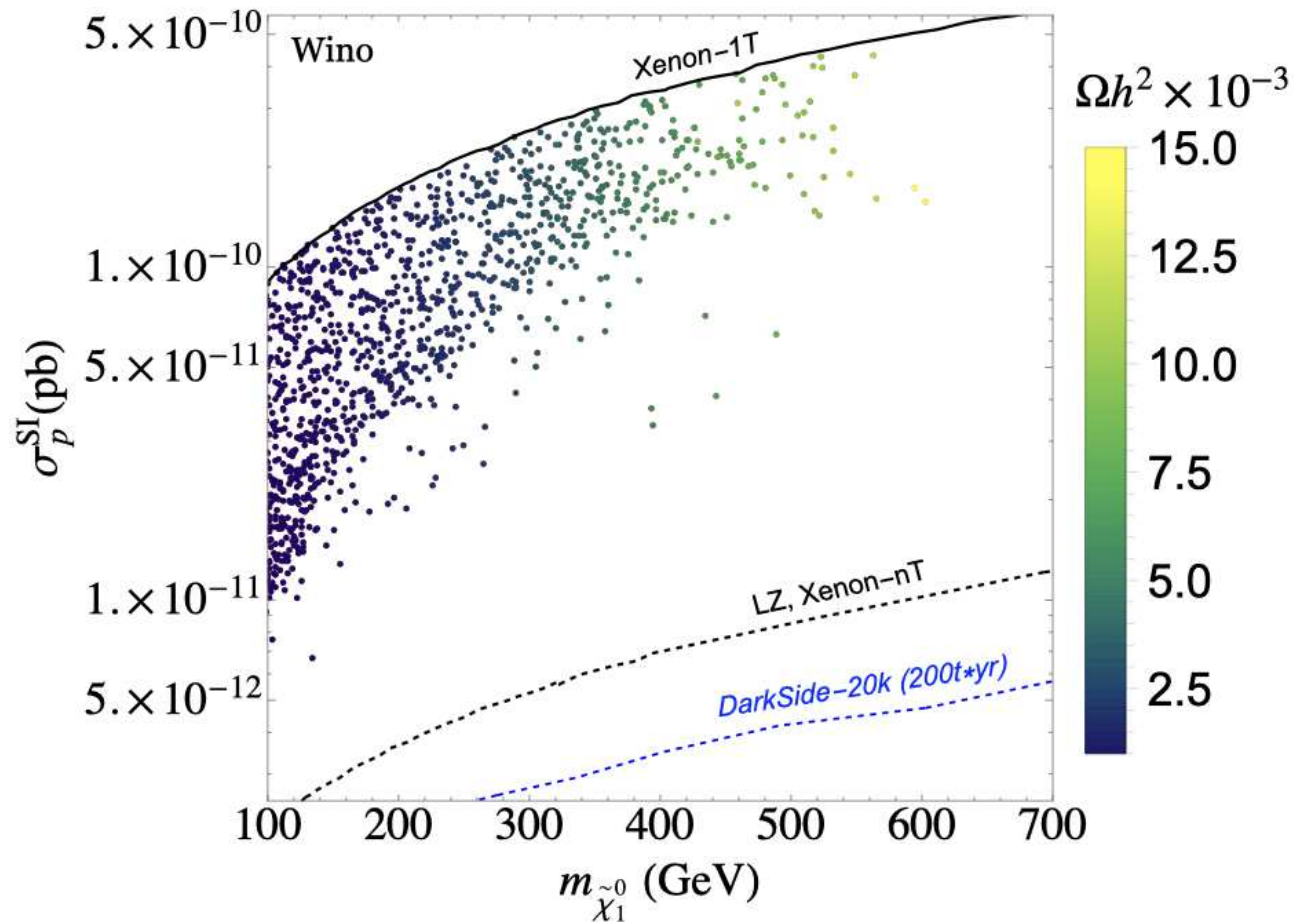
$$\Rightarrow m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_1^\pm} \sim M_2$$

Full DM relic density reached only for $m_{\tilde{\chi}_1^0} \sim 3 \text{ TeV}$

\Rightarrow incompatible with $(g-2)_\mu$

$\Rightarrow m_{(N)\text{LSP}} \lesssim 600 \text{ GeV}$

Results in the $m_{\tilde{\chi}_1^0} - \sigma_p^{\text{SI}}$ plane: [M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ everything covered by XENON-nT/LZ

⇒ Direct Detection experiments cover the full parameter space

3. ILC and CLIC physics opportunities

Scenarios A/B/C:

- ⇒ large part covered by XENON-nT/LZ
- ⇒ but can go below even the neutrino floor
- ⇒ (HL-)LHC has naturally problems because of compressed spectra
- ⇒ (HL-)LHC must go for heavier particles
- ⇒ compressed spectra “easy” for e^+e^- colliders
- ⇒ physics opportunities for ILC/CLIC?!

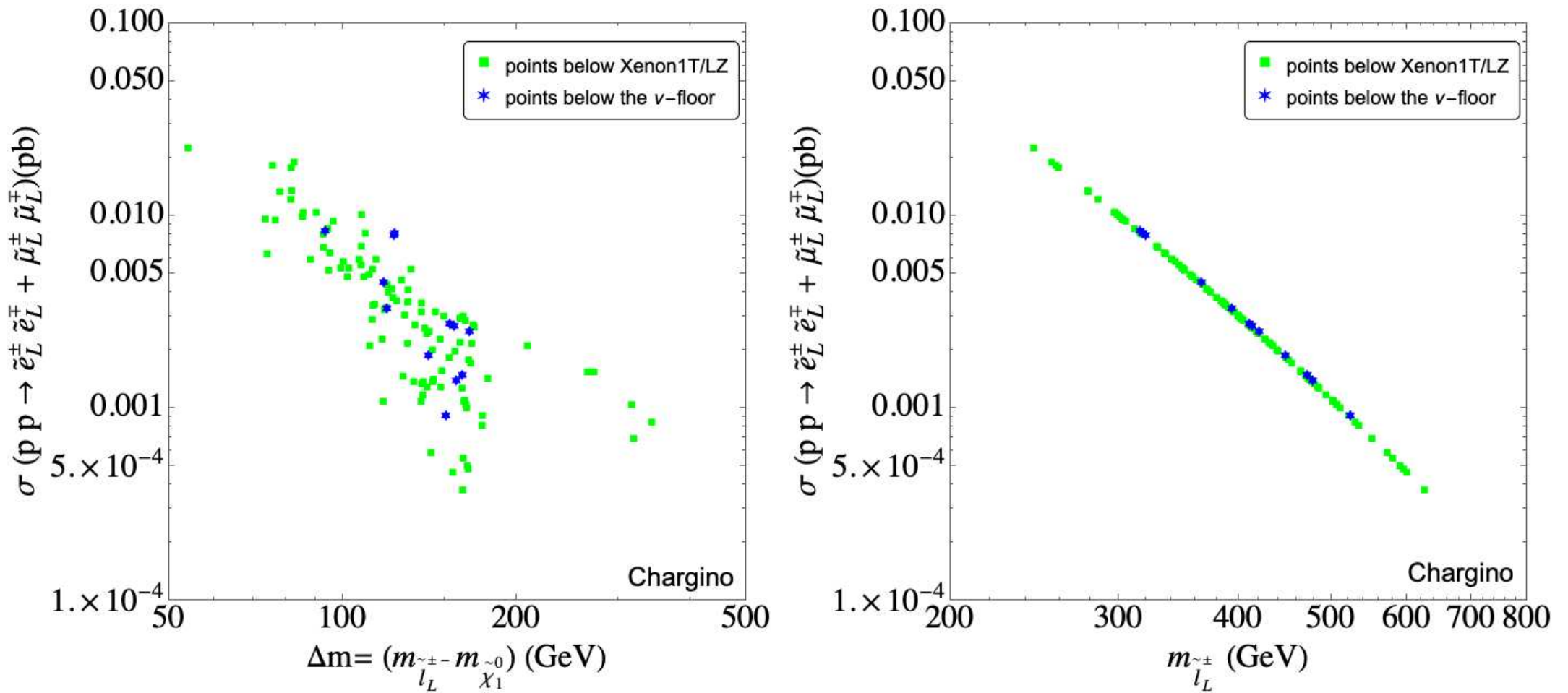
Scenarios D/E:

- ⇒ everything covered by XENON-nT/LZ
- ⇒ Direct Detection experiments cover the full parameter space
- ⇒ what can be learned at ILC/CLIC?

⇒ ILC and CLIC physics opportunities in the light of (HL-)LHC!

(HL-)LHC cross sections for $\tilde{\chi}_1^\pm$ -coannihilation (non-compressed):

[M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



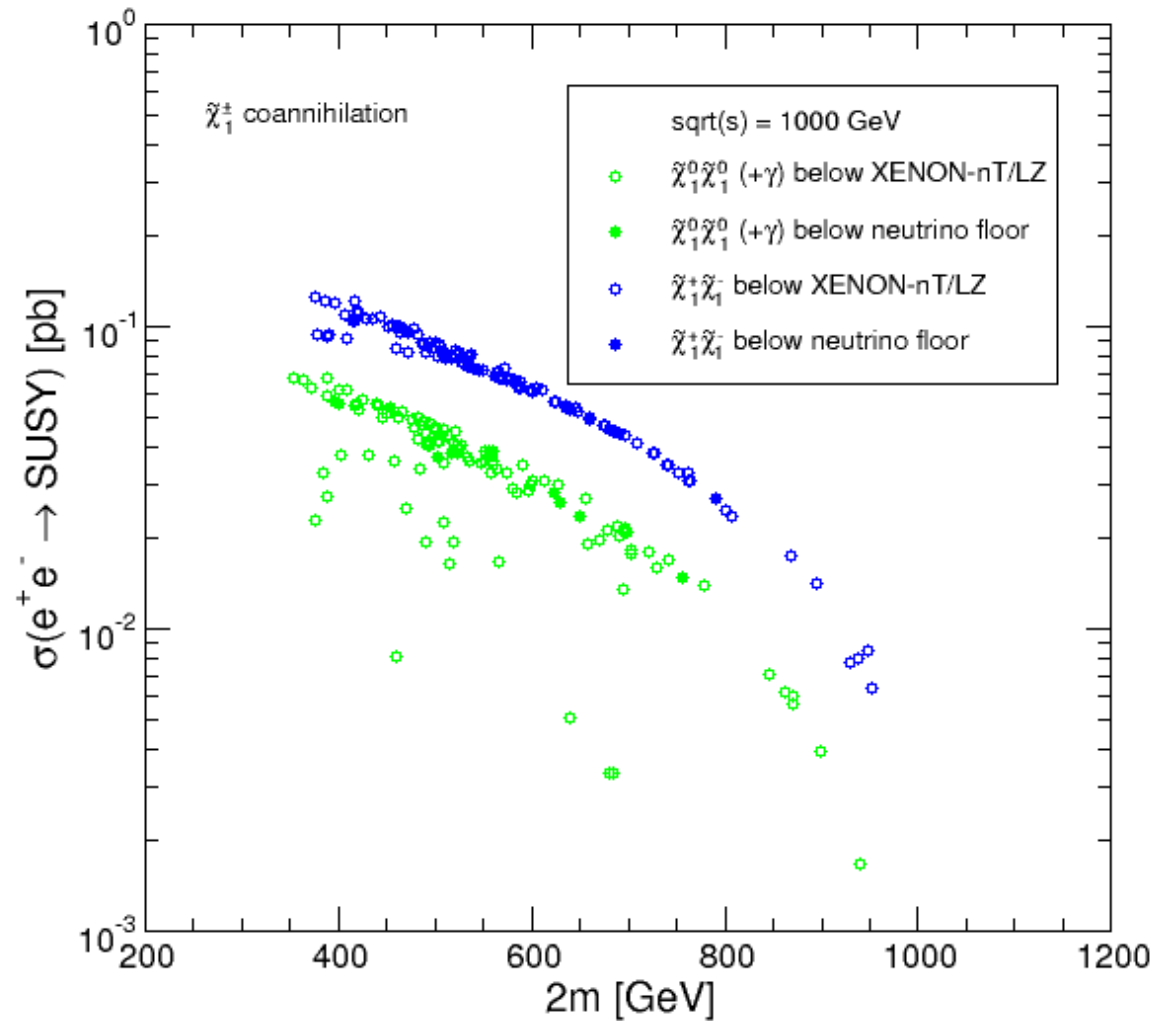
\Rightarrow XS above 0.4 fb \Rightarrow more than 1200 events

\Rightarrow even better for “BNF” points: XS above 1 fb

But: detailed (HL-)LHC analysis missing! (spectra not too compressed!)

ILC1000 cross sections for $\tilde{\chi}_1^\pm$ -coannihilation (compressed):

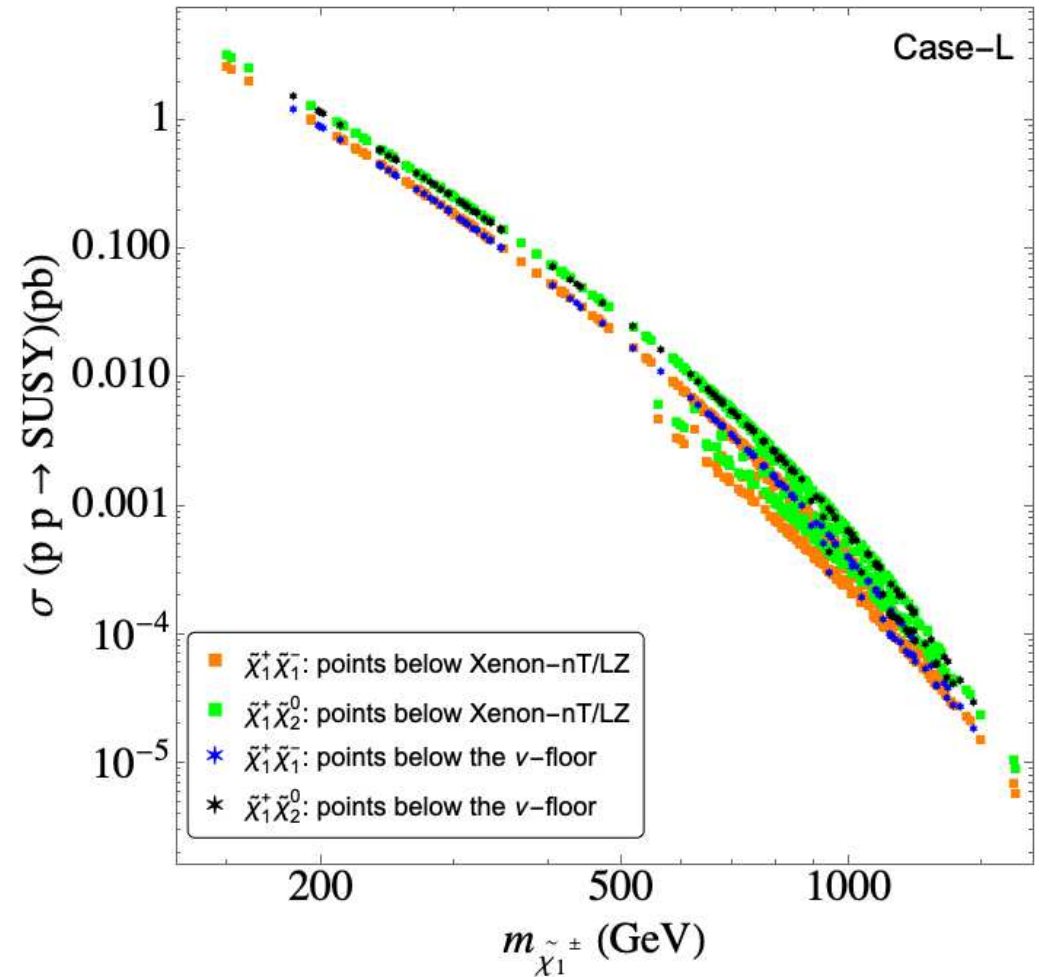
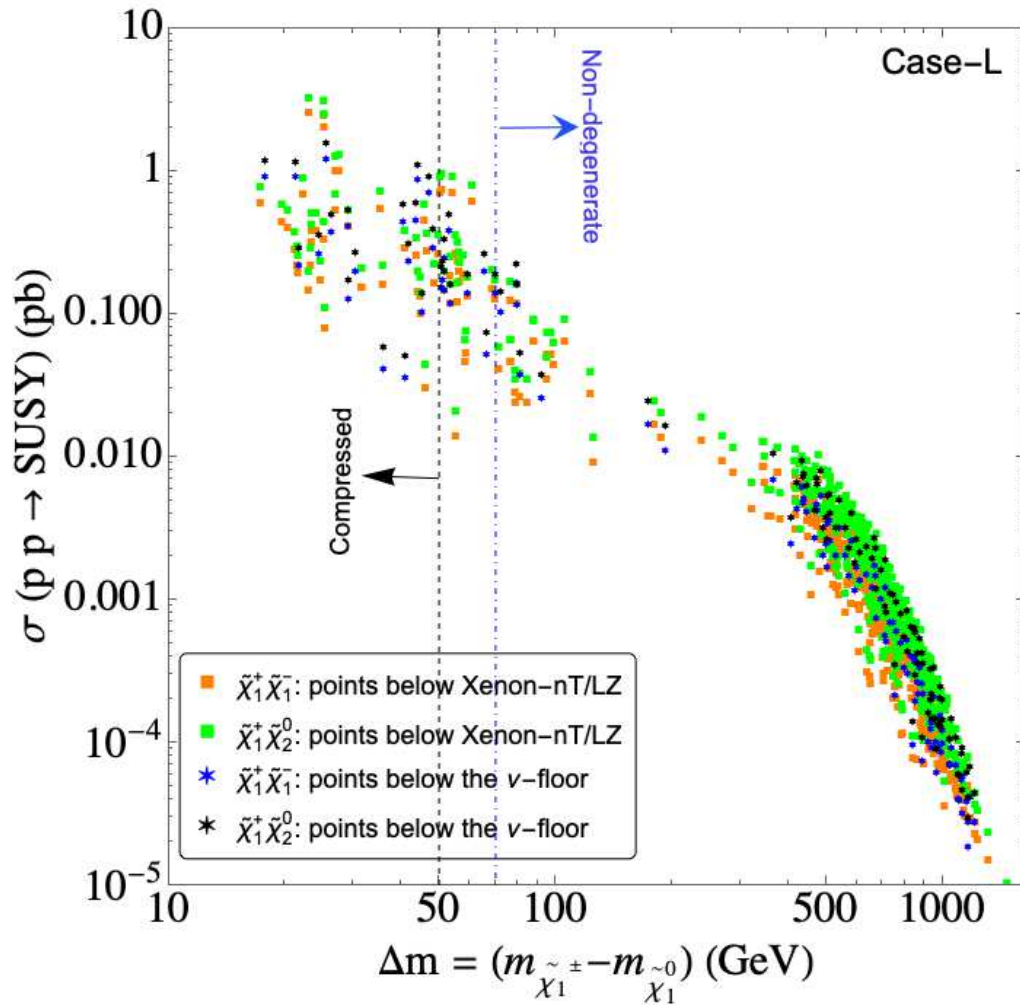
[M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ ILC1000 can cover everything!

(HL-)LHC cross sections for \tilde{l} -coannihilation case-L (non-compressed):

[M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



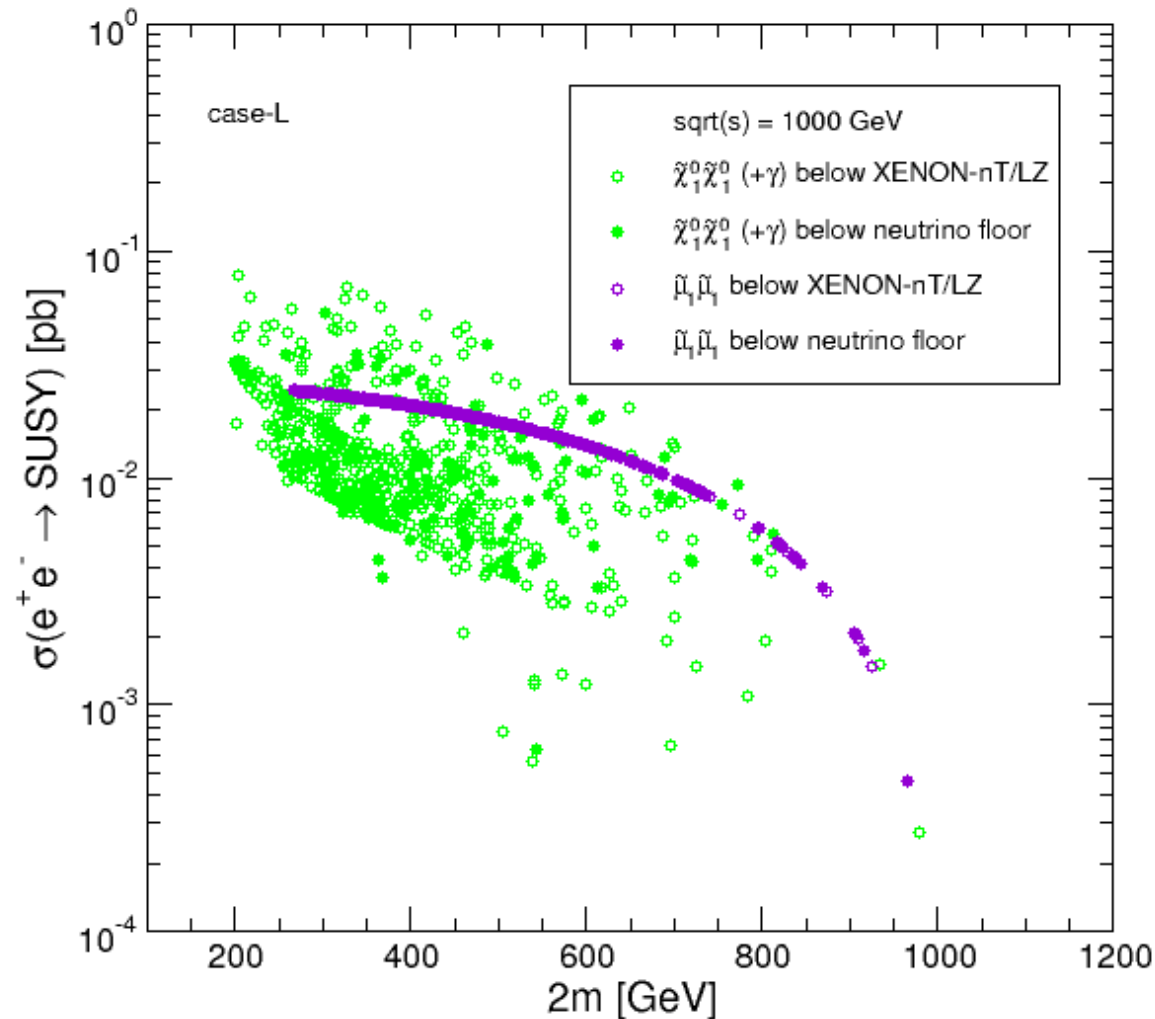
\Rightarrow XS above 0.01 fb \Rightarrow more than 30 events

\Rightarrow no improvement for “BNF” points!

\Rightarrow high-energy e^+e^- collider needed (CLIC3000)!

ILC1000 cross sections for \tilde{l} -coannihilation case-L (compressed):

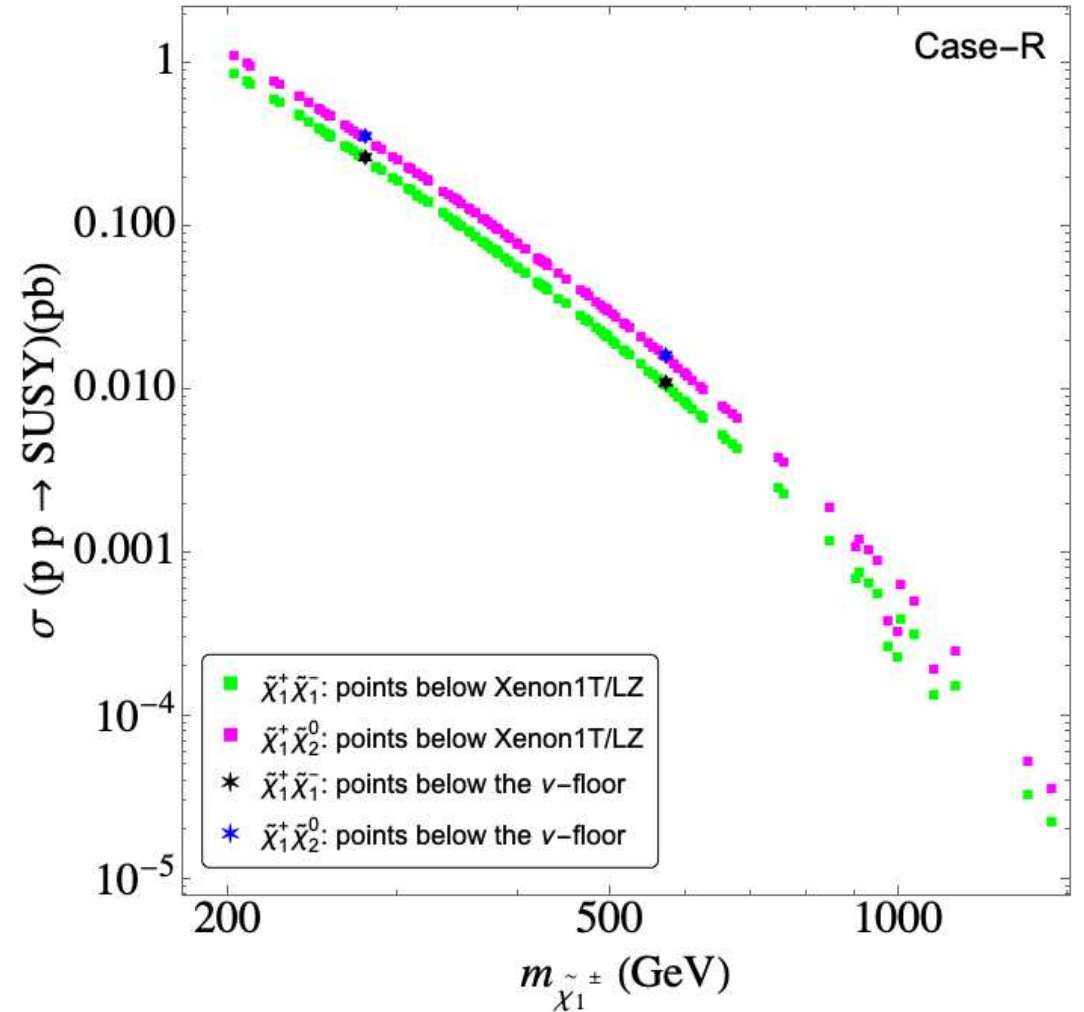
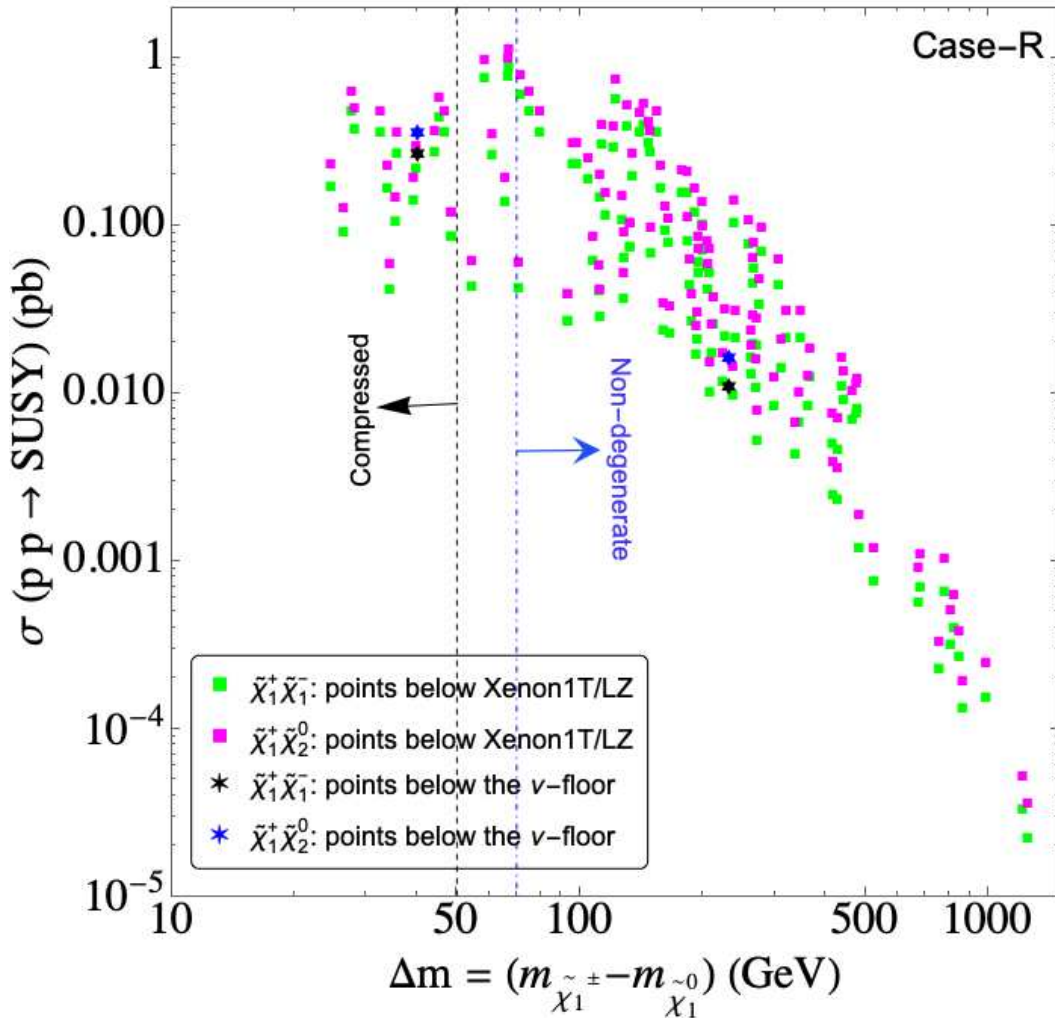
[M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ ILC1000 can cover everything!

(HL-)LHC cross sections for \tilde{l} -coannihilation case-R (non-compressed):

[M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



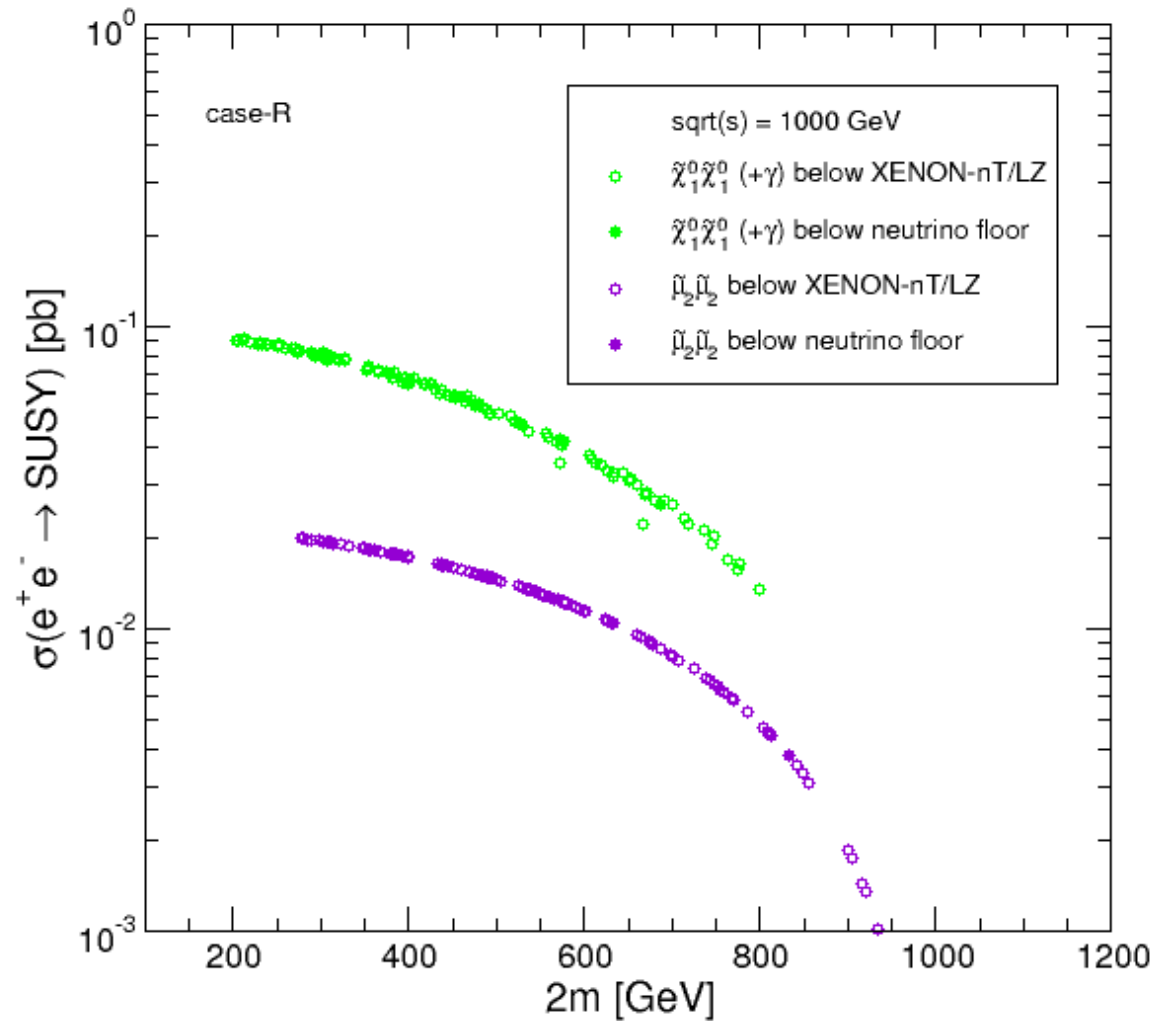
\Rightarrow XS above 0.04 fb \Rightarrow more than 120 events

\Rightarrow very good for “BNF” points: XS above 10 fb

But: detailed (HL-)LHC analysis missing! (spectra can be compressed!)

ILC1000 cross sections for \tilde{l} -coannihilation case-R (compressed):

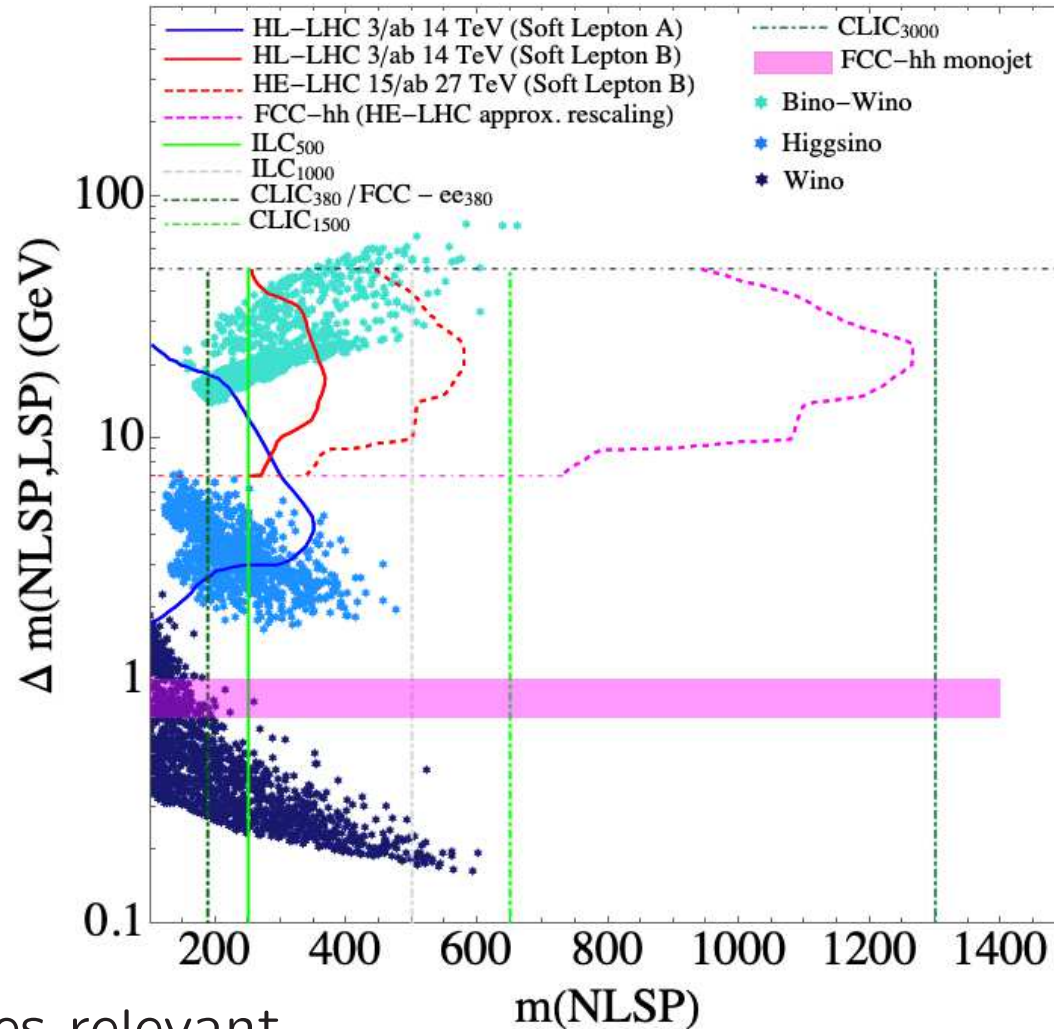
[M. Chakraborti, S.H., I. Saha, C. Schappacher '21]



⇒ ILC1000 can cover everything!

Compressed spectra at current and future colliders

Higgsino, wino and bino/wino DM:



- current searches relevant
- HL-LHC searches can cover some part of the parameter space
- ILC/CLIC needed to cover these scenarios

4. Conclusinos

- Indirect searches: $(g - 2)_\mu \Rightarrow 4.2 \sigma$ discrepancy
- General idea:
 - scan the EW sector of the MSSM with all constraints: $(g - 2)_\mu$, DM relic density, DM DD, LHC EW searches
 - **upper limits** on EW masses
- General results:
 - A) bino/wino DM with chargino coann. (DM full)
 - B/C) bino DM with slepton coann. (DM full)
 - D) higgsino DM $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_2^0} \sim m_{\tilde{\chi}_1^\pm} \sim \mu$ (DM upper limit)
 - E) wino DM $m_{\tilde{\chi}_1^0} \sim m_{\tilde{\chi}_1^\pm} \sim M_2$ (DM upper limit)

\Rightarrow clear upper limits, $m_{(N)\text{LSP}} \lesssim 600$ GeV confirmed
- Direct Detection experiments can cover part of parameter space
 - **ILC** can cover **fully** the remaining points
 - (HL-)LHC has problems with compressed spectra
 - **ILC/CLIC** can “easily” **cover compressed spectra**

A photograph of a man with reddish hair looking up at a full-body Darth Vader costume. The scene is set in a dark, industrial environment with blue lighting from overhead fixtures. The text "Further Questions?" is overlaid in white on the left side of the image.

Further Questions?