

Overview of the Snowmass SMEFT fit results

First ECFA workshop on e^+e^- Higgs/EW/Top Factories

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More details in [2206.08326]



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Introduction

- The SM although being extremely successful does not provide a completely satisfactory description of Nature
- Given the immense number of possibilities of extending the SM, it is specially interesting to analyse the NP in a “model agnostic” way
- The SMEFT provides such a framework although constraining all the operators already at d6 at the same time is not currently possible
- The current available data and the data coming from possible future colliders will be used
- In this work we will show the results of fits on different sectors of the SMEFT
 1. Fit on electroweak and higgs sector
 2. Fit on electroweak sector and 4-fermion operators
 3. Fit on bosonic CPV operators
 4. Fit on on top-quark sector

Higgs + EW fit including helicity conserving 4-fermion operators (M. Peskin's talk): Fixing the SMEFT Lagrangian with data from e^+e^- Higgs factories

SMEFT operators in the Warsaw basis

Operator	Notation	Operator	Notation
$(\overline{l_L \gamma_\mu l_L})(\overline{l_L \gamma^\mu l_L)$	$\mathcal{O}_{ll}^{(1)}$		
$(\overline{q_L \gamma_\mu q_L})(\overline{q_L \gamma^\mu q_L)$	$\mathcal{O}_{qq}^{(1)}$	$(\overline{q_L \gamma_\mu T_A q_L})(\overline{q_L \gamma^\mu T_A q_L)$	$\mathcal{O}_{qq}^{(8)}$
$(\overline{l_L \gamma_\mu l_L})(\overline{q_L \gamma^\mu q_L)$	$\mathcal{O}_{la}^{(1)}$	$(\overline{l_L \gamma_\mu \sigma_a l_L})(\overline{q_L \gamma^\mu \sigma_a q_L)$	$\mathcal{O}_{la}^{(2)}$
$(\overline{e_R \gamma_\mu e_R})(\overline{e_R \gamma^\mu e_R)$	\mathcal{O}_{ee}		
$(\overline{u_R \gamma_\mu u_R})(\overline{u_R \gamma^\mu u_R)$	$\mathcal{O}_{uu}^{(1)}$	$(\overline{d_R \gamma_\mu d_R})(\overline{d_R \gamma^\mu d_R)$	$\mathcal{O}_{dd}^{(1)}$
$(\overline{u_R \gamma_\mu u_R})(\overline{d_R \gamma^\mu d_R)$	$\mathcal{O}_{ud}^{(1)}$	$(\overline{u_R \gamma_\mu T_A u_R})(\overline{d_R \gamma^\mu T_A d_R)$	$\mathcal{O}_{ud}^{(8)}$
$(\overline{e_R \gamma_\mu e_R})(\overline{u_R \gamma^\mu u_R)$	\mathcal{O}_{eu}	$(\overline{e_R \gamma_\mu e_R})(\overline{d_R \gamma^\mu d_R)$	\mathcal{O}_{ed}
$(\overline{l_L \gamma_\mu l_L})(\overline{e_R \gamma^\mu e_R)$	\mathcal{O}_{le}	$(\overline{q_L \gamma_\mu q_L})(\overline{e_R \gamma^\mu e_R)$	\mathcal{O}_{qe}
$(\overline{l_L \gamma_\mu l_L})(\overline{u_R \gamma^\mu u_R)$	\mathcal{O}_{lu}	$(\overline{l_L \gamma_\mu l_L})(\overline{d_R \gamma^\mu d_R)$	\mathcal{O}_{ld}
$(\overline{q_L \gamma_\mu q_L})(\overline{u_R \gamma^\mu u_R)$	$\mathcal{O}_{qu}^{(1)}$	$(\overline{q_L \gamma_\mu T_A q_L})(\overline{u_R \gamma^\mu T_A u_R)$	$\mathcal{O}_{qu}^{(8)}$
$(\overline{q_L \gamma_\mu q_L})(\overline{d_R \gamma^\mu d_R)$	$\mathcal{O}_{qd}^{(1)}$	$(\overline{q_L \gamma_\mu T_A q_L})(\overline{d_R \gamma^\mu T_A d_R)$	$\mathcal{O}_{qd}^{(8)}$
$(\overline{l_L e_R})(\overline{d_R q_L)$	\mathcal{O}_{lelq}		
$(\overline{q_L u_R}) i\sigma_2 (\overline{q_L d_R})^T$	$\mathcal{O}_{qud}^{(1)}$	$(\overline{q_L T_A u_R}) i\sigma_2 (\overline{q_L T_A d_R})^T$	$\mathcal{O}_{qud}^{(8)}$
$(\overline{l_L e_R}) i\sigma_2 (\overline{q_L u_R})^T$	\mathcal{O}_{lequ}	$(\overline{l_L u_R}) i\sigma_2 (\overline{q_L e_R})^T$	$\mathcal{O}_{qel u}$

CP-even dim 6 ops. interfering with SM

EWPO **EW diboson** **Higgs** **Top (Had. Coll., Lept. Coll.)**

Operator	Notation	Operator	Notation
$(\phi^\dagger \phi) \square (\phi^\dagger \phi)$	$\mathcal{O}_{\phi \square}$	$\frac{1}{3} (\phi^\dagger \phi)^3$	\mathcal{O}_ϕ
$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\overline{l_L \gamma^\mu l_L)$	$\mathcal{O}_{\phi l}^{(1)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu^2 \phi) (\overline{l_L \gamma^\mu \sigma_a l_L)$	$\mathcal{O}_{\phi l}^{(3)}$
$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\overline{e_R \gamma^\mu e_R)$	$\mathcal{O}_{\phi e}^{(1)}$		
$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\overline{q_L \gamma^\mu q_L)$	$\mathcal{O}_{\phi q}^{(1)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu^2 \phi) (\overline{q_L \gamma^\mu \sigma_a q_L)$	$\mathcal{O}_{\phi q}^{(3)}$
$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\overline{u_R \gamma^\mu u_R)$	$\mathcal{O}_{\phi u}^{(1)}$	$(\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\overline{d_R \gamma^\mu d_R)$	$\mathcal{O}_{\phi d}^{(1)}$
$(\phi^\dagger i \sigma_2 i D_\mu \phi) (\overline{u_R \gamma^\mu d_R)$	$\mathcal{O}_{\phi ud}$		
$(\overline{l_L \sigma^{\mu\nu} e_R}) \phi B_{\mu\nu}$	\mathcal{O}_{eB}	$(\overline{l_L \sigma^{\mu\nu} e_R}) \sigma^a \phi W_{\mu\nu}^a$	\mathcal{O}_{eW}
$(q_L \sigma^{\mu\nu} u_R) \phi B_{\mu\nu}$	\mathcal{O}_{uB}	$(q_L \sigma^{\mu\nu} u_R) \sigma^a \phi W_{\mu\nu}^a$	\mathcal{O}_{uW}
$(q_L \sigma^{\mu\nu} d_R) \phi B_{\mu\nu}$	\mathcal{O}_{dB}	$(q_L \sigma^{\mu\nu} d_R) \sigma^a \phi W_{\mu\nu}^a$	\mathcal{O}_{dW}
$(\overline{q_L \sigma^{\mu\nu} \lambda^a u_R}) \phi G_{\mu\nu}^A$	\mathcal{O}_{uG}	$(\overline{q_L \sigma^{\mu\nu} \lambda^a d_R}) \phi G_{\mu\nu}^A$	\mathcal{O}_{dG}
$(\phi^\dagger \phi) (\overline{l_L} \phi e_R)$	$\mathcal{O}_{e\phi}$		
$(\phi^\dagger \phi) (\overline{q_L} \phi u_R)$	$\mathcal{O}_{u\phi}$	$(\phi^\dagger \phi) (\overline{q_L} \phi d_R)$	$\mathcal{O}_{d\phi}$
$(\phi^\dagger D_\mu \phi) ((D^\mu \phi)^\dagger \phi)$	$\mathcal{O}_{\phi D}$		
$\phi^\dagger \phi B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{\phi B}$	$\phi^\dagger \phi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{\phi \tilde{B}}$
$\phi^\dagger \phi W_{\mu\nu}^a W^{a\mu\nu}$	$\mathcal{O}_{\phi W}$	$\phi^\dagger \phi \tilde{W}_{\mu\nu}^a W^{a\mu\nu}$	$\mathcal{O}_{\phi \tilde{W}}$
$\phi^\dagger \sigma_a \phi W_{\mu\nu}^a B^{\mu\nu}$	\mathcal{O}_{WB}	$\phi^\dagger \sigma_a \phi \tilde{W}_{\mu\nu}^a B^{\mu\nu}$	$\mathcal{O}_{\tilde{W}B}$
$\phi^\dagger \phi G_{\mu\nu}^A G^{A\mu\nu}$	$\mathcal{O}_{\phi G}$	$\phi^\dagger \phi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$\mathcal{O}_{\phi \tilde{G}}$
$\varepsilon_{abc} W_\mu^a W_\nu^b W_\rho^c W^\mu W^\nu$	\mathcal{O}_W	$\varepsilon_{abc} \tilde{W}_\mu^a W_\nu^b W_\rho^c W^\mu W^\nu$	$\mathcal{O}_{\tilde{W}}$
$f_{ABC} G_\mu^A G_\nu^B G_\rho^C G^\mu G^\nu$	\mathcal{O}_G	$f_{ABC} \tilde{G}_\mu^A G_\nu^B G_\rho^C G^\mu G^\nu$	$\mathcal{O}_{\tilde{G}}$

Slide from J. de Blas at Seattle Snowmass Summer Study

Future Facilities Considered

Machine	Pol. (e^-, e^+)	Energy	Luminosity
HL-LHC	Unpolarised	14 TeV	3 ab^{-1}
ILC	$(\mp 80\%, \pm 30\%)$	250 GeV	2 ab^{-1}
		350 GeV	0.2 ab^{-1}
	$(\mp 80\%, \pm 20\%)$	500 GeV	4 ab^{-1}
		1 TeV	8 ab^{-1}
CLIC	$(\pm 80\%, 0\%)$	380 GeV	1 ab^{-1}
		1.5 TeV	2.5 ab^{-1}
		3 TeV	5 ab^{-1}
FCC- ee	Unpolarised	Z-pole	150 ab^{-1}
		$2m_W$	10 ab^{-1}
		240 GeV	5 ab^{-1}
		350 GeV	0.2 ab^{-1}
		365 GeV	1.5 ab^{-1}
CEPC	Unpolarised	Z-pole	100 ab^{-1}
		$2m_W$	6 ab^{-1}
		240 GeV	20 ab^{-1}
		350 GeV	0.2 ab^{-1}
		360 GeV	1 ab^{-1}
MuC	Unpolarised	125 GeV	0.02 ab^{-1}
		3 TeV	3 ab^{-1}
		10 TeV	10 ab^{-1}

Comparison with European Strategy Update (ESU)

- All the data from the ESU has been updated
- In the diboson channels a new parameterisation including all relevant SMEFT coefficients has been used [Grojean, Montull, Rimbau, 1810.05149] [de Blas, Durieux, Grojean, Gu, Paul, 1907.04311]
- The impact of building a future muon collider has been studied
- A new comprehensive fit is performed focusing on 4-fermion interactions at future colliders
- The impact of the future lepton colliders in constraining the bosonic CPV operators has been studied
- Top-quark sector is studied in a dedicated fit

Fits on electroweak and Higgs sector

Observables included

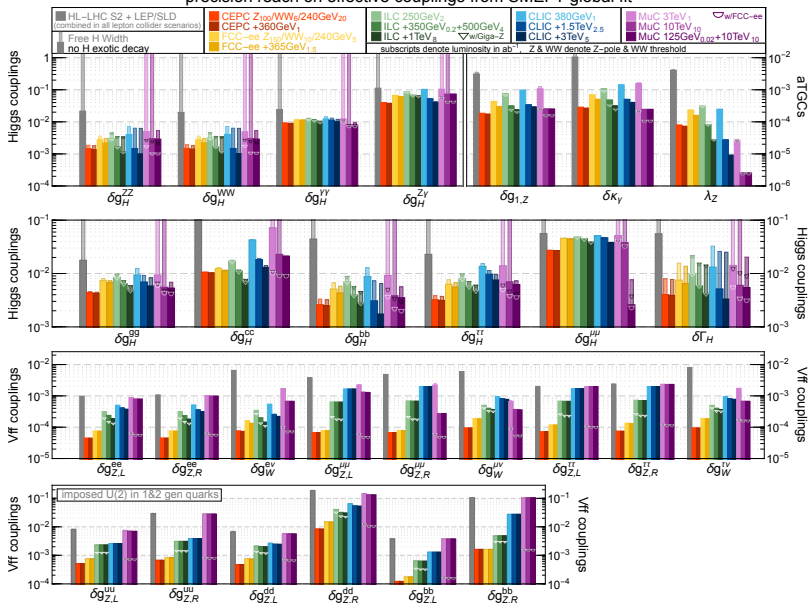
- **Higgs rates:** The results from future colliders have been combined with HL-LHC
- **Electroweak precision observables:** Current measurements have been combined with future colliders
- **Diboson measurements:** Optimal observables analysis for lepton colliders. HL-LHC obtained from [[Grojean, Montull, Riemann, 1810.05149](#)]
- **High energy muon collider measurements:** Only the process $\gamma\gamma \rightarrow W^+W^-$ for the measurements of the W branching fraction has been included

Assumptions

- The effect of 4-fermion operators is mostly negligible in the observables included here (except the 4-lepton operator affecting G_F) and will only be considered in a different fit
- For this sector CP-conservation in the NP effects is also assumed
- The effects of the dipole operators will be considered only in the fit of the top-quark sector
- A $U(2)$ symmetry is imposed in the first two generations quarks for the gauge couplings → Working in relaxing this assumption!
[\[Bresó-Pla, Falkowski, González-Alonso, 2103.12074\]](#)
- Higgs couplings are assumed to be diagonal but independent for different fermion families
- Two scenarios for the Higgs decay are shown:
 1. The Higgs is assumed to decay only to SM particles
 2. The Higgs width is considered as a free parameter

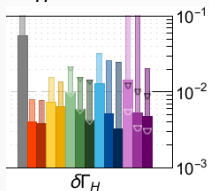
Results

precision reach on effective couplings from SMEFT global fit

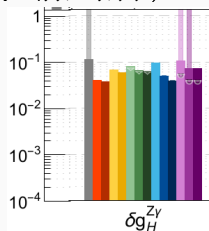


Results: Highlights

A low energy run accessing $e^+e^- \rightarrow HZ$ becomes highly relevant to measure Γ_H

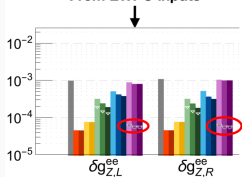


HL-LHC dominates the constraints on rare decays ($\gamma\gamma, Z\gamma, \mu\mu$)

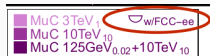
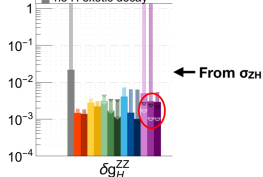


There is an excellent complementarity between e^+e^- and $\mu^+\mu^-$ colliders

From EWPO inputs

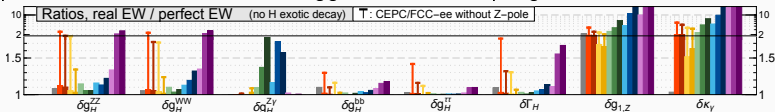


Free H Width
no H exotic decay

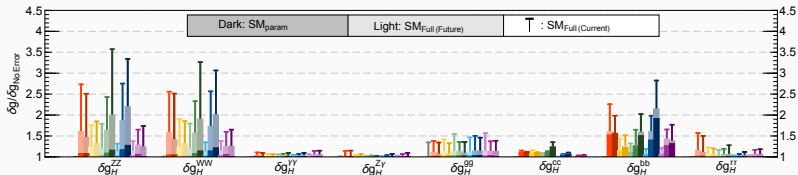
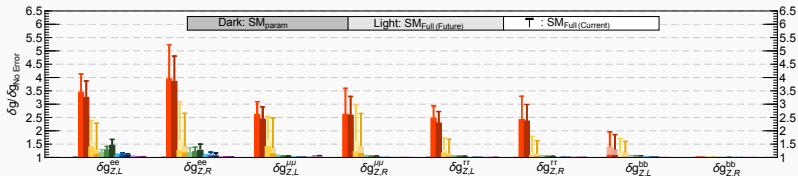


Results: Impact of uncertainties

Impact of EW uncertainties in Higgs and aTG couplings



Impact of theoretical uncertainties in the fit



Fits on electroweak sector and
4-fermion operators

Observables included

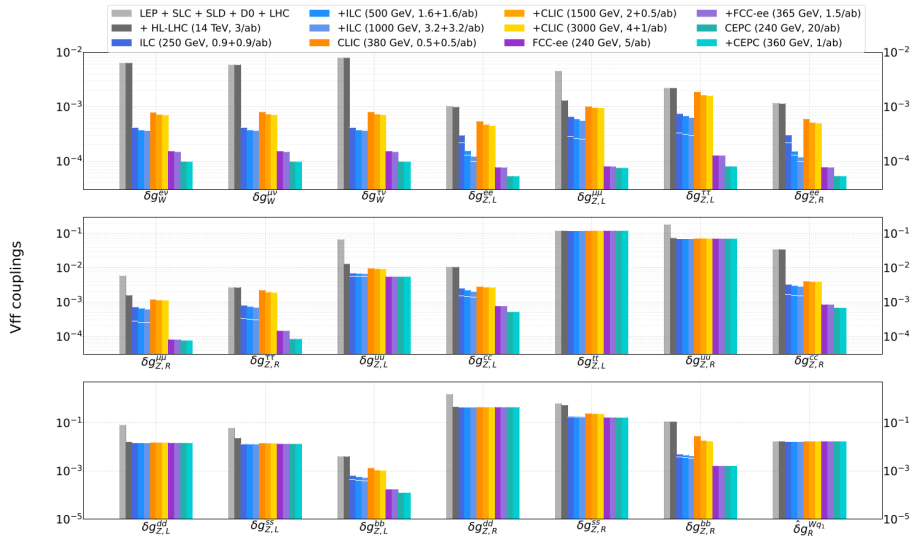
- **Z- and W-pole observables:** Sensitive to the electroweak vertex corrections.
 1. Z-pole observables from LEP-1, A_s from SLD, and R_{uc}
 2. W-pole, LEP-2 data for leptonic branching ratios, R_{Wc} , and R_σ
- **High-energy observables for 4-fermion operators:** LEP-2 data included. Production cross section and A_{FB} for $\mu^+\mu^-$, $\tau^+\tau^-$ and quark final states and, in addition, differential cross section for e^+e^- final state.
- **Low-energy precision observables:** To include these observables a matching with the LEFT must be done with the appropriate running, which is specially relevant for $2\ell 2q$ type operators

Full list of observables in the backup slides

Assumptions

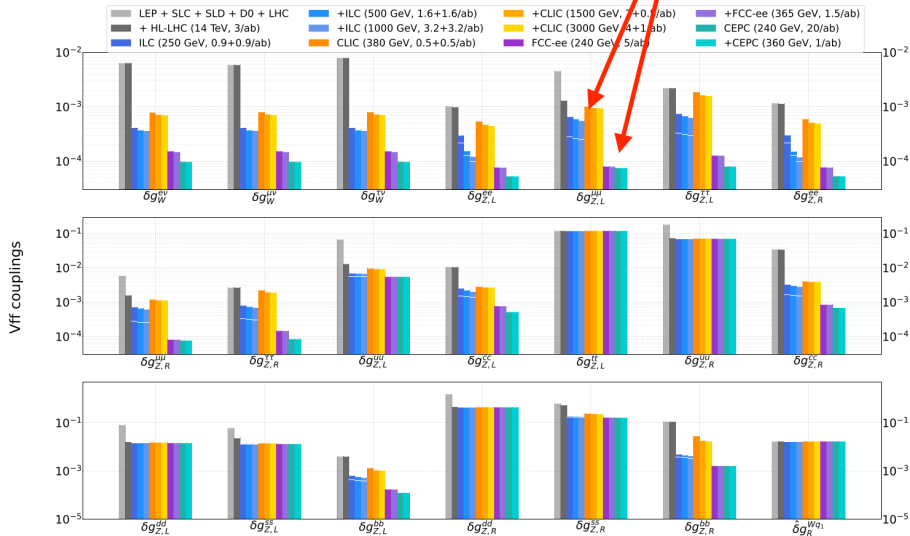
- No flavour symmetries imposed in the EW part (contrary as before)
- Only considered flavour conserving 4-fermion operators
- It is not possible to completely close the fit and several flat directions emerge:
 1. **Flat[top]**: Since LEP was run below the top-pair threshold a flat direction in the third family of $2\ell 2q$ type operators appears
 2. **Flat[strange]($\times 3$)**: The σ and A_{FB} is available for $c\bar{c}$ but not for $s\bar{s}$ generating flat directions in the second family of $2\ell 2q$
 3. **Flat[parity]($\times 5$)**: The $(e\gamma_\mu\gamma_5 e)(q_1\gamma_\mu\gamma_5 q_1)$ and $(\nu_L\gamma_\mu\nu_L)(q_1\gamma_\mu\gamma_5 q_1)$ operators remain unconstrained at the low-energy parity-violating scattering experiments or LEP
 4. **Flat[SPS]**: The muon scattering off the Carbon target at CERN SPS is insufficient to disentangle the contributions from $\mathcal{O}_{eq,eu,ed}$
 5. **Flat[trident]**: The trident process is the only low-energy channel sensitive to the four-muon operators $\mathcal{O}_{\ell\ell,le}$
 6. **Flat[flavour]**: The $\pi_{\mu 2}$ decay rate only provides one constraint on $\varepsilon_P^{d\mu}$ (which depends on \mathcal{O}_{ledq} and \mathcal{O}_{lequ}) from the flavor observable R_π

Results for Vff couplings



Results for Vff couplings

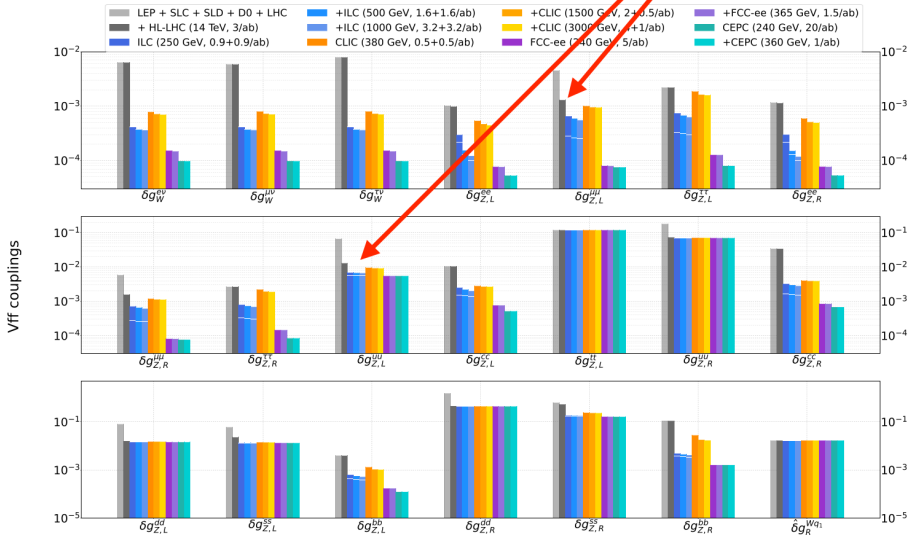
Luminosity wins (through radiative return)



Slide from Y. Du at Seattle Snowmass Summer Study

Results for Vff couplings

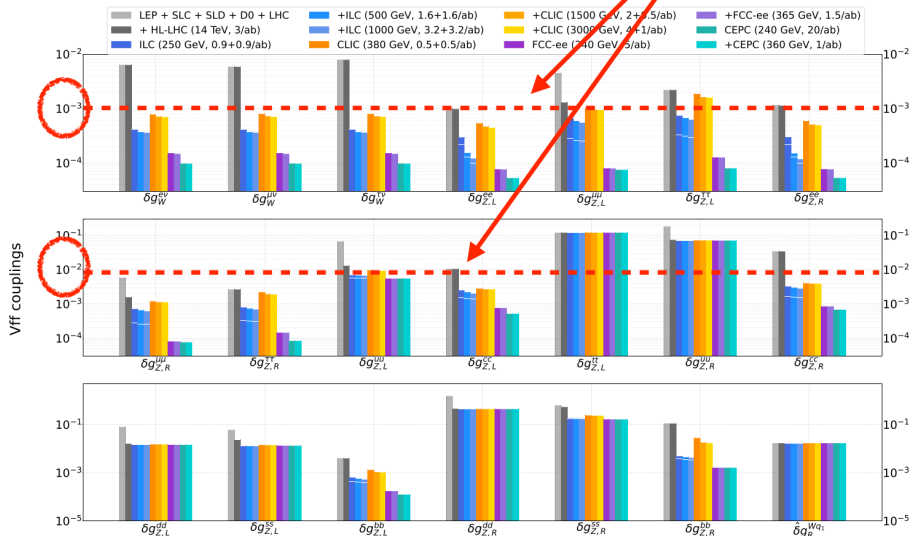
D0 + A_{FB} at the (HL-)LHC relaxes the U2 assumption & improve the fit



Slide from Y. Du at Seattle Snowmass Summer Study

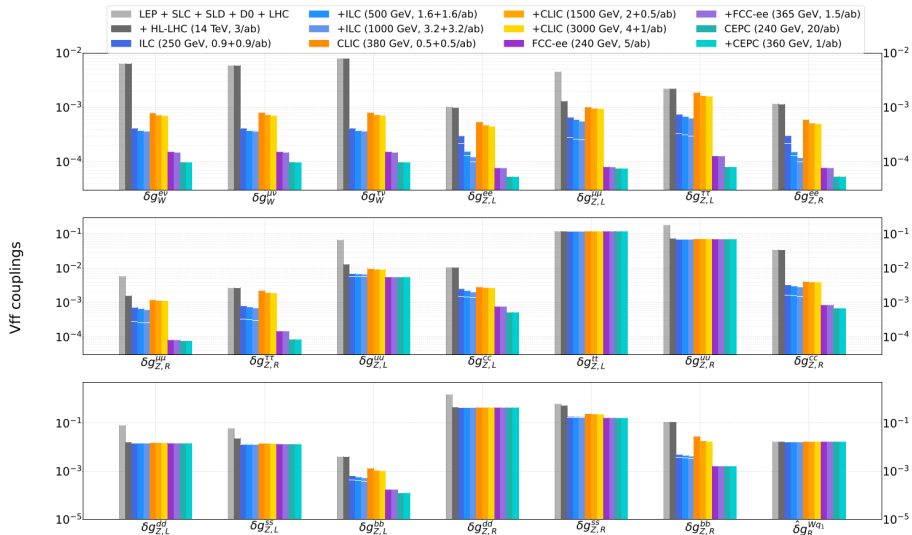
Results for Vff couplings

$\mathcal{O}(10)$ weaker: Limited by the missing projections of R_{UC} , A_{FB}^{SS} , σ^{SS}



Slide from Y. Du at Seattle Snowmass Summer Study

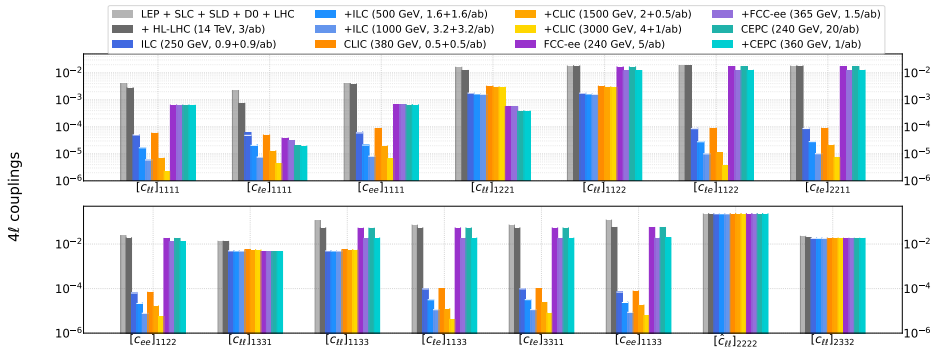
Results for Vff couplings



CKM unitarity test

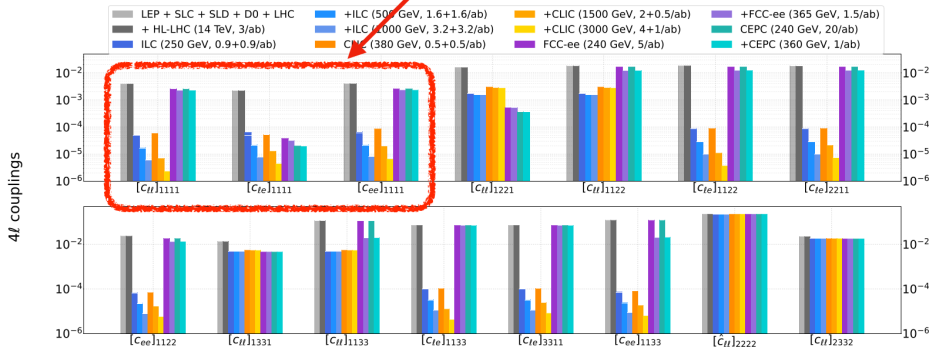
Slide from Y. Du at Seattle Snowmass Summer Study

Results for 4ℓ couplings



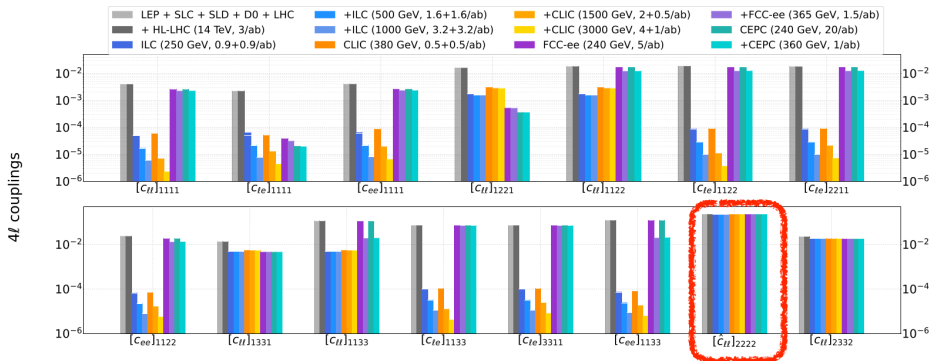
Results for 4ℓ couplings

Beam polarization is the key in beating the (HL-)LHC and also circular colliders



Slide from Y. Du at Seattle Snowmass Summer Study

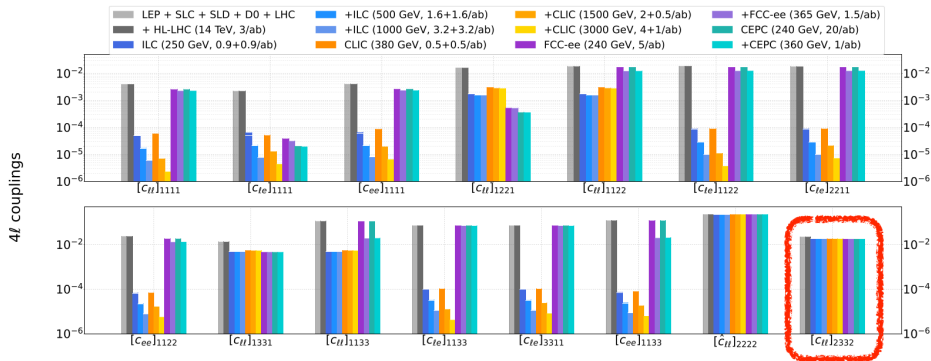
Results for 4ℓ couplings



One input from neutrino trident production at CCFR. Muon colliders/FASERν could play the role of lifting this flat direction

Slide from Y. Du at Seattle Snowmass Summer Study

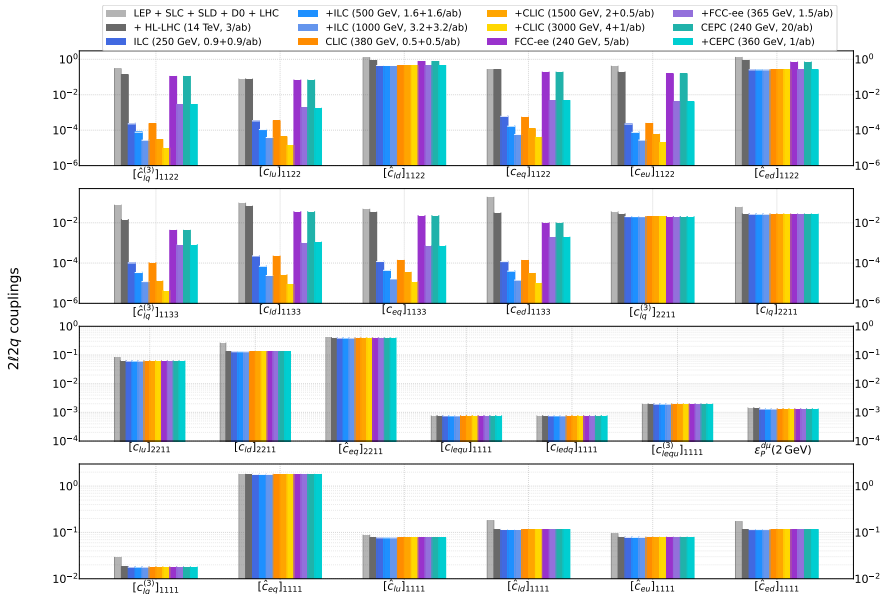
Results for 4ℓ couplings



Limited by leptonic τ decay, but is the only one sensitive to this operator. A muon collider also helps

Slide from Y. Du at Seattle Snowmass Summer Study

Results for $2\ell 2q$ couplings



Fits on bosonic CPV operators

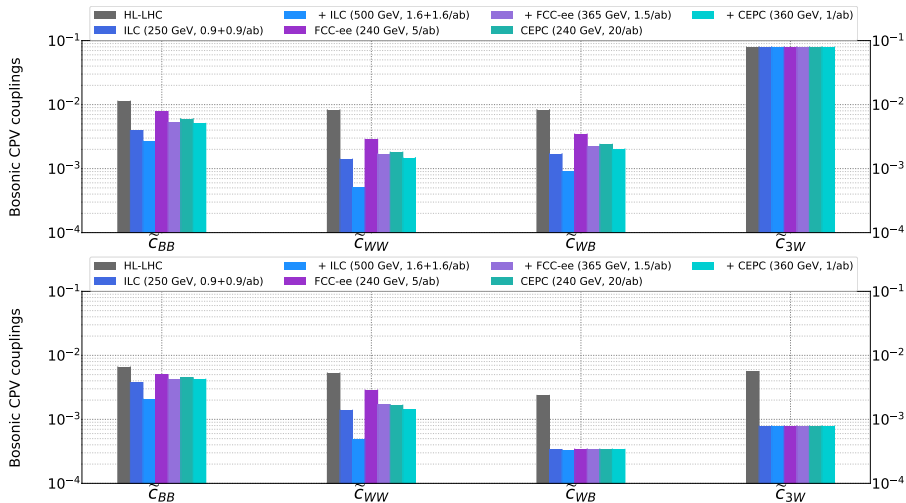
Operators and observables

$$\begin{aligned}
 \mathcal{O}_{\tilde{G}} &= f^{ABC} \tilde{G}_{\mu}^{Av} G_{\nu}^{B\rho} G_{\rho}^{C\mu} & \mathcal{O}_{\varphi\tilde{G}} &= \varphi^{\dagger} \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu} & \mathcal{O}_{\varphi\tilde{W}} &= \varphi^{\dagger} \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu} \\
 \mathcal{O}_{\varphi\tilde{B}} &= \varphi^{\dagger} \varphi \tilde{B}_{\mu\nu} B^{\mu\nu} & \mathcal{O}_{\varphi\tilde{W}B} &= \varphi^{\dagger} \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu} & \mathcal{O}_{\tilde{W}} &= \varepsilon^{IJK} \tilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}
 \end{aligned}$$

- $\mathcal{O}_{\tilde{G}}$ and $\mathcal{O}_{\varphi\tilde{G}}$ will not be included in the fit \rightarrow strongly constraint from neutron and diamagnetic atoms EDMs
- The OPAL measurements of $e^+e^- \rightarrow W^+W^-$ constrains the aTGCs $\mathcal{O}_{\varphi\tilde{W}B}$ and $\mathcal{O}_{\tilde{W}} \rightarrow$ Although weak are essential to lift flat directions
- Stringent bounds can be obtained from the angular distribution of $h \rightarrow 4\ell$
- In future lepton colliders important constraints (on $\mathcal{O}_{\varphi\tilde{W}}$, $\mathcal{O}_{\varphi\tilde{B}}$ and $\mathcal{O}_{\varphi\tilde{W}B}$) are obtained from the angular asymmetries $A_{\phi}^{(1)}$ and $A_{\phi}^{(2)}$ on $e^+e^- \rightarrow ZH$ production

Results

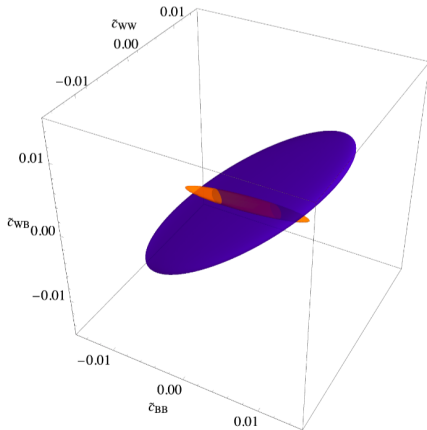
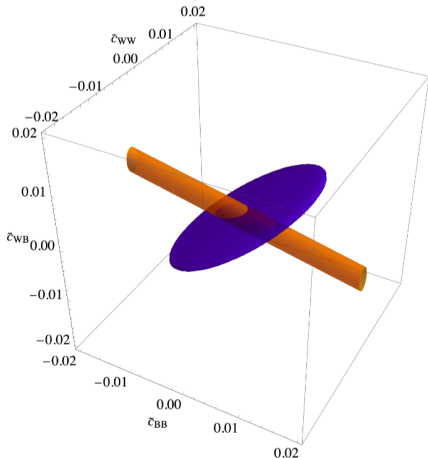
The bottom plot comes from assuming that the OPAL precision on aTGCs is improved by a factor of 10 (100) for HL-LHC (future colliders)



Results: Complementarity HL-LHC/Future e^+e^-

Blue \rightarrow HL-LHC // Orange \rightarrow ILC250

Left \rightarrow current fit // Right \rightarrow Assuming OPAL precision on aTGCs is improved by a factor of 10 (100) for HL-LHC (future colliders)



Fits on top-quark sector

All the details in [2205.02140] and my previous talk:
Prospects for the measurement of top-quark couplings

Observables

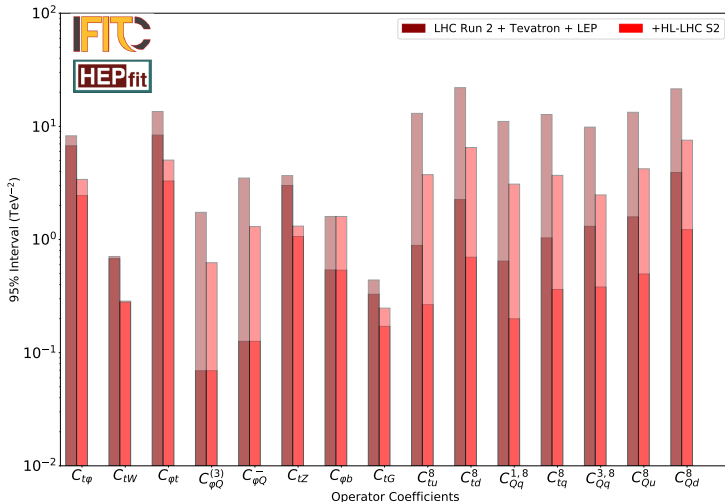
- Pair production of top quarks and in association with SM bosons at LHC
- Single top-quark production at LHC and Tevatron
- Single top-quark production in association with electroweak bosons at LHC
- W boson helicity fractions from top-quark decay at LHC
- R_b and A_{FBLR}^{bb} at LEP and future lepton colliders
- Optimal observables that maximally exploit the information in the fully differential $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+\bar{b}W^-$ distribution at future lepton colliders [[G. Durieux, M. Perelló, M. Vos, C. Zhang 1807.02121](#)]
- Inclusive cross section of $e^+e^- \rightarrow t\bar{t}H$ at future lepton colliders

Assumptions

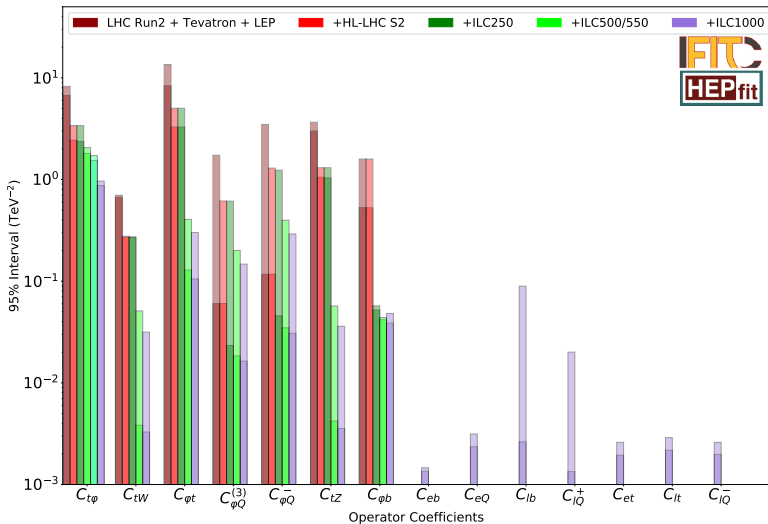
- We will only consider here the operators that affect the top quark and those that affect the bottom quark and enter in the same processes
- CP-conservation in the NP effects is assumed for this part of the fit
- A $U(2)$ symmetry is imposed for the first two generations of quarks
- We will only consider the linear terms of the dimension six operators
- The results will be presented in terms of the Wilson coefficients of the SMEFT

Results at HL-LHC

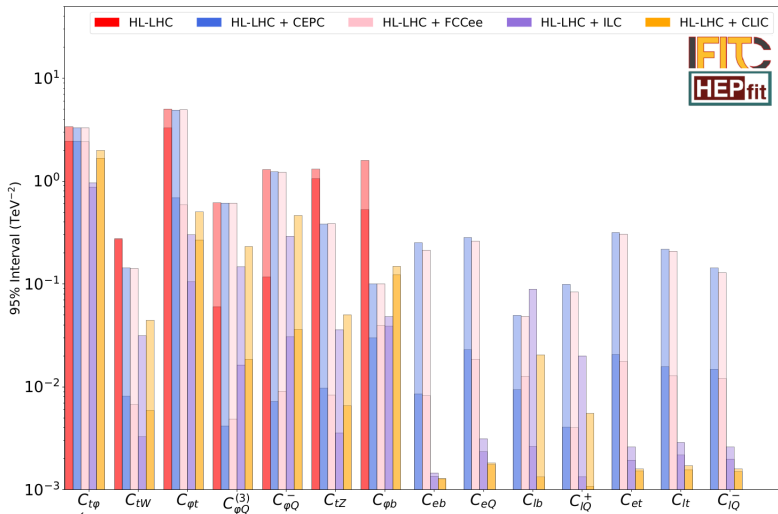
Shadowed (solid) bars → marginalised from global (individual) fit



Results at different energies of a future lepton collider



Results at future lepton colliders



$$\delta y_t = -\frac{C_{t\phi} v^2}{2 \Lambda^2}$$

Values in % units	Operator Coefficients						
	LHC	HL-LHC	ILC500	ILC550	ILC1000	CLIC	
δy_t Global fit	6.12	2.53	1.57	1.30	0.739	1.48	
δy_t Indiv. fit	5.08	1.85	1.41	1.17	0.705	1.26	

Summary

- We performed a few global SMEFT fits with a well defined subset of dimension-6 operators in the Warsaw basis
- Future lepton colliders can advance significantly our understanding of the properties of various SM particles
- Future e^+e^- -machines improve the precision of Higgs measurements (a factor of 2-10) and can test Γ_H as a free parameter
- Muon colliders can offer comparable precision in the cases where, either Γ_H is fixed or the 125 GeV run is combined
- Electroweak effective couplings for W and Z can be improved by a few orders of magnitude at future e^+e^- colliders over what we know of today
- There are important synergies between EWPOs and direct Higgs obs.
- The 4-fermion interactions the reaches are significantly better at linear e^+e^- than circular
- There are important synergies with low-energy measurements without which certain degeneracies can not be lift
- The degeneracies in $eett$ contact interactions can not be lift without running at two different energies well above tt -threshold
- Many top-quark measurements at (HL-)LHC are helpful in the global fit for improving the precision of top-quark EW couplings

Thanks for your attention!



and special thanks to the other
members of the team!

Back up

Effective couplings

- For the Higgs and EW fit the results are shown in terms of electric couplings
- Higgs effective couplings:

$$g_{HX}^{\text{eff}^2} \equiv \frac{\Gamma_{H \rightarrow X}}{\Gamma_{H \rightarrow X}^{\text{SM}}}$$

- Electroweak effective couplings

$$\Gamma_{Z \rightarrow e^+ e^-} = \frac{\alpha M_Z}{6 \sin^2 \theta_w \cos^2 \theta_w} (|g_{Zee,L}^{\text{eff}}|^2 + |g_{Zee,R}^{\text{eff}}|^2), \quad A_e = \frac{|g_{Zee,L}^{\text{eff}}|^2 - |g_{Zee,R}^{\text{eff}}|^2}{|g_{Zee,L}^{\text{eff}}|^2 + |g_{Zee,R}^{\text{eff}}|^2}$$

- To further connect with diboson processes the following aTGC are also used

$$\delta g_{1,Z}, \quad \delta \kappa_\gamma, \quad \lambda_Z$$

Z-(W-)pole obs. used in the EW + 4-fermion fit

Observable	Experimental value	SM prediction
Γ_Z [GeV]	2.4952 ± 0.0023	2.4950
σ_{had} [nb]	41.541 ± 0.037	41.484
R_e	20.804 ± 0.050	20.743
R_μ	20.785 ± 0.033	20.743
R_τ	20.764 ± 0.045	20.743
$A_{\text{FB}}^{0,e}$	0.0145 ± 0.0025	0.0163
$A_{\text{FB}}^{0,\mu}$	0.0169 ± 0.0013	0.0163
$A_{\text{FB}}^{0,\tau}$	0.0188 ± 0.0017	0.0163
R_b	0.21629 ± 0.00066	0.21578
R_c	0.1721 ± 0.0030	0.17226
A_b^{FB}	0.0992 ± 0.0016	0.1032
A_c^{FB}	0.0707 ± 0.0035	0.0738
A_e	0.1516 ± 0.0021	0.1472
A_μ	0.142 ± 0.015	0.1472
A_τ	0.136 ± 0.015	0.1472
A_e	0.1498 ± 0.0049	0.1472
A_τ	0.1439 ± 0.0043	0.1472
A_b	0.923 ± 0.020	0.935
A_c	0.670 ± 0.027	0.668
A_s	0.895 ± 0.091	0.935
R_{uc}	0.166 ± 0.009	0.1724
m_W [GeV]	80.385 ± 0.015	80.364
Γ_W [GeV]	2.085 ± 0.042	2.091
$\text{Br}(W \rightarrow e\nu)$	0.1071 ± 0.0016	0.1083
$\text{Br}(W \rightarrow \mu\nu)$	0.1063 ± 0.0015	0.1083
$\text{Br}(W \rightarrow \tau\nu)$	0.1138 ± 0.0021	0.1083
R_{Wc}	0.49 ± 0.04	0.50
R_σ	0.998 ± 0.041	1.000

High-energy 4-fermion obs. used in the EW + 4-fermion fit

Observable	Experimental value
$\sigma(\mu^+\mu^-)$	$f(s)$
$\sigma(\tau^+\tau^-)$	$f(s)$
$\sum_{q \neq t} \sigma(q\bar{q})$	$f(s)$
$\sigma(b\bar{b})$	$f(s)$
$\sigma(c\bar{c})$	$f(s)$
$\frac{\sigma_{\text{FB}}(b\bar{b})}{\sum_{q \neq t} \sigma(q\bar{q})}$	$f(s)$
$\frac{\sigma_{\text{FB}}(c\bar{c})}{\sum_{q \neq t} \sigma(q\bar{q})}$	$f(s)$
$A_{\text{FB}}(\mu^+\mu^-)$	$f(s)$
$A_{\text{FB}}(\tau^+\tau^-)$	$f(s)$
$\frac{d\sigma}{d\cos\theta}(\text{Bhabha})$	$f(s, \cos\theta)$

Low-energy 4-fermion obs. used in the EW + 4-fermion fit

Process	Observable	Experimental value	Ref.	SM prediction	
$(-)$ $\nu_\mu - e^-$ scattering	$g_{LV}^{\mu e}$	-0.035 ± 0.017	CHARM-II	-0.0396	
	$g_{LA}^{\mu e}$	-0.503 ± 0.017		-0.5064	
τ decay	$\frac{G_F^2}{G_F^2}$	1.0029 ± 0.0046	PDG2014	1	
	$\frac{G_F^2}{G_F^2}$	0.981 ± 0.018			
	$\frac{G_F^2}{G_F^2}$	0.981 ± 0.018			
Neutrino scattering	$R_{V\mu}$	0.3093 ± 0.0031	CHARM ($r = 0.456$)	0.3156	
	$R_{\bar{V}\mu}$	0.390 ± 0.014		0.370	
	$R_{V\mu}$	0.3072 ± 0.0033	CDHS ($r = 0.393$)	0.3091	
	$R_{\bar{V}\mu}$	0.382 ± 0.016		0.380	
	κ	0.5820 ± 0.0041	CCFR	0.5830	
$R_{V_e \bar{V}_e}$	$0.406^{+0.145}_{-0.135}$	CHARM	0.33		
Parity-violating scattering	$(\frac{2}{s_w})^2 M_{\text{inter}}$	0.2397 ± 0.0013	SLAC-E158	0.2381 ± 0.0006	
	$Q_W^{\text{CS}}(55, 78)$	-72.62 ± 0.43	PDG2016	-73.25 ± 0.02	
	$Q_W^{\text{Q}}(1, 0)$	0.064 ± 0.012	QWEAK	0.0708 ± 0.0003	
	A_1	$(-91.1 \pm 4.3) \times 10^{-6}$	PVDIS	$(-87.7 \pm 0.7) \times 10^{-6}$	
	A_2	$(-160.8 \pm 7.1) \times 10^{-6}$		$(-158.9 \pm 1.0) \times 10^{-6}$	
	$g_{VA}^{eu} - g_{VA}^{ed}$		-0.042 ± 0.057	SAMPLE ($\sqrt{Q^2} = 200 \text{ MeV}$)	-0.0360
			-0.12 ± 0.074	SAMPLE ($\sqrt{Q^2} = 125 \text{ MeV}$)	0.0265
b_{SPS}		$-(1.47 \pm 0.42) \times 10^{-4} \text{ GeV}^{-2}$	SPS ($\lambda = 0.81$)	$-1.56 \times 10^{-4} \text{ GeV}^{-2}$	
		$-(1.74 \pm 0.81) \times 10^{-4} \text{ GeV}^{-2}$	SPS ($\lambda = 0.66$)	$-1.57 \times 10^{-4} \text{ GeV}^{-2}$	
τ polarization	\mathcal{P}_τ	0.012 ± 0.058	VENUS	0.028	
	$\mathcal{A}_{\mathcal{P}}$	0.029 ± 0.057		0.021	
Neutrino trident production	$\frac{\sigma}{\sigma^{\text{SM}}}(\nu_\mu \gamma^e \rightarrow \nu_\mu \mu^+ \mu^-)$	0.82 ± 0.28	CCFR	1	
$d_I \rightarrow u_j \ell \bar{\nu}_\ell(\gamma)$	\mathcal{E}_{LRSP}^{deJ}	See text		0	
$e^+ e^- \rightarrow f \bar{f}$	δA_{LR}^e	2.0%	SuperKEKB	0.00015	
	δA_{LR}^{μ}	1.5%		-0.0006	
	δA_{LR}^{τ}	2.4%		-0.0006	
	δA_{LR}^c	0.5%		-0.005	
	δA_{LR}^b	0.4%		-0.020	

Wilson coefficients for the 4-fermion operators

2l2q operators ($p, r = 1, 2, 3$)	4l operators ($p < r = 1, 2, 3$)
Chirality conserving	Two flavors
$[O_{\ell q}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(\bar{q}_r \bar{\sigma}^\mu q_r)$	$[O_{\ell\ell}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(\bar{\ell}_r \bar{\sigma}^\mu \ell_r)$
$[O_{\ell q}^{(3)}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \sigma^i \ell_p)(\bar{q}_r \bar{\sigma}^\mu \sigma^i q_r)$	$[O_{\ell\ell}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_r)(\bar{\ell}_r \bar{\sigma}^\mu \ell_p)$
$[O_{\ell u}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(u_r^c \sigma^\mu \bar{u}_r^c)$	$[O_{\ell e}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(e_r^c \sigma^\mu \bar{e}_r^c)$
$[O_{\ell d}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(d_r^c \sigma^\mu \bar{d}_r^c)$	$[O_{\ell e}]_{rrpp} = (\bar{\ell}_r \bar{\sigma}_\mu \ell_r)(e_p^c \sigma^\mu \bar{e}_p^c)$
$[O_{e q}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(\bar{q}_r \bar{\sigma}^\mu q_r)$	$[O_{\ell e}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_r)(e_r^c \sigma^\mu \bar{e}_p^c)$
$[O_{e u}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(u_r^c \sigma^\mu \bar{u}_r^c)$	$[O_{ee}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(e_r^c \sigma^\mu \bar{e}_r^c)$
$[O_{e d}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(d_r^c \sigma^\mu \bar{d}_r^c)$	
Chirality violating	One flavor
$[O_{\ell e q u}]_{pprr} = (\bar{\ell}_p^j \bar{e}_p^c) \varepsilon_{jk} (\bar{q}_r^k \bar{u}_r^c)$	$[O_{\ell\ell}]_{pppp} = \frac{1}{2} (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(\bar{\ell}_p \bar{\sigma}^\mu \ell_p)$
$[O_{\ell e q u}^{(3)}]_{pprr} = (\bar{\ell}_p^j \bar{\sigma}_{\mu\nu} \bar{e}_p^c) \varepsilon_{jk} (\bar{q}_r^k \bar{\sigma}_{\mu\nu} \bar{u}_r^c)$	$[O_{\ell e}]_{pppp} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(e_p^c \sigma^\mu \bar{e}_p^c)$
$[O_{\ell e d q}]_{pprr} = (\bar{\ell}_p^j \bar{e}_p^c)(d_r^c q_r^j)$	$[O_{ee}]_{pppp} = \frac{1}{2} (e_p^c \sigma_\mu \bar{e}_p^c)(e_p^c \sigma^\mu \bar{e}_p^c)$

Flat directions in 4-fermion operators

Flat[top]:

$$[\hat{c}_{\ell q}^{(3)}]_{1133} = [c_{\ell q}^{(3)}]_{1133} + [c_{\ell q}]_{1133}$$

Flat[strange]:

$$[\hat{c}_{\ell q}^{(3)}]_{1122} = [c_{\ell q}^{(3)}]_{1122} - [c_{\ell q}]_{1122},$$

$$[\hat{c}_{\ell d}]_{1122} = [c_{\ell d}]_{1122} + \left(5 - \frac{3g^2}{g'^2}\right) [c_{\ell q}]_{1122} - [\hat{c}_{eq}]_{1111},$$

$$[\hat{c}_{ed}]_{1122} = [c_{ed}]_{1122} - \left(3 - \frac{3g^2}{g'^2}\right) [c_{\ell q}]_{1122} - [\hat{c}_{eq}]_{1111}$$

Flat[parity]:

$$[\hat{c}_{eq}]_{1111} = [c_{eq}]_{1111} + [c_{\ell q}]_{1111},$$

$$[\hat{c}_{\ell u}]_{1111} = [c_{\ell u}]_{1111} + [c_{\ell q}]_{1111} - [\hat{c}_{eq}]_{1111},$$

$$[\hat{c}_{\ell d}]_{1111} = [c_{\ell d}]_{1111} + [c_{\ell q}]_{1111} - [\hat{c}_{eq}]_{1111},$$

$$[\hat{c}_{eu}]_{1111} = [c_{eu}]_{1111} - [c_{\ell q}]_{1111},$$

$$[\hat{c}_{ed}]_{1111} = [c_{ed}]_{1111} - [c_{\ell q}]_{1111}$$

Flat directions in 4-fermion operators

Flat[SPS]:

$$[\hat{c}_{eq}]_{2211} = [c_{eq}]_{2211} + [c_{ed}]_{2211} - 2 [c_{eu}]_{2211}$$

Flat[trident]:

$$[\hat{c}_{\ell\ell}]_{2222} = [c_{\ell\ell}]_{2222} + \frac{2g'^2}{g^2 + 3g'^2} [c_{\ell e}]_{2222}$$

Flat[flavor]:

$$\varepsilon_P^{d\mu} [2 \text{ GeV}] = 0.86 [c_{ledq}]_{2211} - 0.86 [c_{lequ}]_{2211} + 0.012 [c_{ledq}^{(3)}]_{2211}$$