

Global fits of UV complete models in future e^+e^- colliders

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Outline

- ① UV vs EFT
- ② Global fits
- ③ Supersymmetric models
- ④ THDM
- ⑤ Heavy Neutral Leptons
- ⑥ Conclusions

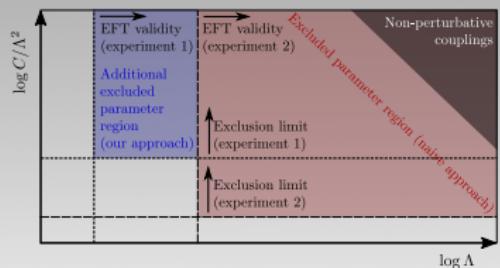
UV vs EFT

UV vs EFT

- EFTs are better at quantified deviations from SM
 - What happens when a deviation is measured? (e.g. $\mathcal{C}_{9,10}$)
 - How to reconstruct a UV model from the EFT? ↗ Ricardo's talk
- Not all UV models correspond to an EFTs (e.g. decays to dark sectors)
- Issues with EFT validity

$$\mathcal{L}_{\text{EFT}} = \sum_{a,d} \frac{\mathcal{C}_a^{(d)}}{\Lambda^{d-4}} \mathcal{Q}_a^{(d)}$$

- Missing low Λ in weakly coupled
- Redundant dependency on \mathcal{C} & Λ
- Inclear clear cutoffs ($m_{\chi\chi} < \Lambda$)



[GAMBIT, Eur.Phys.J.C 81 (2021) 11, 992]

- UV complete models are valid at many energy scales, they can be tested by colliders, precision experiments, astrophysical and cosmological observatories

Global fits

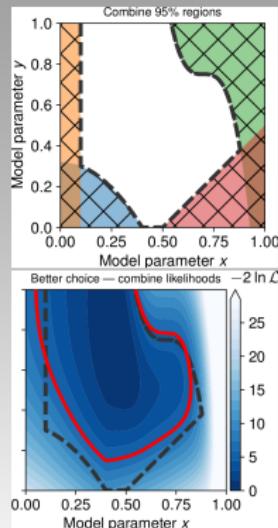
[GAMBIT, MasterCode, Fittino, HEPfit et al, Rept.Prog.Phys. 85 (2022) 5, 052201]

Global fits

- Combine all constraints into a composite likelihood
(e.g. existing LHC searches with e^+e^- Higgs measurements)

$$\mathcal{L} = \mathcal{L}_{\text{Collider}} \mathcal{L}_{\text{Higgs}} \mathcal{L}_{\text{DM}} \mathcal{L}_{\text{Flavour}} \dots$$

- Perform an extensive parameter scan
 - Old-school sampling methods (random, grid) are inefficient
 - Harder to make statement about statistics
 - Need smart sampling strategies (differential, nested, genetic,...)
- Rigorous statistical interpretation (frequentist/Bayesian)
 - Goodness-of-fit
 - Parameter estimation
 - Model comparison
- BSM global fitting tools (GAMBIT, HEPFit,...)



[arXiv:2012.09874 [hep-ph]]

Global fits

GAMBIT: The Global And Modular BSM Inference Tool

gambit.hepforge.org

github.com/GambitBSM

EPJC 77 (2017) 784

arXiv:1705.07908

- Extensive model database, beyond SUSY
- Fast definition of new datasets, theories
- Extensive observable/data libraries
- Plug&play scanning/physics/likelihood packages
- Various statistical options (frequentist /Bayesian)
- Fast LHC likelihood calculator
- Massively parallel
- Fully open-source



Members of: ATLAS, Belle-II, CLIC, CMS, CTA, Fermi-LAT, DARWIN, IceCube, LHCb, SHiP, XENON

Authors of: BubbleProfiler, Capt'n General, Contur, DarkAges, DarkSUSY, DDCalc, DirectDM, Diver, EasyScanHEP, ExoCLASS, FlexibleSUSY, gamLike, GM2Calc, HEPLike, IsaTools, MARTY, nuLike, PhaseTracer, PolyChord, Rivet, SOFTSUSY, SuperIso, SUSY-AI, xsec, Vevacious, WIMPSim

Recent collaborators: P Athron, C Balázs, A Beniwal, S Bloor, T Bringmann, A Buckley, J-E Camargo-Molina, C Chang, M Chrzaszcz, J Conrad, J Cornell, M Danninger, J Edsjö, T Emken, A Fowlie, T Gonzalo, W Handley, J Harz, S Hoof, F Kahlhoefer, A Kvællestad, P Jackson, D Jacob, C Lin, N Mahmoudi, G Martinez, MT Prim, A Raklev, C Rogan, R Ruiz, P Scott, N Serra, P Stöcker, W. Su, A Vincent, C Weniger, M White, Y Zhang, ++

70+ participants in many experiments and numerous major theory codes

Supersymmetric models

[GAMBIT, Eur.Phys.J.C 77 (2017) 12, 824, Eur.Phys.J.C 77 (2017) 12, 879]

[P. Athron et al, Phys.Rev.D 105 (2022) 11, 115029]

SUSY

- Most “current” global fit results for CMSSM, NUHM1 and MSSM7
 - LHC searches → Relic Density
 - Higgs measurements → DM direct and indirect detection
 - Flavour constraints → EW precision measurements
- Future e^+e^- colliders can improve Higgs measurements $e^+e^- \rightarrow hZ$

$$\mathcal{L}_{\text{Higgs}} = -\frac{(\sigma_{hZ} - \sigma_{hZ}^{\text{obs}})^2}{2\sigma_{\sigma_{hZ}}^2} - \sum_i \frac{(\mu_i - \mu_i^{\text{obs}})^2}{2\sigma_{\mu_i}}, \quad \mu_i = \frac{(\sigma BR)_i}{(\sigma BR)_i^{\text{SM}}}$$

- Can also perform very precise measurements of EW observables

$$\mathcal{L}_{\text{EW}} = -\frac{(m_t - m_t^{\text{obs}})^2}{2\sigma_{m_t}^2} - \frac{(\alpha_s - \alpha_s^{\text{obs}})^2}{2\sigma_{\alpha_s}} - \frac{(m_W - m_W^{\text{obs}})^2}{2\sigma_{m_W}^2} - \frac{(\sin^2 \theta_W - \sin^2 \theta_W^{\text{obs}})^2}{2\sigma_{\sin^2 \theta_W}}$$

- Central values x^{obs} are taken as those predicted by best fit point

SUSY

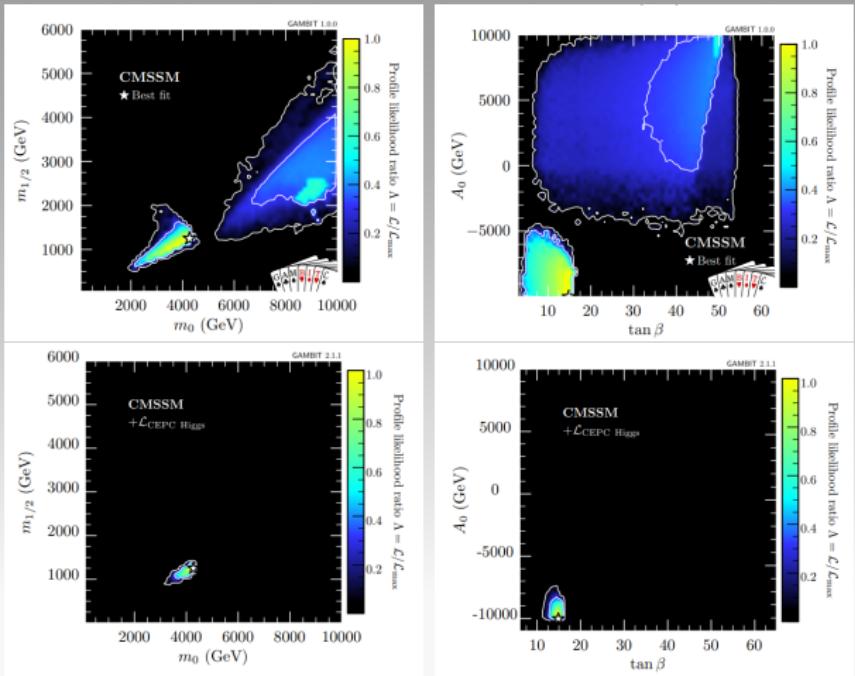
- Estimated precisions for Higgs measurements and EW observables

| | ILC 250 GeV 2 ab ⁻¹ | ILC 350 GeV 200 fb ⁻¹ | ILC 500 GeV 4 ab ⁻¹ | FCC-ee 240 GeV 5 ab ⁻¹ | FCC-ee 365 GeV 1.5 ab ⁻¹ | CEPC 240 GeV 20 ab ⁻¹ | CEPC 360 GeV 1 ab ⁻¹ |
|--|--------------------------------------|--|--------------------------------------|---|---|--|---------------------------------------|
| σ_{Zh} | 0.71% | 2.0% | 1.05% | 0.5% | 0.9% | 0.26% | 1.4% |
| Decay mode | $\sigma_{Zh} \text{Br}$ | $\sigma_{Zh} \text{Br}$ | $\sigma_{\nu\bar{\nu}h} \text{Br}$ | $\sigma_{Zh} \text{Br}$ | $\sigma_{\nu\bar{\nu}h} \text{Br}$ | $\sigma_{Zh} \text{Br}$ | $\sigma_{\nu\bar{\nu}h} \text{Br}$ |
| $h \rightarrow b\bar{b}$ | 0.46% | 1.7% | 2.0% | 0.63% | 0.23% | 0.3% | 0.5% |
| $h \rightarrow c\bar{c}$ | 2.9% | 12.3% | 21.2% | 4.5% | 2.2% | 2.2% | 6.5% |
| $h \rightarrow gg$ | 2.5% | 9.4% | 8.6% | 3.8% | 1.5% | 1.9% | 3.5% |
| $h \rightarrow WW^*$ | 1.6% | 6.3% | 6.4% | 1.9% | 0.85% | 1.2% | 2.6% |
| $h \rightarrow \tau^+\tau^-$ | 1.1% | 4.5% | 17.9% | 1.5% | 2.5% | 0.9% | 1.8% |
| $h \rightarrow ZZ^*$ | 6.4% | 28.0% | 22.4% | 8.8% | 3.0% | 4.4% | 12% |
| $h \rightarrow \gamma\gamma$ | 12.0% | 43.6% | 50.3% | 12.0% | 6.8% | 9.0% | 18% |
| $h \rightarrow \mu^+\mu^-$ | 25.5% | 97.3% | 178.9% | 30.0% | 25.0% | 19% | 40% |
| $(\nu\bar{\nu})h \rightarrow b\bar{b}$ | 3.7% | - | - | - | - | 3.1% | - |

| | CMSSM BF point | Present central value | ILC | Precision FCC-ee | CEPC |
|--|-------------------|--------------------------|----------------------|----------------------|----------------------|
| m_Z | 91.1876 GeV | 91.1876 GeV | 2.1 MeV | 0.1 MeV | 0.5 MeV |
| m_t | 173.267 GeV | 173.34 GeV | 0.03 GeV | 0.6 GeV | 0.6 GeV |
| $\alpha_s^{\overline{\text{MS}}}(m_Z)$ | 0.11862 | 0.1185 | 1.0×10^{-4} | 1.0×10^{-4} | 1.0×10^{-4} |
| m_W | 80.3786 GeV | 80.385 GeV | 5 MeV | 8 MeV | 3 MeV |
| $\sin^2 \theta_W$ | 0.231424 | 0.23155 | 1.3×10^{-5} | 0.3×10^{-5} | 4.6×10^{-5} |

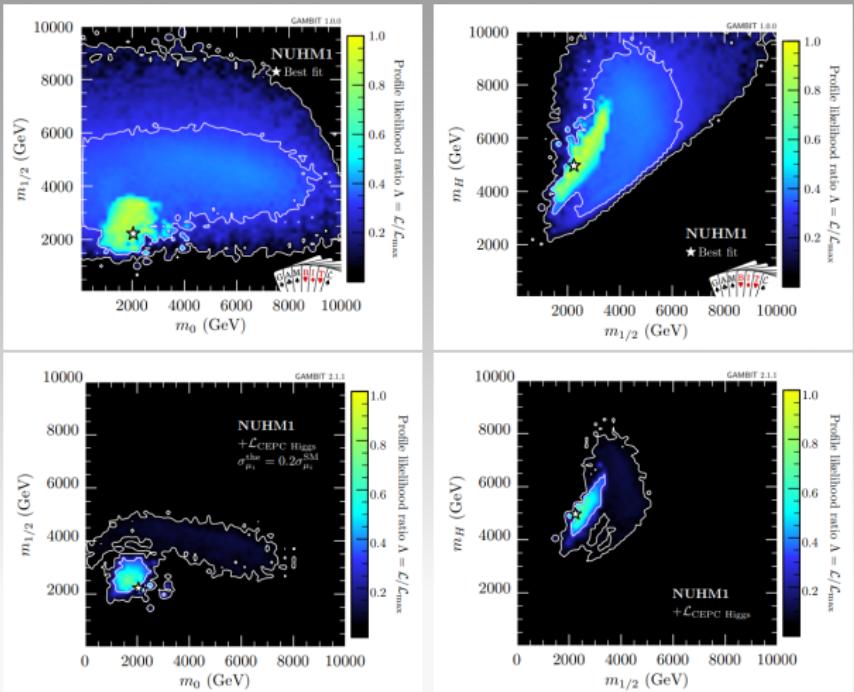
SUSY

- CMSSM $\{m_0, m_{1/2}, A_0, \tan \beta, \text{sign}(\mu)\}$



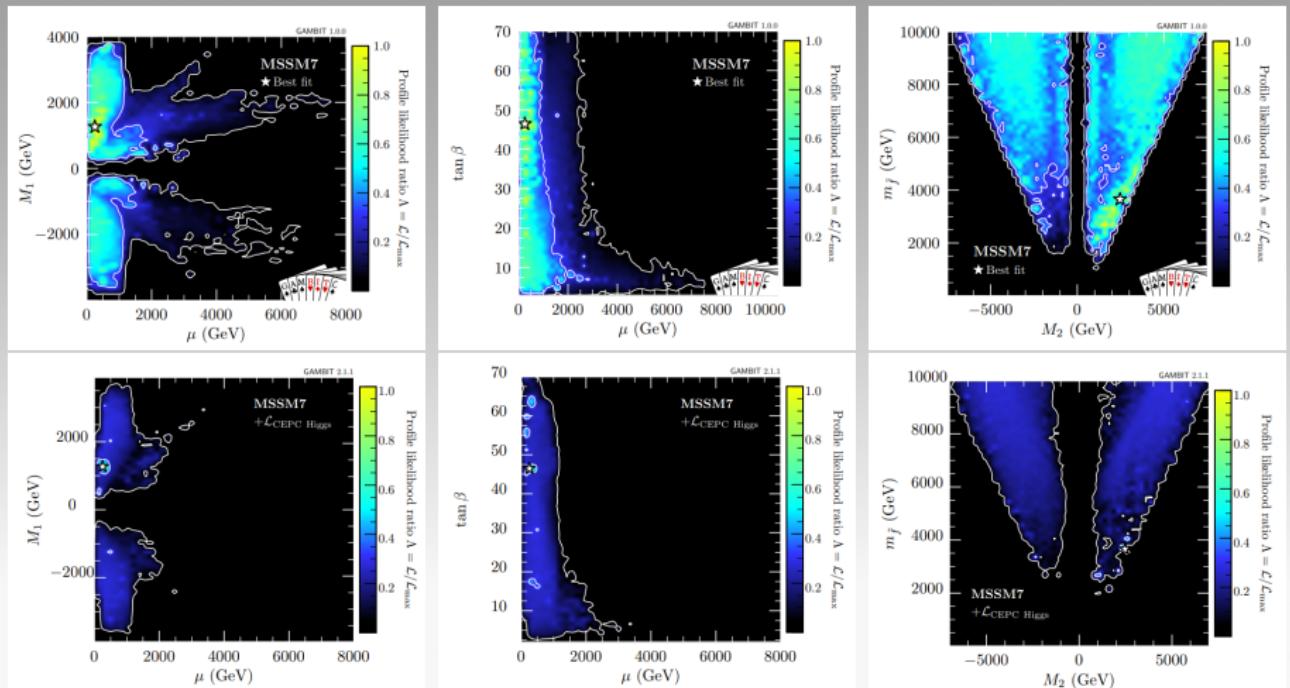
SUSY

- NUHM1 $\{m_0, m_H, m_{1/2}, A_0, \tan \beta, \text{sign}(\mu)\}$



SUSY

- MSSM7 $\{M_2, A_t, A_b, m_f^2, m_{H_u}^2, m_{H_d}^2, \tan \beta, \text{sign}(\mu)\}$



THDM

[GAMBIT, *in preparation*]

[A. Beniwal et al, 2203.07883 [hep-ph]]

THDM

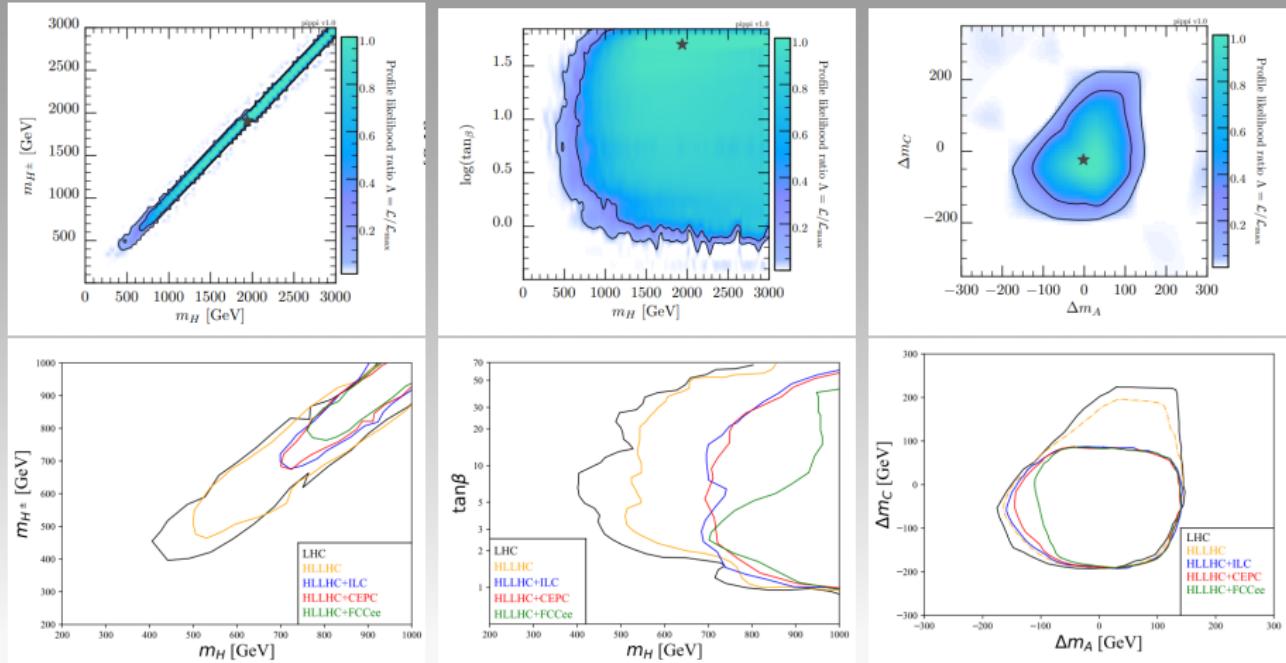
- Type II Two Higgs doublet model in preparation with
 - Theoretical constraints → EW precision measurements
 - Higgs measurements → Flavour constraints
- Future e^+e^- colliders can improve Higgs measurements $e^+e^- \rightarrow hZ$
- EW precision corrections are codified in oblique parameters S, T, U

| | Current ($1.7 \times 10^7 Z$'s) | | | CEPC ($10^{10} Z$'s) | | | FCC-ee ($7 \times 10^{11} Z$'s) | | | ILC ($10^9 Z$'s) | | | |
|-----|-----------------------------------|-------------|------|---------------------------|-------------|-----|-----------------------------------|-------------|------|---------------------------|-------------|--------|------|
| | σ | correlation | | σ (10^{-2}) | correlation | | σ (10^{-2}) | correlation | | σ (10^{-2}) | correlation | | |
| | | S | T | U | S | T | U | S | T | U | S | T | U |
| S | 0.04 ± 0.11 | 1 | 0.92 | -0.68 | 2.46 | 1 | 0.862 | -0.373 | 0.67 | 1 | 0.812 | 0.001 | 3.53 |
| T | 0.09 ± 0.14 | - | 1 | -0.87 | 2.55 | - | 1 | -0.735 | 0.53 | - | 1 | -0.097 | 4.89 |
| U | -0.02 ± 0.11 | - | - | 1 | 2.08 | - | - | 1 | 2.40 | - | - | 1 | 3.76 |

$$\mathcal{L}_{\text{Future}} = - \sum_i \frac{(\mu_i - \mu_i^{\text{obs}})^2}{2\sigma_{\mu_i}^2} - \sum_{ij} (X_i - X_i^{\text{obs}})(\sigma^2)_{ij}^{-1}(X_j - X_j^{\text{obs}})$$

- Central values are set to null hypothesis $\mu_i^{\text{obs}} = 1, X_i^{\text{obs}} = 0$

THDM



Heavy Neutral Leptons

[M. Chrzaszcz, M. Drewes, T.G, et al, Eur.Phys.J.C 80 (2020) 6, 569]

[M. Drewes, T.G et al, *in preparation*]

Heavy Neutral Leptons

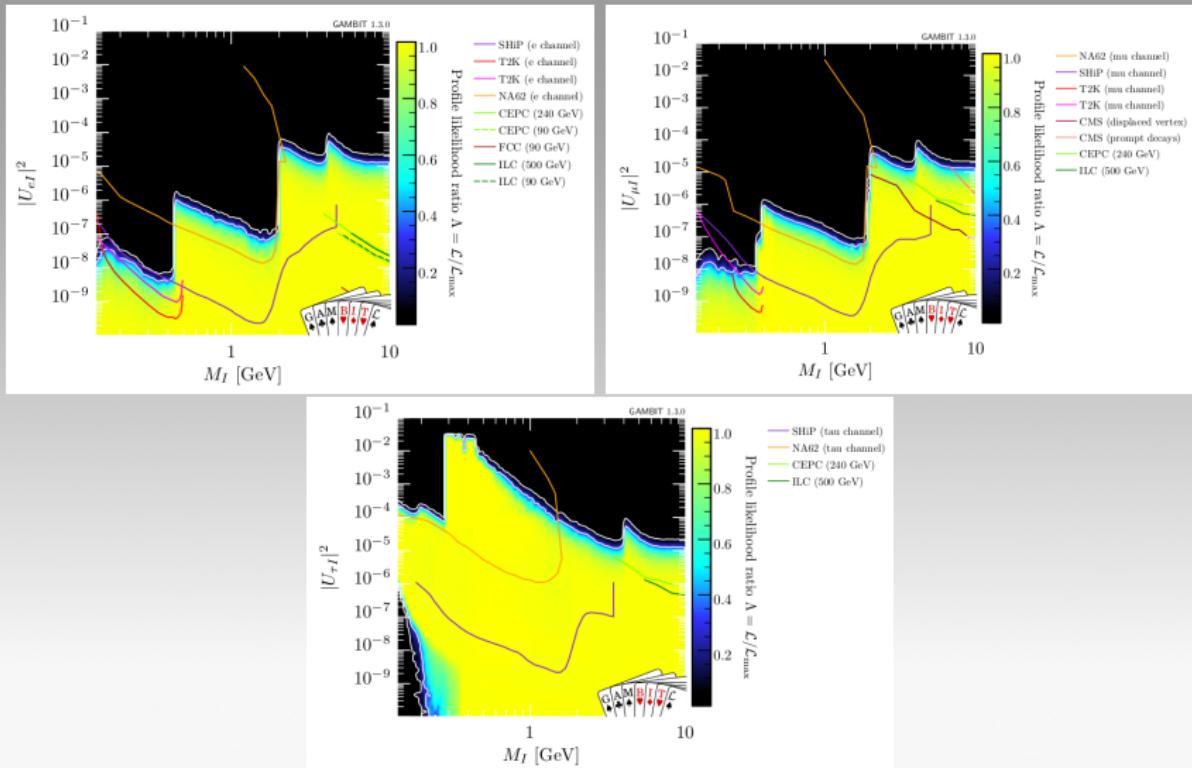
- Heavy neutrinos in $\mathcal{O}(100)$ MeV - $\mathcal{O}(10)$ GeV scale
 - Direct searches → Oscillations
 - Lepton flavour violation → CKM unitarity
 - Lepton universality → EW precision observables
- Current collider searches look at $pp \rightarrow W^* \rightarrow lN$
- Future e^+e^- colliders running at the Z pole can look at $e^+e^- \rightarrow Z \rightarrow \nu N$

$$BR(Z \rightarrow \nu N) = \frac{2}{3} |U_N|^2 BR(Z \rightarrow \text{inv}) \left(1 + \frac{m_N^2}{2m_Z^2}\right) \left(1 - \frac{m_N^2}{m_Z^2}\right)$$

- Subsequent EW decays of N at displaced vertices

$$N_{\text{obs}} \propto L |U_N|^4 M^5$$

Heavy Neutral Leptons



Summary and Conclusions

- UV models are often more suitable candidates than EFT models
 - UV mapping, EFT validity, applicability of constraints,...
- Global fits are the best solution to explore UV models
 - Multidisciplinary constraints, smart sampling, existing tools
- Higgs and EW measurements from e^+e^- colliders can significantly reduce the available parameter space in SUSY and THDM models
 - CMSSM and NUMH1 almost “excluded” with precision Higgs physics
 - Strong preference for wino/higgsino-like scenarios in MSSM7
 - Strong constraints on Higgs masses and splittings in THDM
- Displaced vertex searches very critical in e^+e^- colliders
 - Searches for HNLs can probe low couplings $|U|^2 \gtrsim 10^{-8} - 10^{-10}$
- Future e^+e^- colliders working at the Higgs and Z poles can be critical to exclude or constrained UV models
- Global fits are fundamental to combine those constraints with new physics searches and other constraints