

Higgs self-coupling projections for future e^+e^- colliders.

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HELMHOLTZ



The Higgs self-coupling

- Establish **Higgs mechanism** experimentally \rightarrow reconstruct **Higgs potential**

Higgs potential in SM after SSB

$$V(h) = \frac{1}{2} m_H^2 h^2 + \lambda_3 \nu h^3 + \frac{1}{4} \lambda_4 h^4$$

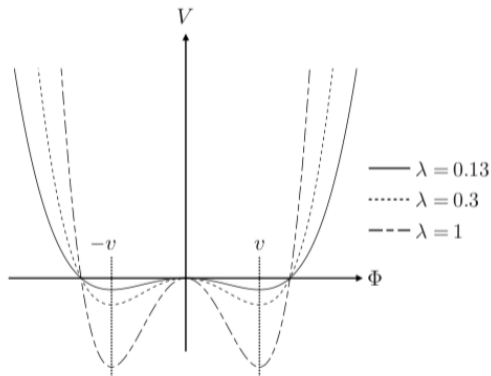
with $\lambda_3^{SM} = \lambda_4^{SM} = \frac{m_H^2}{2\nu^2}$

- Measure λ \rightarrow determine shape of **Higgs potential**

SM: self-couplings determined by m_H, ν

EXP: need measurements to confirm/refute this

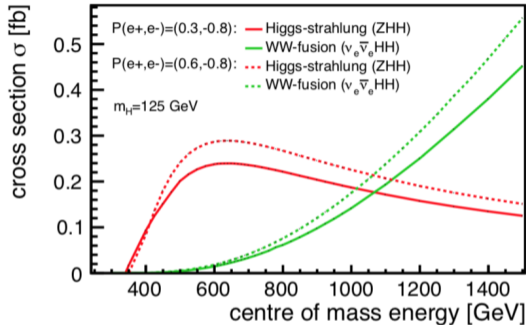
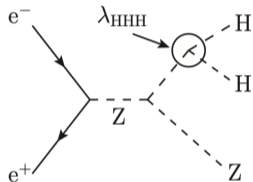
BSM: deviations in λ \rightarrow new physics in Higgs sector



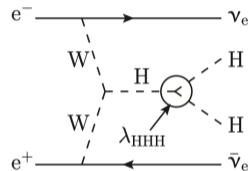
- Direct access to trilinear Higgs self-coupling through the measurement of double Higgs production

Accessing the Higgs self-coupling directly at e^+e^- colliders

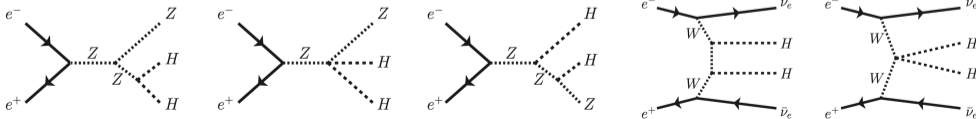
Di-Higgs strahlung:
dominant below 1 TeV



WW fusion:
dominant above 1 TeV



Interference diagrams:

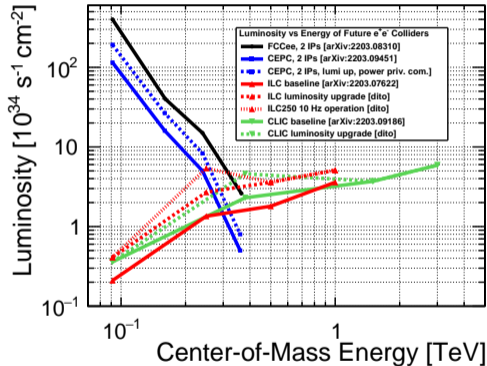


Linear vs circular colliders

Proposed future e^+e^- colliders

circular	linear
FCC-ee	ILC
CEPC	CLIC

Precision requires luminosity



Precision reach in direct measurements at future colliders

Expected precision from HH production channels (1σ bounds)

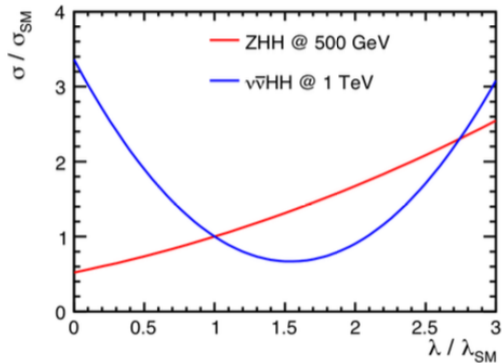
collider	excl. from HH	End of data taking
HL-LHC	50 %	primo 2040s
ILC 500	27 %	ultimo 2050s
ILC 500+1000	10 %	primo 2070s
CLIC 1500	36 %	medio 2060s
CLIC 1500+3000	[-7 %, 11 %]	medio 2070s
FCC-hh ¹	[3.4 %-7.8 %]	2090s

Assumes
 $\lambda = \lambda_{SM}$

- high-energy colliders (ILC₅₀₀₊₁₀₀₀, CLIC₁₅₀₀₊₃₀₀₀, FCC-hh) can reach the <10% precision level
- Higgs self-coupling can also be measured indirectly in EFT fit
 - e.g. projected precision at FCC-ee is 27 %

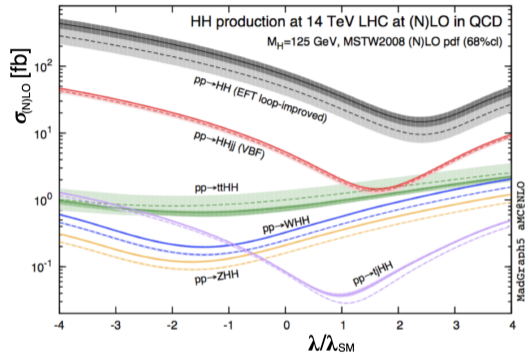
¹DELPHES based analysis

Precision as a function of new physics



The two channels provide complementary information

- ZHH gives stronger constraints on $\lambda / \lambda_{SM} > 1$
- $\nu\bar{\nu}HH$ gives stronger constraints on $\lambda / \lambda_{SM} < 1$



- LHC gives stronger constraints on $\lambda / \lambda_{SM} < 1$

Projections for Higgs self-coupling measurement at CLIC

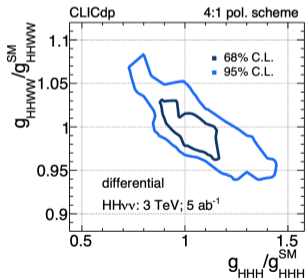
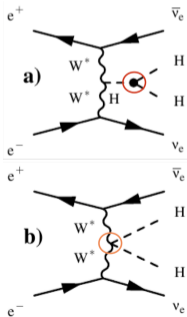
arXiv:1901.05897

Double Higgs production at CLIC:

Access to both ZHH and $HH\nu\nu$ at $\sqrt{s} = 1500$ GeV and $\sqrt{s} = 3000$ GeV

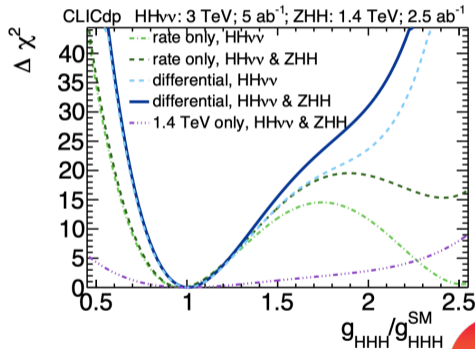
Observables: σ_{ZHH} , $\sigma_{HH\nu\nu}$, and $M(HH)$ distribution with $HH \rightarrow bbbb + HH \rightarrow bbWW$

HHH vs. HHWW vertex



After full CLIC running scenario

$$\rightarrow \Delta\lambda_{SM}/\lambda_{SM} = [-7\%, 11\%]$$



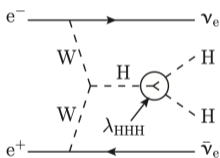
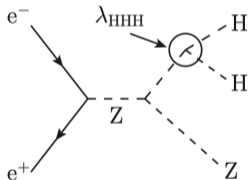
Projections for Higgs self-coupling measurement at ILC

DESY-THESIS-2016-027

Double Higgs production at ILC:

Access to both ZHH at $\sqrt{s} = 500$ GeV and $HH\nu\nu$ at $\sqrt{s} = 1000$ GeV

Observables: σ_{ZHH} and $\sigma_{HH\nu\nu}$ with $HH \rightarrow bbbb + HH \rightarrow bbWW$



$$\frac{\Delta\lambda}{\lambda} = 1.62 \frac{\Delta\sigma_{ZHH}}{\sigma_{ZHH}}$$

Interference degrades the sensitivity to the Higgs self-coupling

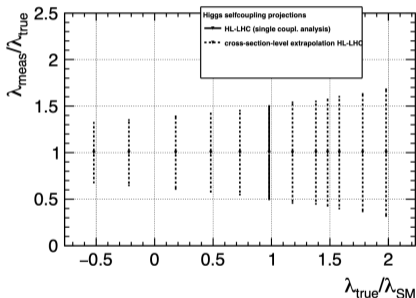
$$\frac{\Delta\lambda}{\lambda} = 0.73 \frac{\Delta\sigma_{WW}}{\sigma_{WW}}$$

After full ILC running scenario

→ $\Delta\sigma_{ZHH}/\sigma_{ZHH} = 16.8\%$ for ZHH only

→ $\Delta\lambda_{SM}/\lambda_{SM} = 26.6\%$ for ZHH only

→ $\Delta\lambda_{SM}/\lambda_{SM} = 10\%$ for ZHH & $HH\nu\nu$



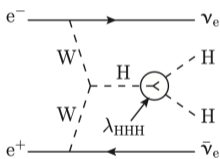
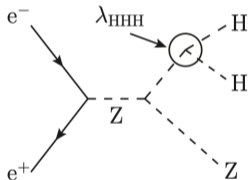
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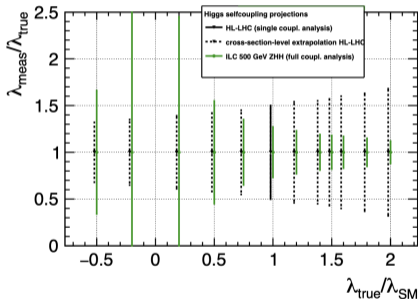
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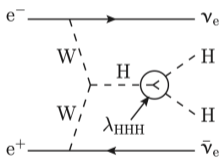
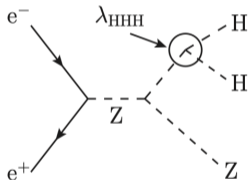
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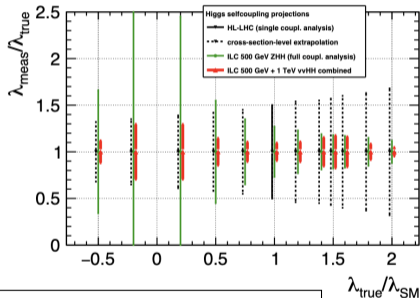
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Combination of ZHH and $\nu\nu HH$ ensures at least 10 – 15% precision for all λ

Strategy for improving the Higgs self-coupling measurement at ILC

DESY-THESIS-2016-027

State-of-the-art projections at ILC performed 6-9 years ago
Meanwhile → significant improvements in our analysis tools

Jet clustering

Perfect jet clustering
→ ~ 40% relative improvement in $\Delta\sigma_{ZH}/\sigma_{ZH}$

Flavour tagging

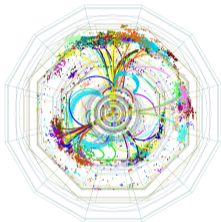
- ✓ Better b -tagging efficiency

5% relative improvement in $\varepsilon_{b\text{-tag}}$
→ 11% relative improvement in $\Delta\sigma_{ZH}/\sigma_{ZH}$

Isolated lepton tagging

- ☰ Optimised for $\ell = \{e, \mu\}$

For $\varepsilon_{\tau} \sim \varepsilon_{e, \mu}$
→ 8% relative improvement in $\Delta\sigma_{ZH}/\sigma_{ZH}$



Error parametrisation in kinematic fitting

Mass resolution \propto jet energy resolution

- ✓ Errorflow: Energy resolution parametrisation for individual jets

Overlay removal

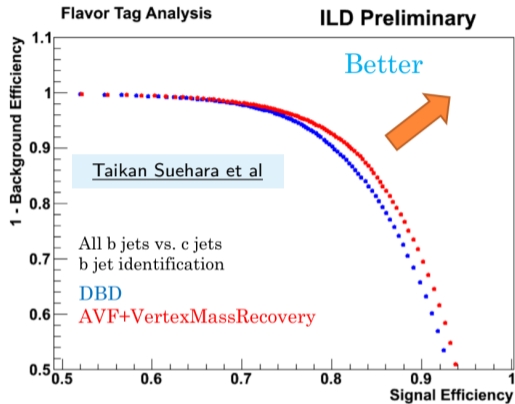
$\gamma\gamma \rightarrow$ low- p_T hadrons

Expect $\langle N_{\text{overlay}} \rangle = 1.2$ event @ 500 GeV

Not included previously

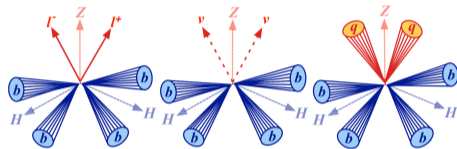
- ✓ Better modelling of the $\gamma\gamma$ overlay
- ☰ Advanced overlay removal strategy

Flavour tagging



Example @ 80% signal efficiency:

	DBD	new	ATLAS
1-eff(c)	90%	95%	75%
Rejection factor	10	20	4

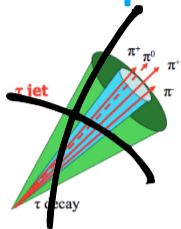


Better signal efficiencies in preselections

- $\nu\nu HH$: 74 % relative improvement after b-tag cut
- $qq HH$: 70 % relative improvement after b-tag cut

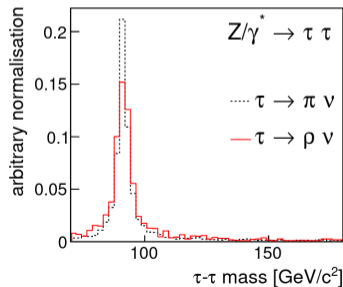
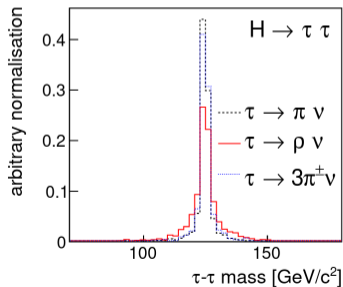
Tau lepton reconstruction

arXiv:1507.01700



Reconstruction using impact parameters

- > requires accurate τ vertex + precise measurement of decay products
- > parametrisation only for single neutrino production
- > $e^+e^- \rightarrow \mu^+\mu^-\tau^+\tau^-$ simulated in ILD

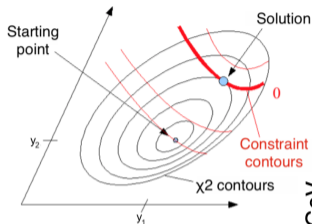


Kinematic fitting & ErrorFlow

arXiv:2110.13731

Exploit well-known initial state in e^+e^- colliders for:

- > Improve kinematics, e.g. mass resolution
- > Hypothesis testing
- > Jet-pairing



χ^2 -function to minimise:

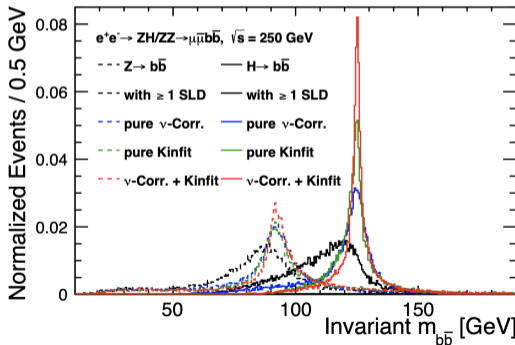
$$L(y) = \Delta y^T \mathbf{V}(y)^{-1} \Delta y + 2 \sum_{k=1}^m \lambda_k f_k(a, y)$$

Correct error parametrisation is crucial for kinematic fitting

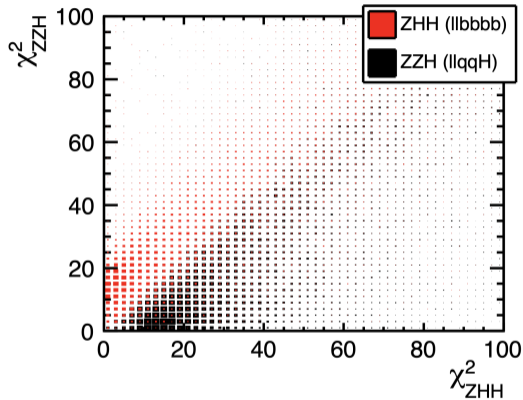
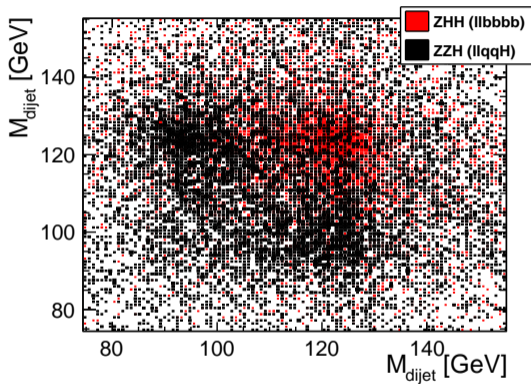
ErrorFlow: Parametrizes the sources of uncertainties for individual jets

$$\sigma_{E_{jet}} = \sigma_{Det} \oplus \sigma_{Conf} \oplus \sigma_{\nu} \oplus \sigma_{Clus} \oplus \sigma_{Had} \oplus \sigma_{\gamma\gamma}$$

- > σ_{Det} : Detector resolution
- > σ_{Conf} : Particle confusion in Particle Flow Algorithm
- > σ_{ν} : Neutrino correction



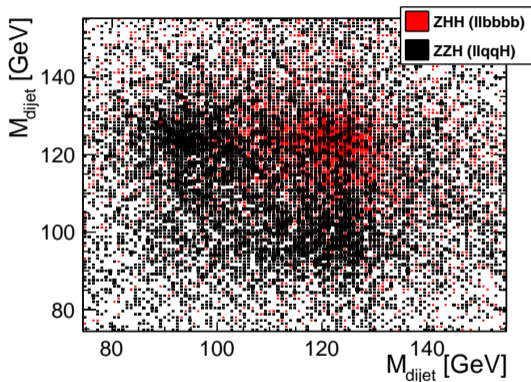
Kinematic fitting for hypothesis testing



- Pre-fitted dijet-masses show large overlap between signal (ZHH) and background (ZZH)

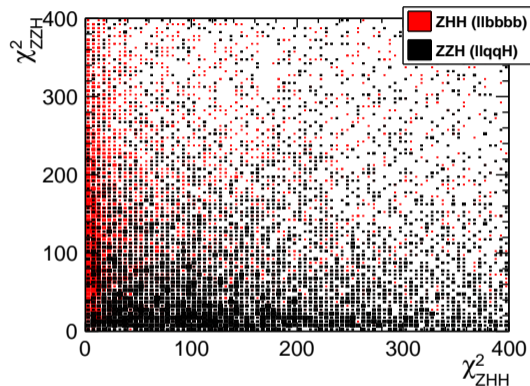
- Hypothesis testing showed good separation for low χ^2 -values of signal (ZHH) and background (ZZH) in previous analysis [DESY-THESIS-2016-027](#)

Kinematic fitting for hypothesis testing



- Pre-fitted dijet-masses show large overlap between signal (ZHH) and background (ZZH)

→



- With ErrorFlow → larger separation of signal (ZHH) and background (ZZH)

Summary and next steps

Future high-energy e^+e^- colliders can directly access the Higgs self-coupling through HH production. ILC and CLIC both hold the opportunity to reach the $< 10\%$ precision level.

Next steps: Continue work of propagating improvements in reconstruction tools to ZHH analysis @ ILC

- Update state-of-the-art projections — important for shaping the landscape of future colliders

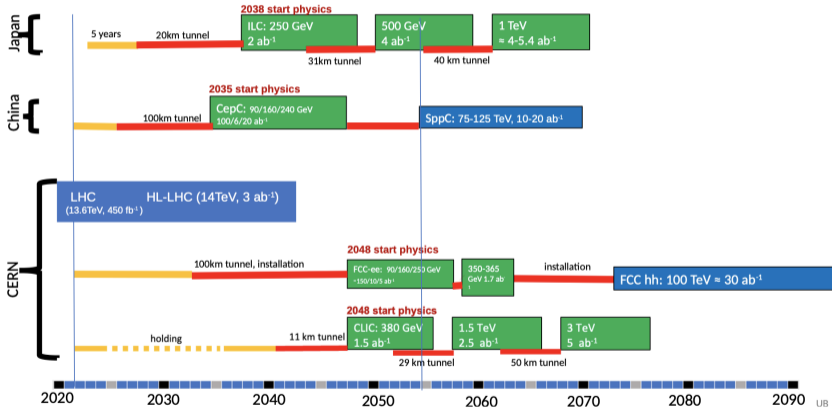
Backup

"Updated" timelines

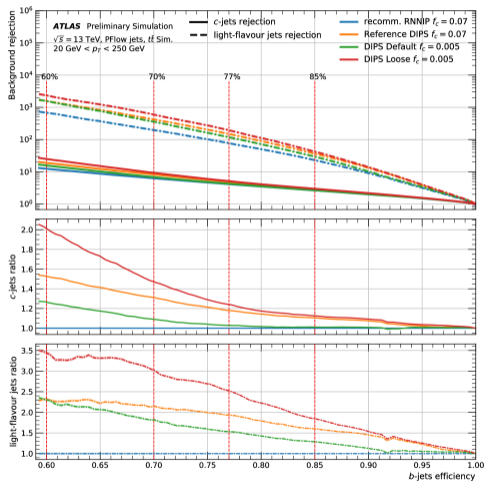
Indicative scenarios of future colliders [considered by ESG]

- Proton collider
- Electron collider
- Muon collider
- Construction/Transformation
- Preparation / R&D

Original from ESG by UB
Updated July 25, 2022 by MN



Flavor Tagging at ATLAS



FTAG-2021-004