Quantum GAN for HEP Detector Simulations

GRID 2021 slides for NiQ 2022

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Future Simulations

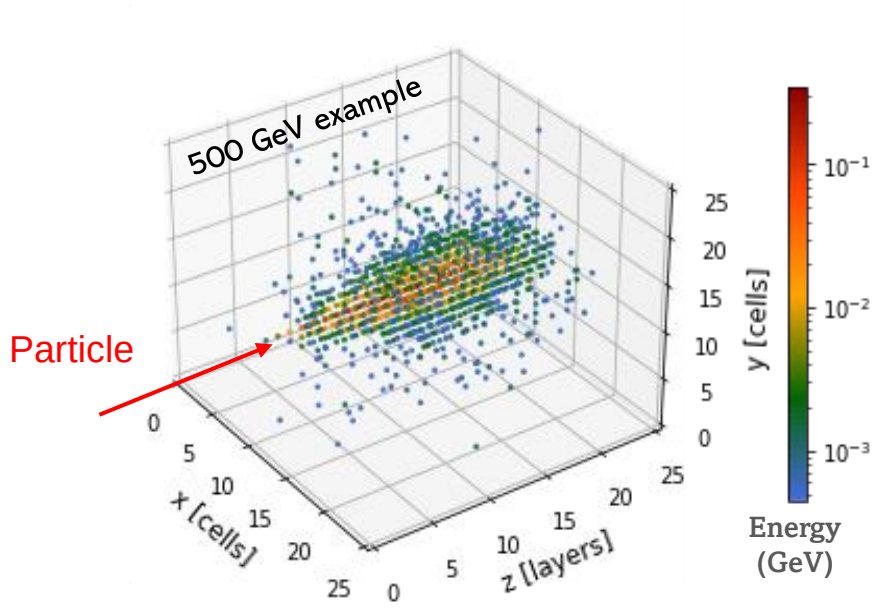
Alternative to Calorimeter Monte Carlo Simulations

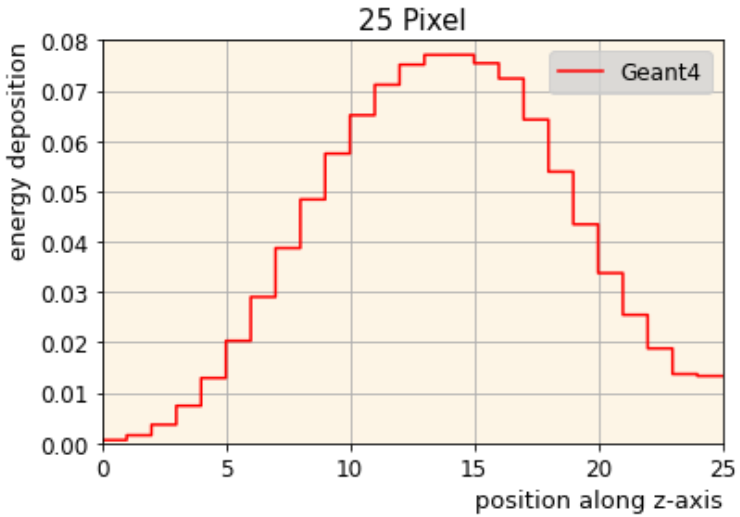
- Previously: **Deep Learning**
  - → Developed a Deep Learning (DL) approach for calorimeter simulations which requires fewer computing resources compared to Geant4
    - DL GAN (up to 160 000x speed up)

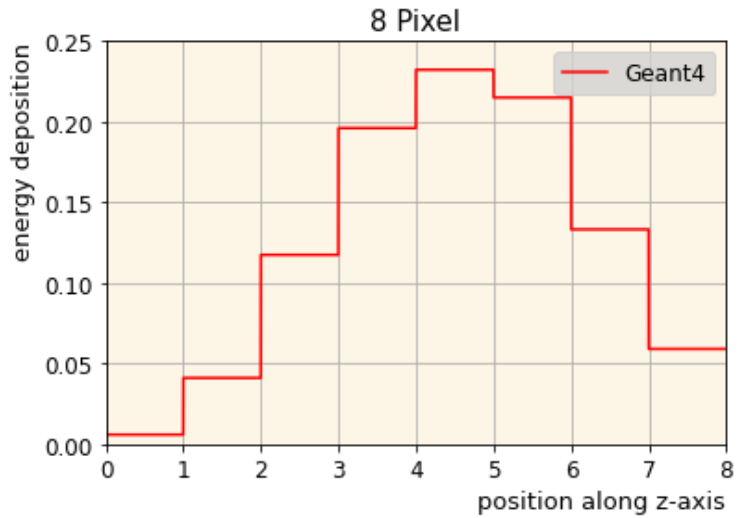
- Now: **Explore potential of quantum computing**
  - Hope to solve problems faster and / or more accurately
  - “Quantum Advantage” not yet reached → only initial investigations
    - Using simplified models
    - Understanding advantages and challenges

Calorimeter Training Data

- 3D particle shower images
- Average the image over z-axis → 1D image
- Down sample to only 8 pixel
- Average of all input energies



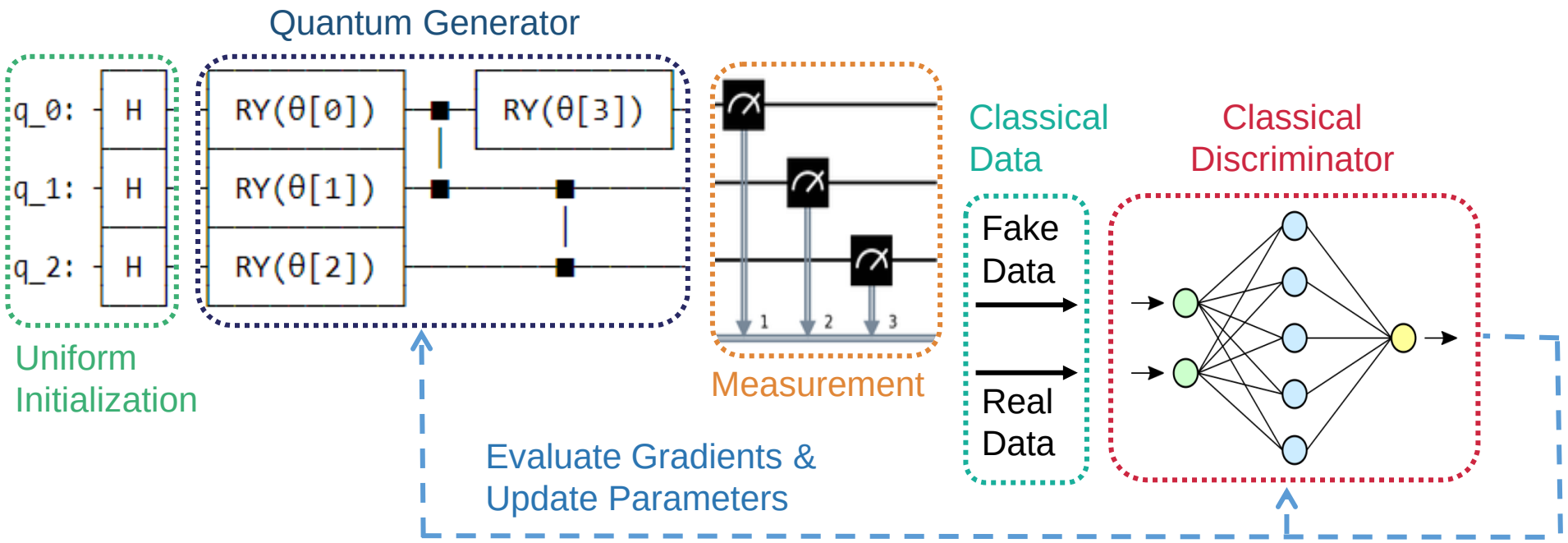




Hybrid qGAN

Quantum Generative Adversarial Networks

- Hybrid quantum – classical ansatz for generating calorimeter shower images

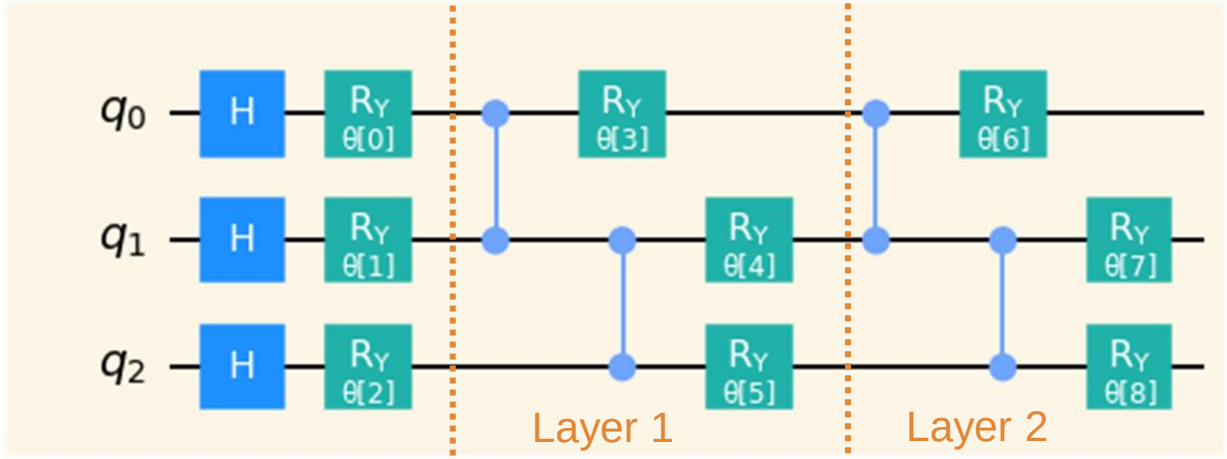


1D Quantum GAN

1D Quantum Generator Circuit

- Modified a Qiskit qGAN model developed by IBM
- 1D 8-pixel images
  - Amplitude encoding: 3 qubits ($2^3 = 8$ states) in quantum generator circuit

Quantum Generator Circuit:



Hadarmard Gate

$$H = \frac{1}{\sqrt{2}}\begin{bmatrix}1 & 1\\ 1 & 1\end{bmatrix}$$

Y-Rotational Gate

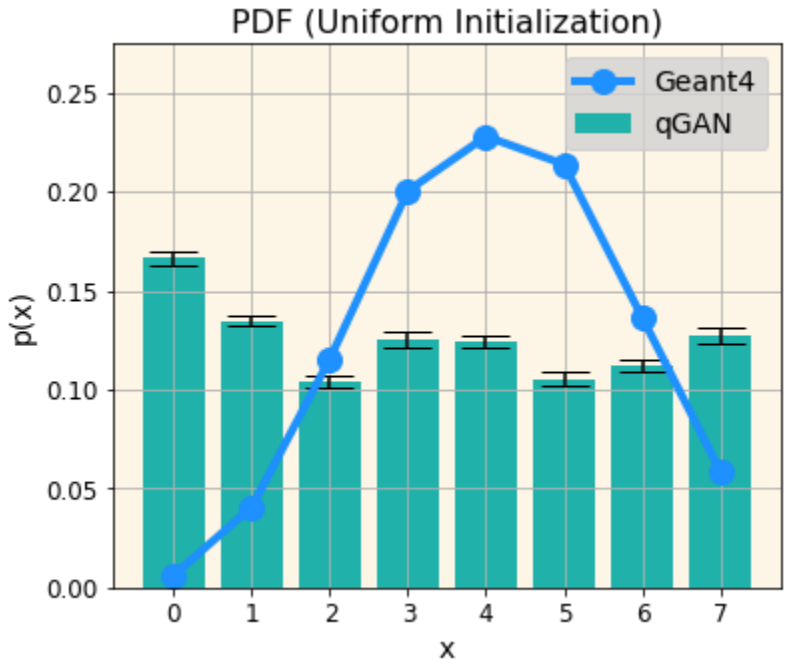
$$R_Y(\theta(i)) = \begin{pmatrix}\cos\left(\frac{\theta}{2}\right) & -\sin\left(\frac{\theta}{2}\right)\\ \sin\left(\frac{\theta}{2}\right) & \cos\left(\frac{\theta}{2}\right)\end{pmatrix}$$

Controlled-Z Gate

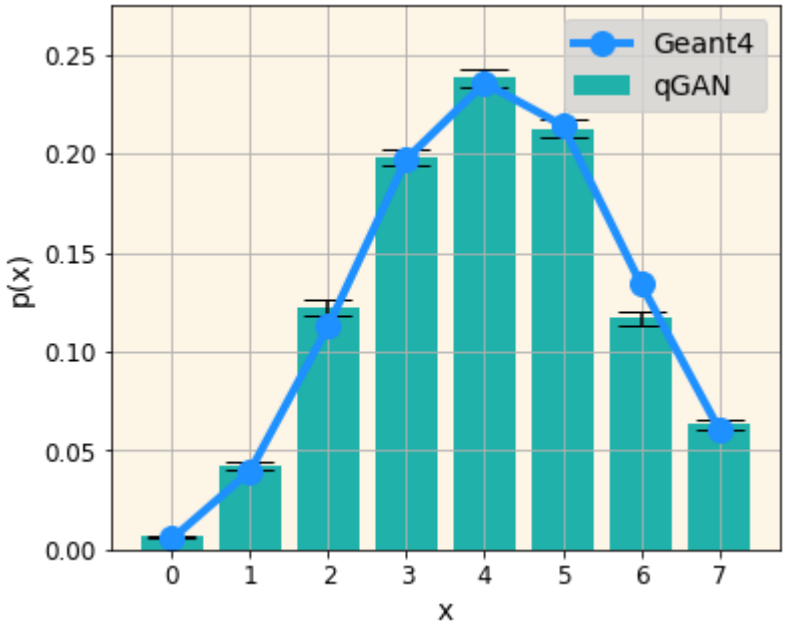
$$= \begin{pmatrix}1 & 0 & 0 & 0\\ 0 & 1 & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & -1\end{pmatrix}$$

1D Training without Noise

- Simulating the quantum computer on a classical computer
- Hyperparameter search reduced training time and increased accuracy



Uniform Initialization

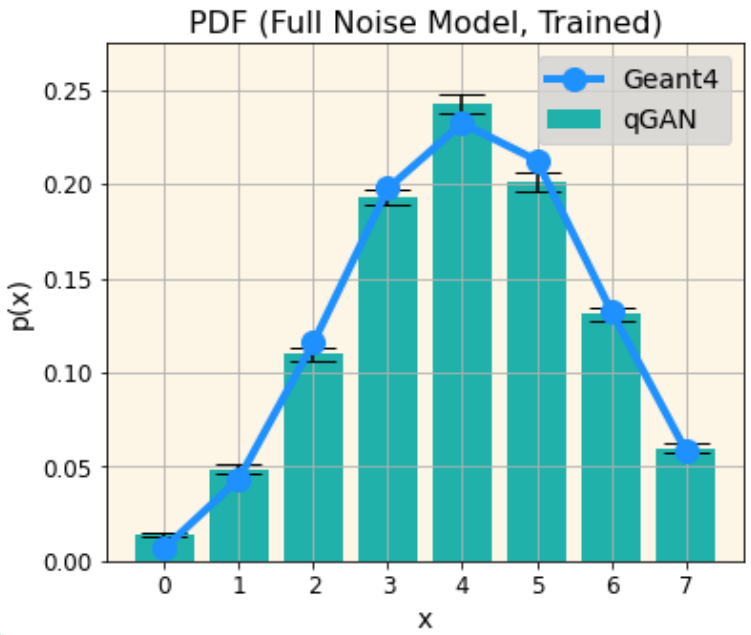


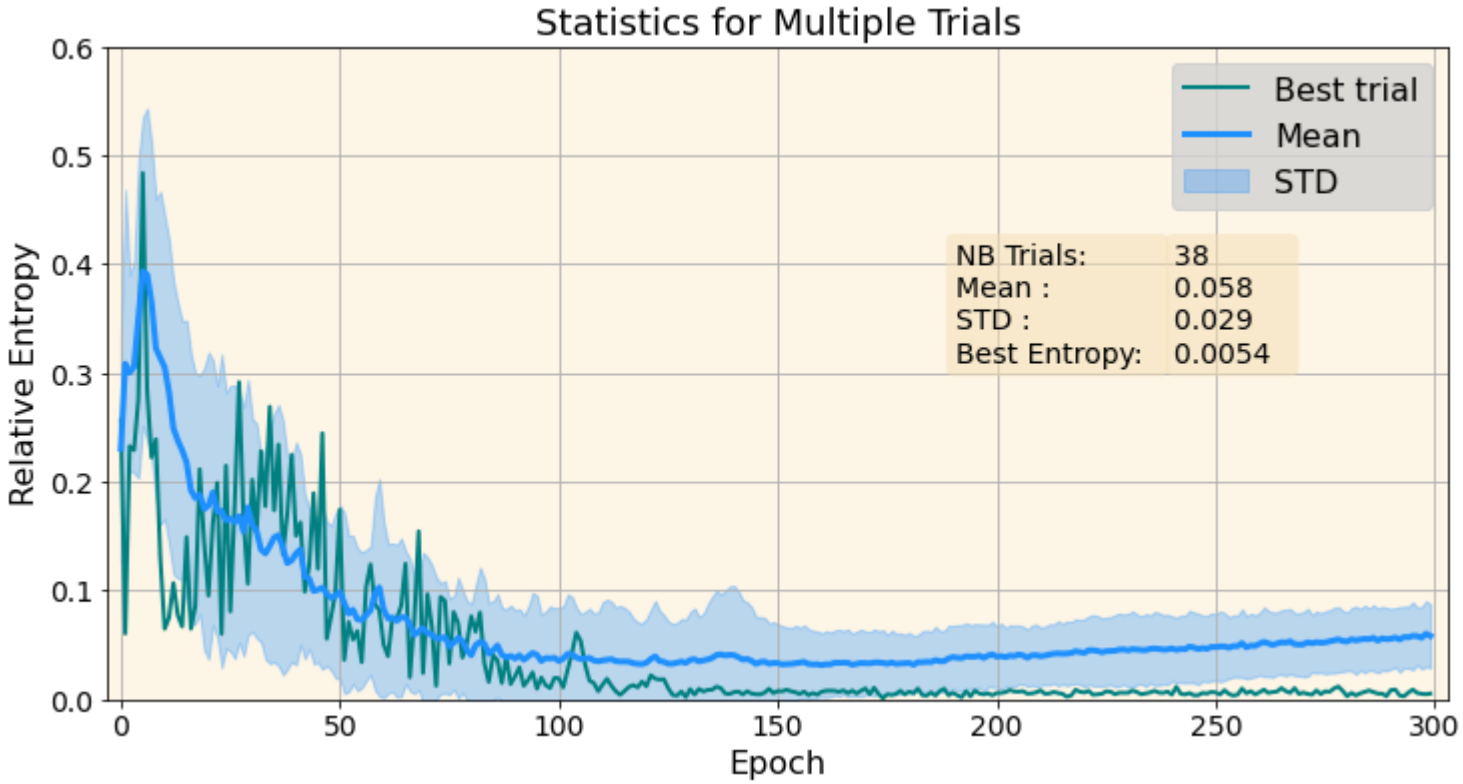
Trained Model

→ Good results

1D Training with Noise

- Custom Noise Model:
  - 2.5% readout noise
  - 1.5% gate-level noise

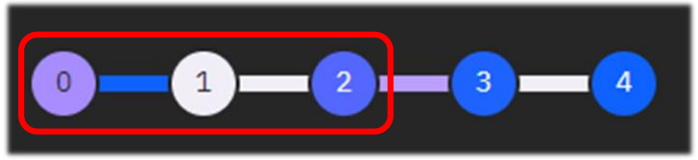




→ Good accuracy
→ Training could have stopped earlier
→ Repeated with real hardware noise → same results

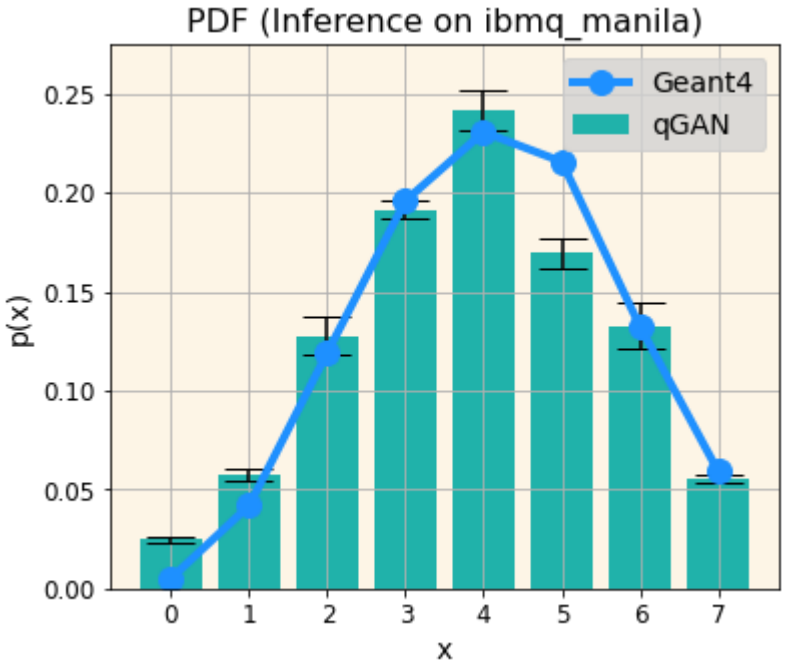
1D Inference on Real Hardware

- Run inference on IBMQ Manila Quantum Computer



- Different noise level than in training

Qubit Number	0	1	2	Average
Readout Error	2.34%	2.66%	2.05%	**2.35%**
CX-gate Error	1.11%		1.75%	**1.43%**



→ Good accuracy

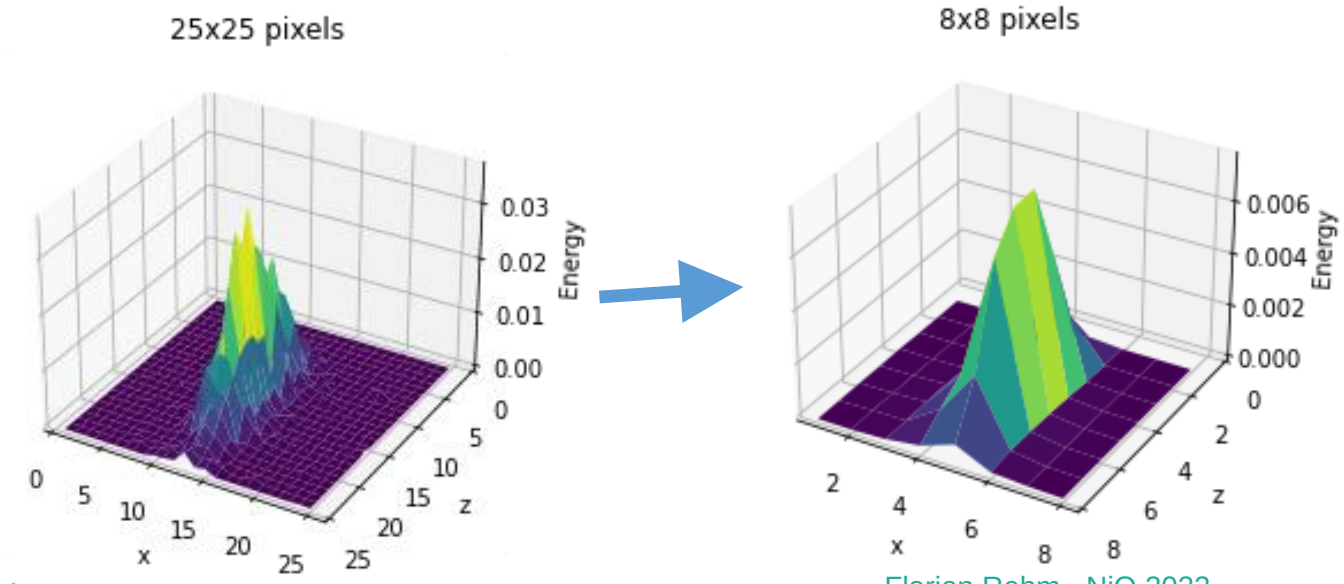
2D Quantum GAN

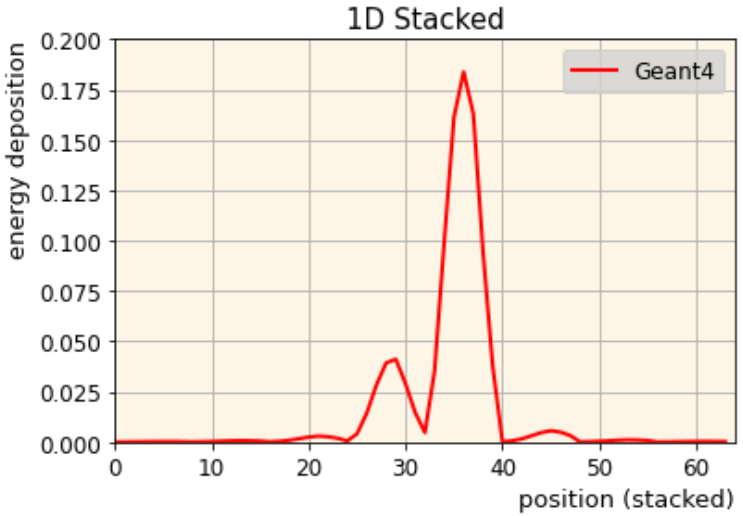
2D qGAN

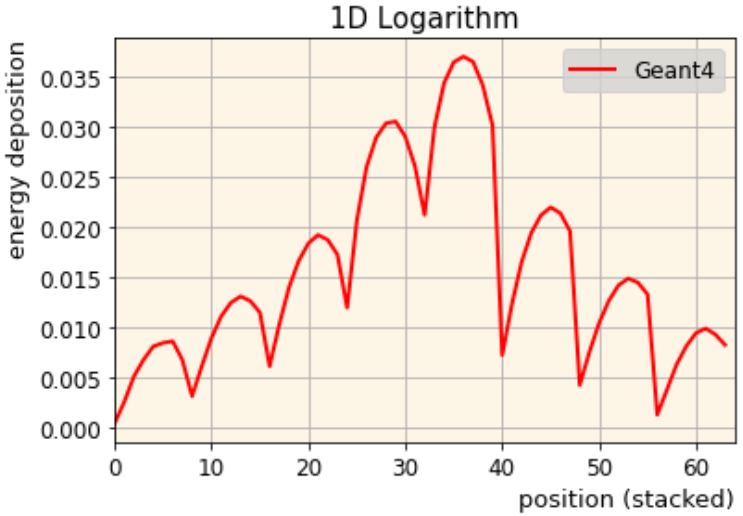
2D Data Representation

2D: 8x8 pixel images

1. Down sample
2. 1D stacking
3. Apply logarithm



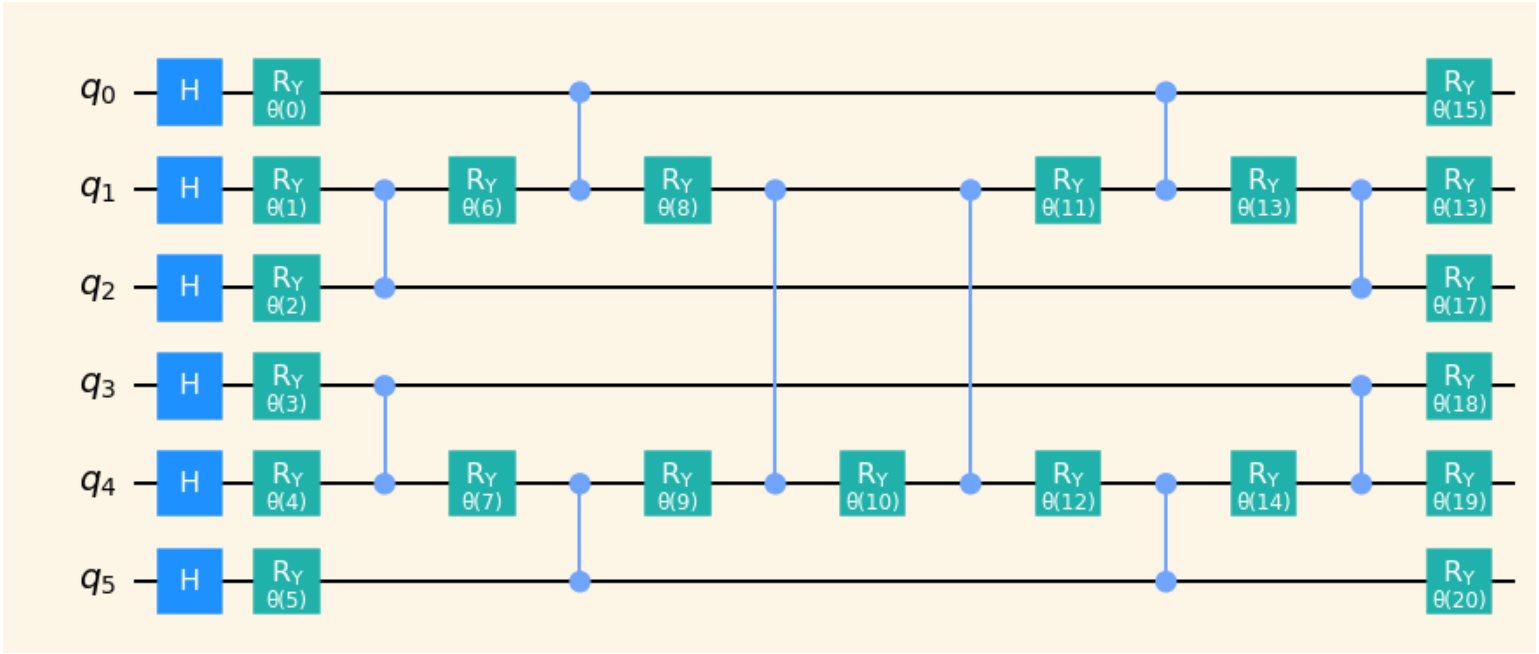


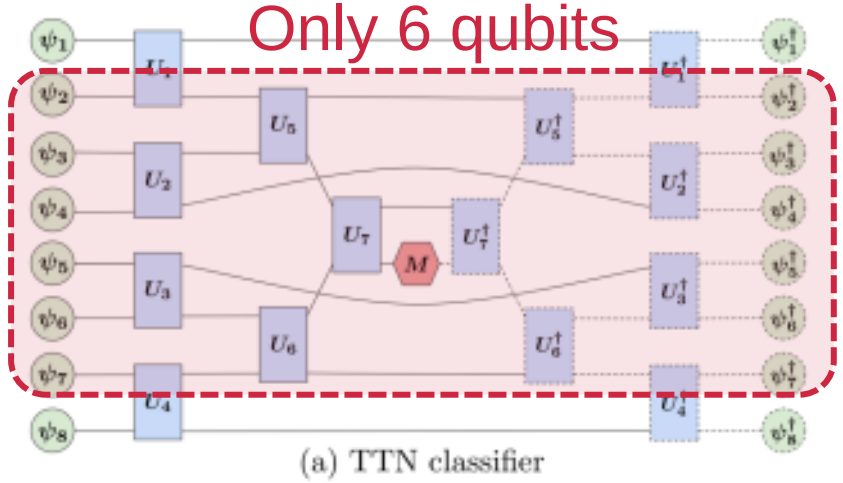


2D Quantum Generator Circuit

Tree Tensor Network Architecture

64 pixels = 2^6 → **6 qubits** for amplitude encoding



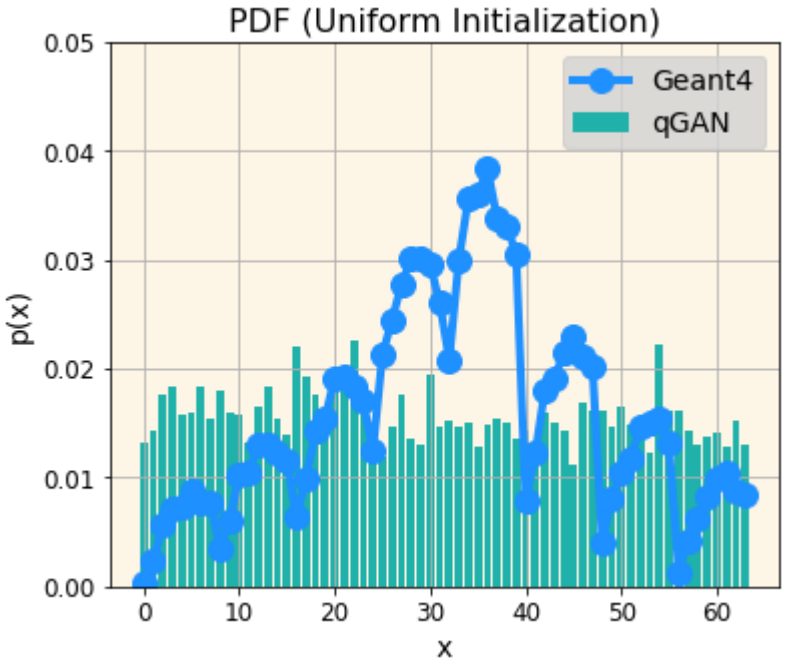


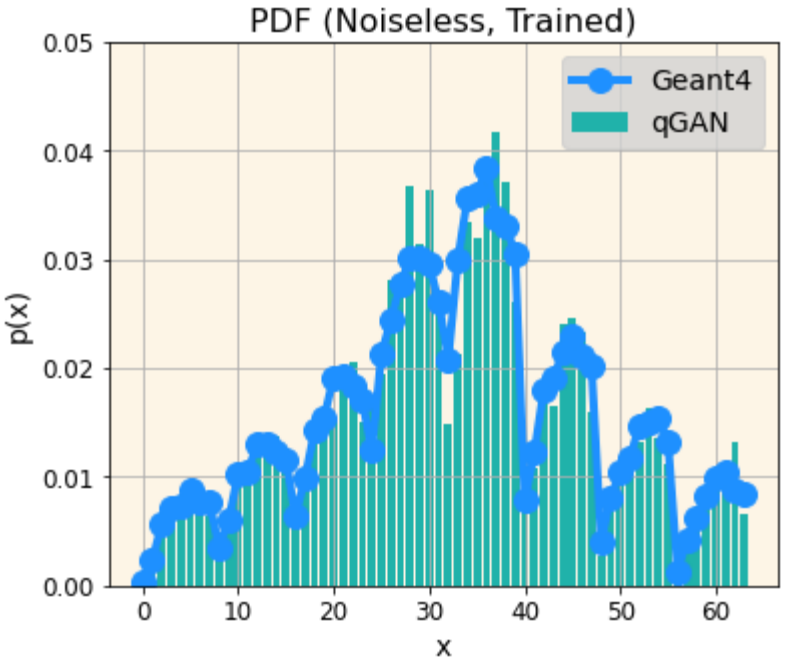
Grant, E., Benedetti, M., Cao, S. *et al.* Hierarchical quantum classifiers. *npj Quantum Inf* **4,** 65 (2018). https://doi.org/10.1038/s41534-018-0116-9

2D qGAN

Best Training Results

- Run on quantum simulator **without** noise





→ Good results

qGAN Future Work

- More tests with the full noise model
  - Does the training benefit from the noise?
  - Test error mitigation techniques

- Conditional qGAN
  - Recent qGAN model learns only averaged distribution
- Run training on real quantum hardware
  - qGAN training to expensive
- 2D qGAN convergence is rare + training takes ~5 days on simulator

→ Search alternative quantum generative model

Thank you for Listening

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