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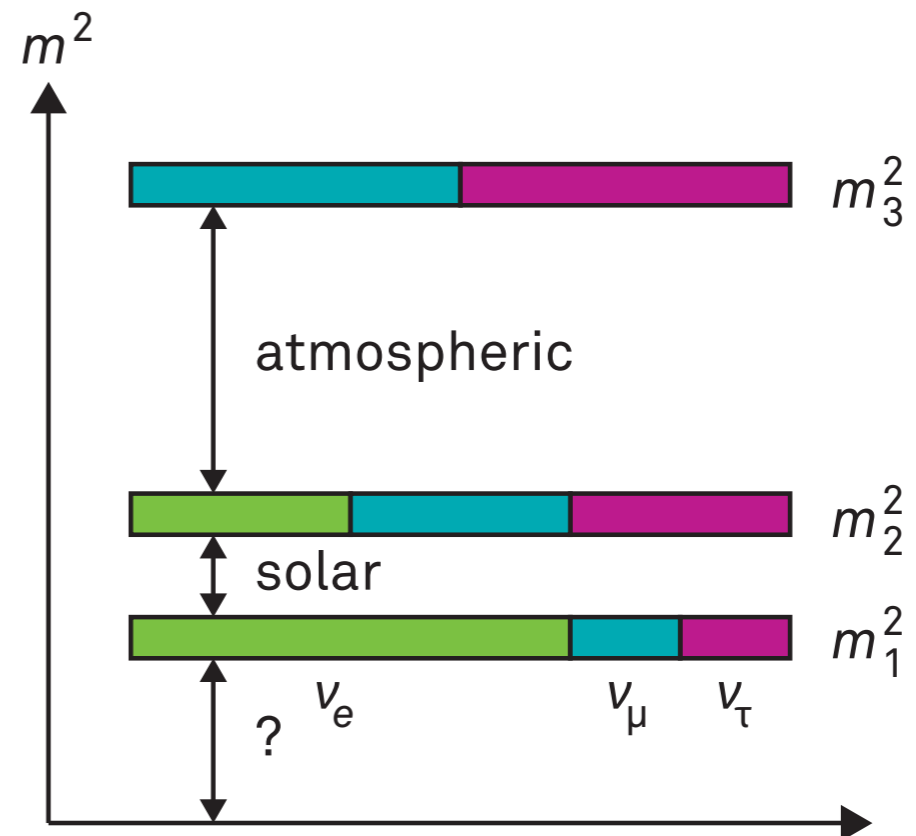
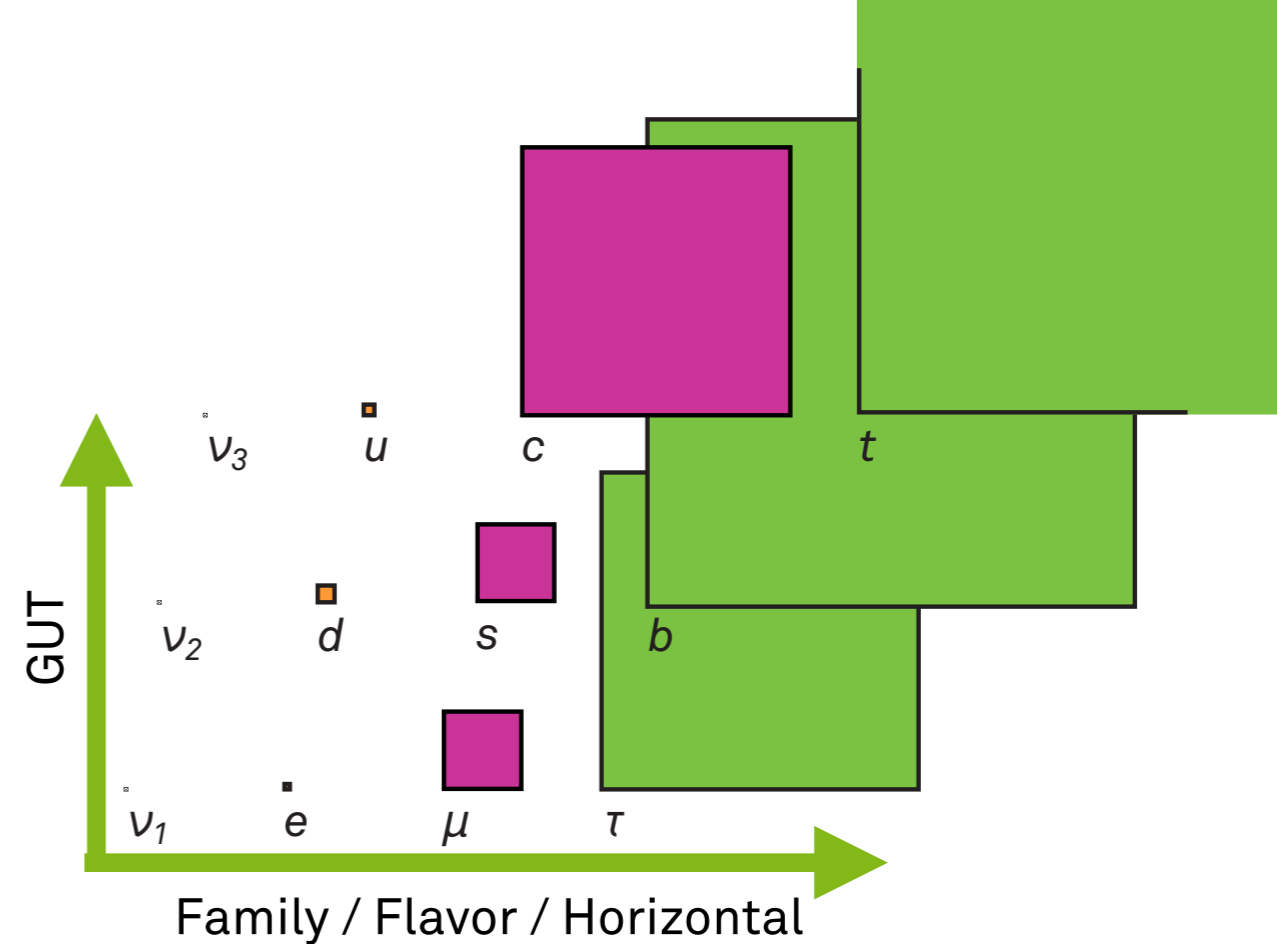
# $S_3$ flavor symmetry at the LHC

G. Bhattacharyya, P. Leser, H. Päs, Phys. Rev. **D83**, 011701 (2011)  
+ work in progress

# Why flavor symmetries?

- ▶ Flavor symmetries have the potential to explain:
- ▶ Masses, mass relations, hierarchies
- ▶ Patterns in the mixing matrices (CKM vs. PMNS)

$$V_{\text{TBM}} = \begin{pmatrix} -\sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} & 0 \\ \sqrt{\frac{1}{6}} & \sqrt{\frac{1}{3}} & \sqrt{\frac{1}{2}} \\ \sqrt{\frac{1}{6}} & \sqrt{\frac{1}{3}} & -\sqrt{\frac{1}{2}} \end{pmatrix}$$



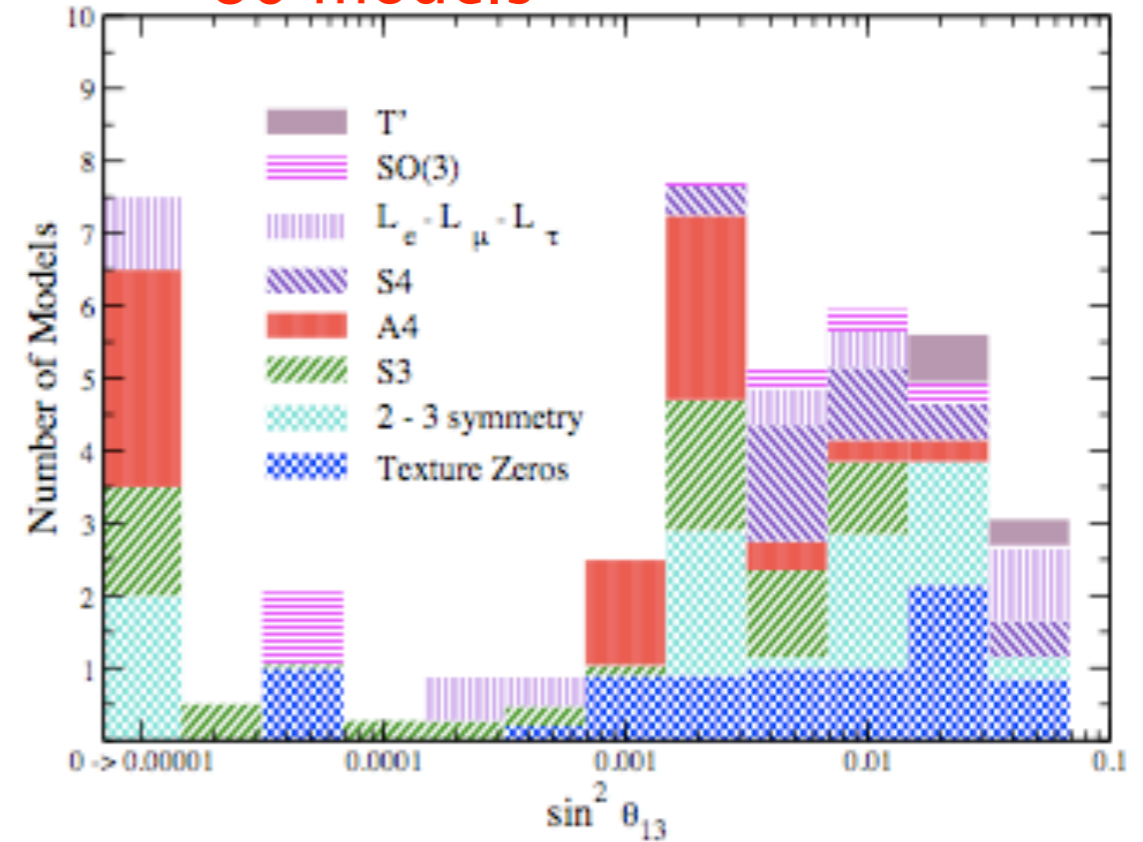
# What kind of symmetries?

- ▶ Abelian symmetries like Froggatt-Nielsen  $U(1)$ , or  $Z_n$
- ▶ All kinds of non-abelian discrete symmetries like  $S_3, A_4, S_4, \dots$  can be used to deduce some of these relations
  - ▶ through **specific choice of representations** for particle content
  - ▶ through **vacuum alignment** of extra scalars

# How to discriminate?

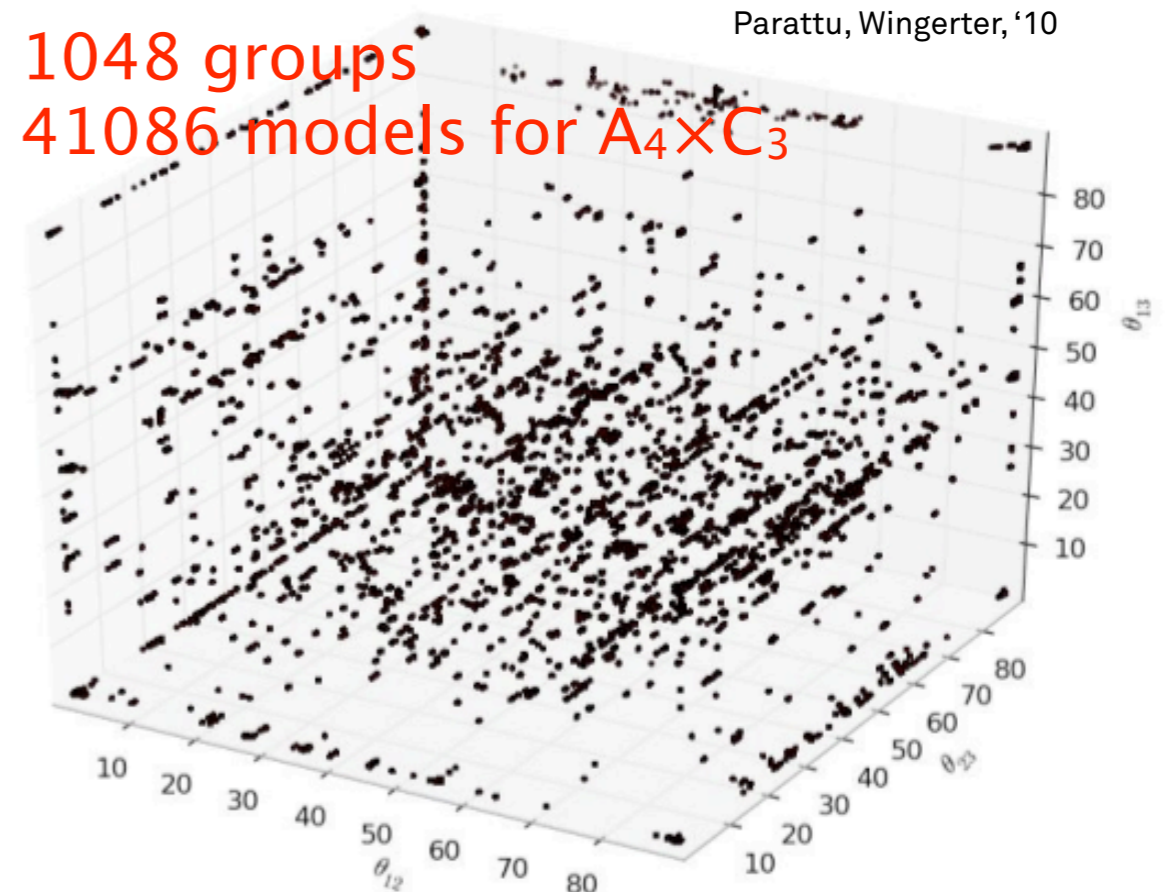
- ▶ Huge variety of models
- ▶ A lot of them fit neutrino data reasonably well, but the allowed parameter space is large
- ▶ Search for other ways to test flavor symmetries

86 models



1048 groups  
41086 models for  $A_4 \times C_3$

Parattu, Wingerter, '10



# Phenomenology of discrete symmetries

- ▶ Typical interesting predictions:
  - ▶ sum rules / connections between lepton and quark sectors ( $\Rightarrow$  GUT embedding)
  - ▶ enlarged scalar sector (masses, mixings)
  - ▶ branching ratios of scalar decays differ from SM
  - ▶ unusual collider signatures
  - ▶ FCNCs in scalar decays

# An exemplary $S_3$ model

Chen, Frigerio, Ma, *Phys. Rev. D* **70**, 073008 (2004)

Lepton doublets



$$(L_1, L_2) \propto \mathbf{2}$$

$$(Q_1, Q_2) \propto \mathbf{2}$$

$$(\phi_1, \phi_2) \propto \mathbf{2}$$

Quark doublets

RH singlets



$$L_3, \ell_3^c, \ell_1^c \propto \mathbf{1}$$

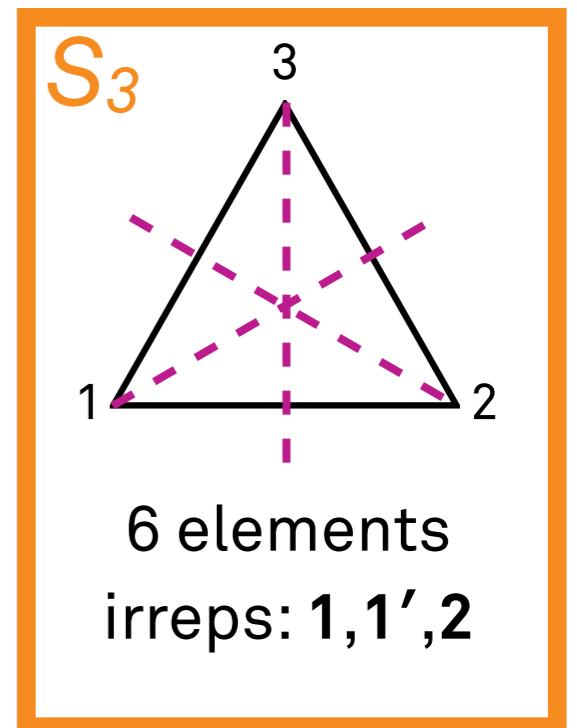
$$Q_3, u_3^c, u_1^c, d_3^c, d_1^c \propto \mathbf{1}$$

$$\phi_3 \propto \mathbf{1}$$

$$\ell_2^c \propto \mathbf{1}'$$

$$u_2^c, d_2^c \propto \mathbf{1}'$$

- ▶ Two generations  $\rightarrow S_3$  doublet; the other  $\rightarrow S_3$  singlet



# A specific $S_3$ model

Chen, Frigerio, Ma, *Phys. Rev. D* **70**, 073008 (2004)

- ▶ One scalar for each generation
- ▶ Neutrino sector separate, diagonal (See-Saw II, 2 heavy EW triplet scalars)
- ▶ Simple vacuum alignment:

$$\langle \phi_1 \rangle = \langle \phi_2 \rangle = v \quad \langle \phi_3 \rangle = v_3$$

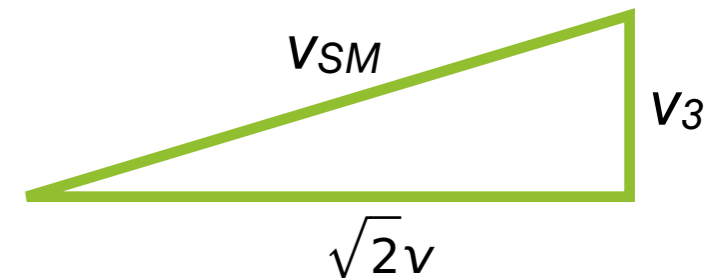
$$2v^2 + v_3^2 = v_{SM}^2$$

translates  
directly into  
PMNS matrix

$$\mathcal{M}_\ell = \begin{pmatrix} f_4 v_3 & f_5 v_3 & 0 \\ 0 & f_1 v & -f_2 v \\ 0 & f_1 v & f_2 v \end{pmatrix}$$

# Minimization of the potential

- ▶ Conditions applied for minimization
  - ▶ Wanted **vacuum alignment**  $\langle \phi_1 \rangle = \langle \phi_2 \rangle = v$  must be a solution
  - ▶ It must actually be a minimum
  - ▶ **Global stability** of the solution
  - ▶ Allow fixed ratio of  $v_3$  and  $v$
  - ▶ We only consider real parameters

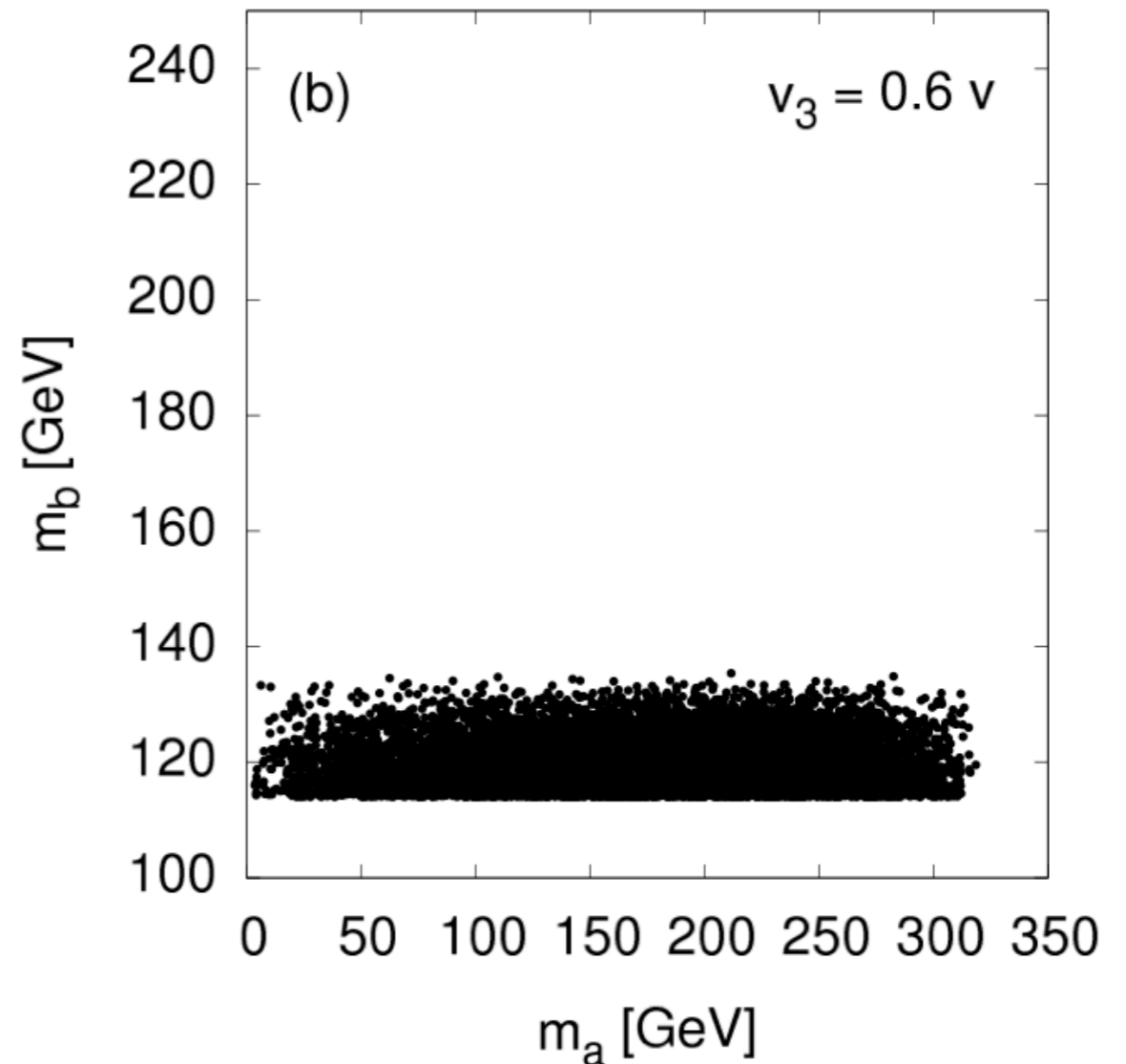
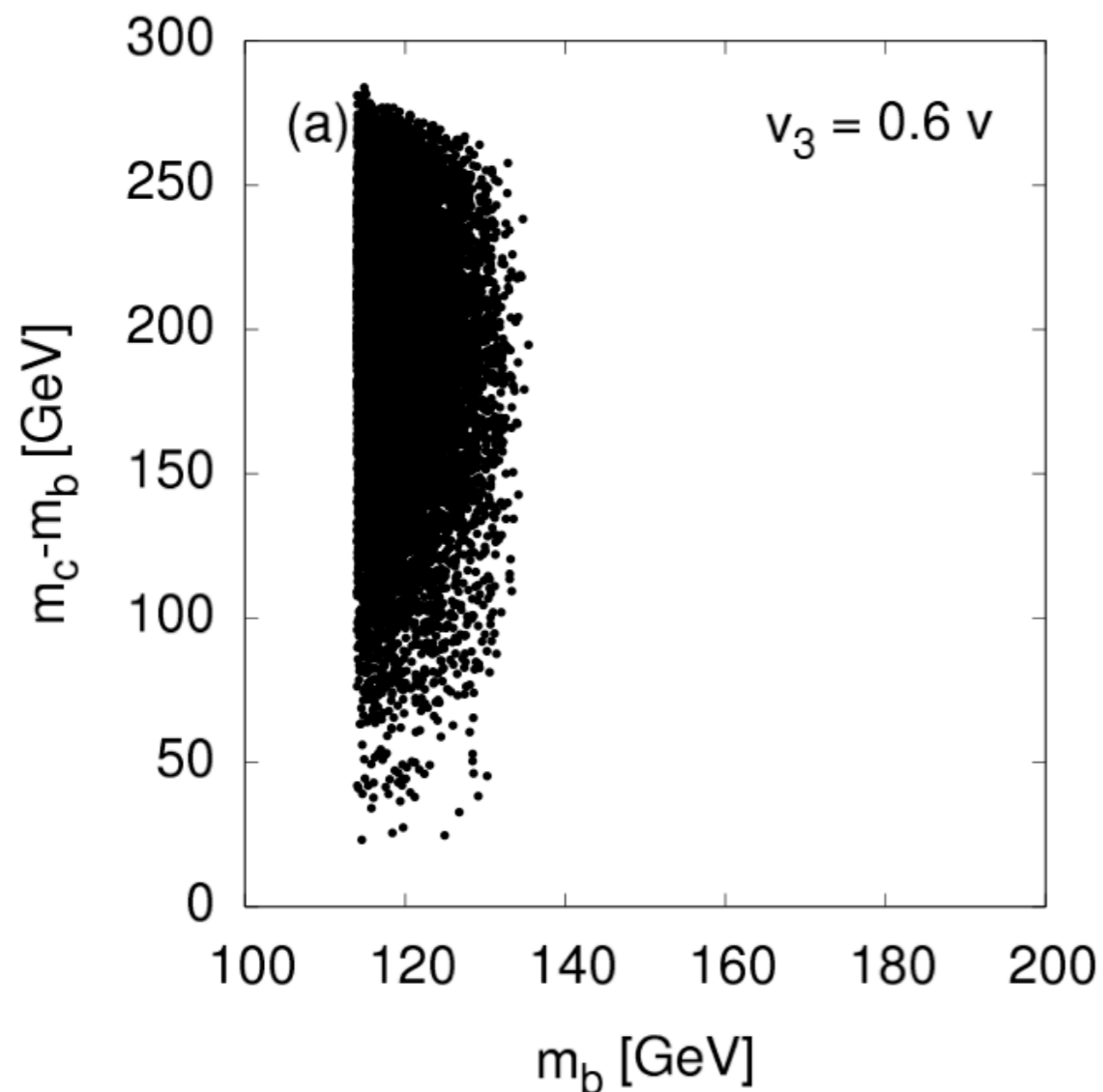


restrict parameters  
of the potential, but  
the parameter  
space is still large



# Results of parameter scan for scalars

- ▶ Physical CP-even neutral scalars:  
 $m_b$  light ( $< 200$  GeV),  $m_c$  heavier ( $200$  GeV  $< m_c < 450$  GeV),  $m_a < 350$  GeV



# Scalar mixing

- ▶ Weak basis scalars  $h_{1/2/3}$  are connected to physical scalars  $h_{a/b/c}$  via

$$h_1 = U_b h_b + U_c h_c - \frac{1}{\sqrt{2}} h_a$$

$$h_2 = U_b h_b + U_c h_c + \frac{1}{\sqrt{2}} h_a$$

$$h_3 = U_{3b} h_b + U_{3c} h_c$$

- ▶ The  $U$  are analytically tractable but complicated functions of the parameters of the scalar potential

# Couplings to gauge and matter fields

- ▶ Couplings of symmetry basis scalars  $h_i$  to  $W$  and  $Z$  are **modified by a factor** of  $v_i/v_{SM} < 1$  compared to Standard Model
- ▶ In terms of physical scalars  $h_a, h_b$  and  $h_c$ :
  - ▶ **Suppression** of the couplings of  $h_b$  and  $h_c$  to gauge fields is governed by VEVs and scalar mixing parameters

## $h_a$ is special

- ▶  **$h_a$  does not couple to  $W$  or  $Z$  via the three-point-vertex**
  - ▶ this follows because the  $h_a$  content in the symmetry basis scalars  $h_1$  and  $h_2$  is equal, but has opposite signs.
  - ▶ As the VEVs  $v_1$  and  $v_2$  are equal, the  $h_a$  coupling vanishes

# Yukawa couplings

- ▶ **Identical structures** in charged lepton sector and up- / down quark sectors
- ▶ 2 scalars  $h_{b,c}$  couple similarly to SM Higgs:
  - ▶  $h_{b,c} \rightarrow ee(uu, dd)$
  - $h_{b,c} \rightarrow \mu\mu(ss, cc)$
  - $h_{b,c} \rightarrow \tau\tau(bb, tt)$
- ▶ Additional FCNC coupling:  $h_{b,c} \rightarrow e\mu$

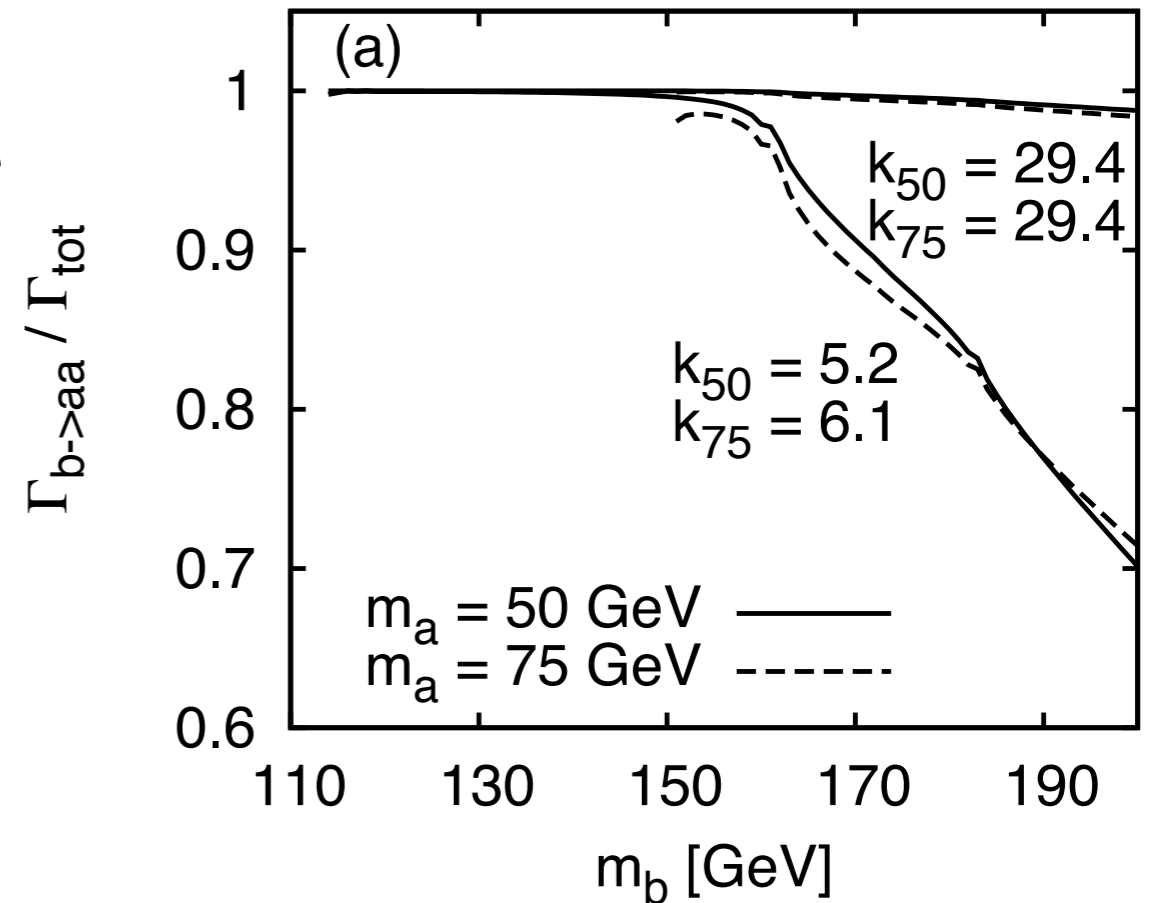
## $h_a$ is special, again

- ▶ The 3<sup>rd</sup> scalar  $h_a$  **only couples off-diagonally**, always with 3<sup>rd</sup> generation:
  - ▶  $h_a \rightarrow e\tau(db, ut)$        $h_a \rightarrow \mu\tau(sb, ct)$
- ▶ FCNC couplings are numerically small and fixed by fermion masses

$$Y_{h_a} = \begin{pmatrix} 0 & 0 & \gamma_{eL\tau R}^a \\ 0 & 0 & \gamma_{\mu L\tau R}^a \\ \gamma_{\tau L e R}^a & \gamma_{\tau L \mu R}^a & 0 \end{pmatrix}, \quad Y_{h_b} = \begin{pmatrix} \gamma_{eL e R}^b & \gamma_{eL \mu R}^b & 0 \\ \gamma_{\mu L e R}^b & \gamma_{\mu L \mu R}^b & 0 \\ 0 & 0 & \gamma_{\tau L \tau R}^b \end{pmatrix}, \quad Y_{h_c} = \begin{pmatrix} \gamma_{eL e R}^c & \gamma_{eL \mu R}^c & 0 \\ \gamma_{\mu L e R}^c & \gamma_{\mu L \mu R}^c & 0 \\ 0 & 0 & \gamma_{\tau L \tau R}^c \end{pmatrix}$$

# Signatures of $h_b$ and $h_c$

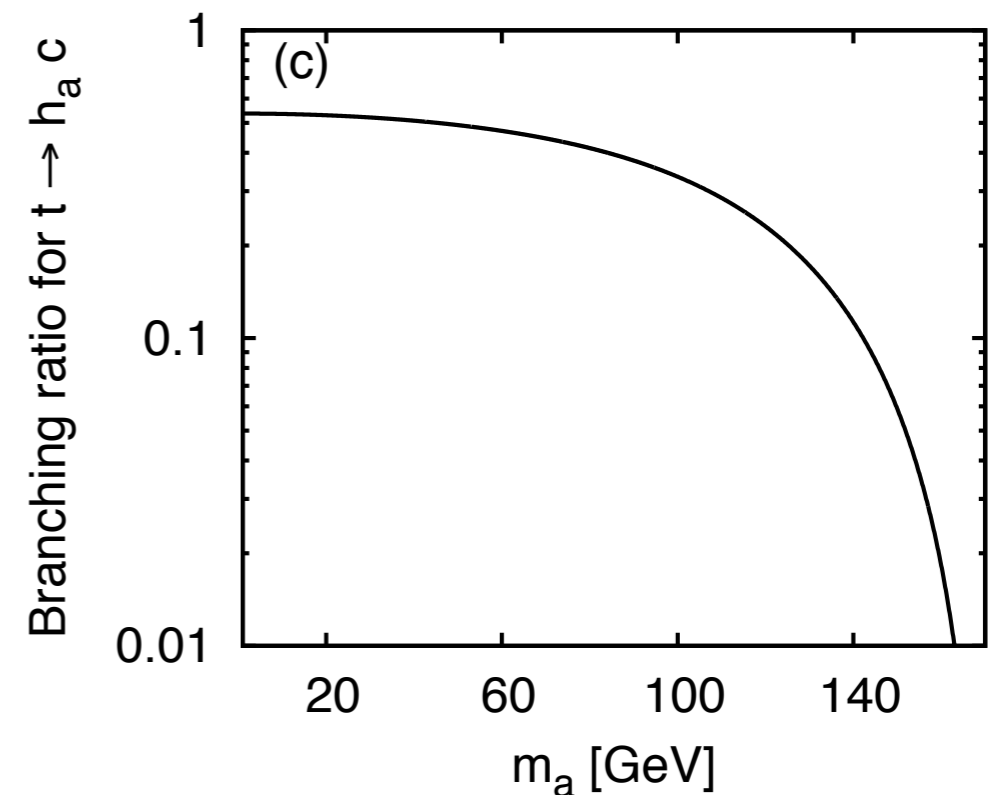
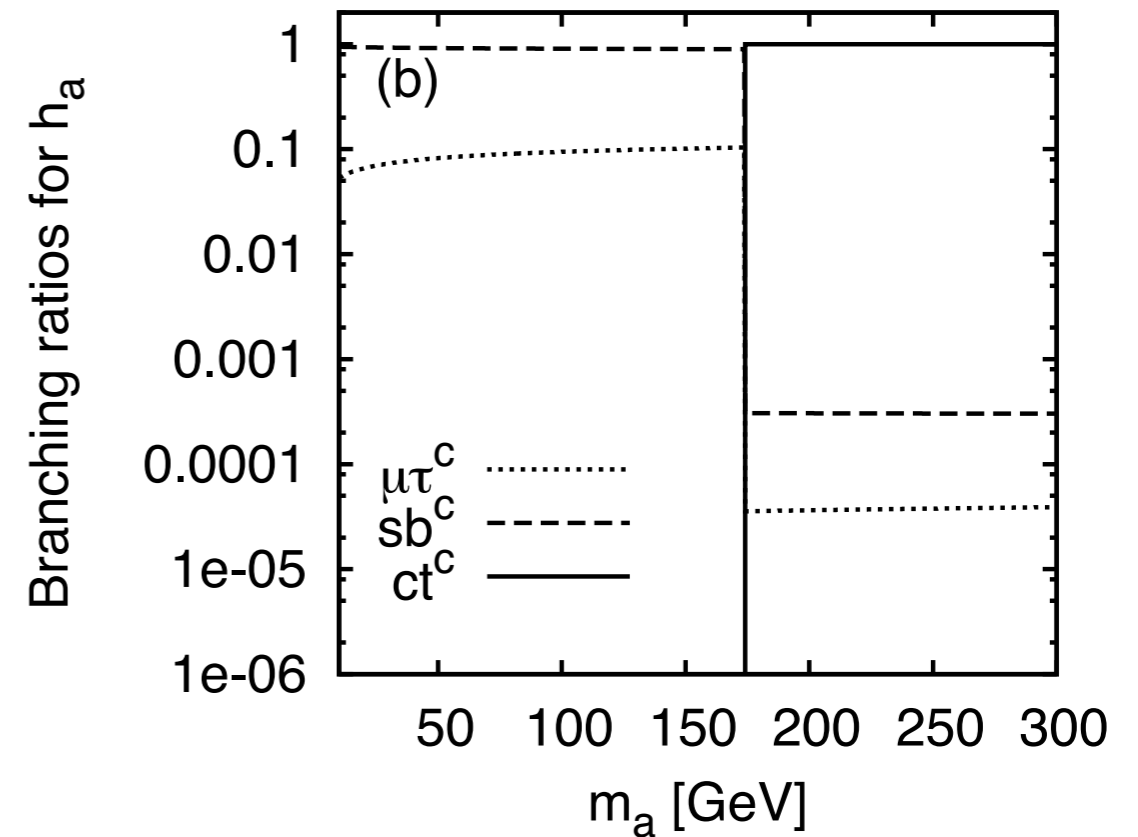
- ▶ Both can decay into usual Higgs decay modes ( $ZZ, WW, b\bar{b}, \gamma\gamma, \dots$ ), but:
- ▶ **Dominant decay** for a light scalar  $h_a$  is three-scalar mode  $h_{b/c} \rightarrow h_a h_a$
- ▶ Parameter  $k$  is the ratio between three-scalar coupling and  $h_b WW$  coupling



- ▶ For  $m_a = 50 \text{ GeV}$ ,  $k \approx 10$
- ▶ Compare to THDM, where it is typically  $5 \lesssim k \lesssim 30$  for a 400 GeV scalar decaying into two 114 GeV scalars

# Signatures of $h_a$

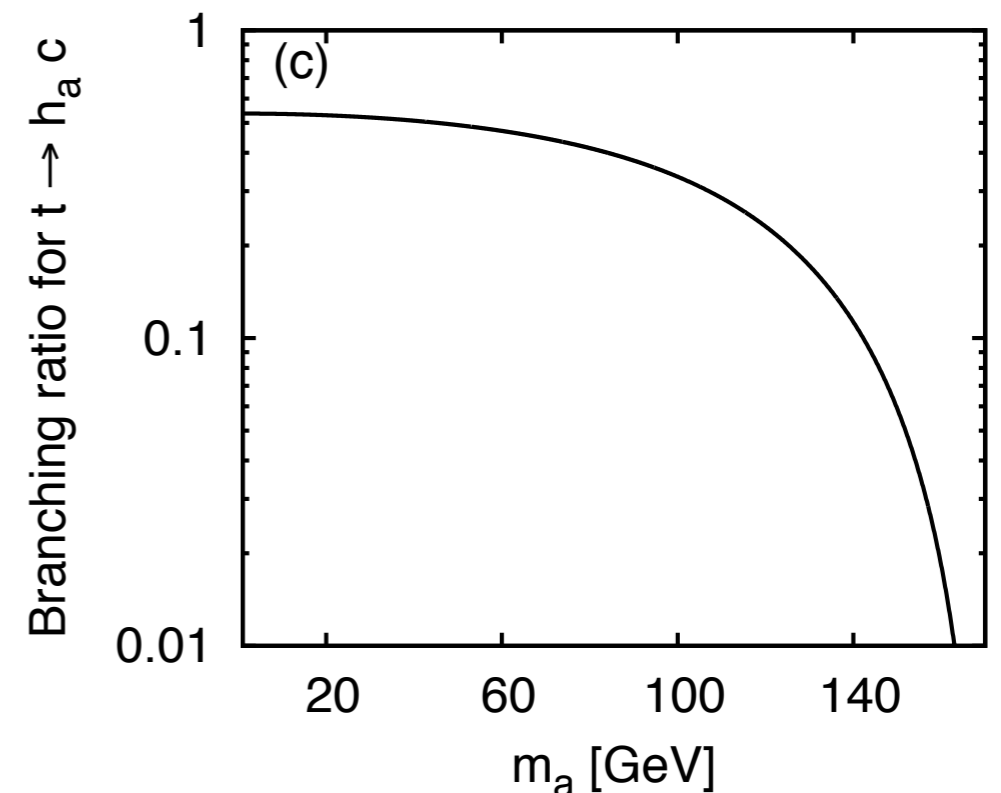
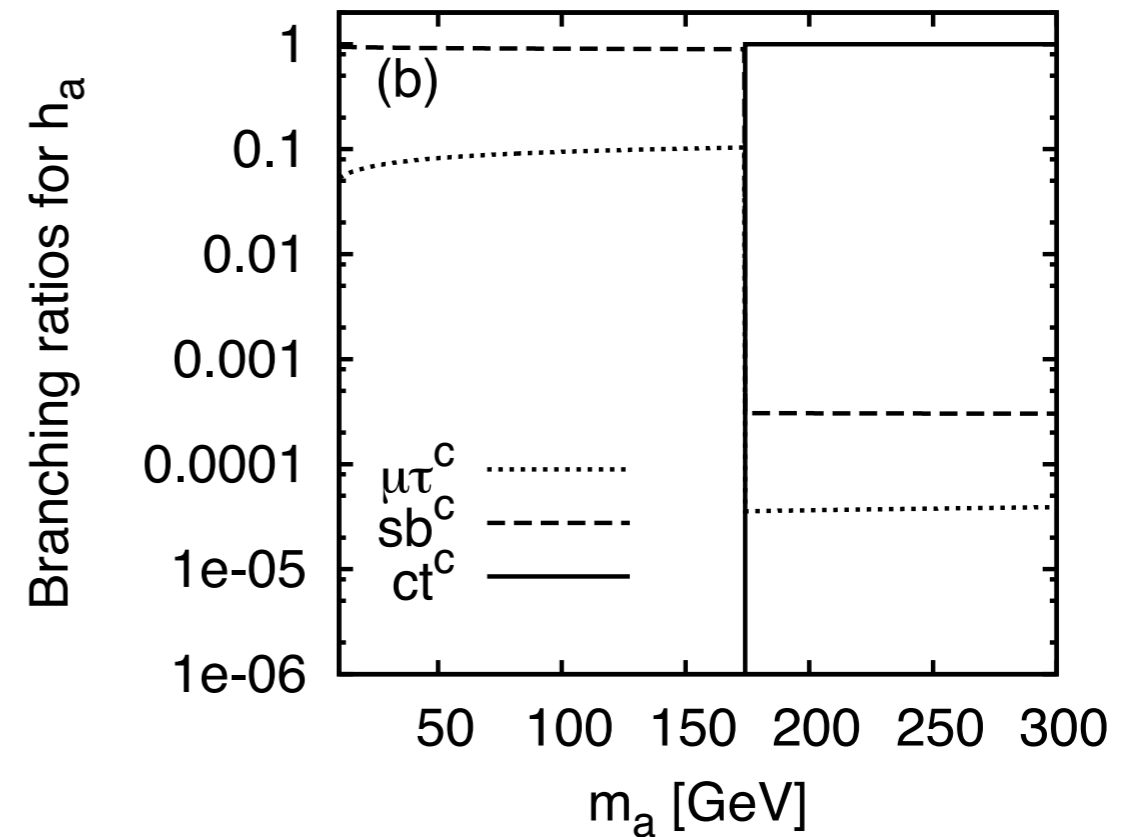
- ▶ As long as  $m_a < m_t$ , the dominant decay mode is into jets
- ▶ Possibly significant decay mode into  $\mu\tau$





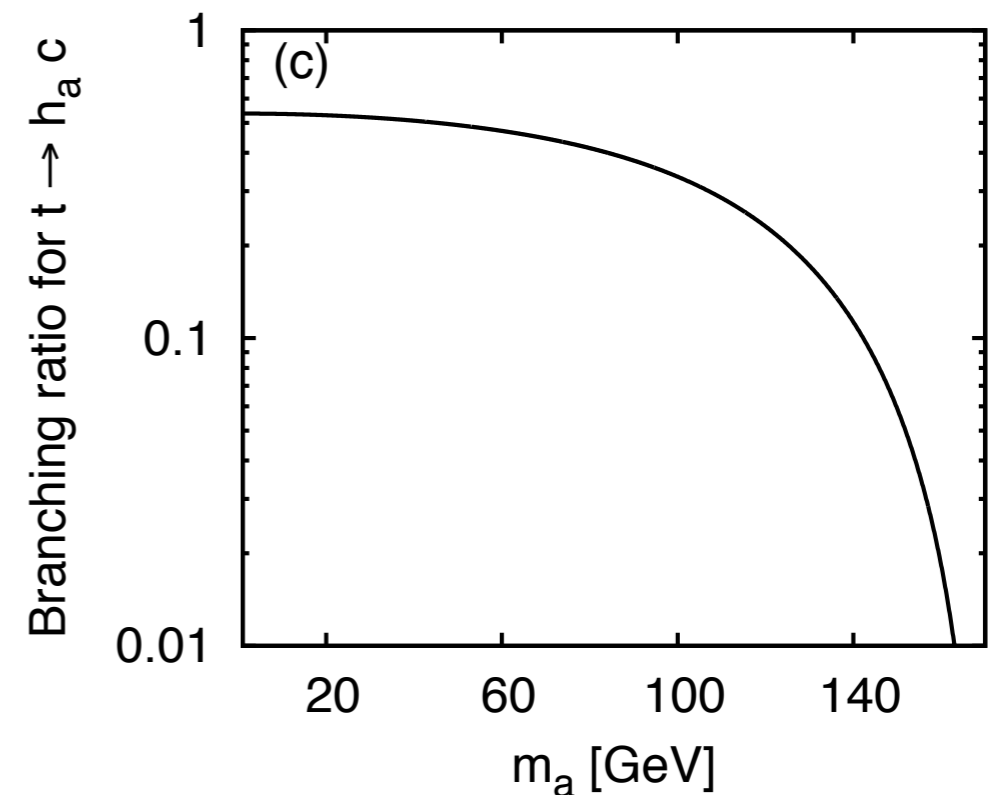
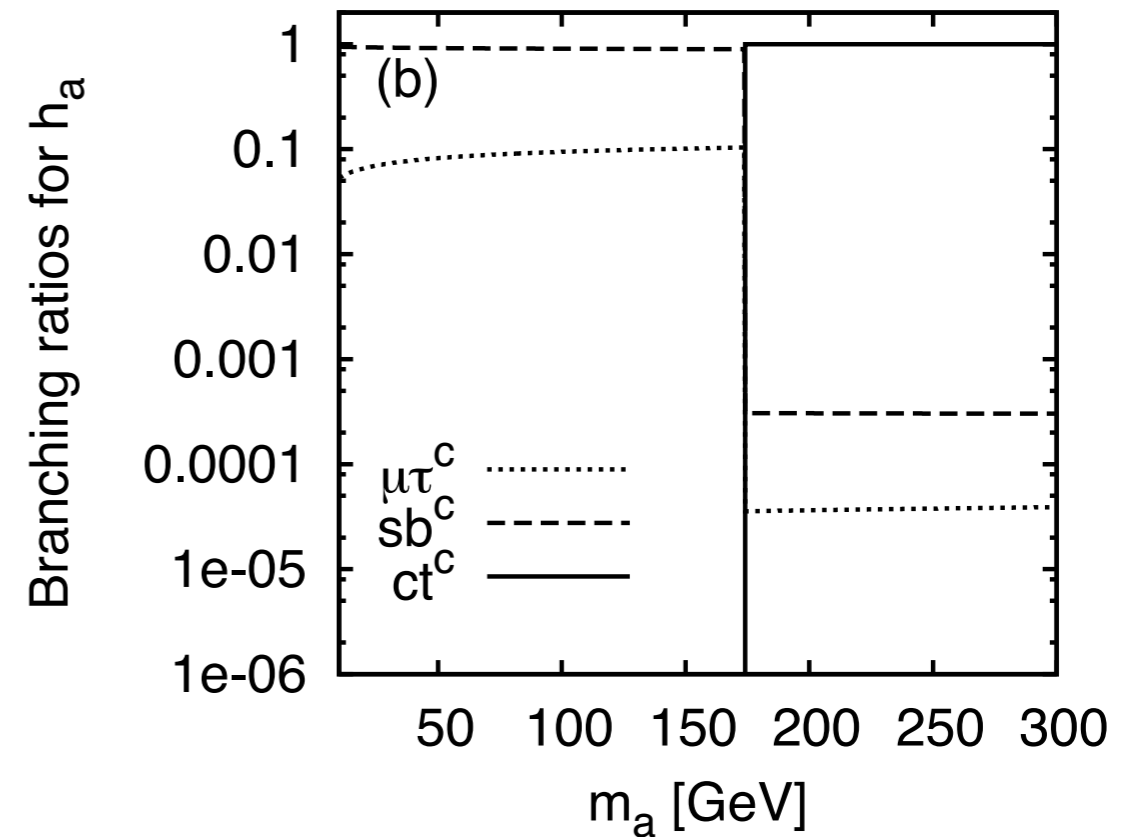
# Production of $h_a$

- ▶ Light  $h_a$  is a decay product of  $h_{b/c}$
- ▶ Production of  $h_a$  possible through **top decays** for light  $h_a$ , subsequent decay into  $\mu\tau$  might be possible to detect
- ▶ For  $m_a > m_t$ ,  $h_a$  dominantly decays off-diagonally into  $ct$



## $h_a$

- ▶ Dependency on vacuum alignment:
- ▶ Quark mixing requires small deviation from (1, 1, 0) vacuum alignment
- ▶  $\Rightarrow$  some weakening of special properties of  $h_a$ , i.e. small three-vertex couplings to vector bosons



# Pseudo-scalars

- ▶ Physical pseudo-scalars  $\chi_a$  and  $\chi_b$  have patterns of couplings to quarks / leptons identical to  $h_a$  and  $h_b/h_c$ :

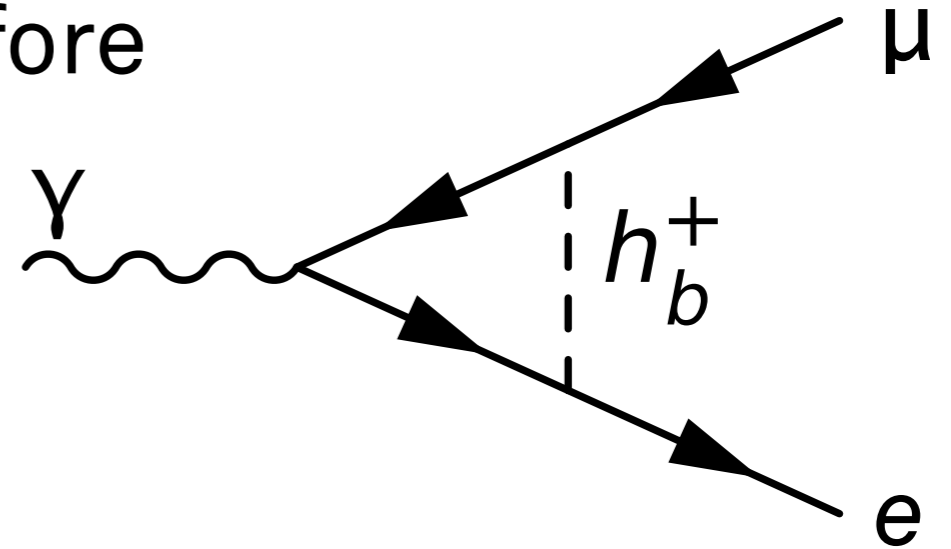
$$Y_{\chi_a} = \begin{pmatrix} 0 & 0 & \gamma_{e_L \tau_R}^a \\ 0 & 0 & \gamma_{\mu_L \tau_R}^a \\ \gamma_{\tau_L e_R}^a & \gamma_{\tau_L \mu_R}^a & 0 \end{pmatrix}, \quad Y_{\chi_b} = \begin{pmatrix} \gamma_{e_L e_R}^b & \gamma_{e_L \mu_R}^b & 0 \\ \gamma_{\mu_L e_R}^b & \gamma_{\mu_L \mu_R}^b & 0 \\ 0 & 0 & \gamma_{\tau_L \tau_R}^b \end{pmatrix}$$

- ▶ In volume of parameter space where  $h_a \rightarrow \chi_a \chi_b$  opens,  $h_a$  cannot be very light

# Charged scalars

$$Y_{h_a^+} = \begin{pmatrix} 0 & 0 & Y_{13}^a \\ 0 & 0 & Y_{23}^a \\ Y_{31}^a & Y_{32}^a & 0 \end{pmatrix}, \quad Y_{h_b^+} = \begin{pmatrix} Y_{11}^b & Y_{12}^b & 0 \\ Y_{21}^b & Y_{22}^b & 0 \\ 0 & 0 & Y_{33}^b \end{pmatrix}$$

- ▶  $h_a^+$  has limited gauge couplings, similar to  $h_a$ : no three-vertices
- ▶ The couplings of  $h_a^+$  and  $h_b^+$  to quarks and leptons follow the same pattern as before
- ▶ There is no  $b \rightarrow s\gamma$ .
- ▶ The off-diagonal (12) coupling of  $h_b^+$  allows for  $\mu \rightarrow e\gamma$



# Summary

- ▶ Scalar sector is an interesting avenue to test flavor symmetries
- ▶  $S_3$  can **explain some mixing angles**, comes with an **enlarged scalar sector**.
- ▶ **Two SM-Higgs-like scalars**  $h_b$  and  $h_c$ . Decay dominantly into third scalar  $h_a$
- ▶ Scalar  $h_a$  has **limited gauge interactions**
- ▶  $h_a$  has only off-diagonal Yukawa couplings, involving a lepton or quark from the third generation
- ▶ Scalars might already be buried in existing LEP or Tevatron data
- ▶ Currently expanding the analysis to include all scalar degrees of freedoms