

Dependence of Z +multi-jet events on the merging scale in TMD
multi-jet merging
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TMD multi-jet merging for Z+jets

A. Bermudez Martinez, F. Hautmann, M.L. Mangano [JHEP 09 (2022) 060]

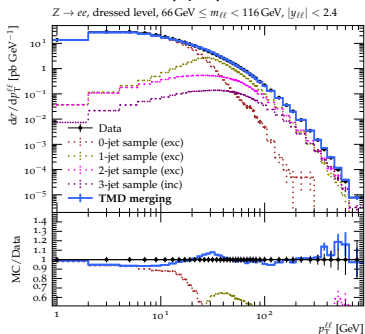
TMD multi-jet merging method

- Include higher order matrix element contributions; hard emissions
- Combining ME with Parton Branching TMDs and TMD ISR within CASCADE3 Baranov S., AMvK, et al. [Eur.Phys.J.C 81 (2021) 5, 425]

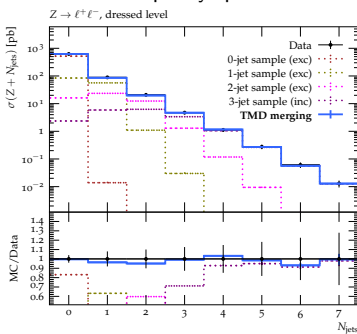
Z + 0,1,2,3 jets at $\sqrt{s} = 8$ TeV, $m_{ll} \simeq m_Z$
merged with

Parton Branching TMD and $E_{\perp, \text{clus}} = 23$ GeV

Z boson p_T spectrum



Jet multiplicity spectrum



Motivation for high DY mass studies

- TMD merging predictions accurate up to high jet p_T and large N_{jets} due to properly combining matrix element and parton showers
- Combination depends on merging parameters:

$$R_{clus}, E_{\perp,clus}, \eta_{max,clus}$$

- The merging scale $E_{\perp,clus}$ separates **hard radiation** from **soft radiation**.
 - **Hard radiation** should come from the matrix element: $p_T > E_{\perp,clus}$
 - **Soft radiation** should come from the parton shower: $p_T < E_{\perp,clus}$
- Does this methodology still work when we move away from the Z mass and to events with a very different hard scale?
- Interesting question in its own right and from experimental point of view; measurements of Z + jets starting to be performed e.g. by *CMS collaboration* in [Eur.Phys.J.C 83 (2023) 7, 628]

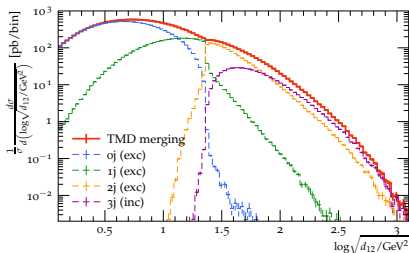
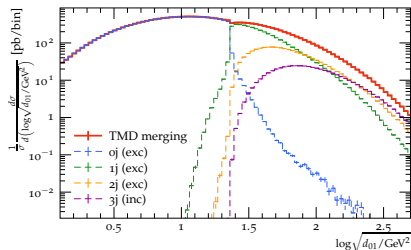
Differential jet rates for test of methodology

Test of merging algorithm: **Differential jet rates (DJRs)** d_{ij}

$d_{i,(i+1)}$ contains the squared energy scale at which an i -jet configuration is resolved in an $(i + 1)$ -jet configuration

The **smoothness** of DJRs is a strong indication of the efficiency and accuracy of the merging algorithm.

Z +jets @ $\sqrt{s} = 13$ TeV with $m_{ll} \simeq m_Z$ and $E_{\perp, \text{clus}} = 23$ GeV
 k_T jet algorithm



Merging scale test: smoothness DJR

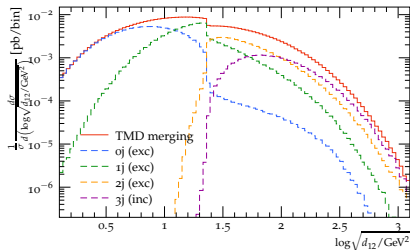
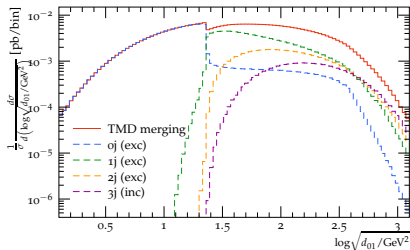
Generate DY hard scattering events with high di-lepton mass with MADGRAPH5:

$$m_{ll} = 800 \text{ GeV}$$

TMD PDFs + TMD shower + TMD merging with CASCADE3

Calculated DJRs show **large discontinuities** when

$$E_{\perp, \text{clus}} \equiv \mu_m = 23 \text{ GeV}$$

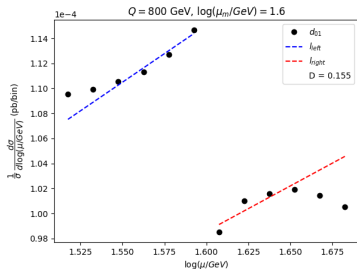


Definition of smoothness in DJR

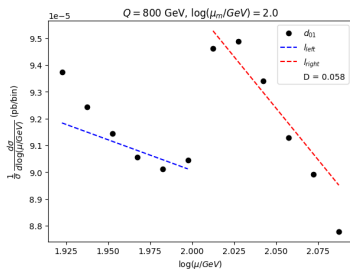
- Zoom on merging scale region in d_{01}
- Fit tangent lines to both sides of the discontinuity: $l = a \log(\sqrt{d_{ij}}) + b$
 - 0th-order discontinuity equals: $l_{left}(\mu_m) - l_{right}(\mu_m)$
 - 1st-order discontinuity includes slope: $a_{left}\delta - a_{right}\delta$
- Result is the following quantification of discontinuity:

$$D(Q, \mu_m) = \frac{|L_l(\mu_m) - L_r(\mu_m)|}{(L_l(\mu_m) + L_r(\mu_m))/2}$$

with $L_i(\mu) = l_i(\mu) + a_i \cdot \delta$.



$$m_{ll}^{\min} = 800 \text{ GeV}, \mu_m = 40 \text{ GeV}$$



$$m_{ll}^{\min} = 800 \text{ GeV}, \mu_m = 100 \text{ GeV}$$

Smoothness distribution from d_{01} analysis

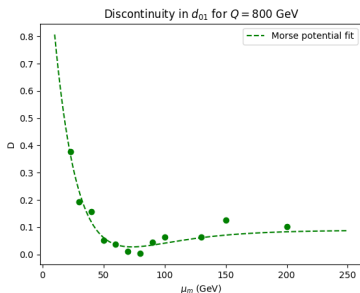
- Distribution of discontinuity D versus the merging scale μ_m values
- Minimum discontinuity reflects **the merging scale that works well** $\mu_m^{(0)}$

Morse potential

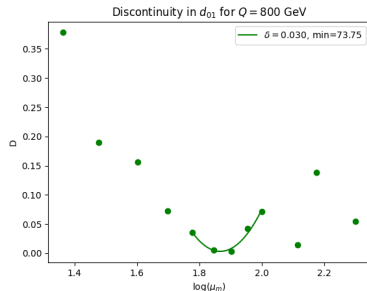
$$D_{fit} = a \left(e^{-2b(\mu_m - c)} - 2e^{-b(\mu_m - c)} \right) + d$$

Parabola

$$D_{fit} = a(\log_{10}(\mu_m))^2 + b \log_{10}(\mu_m) + c$$



Linear scale



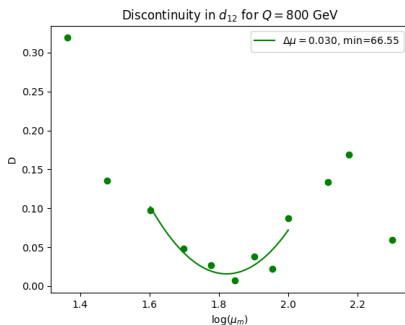
Logarithmic scale

- Shape of this distribution is "Morse potential"-like (nuclear physics)
- Use **polynomial fit through points near the minimum**

Smoothness distribution from d_{12} analysis

- Move to higher order DJR: d_{12}
- Observe similar behavior of discontinuities

$$D_{fit} = a(\log(\mu_m))^2 + b \log(\mu_m) + c$$



- Log scale, smoothest DJR at $\mu_m \sim 10^{1.85} \simeq 70$ GeV

Theoretical uncertainties

Which sources of uncertainty on $\mu_m^{(0)}$? Two uncertainty sources at DJR level:

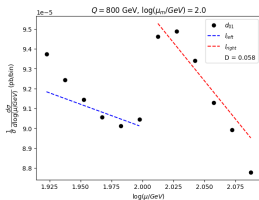
- Statistical: Monte Carlo errors calculated by varying DJR using σ_{MC} ; tiny variations, $\leq 0.5\%$
- Systematic: bin size of DJR $\delta = \Delta \log(\sqrt{d_{ij}/\text{GeV}^2})$

Bin size uncertainties

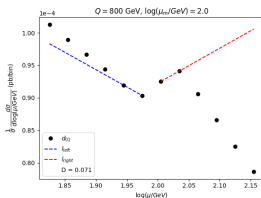
- Vary bin size δ by adding bins of DJR to have $\delta \in \{0.015, 0.030, 0.045\}$
- Tangent line fitted only through a few data points:
 - $\delta = 0.015$: fit of $l(\mu)$ through 4 data points
 - $\delta = 0.030$: fit of $l(\mu)$ through 2 data points
 - $\delta = 0.045$: fit of $l(\mu)$ through 2 data points

Example d_{01} for $m_{H^{\pm}} = 800$ GeV, $\mu_m = 100$ GeV

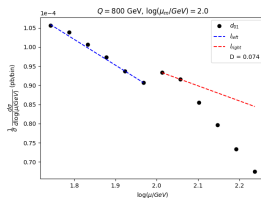
$\delta = 0.015$



$\delta = 0.030$

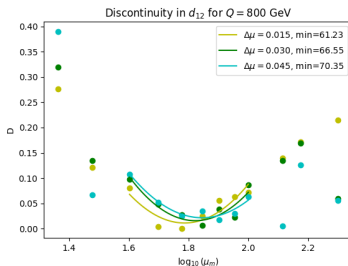
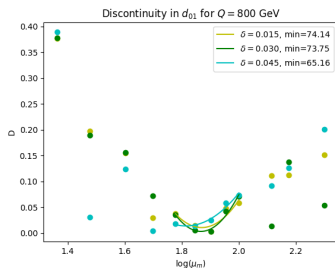


$\delta = 0.045$



Systematic uncertainties

Three distributions D for the same hard scale Q for d_{01} (left) and d_{12} (right):



- Shape of discontinuity most pronounced near minimum
- Bin size uncertainty calculated by:

$$\sigma_{bin.} = \frac{1}{2} \left(\max_k \mu_{m,k}^{(0)} - \min_k \mu_{m,k}^{(0)} \right) \quad (1)$$

A second source of systematic uncertainty: number of data points used for fitting D .

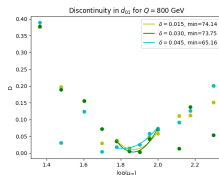
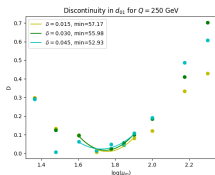
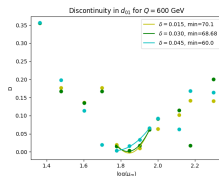
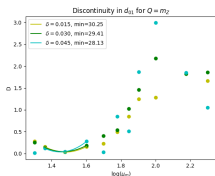
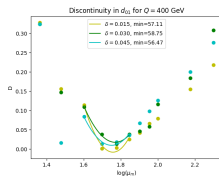
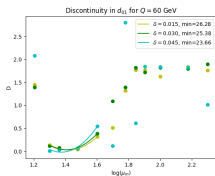
This error is circumvented!

\Rightarrow pick data close to the minimum and use χ^2 for goodness of fit.

Multiple DY mass windows

Six sets of hard scattering events (LHE) with hard scales $Q = m_{ll}$:

- $Q = 60$ GeV:
 $m_{ll}^{\min} = 58$ GeV, $m_{ll}^{\max} = 62$ GeV
- $Q \simeq m_Z$:
 $m_{ll}^{\min} = 40$ GeV
- $Q = 250, 400, 600, 800$ GeV:
 $m_{ll}^{\min} = Q$
- Shape of discontinuity distributions for various masses is similar!
- **Remarkable observation:** minimum $\mu_m^{(0)}$ shifts with the increase of the hard scale!



Same features at higher order DJR d_{12}

Final results

- Plot results for merging scales $\mu_m^{(0)}$ versus the hard scale Q with $\sigma = \sqrt{\sigma_{bin}^2 + \sigma_{stat}^2}$.
- Data from d_{01} and d_{12} follow similar pattern

Find the functional form of $\mu_m^{(0)}(Q)$:

- Ansatz; logarithmic behavior with off-set
- Z boson mass used in ansatz to fix the units
- Leaves two free parameters to fit

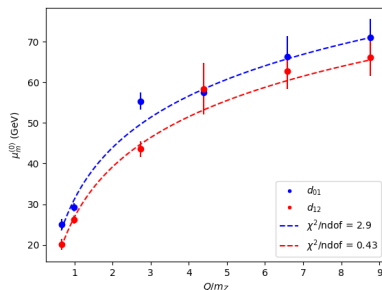
$$\mu_m^{(0)} = m_Z \left(a + b \ln \left(\frac{m_{||}}{m_Z} \right) \right)$$

Fits result in

$$\mu_m^{(0)}(m_{||}) = m_Z \left(0.34 + 0.20 \ln \left(\frac{m_{||}}{m_Z} \right) \right) \quad \text{for } d_{01}$$

$$\mu_m^{(0)}(m_{||}) = m_Z \left(0.29 + 0.20 \ln \left(\frac{m_{||}}{m_Z} \right) \right) \quad \text{for } d_{12}$$

Note that $\mu_m^{(0)} \simeq m_Z/3$ in case $m_{||} = m_Z$



- Studies on differential jet rates of $Z + \text{jets}$ in TMD merging
- A **measure for smoothness** D is defined which includes two orders of discontinuity: the zeroth and first order.
- Jet merging is studied for varying di-lepton masses from 60 GeV up to 800 GeV
- Systematic (bin size) and statistical (Monte Carlo) uncertainties are included
- An expression for the merging scale dependence on the DY mass is found corresponding to results from both analyses of d_{01} as d_{12} :

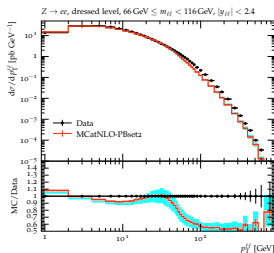
$$E_{\perp, \text{clus}}^{(0)}(m_{ll}) = \mu_m^{(0)}(m_{ll}) = m_Z \left[0.3 + 0.2 \ln \left(\frac{m_{ll}}{m_Z} \right) \right]$$

Backup

Combining PB with higher orders

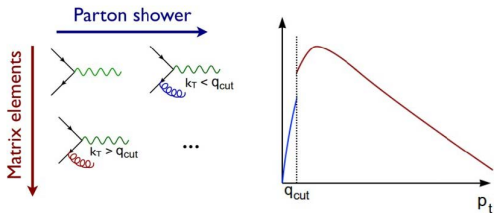
Matching TMD and NLO

- Match with MC@NLO procedure, subtraction terms HERWIG6
- Intermediate p_T region described
- Deficit at large p_T



Multi-jet merging at TMD level New!

- Include higher fixed-order calculations: **multi-jets**
- Make ME exclusive by Sudakov suppression
- Avoid double counting between initial state TMD evolution & hard emissions



$$\begin{aligned}
 & - \text{1st emission PS: } \mathcal{R}^{PS}(p_t^2) \times \exp \left[- \int_{p_t^2} dp_t'^2 \frac{\mathcal{R}^{PS}(p_t'^2)}{B} \right] \\
 & - \text{1st emission ME: } \mathcal{R}(p_t^2) \rightarrow \mathcal{R}(p_t^2) \times \exp \left[- \int_{p_t^2} dp_t'^2 \frac{\mathcal{R}^{PS}(p_t'^2)}{B} \right]
 \end{aligned}$$

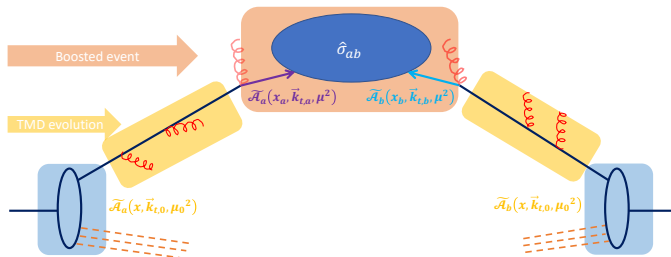
figure by A. Bermudez Martinez \rightarrow

TMD merging

A. Bermudez Martinez, F. Hautmann, M.L. Mangano Phys.Lett.B 822 (2021) 136700

TMD multi-jet merging method

- 1 Evaluate n-jet matrix elements: $\hat{\sigma}_{ab}$
- 2 Reweight the strong coupling
- 3 Apply forward PB-TMD evolution with condition: $|k_t|^2 \leq \mu_{min}^2$
- 4 Shower the events using the backward PB evolution
- 5 Apply MLM¹ prescription between **boosted events** and the **showered events**



¹Other merging prescriptions can potentially also be used