ESSNUSB+ PROJECT: TOWARDS PRECISION MEASUREMENT OF THE CP VIOLATION AT THE SECOND NEUTRINO OSCILLATION MAXIMUM

ALESSIO GIARNETTI, ON BEHALF OF THE ESSNUSB+ PROJECT

Co-funded by the European Union

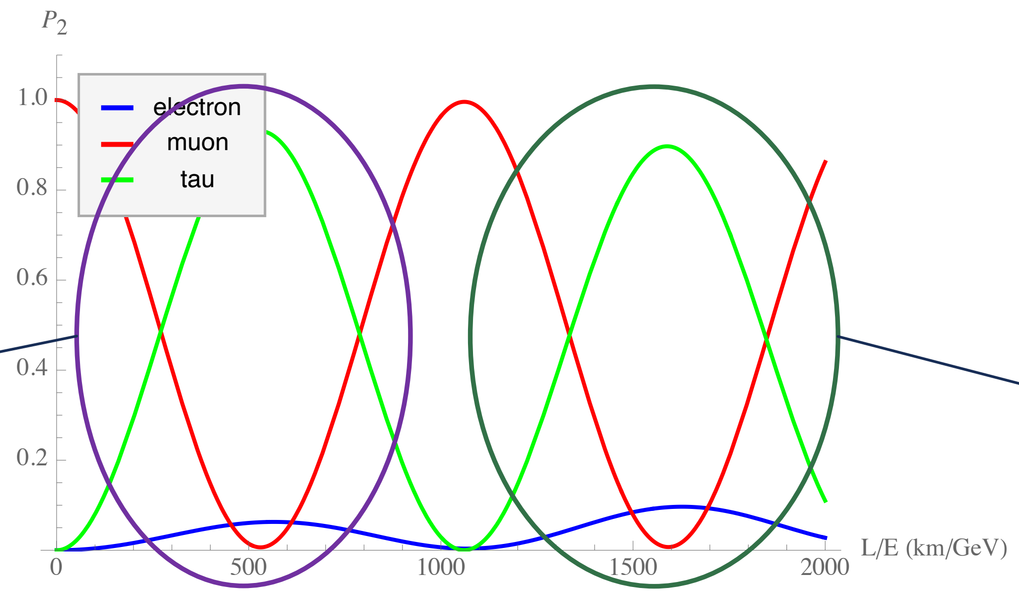
ESS neutrino Super Beam plus

EPS-HEP, HAMBURG, 22/08/2023

ROMA TRE UNIVERSITÀ DEGLI STUDI

ESSNUSB/ESSNUSB+: NEUTRINO OSCILLATION AT SECOND MAXIMUM

ESSnuSB/ESSnuSB+ is a design study for a next-to-next generation neutrino oscillation experiment which aims at the precise measurement of the CP violation in the leptonic sector looking at neutrino oscillation at the second atmospheric oscillation maximum.



LBL experiments

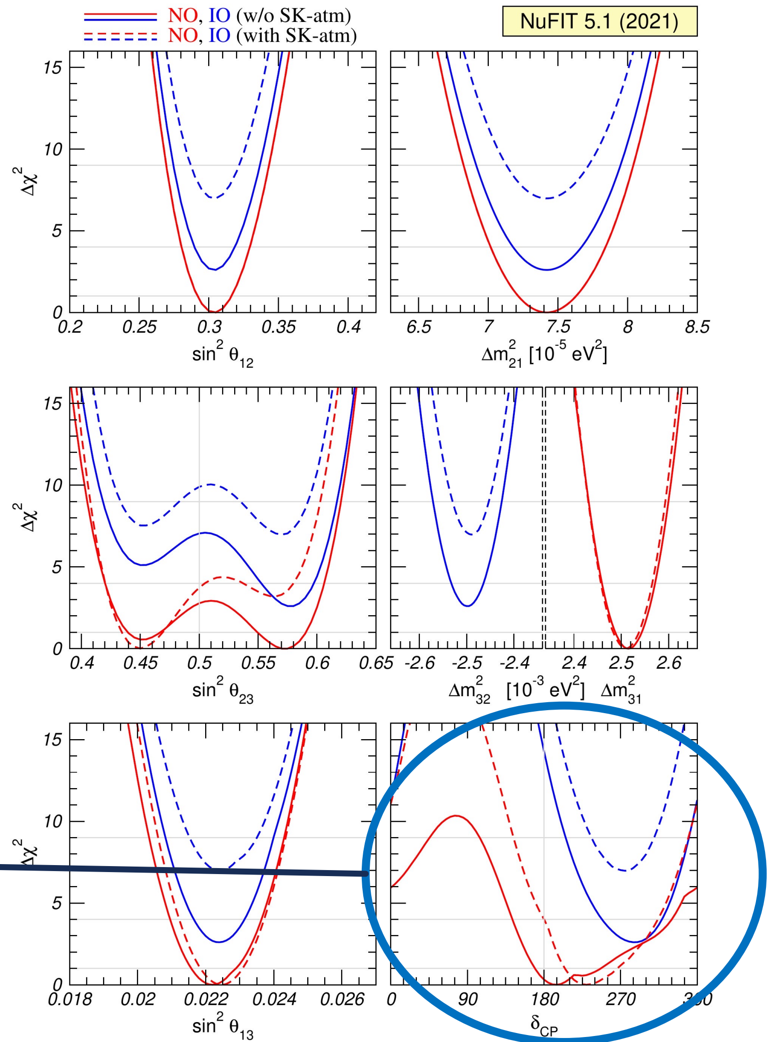
ESSnuSB

OSCILLATION PHYSICS AT THE SECOND MAXIMUM

In the precision era for the oscillation parameters measurements, we still do not know the amount of CP violation in the leptonic sector.

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{CP}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{CP}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{CP}} & c_{23}c_{13} \end{pmatrix}$$

Most of the possible values for the mixing matrix phase are allowed by current measurements, especially in Normal Ordering



OSCILLATION PHYSICS AT THE SECOND MAXIMUM

How to measure the phase?

$\bar{J} \equiv cos\theta_{13} sin2\theta_{12} sin2\theta_{23} sin2\theta_{13}$

Electron neutrino appearance

$$P(\nu_\mu \to \nu_e) = \underbrace{sin^2\theta_{23} sin^2 2\theta_{13} sin^2\left(\frac{\Delta m^2_{31} L}{4E}\right)}_{\text{Atmospheric oscillations, leading term}} + \underbrace{cos^2\theta_{23} sin^2 2\theta_{12} sin^2\left(\frac{\Delta m^2_{21} L}{4E}\right)}_{\text{Solar subleading term}} + \underbrace{\bar{J} cos\left(\delta_{CP} - \frac{\Delta m^2_{31} L}{4E}\right) sin\left(\frac{\Delta m^2_{21} L}{4E}\right) sin\left(\frac{\Delta m^2_{31} L}{4E}\right)}_{\text{Interference term, depends on the phase!}}$$

Atmospheric oscillations, leading term

Solar subleading term

Interference term, depends on the phase!

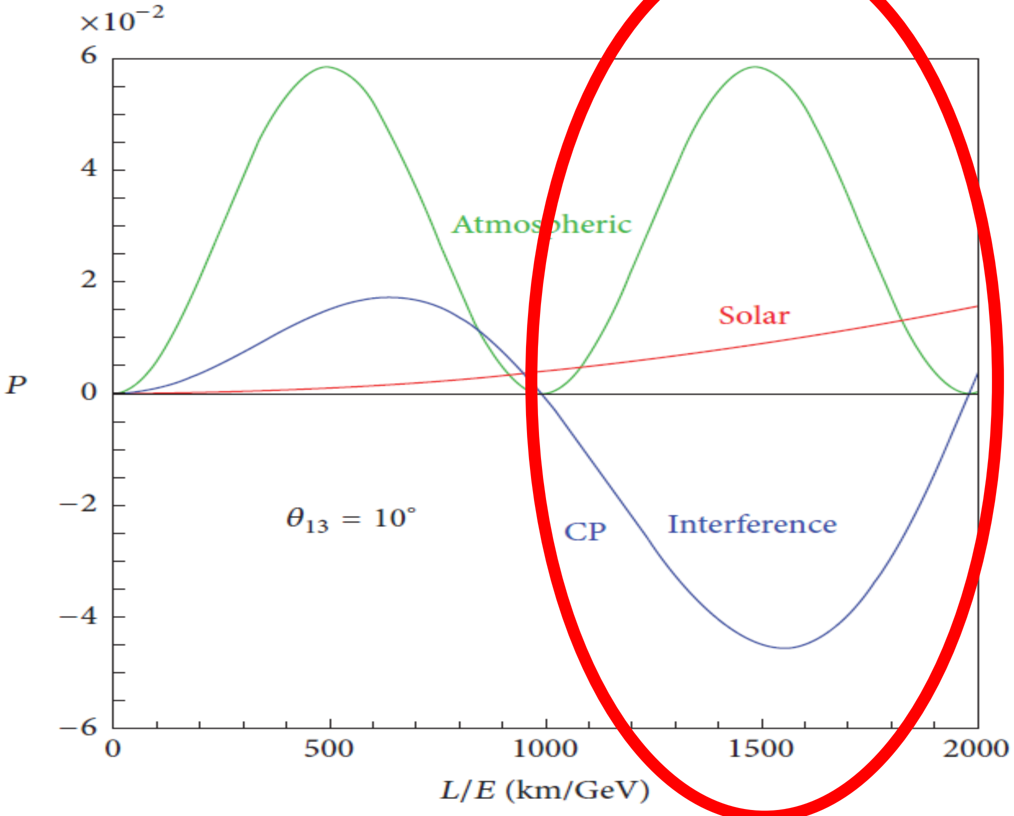
CP VIOLATION → $P_{\nu_\mu \to \nu_e} \neq P_{\overline{\nu}_\mu \to \overline{\nu}_e}$ $(\delta \to -\delta)$

We want to look at both electron neutrino and antineutrino appearance starting with two different fluxes:

Muon neutrinos and Muon antineutrinos

OSCILLATION PHYSICS AT THE SECOND MAXIMUM

Why 2° maximum?



arXiv:1110.4583v2 (2012)

$$\mathcal{A}_{CP}^{\alpha\to\beta} = P_{\nu_\alpha\to\nu_\beta} - P_{\overline{\nu}_\alpha\to\overline{\nu}_\beta}$$

<u>At the second oscillation maximum the interference term is large!</u>

$$\frac{\mathcal{A}_{CP}^{\mu\to e}\left(x_{\max}^{(2)}\right)}{\mathcal{A}_{CP}^{\mu\to e}\left(x_{\max}^{(1)}\right)} \approx 2.7$$

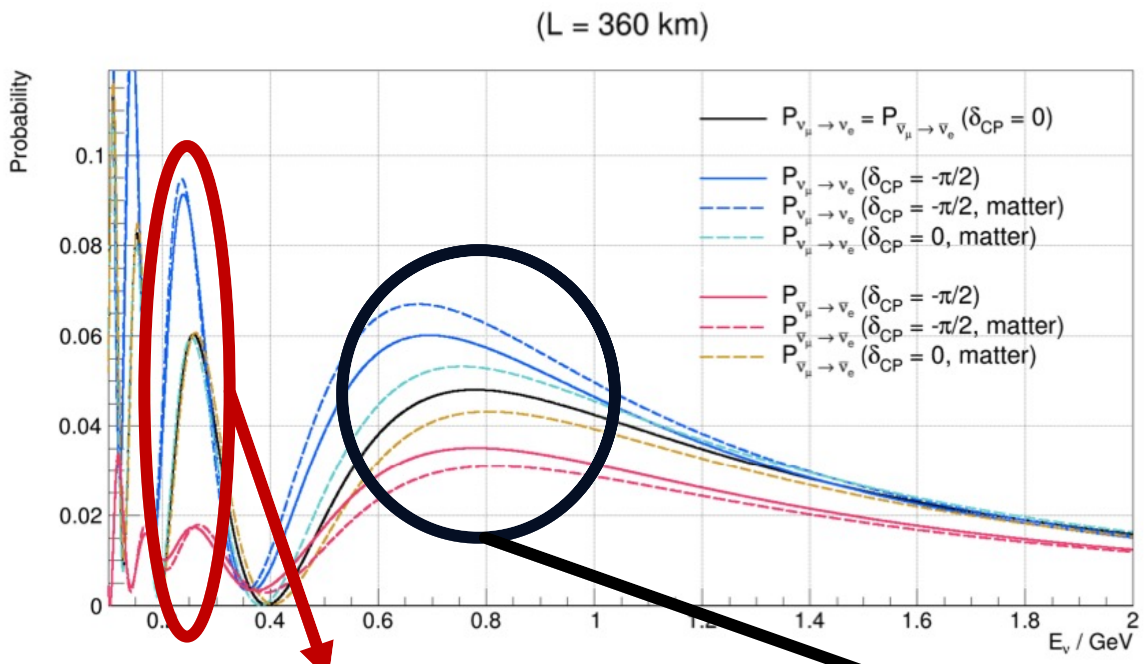
OSCILLATION PHYSICS AT THE SECOND MAXIMUM

What about matter effects?

$$i\frac{d}{dt}\begin{pmatrix}\nu_e\\ \nu_\mu\\ \nu_\tau\end{pmatrix} = \left[\frac{1}{2E_\nu}U\begin{pmatrix}0 & 0 & 0\\ 0 & \Delta m^2_{21} & 0\\ 0 & 0 & \Delta m^2_{31}\end{pmatrix}U^\dagger + A_{CC}\begin{pmatrix}1 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 0\end{pmatrix}\right]\begin{pmatrix}\nu_e\\ \nu_\mu\\ \nu_\tau\end{pmatrix}$$

Change sign for antineutrinos,
like the CP-violating phase

FAKE CP VIOLATION

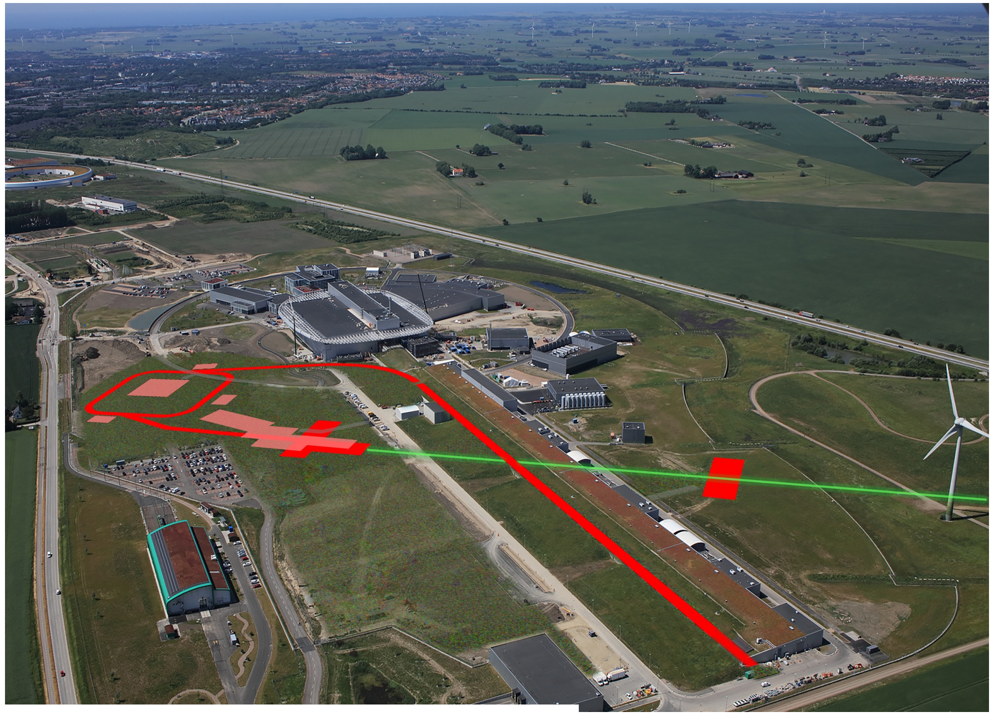


Second maximum, the matter effects are not important,
pure phase determination

First maximum, matter and CP phase have the same effect

THE ESSNUSB PROJECT (2017-2022)

ESS PROTON ACCELERATOR



EUROPEAN SPALLATION SOURCE

First beam on target expected in 2026.

Under construction in Lund, Sweden

•The ESS will be a copious source of spallation neutrons.

•**5 MW average beam power.**

•14 Hz repetition rate (2.86 ms pulse duration, 10^{15} protons).

•Duty cycle 4%.

•2.0 GeV kinetic energy protons

•○ up to 3.5 GeV with linac upgrades

•**>2.7x10^{23} p.o.t/year.**

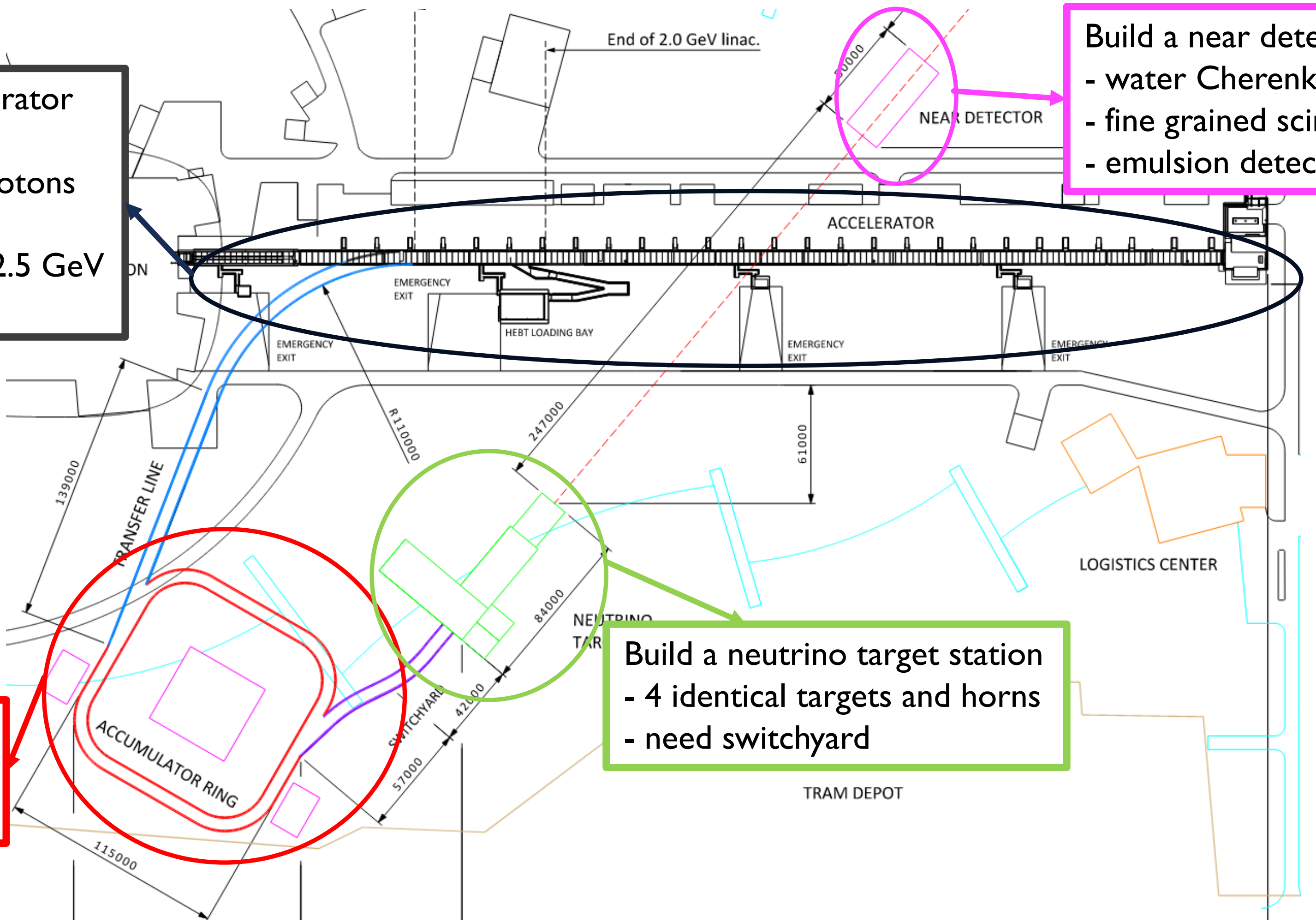
From such a powerful accelerator, we can produce an intense neutrino beam!

The European Spallation Source neutrino Super Beam (ESSνSB)

UPGRADE OF THE ESS SITE

Upgrade of the accelerator
- 14 Hz to 28 Hz
- use H^- instead of protons in ESSnuSB cycles
- increase energy to 2.5 GeV kinetic

Build a near detector site
- water Cherenkov detector
- fine grained scintillator
- emulsion detector



Build a neutrino target station
- 4 identical targets and horns
- need switchyard

Build an accumulator ring
- shorten ESS pulses from 2.86 ms to ≈ 1 μs

NEUTRINO PRODUCTION: TARGET STATION

Hot Cell
- Able to manipulate/repair hadronic collector
- Work under Radioactive Environment

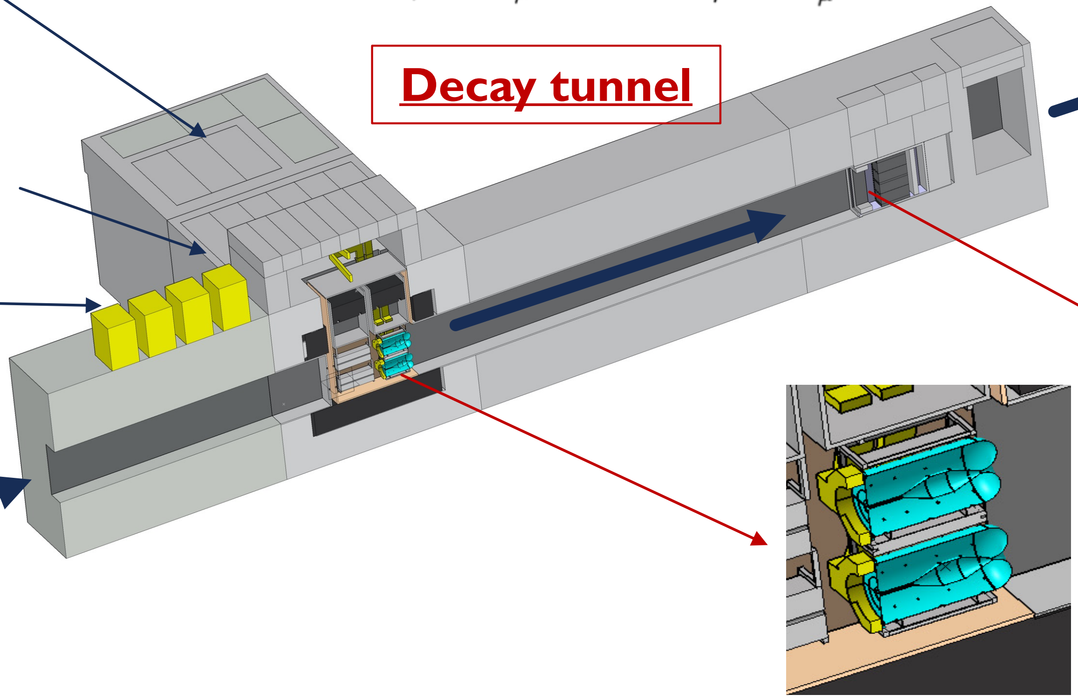
$\pi^+ \rightarrow \mu^+ + \nu_\mu$ $\pi^- \rightarrow \mu^- + \overline{\nu}_\mu$

Neutrino beam

Decay tunnel

Power Supply Unit
- 16 modules (350 kA, 1.3 μs)
- Located above the switchyard
- Outside of radioactive part of Facility

Morgue
To Store radioactive wastes

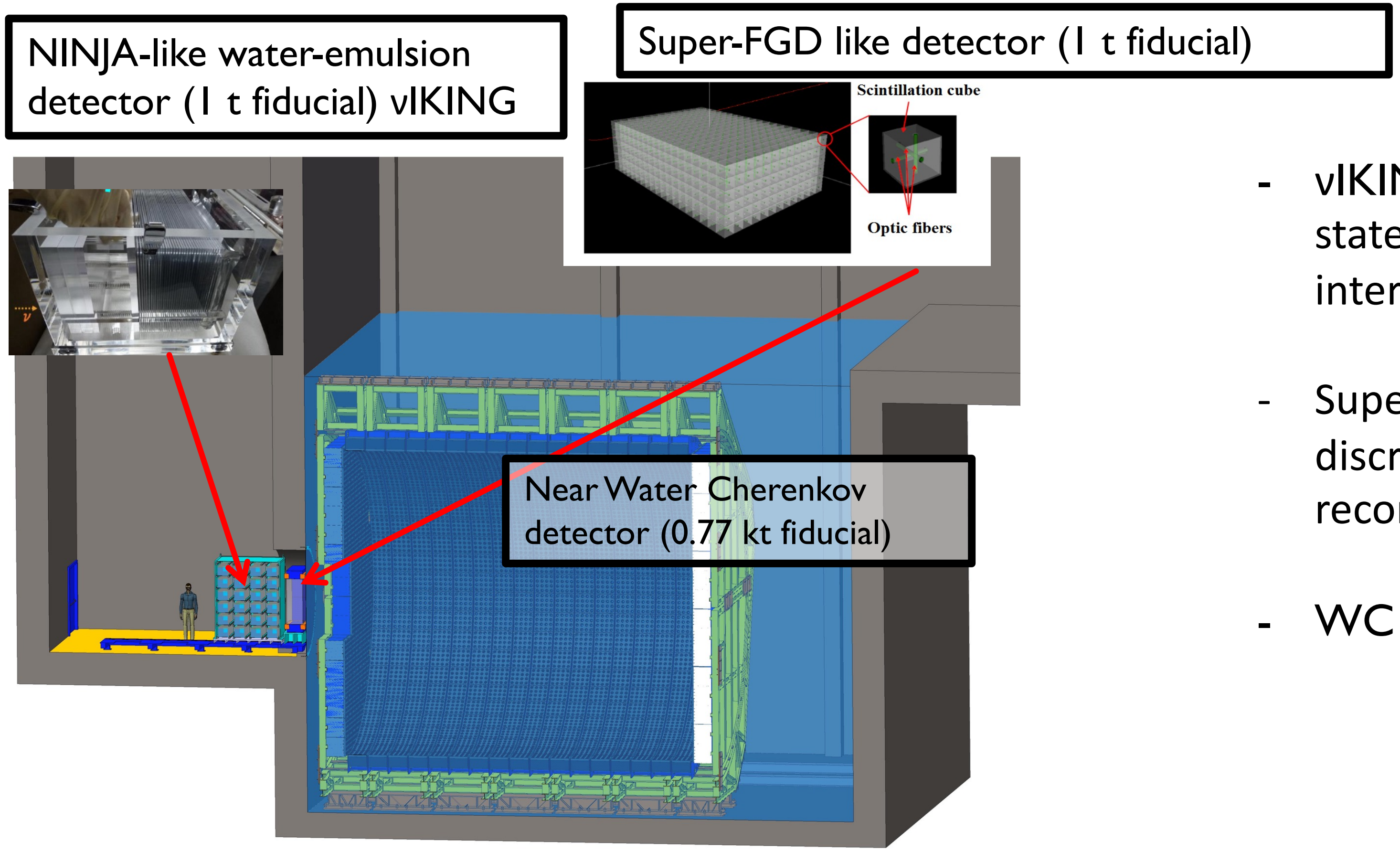


Beam dump

Proton Beam
(Ep=2.5 GeV, 14 Hz)
4 x 1.25 MW

Hadronic Collector: Target + Horns

NEAR DETECTOR SITE

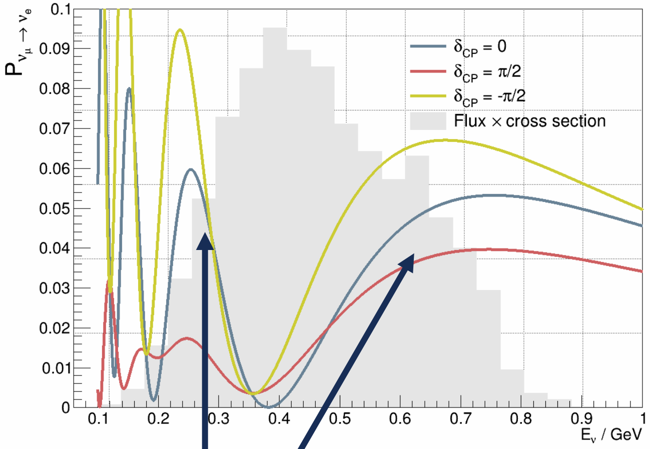


- νIKING: precise measurement of the final state topology of the neutrino–water interactions

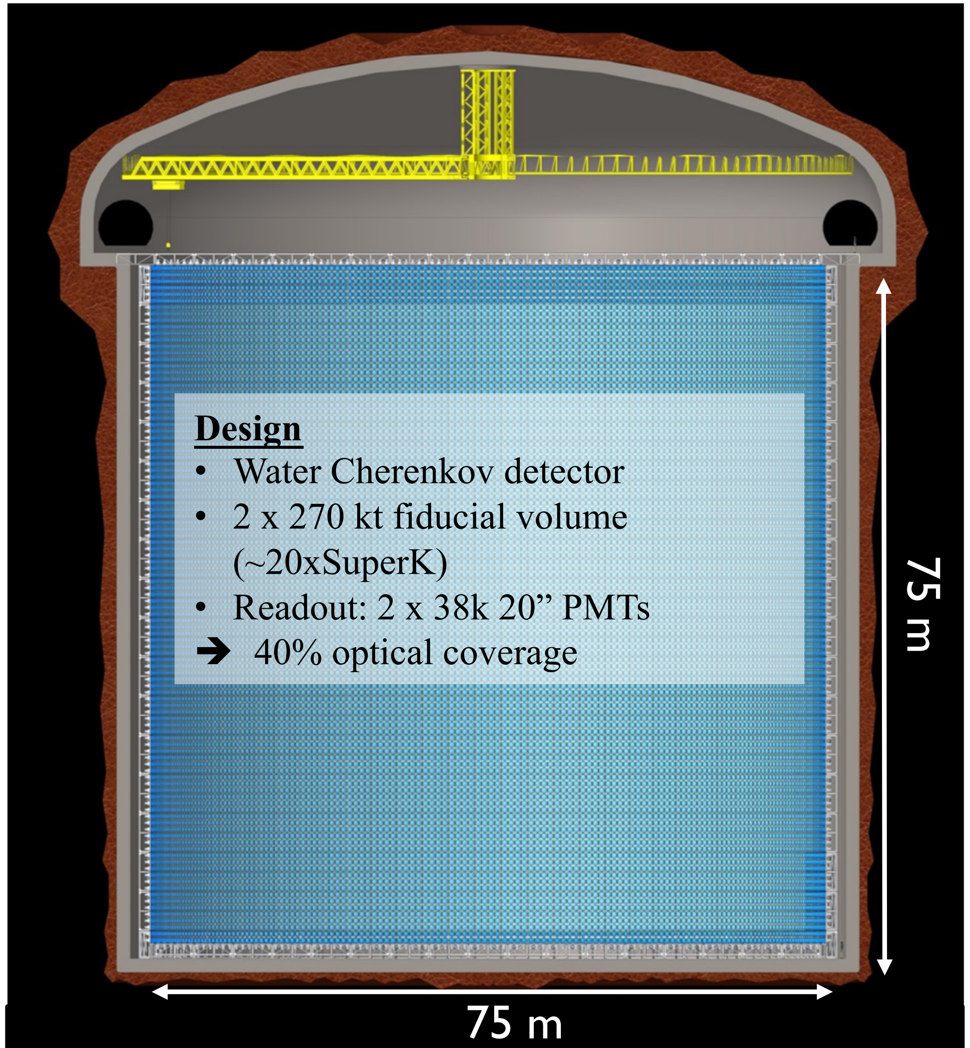
- Super-FGD: magnetized, charge discrimination and neutrino energy reconstruction for the ND detectors

- WC detector: flux determination

THE FAR DETECTOR



First and second oscillation maxima covered at 365 km baseline!



THE EVENT SPECTRA AT 360 KM

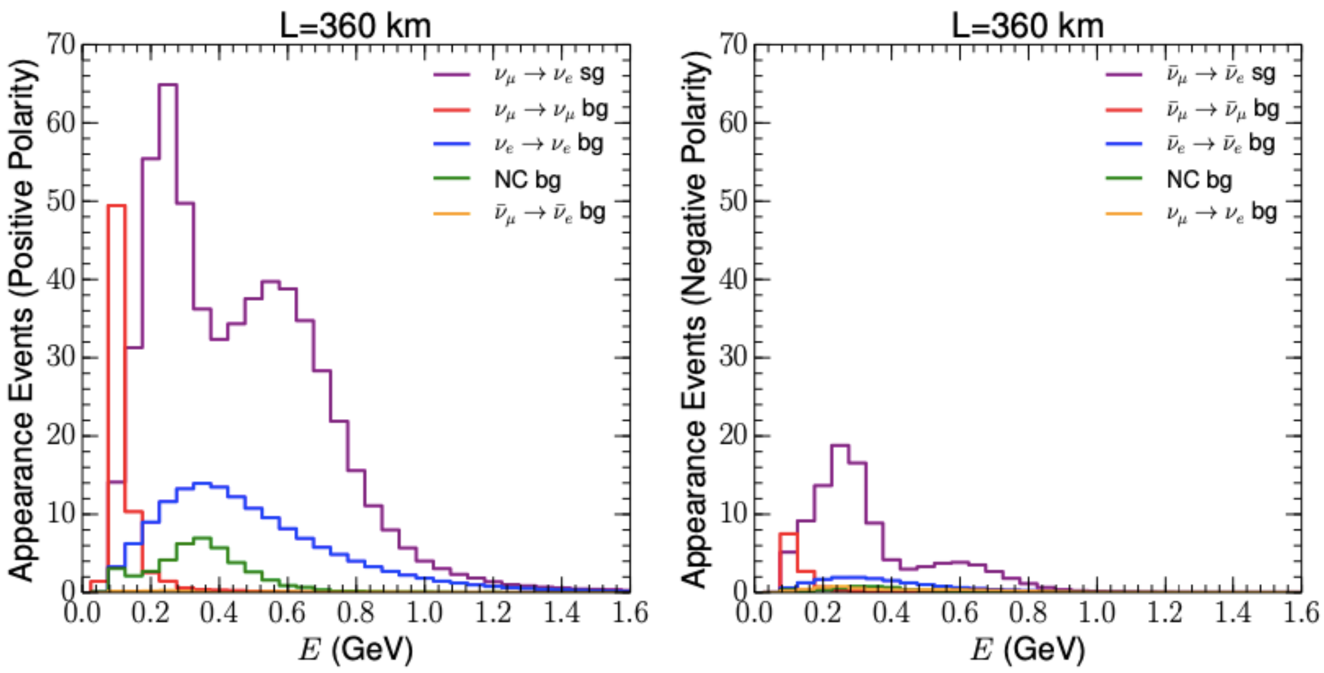
Table 29 Number of expected neutrino interactions in the detector per running year, per flavour and interaction type, and per each horn polarity

All interactions

	ν_μ CC	ν_e CC	$\bar{\nu}_\mu$ CC	$\bar{\nu}_e$ CC	ν_μ NC	ν_e NC	$\bar{\nu}_\mu$ NC	$\bar{\nu}_e$ NC
Positive polarity	5.20×10^7	1.07×10^6	9.25×10^4	1.11×10^3	4.42×10^7	6.11×10^5	3.36×10^5	8.72×10^2
Negative polarity	1.06×10^6	8.90×10^3	9.74×10^6	1.89×10^5	8.81×10^5	1.11×10^4	9.65×10^6	1.36×10^5

Initial flux

At FD w oscillation

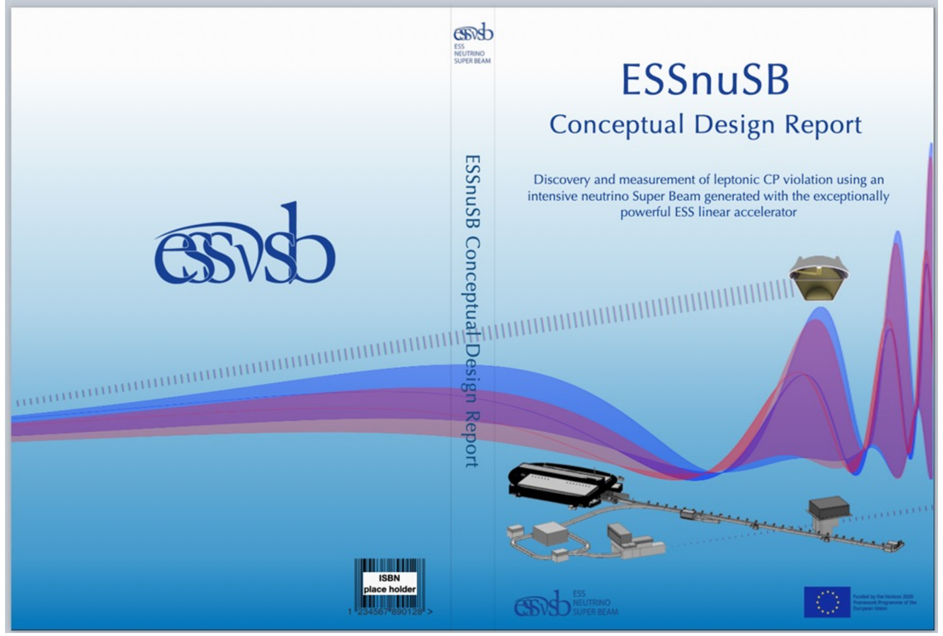


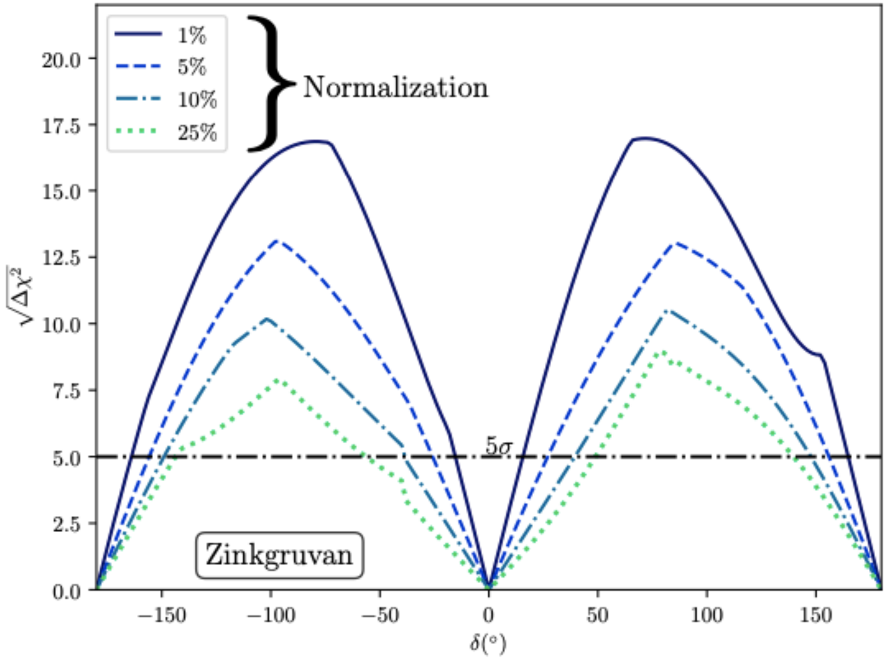
- Almost pure ν_μ beam
- Small ν_e contamination -> ν_e cross-sections at the ND

THE PHYSICS AT ESSNUSB

CP VIOLATION

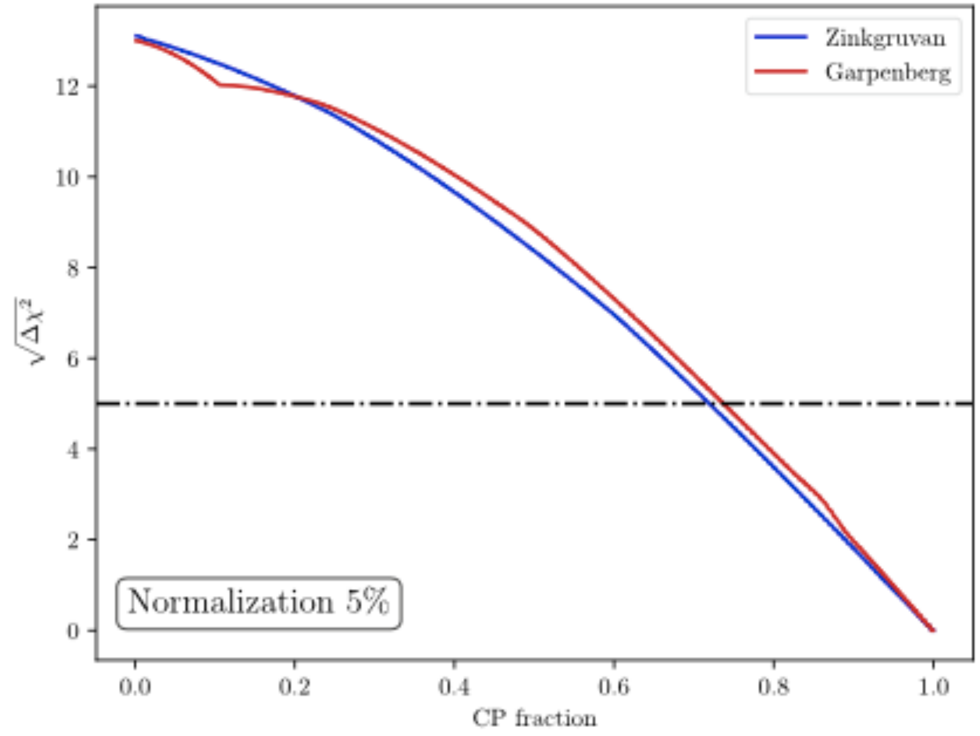
Conceptual Design Report Eur. Phys. J. ST. 231 (21), (2022) 3779





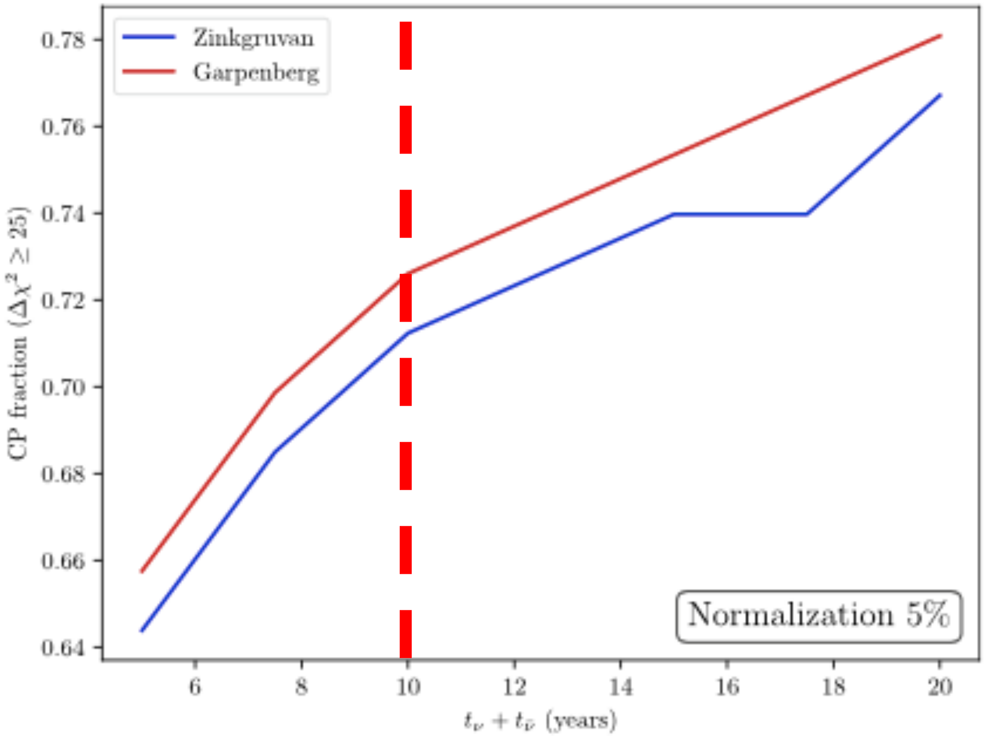
With 5% systematic uncertainty, up to 12.5 σ for maximum CPV!

CP VIOLATION



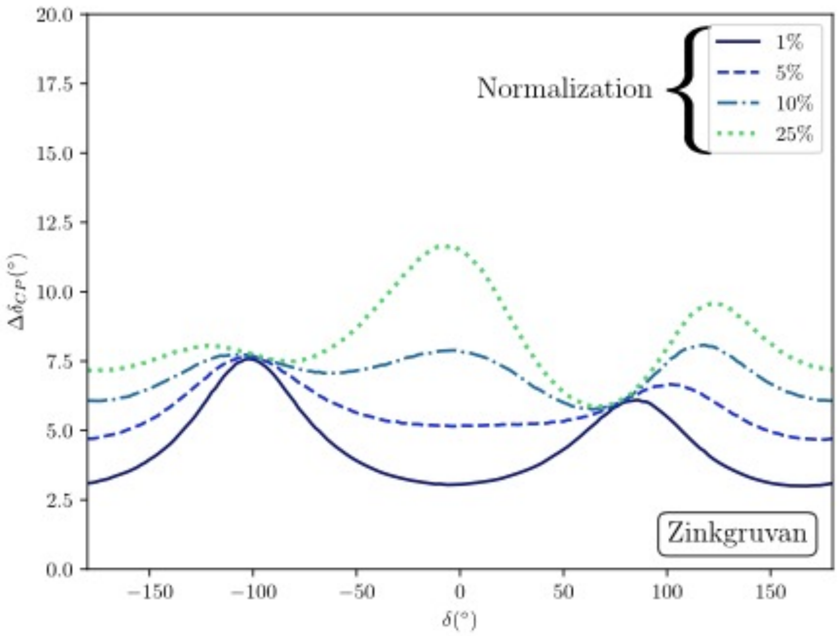
70% CP coverage at 5 σ

Nominal 5+5 yrs

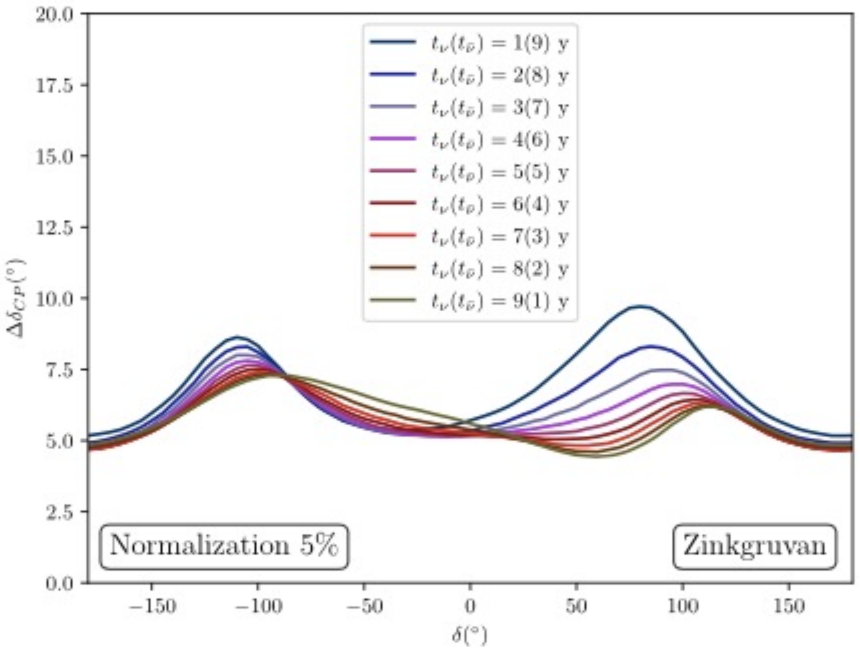


Results gets better with more running time

CP VIOLATION

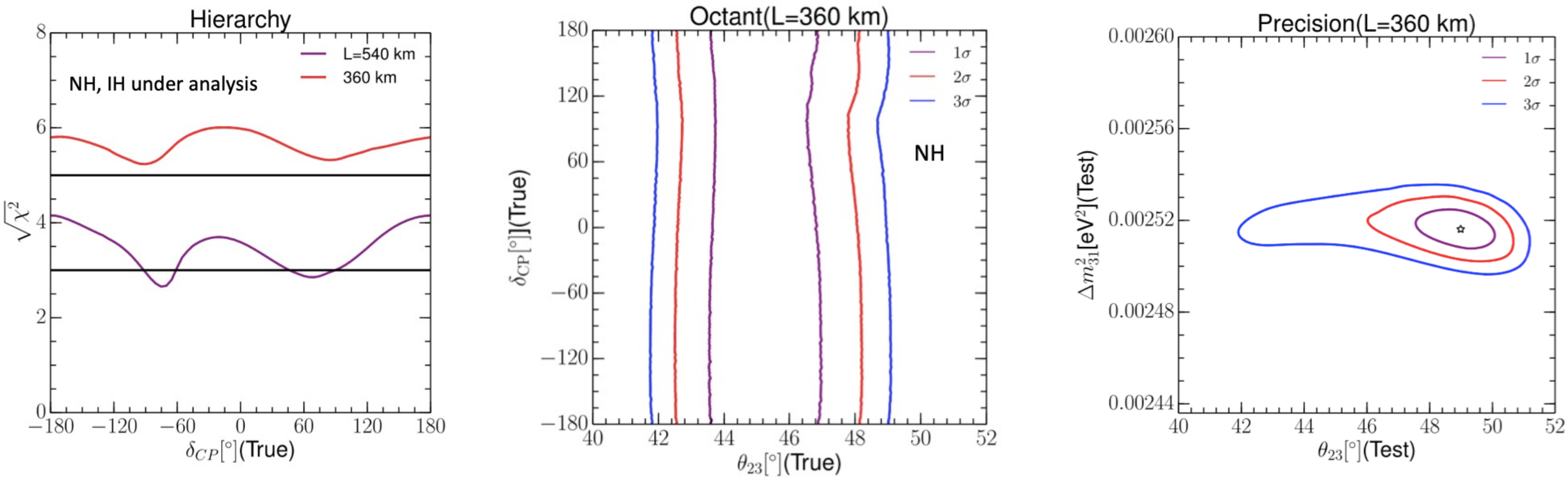


CP precision always under 7.5° for 5% sys



Precision optimized in a balanced run (5+5 yrs)

OSCILLATION BEYOND CPV

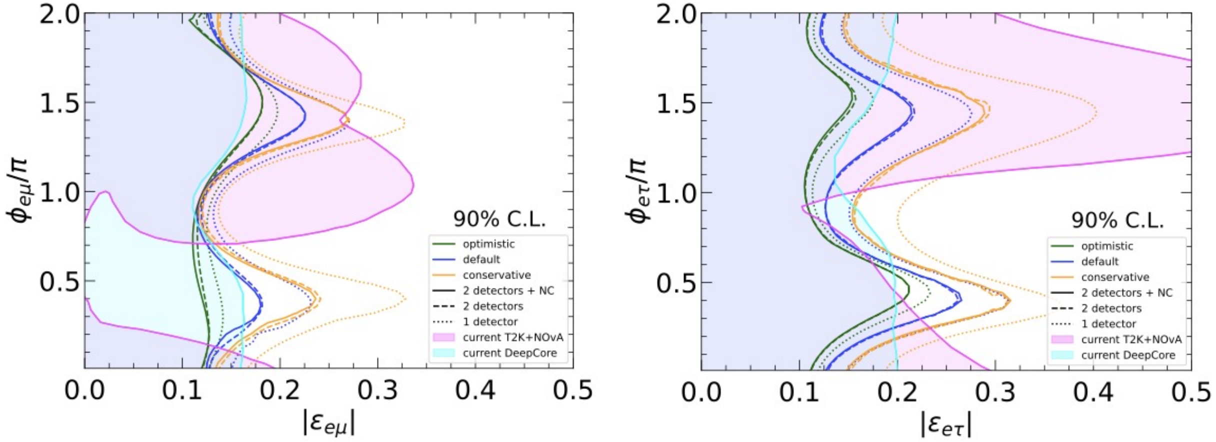


From: DOI:10.1140/epjc/s10052-021-09845-8, arXiv:2107.07585

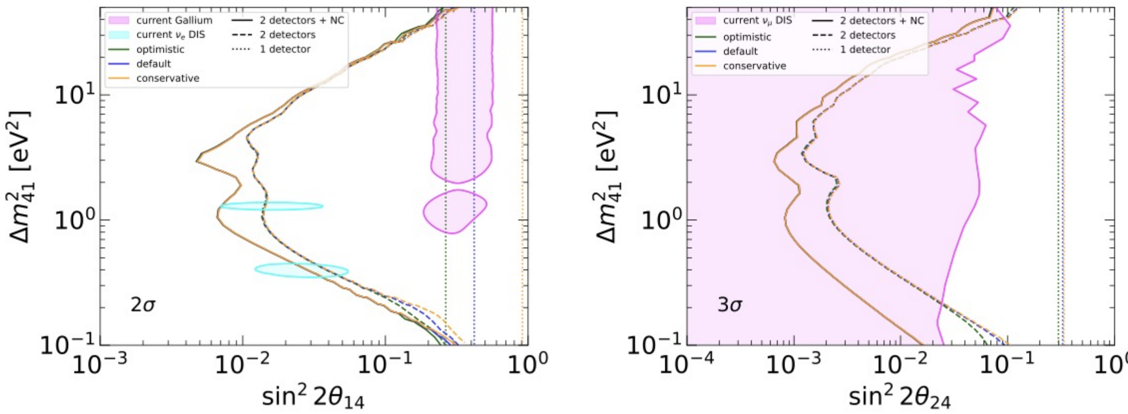
WHAT ABOUT BSM?

https://doi.org/10.1007/JHEP04(2023)130

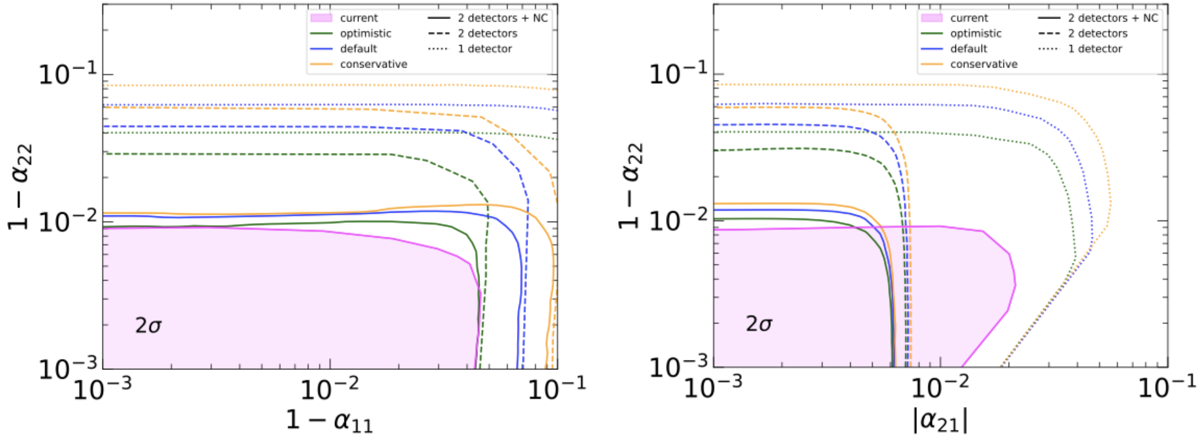
Non-Standard Interactions



Steriles



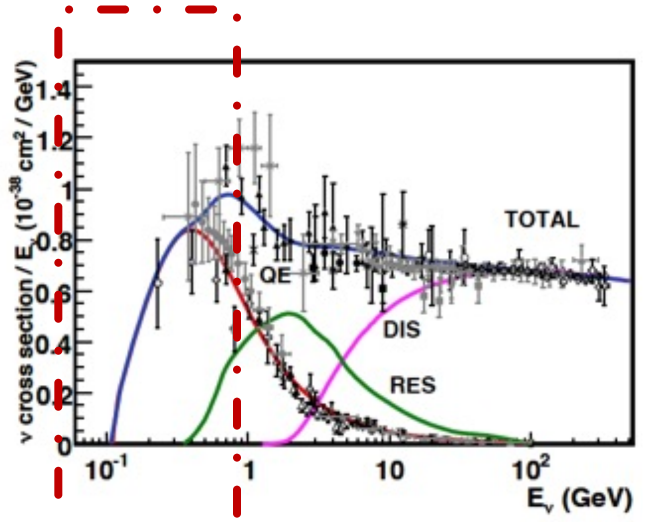
Non-Unitarity of PMNS matrix



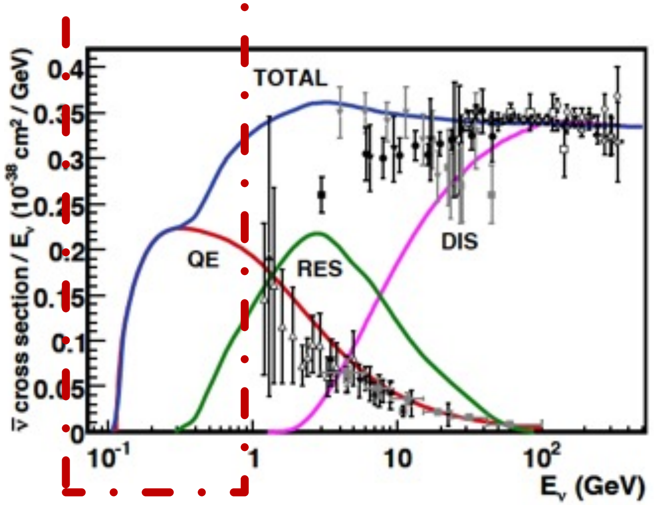
See also:
- https://doi.org/10.1007/JHEP03(2020)026
- https://doi.org/10.1007/JHEP05(2021)133
- https://doi.org/10.48550/arXiv.2305.16234
- https://doi.org/10.1103/PhysRevD.106.075016
- https://doi.org/10.1103/PhysRevD.107.075023
- ....

THE FUTURE: ESSNUSB+

THE LOW ENERGY NEUTRINO CROSS SECTION



Lack of neutrino cross section measurements in the low energy region fundamental for ESSnuSB!



Even though the effect of systematics for the CP violation measurement is much less in ESSnuSB is crucial to obtain new precise results in this direction

From eV to EeV: Neutrino cross sections across energy scales, *Rev. Mod. Phys. 84, 1307* – *Published 24 September 2012*

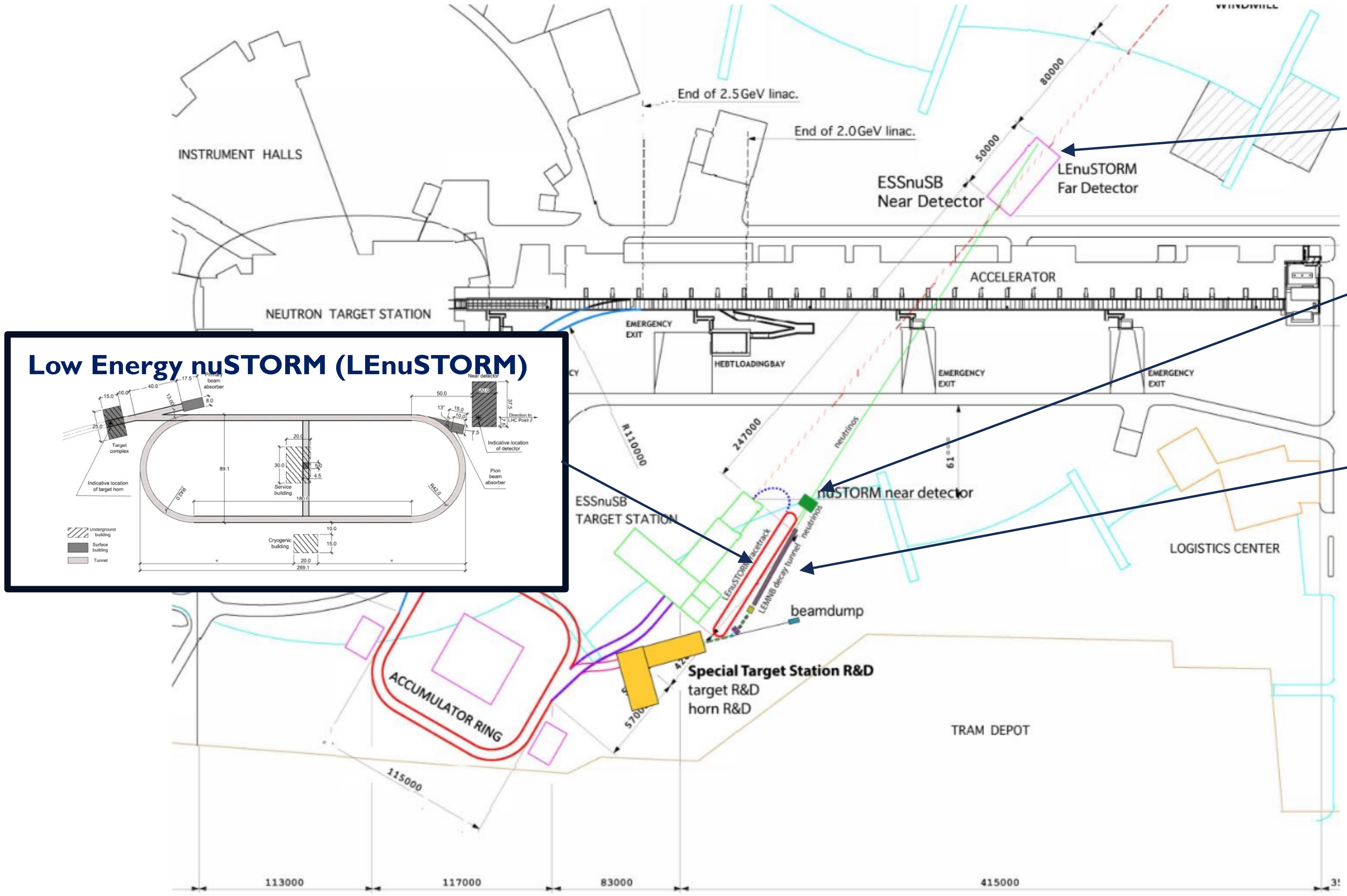
POSSIBLE STUDIES FOR THE CROSS SECTION MEASUREMENTS

1. Design a **transfer line** from the ESSνSB accumulator ring to the target
2. Design a **special target facility** that depends on one horn-target system
3. Design a pion **extraction and deflection system**
4. Design an **injection scheme** for the extracted pions to the racetrack storage ring, where the pions will decay to muons
5. Design a **storage ring** for the low energy nuSTROM (for cross section measurements and sterile neutrino searches)
6. Design a **Monitored Neutrino Beam** (low energy ENUBET for cross section measurements)
7. **Optimize the performance** of the ESSνSB detectors

Cross-section measurements with:

- Low Energy nuSTORM: $\pi \longrightarrow \mu \longrightarrow e + \nu_\mu + \nu_e$
- Low Energy ENUBET: $\pi \longrightarrow \mu + \nu_\mu$

ESSNUSB+



Gd doping for WC detectors

New Near Detector

Monitored Beam (LEMNB)

ESSNUSB+

Research and Innovation actions

Design Study

HORIZON-INFRA-2022-DEV-01

Title of Proposal:

Study of the use of the ESS facility to accurately measure the neutrino cross-sections for ESSνSB leptonic CP violation measurements and to perform sterile neutrino searches and astroparticle physics.

Acronym of Proposal: ESSνSB+

Marcos DRACOS
CENTRE NATIONAL DE LA RECHERCHE SCIENTIFIQUE CNRS
RUE MICHEL ANGE 3
75794 PARIS
FRANCE

Subject: Horizon Europe (HORIZON)
Call: HORIZON-INFRA-2022-DEV-01
Project: 101094628 — ESSnuSBplus
GAP invitation letter

Dear Applicant,

I am writing in connection with your proposal for the above-mentioned call.

Having completed the evaluation, we are pleased to inform you that your proposal has passed this phase and that we would now like to start grant preparation.

Please find enclosed the evaluation summary report (ESR) for your proposal.

Invitation to grant preparation

Approved! 26/07/2022

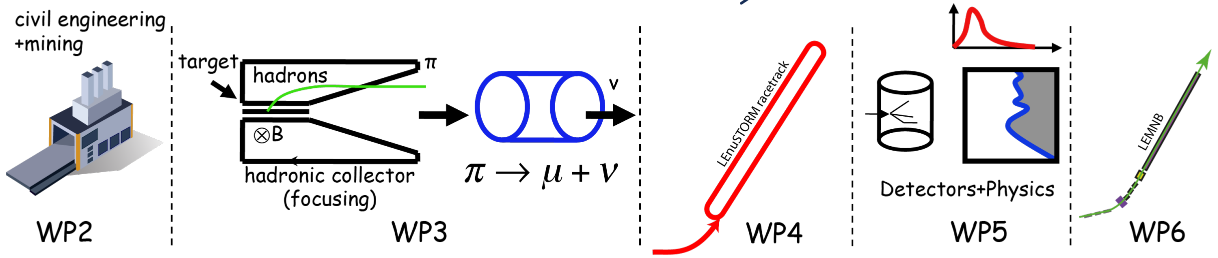
3 M €, 4 YEARS

ESSNUSB+

20 participant institutes

Participant no.	Participant organisation name	Part. short name	Country
1 (Coordinator)	Centre National de la Recherche Scientifique	CNRS	France
2	Université de Strasbourg	UNISTRA[1]	France
3	Rudjer Boskovic Institute	RBI	Croatia
4	Tokai National Higher Education and Research System, National University Corporation	NU[2]	Japan
5	Uppsala Universitet	UU	Sweden
6	Lunds Universitet	ULUND	Sweden
7	European Spallation Source ERIC	ESS	Sweden
8	Kungliga Tekniska Hoegskolan	KTH	Sweden
9	Universitaet Hamburg	UHH	Germany
10	University of Cukurova	CU	Turkey
11	National Center for Scientific Research "Demokritos"	NCSRD	Greece
12	Aristotelio Panepistimio Thessalonikis	AUTH[1]	Greece
13	Sofia University St. Kliment Ohridski	UniSofia	Bulgaria
14	Lulea Tekniska Universitet	LTU	Sweden
15	European Organisation for Nuclear Research	CERN	IEIO[3]
16	Universita degli Studi Roma Tre	UNIROMA3	Italy
17	Universita degli Istudi di Milano-Bicocca	UNIMIB	Italy
18	Istituto Nazionale di Fisica Nucleare	INFN	Italy
19	Universita degli Istudi di Padova	UNIPD[1]	Italy
20	Consorcio para la construccion, equipamiento y explotacion de la sede espanola de la fuente Europea de neutrones por espalacion	ESSB	Spain

Cross-sections and steriles



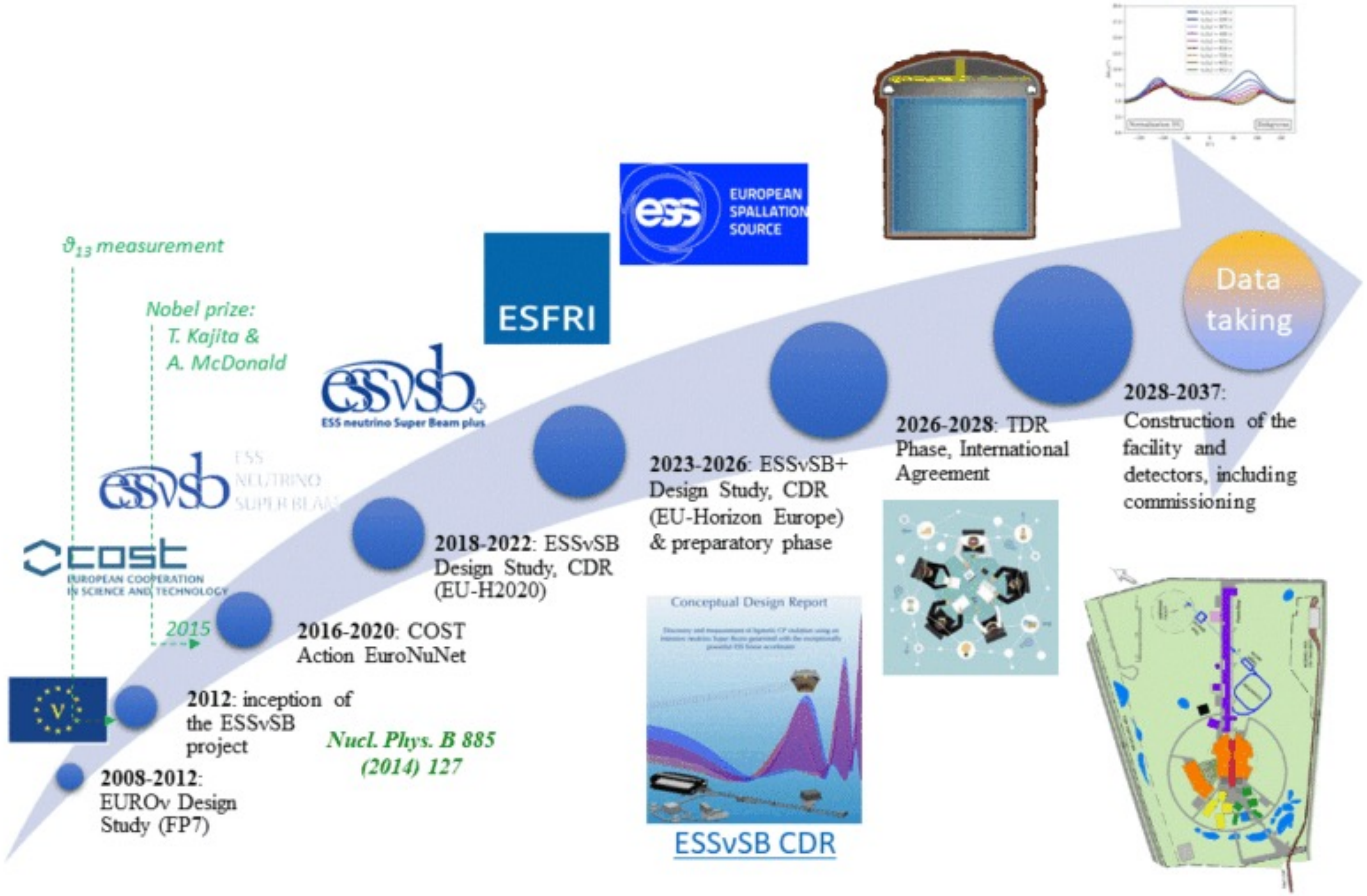
Non Beam physics:

-Atmospheric

-Supernovae

-…

TIMELINE



ϑ_{13} measurement
Nobel prize:
T. Kajita &
A. McDonald
2015
ESFRI
EUROPEAN SPALLATION SOURCE
ESS neutrino Super Beam plus
Data taking
2008-2012: EUROν Design Study (FP7)
2012: inception of the ESSνSB project
Nucl. Phys. B 885 (2014) 127
2016-2020: COST Action EuroNuNet
2018-2022: ESSνSB Design Study, CDR (EU-H2020)
2023-2026: ESSνSB+ Design Study, CDR (EU-Horizon Europe) & preparatory phase
2026-2028: TDR Phase, International Agreement
2028-2037: Construction of the facility and detectors, including commissioning
Conceptual Design Report
ESSνSB CDR

CONCLUSIONS

- ESSnuSB is a next-to-next generation neutrino oscillation experiment which aims to precisely measure CP violation looking at neutrino oscillations at the 2nd oscillation maximum

- This baseline choice allows to have a measurement less affected by systematic errors and matter effects

- We predict that in 10 years of data taking ESSnuSB will be able to reach a 70% coverage for the CP violating phase and a precision of less than 8°

- The accelerator complex will be based at the ESS linac, the most powerful proton accelerator in the world

- The large far detectors can also be used for rich astroparticle physics programme

- The ESSnuSB Design Study has been supported by EU-Horizon 2020 during the period 2018-2022 and the ESSnuSB+ Project which started this year has further enriched the great physics program of the experiment

THANK YOU FOR YOUR ATTENTION

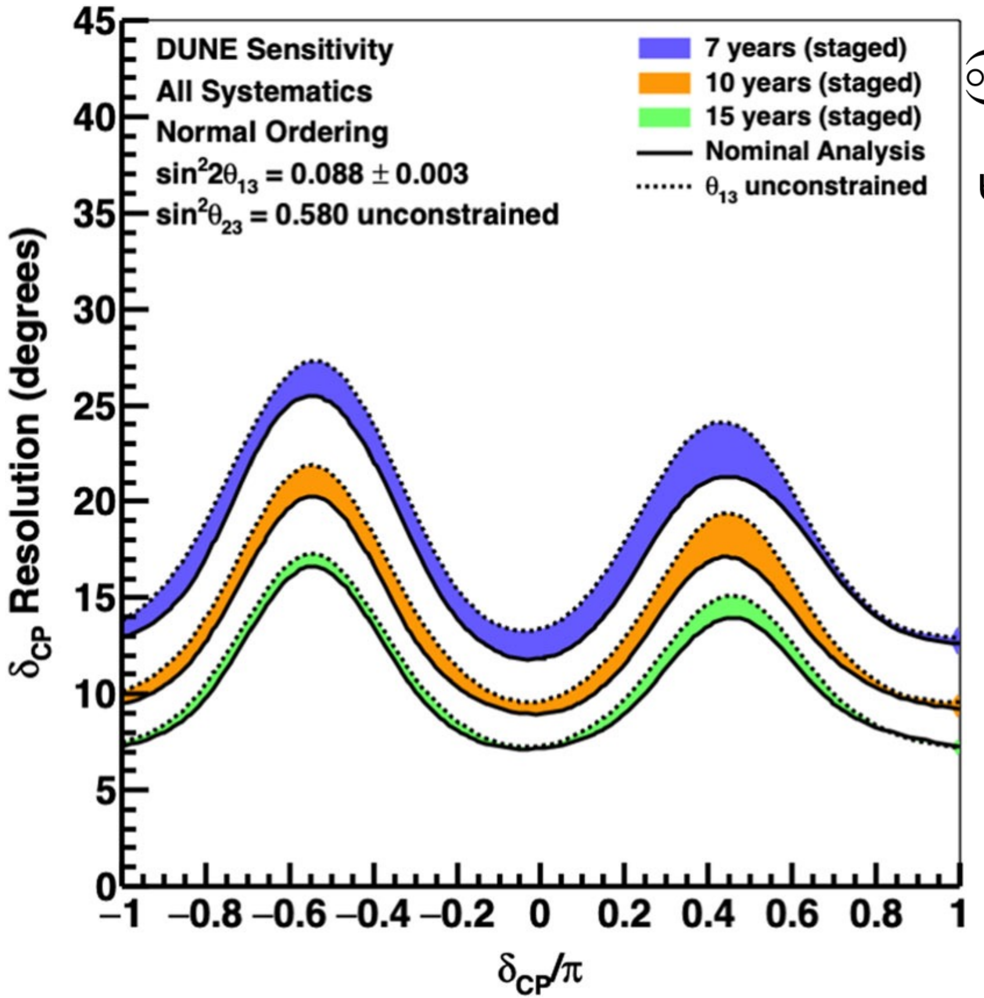
BACKUP

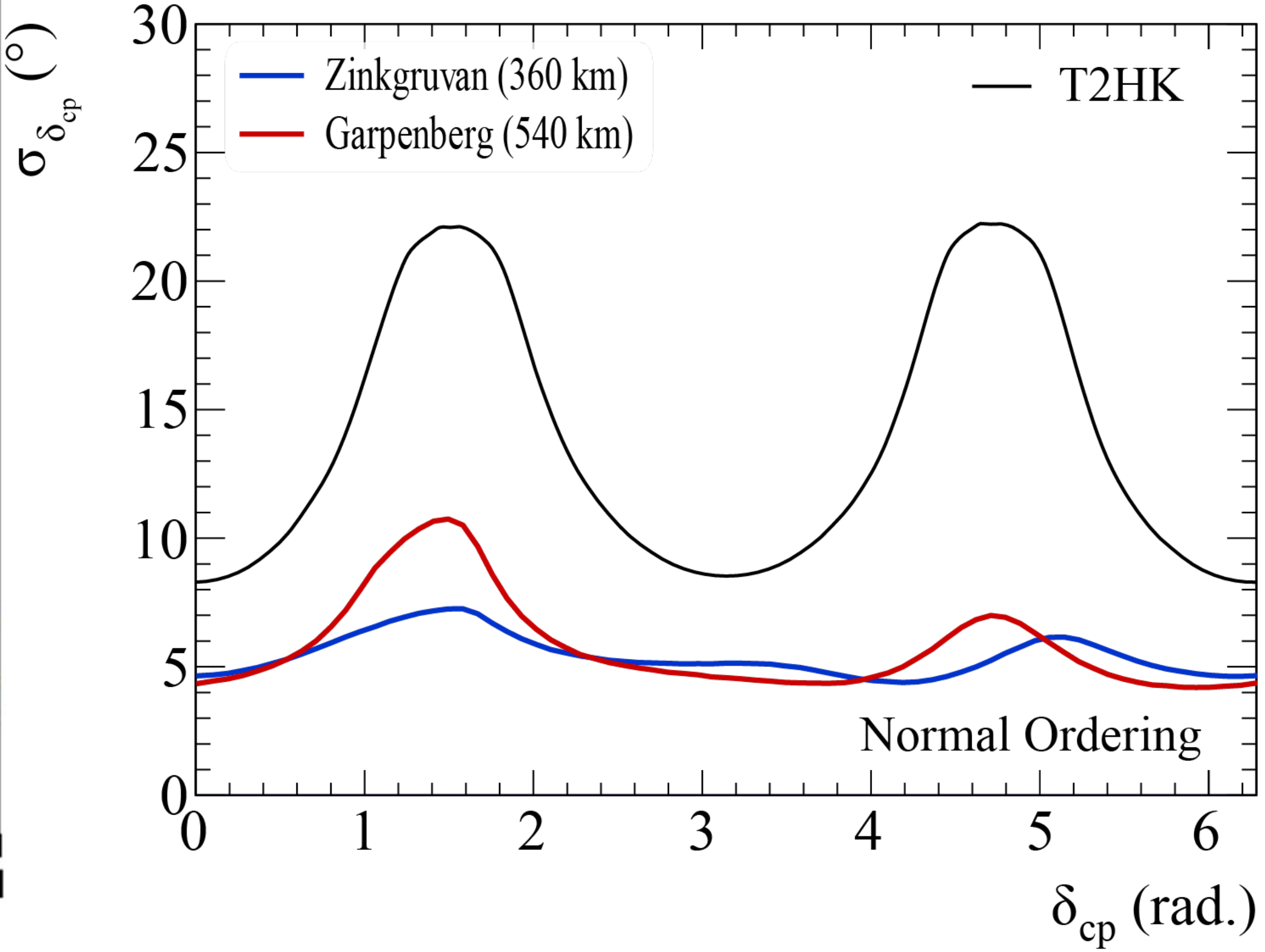
SYSTEMATICS

Systematics	SB Opt.	SB Def.	SB Cons.	BB Opt.	BB Def.	BB Cons.	NF Opt.	NF Def.	NF Cons.
Fiducial volume ND	0.2%	0.5%	1%	0.2%	0.5%	1%	0.2%	0.5%	1%
Fiducial volume FD (incl. near-far extrap.)	1%	2.5%	5%	1%	2.5%	5%	1%	2.5%	5%
Flux error signal ν	5%	7.5%	10%	1%	2%	2.5%	0.1%	0.5%	1%
Flux error background ν	10%	15%	20%	correlated			correlated		
Flux error signal $\bar{\nu}$	10%	15%	20%	1%	2%	2.5%	0.1%	0.5%	1%
Flux error background $\bar{\nu}$	20%	30%	40%	correlated			correlated		
Background uncertainty	5%	7.5%	10%	5%	7.5%	10%	10%	15%	20%
Cross secs × eff. QE†	10%	15%	20%	10%	15%	20%	10%	15%	20%
Cross secs × eff. RES†	10%	15%	20%	10%	15%	20%	10%	15%	20%
Cross secs × eff. DIS†	5%	7.5%	10%	5%	7.5%	10%	5%	7.5%	10%
Effec. ratio ν_e/ν_μ QE*	3.5%	11%	–	3.5%	11%	–	–	–	–
Effec. ratio ν_e/ν_μ RES*	2.7%	5.4%	–	2.7%	5.4%	–	–	–	–
Effec. ratio ν_e/ν_μ DIS*	2.5%	5.1%	–	2.5%	5.1%	–	–	–	–
Matter density	1%	2%	5%	1%	2%	5%	1%	2%	5%

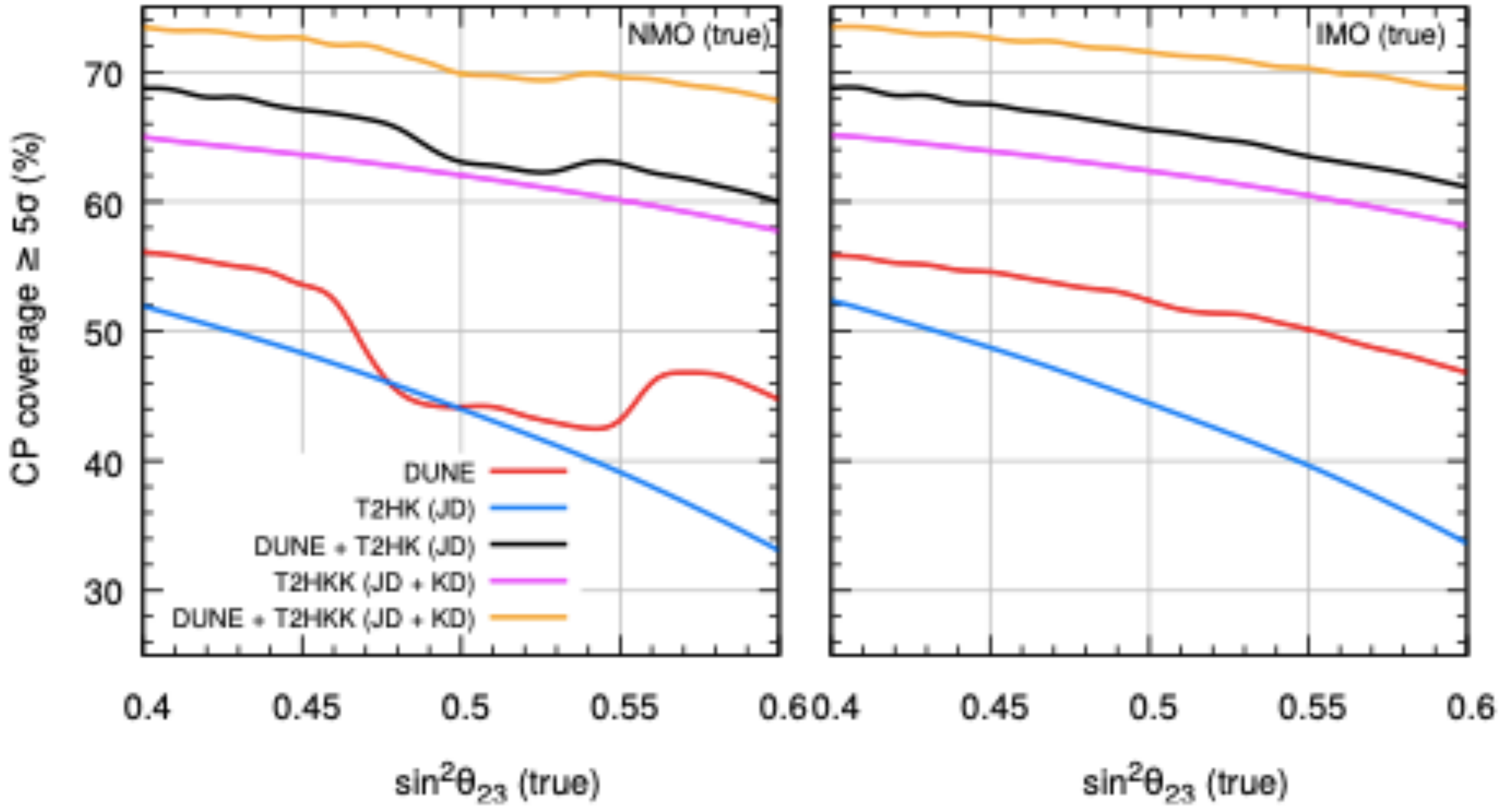
Phys. Rev. D 87 (2013) 3, 033004 [arXiv:1209.5973 [hep-ph]]

COMPARISON WITH LBL





COMPARISON WITH LBL



arXiv:2211.10620

EVENTS

Table 5.13: Expected number of neutrino interactions in 538 kt FD fiducial volume at a distance of 360 km (Zinkgruvan mine) in 200 days (one effective year). Shown for positive (negative) horn polarity.

	Channel	Non oscillated	Oscillated $\delta_{CP} = 0$	Oscillated $\delta_{CP} = \pi/2$	Oscillated $\delta_{CP} = -\pi/2$
CC	$\nu_\mu \to \nu_\mu$	22 630.4 (231.0)	10 508.7 (101.6)	10 430.6 (5.8)	10 430.6 (100.9)
	$\nu_\mu \to \nu_e$	0 (0)	768.3 (8.6)	543.8 (5.8)	1 159.9 (12.8)
	$\nu_e \to \nu_e$	190.2 (1.2)	177.9 (1.1)	177.9 (1.1)	177.9 (1.1)
	$\nu_e \to \nu_\mu$	0 (0)	5.3 (3.3×10^{-2})	7.3 (4.5×10^{-2})	3.9 (2.4×10^{-2})
	$\bar{\nu}_\mu \to \bar{\nu}_\mu$	62.4 (3 640.3)	26.0 (1 896.8)	26.0 (1 898.9)	26.0 (1 898.9)
	$\bar{\nu}_\mu \to \bar{\nu}_e$	0 (0)	2.6 (116.1)	3.5 (164.0)	1.4 (56.8)
	$\bar{\nu}_e \to \bar{\nu}_e$	1.3×10^{-1} (18.5)	1.3×10^{-1} (17.5)	1.3×10^{-1} (17.5)	1.2×10^{-1} (17.5)
	$\bar{\nu}_e \to \bar{\nu}_\mu$	0 (0)	3.0×10^{-3} (4.0×10^{-1})	1.5×10^{-3} (2.1×10^{-1})	4.1×10^{-3} (5.6×10^{-1})
NC	ν_μ	16 015.1 (179.3)			
	ν_e	103.7 (0.7)			
	$\bar{\nu}_\mu$	55.2 (3 265.5)			
	$\bar{\nu}_e$	1×10^{-1} (13.6)			

EVENTS

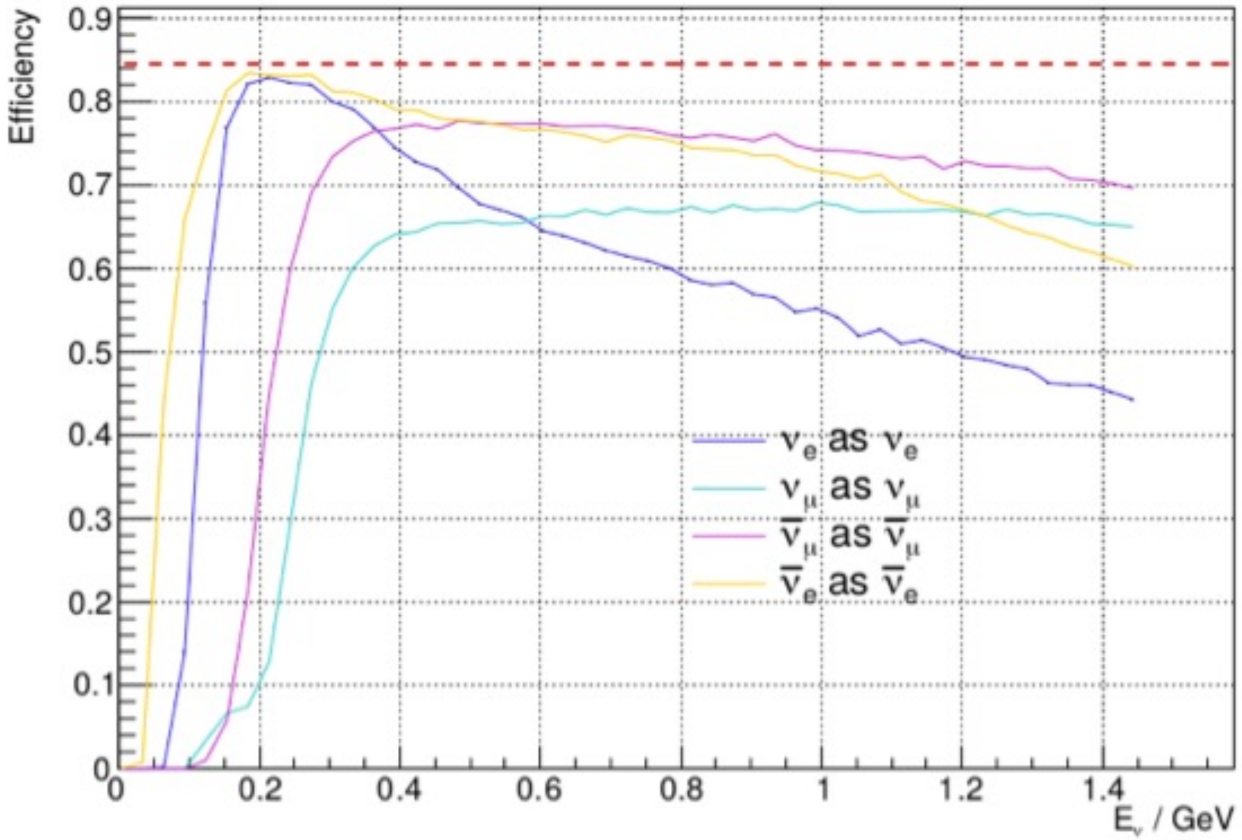
	Channel	$L = 540$ km	$L = 360$ km
Signal	$\nu_\mu \to \nu_e$ ($\bar{\nu}_\mu \to \bar{\nu}_e$)	272.22 (63.75)	578.62 (101.18)
Background	$\nu_\mu \to \nu_\mu$ ($\bar{\nu}_\mu \to \bar{\nu}_\mu$)	31.01 (3.73)	67.23 (11.51)
	$\nu_e \to \nu_e$ ($\bar{\nu}_e \to \bar{\nu}_e$)	67.49 (7.31)	151.12 (16.66)
	ν_μ NC ($\bar{\nu}_\mu$ NC)	18.57 (2.10)	41.78 (4.73)
	$\bar{\nu}_\mu \to \bar{\nu}_e$ ($\nu_\mu \to \nu_e$)	1.08 (3.08)	1.94 (6.47)

Table 1: Signal and major background events for the appearance channel corresponding to positive (negative) polarity per year for $\delta_{CP} = 0°$.

	Channel	$L = 540$ km	$L = 360$ km
Signal	$\nu_\mu \to \nu_\mu$ ($\bar{\nu}_\mu \to \bar{\nu}_\mu$)	4419.69 (733.31)	7619.16 (1602.02)
Background	$\nu_e \to \nu_e$ ($\bar{\nu}_e \to \bar{\nu}_e$)	7.77 (0.02)	17.08 (0.05)
	ν_μ NC ($\bar{\nu}_\mu$ NC)	69.23 (8.24)	155.77 (18.54)
	$\nu_\mu \to \nu_e$ ($\bar{\nu}_\mu \to \bar{\nu}_e$)	14.68 (0.06)	61.30 (0.17)
	$\bar{\nu}_\mu \to \bar{\nu}_\mu$ ($\nu_\mu \to \nu_\mu$)	12.35 (41.00)	21.39 (72.59)

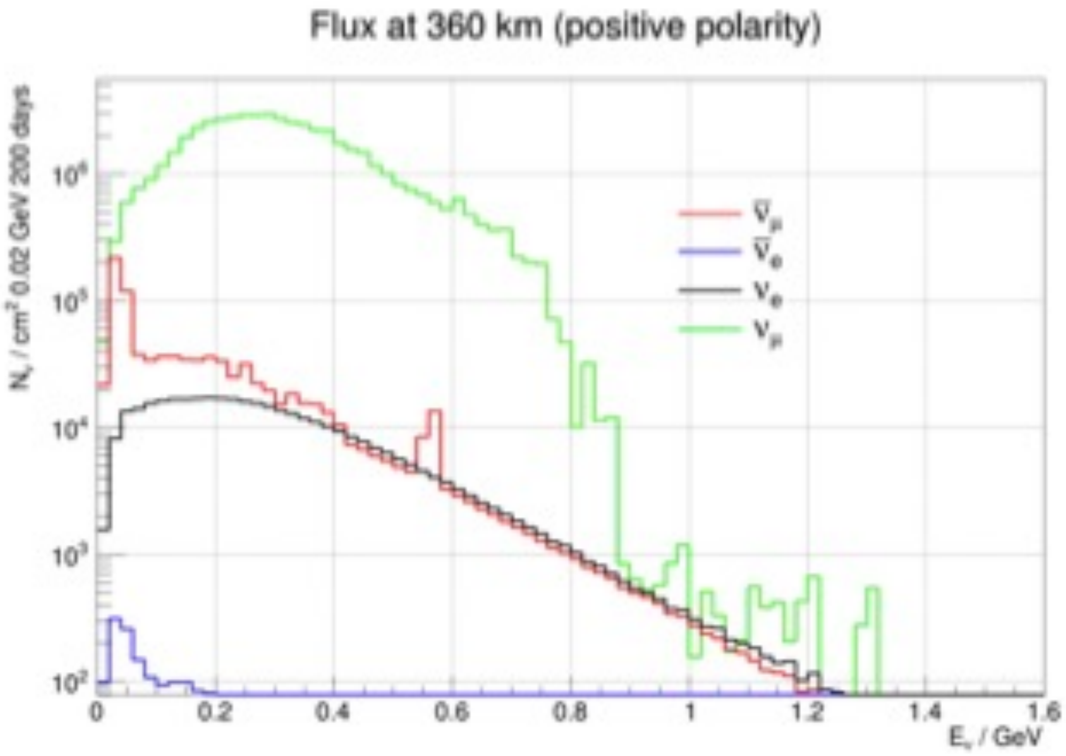
Table 2: Signal and major background events for the disappearance channel corresponding to positive (negative) polarity per year for $\delta_{CP} = 0°$.

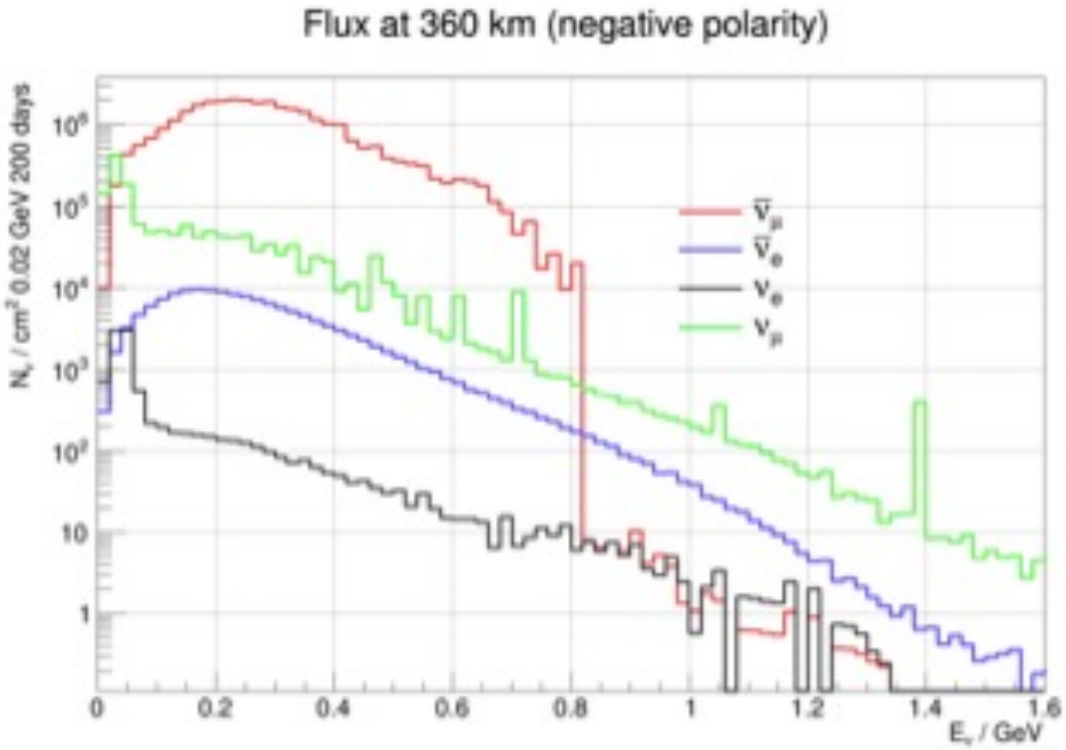
EFFICIENCY



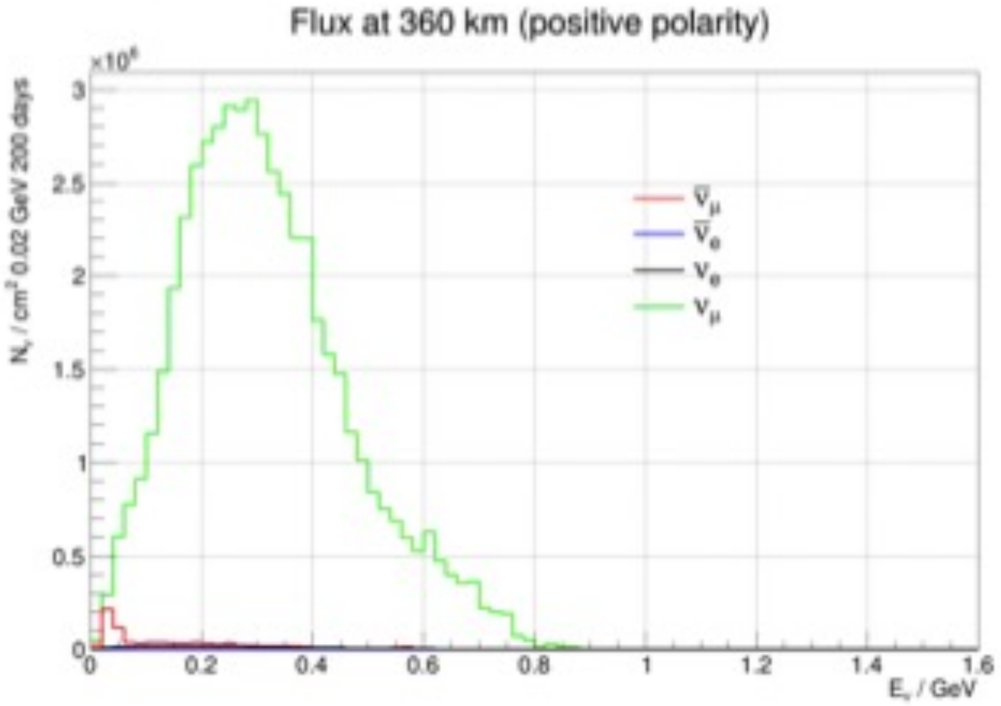
Efficiency
0.9
0.8
0.7
0.6
0.5
0.4
0.3
0.2
0.1
0
0
0.2
0.4
0.6
0.8
1
1.2
1.4
E_ν / GeV
ν_e as ν_e
ν_μ as ν_μ
$\bar{\nu}_\mu$ as $\bar{\nu}_\mu$
$\bar{\nu}_e$ as $\bar{\nu}_e$

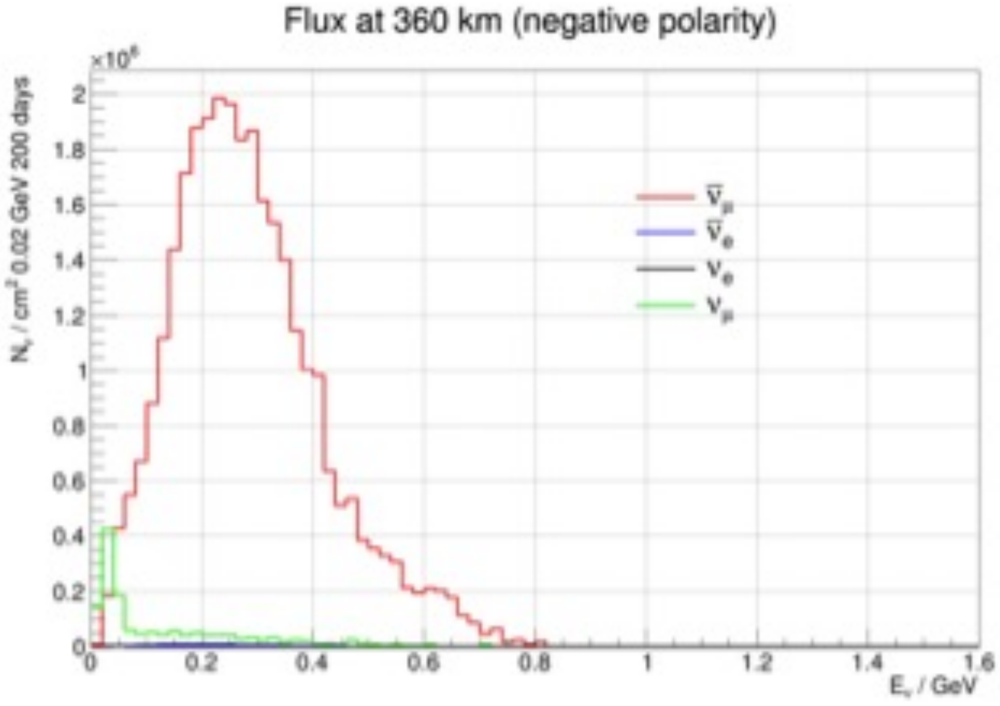
FLUXES


Flux at 360 km (positive polarity)
N_ν / cm^2 0.02 GeV 200 days
$\bar{\nu}_\mu$
$\bar{\nu}_e$
ν_e
ν_μ
E_ν / GeV


Flux at 360 km (negative polarity)
N_ν / cm^2 0.02 GeV 200 days
$\bar{\nu}_\mu$
$\bar{\nu}_e$
ν_e
ν_μ
E_ν / GeV

FLUXES


Flux at 360 km (positive polarity)
×10⁶
N_ν / cm² 0.02 GeV 200 days
E_ν / GeV
0
0.5
1
1.5
2
2.5
3
0.2
0.4
0.6
0.8
1.2
1.4
1.6
ν̄_μ
ν̄_e
ν_e
ν_μ


Flux at 360 km (negative polarity)
×10⁶
N_ν / cm² 0.02 GeV 200 days
E_ν / GeV
0
0.2
0.4
0.6
0.8
1
1.2
1.4
1.6
1.8
2
ν̄_μ
ν̄_e
ν_e
ν_μ

FLUXES

Flavour	ν Mode		$\bar{\nu}$ Mode	
	N_ν (10^5/ cm^2)	%	N_ν (10^5/ cm^2)	%
ν_μ	**520.06**	**97.6**	15.43	4.7
ν_e	**3.67**	**0.67**	0.10	0.03
$\bar{\nu}_\mu$	9.10	1.7	**305.55**	**94.8**
$\bar{\nu}_e$	0.023	0.03	**1.43**	**0.43**

Events at 360 km w/o oscillations

BSM: NSI

$$i\frac{d}{dt}\begin{pmatrix}\nu_e\\ \nu_\mu\\ \nu_\tau\end{pmatrix} = \left[\frac{1}{2E_\nu}U\begin{pmatrix}0 & 0 & 0\\ 0 & \Delta m^2_{21} & 0\\ 0 & 0 & \Delta m^2_{31}\end{pmatrix}U^\dagger + A_{CC}\begin{pmatrix}1 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 0\end{pmatrix}\right]\begin{pmatrix}\nu_e\\ \nu_\mu\\ \nu_\tau\end{pmatrix}$$

$$\tilde{V}_{\rm MSW} = a_{\rm CC}\begin{pmatrix}1+\varepsilon^m_{ee} & \varepsilon^m_{e\mu} & \varepsilon^m_{e\tau}\\ \varepsilon^{m*}_{e\mu} & \varepsilon^m_{\mu\mu} & \varepsilon^m_{\mu\tau}\\ \varepsilon^{m*}_{e\tau} & \varepsilon^{m*}_{\mu\tau} & \varepsilon^m_{\tau\tau}\end{pmatrix}$$

BSM: STERILE

$$U = R(\theta_{34})R(\theta_{24})R(\theta_{23},\delta_3)R(\theta_{14})R(\theta_{13},\delta_2)R(\theta_{12},\delta_1)$$

New sources of CP violation!

$$i\frac{d}{dt}\begin{pmatrix}\nu_e\\ \nu_\mu\\ \nu_\tau\\ \nu_s\end{pmatrix} = \left[\frac{1}{2E_\nu}U\begin{pmatrix}0&0&0&0\\0&\Delta m^2_{21}&0&0\\0&0&\Delta m^2_{31}&0\\0&0&0&\Delta m^2_{41}\end{pmatrix}U^\dagger + \begin{pmatrix}A_{CC}+A_{NC}&0&0&0\\0&A_{NC}&0&0\\0&0&A_{NC}&0\\0&0&0&0\end{pmatrix}\right]\begin{pmatrix}\nu_e\\ \nu_\mu\\ \nu_\tau\\ \nu_s\end{pmatrix}$$

BSM: NU

$$N = (1 + \alpha)U_{PMNS} \cdot$$

$$\alpha = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}|e^{i\phi_{21}} & \alpha_{22} & 0 \\ |\alpha_{31}|e^{i\phi_{31}} & |\alpha_{32}|e^{i\phi_{32}} & \alpha_{33} \end{pmatrix}$$

NEUTRINO INTERACTIONS