

# QUANTUM CORRECTIONS TO A NEW WILSON LINE-BASED ACTION FOR GLUODYNAMICS

PIOTR KOTKO

AGH UST, Krakow

in collaboration with:

H. KAKKAD, A. STASTO,

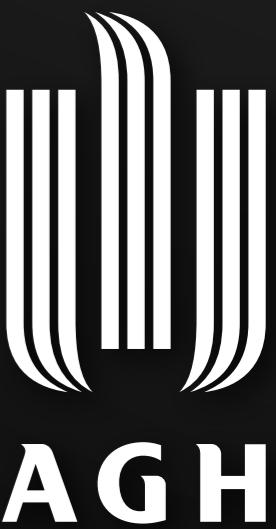
based on:

JHEP 07 (2021) 187, JHEP 11 (2022) 132,

and work in preparation

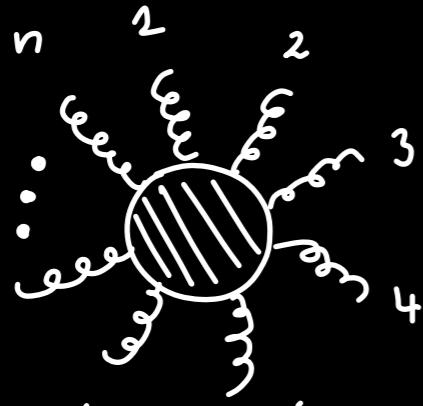
supported by:

NATIONAL SCIENCE CENTRE POLAND,  
GRANT NO. DEC-2020/39/O/ST2/03011



# INTRODUCTION

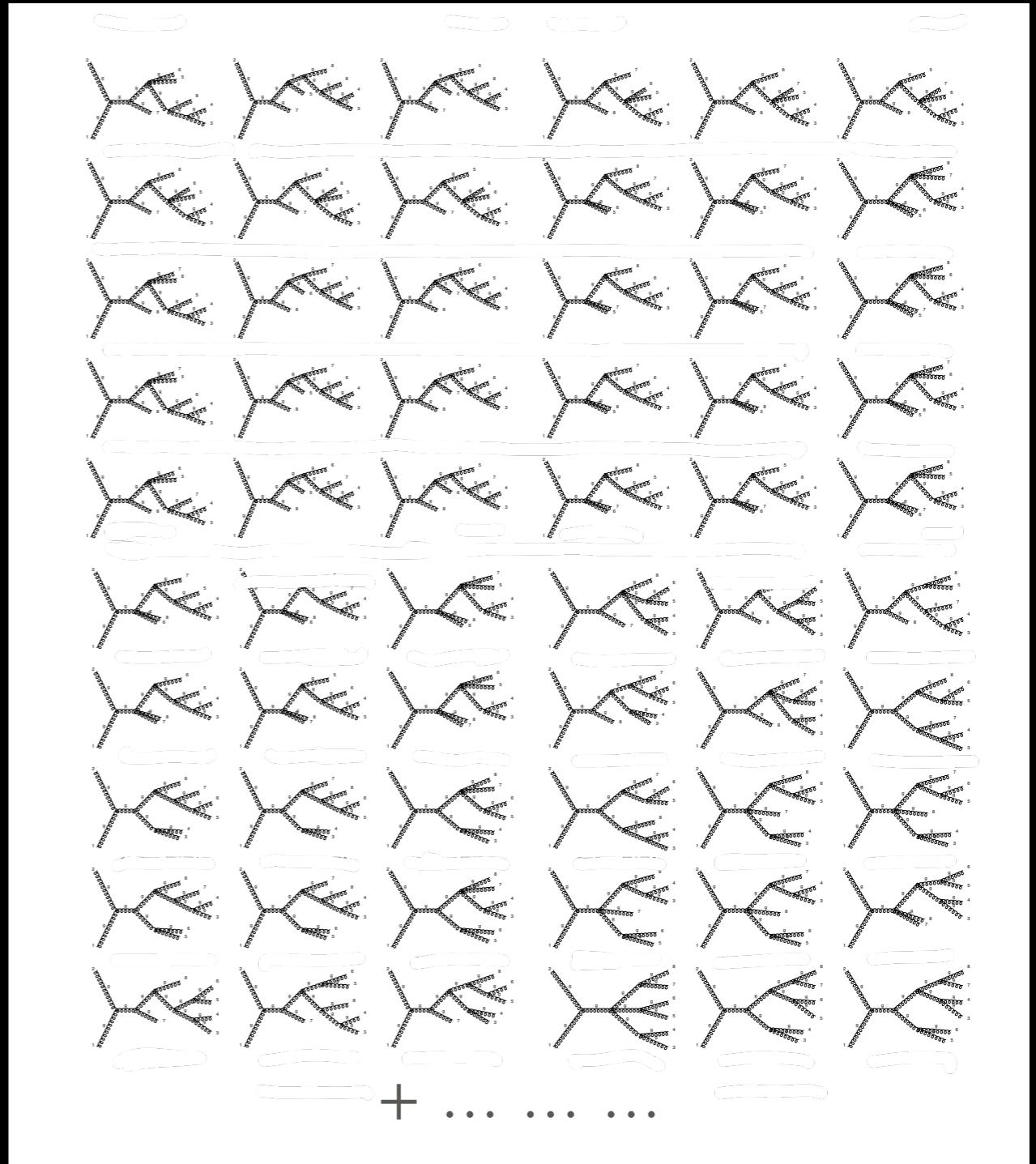
## $n$ -gluon scattering amplitudes



# legs	4	5	6	7	8
# diagrams	4	25	220	2485	34300

Many diagrams, but when expressed using the helicity spinors results are suspiciously simple...

## Example: tree 8-point amplitude



### Color decomposition

$$\mathcal{M}^{a_1, \dots, a_n} = \sum_{\text{non-cyclic permutations}} \text{Tr}(t^{a_1} \dots t^{a_n}) \mathcal{A}(1, \dots, n)$$

$$\text{Tr}(t^a t^b) = \delta_{ab}$$

$$[t^a, t^b] = i\sqrt{2}f^{abc}t^c$$

↗  
 color  
 ordered  
 amplitudes →

# legs	4	5	6	7	8
# diagrams	4	25	220	2485	34300
# planar diagrams	3	10	38	154	654

### Spinor helicity method

SL(2,C) representation for Lorentz group.

$$k_{\alpha\dot{\alpha}} = (k_\mu \sigma^\mu)_{\alpha\dot{\alpha}} = \lambda_\alpha \tilde{\lambda}_{\dot{\alpha}} \quad \rightarrow \quad \begin{pmatrix} -k^0 + k^3 & k^1 - ik^2 \\ k^1 + ik^2 & -k^0 - k^3 \end{pmatrix}$$

for  $k^2 = 0$ .

$$\nu_+ = \begin{pmatrix} \lambda_\alpha \\ 0 \\ 0 \end{pmatrix}, \quad \nu_- = \begin{pmatrix} 0 \\ 0 \\ \tilde{\lambda}_{\dot{\alpha}} \end{pmatrix}$$

where  $\nu_\pm$  are solution to Dirac equation:

$$k\nu_\pm(k) = 0$$

spinor products:

$$\langle ij \rangle = \lambda_i^\alpha \lambda_{j\alpha} \quad [ij] = \tilde{\lambda}_i^{\dot{\alpha}} \tilde{\lambda}_{j\dot{\alpha}}$$

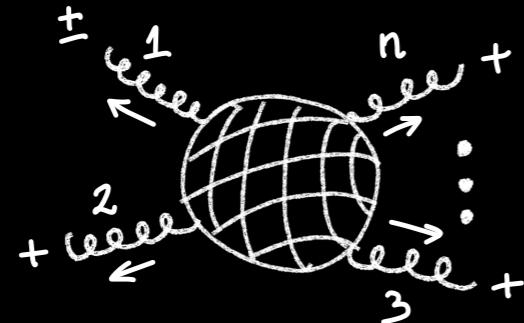
for on-shell momenta  $k_i, k_j$ .

# INTRODUCTION

## Helicity amplitudes

### Key tree-level results for any number of gluons

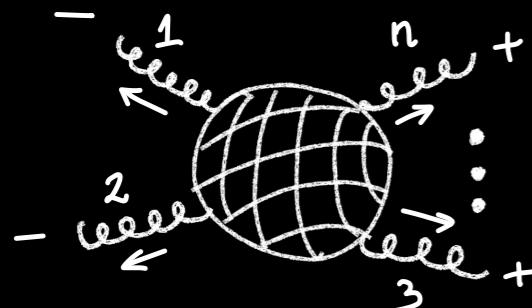
The simplest (color-ordered) helicity amplitudes:



helicity

$$\mathcal{A}(1^+, 2^+, \dots, n^+) = 0$$
$$\mathcal{A}(1^-, 2^+, \dots, n^+) = 0$$

Maximally Helicity Violating (MHV) amplitudes:



$$\mathcal{A}(1^-, 2^-, 3^+, \dots, n^+) = g^{n-2} \frac{\langle 12 \rangle^4}{\langle 12 \rangle \langle 23 \rangle \dots \langle (n-1)n \rangle \langle n1 \rangle}$$

[S.J. Parke, T.R Taylor, 1986]

Simplicity of the MHV amplitudes triggered incredible developments in theory over last 20 years...

# INTRODUCTION

## Cachazo-Svrcek-Witten (CSW) method

### MHV vertices

The Maximally Helicity Violating (MHV) amplitudes can be treated as interaction vertices.

[F. Cachazo, P. Svrcek, E. Witten, 2004]

$$= g^{n-2} \frac{\langle ij \rangle^4}{\langle 12 \rangle \langle 23 \rangle \dots \langle n1 \rangle}$$

↑  
 off-shell  
 spinor products

### spinor products (on-shell)

$$\langle ij \rangle = \epsilon_{\alpha\beta} \lambda_i^\alpha \lambda_j^\beta$$

+ helicity  
 spinor

$$[ij] = \epsilon_{\dot{\alpha}\dot{\beta}} \tilde{\lambda}_i^{\dot{\alpha}} \tilde{\lambda}_j^{\dot{\beta}}$$

- helicity  
 spinor

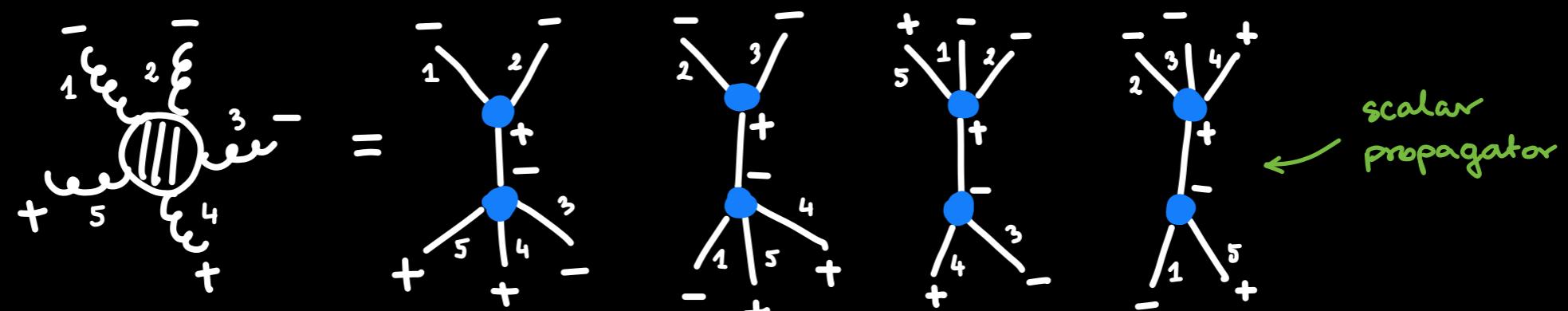
### off-shell continuations

$$\lambda_{i\alpha}^* = (k_i)_{\alpha\dot{\alpha}} \tilde{\eta}_j^{\dot{\alpha}} = (k_i^\mu \sigma_\mu)_{\alpha\dot{\alpha}} \tilde{\eta}_j^{\dot{\alpha}}$$

↑  
 $(\frac{1}{2}, 0) \times (0, \frac{1}{2})$  representation  
 of  $k^1, k^2 \neq 0$

↑  
 auxiliary  
 spinor

### example: tree-level NMHV



# INTRODUCTION

## Lagrangian for the CSW method (1)

### Yang-Mills theory on the light cone

[J. Scherk, J.H. Schwarz, 1975]

Set the light cone gauge  $A^+ = 0$  and integrate out  $A^-$ :

$$\hat{A} \equiv t^a A_a(x^+, \mathbf{x})$$

$$\mathbf{x} \equiv (x^-, x^\bullet, x^\star)$$

$$S_{\text{Y-M}}^{(\text{LC})} [A^\bullet, A^\star] = \int dx^+ \int d^3\mathbf{x} \left\{ \begin{array}{ll} + \text{---} & + \text{---} \\ \text{---} & \xi^- \\ - \text{---} & + \text{---} \\ \text{---} & \xi^+ \\ \text{---} & + \text{---} \\ \text{---} & \xi^+ \\ \text{---} & + \text{---} \\ \text{---} & \xi^- \\ \text{---} & + \text{---} \end{array} \right. \begin{array}{l} -\text{Tr} \hat{A}^\bullet \square \hat{A}^\star \\ -2ig \text{Tr} \partial_-^{-1} \partial_\bullet \hat{A}^\bullet [\partial_- \hat{A}^\star, \hat{A}^\bullet] \\ -2ig \text{Tr} \partial_-^{-1} \partial_\star \hat{A}^\star [\partial_- \hat{A}^\bullet, \hat{A}^\star] \\ -2g^2 \text{Tr} [\partial_- \hat{A}^\bullet, \hat{A}^\star] \partial_-^{-2} [\partial_- \hat{A}^\star, \hat{A}^\bullet] \end{array} \right\}$$

+   
 -   
 helicity field

### double-null coordinates

$$\begin{array}{lll} v^+ = v \cdot \eta = \frac{1}{\sqrt{2}}(v^0 + v^3) & v^\bullet = v \cdot \epsilon_\perp^+ = \frac{1}{\sqrt{2}}(v^1 + iv^2) & \eta = \frac{1}{\sqrt{2}}(1,0,0,-1) \quad \epsilon_\perp^+ = \frac{-1}{\sqrt{2}}(0,1,+i,0) \\ v^- = v \cdot \tilde{\eta} = \frac{1}{\sqrt{2}}(v^0 - v^3) & v^\star = v \cdot \epsilon_\perp^- = \frac{1}{\sqrt{2}}(v^1 - iv^2) & \tilde{\eta} = \frac{1}{\sqrt{2}}(1,0,0,1) \quad \epsilon_\perp^- = \frac{-1}{\sqrt{2}}(0,1,-i,0) \end{array}$$

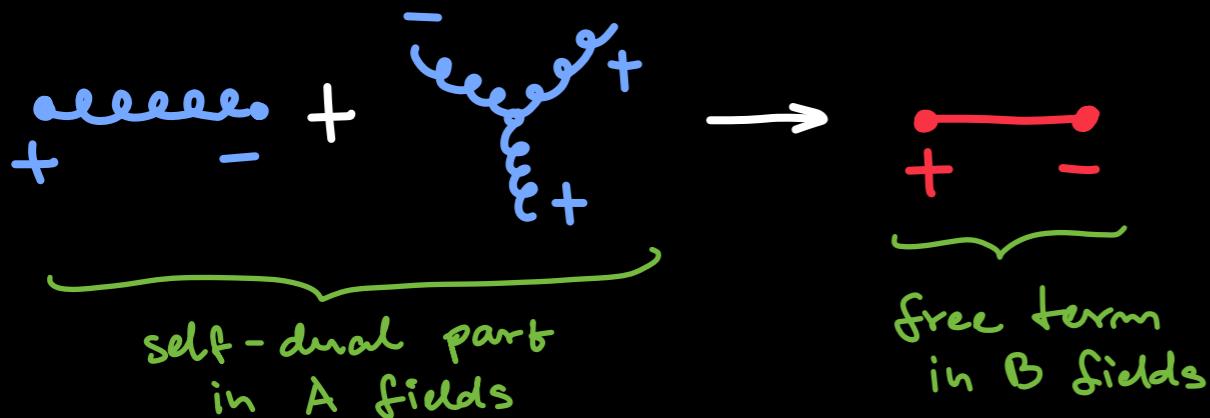
# INTRODUCTION

## Lagrangian for the CSW method (2)

### MHV action

Apply the canonical field transformation (at equal LC time)  $\{A^\bullet, A^\star\} \rightarrow \{B^\bullet, B^\star\}$

such that:



[P. Mansfield, 2006]

and

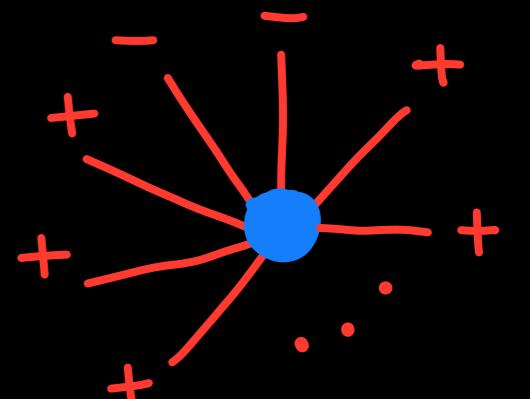
$$\partial_- A_a^\star(x^+; \mathbf{x}) = \int d^3y \frac{\delta B_c^\bullet(x^+; \mathbf{y})}{\delta A_a^\bullet(x^+; \mathbf{x})} \partial_- B_c^\star(x^+; \mathbf{y})$$

the solutions:  $\widetilde{A}_a^\bullet[B^\bullet](x^+; \mathbf{P}) = \sum_{n=1}^{\infty} \int d^3\mathbf{p}_1 \dots d^3\mathbf{p}_n \widetilde{\Psi}_n^{ab_1 \dots b_n}(\mathbf{P}; \mathbf{p}_1, \dots, \mathbf{p}_n) \prod_{i=1}^n \widetilde{B}_{b_i}^\bullet(x^+; \mathbf{p}_i)$

$$\widetilde{A}_a^\star[B^\bullet, B^\star](x^+; \mathbf{P}) = \sum_{n=1}^{\infty} \int d^3\mathbf{p}_1 \dots d^3\mathbf{p}_n \widetilde{\Omega}_n^{ab_1 b_2 \dots b_n}(\mathbf{P}; \mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_n) \widetilde{B}_{b_1}^\star(x^+; \mathbf{p}_1) \prod_{i=2}^n \widetilde{B}_{b_i}^\bullet(x^+; \mathbf{p}_i),$$

$$S_{Y-M}^{(LC)}[B^\bullet, B^\star] = \int dx^+ \left( - \int d^3\mathbf{x} \text{Tr} \hat{B}^\bullet \square \hat{B}^\star + \mathcal{L}_{--+}^{(LC)} + \dots + \mathcal{L}_{--+ \dots +}^{(LC)} + \dots \right)$$

MHV vertices



## (Incomplete) List of papers on the subject

### CSW method

- F. Cachazo, P. Svrcek, E. Witten, JHEP 09 (2004) 006
- F. Cachazo, P. Svrcek, E. Witten, JHEP 10 (2004) 074
- G. Georgiou, V. Khoze, JHEP 05 (2004)
- G. Georgiou, E.W.N. Glover, V.V. Khoze, JHEP 07 (2004)
- J.-B. Wu, C.-J. Zhu, JHEP 07 (2004) 032
- L.J. Dixon, E.W.N. Glover, V.V. Khoze, JHEP 12 (2004) 015
- K. Risager, JHEP 12 (2005) 003
- A. Brandhuber, B. Spence, G. Travaglini, JHEP 01 (2006) 142
- M. Kiermaier, S.G. Naculich, JHEP 05 (2009) 072
- T. Adamo, L. Mason, Phys.Rev.D 86 (2012) 065019

### Lagrangian formulation of CSW

- P. Mansfield, JHEP 03 (2006) 037
- J.H. Ettle, T.R. Morris, JHEP 08 (2006) 003
- A. Gorsky, A. Rosly, JHEP 01 (2006) 101
- J.H. Ettle, T.R. Morris, Z. Xiao, JHEP 08 (2008) 103
- T.R. Morris, Z. Xiao, JHEP 12 (2008) 028
- H. Feng, Y.-T. Huang, JHEP 04 (2009) 047
- C.-H. Fu, JHEP 04 (2010) 044
- S. Buchta, S. Weinzierl, JHEP 09 (2010) 071
- P.K, A. Stasto, JHEP 09 (2017)
- H. Kakkad, P.K, A. Stasto, Phys.Rev.D 102 (2020) 9

### Lagrangian formulation of CSW at loop level

- A. Brandhuber, B. Spence, G. Travaglini, JHEP 02 (2007) 088
- A. Brandhuber, B. Spence, G. Travaglini, K. Zoubos, JHEP 07 (2007) 002
- J.H. Ettle, C.-H. Fu, J.P. Fudger, P. Mansfield, T.R. Morris, JHEP 05 (2007) 011
- R. Boels, C. Schwinn, JHEP 07 (2008) 007
- C.-H. Fu, J.P. Fudger, P. Mansfield, T.R. Morris, Z. Xiao, JHEP 06 (2009) 035
- H. Elvang, D.Z. Freedman, M. Kiermaier, JHEP 06 (2012) 015
- H. Kakkad, P.K, A. Stasto, JHEP 11 (2022) 132

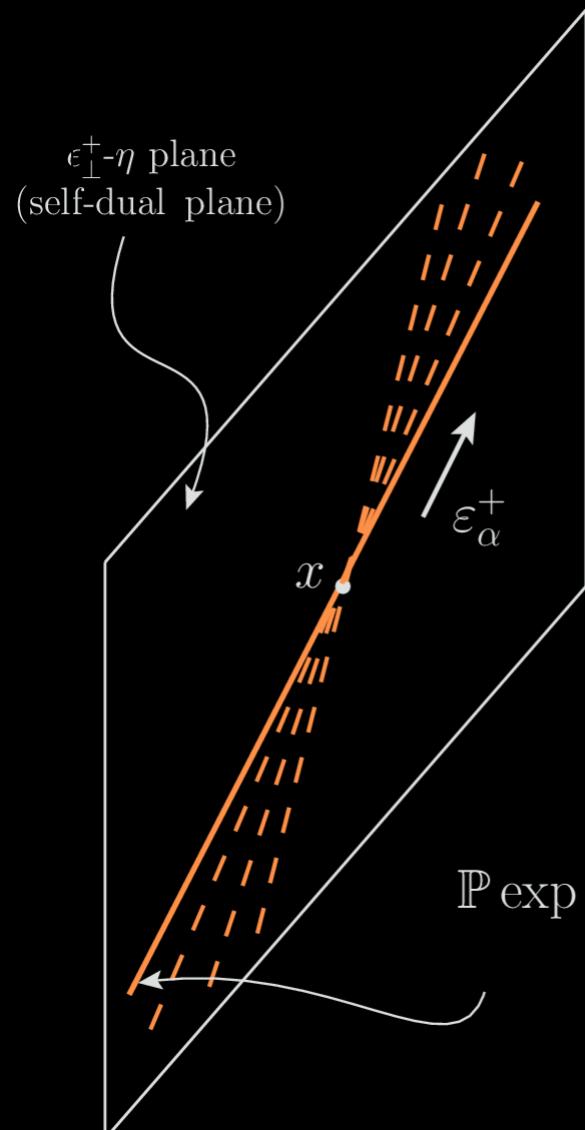
## Inverse solutions to field transformations

[PK, A. Stasto, 2017]

[H. Kakkad, PK, A. Stasto, 2020]

In order to understand the field transformations better, solve for  $B$  fields:

$$B_a^\bullet[A^\bullet](x) = \frac{1}{2\pi g} \int_{-\infty}^{\infty} d\alpha \operatorname{Tr} \left\{ t^a \partial_- \mathbb{P} \exp \left[ ig \int_{-\infty}^{\infty} ds \underbrace{\varepsilon_\alpha^+ \cdot \hat{A}}_{\mathbf{A}^\bullet} (x + s\varepsilon_\alpha^+) \right] \right\}$$



where  $\varepsilon_\alpha^{\pm\mu} = \varepsilon_\perp^{\pm\mu} - \alpha\eta^\mu$   $x \equiv (x^+, x^-, x^\bullet, x^\star)$

$$B_a^\star[A^\bullet; A^\star](x) = \int d^3y \left[ \frac{\partial_-^2(y)}{\partial_-^2(x)} \frac{\delta B_a^\bullet[A^\bullet](x^+; \mathbf{y})}{\delta A_c^\bullet(x^+; \mathbf{y})} \right] A_c^\star(x^+; \mathbf{y})$$

↑  
functional derivative  
of the Wilson line

Can one generalize to transformations supported on both self-dual and anti-self-dual plane?

## New fields $Z^\bullet, Z^*$

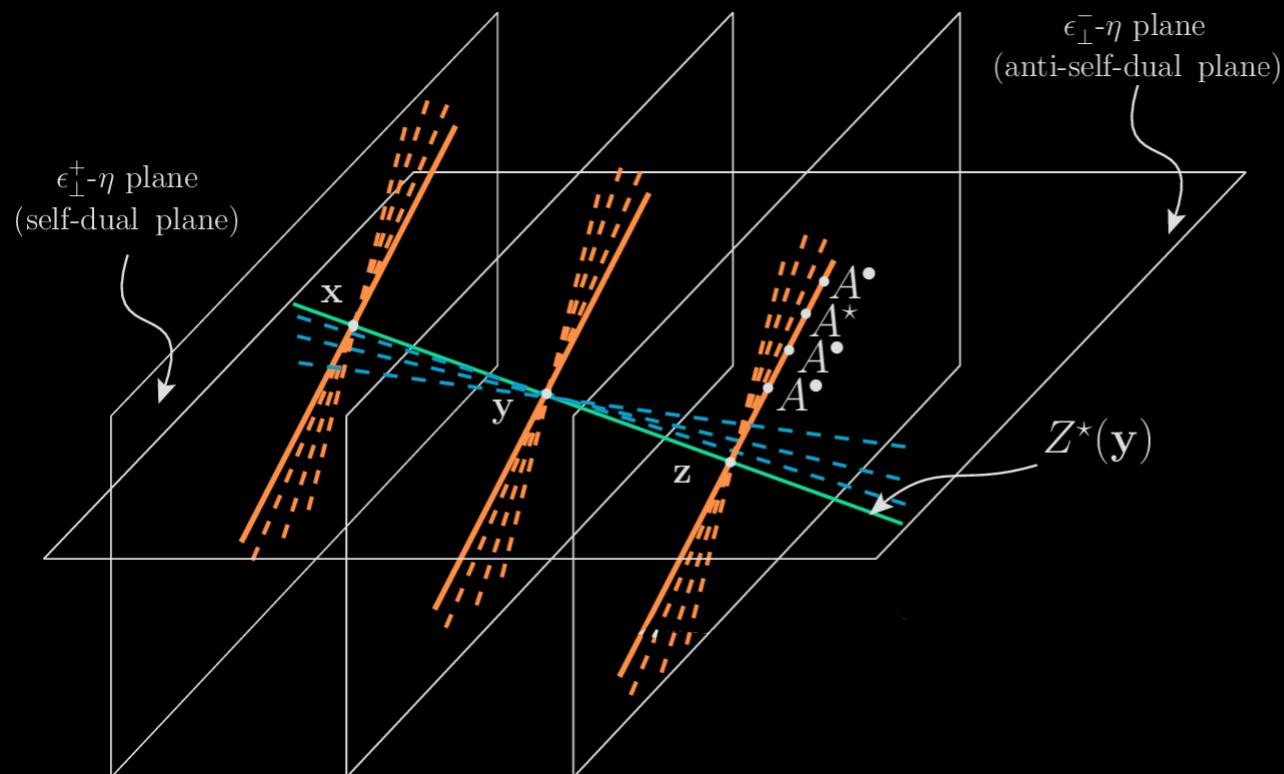
[H. Kakkad, PK, A. Stasto, 2021]

Introduce a canonical transformation  $\{A^\bullet, A^*\} \rightarrow \{Z^\bullet, Z^*\}$  given by the generating functional:

$$\mathcal{G}[A^\bullet, Z^*](x^+) = - \int d^3\mathbf{x} \text{ Tr } \hat{\mathcal{W}}_{(-)}^{-1}[Z](x) \partial_- \hat{\mathcal{W}}_{(+)}[A](x)$$

where

$$\mathcal{W}_{(\pm)}^a[K](x) = \frac{1}{2\pi g} \int_{-\infty}^{\infty} da \text{ Tr} \left\{ t^a \partial_- \mathbb{P} \exp \left[ ig \int_{-\infty}^{\infty} ds \ \varepsilon_\alpha^\pm \cdot \hat{K}(x + s\varepsilon_\alpha^\pm) \right] \right\}$$



Wilson line on self-dual  
or anti-self-dual plane

Relations between  $A$  and  $Z$  fields:

$$\partial_- A_a^*(x^+, \mathbf{y}) = \frac{\delta \mathcal{G}[A^\bullet, Z^*](x^+)}{\delta A_a^\bullet(x^+, \mathbf{y})}$$

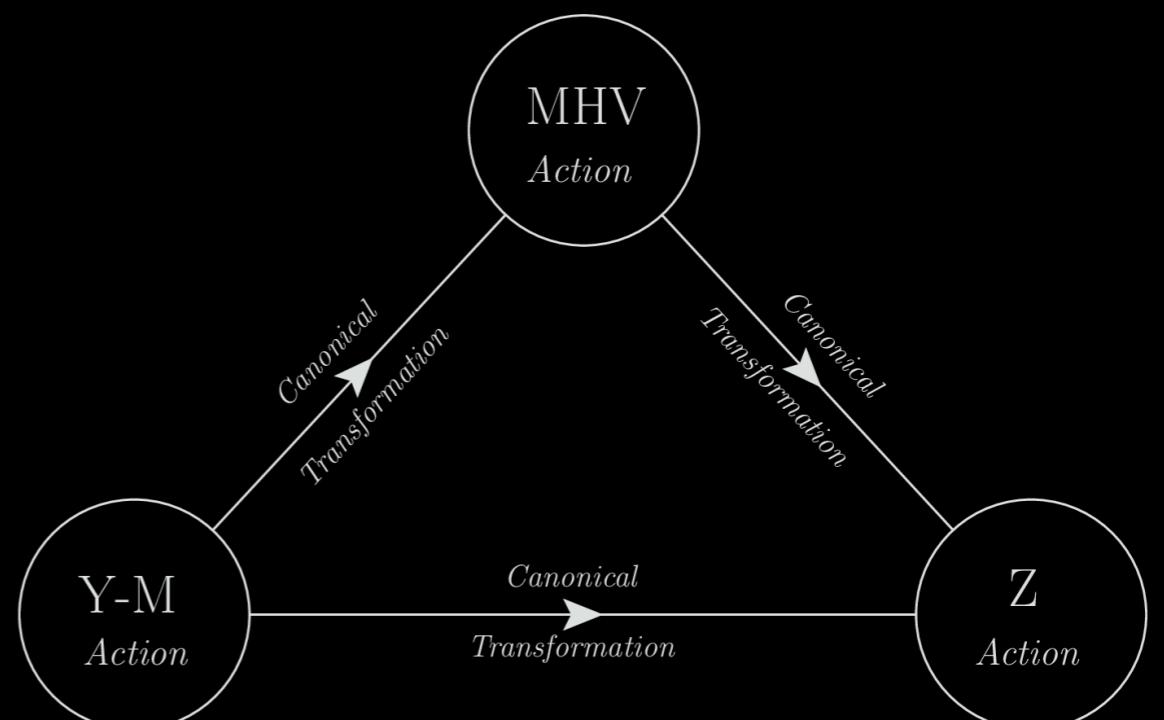
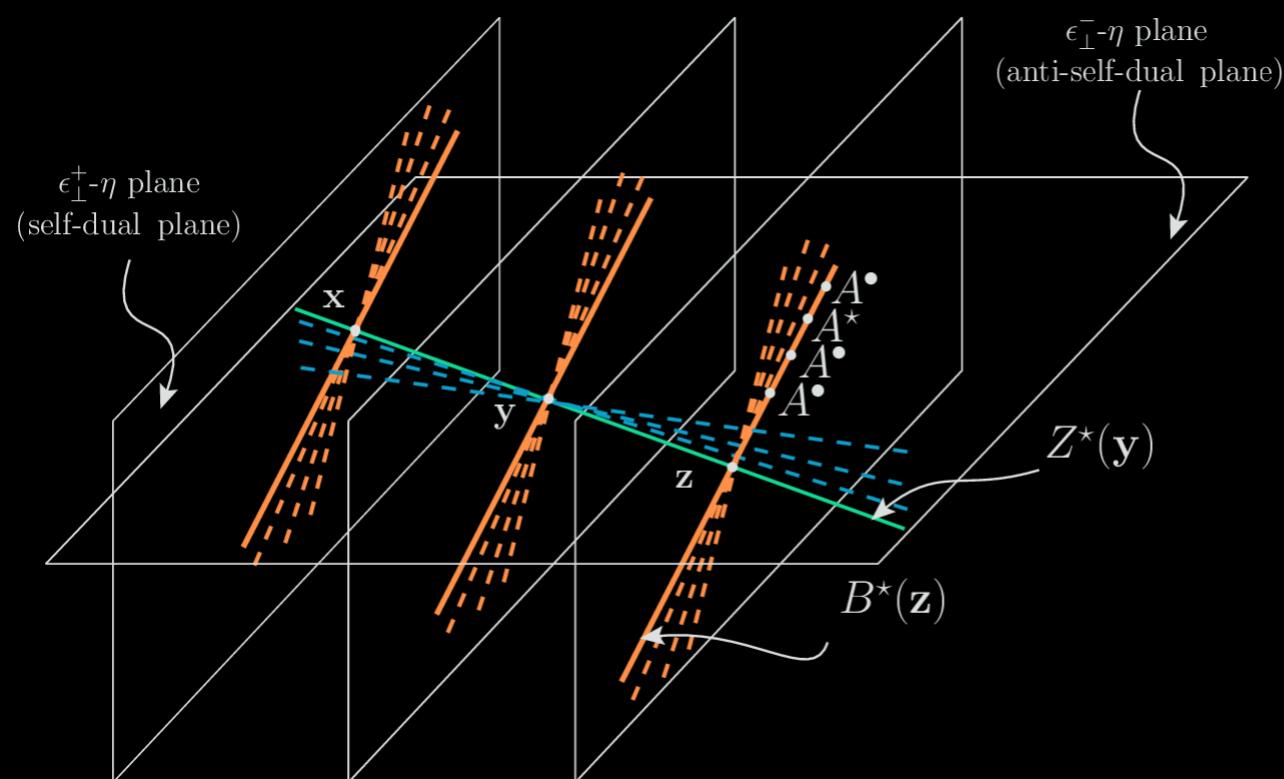
$$\partial_- Z_a^\bullet(x^+, \mathbf{y}) = - \frac{\delta \mathcal{G}[A^\bullet, Z^*](x^+)}{\delta Z_a^*(x^+, \mathbf{y})}$$

## Canonical transformation of the $B$ fields in the MHV action

[H. Kakkad, PK, A. Stasto, 2021]

It turns out, that the new fields can be introduced also from the MHV action :

$$\begin{cases} Z_a^\star[B^\star](x) = \mathcal{W}_{(-)}^a[B](x) \\ Z_a^\star[B^\star, B^\star](x) = \int d^3y \left[ \frac{\partial_-^2(y)}{\partial_-^2(x)} \frac{\delta Z_a^\star[B^\star](x^+; \mathbf{x})}{\delta B_c^\star(x^+; \mathbf{y})} \right] B_c^\star(x^+; \mathbf{y}) \end{cases}$$



## Z-field action

[H. Kakkad, PK, A. Stasto, 2021]

Solving the field transformation relations we get the following action:

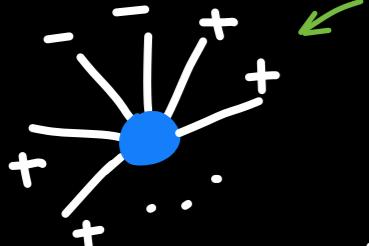
$$S_{Y-M}^{(LC)} [Z^\bullet, Z^*] = \int dx^+ \left\{ - \int d^3x \text{Tr} \hat{Z}^\bullet \square \hat{Z}^* \right.$$

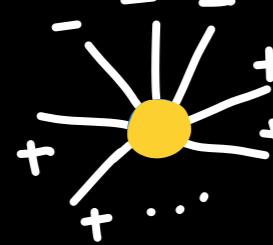

$$\left. + \mathcal{L}_{--+}^{(LC)} + \mathcal{L}_{--++}^{(LC)} + \mathcal{L}_{---++}^{(LC)} + \dots \right.$$

$$\left. + \mathcal{L}_{-+-+}^{(LC)} + \mathcal{L}_{-+-++}^{(LC)} + \mathcal{L}_{-+-++}^{(LC)} + \dots \right.$$

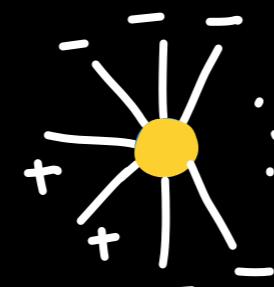
$$\vdots$$

$$\left. + \mathcal{L}_{---...-++}^{(LC)} + \mathcal{L}_{---...-++}^{(LC)} + \mathcal{L}_{---...-++}^{(LC)} + \dots \right\}$$

**MHV vertices** → 

NMHV → 

etc...

**MHV vertices** → 

**No triple gluon vertices!**

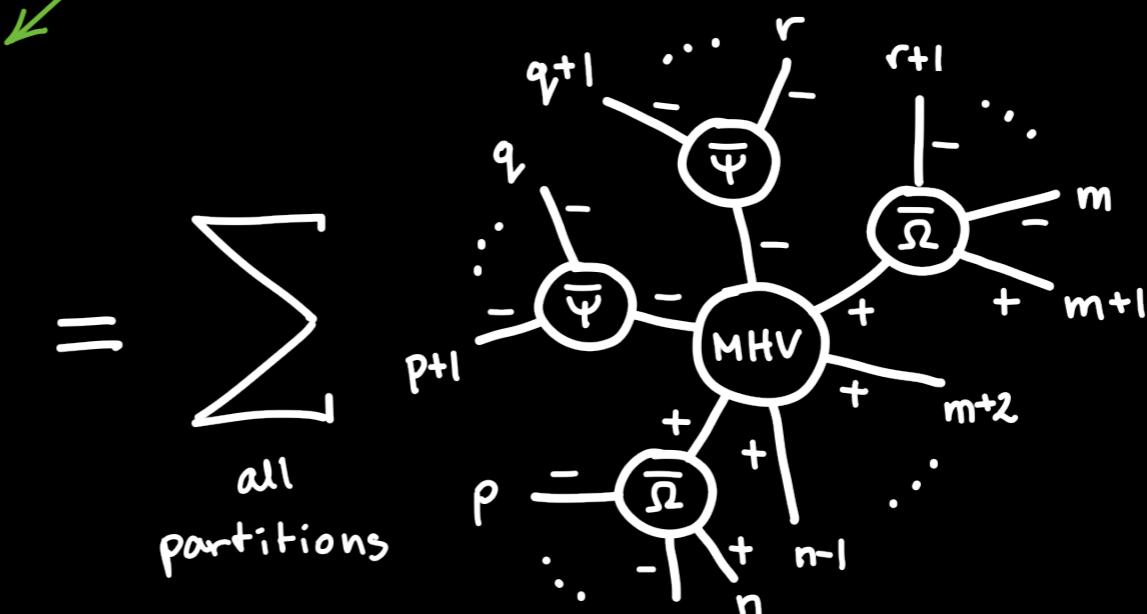
# NEW ACTION

# Structure of vertices

## Master formula for a vertex

[H. Kakkad, PK, A. Stasto, 2021]

$$\mathcal{L}_{\underbrace{- \dots -}_m \underbrace{+ \dots +}_{n-m}}^{(LC)} = \int d^3 \mathbf{y}_1 \dots d^3 \mathbf{y}_n \mathcal{U}_{\dots}^{b_1 \dots b_n} (\mathbf{y}_1, \dots, \mathbf{y}_n) \prod_{i=1}^m Z_{b_i}^\star(x^+; \mathbf{y}_i) \prod_{j=1}^{n-m} Z_{b_j}(x^+; \mathbf{y}_j)$$



Inverse  
Wilson line  
kernels

$$\widetilde{\Psi}_n^{ab_1 \dots b_n}(\mathbf{P}; \{\mathbf{p}_1, \dots, \mathbf{p}_n\}) = -(-g)^{n-1} \frac{\tilde{v}_{(1 \dots n)1}}{\tilde{v}_{1(1 \dots n)}} \frac{\delta^3(\mathbf{p}_1 + \dots + \mathbf{p}_n - \mathbf{P})}{\tilde{v}_{21} \tilde{v}_{32} \dots \tilde{v}_{n(n-1)}} \text{Tr}(t^a t^{b_1} \dots t^{b_n})$$

$$\widetilde{\Omega}_n^{ab_1 \dots b_n}(\mathbf{P}; \mathbf{p}_1, \{\mathbf{p}_2, \dots, \mathbf{p}_n\}) = n \left( \frac{p_1^+}{p_{1 \dots n}^+} \right)^2 \widetilde{\Psi}_n^{ab_1 \dots b_n}(\mathbf{P}; \mathbf{p}_1, \dots, \mathbf{p}_n).$$

$$\begin{aligned} \tilde{v}_{ij} &= p_i^+ \left( \frac{p_j^\star}{p_j^+} - \frac{p_i^\star}{p_i^+} \right) \\ &= -(\epsilon_i^- \cdot p_j) \sim [ij] \end{aligned}$$

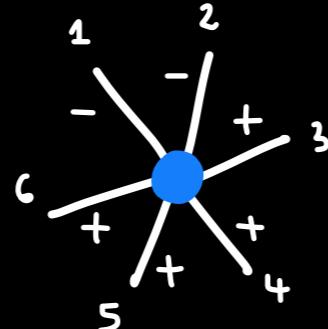
# NEW ACTION

## Example of amplitude calculation (1)

### 6-point amplitudes

$$\mathcal{A}(1^\pm, 2^+, 3^+, 4^+, 5^+, 6^+) = 0$$

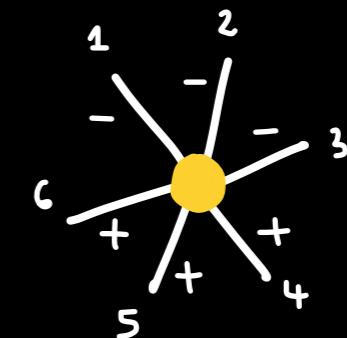
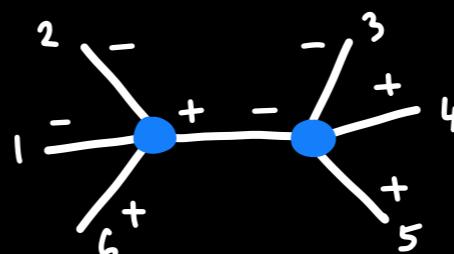
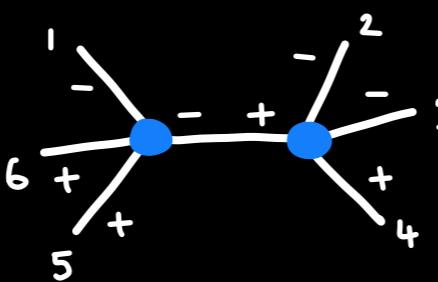
$$\mathcal{A}(1^-, 2^-, 3^+, 4^+, 5^+, 6^+) =$$



$$= g^4 \left( \frac{p_1^+}{p_2^+} \right)^2 \frac{\tilde{u}_{21}^4}{\tilde{u}_{16}\tilde{u}_{65}\tilde{u}_{54}\tilde{u}_{43}\tilde{u}_{32}\tilde{u}_{21}}$$

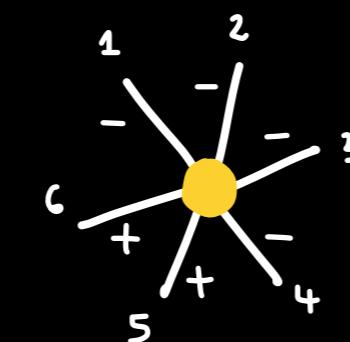
MHV

$$\mathcal{A}(1^-, 2^-, 3^-, 4^+, 5^+, 6^+) =$$



NMHV

$$\mathcal{A}(1^-, 2^-, 3^-, 4^-, 5^+, 6^+) =$$



$$= g^4 \left( \frac{p_5^+}{p_6^+} \right)^2 \frac{\tilde{v}_{65}^4}{\tilde{v}_{16}\tilde{v}_{65}\tilde{v}_{54}\tilde{v}_{43}\tilde{v}_{32}\tilde{v}_{21}}$$

$\overline{\text{MHV}}$

$$\tilde{v}_{ij} = -(\epsilon_i^- \cdot p_j) = p_i^+ \left( \frac{p_j^\star}{p_j^+} - \frac{p_i^\star}{p_i^+} \right) \sim [ij]$$

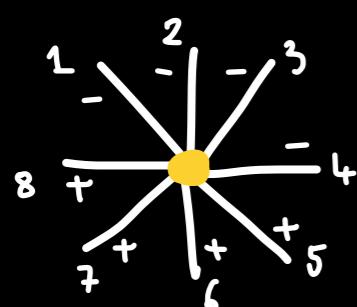
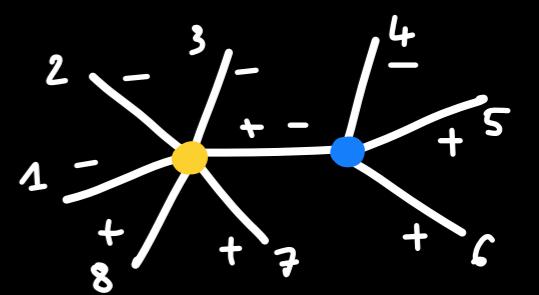
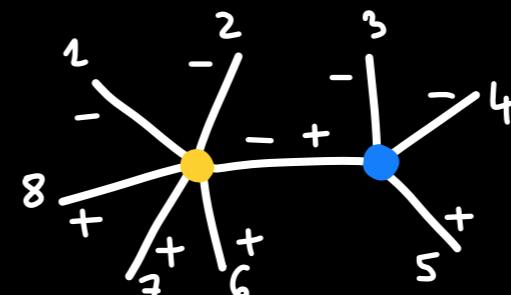
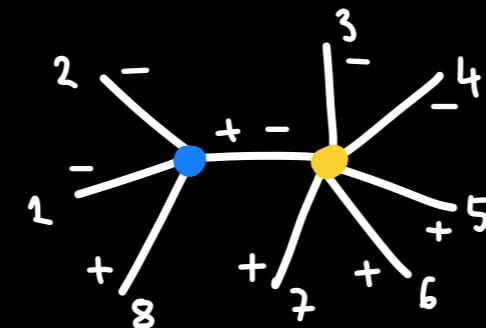
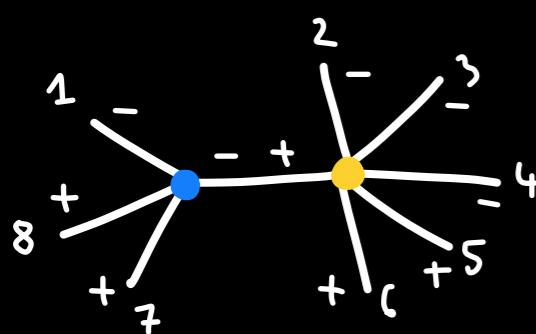
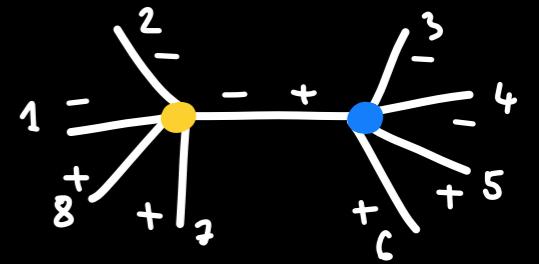
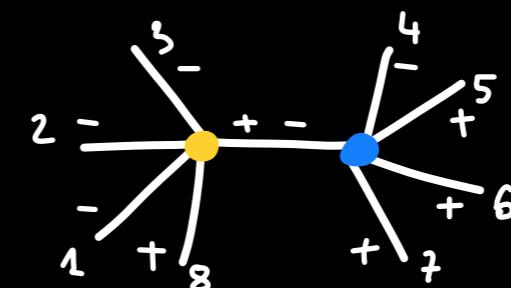
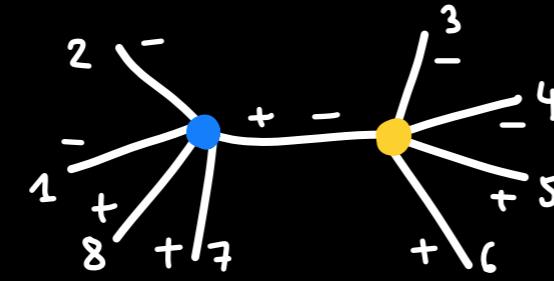
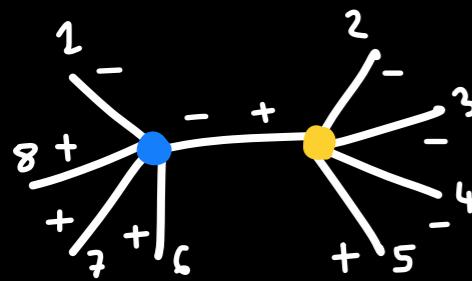
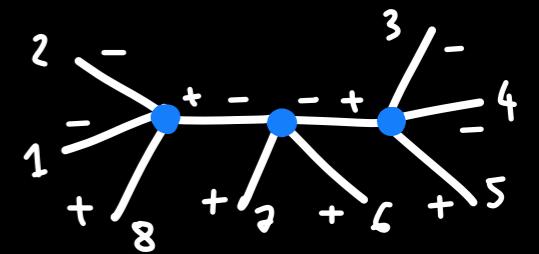
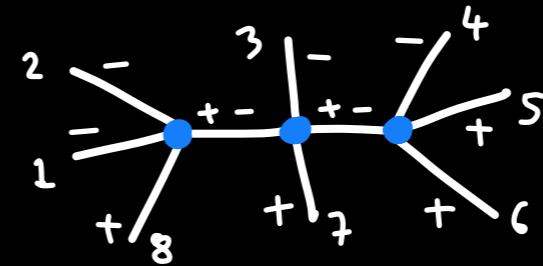
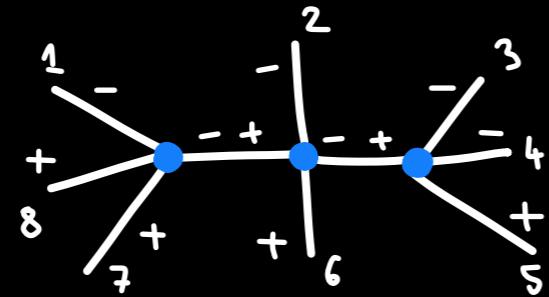
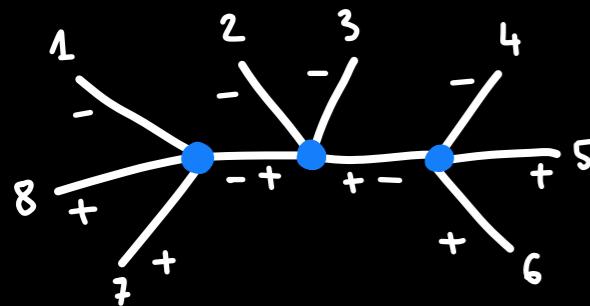
$$\tilde{u}_{ij} = -(\epsilon_i^+ \cdot p_j) = p_i^+ \left( \frac{p_j^\bullet}{p_j^+} - \frac{p_i^\bullet}{p_i^+} \right) \sim \langle ij \rangle$$

# NEW ACTION

## Example of amplitude calculation (2)

8-point NNMHV amplitude  $\mathcal{A}(1^-, 2^-, 3^-, 4^-, 5^+, 6^+, 7^+, 8^+)$

[H. Kakkad, PK, A. Stasto, 2021]



Summary: 13 diagrams

vertices used: 4p-MHV, 5p-MHV, 5p- $\overline{\text{MHV}}$ , 6p-NMHV, 8p-NNMHV

## All-plus-helicity amplitude at one loop

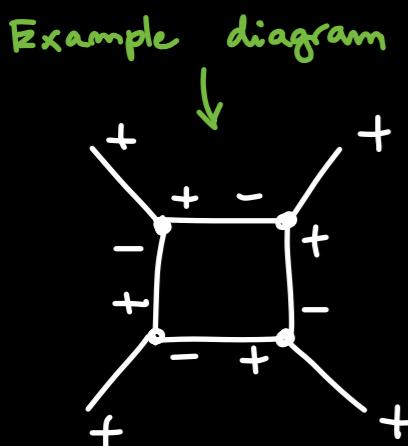
Amplitude with all same helicity gluons is non-zero at one loop and is a rational function:

$$\mathcal{A}^{(1)}(1^+, 2^+, 3^+, \dots, n^+) = g^n \sum_{q \leq i < j < k < l \leq n} \frac{\langle ij \rangle [jk] \langle kl \rangle [li]}{\langle 12 \rangle \langle 23 \rangle \dots \langle n1 \rangle}$$

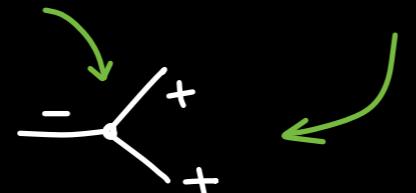
[Z. Bern, G. Chalmers, L. Dixon, D.A. Kosover, 1993]  
 [G. Mahlon, 1994]

## Problems with MHV action (or Z-field action) at quantum level

It is not possible to reconstruct  $(\pm + + \dots +)$  amplitudes in the MHV theory or the Z-field action.



the only contributing vertex



The self-dual vertex  $(- + +)$  was removed in both MHV action and in the Z-field action.

One also cannot get the rational parts of other (singular) amplitudes...

[J. Bedford, A. Brandhuber, B.J. Spence, G. Travaglini, 2005]

### One loop effective action

Generating functional for Y-M theory:

$$\mathcal{Z}_{\text{Y-M}}[J] = \int [dA^\bullet][dA^\star] e^{i\{S[A^\bullet, A^\star] + \int d^4x \text{Tr}(\hat{J}_\bullet \hat{A}^\bullet + \hat{J}_\star \hat{A}^\star)\}}$$

Apply the field transformation  $A \rightarrow Z$ :  
 (warning: transform also the current terms!)

$$\mathcal{Z}[J] = \int [dZ^\bullet][dZ^\star] e^{i\{S[Z^\bullet, Z^\star] + \int d^4x \text{Tr}(\hat{J}_\bullet \hat{A}^\bullet[Z] + \hat{J}_\star \hat{A}^\star[Z])\}}$$

Integrate quadratic fluctuations around the classical solution:

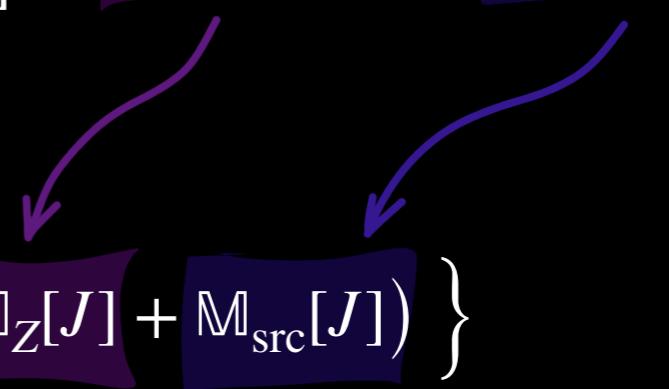
*Z-field theory  
vertices*

$$\mathcal{Z}[J] \approx \exp \left\{ iS[Z_c^\bullet[J], Z_c^\star[J]] - i\frac{1}{2}\text{Tr} \ln (\mathbb{M}_Z[J] + \mathbb{M}_{\text{src}}[J]) \right\}$$



$$(\mathbb{M}_Z[J])_{kl} = \left( \frac{\delta^2 S[Z]}{\delta Z^k \delta Z^l} \right), \quad (\mathbb{M}_{\text{src}}[J])_{kl} = \left( J_m \frac{\delta^2 A^m[Z]}{\delta Z^k \delta Z^l} \right)$$

*missing contributions*



where  $k, l, m, \dots = \{\{\bullet, \star\}, x^\mu, a\}$  are collective indices.

Legendre transform to  
one-loop effective action:

$$\mathcal{Z}[J] \rightarrow \Gamma[\phi] = S[\phi] - \frac{1}{2}\text{Tr} \ln (\mathbb{M}_Z + \mathbb{M}_{\text{src}})_{Z_c[J]=\phi}$$

### Further steps

- The log can be “computed” to the desired number of legs, but it’s complicated as there are multiple nested sums ( I used FORM ... )

$$\text{Tr} \ln (\mathbb{M}_Z + \mathbb{M}_{\text{src}}) = \text{tadpoles} - 4 \begin{array}{c} \square Z^* \\ \text{---} \\ \Xi \quad \Lambda \\ \text{---} \end{array} - \frac{1}{2} \begin{array}{c} \square Z^* \\ \text{---} \\ \Xi \quad \Lambda \\ \text{---} \end{array} - \frac{1}{2} \begin{array}{c} \square Z^* \\ \text{---} \\ \Lambda \quad \Xi \\ \text{---} \end{array} + \dots$$

- We can prove that the one loop effective action is “quantum complete” (the rational contributions are not missing).
- Diagrams can be calculated in 4D world-sheet regularization scheme Chakrabarti-Qiu-Thorn (CQT).

[ for some examples see H. Kakkad thesis, ArXiv:2308.07695 ]

# CONCLUSIONS

But... is it worth it?

- The structure at quantum level gets very complicated (unlike the classical level), just because of the self-dual and anti-self dual sectors.
- Still, the number of diagrams for loop amplitudes is smaller than in Y-M, because of very efficient tree management.
- The new fields have very interesting geometric structure given by the Wilson line functionals. What to do with that?
- This formulation bags for N=4 SYM extension (or reduction, taking into account that the rational contributions are zero there...).