

X-Ray Nano-Analytics and Microscopy

Part I



Christian G. Schroer
DESY & Universität Hamburg

HELMHOLTZ RESEARCH FOR
GRAND CHALLENGES



Universität Hamburg
DER FORSCHUNG | DER LEHRE | DER BILDUNG

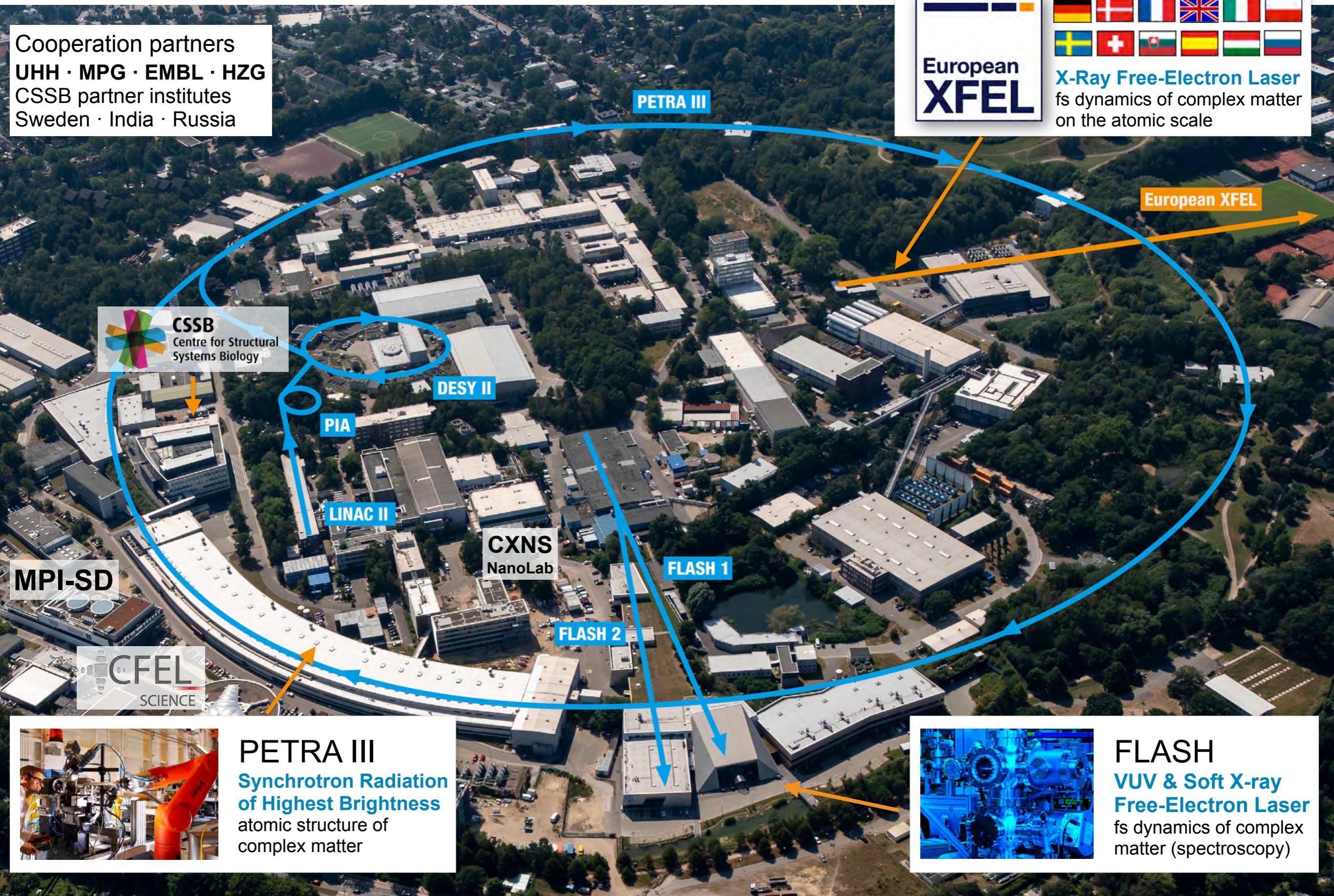


DESY: Bright Light for Science

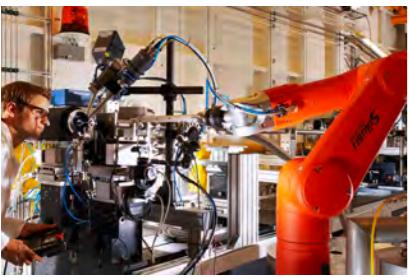
Cooperation partners
UHH · MPG · EMBL · HZG
CSSB partner institutes
Sweden · India · Russia



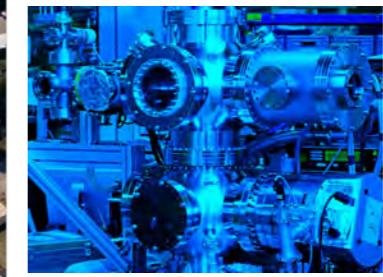
European XFEL
X-Ray Free-Electron Laser
fs dynamics of complex matter
on the atomic scale



PETRA III
Synchrotron Radiation
of Highest Brightness
atomic structure of
complex matter



FLASH
VUV & Soft X-ray
Free-Electron Laser
fs dynamics of complex
matter (spectroscopy)



X-ray Scanning Microscopy

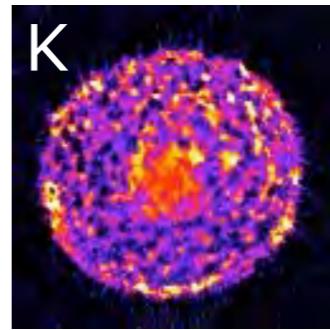
Broad field of applications:

- > Main advantage: large penetration depth
 - *in-situ* and *operando* studies
 - 3D bulk analysis without destructive sample preparation
- > X-ray analytical contrasts: XRD, XAS, XRF, ...
 - elemental, chemical, and structural information

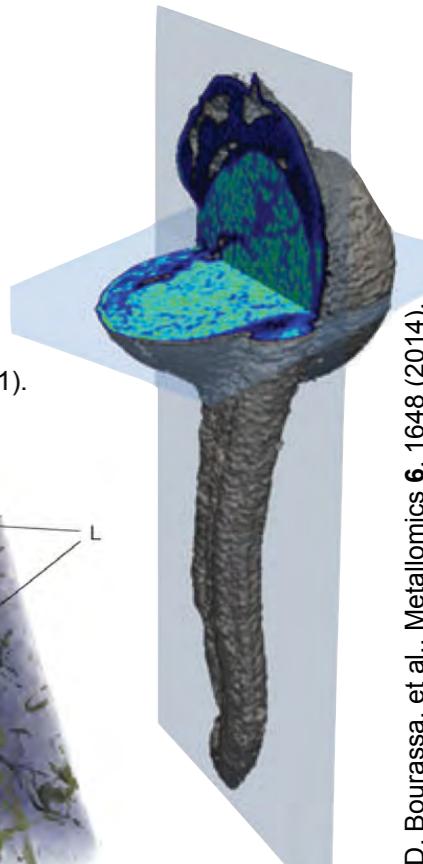
Today: „mesoscopic gap“

real-space resolution: down to about 10 nm

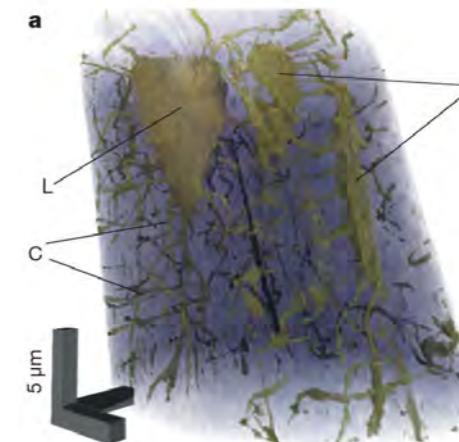
XRD and XAS: atomic scale



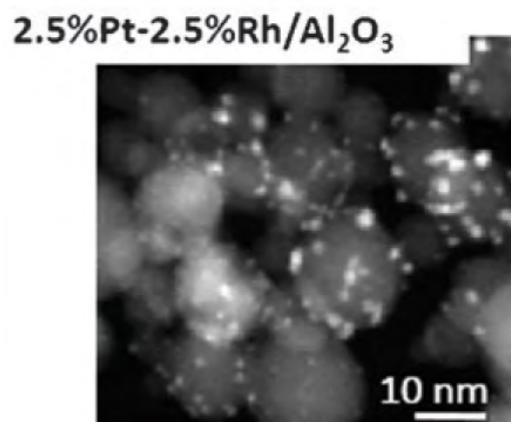
C. G. Schroer, APL **79**, 1912 (2001).



D. Bourassa, et al., Metallomics **6**, 1648 (2014).

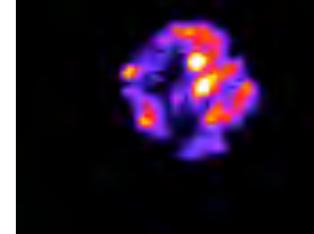


M. Dierolf, et al., Nature **467**, 436 (2010).



catalysts

Cu(I)₂O



C. G. Schroer, et al., APL **82**, 3360 (2003).

Many interesting physics and chemistry (e. g. catalysis)
at the 1 - 10 nm scale!

X-ray Microscopy

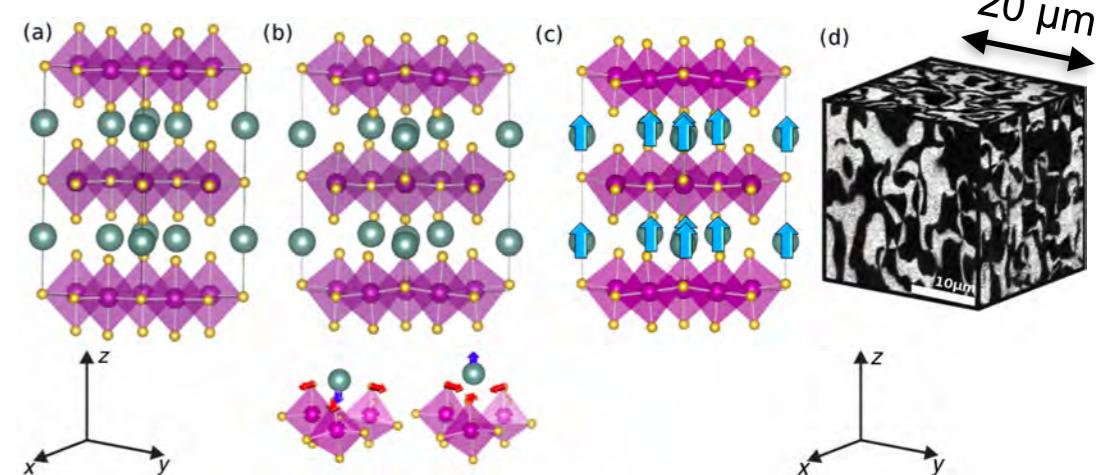
Many interesting physics and chemistry questions:

investigate local states:

- > individual defects (0D): changes in electron density, charge ordering
- > (structural) domain boundaries (2D), e. g., in multiferroics
- > mesoscopic dynamics at (solid-state) phase transitions
- > catalytic nanoparticles (under reaction conditions)
- > ...

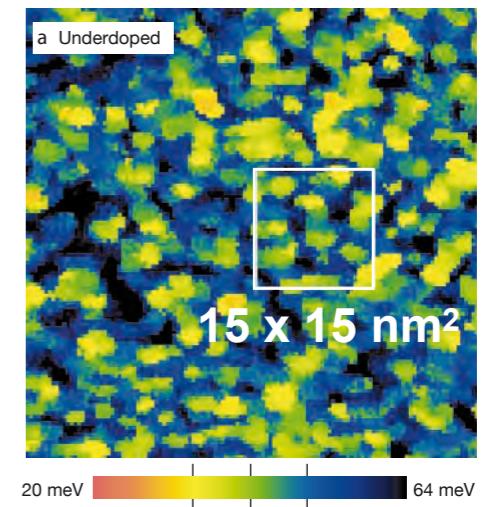
Mesoscale also very important for nanotechnology (e. g., defects in devices)!

ferroelectric phase transition



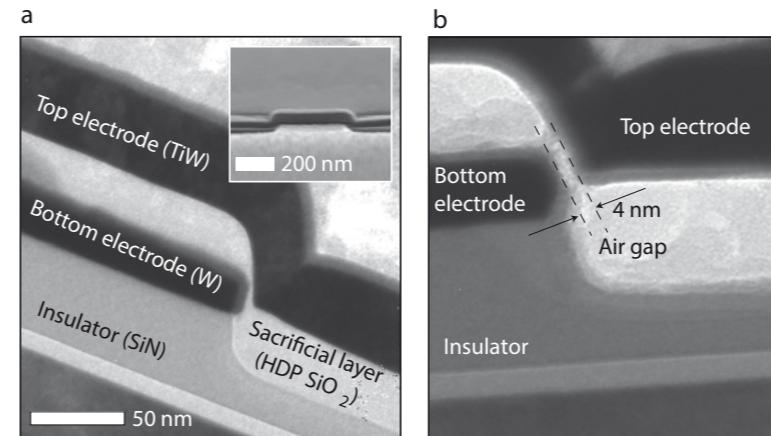
Griffin, et al., PRX 2, 041022 (2012).

variation of supercond. gap



Lang, et al., Nature 415, 412 (2002).

nanoelectromechanical switch



Lee, et al., Nature Nanotech. 8, 36 (2012).

Current State of X-Ray Microscopy

Conventional X-ray microscopy

- optics limit spatial resolution: diffraction limit

$$d = \frac{\lambda}{2n \sin \alpha}$$

(typically: a few tens of nanometers)

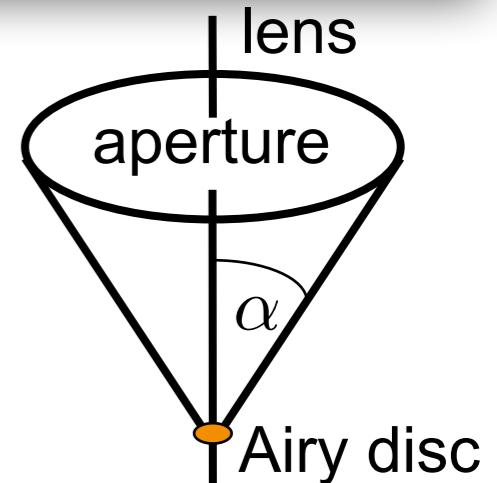
optics are technology limited!

Theoretical extrapolation of X-ray optical performance to the atomic level.

[PRB **74**, 033405 (2006); H. Yan, et al., PRB **76**, 115438 (2007)]



Ernst Abbe



Coherent X-ray imaging techniques (CXDI, ptychography)

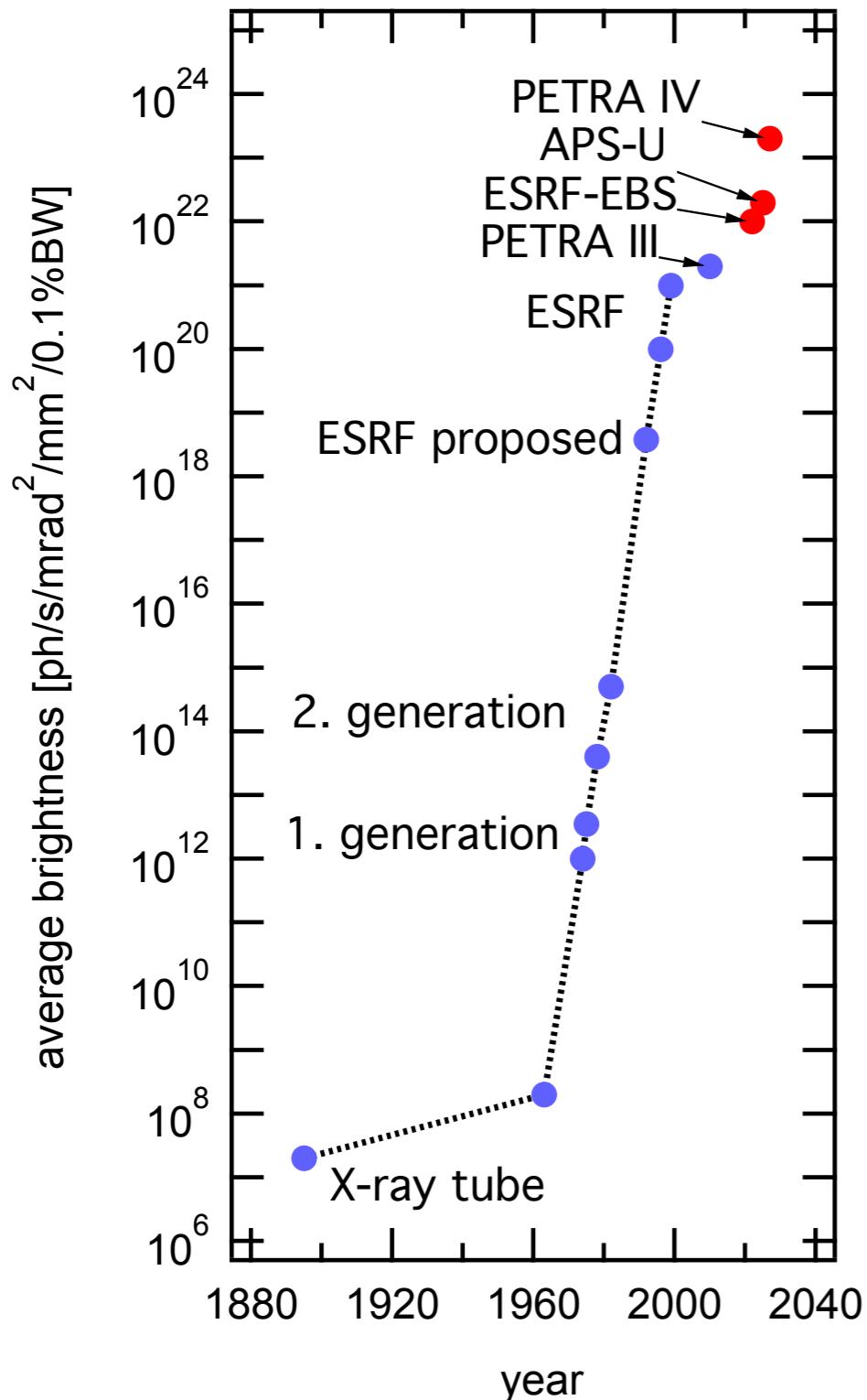
- no imaging optics needed!
- limited by statistics of far-field diffraction patterns ...

highest resolution: a few nanometers, focusing coherent beam

[PRL **101**, 090801 (2008); Y. Takahashi, et al., PRB **80**, 054103 (2009);
A. Schropp, et al., APL **100**, 253112 (2012)]

Spectral Brightness

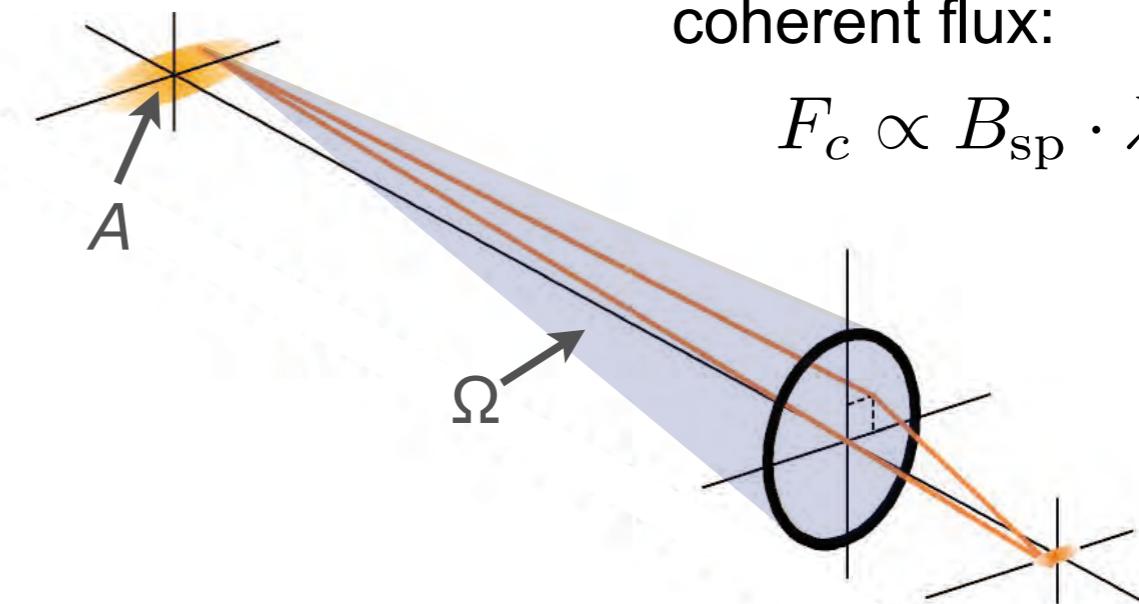
10000x more light per decade (since 1965)



Spectral brightness:

$$B_{\text{sp}} = \frac{F}{\Omega \cdot A \cdot \Delta E / E}$$

Flux per phase-space volume



coherent flux:

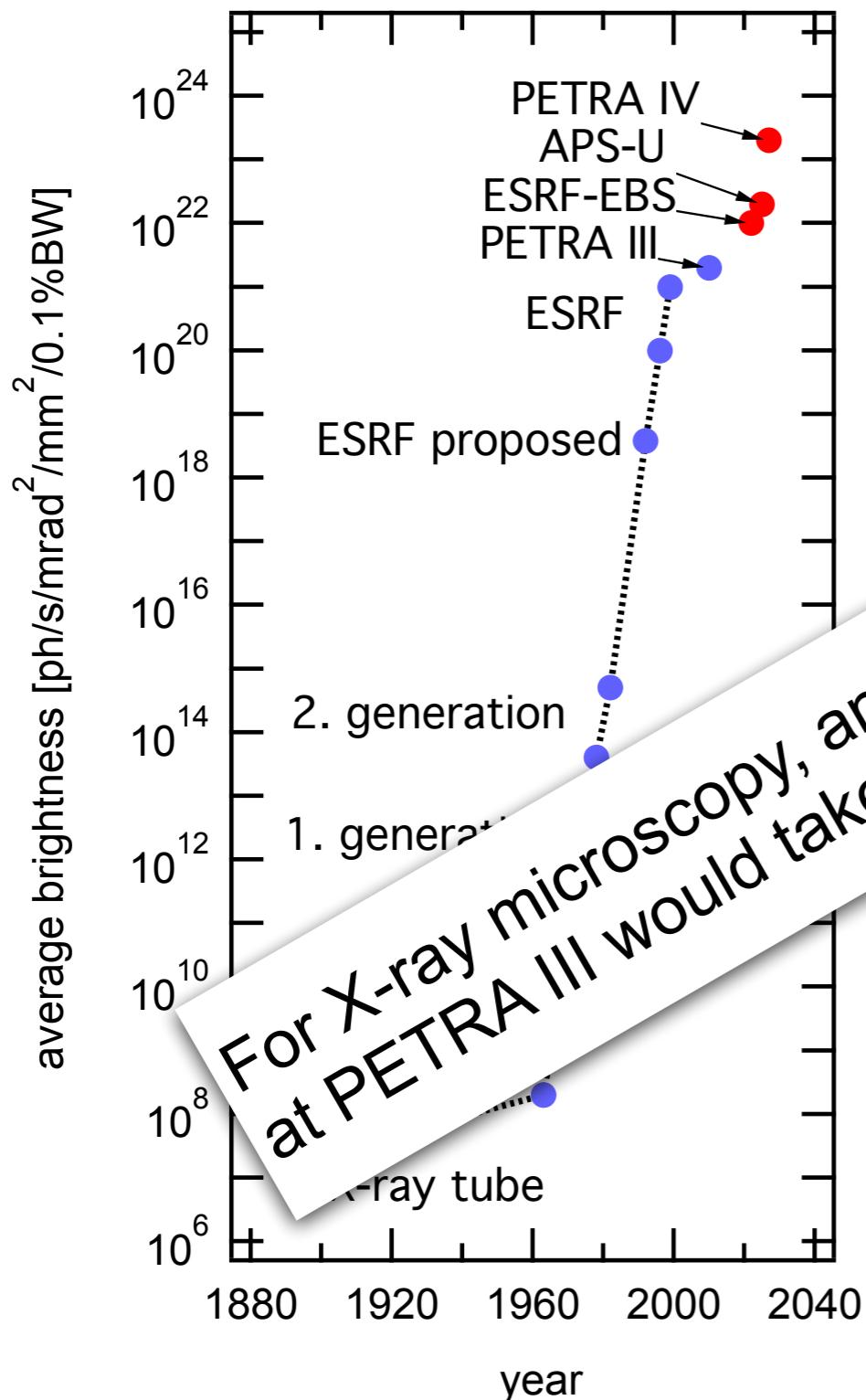
$$F_c \propto B_{\text{sp}} \cdot \lambda^2 \cdot \frac{\Delta E}{E}$$

Improvements in brightness:

- > faster measurements (time resolution)
- > nano-imaging (spatial resolution)
- > spectroscopy (energy resolution)

Spectral Brightness

10000x more light per decade (since 1965)



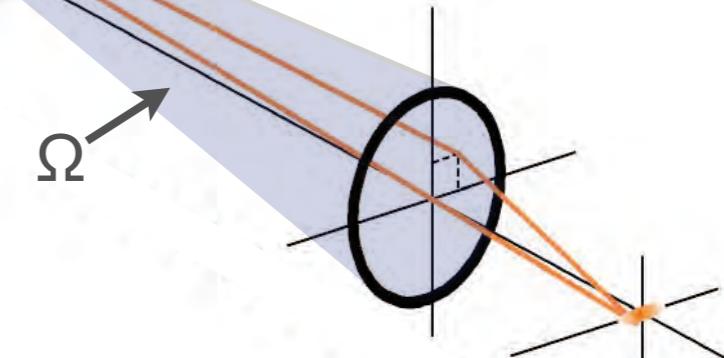
Spectral brightness:

$$B_{sp} = \frac{F}{\Omega \cdot t}$$

Flux per phase

Inherent flux:

$$F_c \propto B_{sp} \cdot \lambda^2 \cdot \frac{\Delta E}{E}$$



Improvements in brightness:

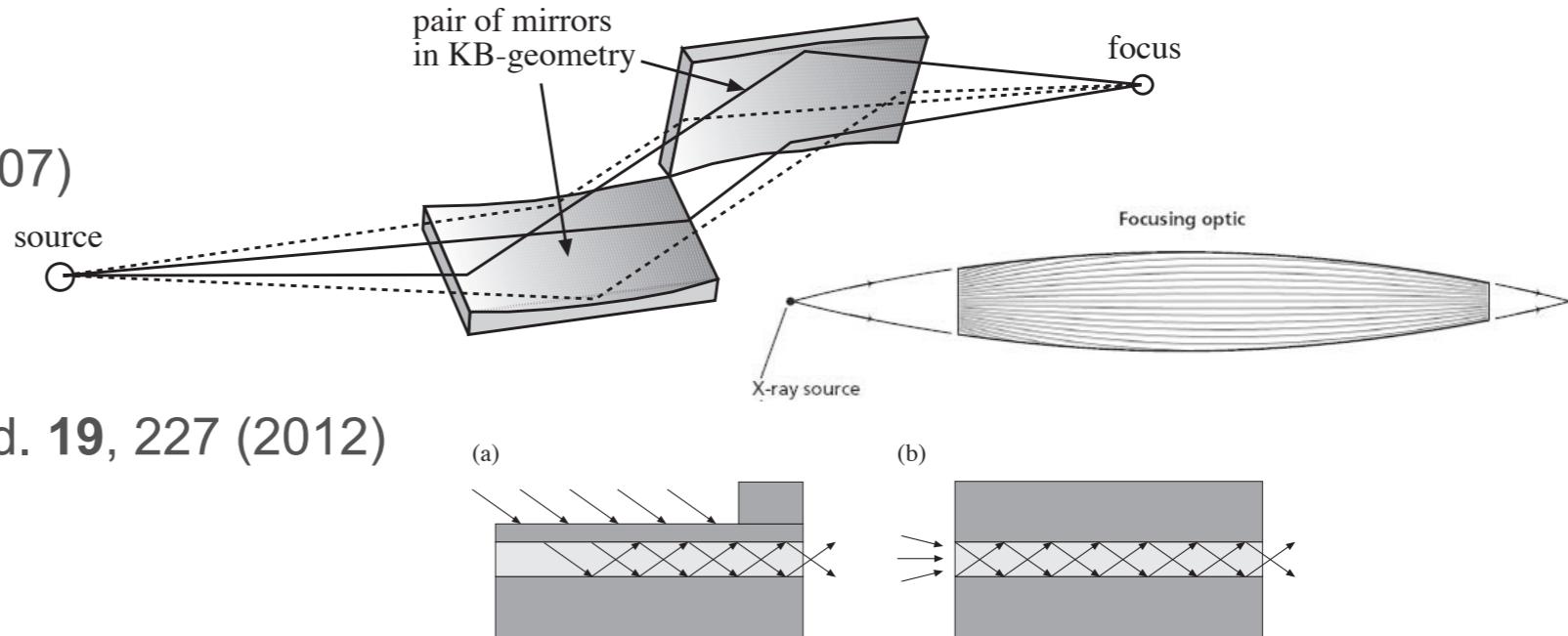
- > faster measurements (time resolution)
- > nano-imaging (spatial resolution)
- > spectroscopy (energy resolution)

Nanofocusing Optics

reflection:

- > mirrors (25 nm)

H. Mimura, et al., APL **90**, 051903 (2007)



- > capillaries

- > wave guides (~10 nm)

S. P. Krüger, et al., J. Synchrotron Rad. **19**, 227 (2012)

diffraction:

- > Fresnel zone plates (< 10 nm)

J. Vila-Comamala, et al., Ultramic. **109**, 1360 (2009)

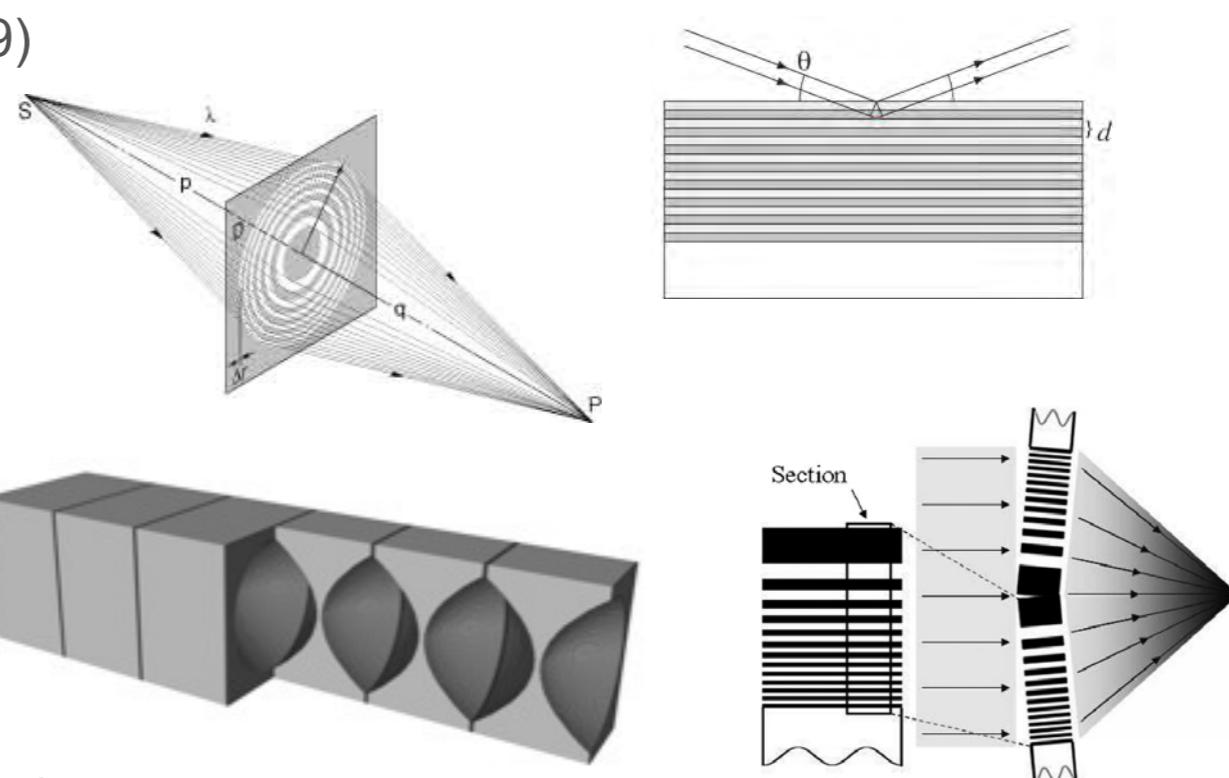
- > multilayer mirrors (7 nm)

H. Mimura, et al., Nat. Phys. **6**, 122 (2010)

- > multilayer Laue lenses (8 x 7 nm)

S. Bajt, et al., Light: Sci. & App. **7**, 17162 (2018)

- > bent crystals



refraction:

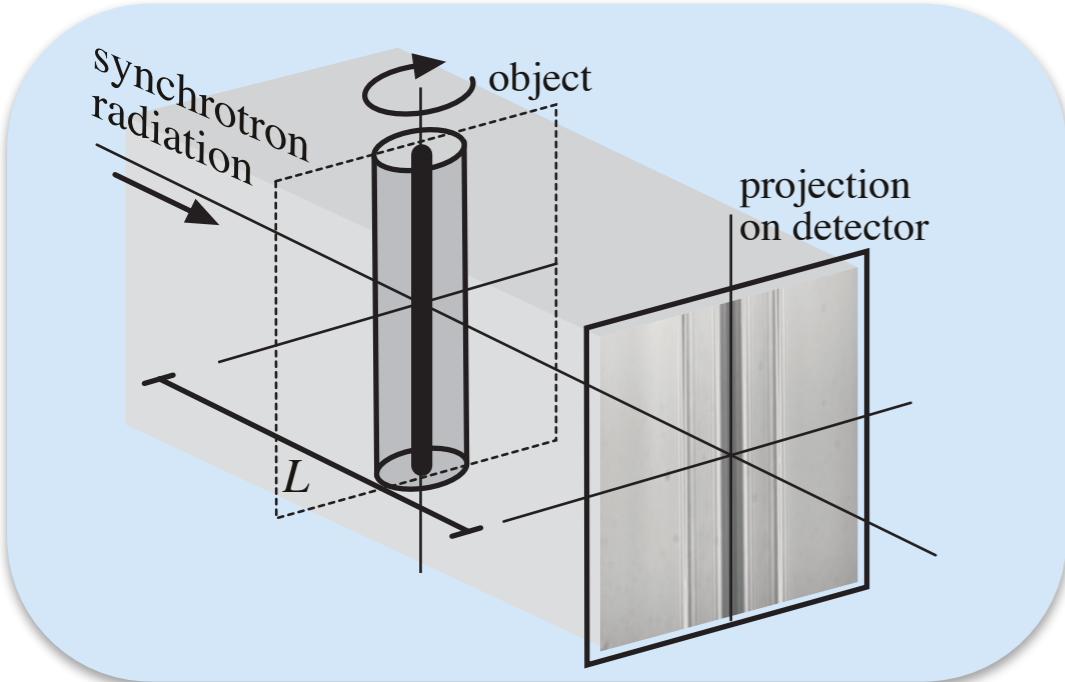
- > lenses (43 nm, 18 nm)

C. G. Schroer, et al., AIP Conf. Ser. **1365**, 227 (2011)

J. Patommel, et al., APL **110**, 101103 (2017)

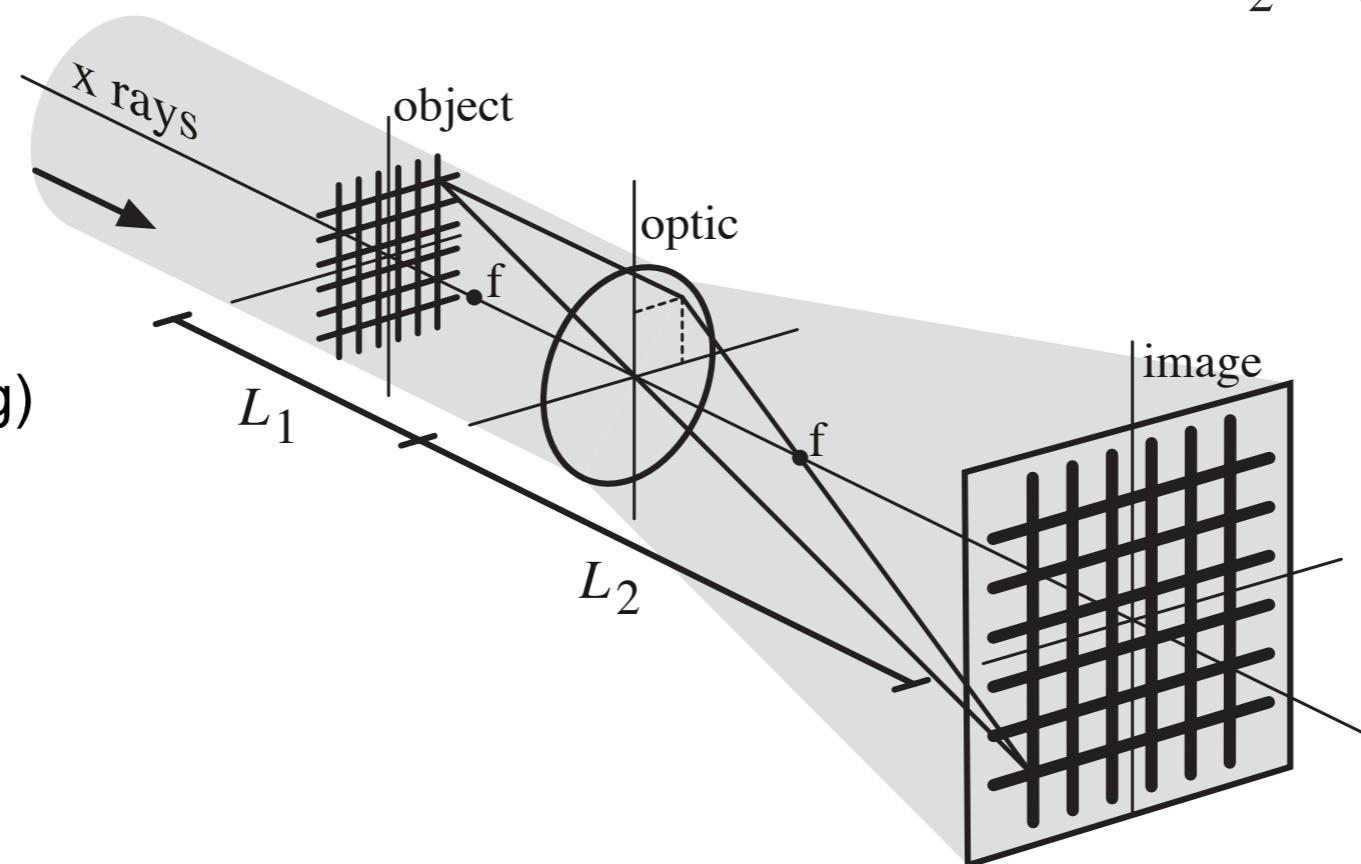
X-Ray Microscopy Techniques: Full-Field Imaging

Projection imaging:



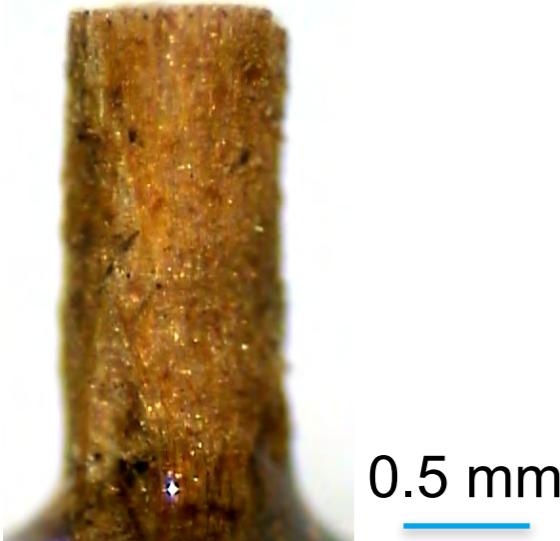
Imaging through objective lens:

x-rays focused by
condensor
(aperture matching)



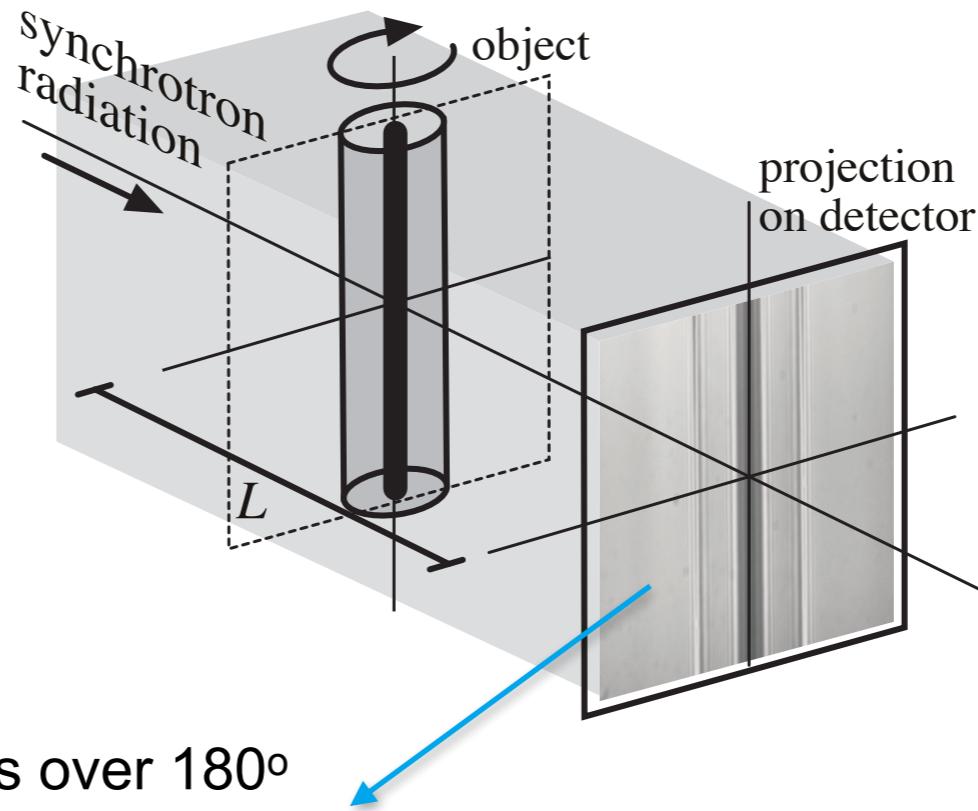
Example: Projection Imaging (Phase Contrast)

Example: plant physiology

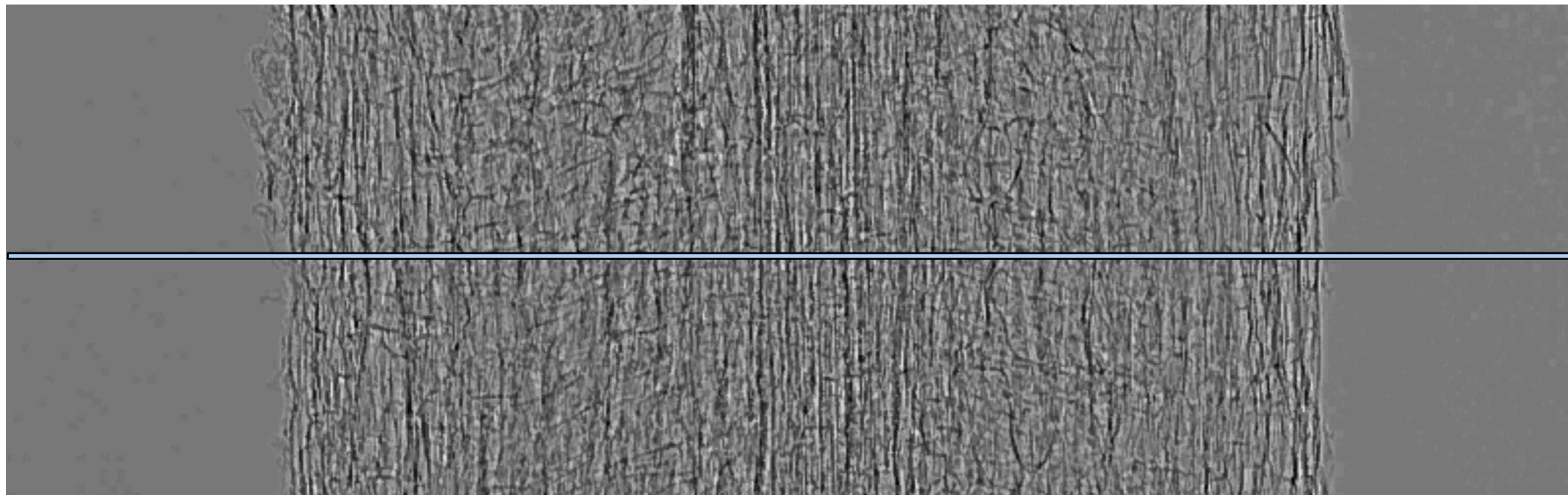


root of mahogany tree
(W. H. Schröder, FZ Jülich)

Reveal inner structures of object:



1250 projections over 180°



energy: 20 keV
 $L = 50 \text{ mm}$
pixel size: 1.4 μm

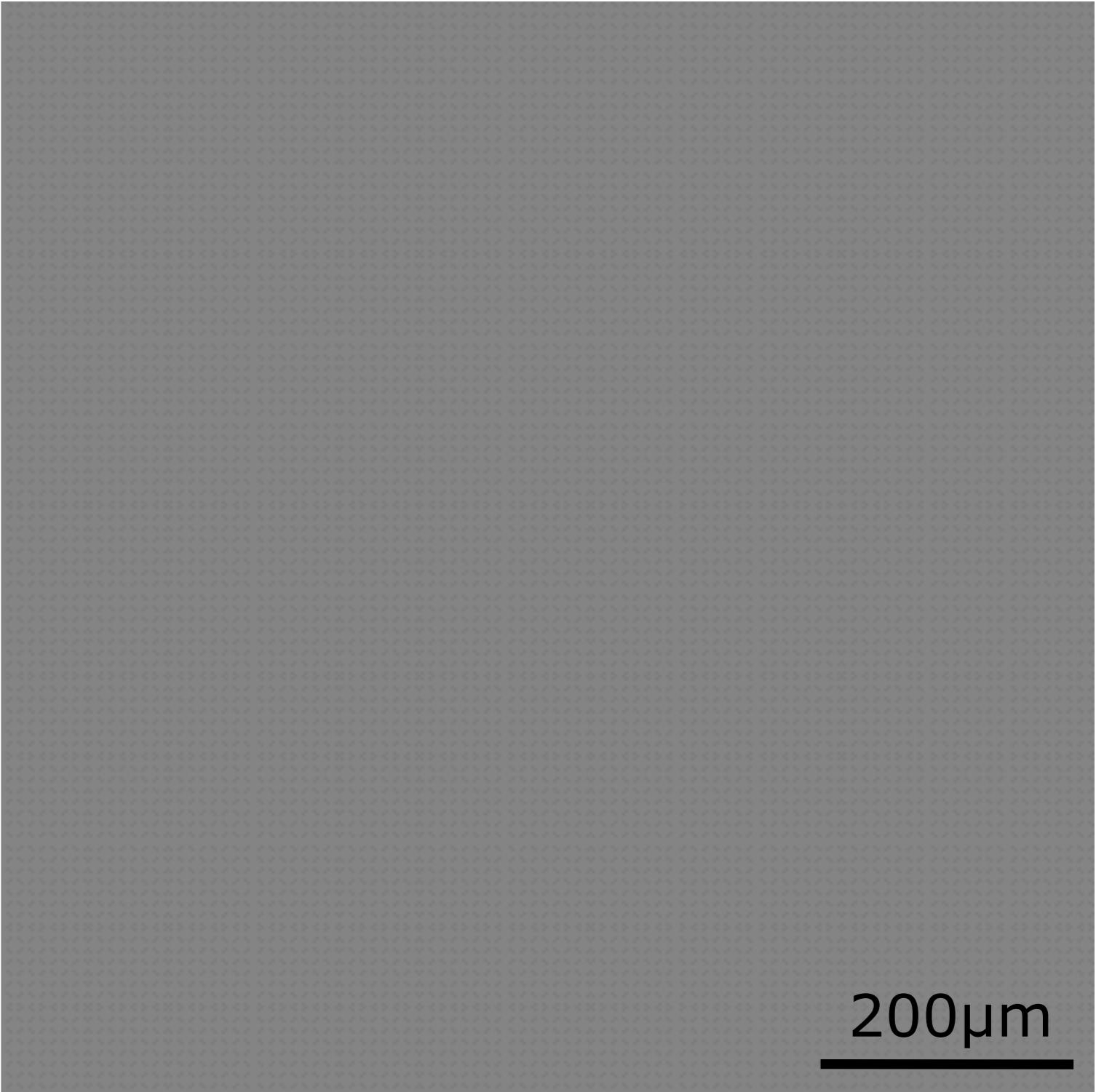
Tomographic Reconstruction

Single slice:

reconstructed from
1250 projections



root of mahogany tree
(W. H. Schröder, FZ Jülich)



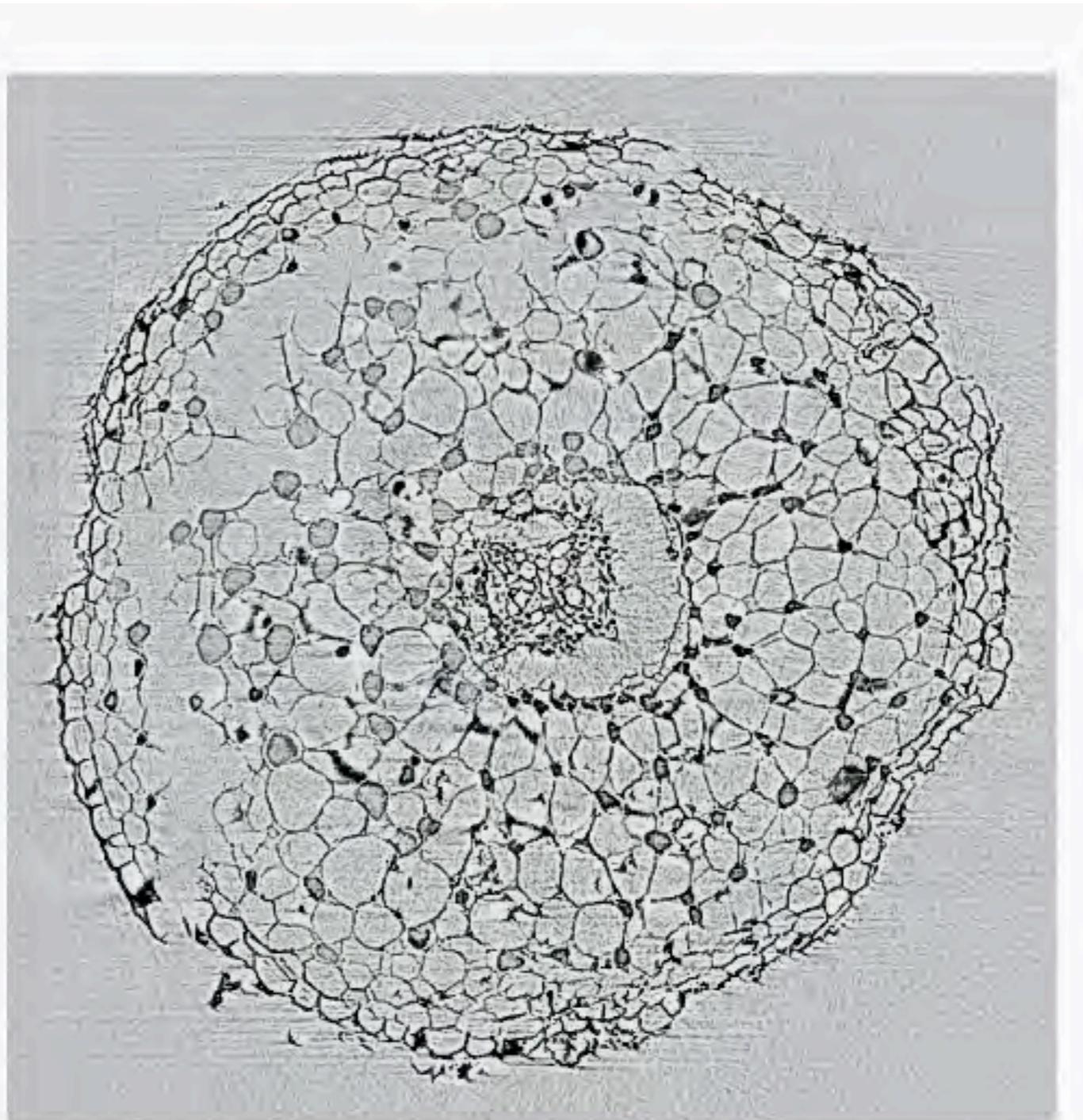
3D Reconstruction

Many slices:

3D structure



root of mahogany tree
(W. H. Schröder, FZ Jülich)



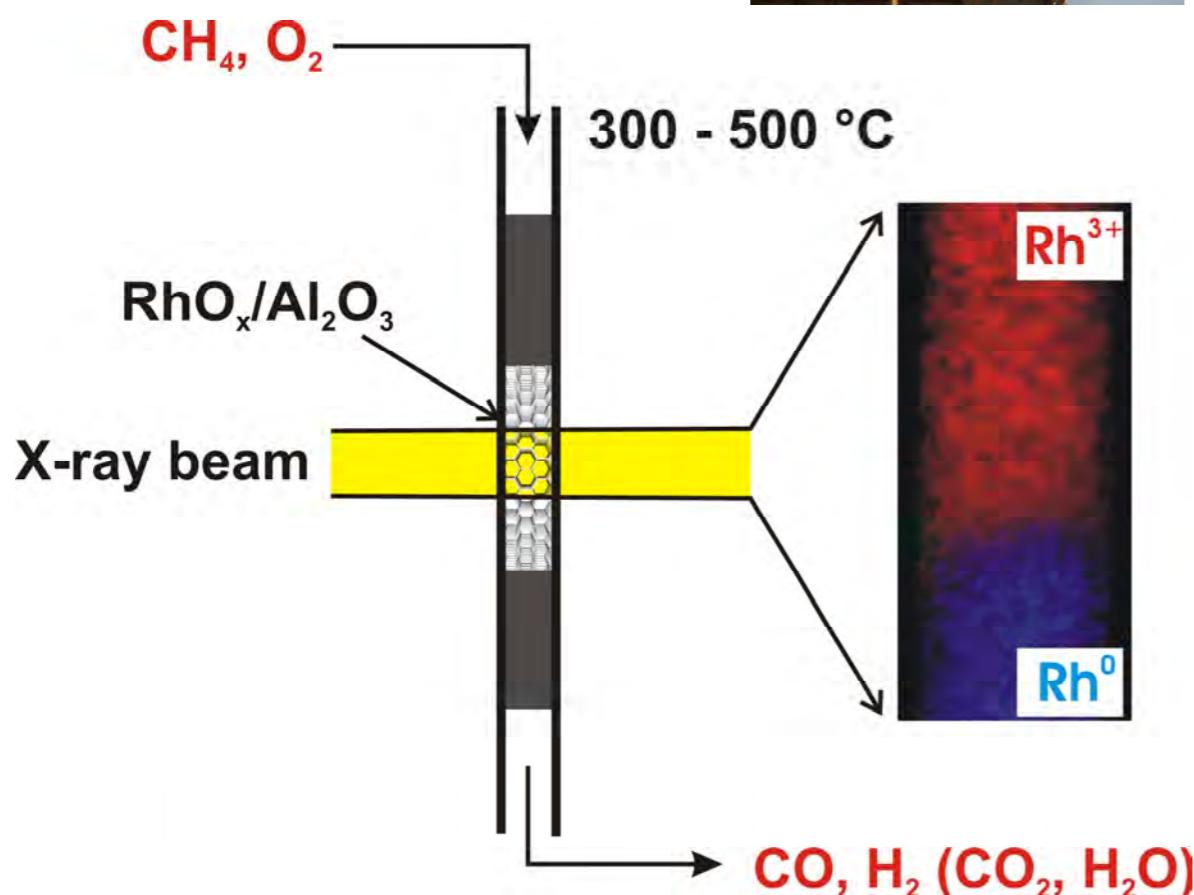
resolution: $\sim 3 \mu\text{m}$

Visualize Catalysts in Action

Methane often wasted during oil production:



First step to convert methane into liquid fuels (syngas production):



Grunwaldt, et al.,
J. Chem. Phys. B **110**, 8674 (2006)

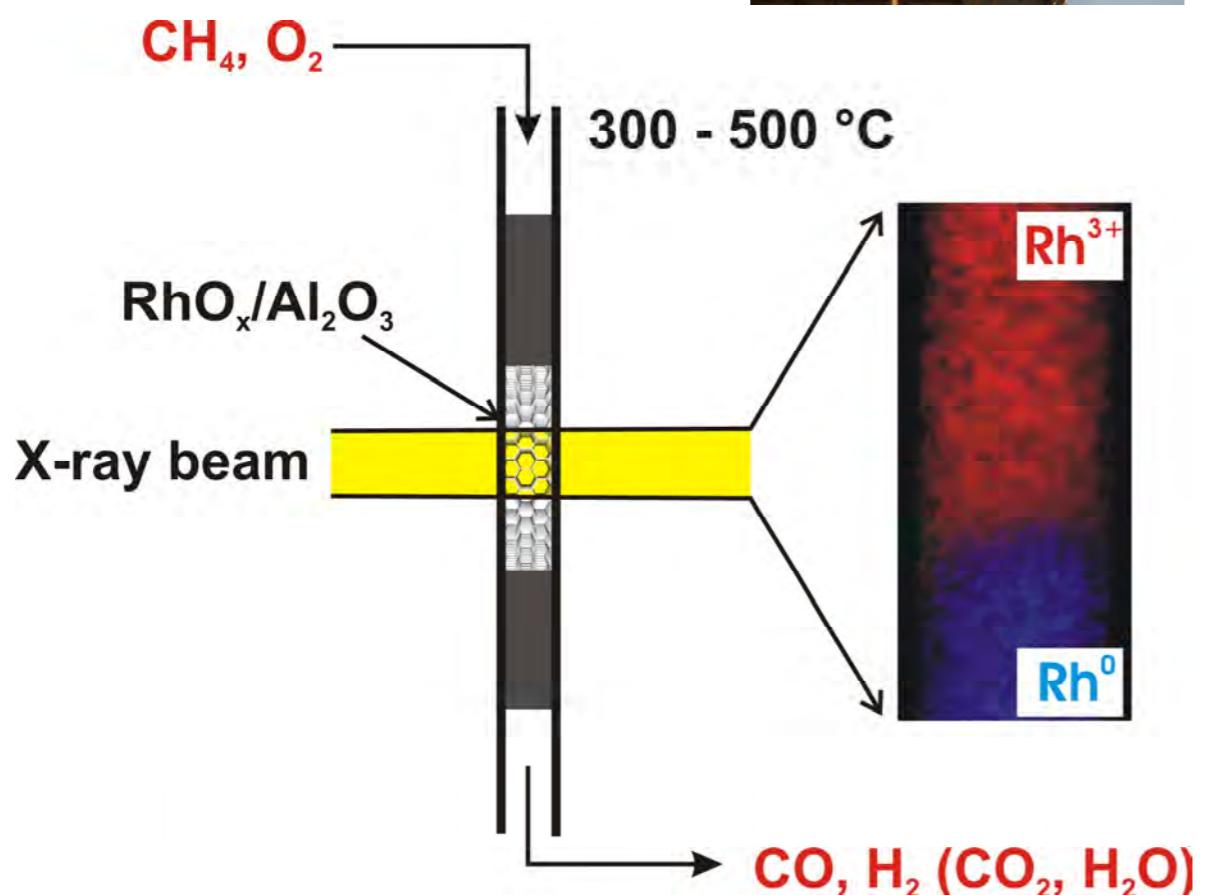


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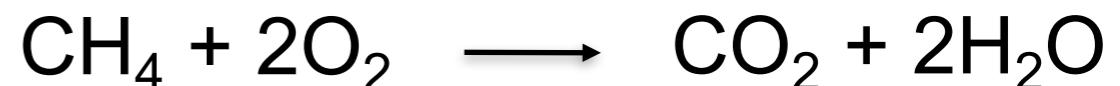


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Grunwaldt, et al.,
J. Chem. Phys. B **110**, 8674 (2006)

Combustion of methane:

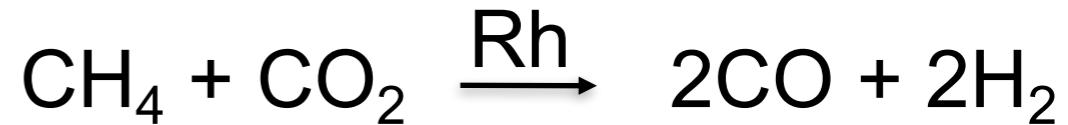


(exothermal: $-801,7\text{ kJ/mol}$)

reforming of methane to H_2 :

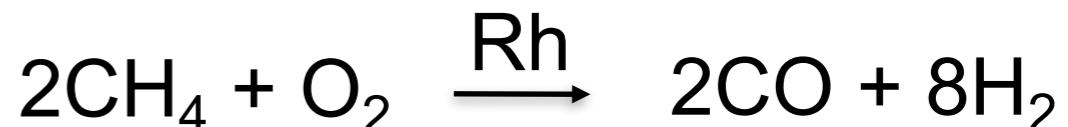


(endothermal: 206.1 kJ/mol)



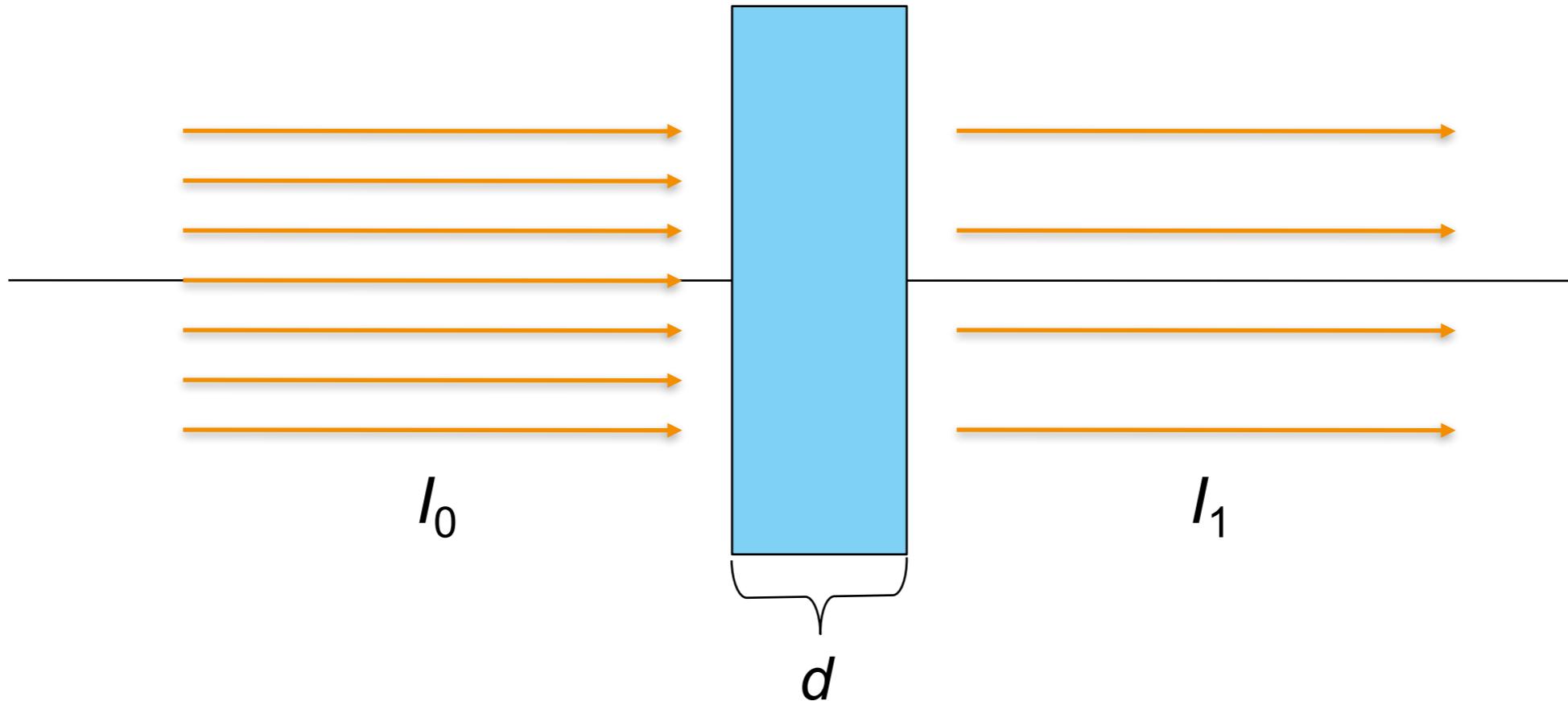
(endothermal: $247,5\text{ kJ/mol}$)

potentially other reaction:
direct partial oxidation:



(exothermal: $-35,5\text{ kJ/mol}$)

X-Ray Absorption: Lambert-Beer Law

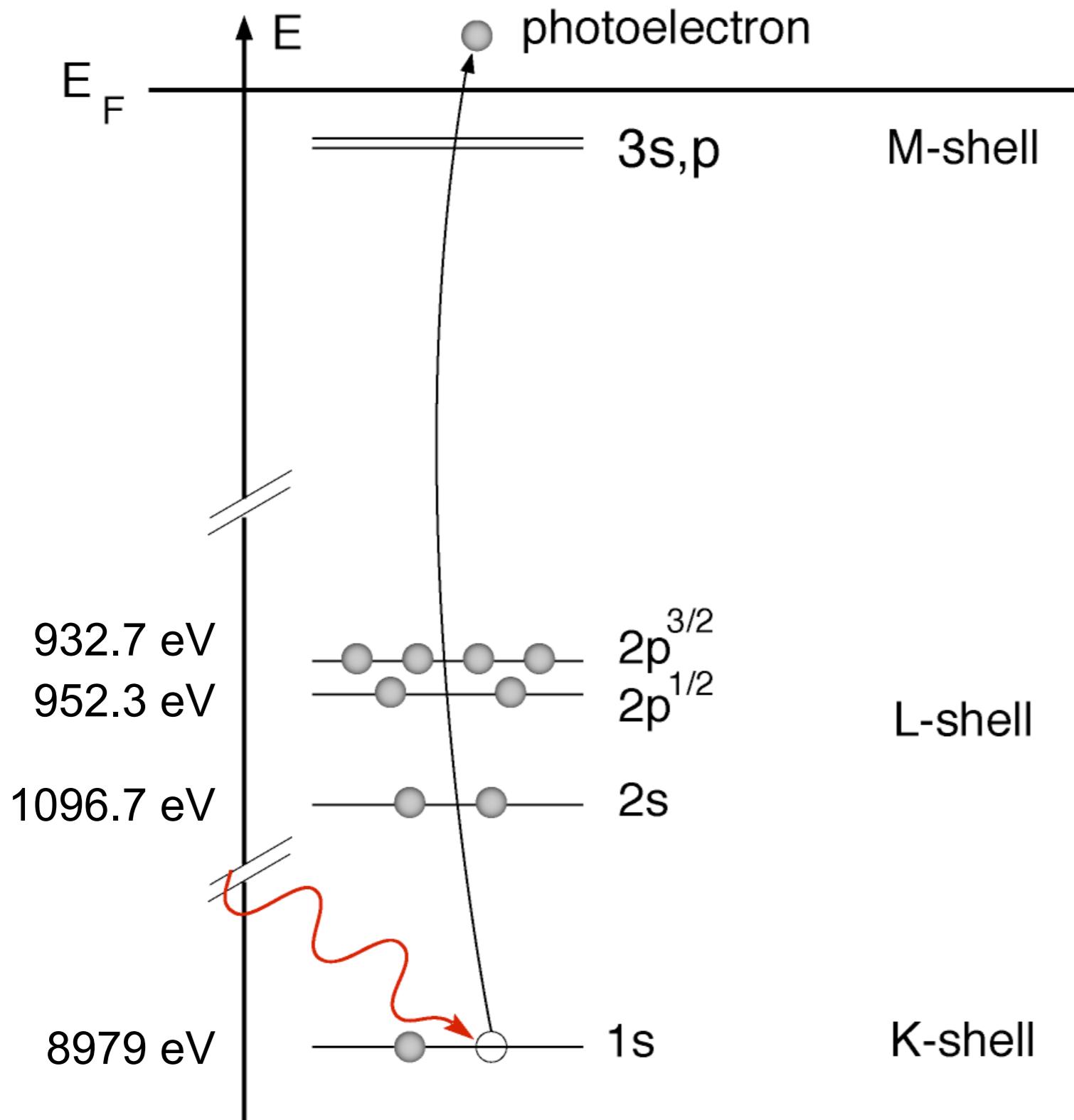


$$I_1(E) = I_0(E) \cdot \exp [-\mu(E)d]$$

$\mu(E)$: linear attenuation coefficient

$$\mu(E) \cdot d = \ln \left(\frac{I_0}{I_1} \right)$$

Photo Absorption



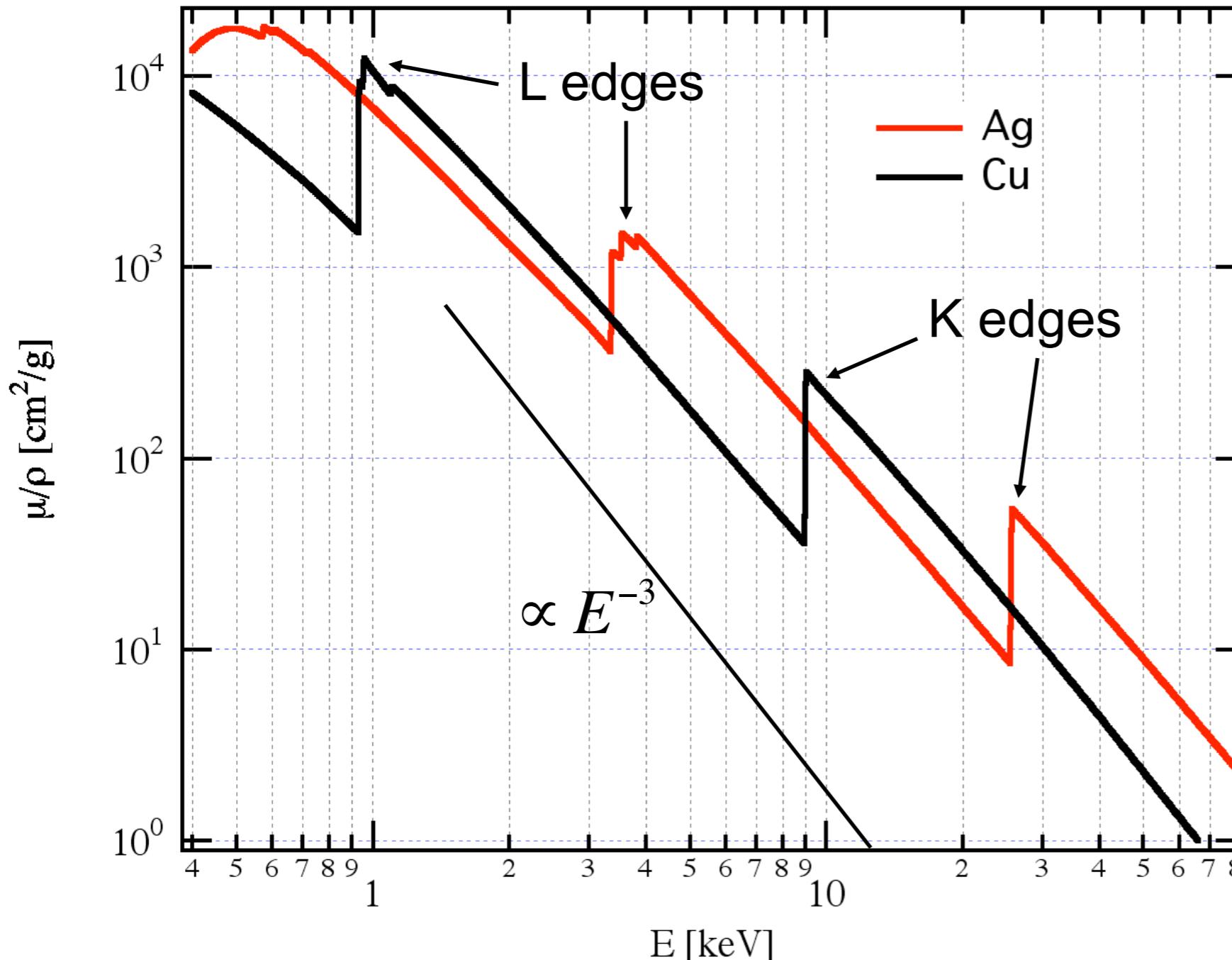
- > electrons populate specific atomic states: binding energies are atom specific: K, L, M
- > atom can absorb x-ray photon if:

$$E_{\text{photon}} > E_{\text{ionization}}$$

(follows from Pauli principle)

Example: Absorption in Cu & Ag

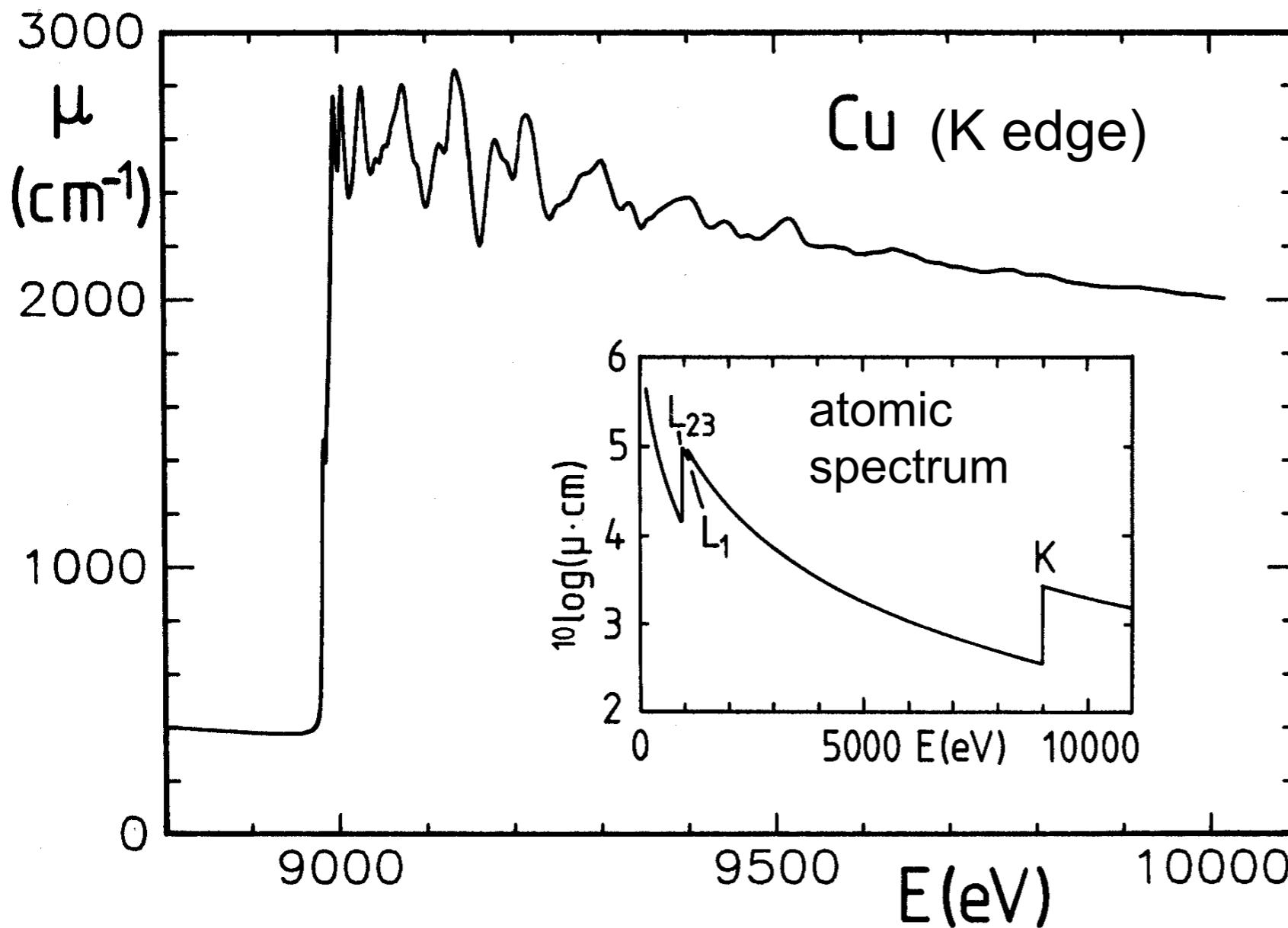
$\mu(E)$: linear attenuation coefficient



- > mainly atomic effect
- > strong dependence on x-ray energy:
 $\propto E^{-2.78}$
- > strong dependence on atomic number:
 $\propto Z^{2.7}$
- > largest contribution from inner shells

Example: Absorption in Cu

$\mu(E)$: linear attenuation coefficient

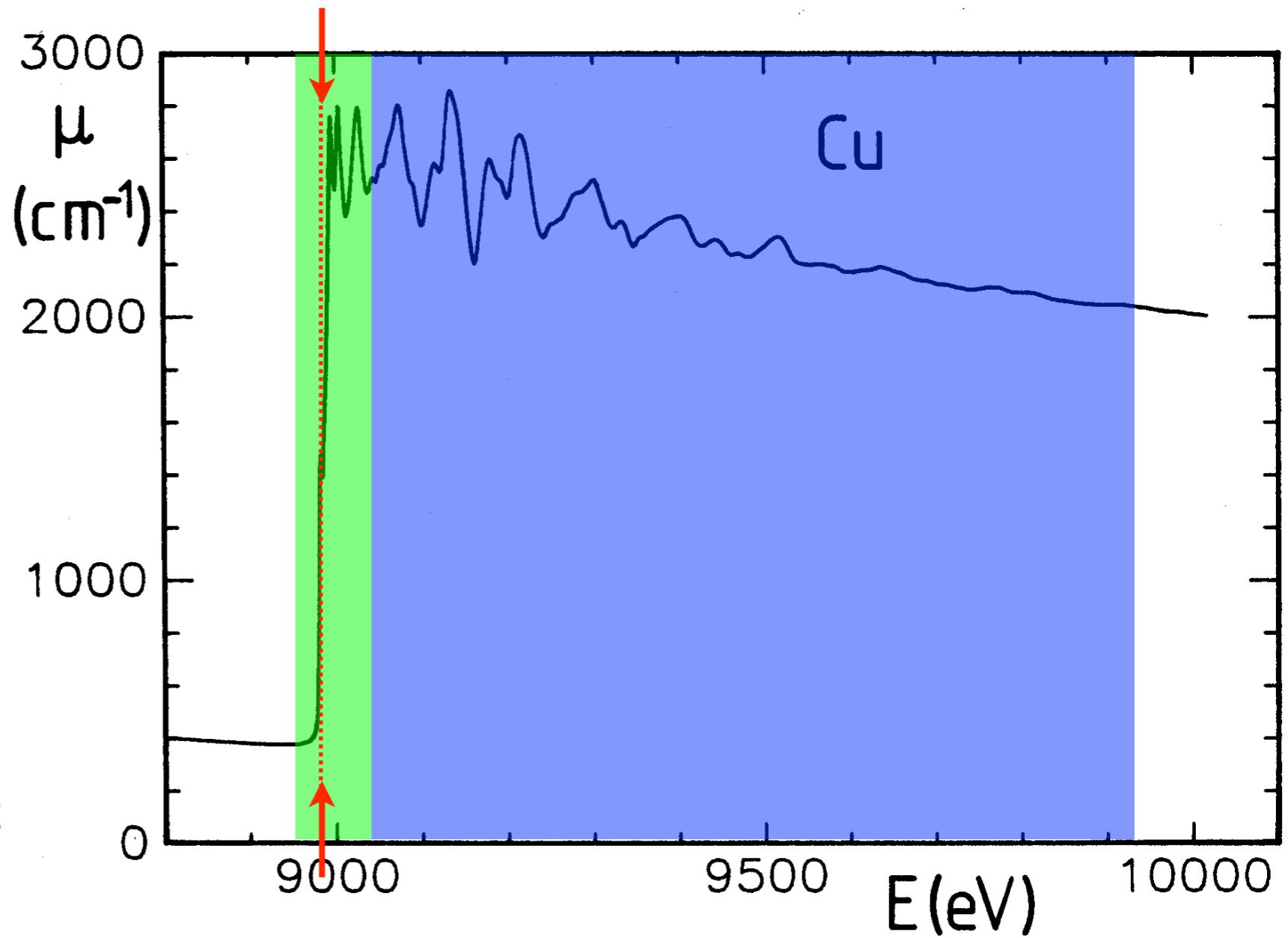


Metallic Cu:
mainly atomic effect
fine structure in solid:
[X-ray Absorption](#)
[Fine Structure](#)

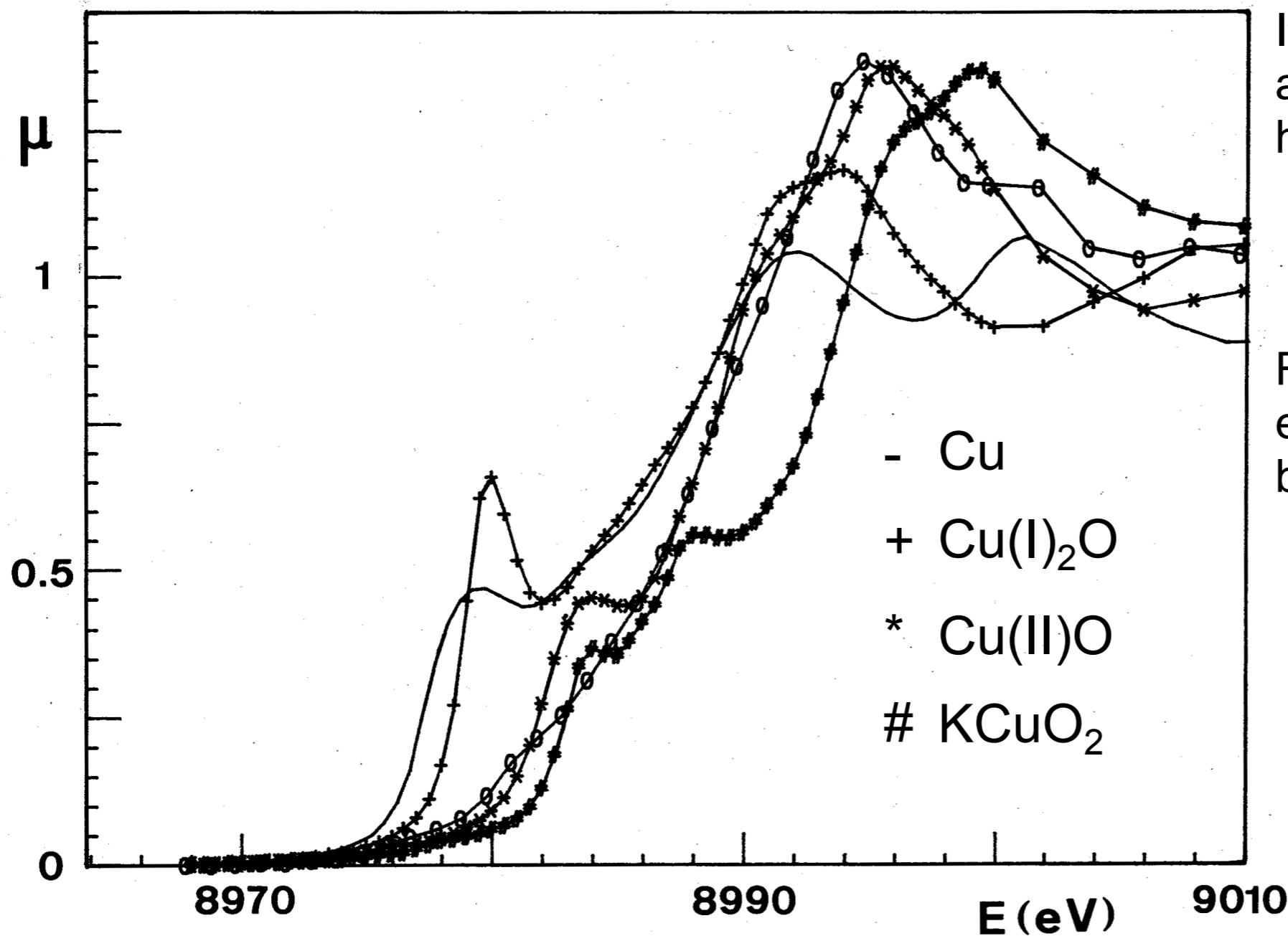
X-ray Absorption Spectrum

Three characteristic features:

- > Energy of absorption edge: oxidation state
- > Near-edge region: (XANES: x-ray absorption near edge structure) local, projected density of states
- > Extended fine structure: (EXAFS: extended x-ray absorption fine structure) local chemical environment of atomic species



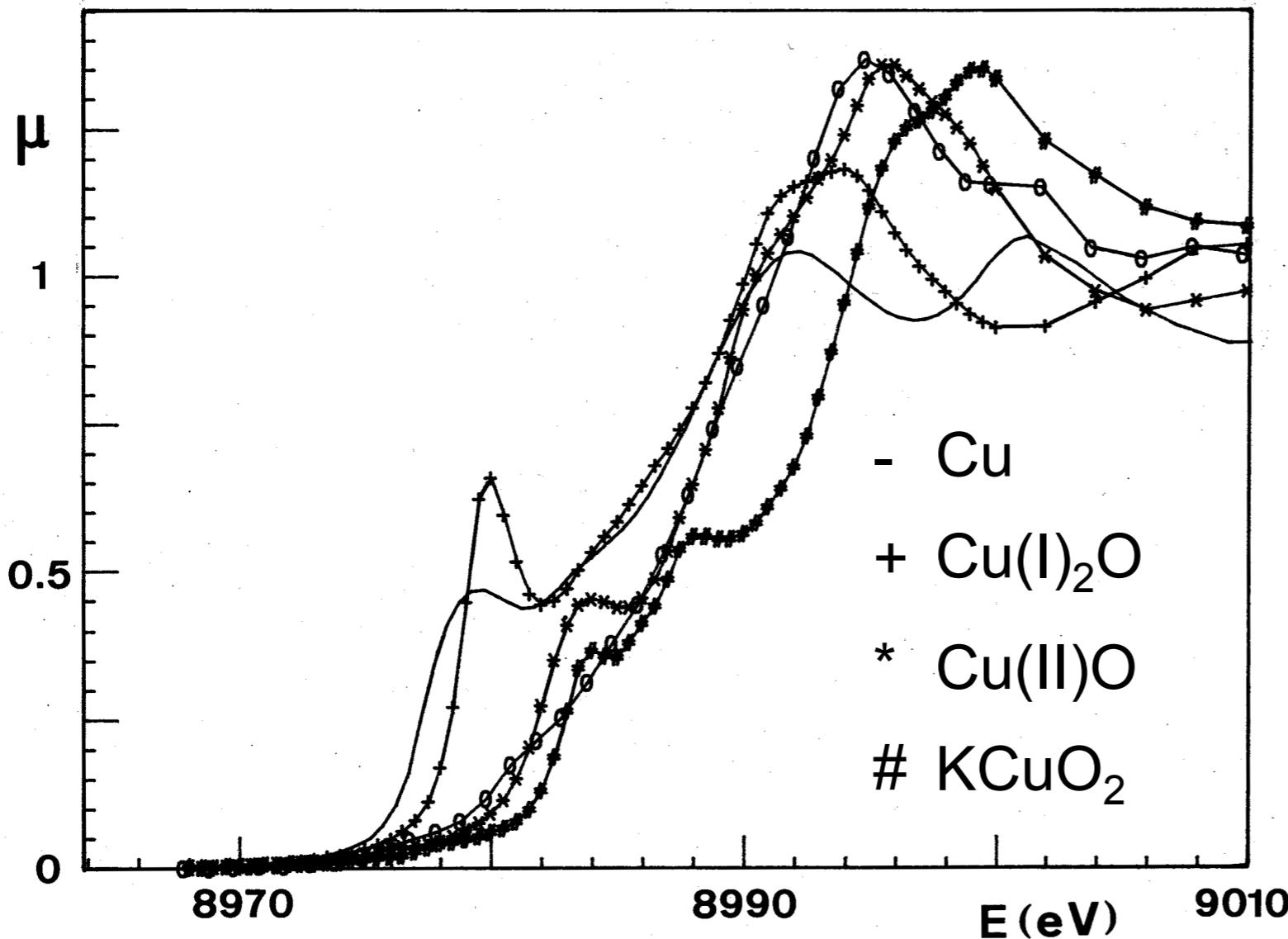
Energy of Absorption Edge



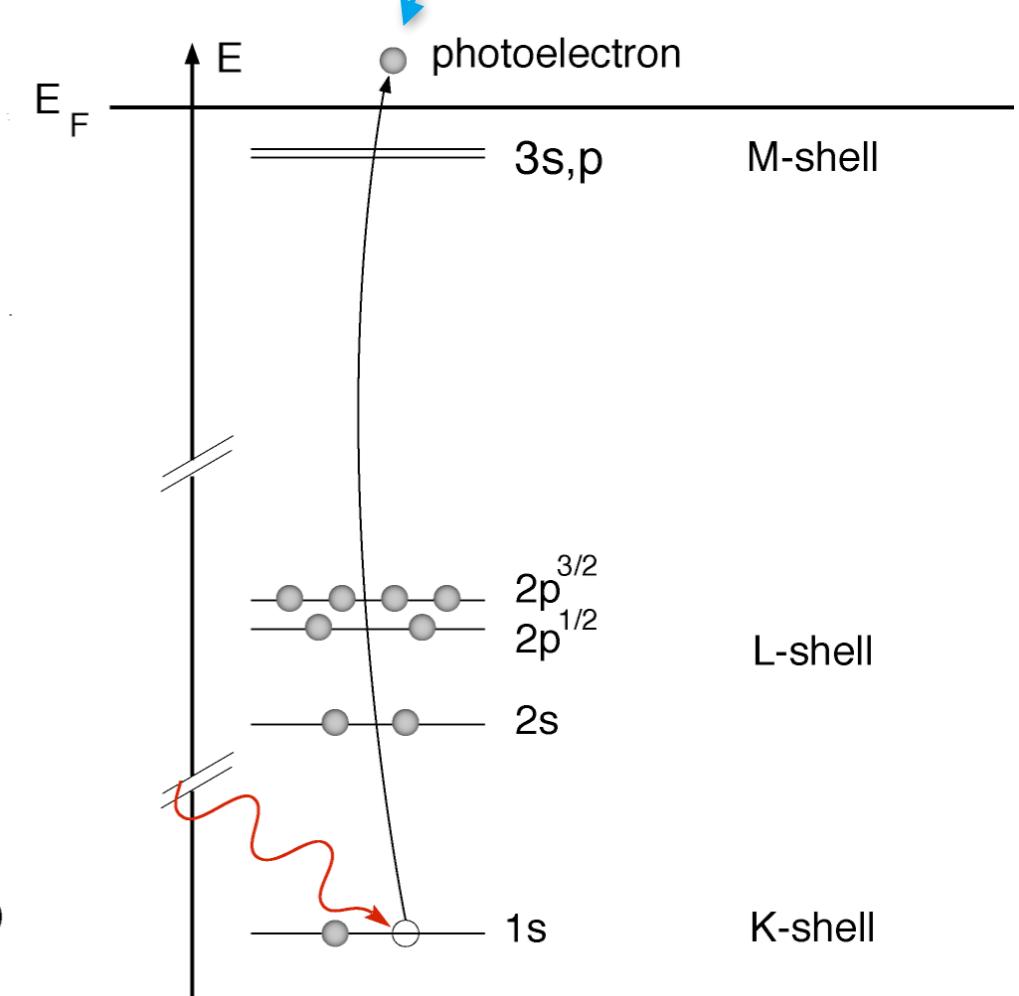
Increasing oxidation state:
absorption edge shifts to
higher x-ray energies

Reduced screening of
electric field of nucleus
by valence electrons:
other electrons more
tightly bound!

Shape of Near-Edge Spectrum



depends on density of states available to photoelectron



Shape of spectrum:

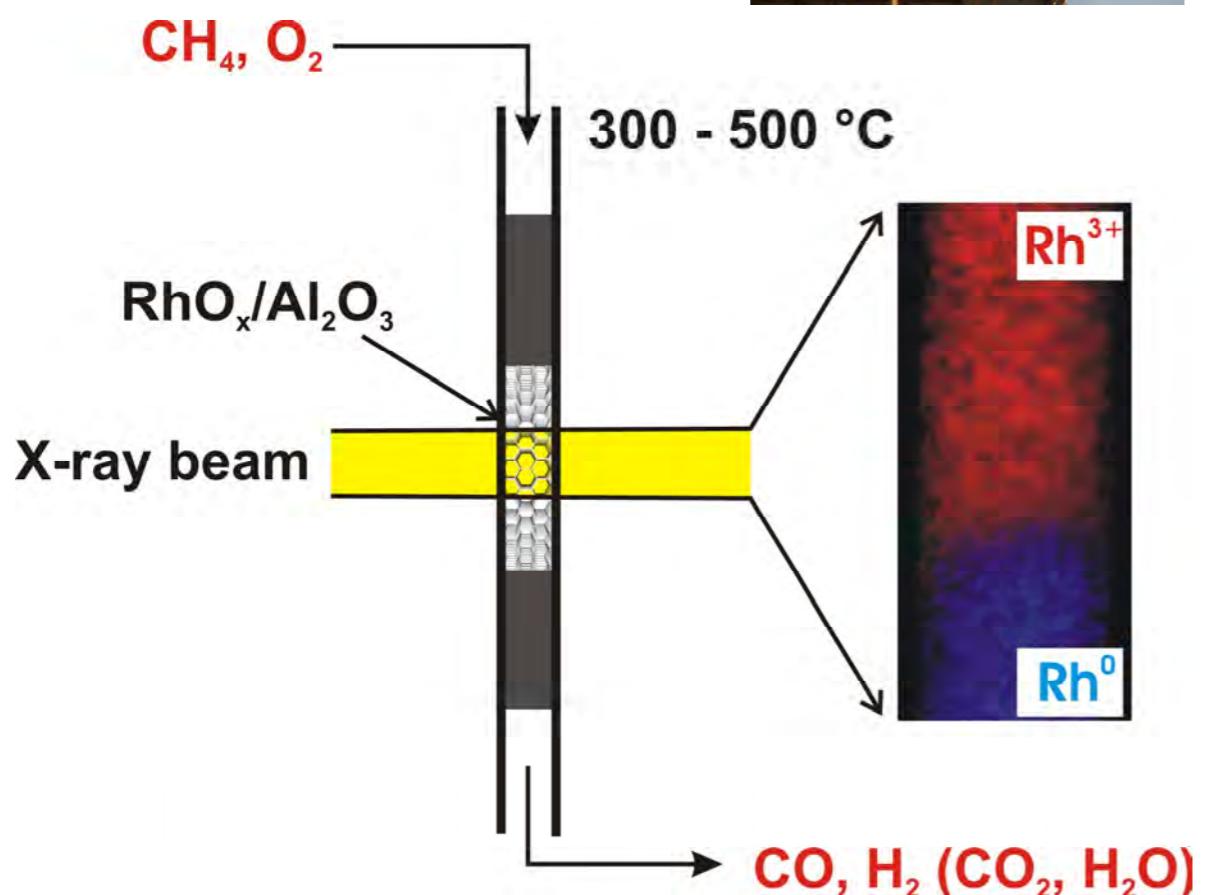
- > can be modeled by methods in theoretical solid state physics
- > can be used as „fingerprint“ to identify a given chemical environment

Visualize Catalysts in Action

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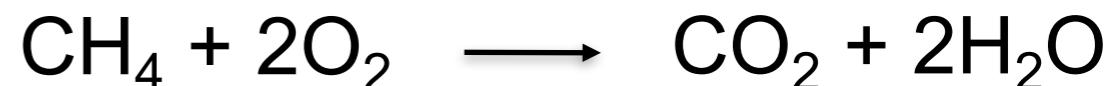


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Grunwaldt, et al.,
J. Chem. Phys. B **110**, 8674 (2006)

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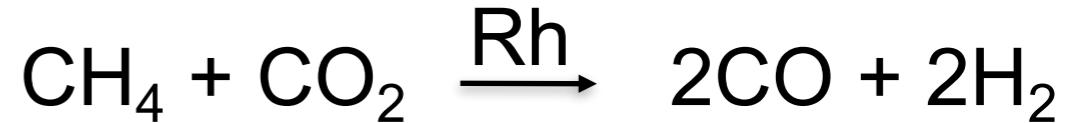


(exothermal: -801,7 kJ/mol)

reforming of methane to H₂:

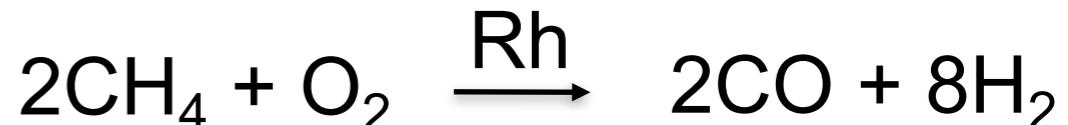


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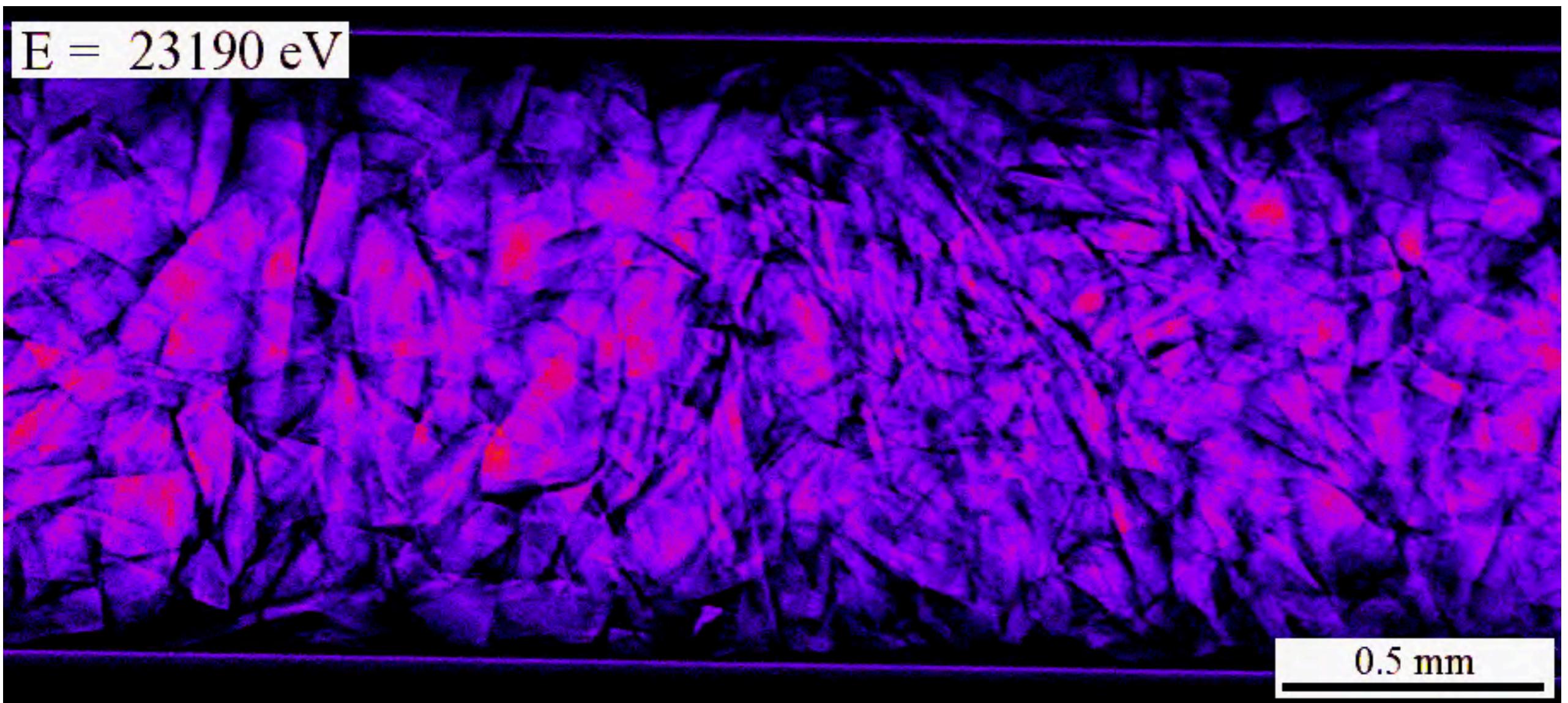
potentially other reaction:
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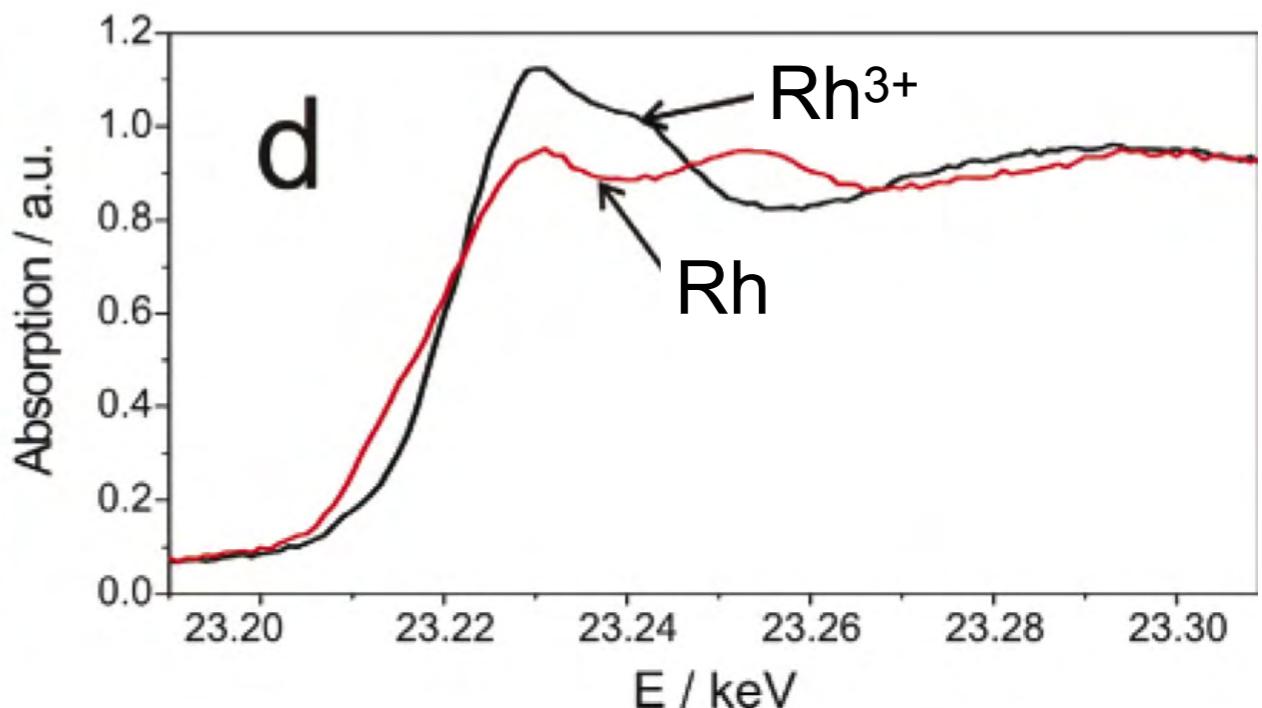
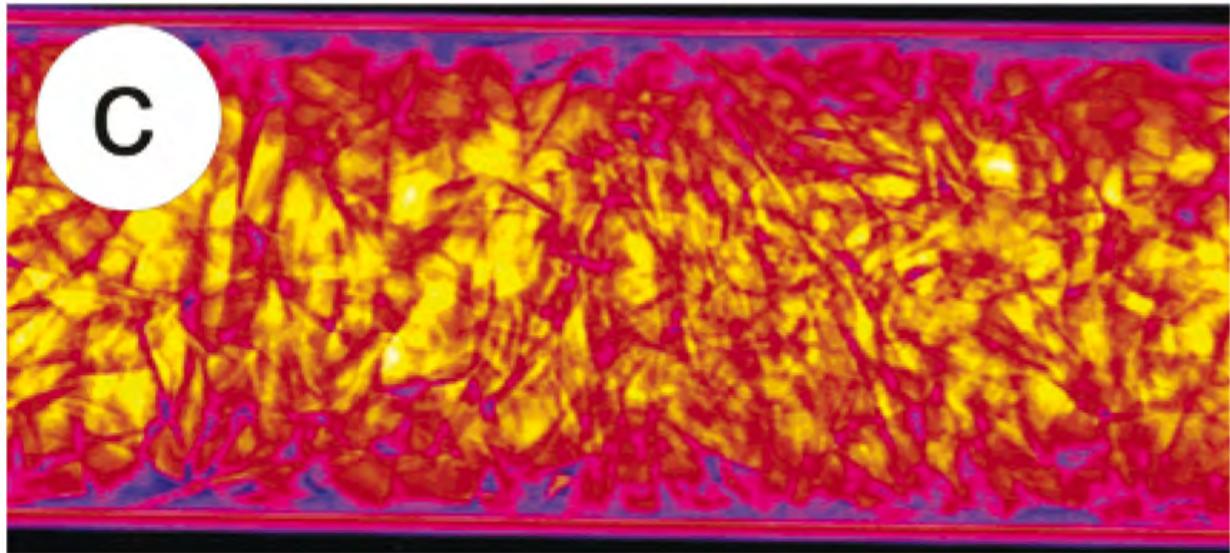
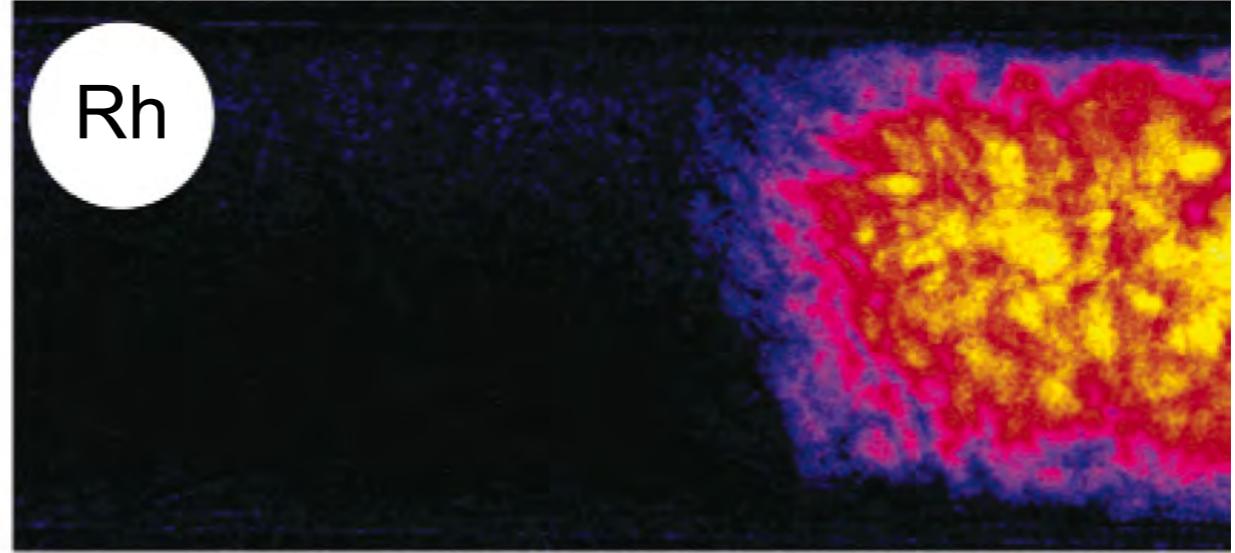
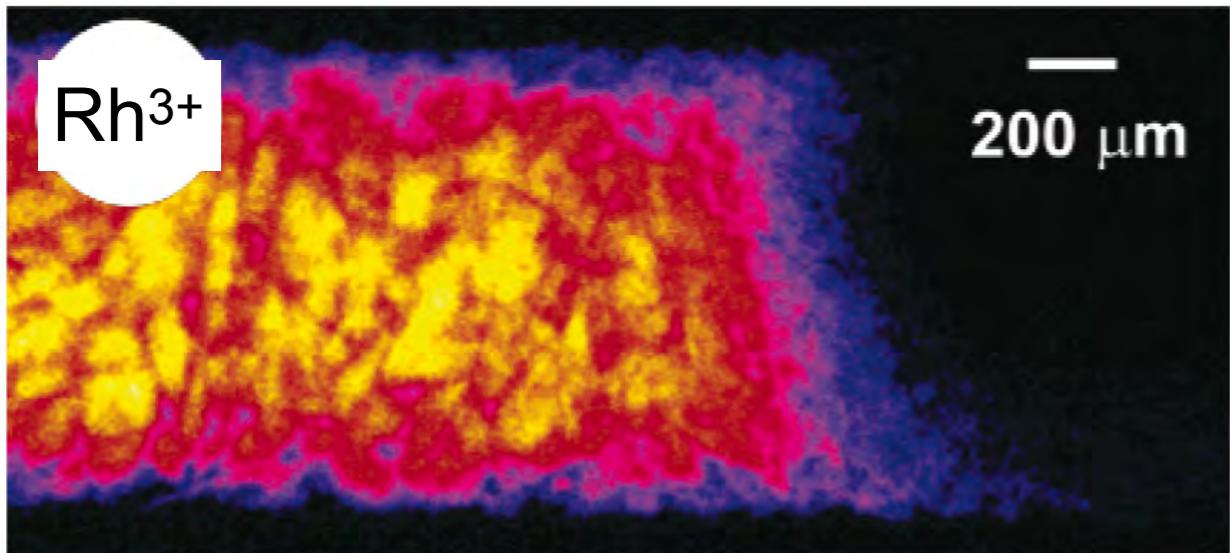
Visualize Catalysis

In-situ transmission imaging of catalyst bed inside chemical reactor



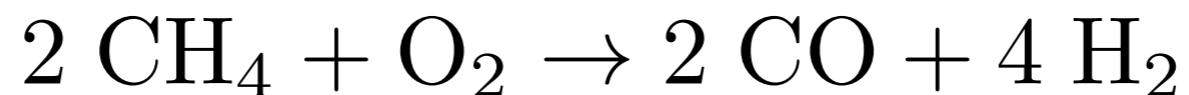
Grunwaldt, et al.,
J. Chem. Phys. B **110**, 8674 (2006)

Visualize Catalysis

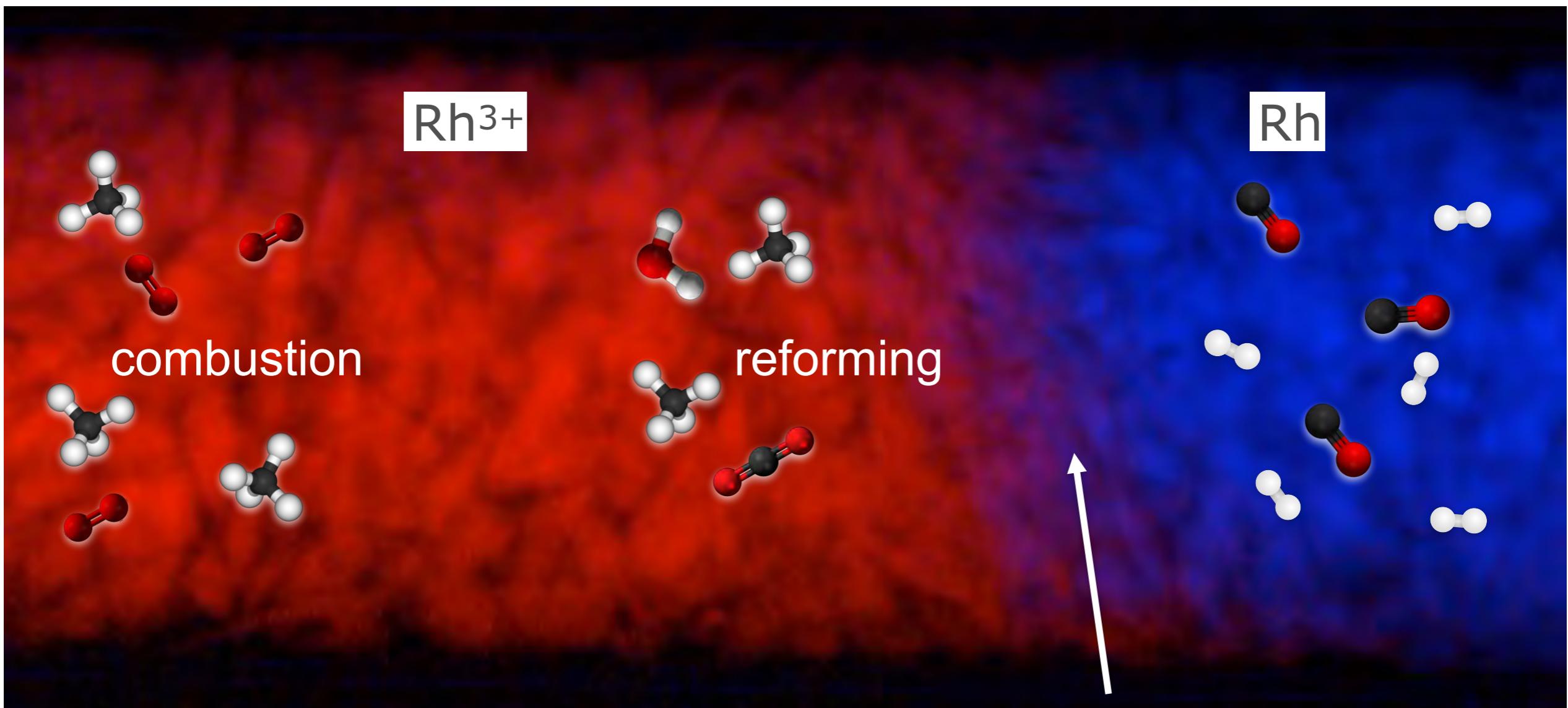


Grunwaldt, et al.,
J. Chem. Phys. B **110**, 8674 (2006)

Visualize Catalysis



direction of flow
→

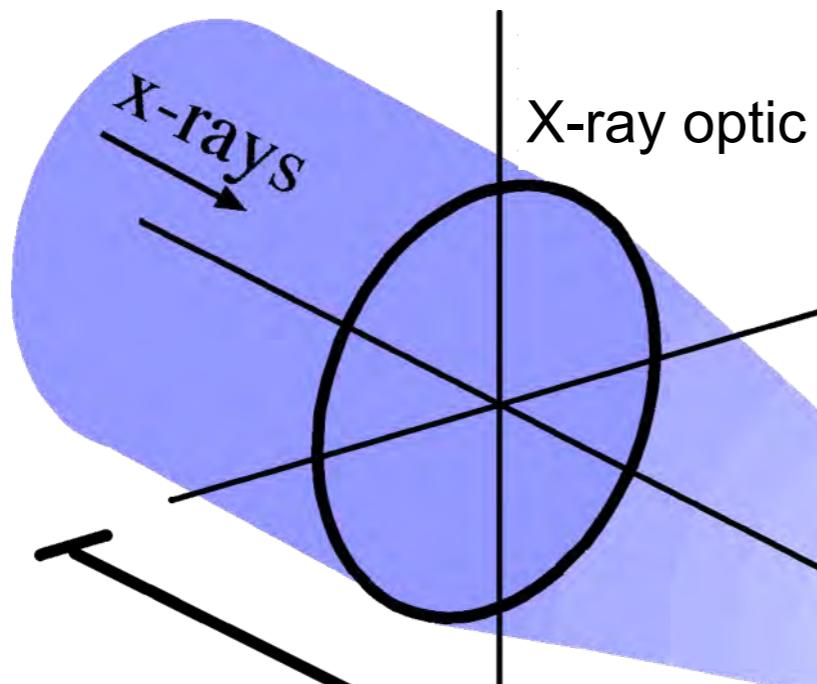


Grunwaldt, et al.,
J. Chem. Phys. B **110**, 8674 (2006)

production of hydrogen
Rh is reduced!

Scanning Microscopy and Tomography: Nanoprobe

X rays are focused onto the sample

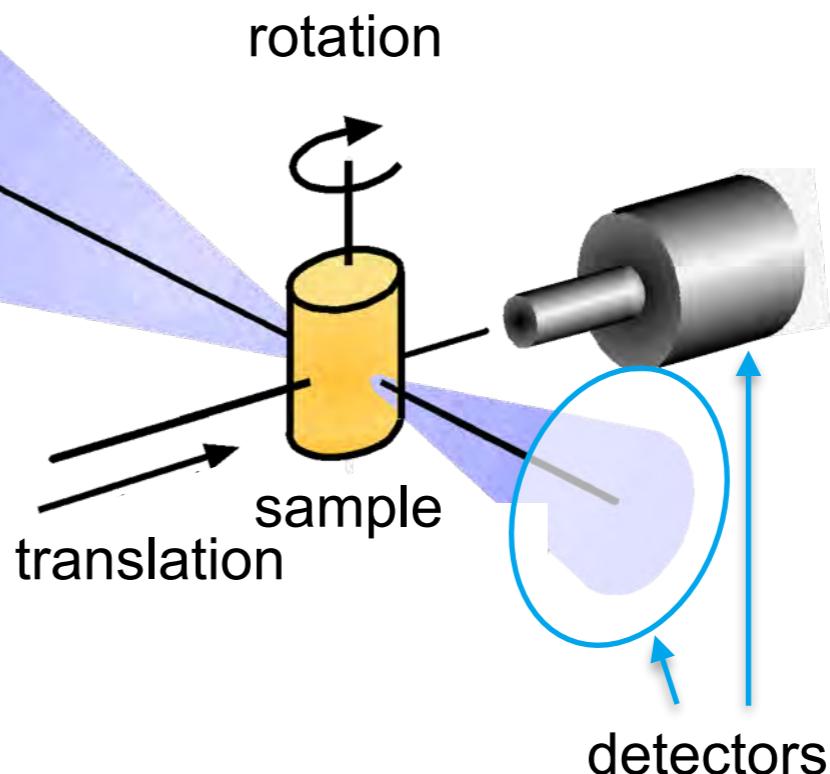


different contrast mechanisms:

- > x-ray fluorescence (XRF)
- > x-ray absorption (XAS)
- > x-ray diffraction (XRD, SAXS, WAXS)
- > maybe in future even IXS (RIXS)
- > ...

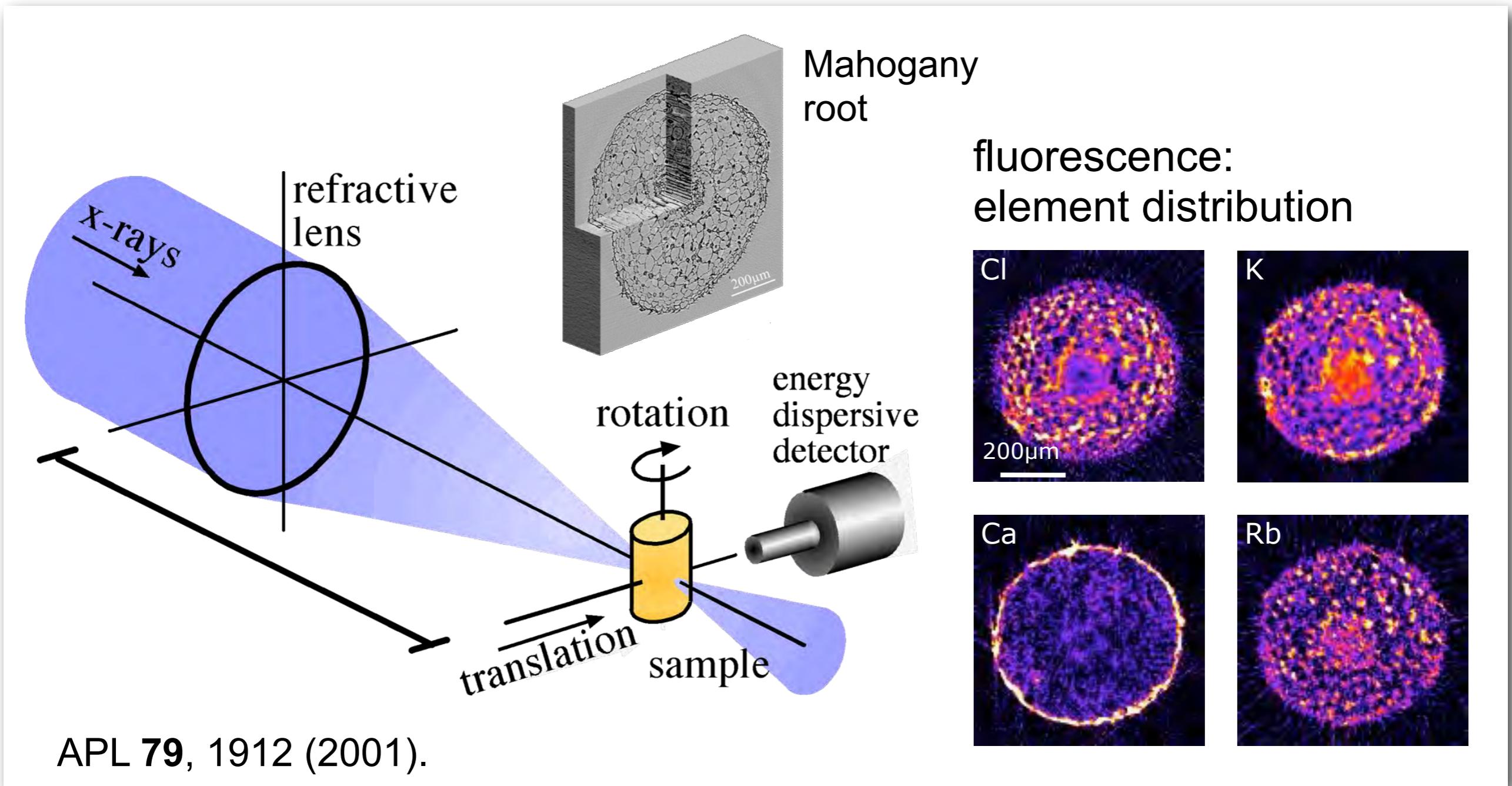
raster scan sample through beam:

- get x-ray analytical information locally and on nanoscale (resolution limited by focus size).



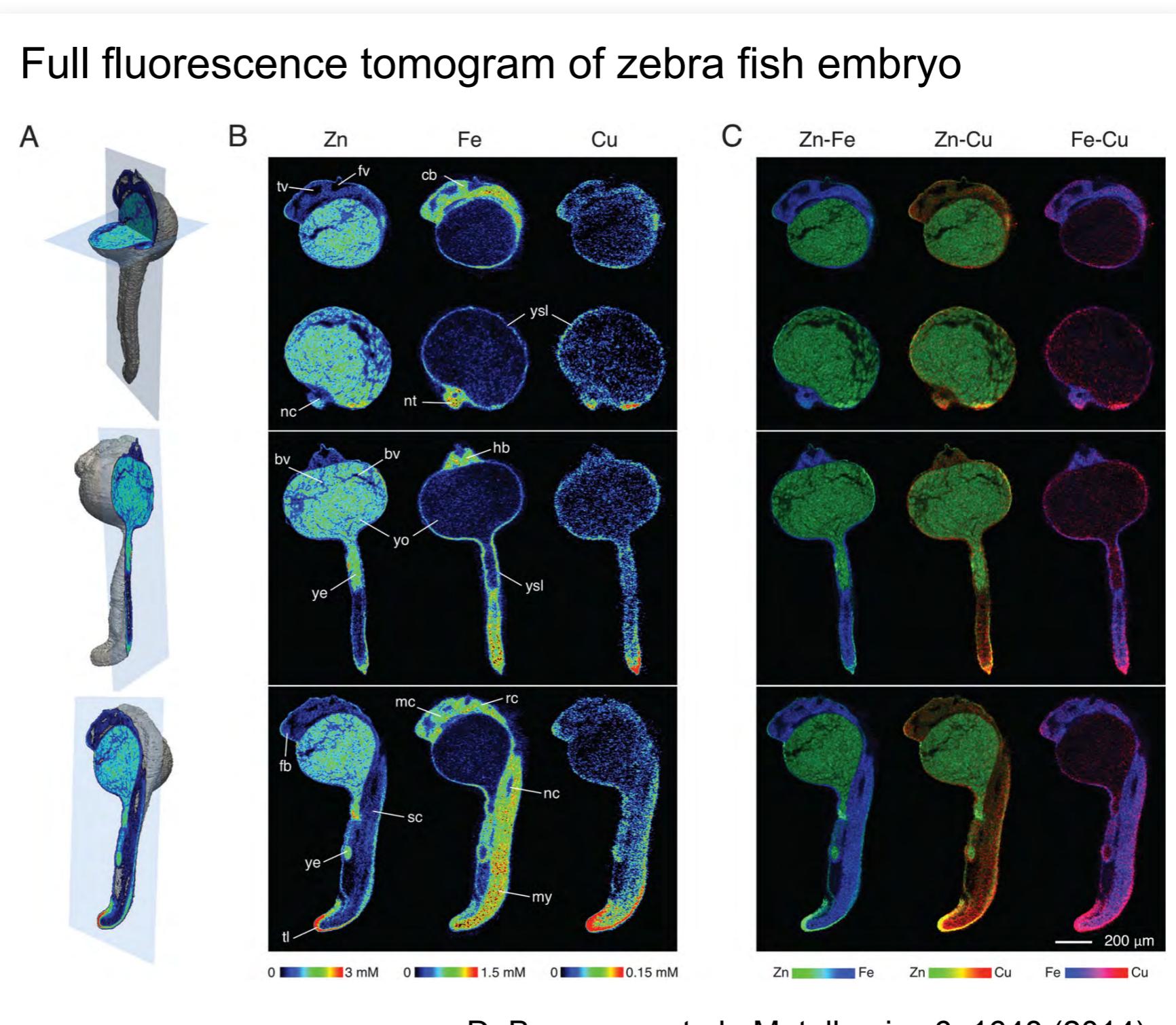
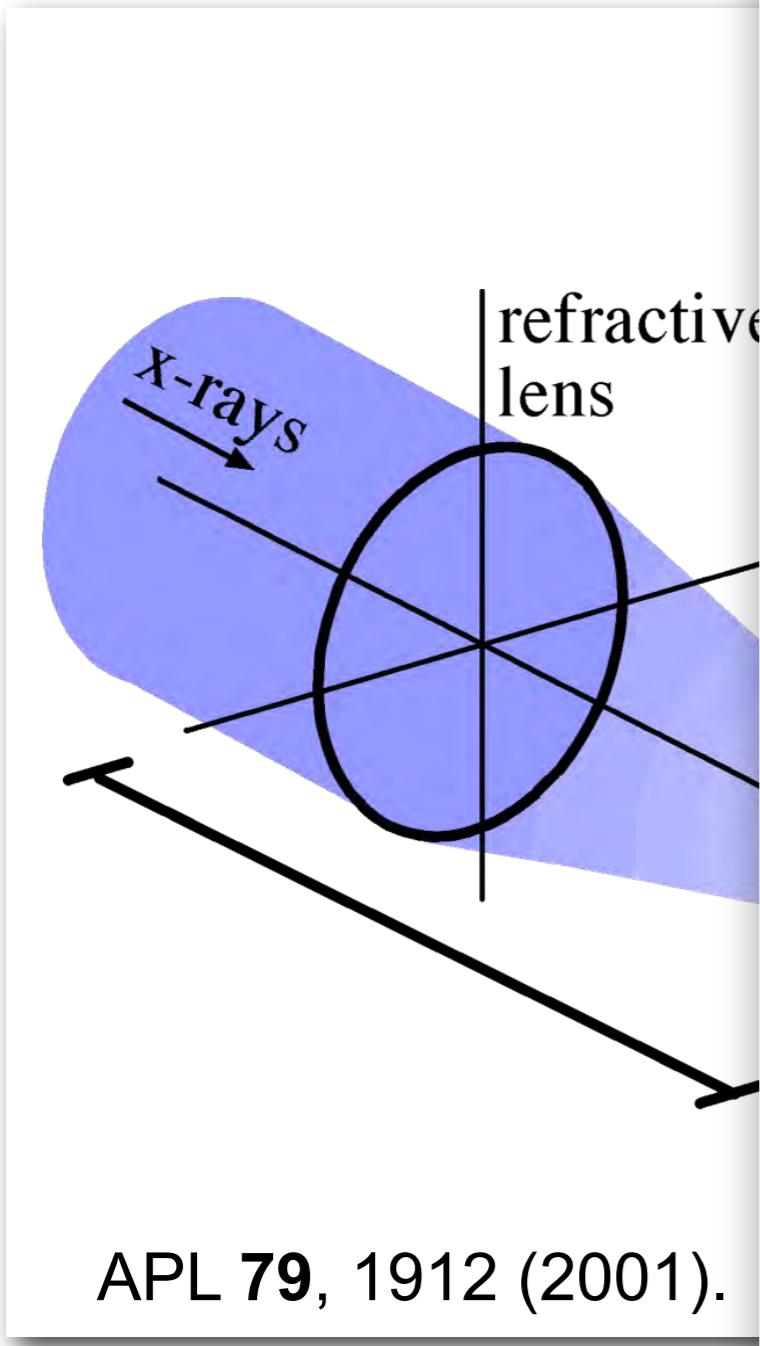
X-Ray Scanning Microscopy and Tomography

>Fluorescence microtomography



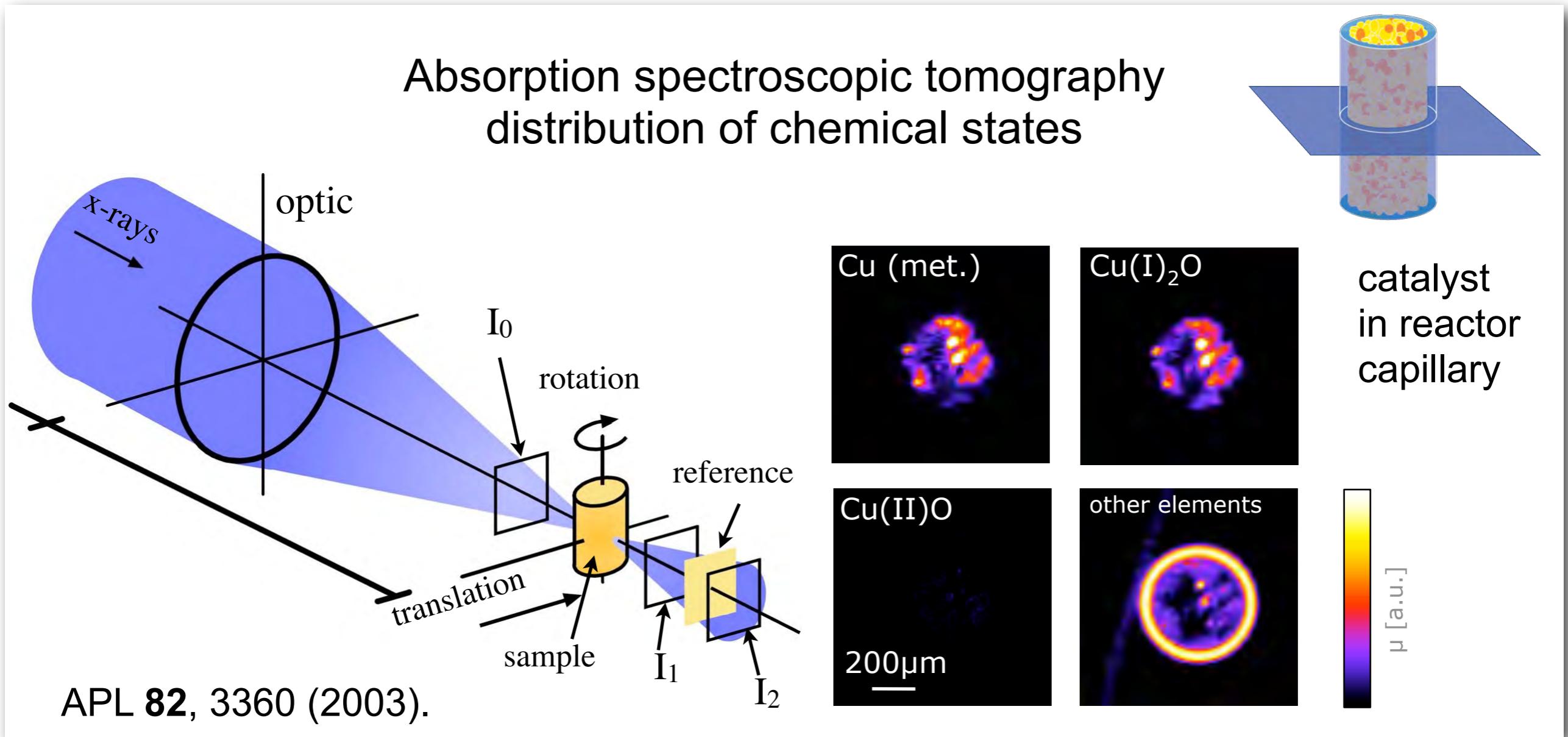
X-Ray Scanning Microscopy and Tomography

>Fluorescence microscopy



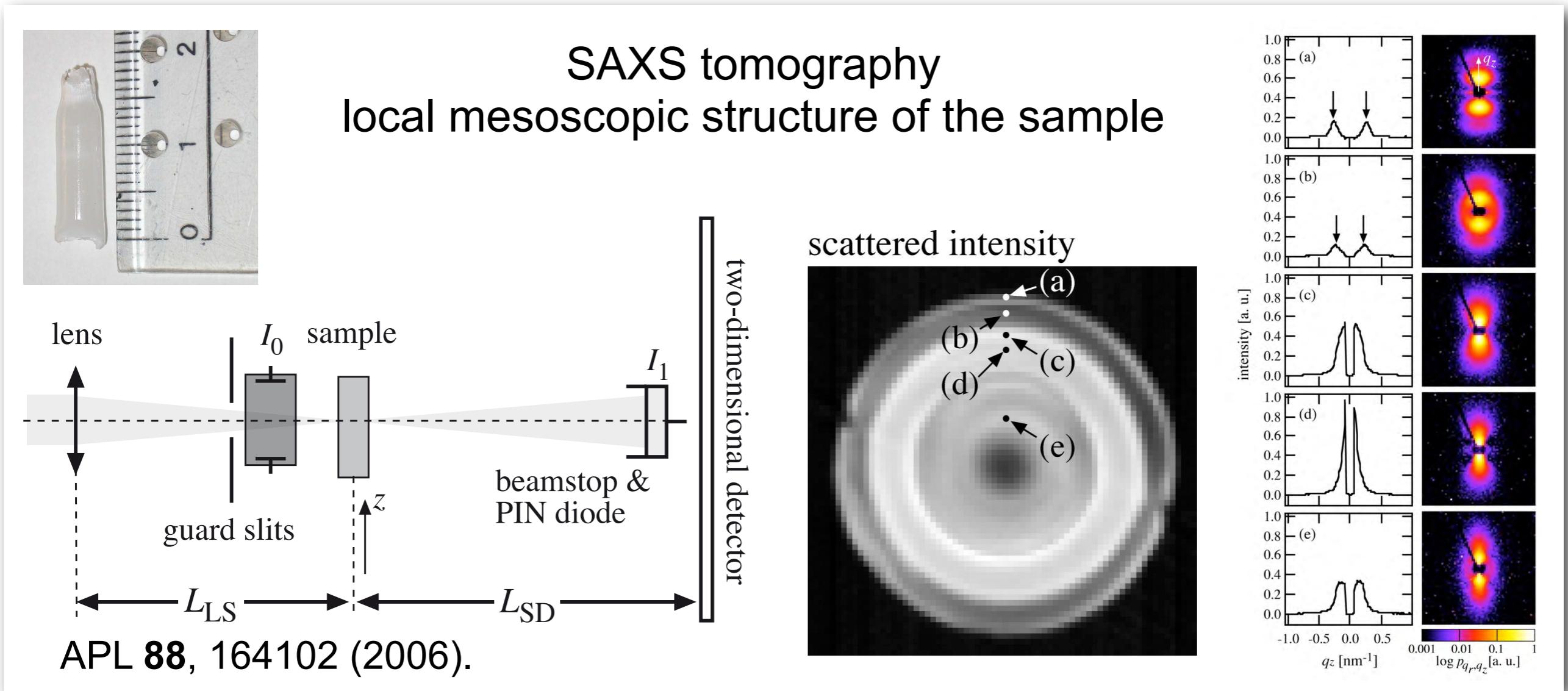
X-Ray Scanning Microscopy and Tomography

- › Fluorescence microtomography
- › Tomographic absorption spectroscopy (XANES tomography)



X-Ray Scanning Microscopy and Tomography

- › Fluorescence microtomography
- › Tomographic absorption spectroscopy (XANES tomography)
- › Small-angle x-ray scattering tomography (SAXS tomography)



X-Ray Scanning Microscopy and Tomography

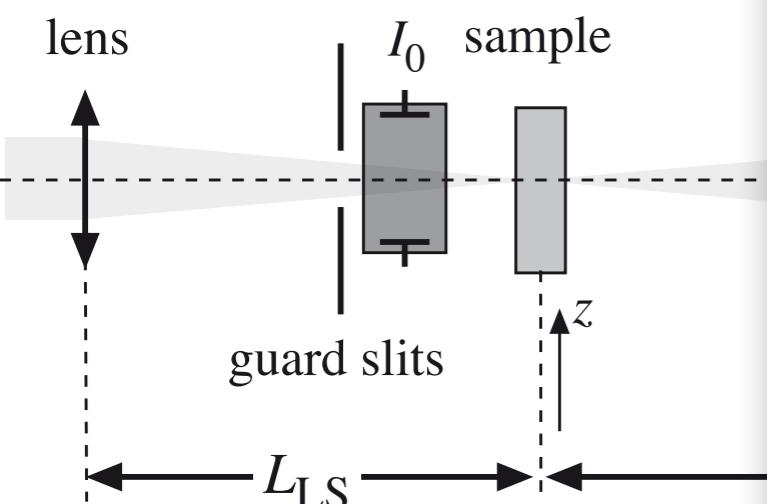
› Fluorescence microtomography

› Tomographic absorption

› Small-angle x-ray scattering

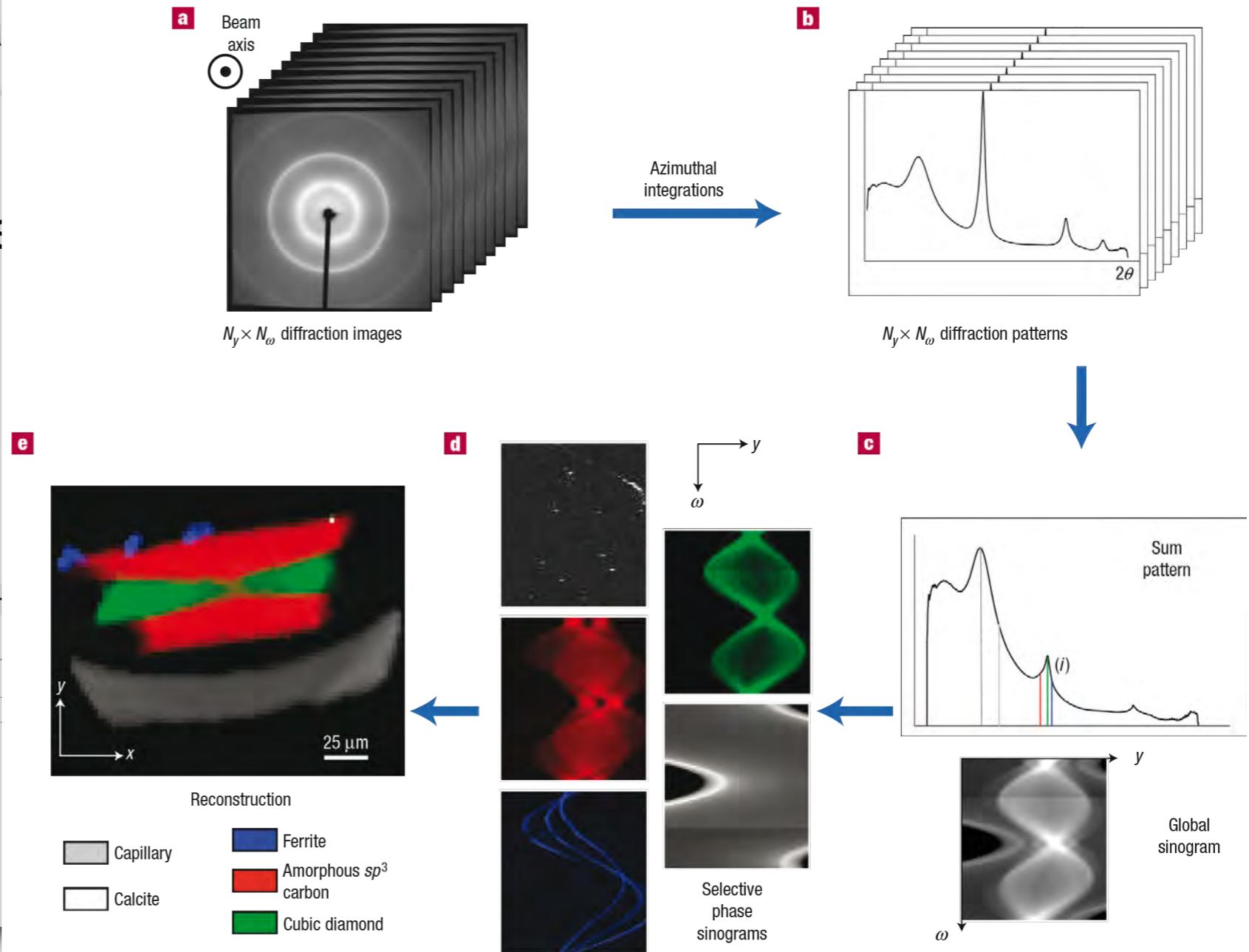


local me



APL 88, 164102 (2006).

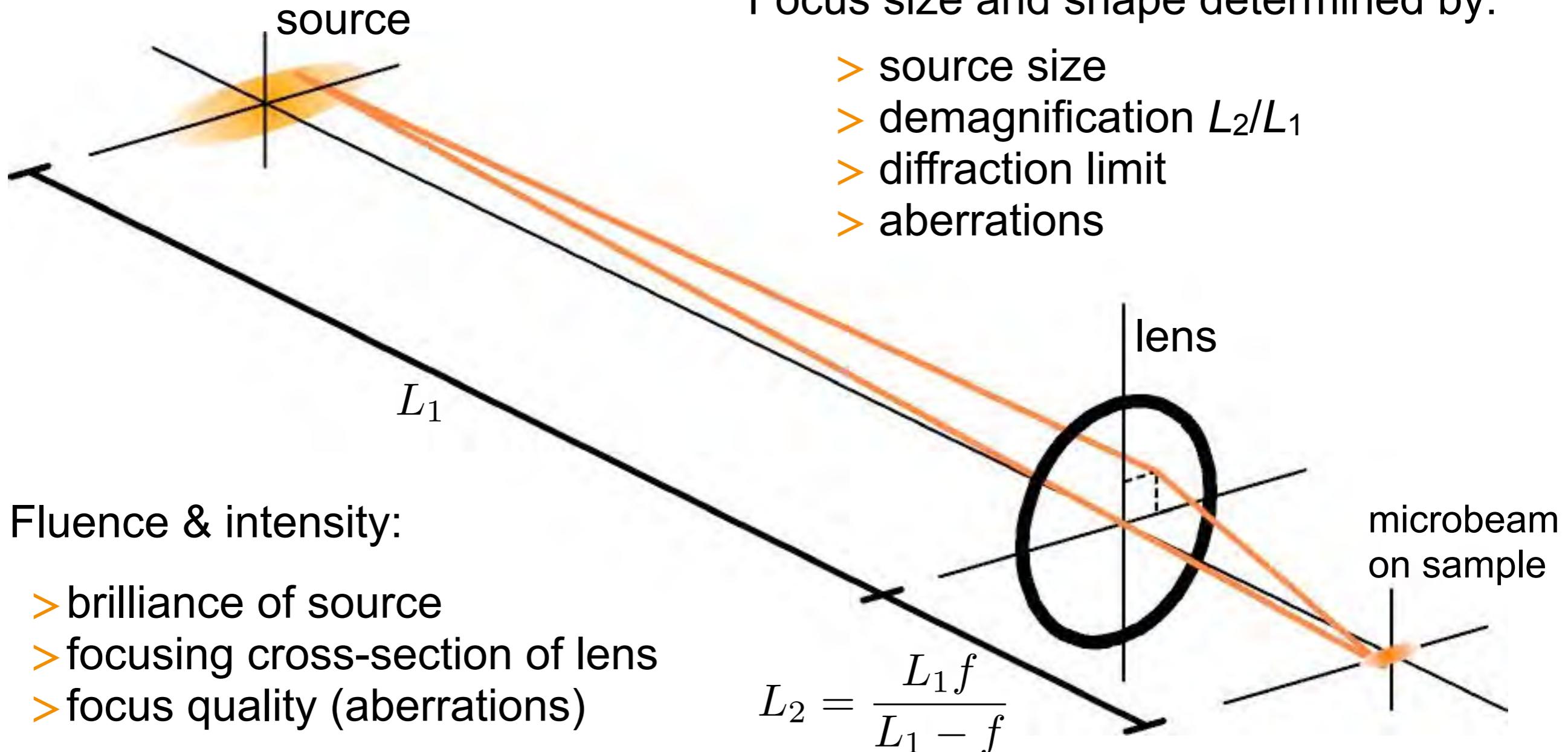
Wide-Angle-X-Ray-Scattering (WAXS) Tomography



P. Bleuet, et al., Nat. Materials 7, 468 (2008).

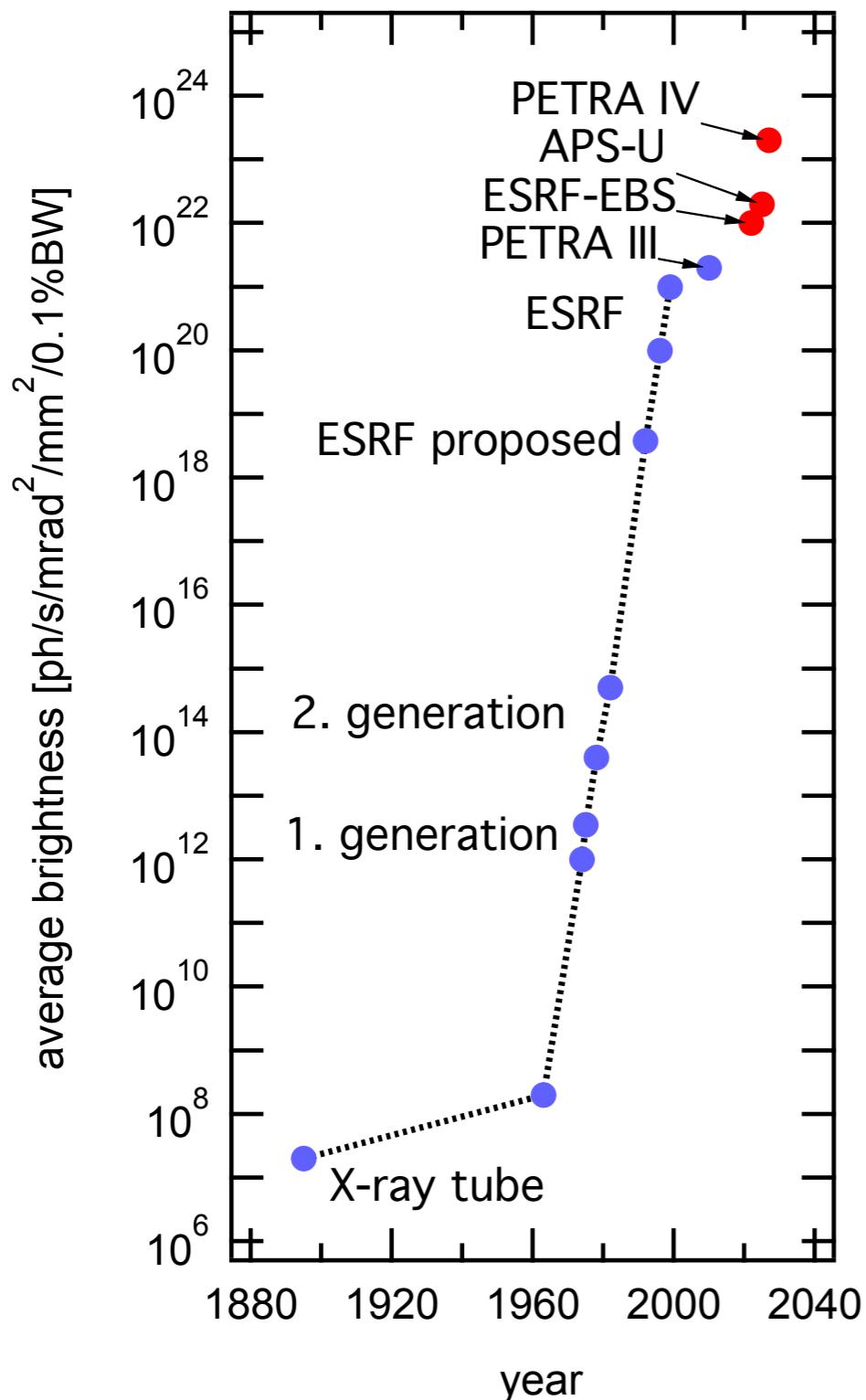
Scanning Microscopy with Hard X-Rays

Source is imaged onto the sample to create an intensive micro-/nanobeam:



Spectral Brightness

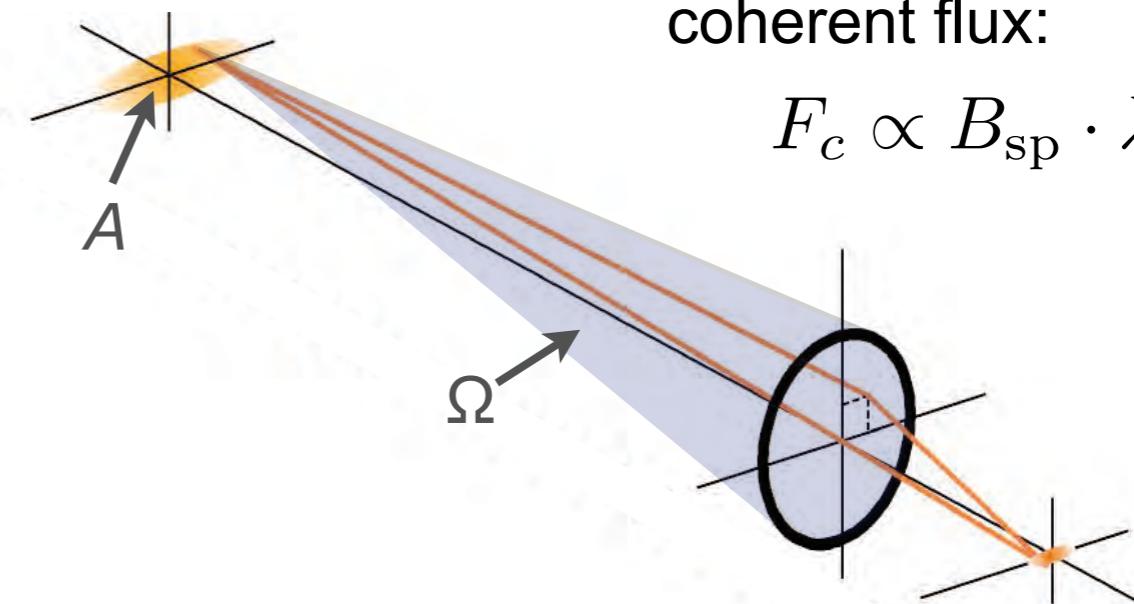
10000x more light per decade (since 1965)



Spectral brightness:

$$B_{\text{sp}} = \frac{F}{\Omega \cdot A \cdot \Delta E / E}$$

Flux per phase-space volume



coherent flux:

$$F_c \propto B_{\text{sp}} \cdot \lambda^2 \cdot \frac{\Delta E}{E}$$

Improvements in brightness:

- > faster measurements (time resolution)
- > nano-imaging (spatial resolution)
- > spectroscopy (energy resolution)

Fluorescence Tomography

Example: investigating the ion transport in plants

Fluorescence analysis of plants:

- > strong diffusion of elements
- > cell structure complicated and delicate

Difficult sample preparation

- > cryo sections
- > fracture surfaces

ideal:

nondestructive probe of
inner structures of sample

root of Mahogany tree

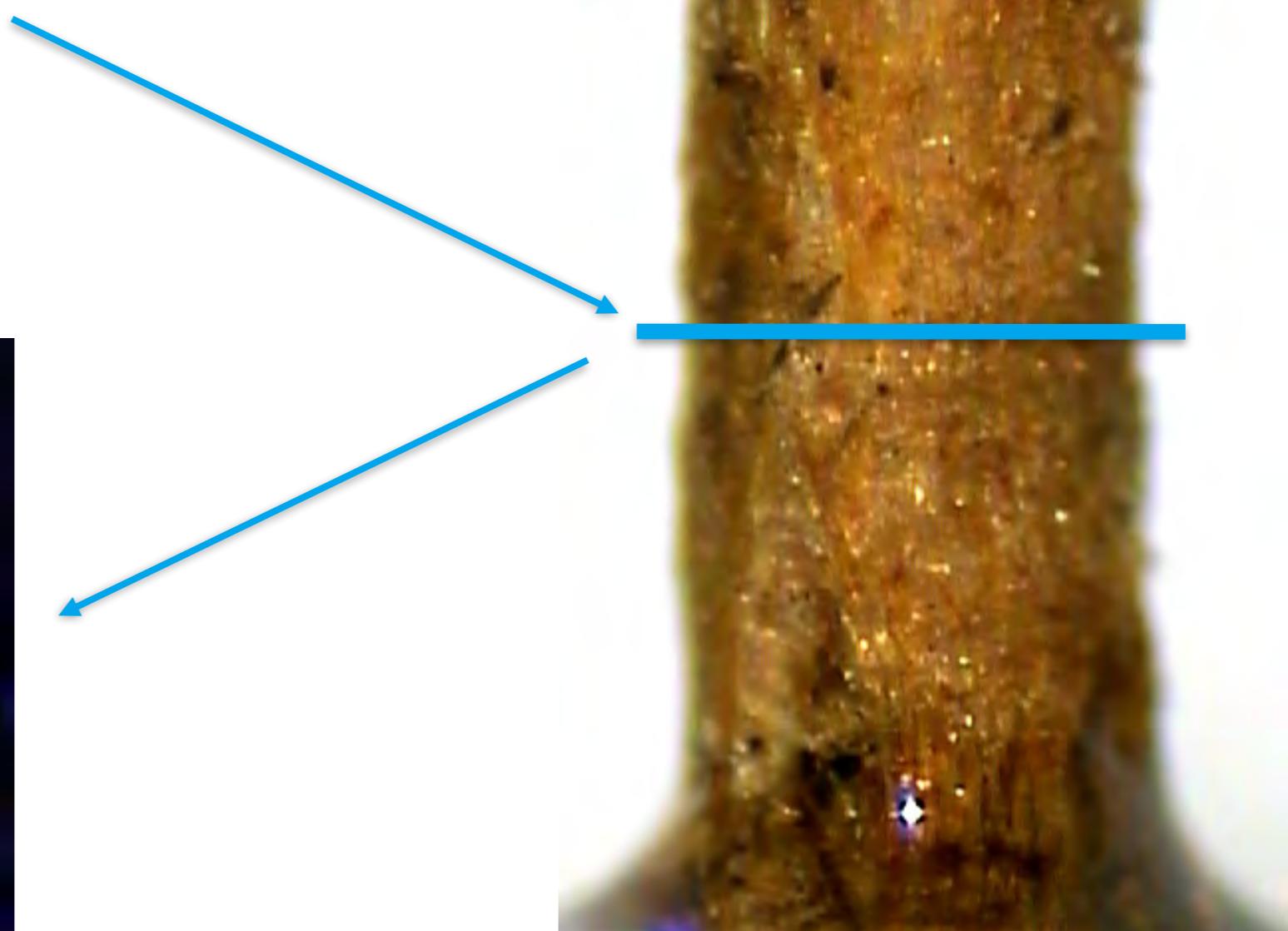
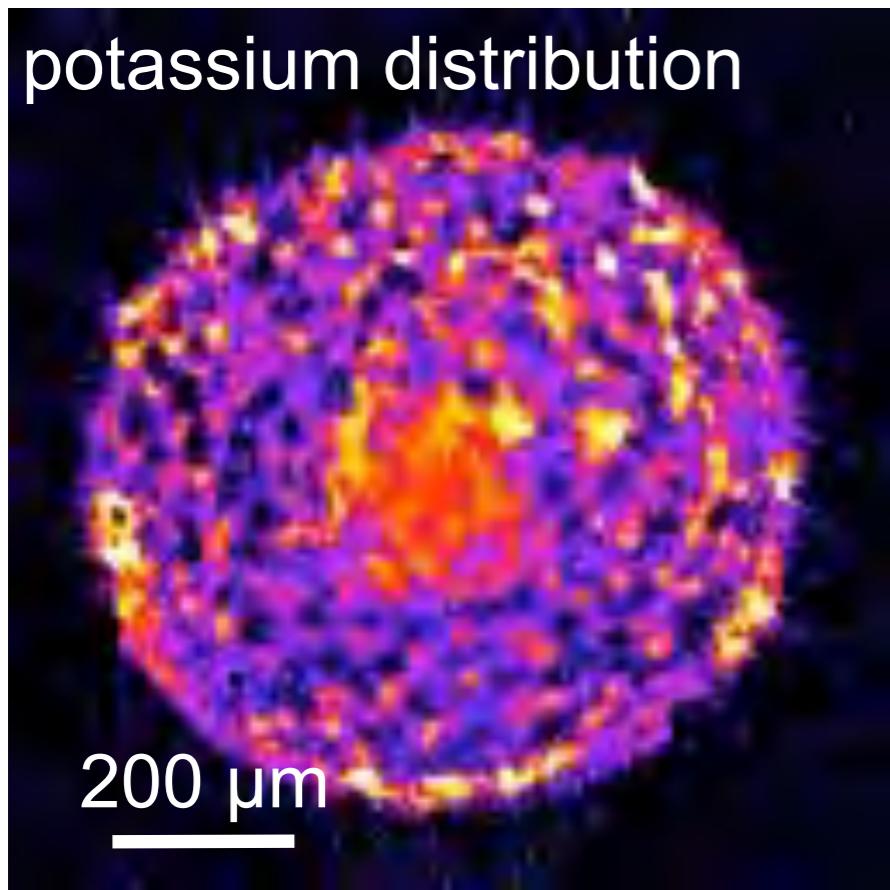


Fluorescence Tomography

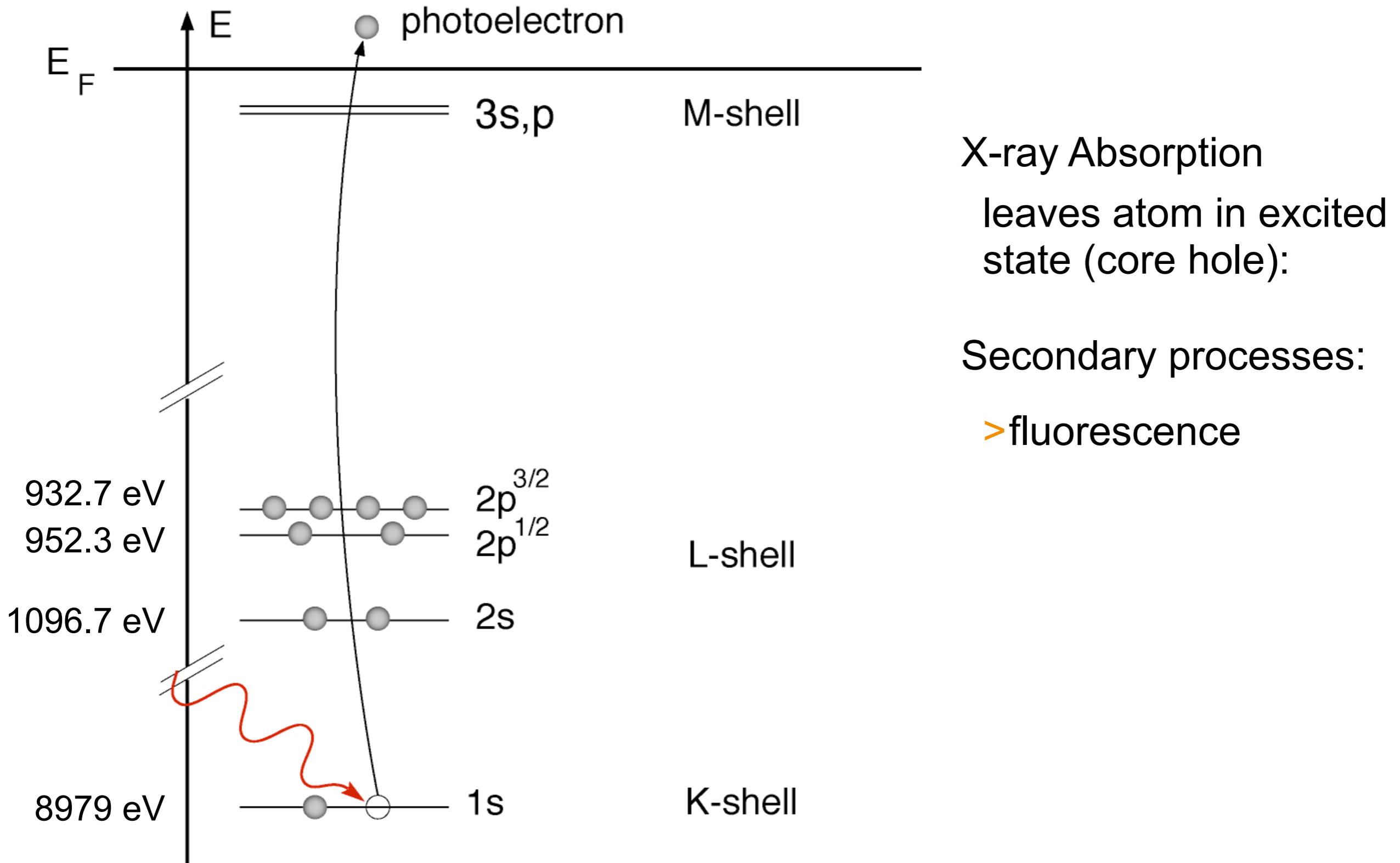
Root of Mahogany tree

element distribution on virtual
section through sample

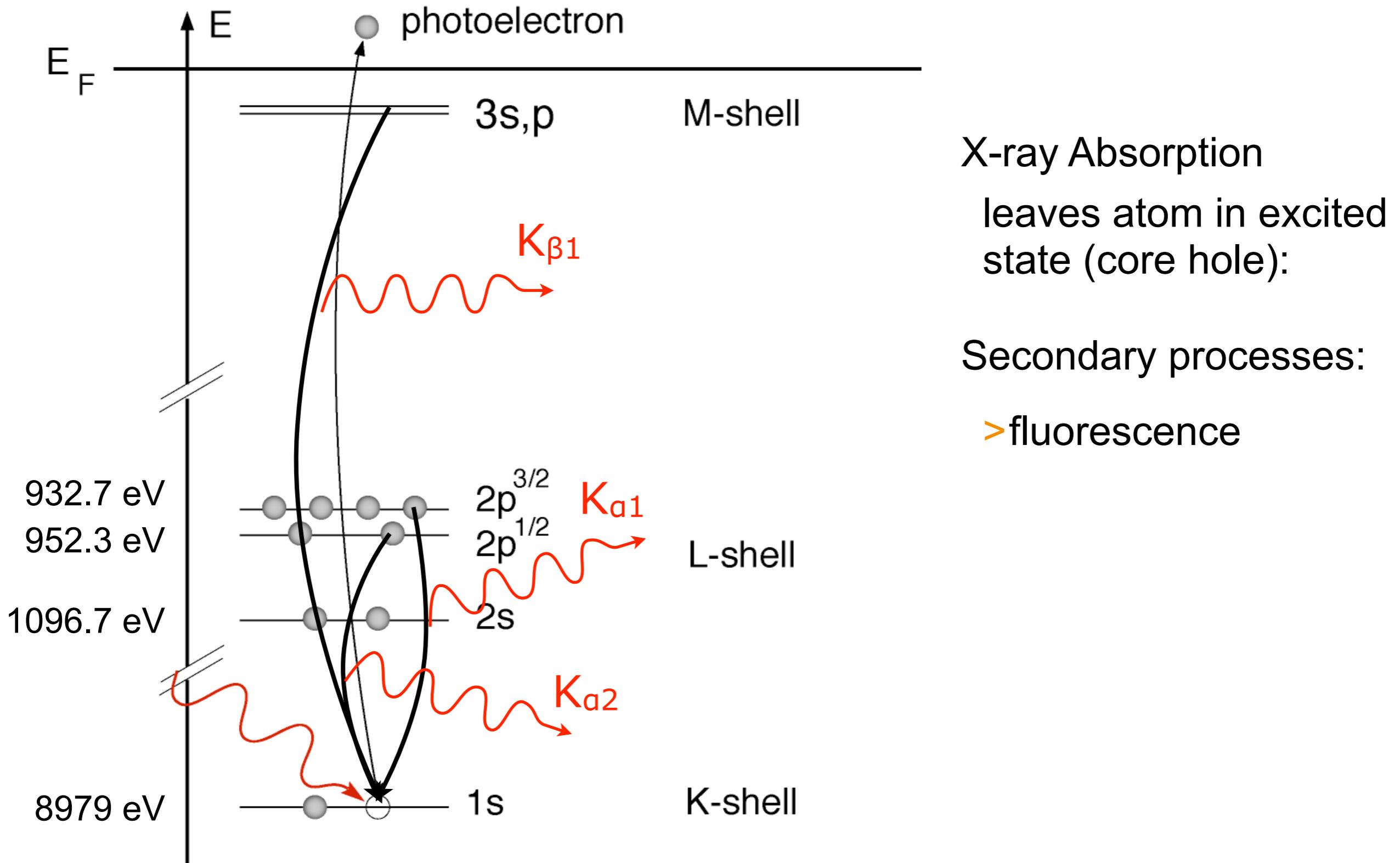
Example:



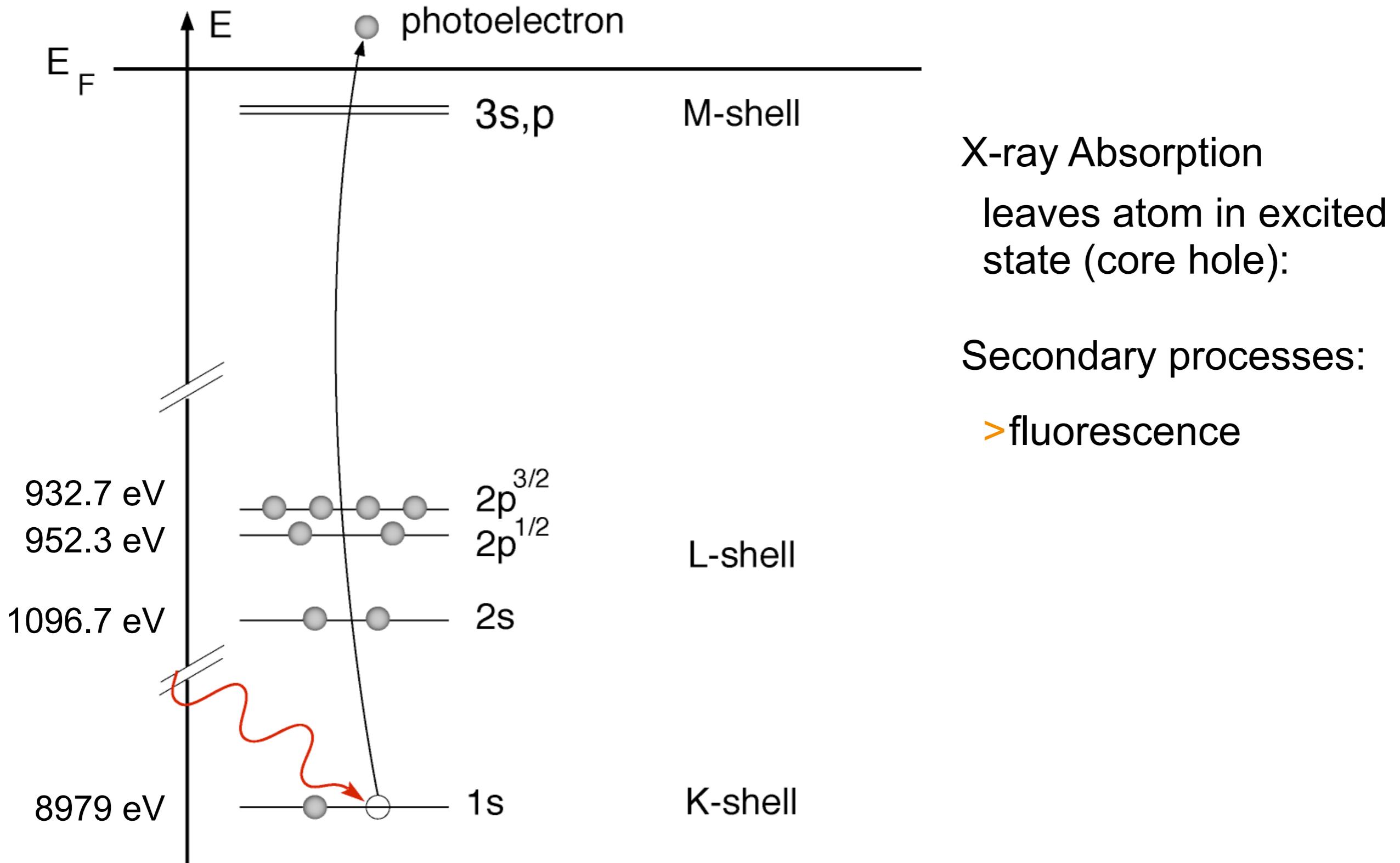
X-ray Fluorescence & Auger Process



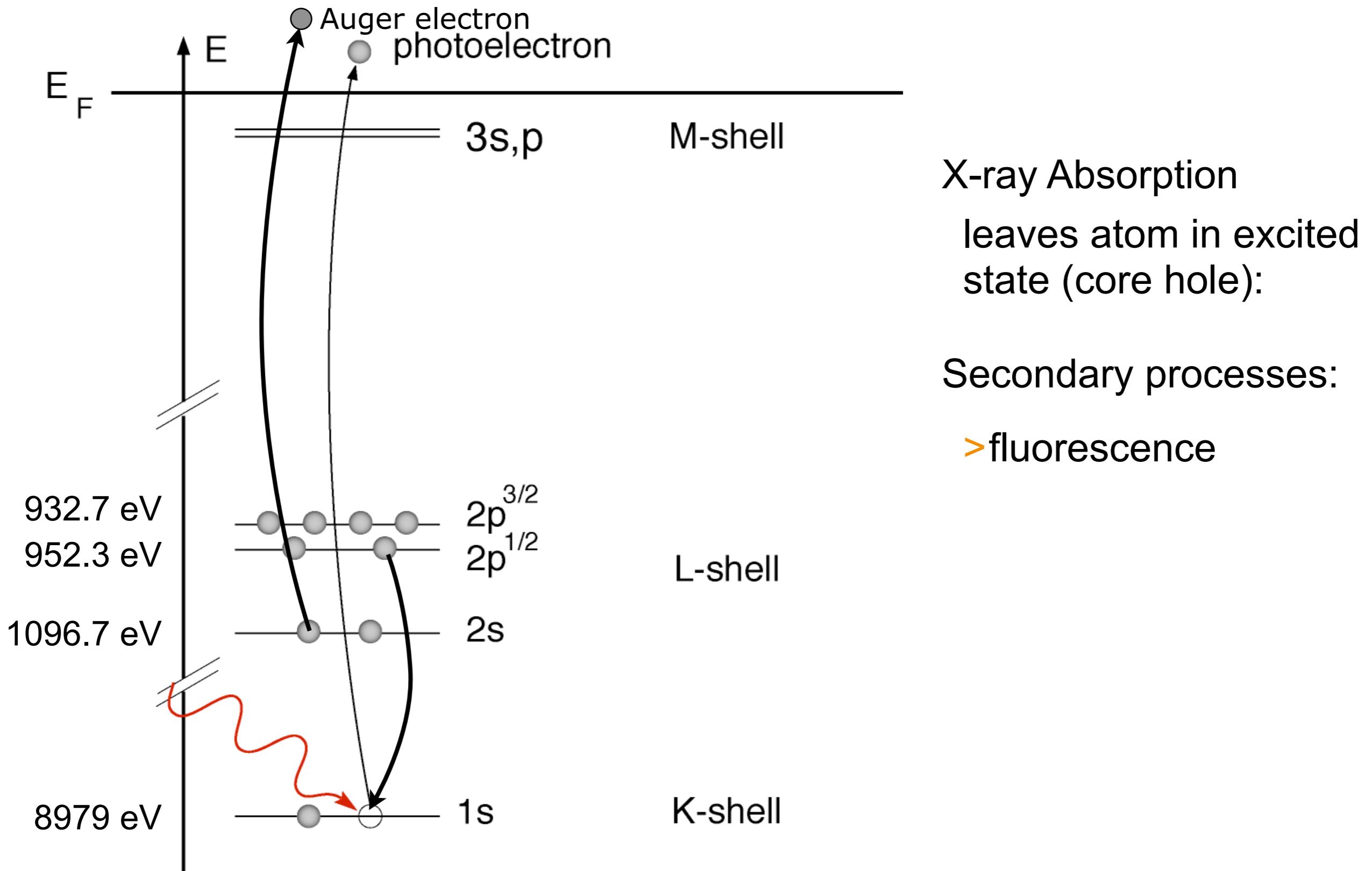
X-ray Fluorescence & Auger Process



X-ray Fluorescence & Auger Process



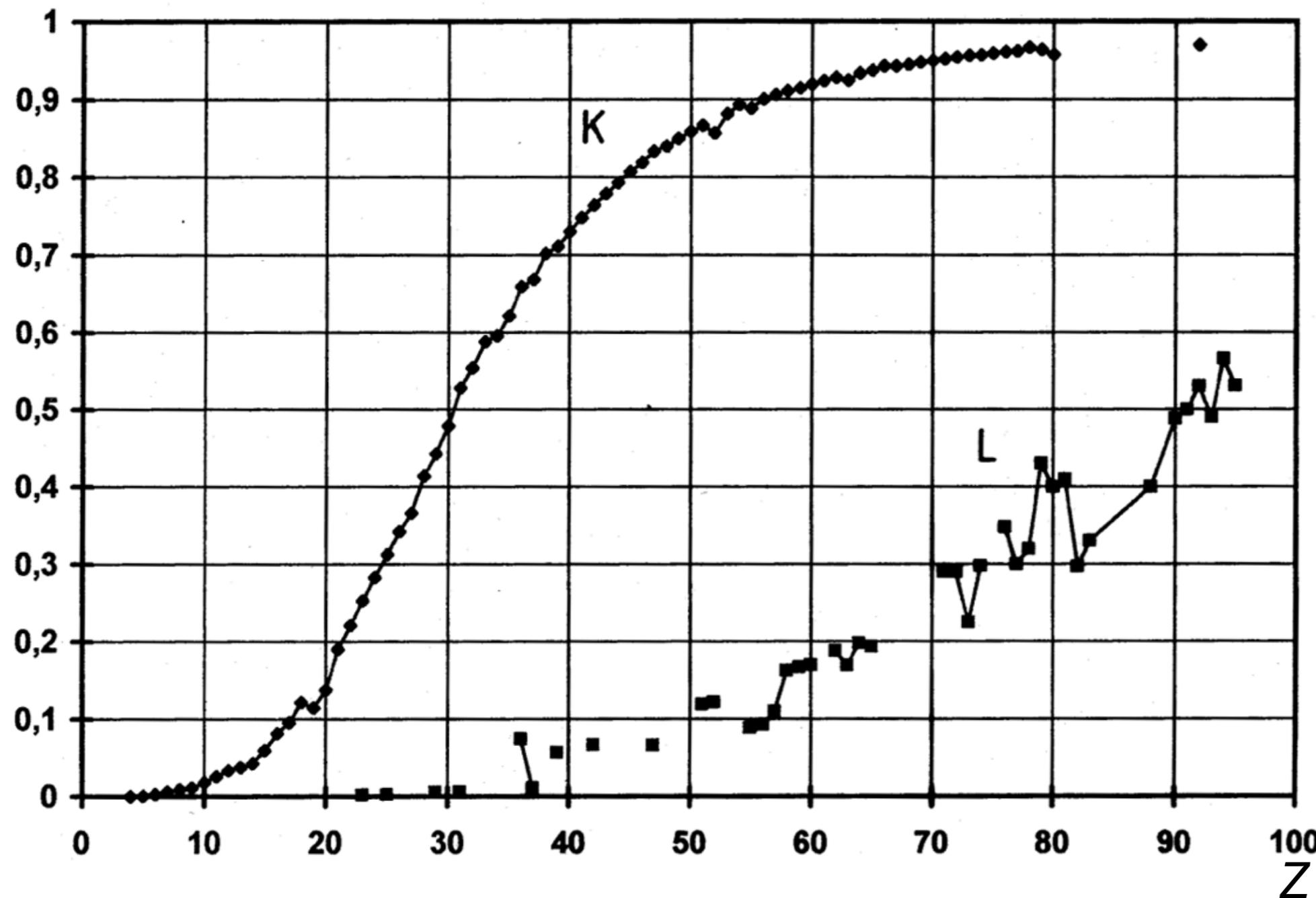
X-ray Fluorescence & Auger Process



Fluorescence Yield

$\epsilon_K \epsilon_L$

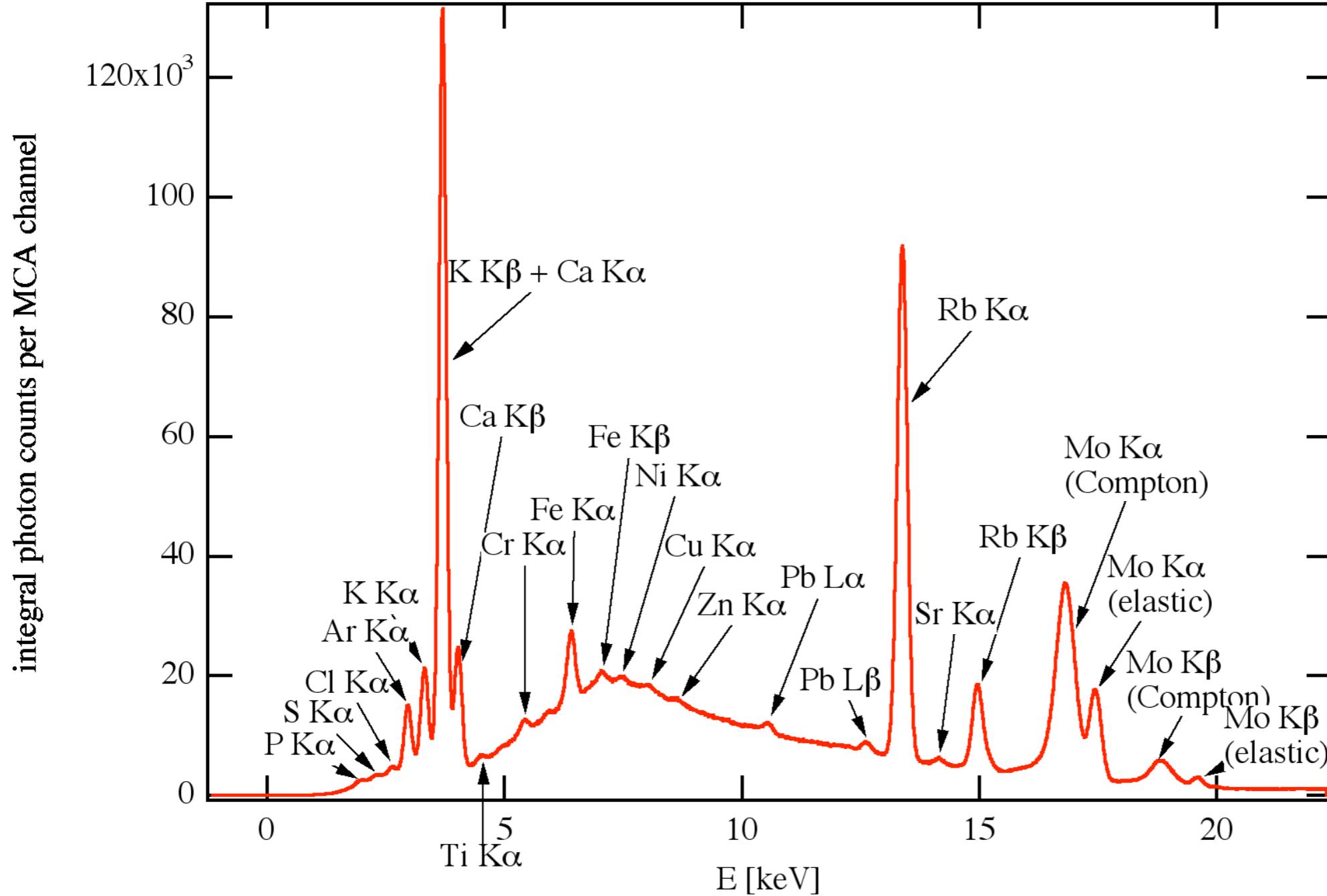
$1 - \epsilon = \text{Auger yield}$



element specific

Fluorescence dominates at higher binding energies for core hole excitation (growing with atomic number Z)

Fluorescence Spectrum



Illuminated atoms emit characteristic fluorescence radiation!

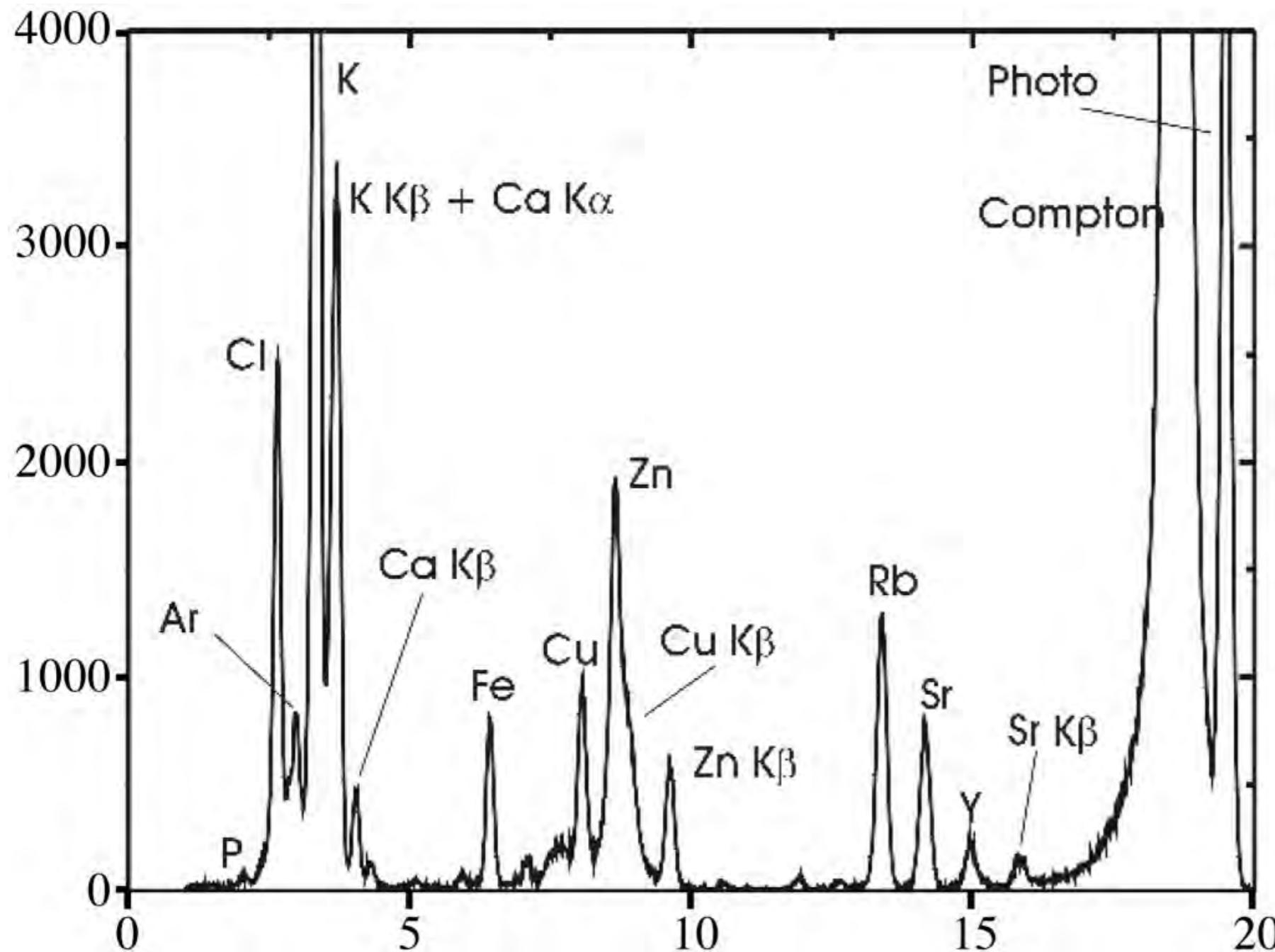
Example spectrum excitation with X-ray tube:

Background due to scattered spectrum of X-ray tube

Limitation of detection limits by background!

Excitation with Monochromatic Synchrotron Radiation

Example: undulator radiation (Si 111 monochrom.): 19.5 keV

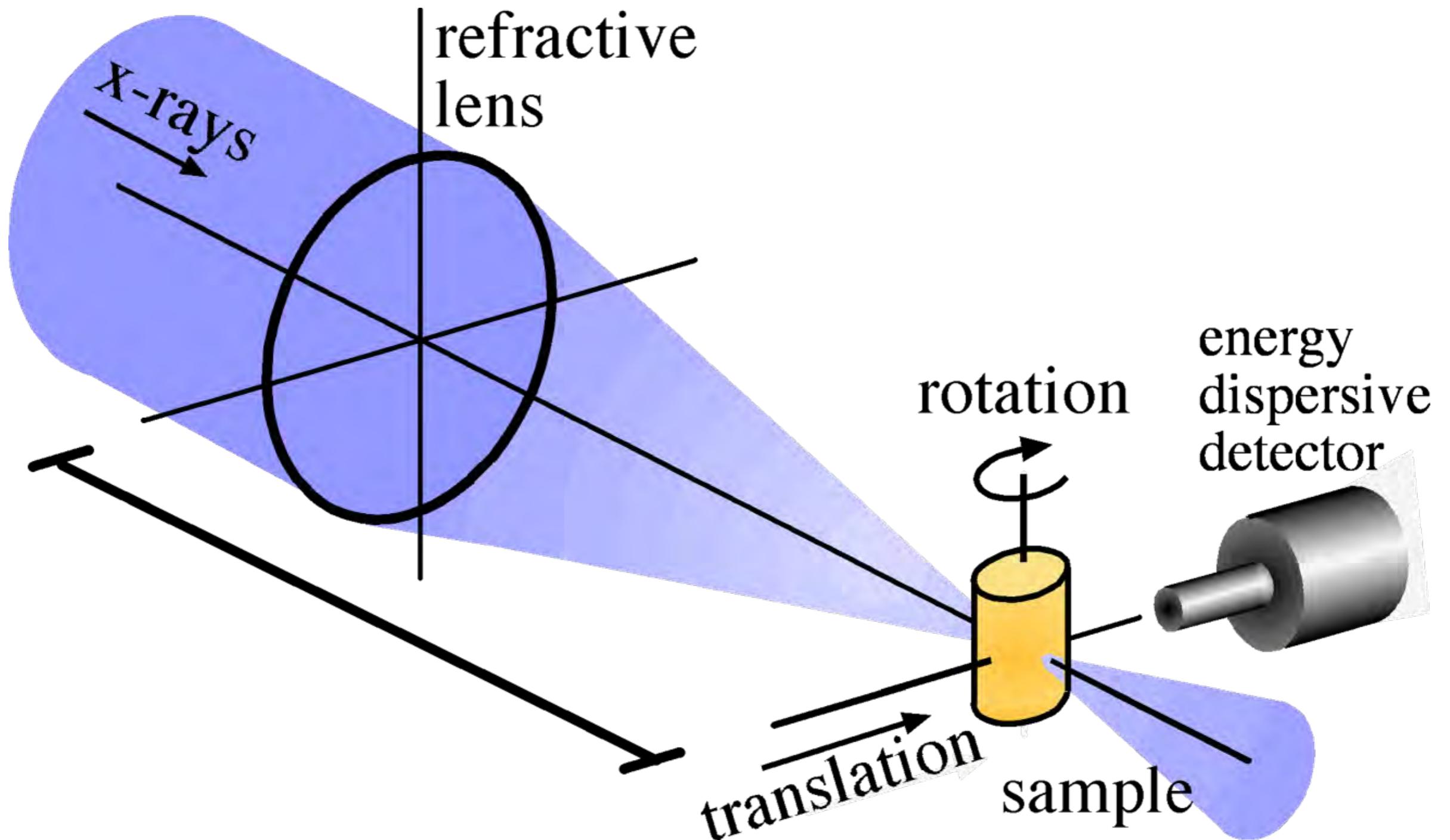


No background due to scattered radiation at fluorescence energy

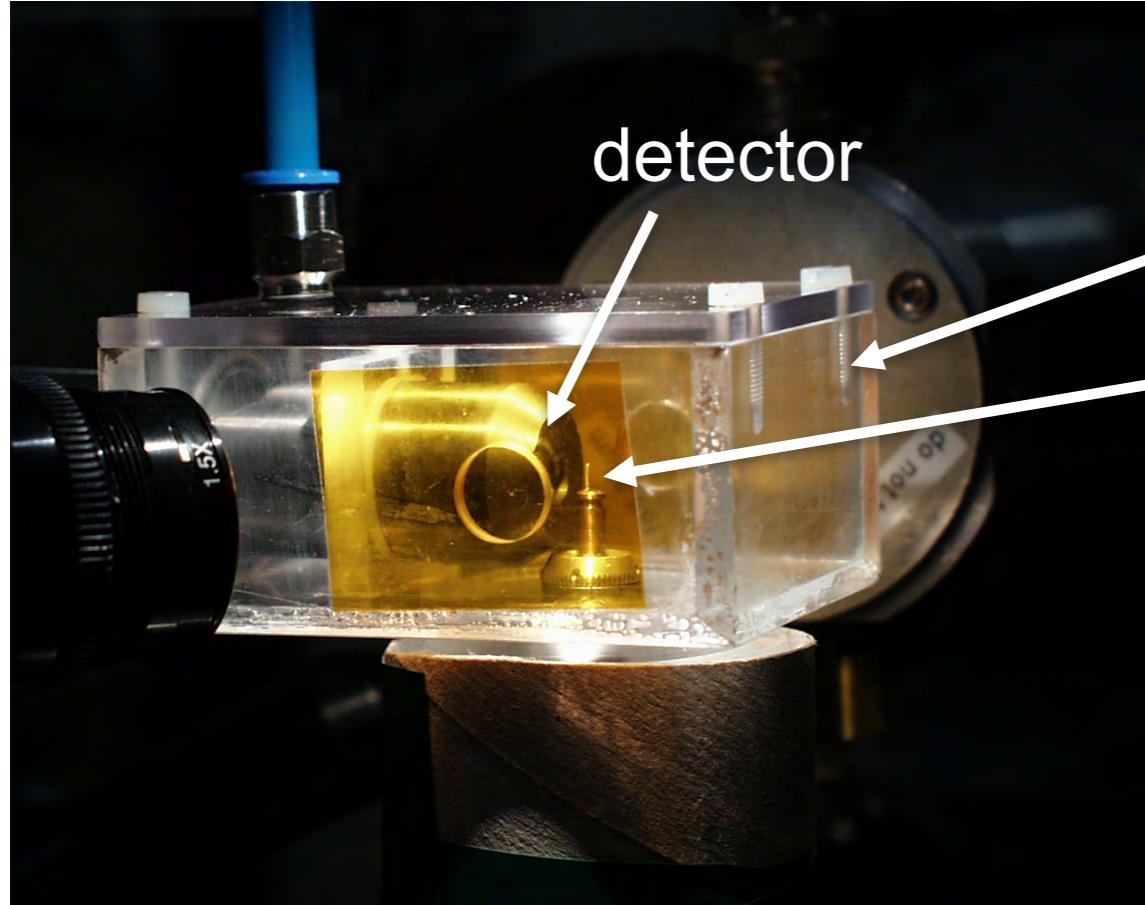
High signal-to-background ratio!!

very low detection limits possible (ppb-level)!

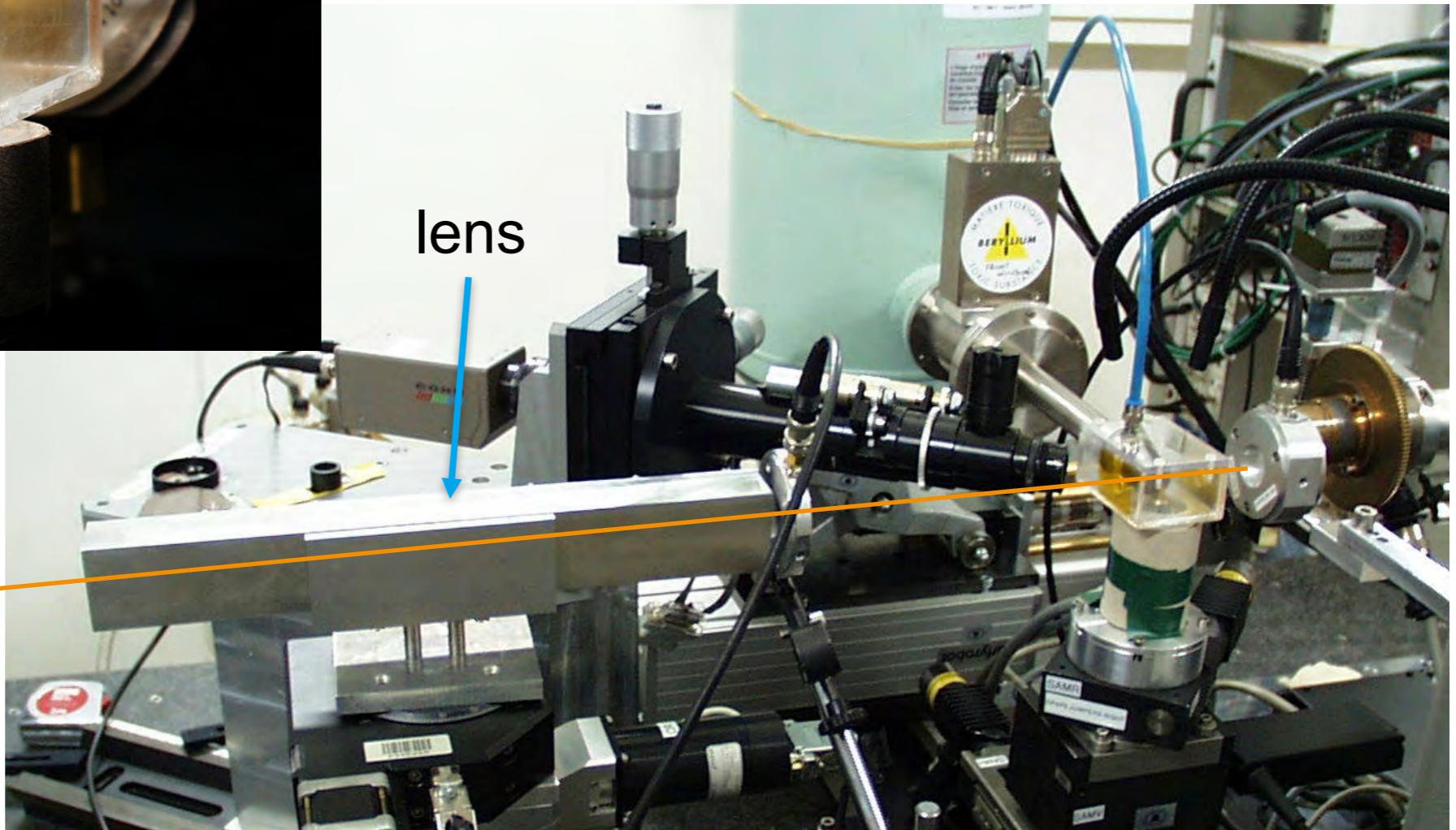
Scanning Probe: Fluorescence Microtomography



Fluorescence Microtomography

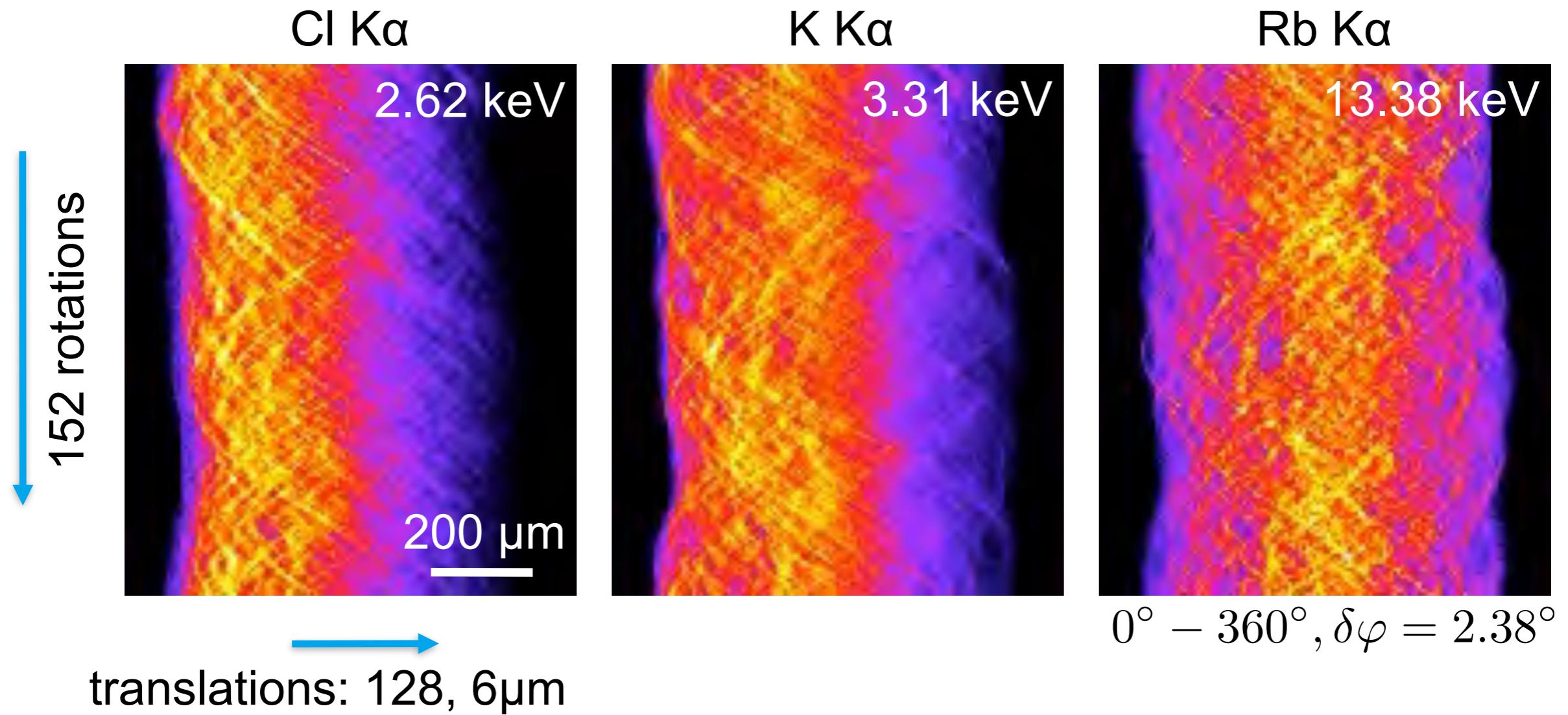


synchrotron
radiation



Fluorescence Tomography: Measured Data

Sinograms:

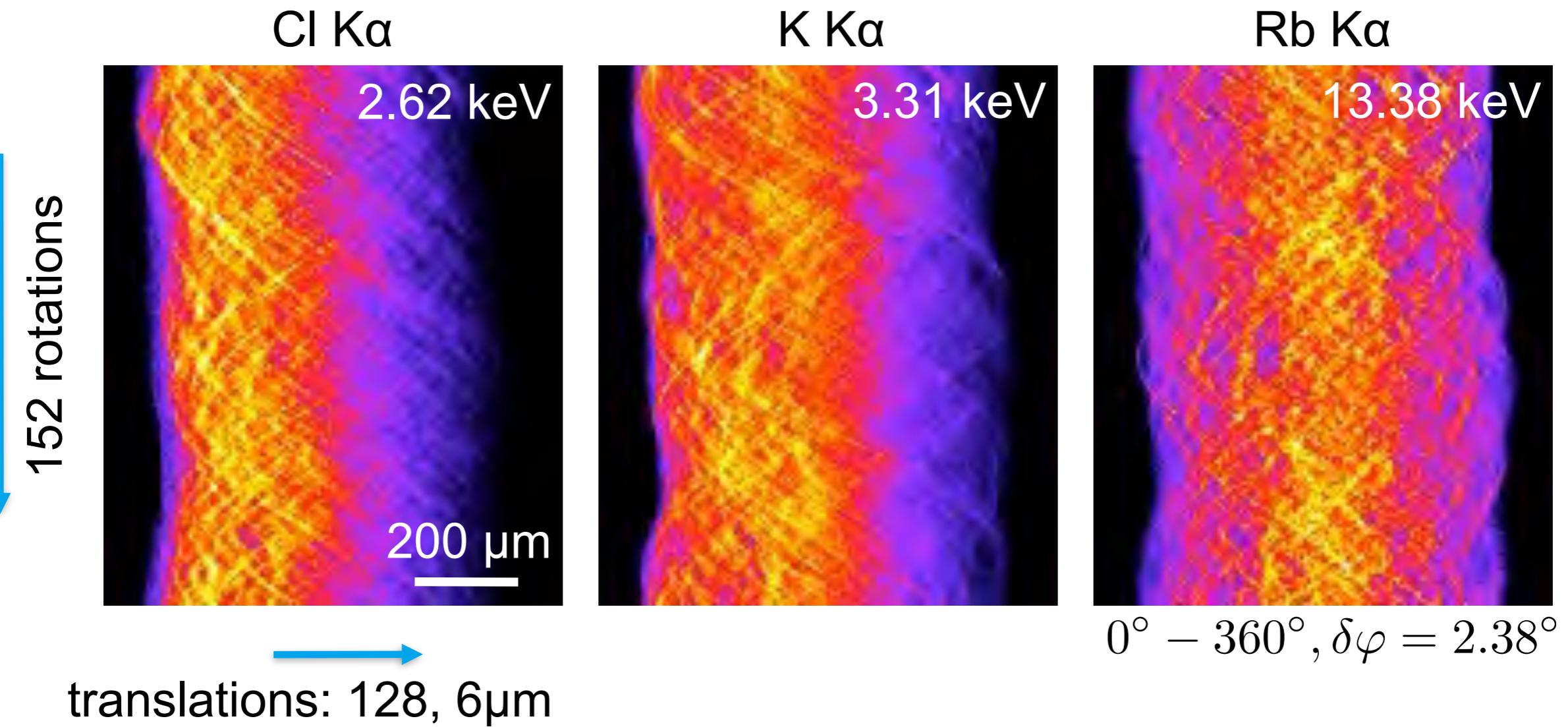


experimental parameters:

- > energy: 19.5 keV
- > refractive lens (Al): $N = 150$, $f = 45.4$ cm, $m = 1/127$
- > beam size: $1.5 \times 6 \mu\text{m}^2$, flux: $1.1 \cdot 10^{10}$ ph/s

Fluorescence Tomography: Measured Data

Sinograms:

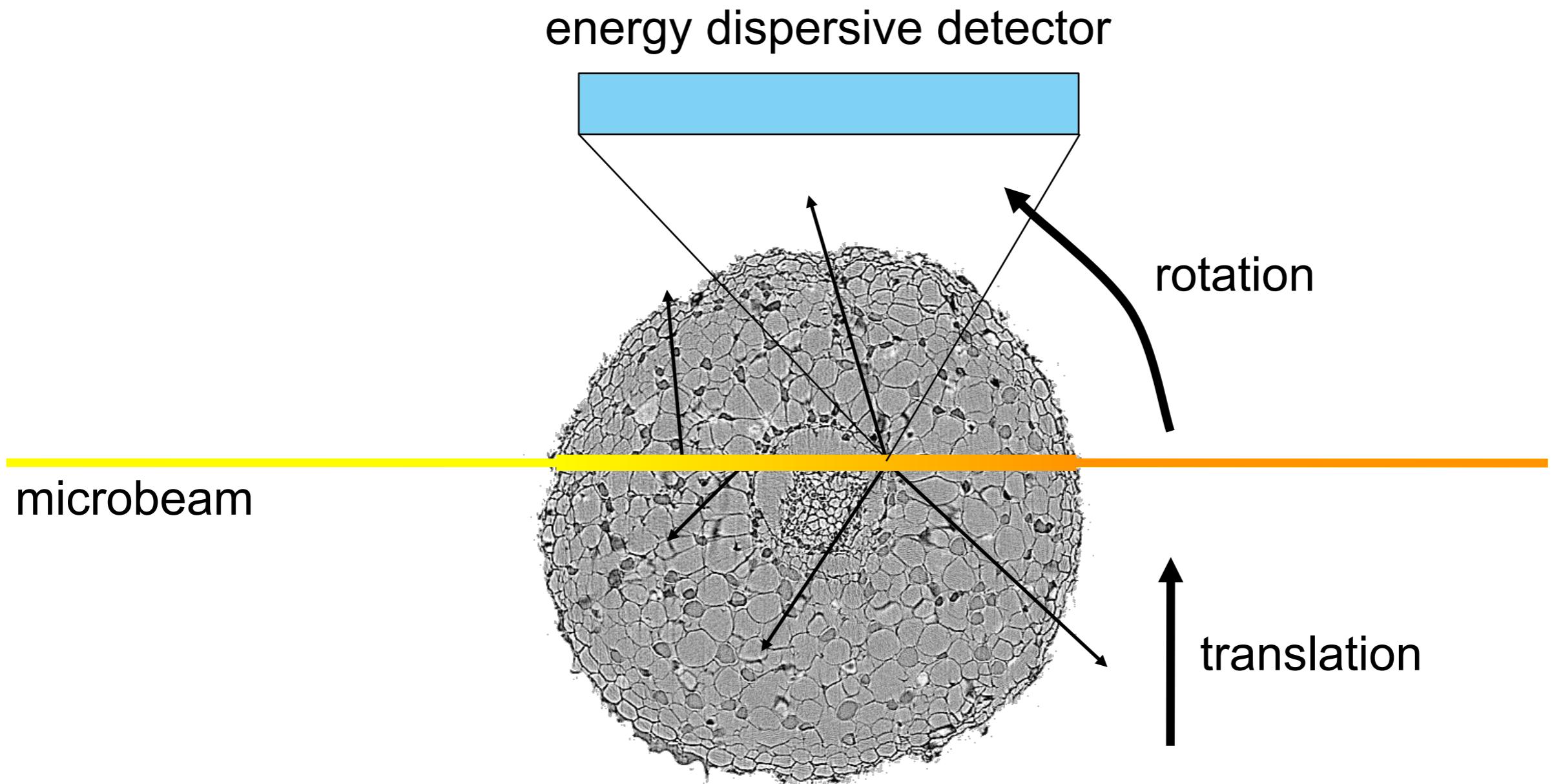


Symmetry:

$$I_{i\nu}(-r, \varphi + \pi) = I_{i\nu}(r, \varphi)$$

only holds (approx.) for Rb!
Absorption of fluorescence radiation:
asymmetry in sinogram.

Fluorescence Tomography: Model

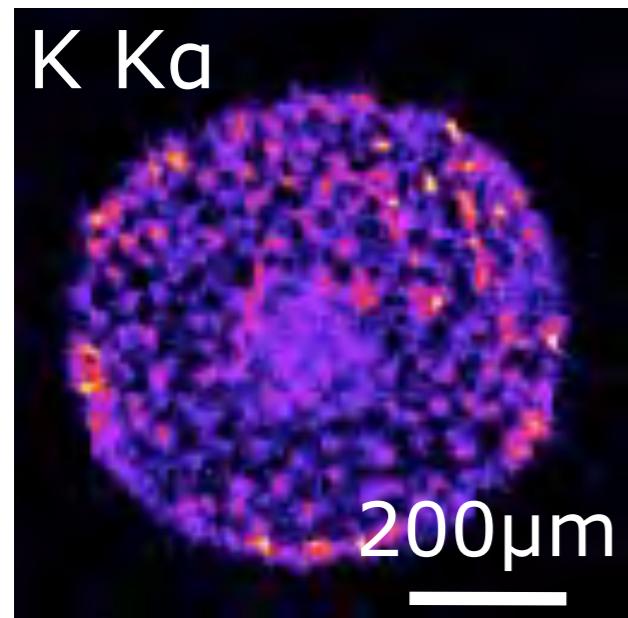


$$I_{i\nu}(r, \varphi) = I_0 \int ds \left[e^{-\int_{-\infty}^s ds' \mu_0(x,y)} \cdot p_{i\nu}(x, y) \cdot \int d\gamma e^{-\int dr' \mu_{i\nu}(x,y)} \right]$$

Absorption Correction

Example: potassium distribution in Mahogany root

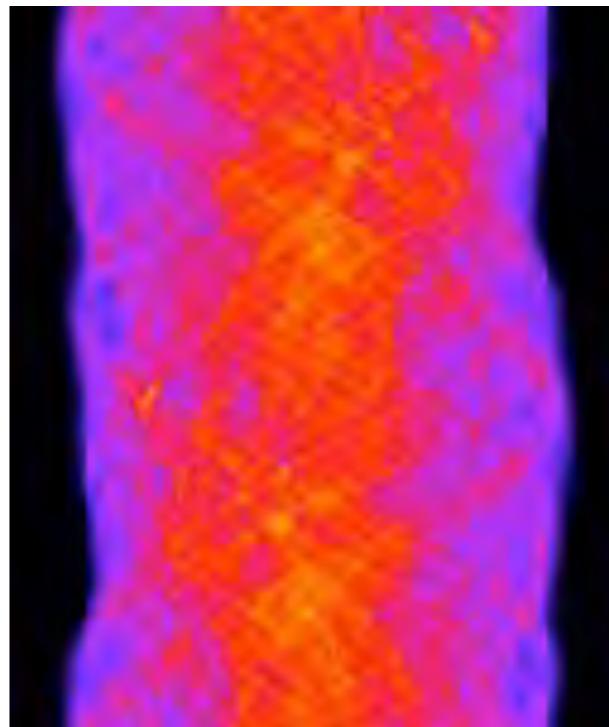
Disregarding attenuation of fluorescence:



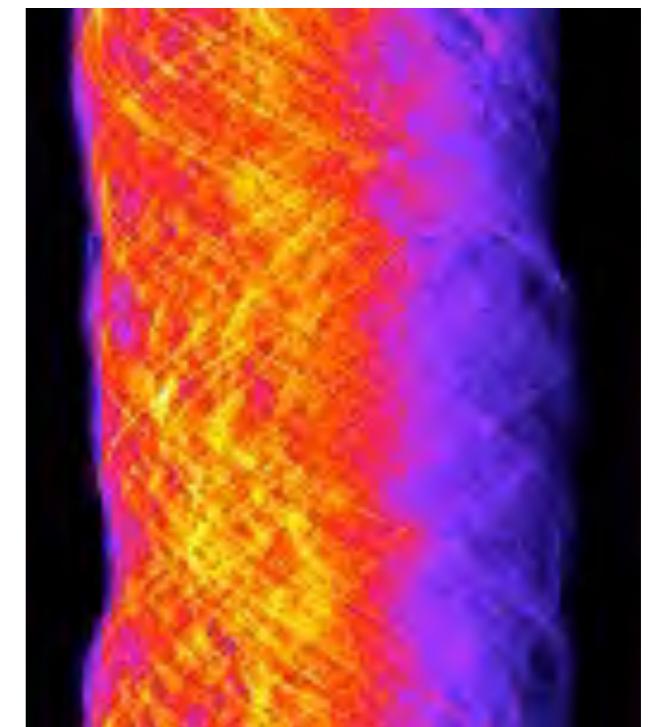
$$\mu_{\text{K} \text{K}\alpha} = 0$$

simple
tomographic
model

reconstructed
sinogram



measured
sinogram

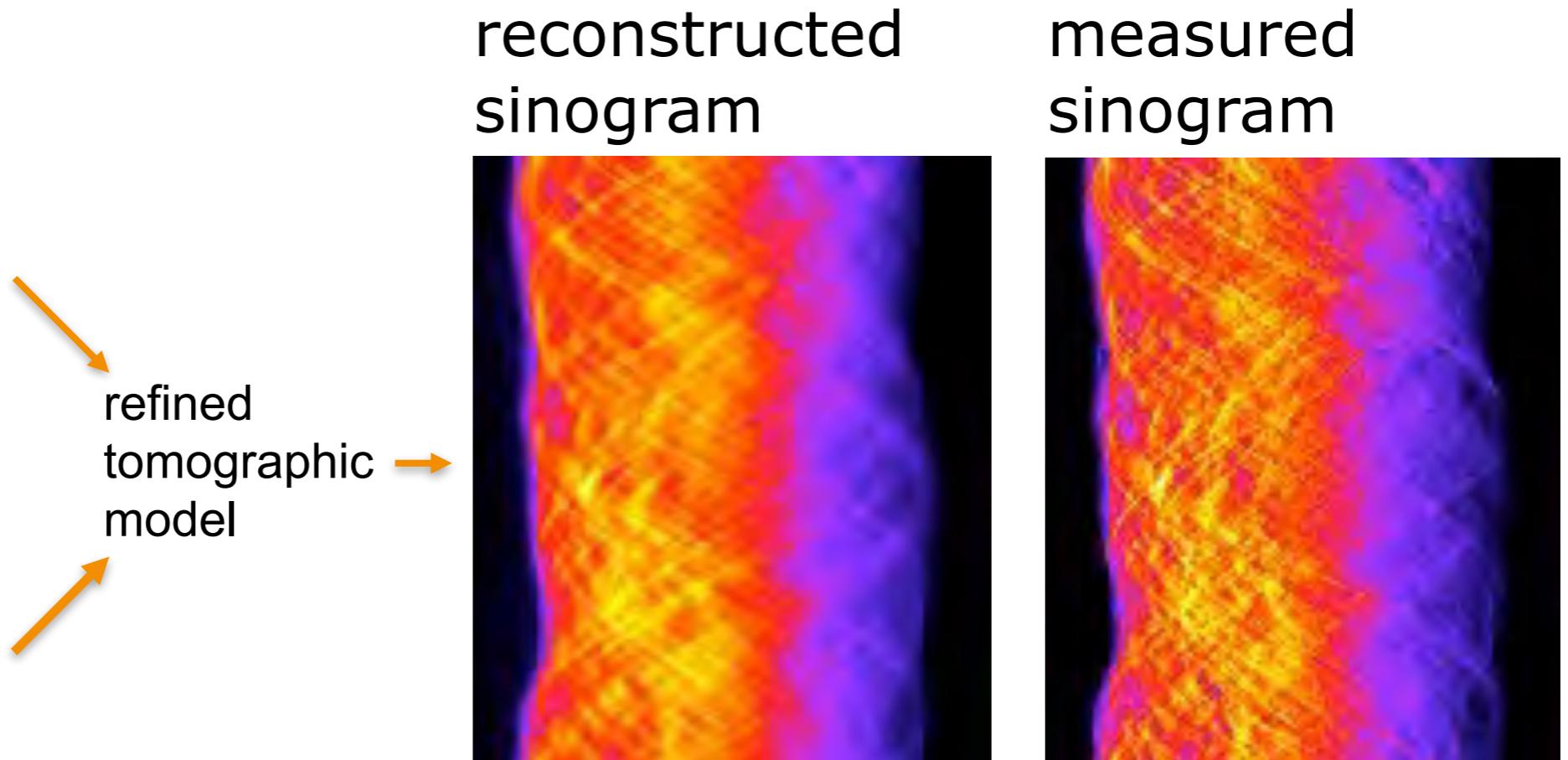
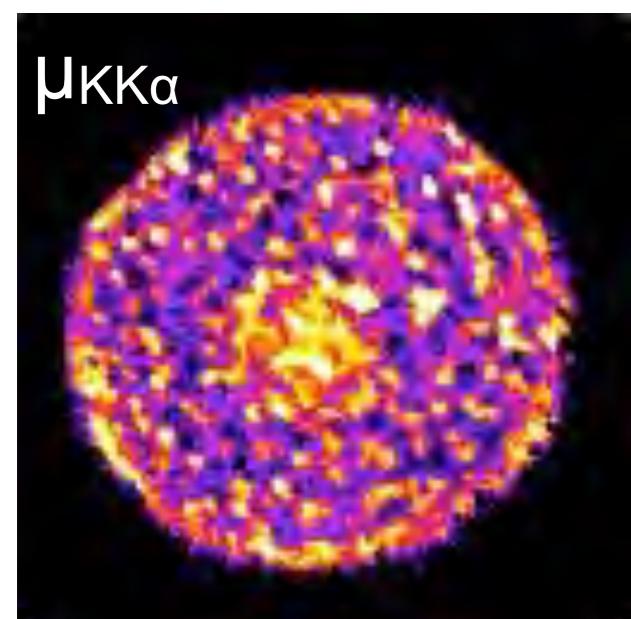
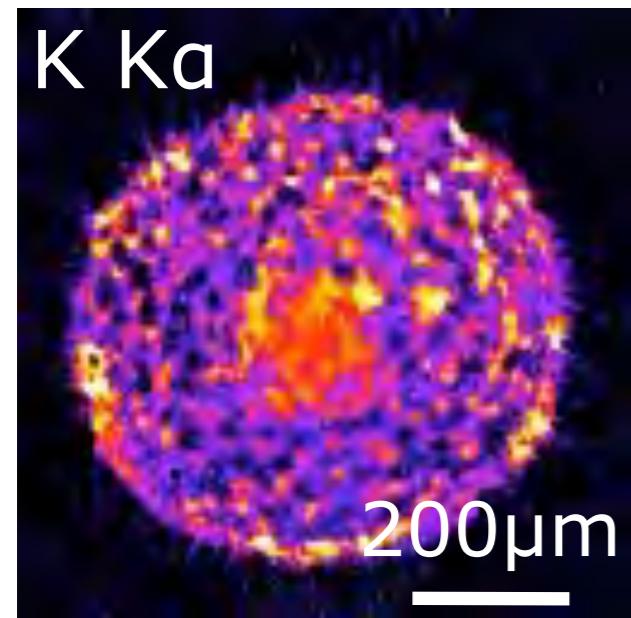


C. Schroer, Appl. Phys. Lett. 79, 1912 (2001).

Absorption Correction

Example: potassium distribution in Mahogany root

Accounting for attenuation of fluorescence:

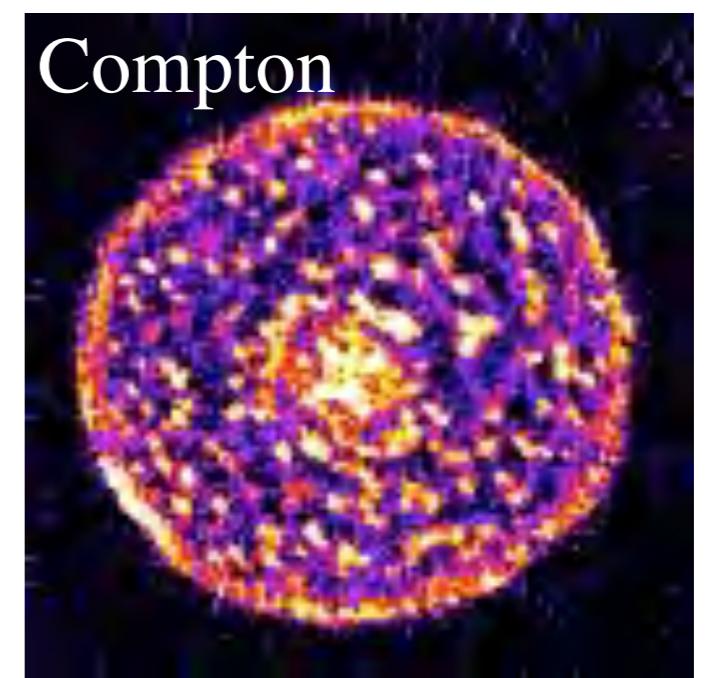
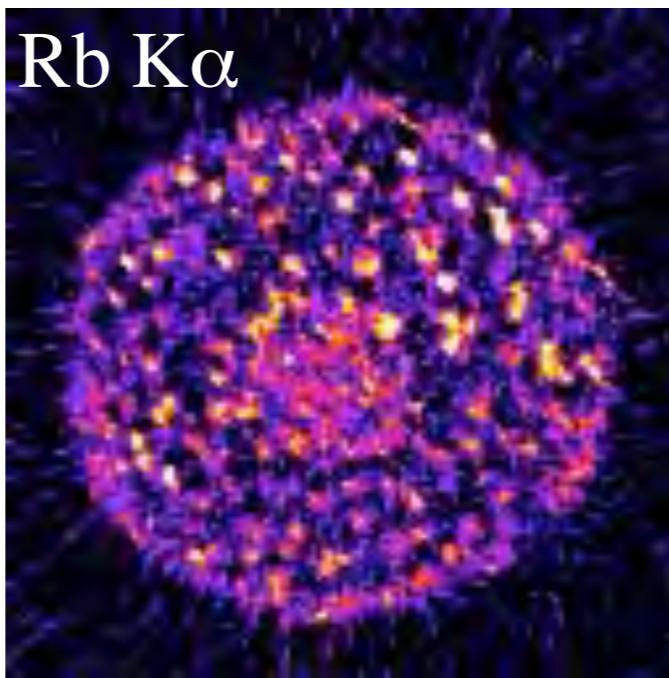
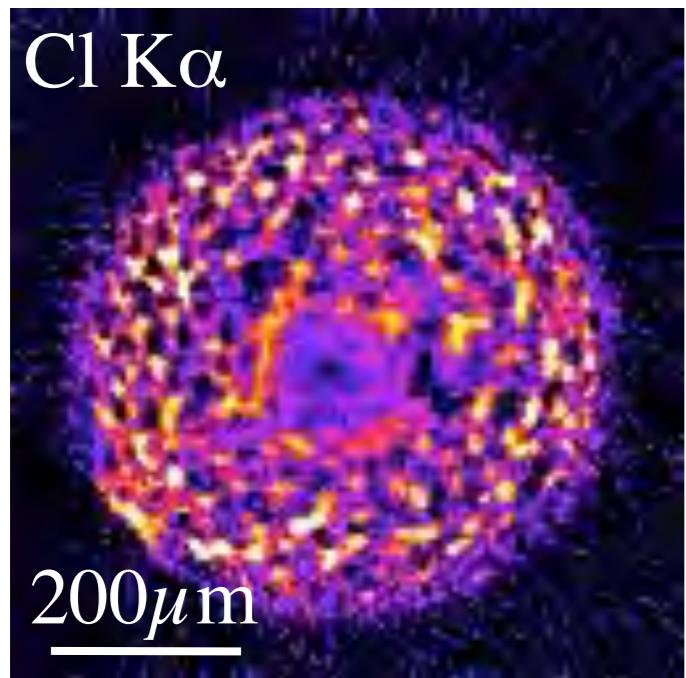
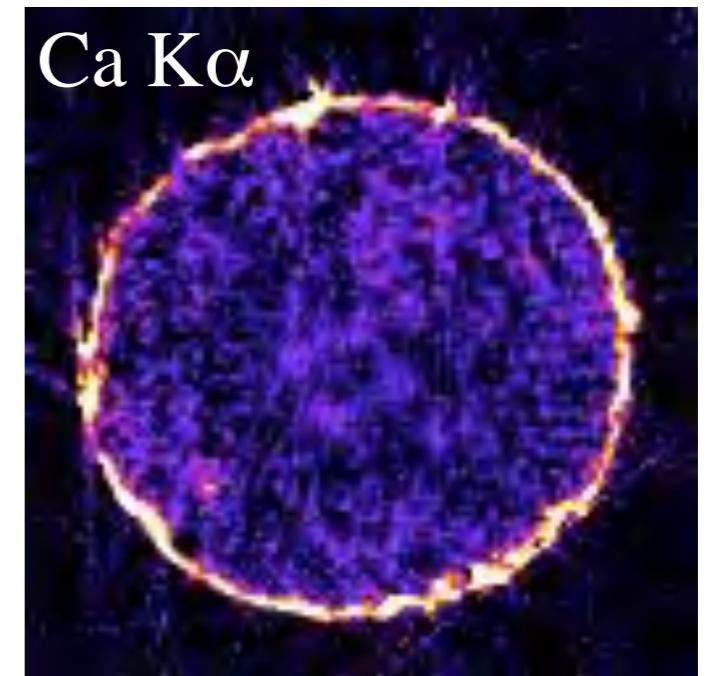
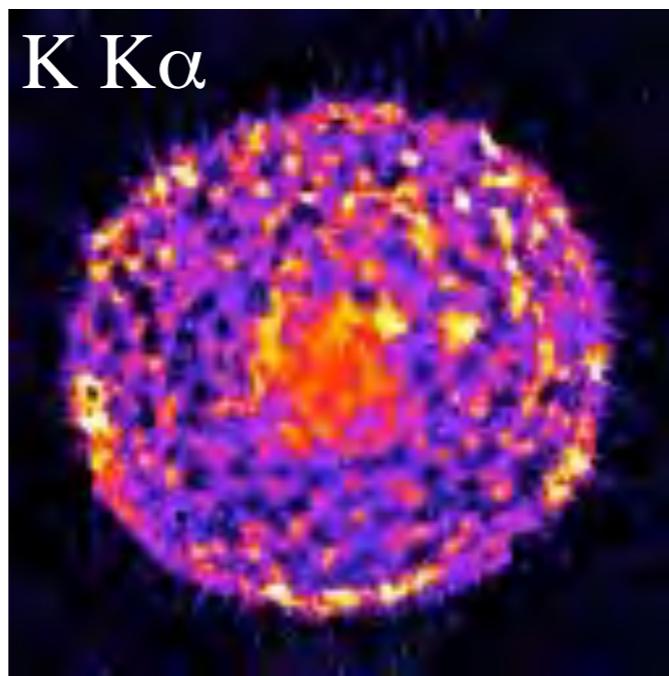


C. Schroer, Appl. Phys. Lett. 79, 1912 (2001).

Fluorescence Tomography

root of Mahogany tree

pixel size: 6 μm



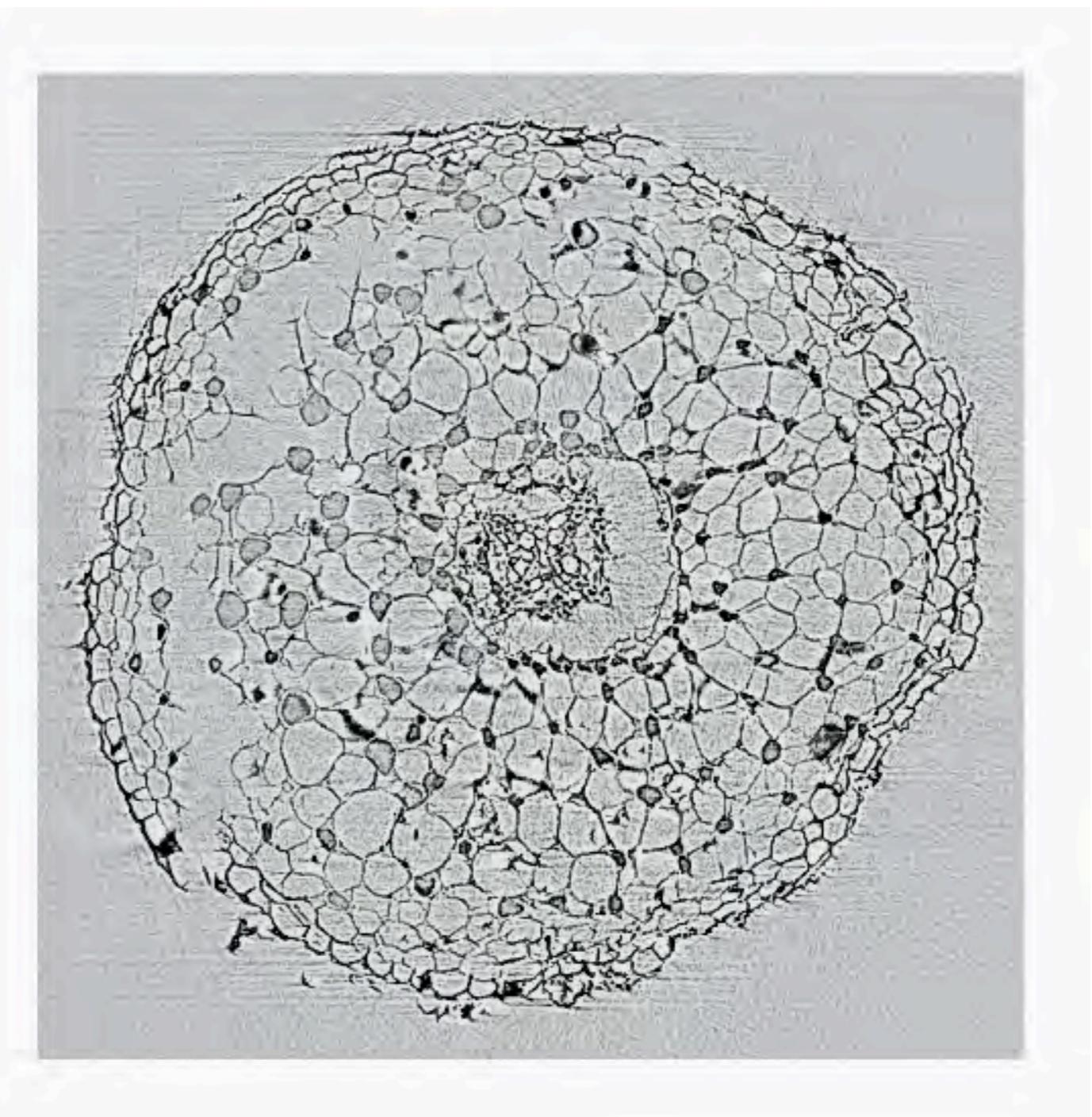
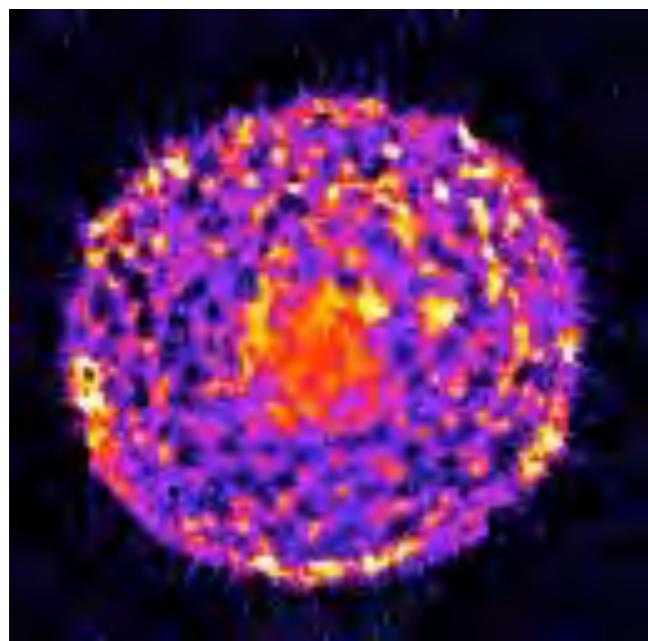
Fluorescence Tomography

Take advantage of:

- >large penetration depth of x-rays
- >element specific contrast

Compare with structural data
from transmission tomogram:

K K α



SAXS Tomography: Local Nanostructure

SAXS: Small-Angle X-ray Scattering

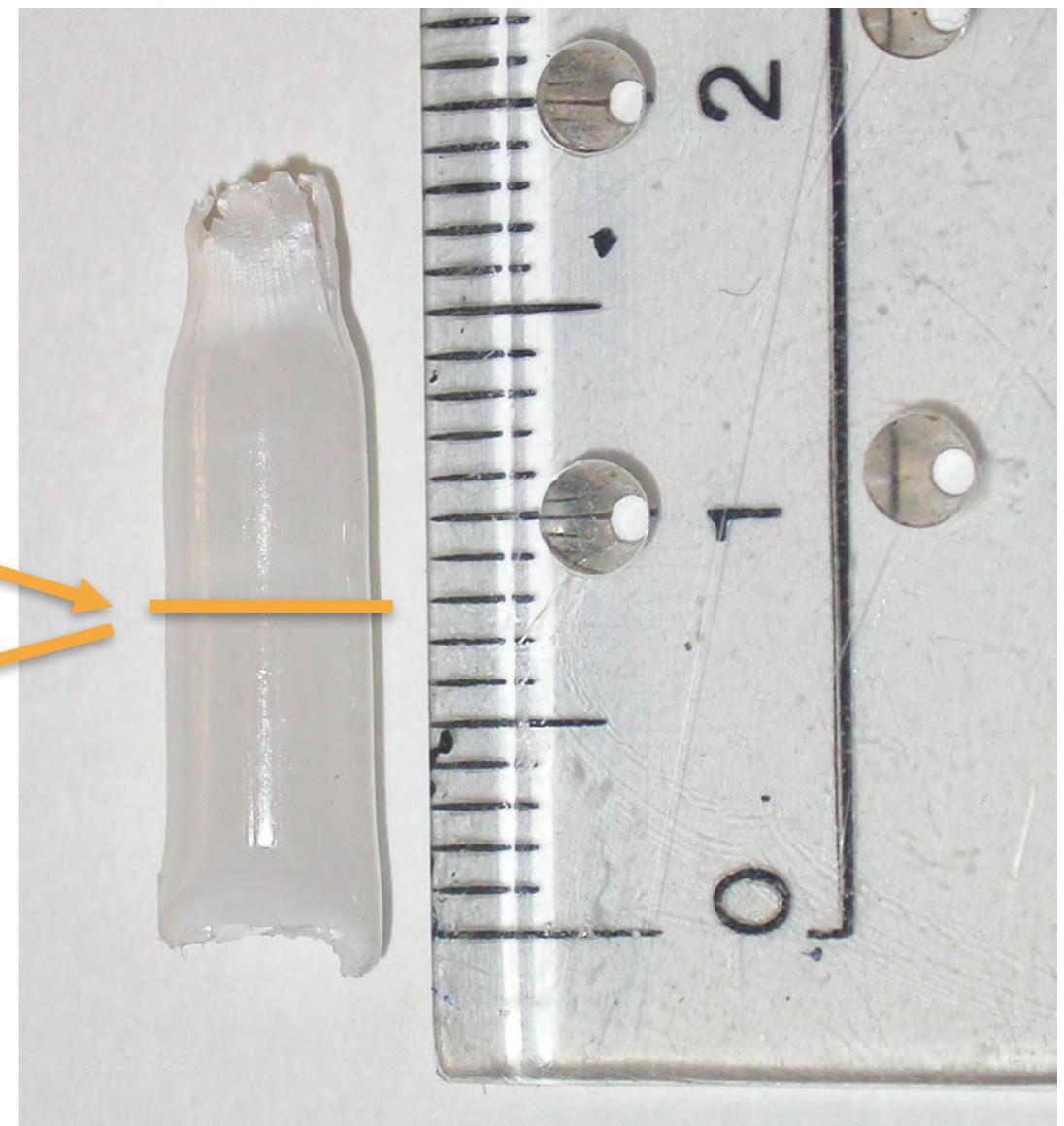
Investigating the local nanostructure on a virtual section through sample

Non-destructive investigation
of inner structure of sample

virtual section

reconstructed SAXS
cross section at each point
on the virtual section

Sample:

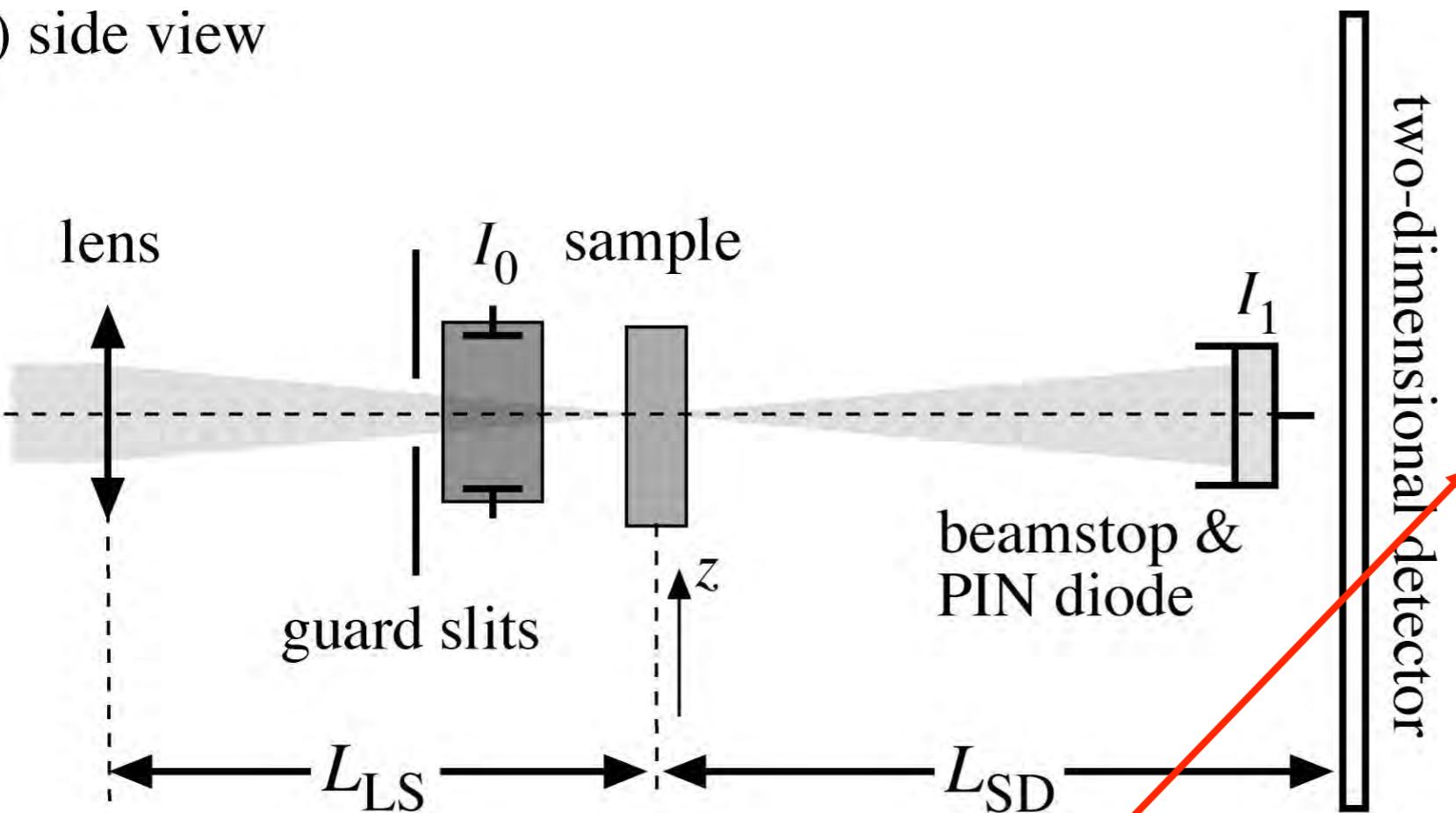


polyethylene rod

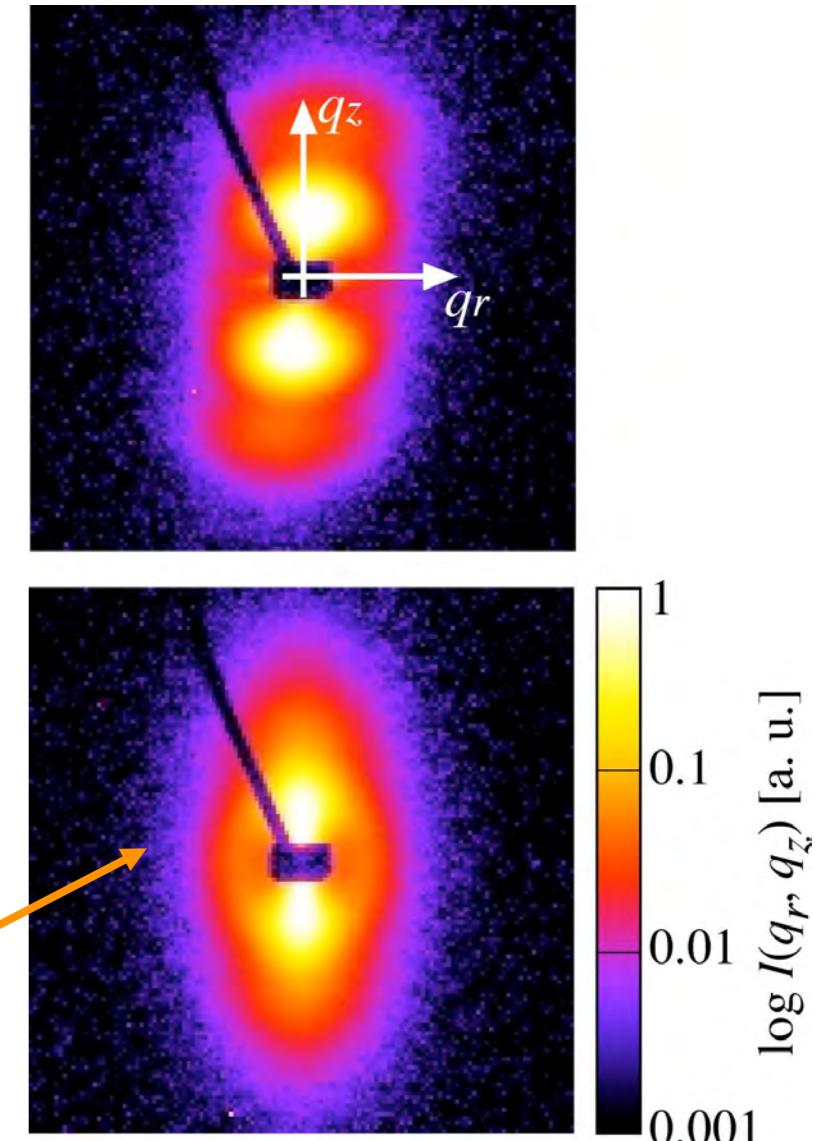
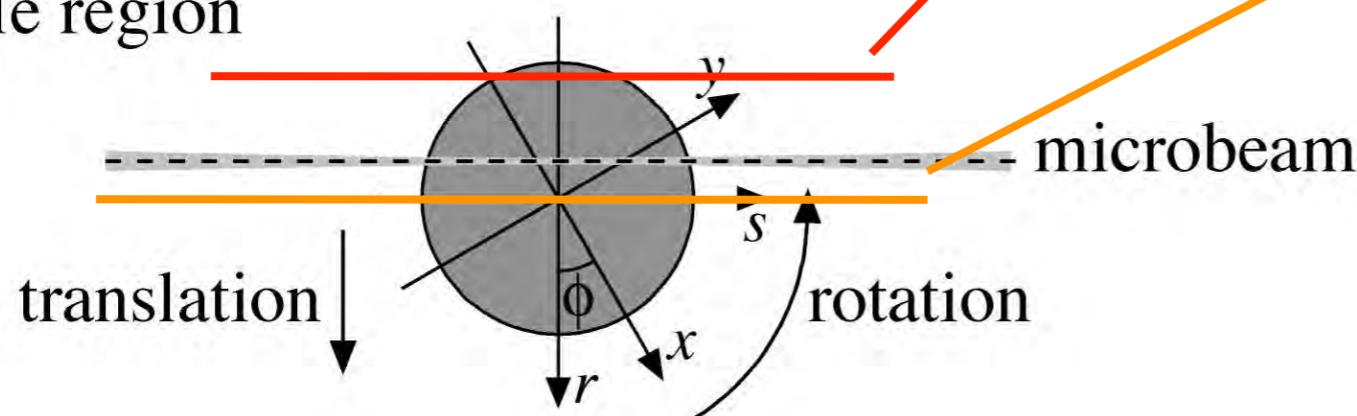
C. Schroer, et al., Appl. Phys. Lett. **88**, 164102 (2006)

Tomographic Small-Angle X-Ray Scattering

(a) side view

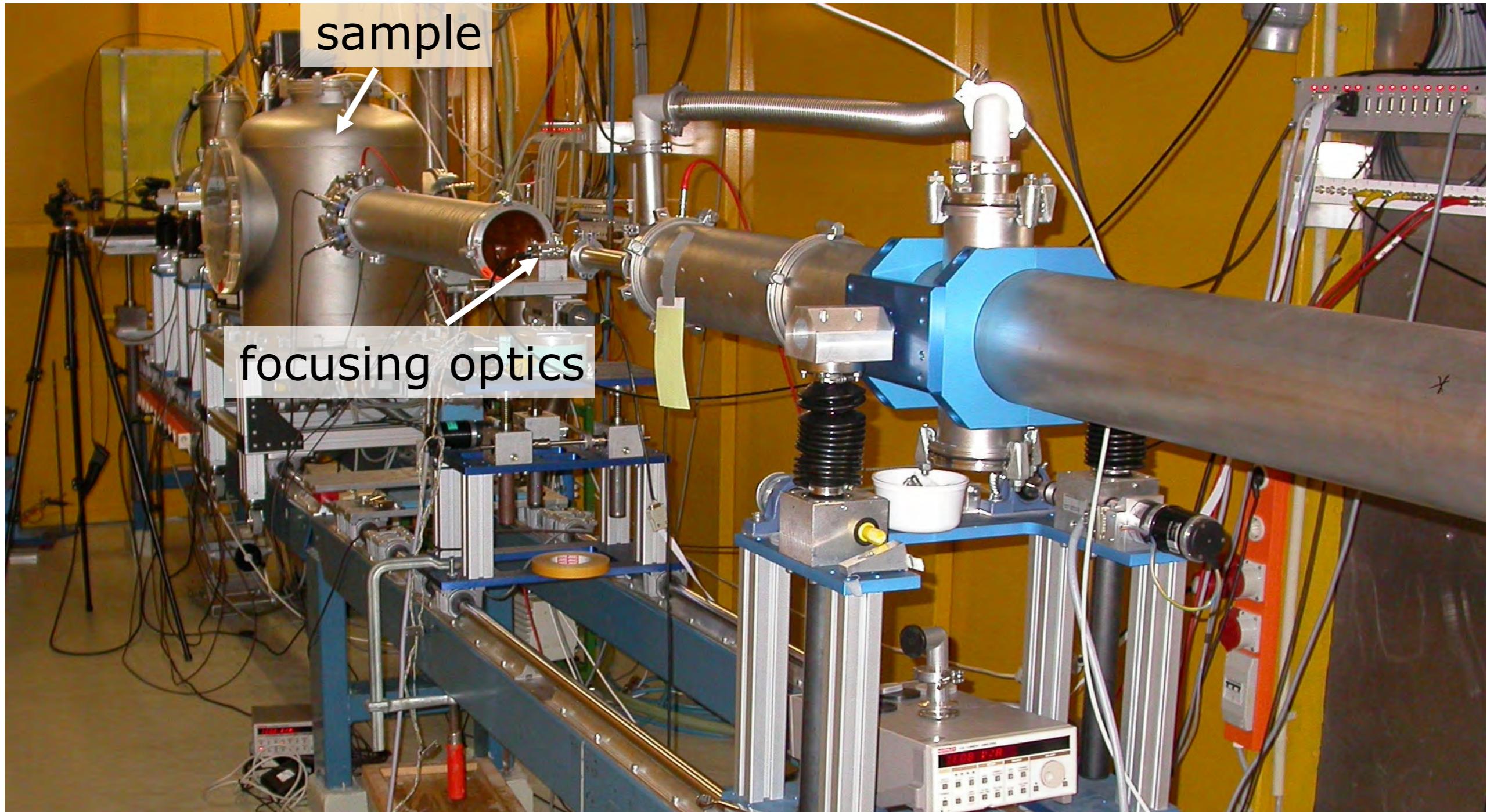


(b) top view of sample region

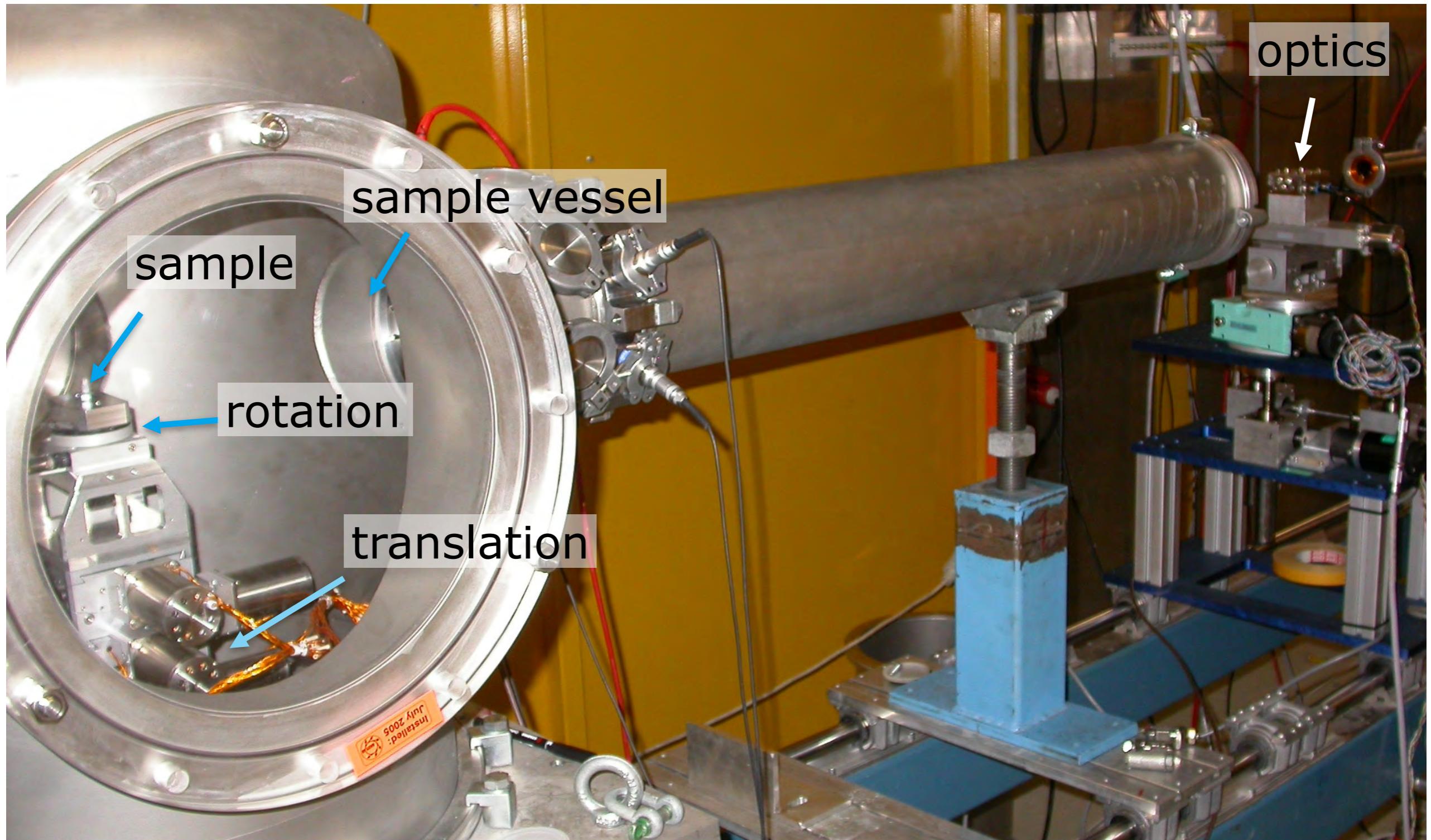


101 projection with
70 steps of
80 μm step size

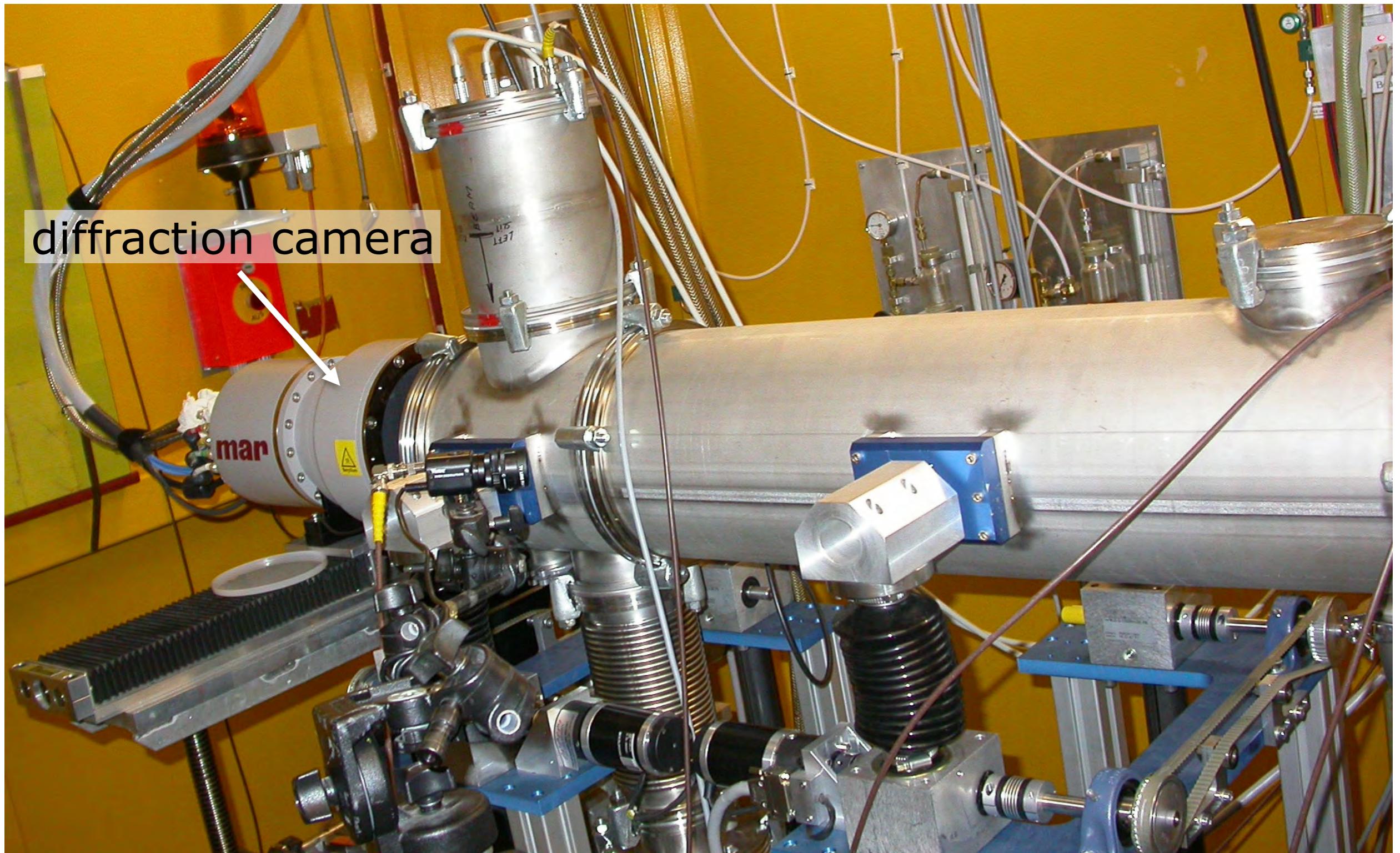
SAXS Tomography



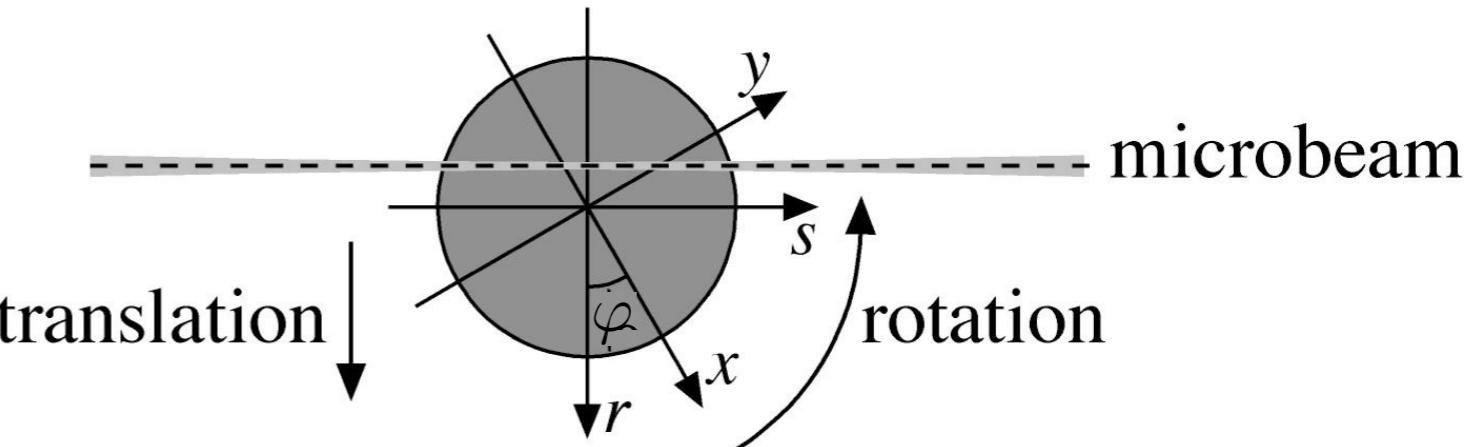
SAXS Tomography



SAXS Tomography



SAXS Tomography



Transmitted beam:

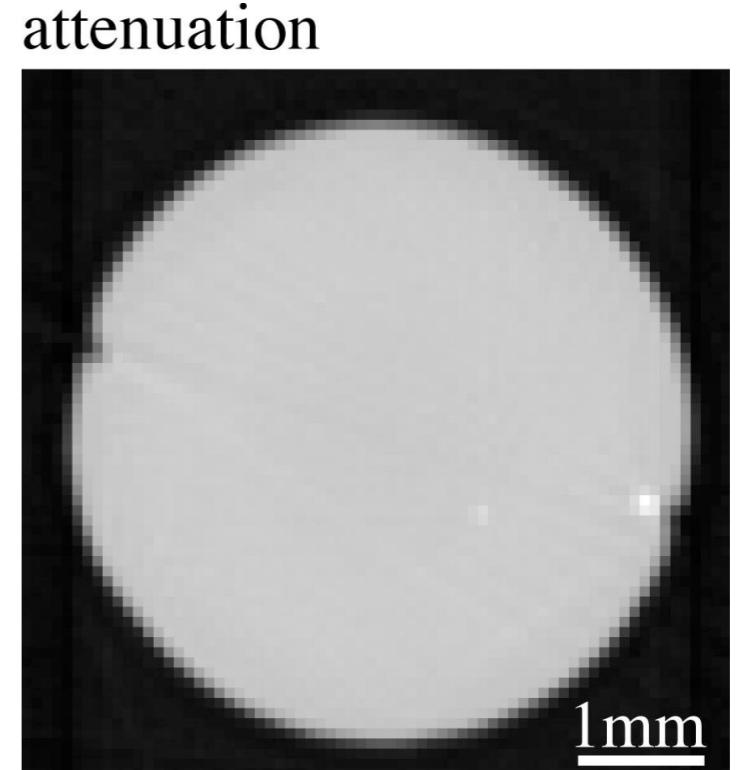
$$I_1(r, \varphi) = I_0 \exp \left\{ - \int ds' \mu [x(s', r), y(s', r)] \right\}$$

Standard tomography:

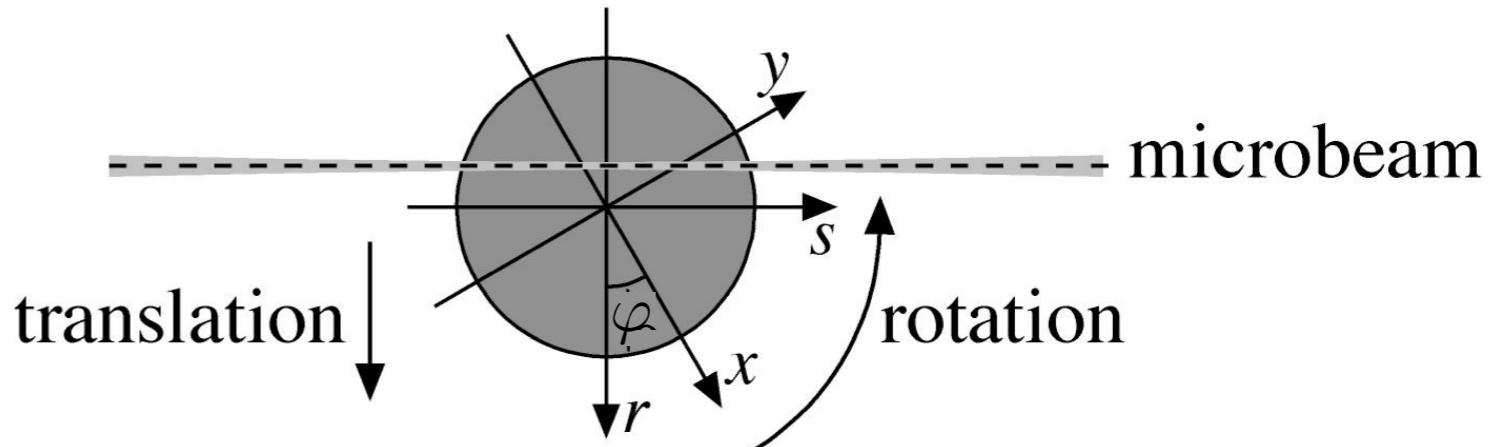
homogeneous density (polyethylene):

$$\rho = [0.88 \pm 0.04] \text{ g/cm}^3$$

C. Schroer, et al., Appl. Phys. Lett. **88**, 164102 (2006)



SAXS Tomography



scattered signal:

$$I_{\vec{q}}(r, \varphi) = I_0 \int ds f(\varphi, s, r) p_{\vec{q}, \varphi}(x, y) g(\varphi, s, r)$$

attenuation of primary beam:

$$f(\varphi, s, r) = \exp \left\{ - \int_{-\infty}^s ds' \mu(x, y) \right\}$$

attenuation of scattered beam

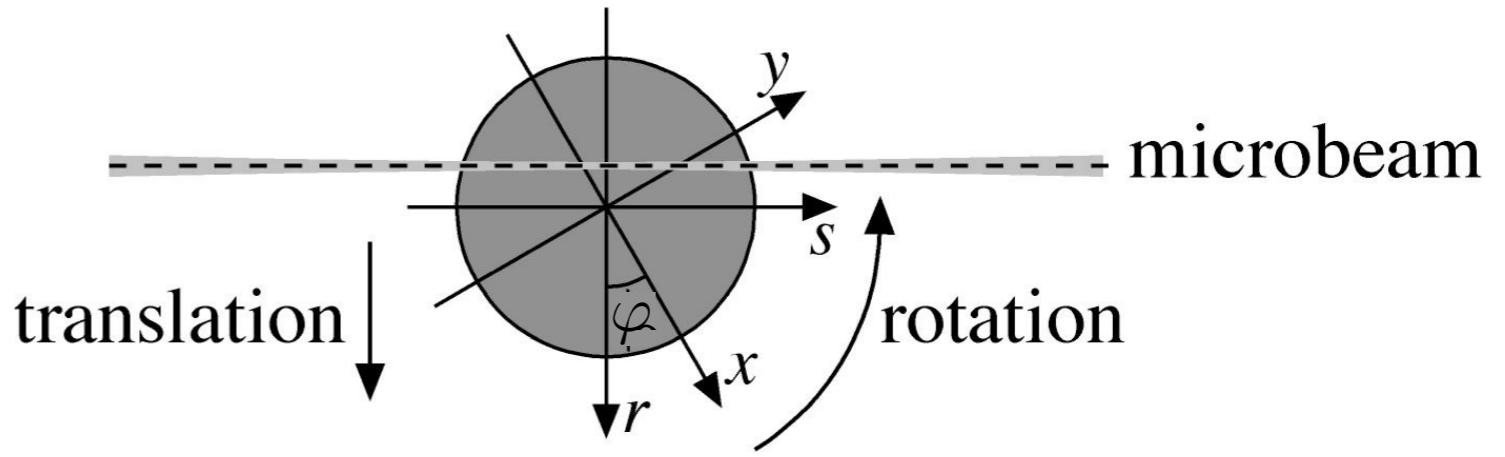
$$g(\varphi, s, r) = \exp \left\{ - \int_s^{\infty} ds' \mu(x, y) \right\}$$

Diffraction signal in forward direction:

$$I_1(r, \varphi) = I_0(r, \varphi) \cdot f(\varphi, s, r) \cdot g(\varphi, s, r) \quad \text{independent of } s$$

C. Schroer, et al., Appl. Phys. Lett. **88**, 164102 (2006)

SAXS Tomography



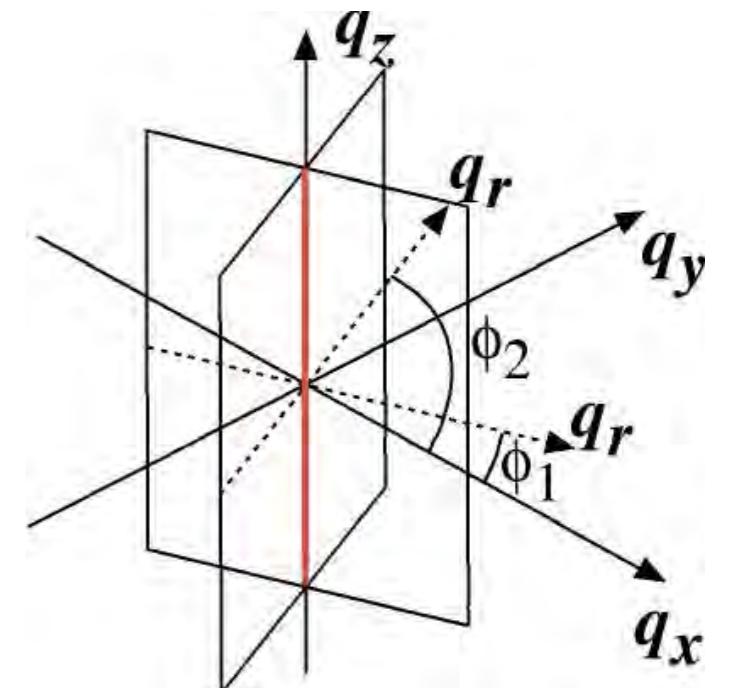
scattered signal:

$$I_{\vec{q}}(r, \varphi) = I_1 \int ds p_{\vec{q}, \varphi}(x, y)$$

tomography works only if $p_{\vec{q}, \varphi}(x, y)$ is independent φ

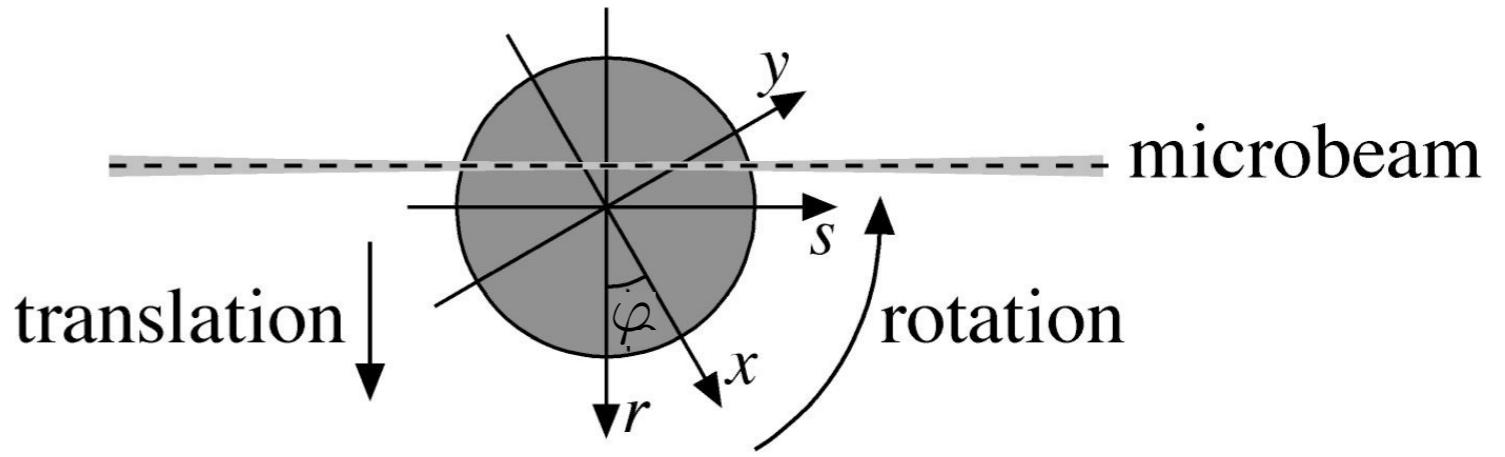
general case: $p_{\vec{q}, \varphi}(x, y)$ complicated function

reconstruction only for $q_r = 0$
(q along rotation axis)



C. Schroer, et al., Appl. Phys. Lett. **88**, 164102 (2006)

SAXS Tomography



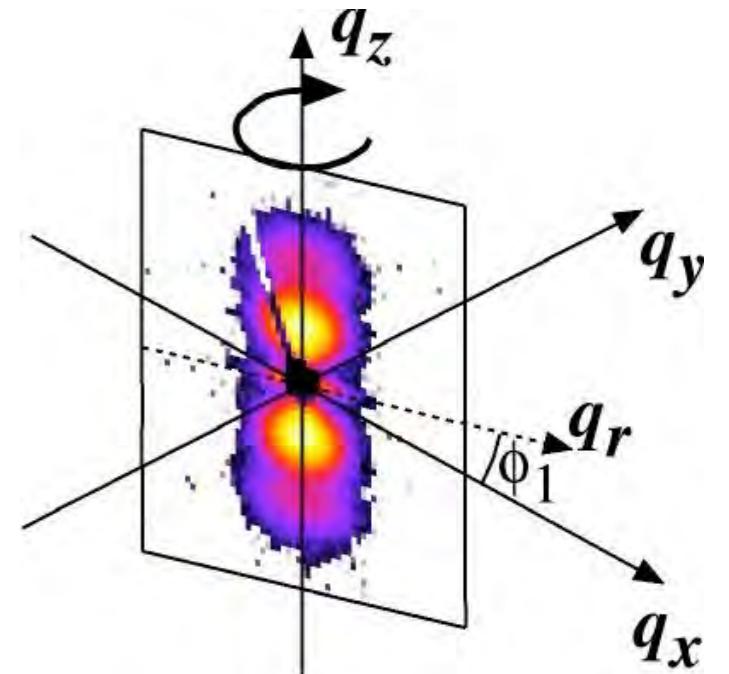
scattered signal:

$$I_{\vec{q}}(r, \varphi) = I_1 \int ds p_{\vec{q}, \varphi}(x, y)$$

tomography works only if $p_{\vec{q}, \varphi}(x, y)$ is independent φ

special case: $p_{\vec{q}, \varphi}(x, y)$ has rotation symmetry
around rotation axis

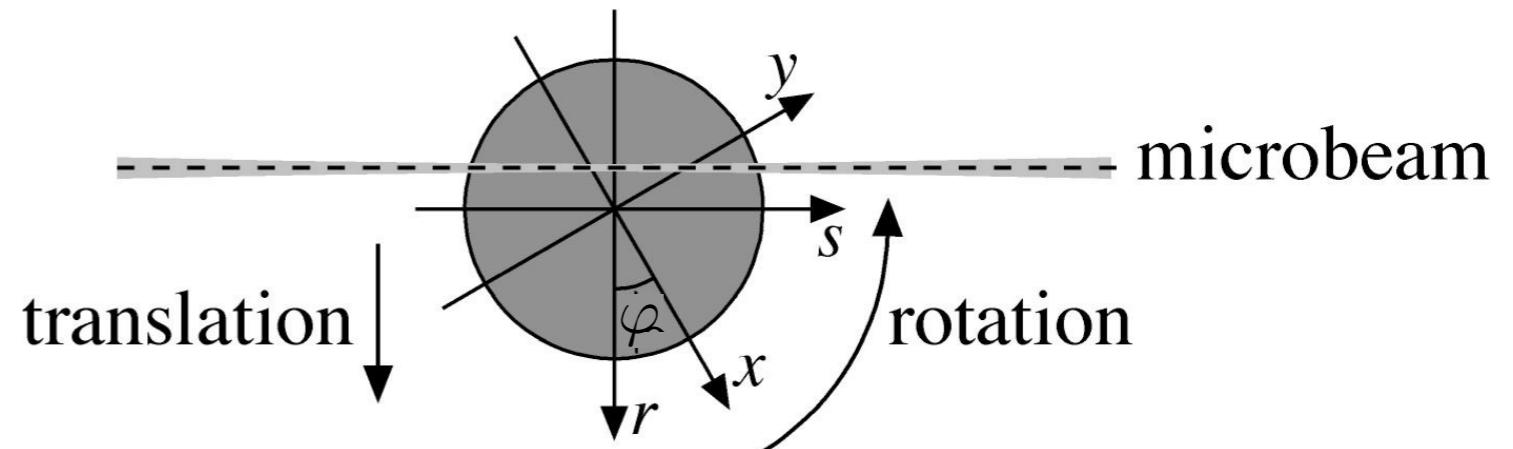
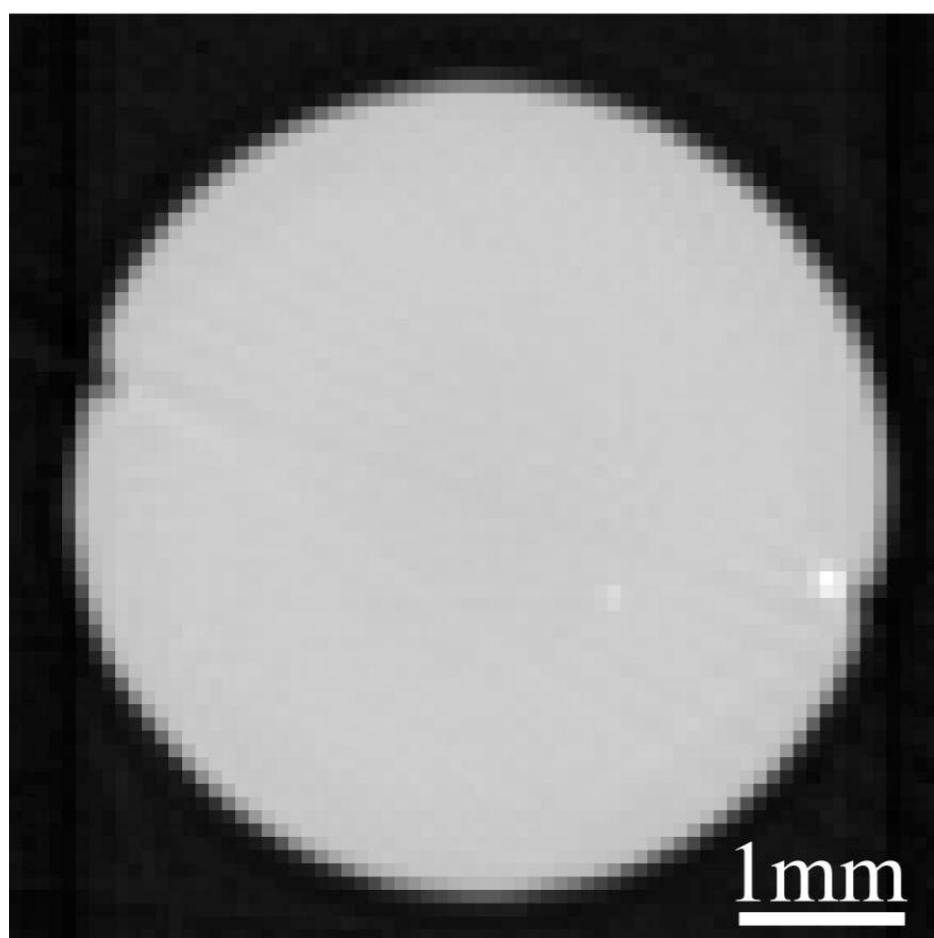
reconstruction of full SAXS cross section
in the vicinity of $q = 0$



C. Schroer, et al., Appl. Phys. Lett. **88**, 164102 (2006)

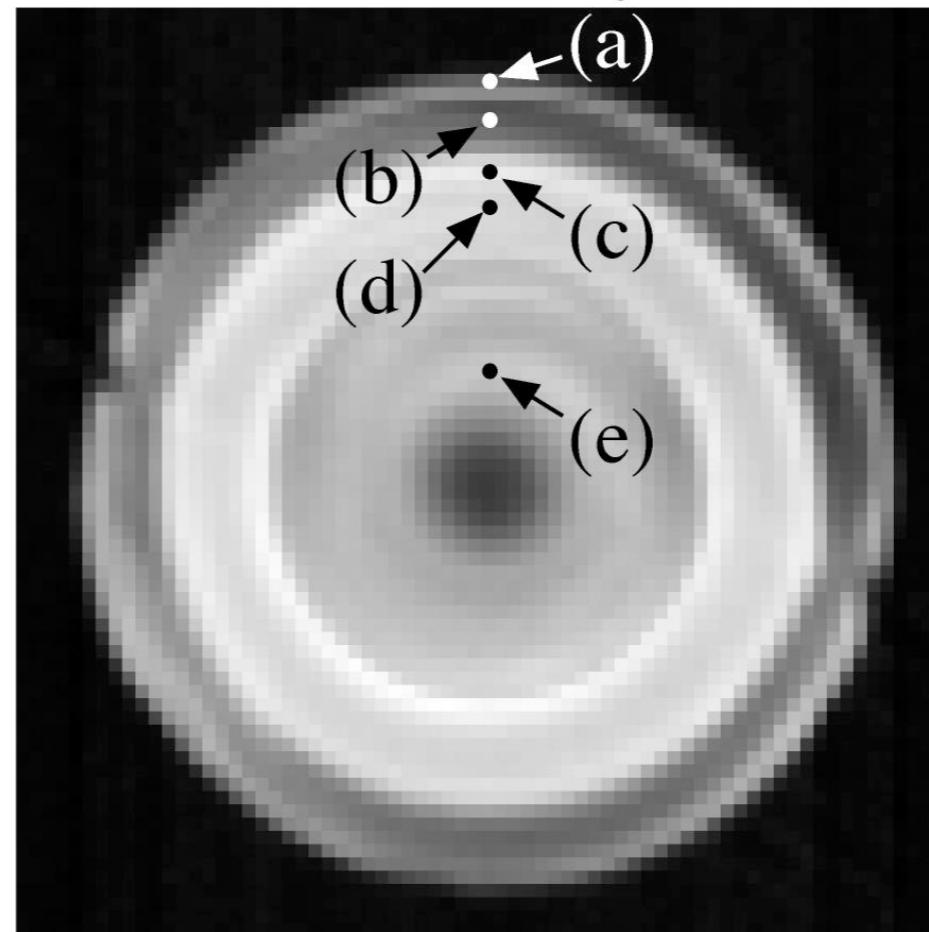
SAXS Tomography

reconstruction:



attenuation

scattered intensity

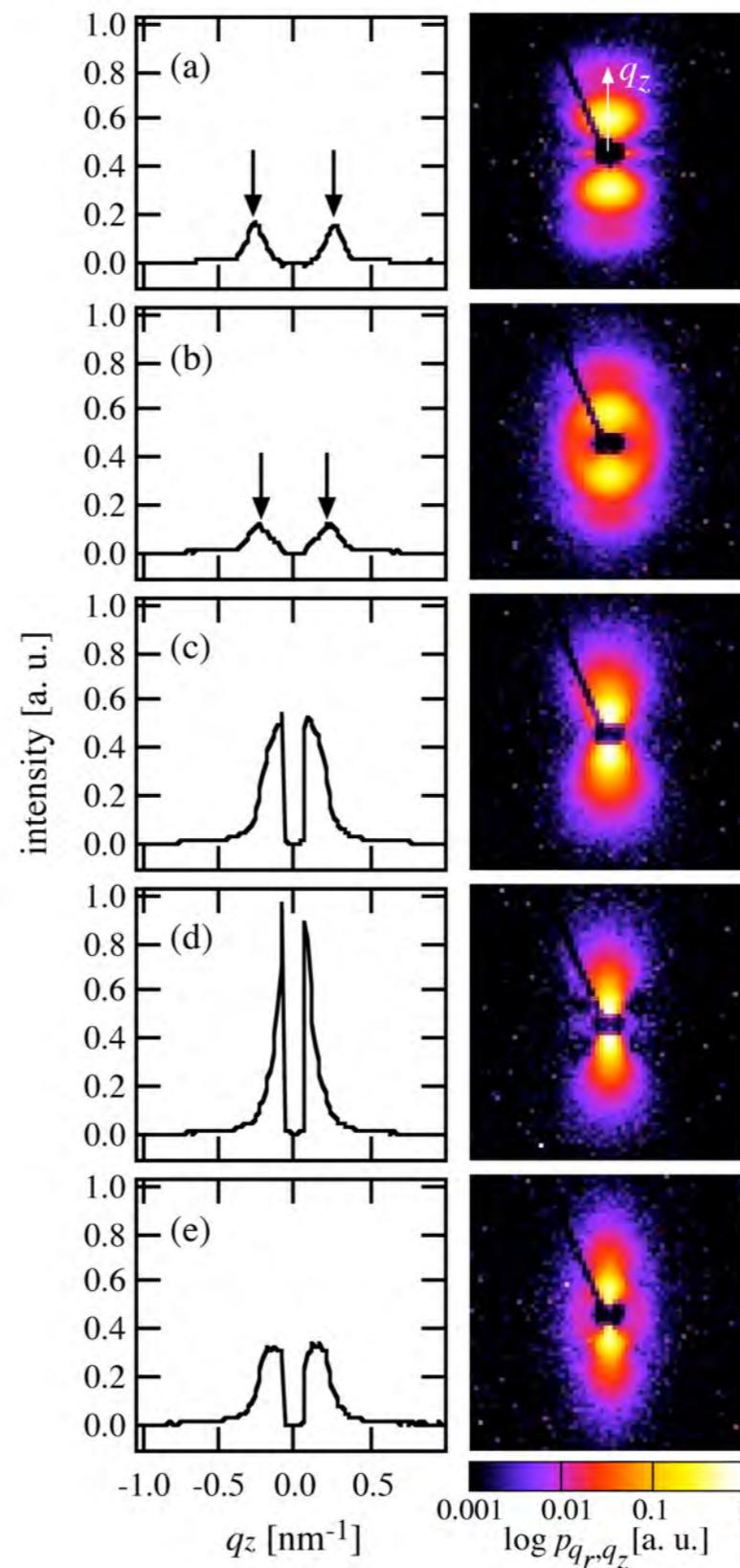
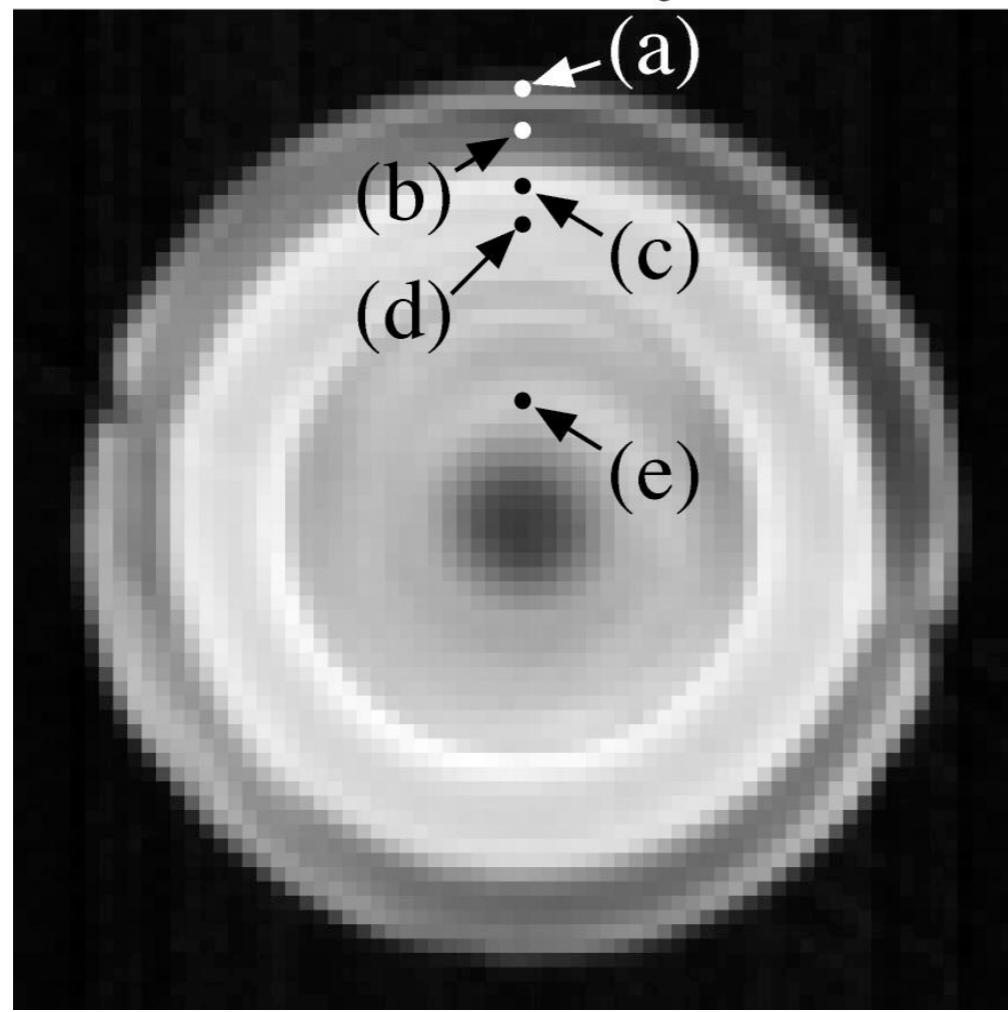


integral scattering
cross section
along rotation axis

SAXS Tomography

Sample with fibre texture:

scattered intensity

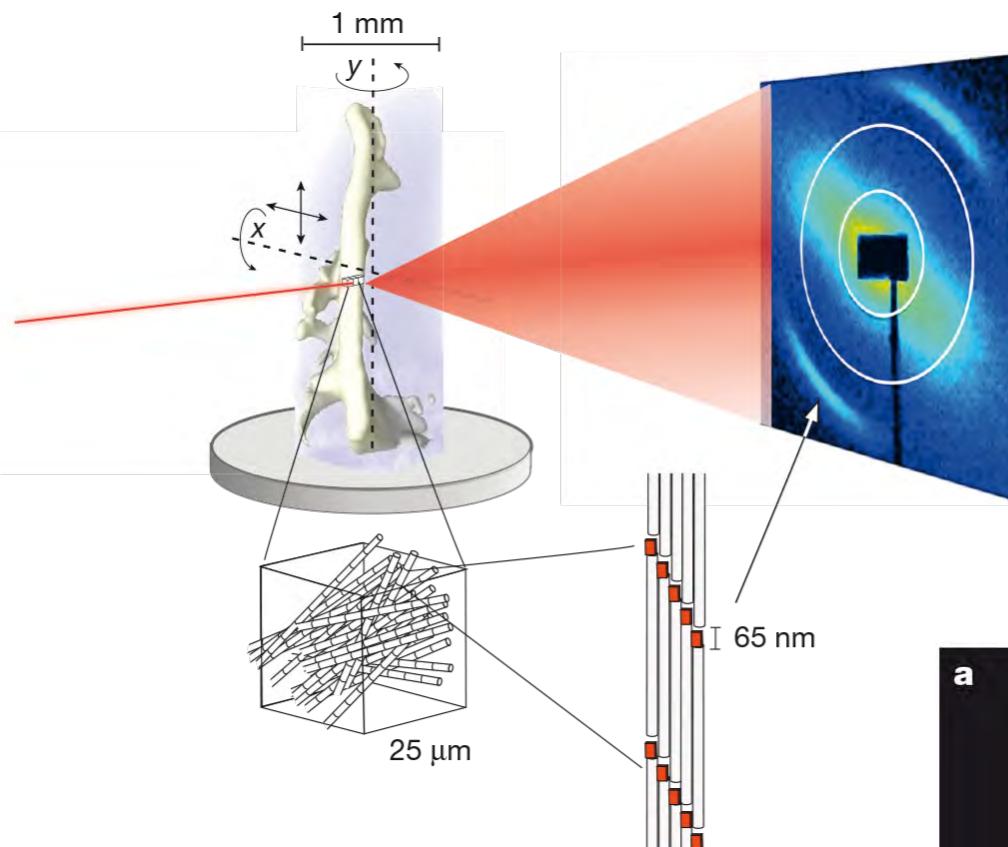


inhomogeneous nanostructure

scattering cross section
in each pixel
(rotation symmetry)!

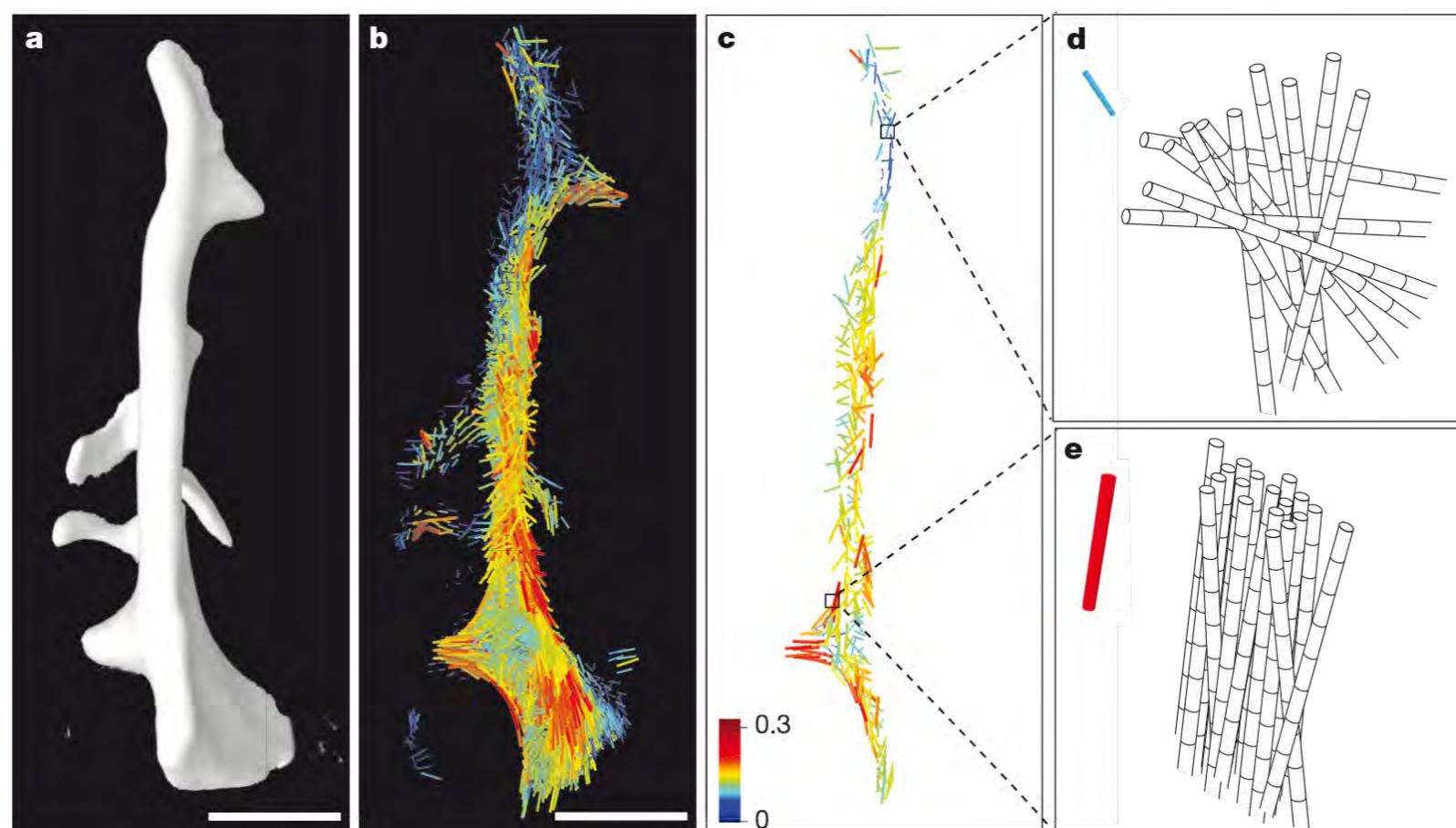
C. Schroer, et al., Appl. Phys. Lett. **88**, 164102 (2006)

SAXS Tomography in 3D



general SAXS-tomographic oroblem

in general: measure 6 dimensional information!
Scan in 4 dimensions and record 2D patterns
(coarse mesh due to time limitations)



Liebi, M., et al.,
Nature, **527**(7578),
349–352. (2015).

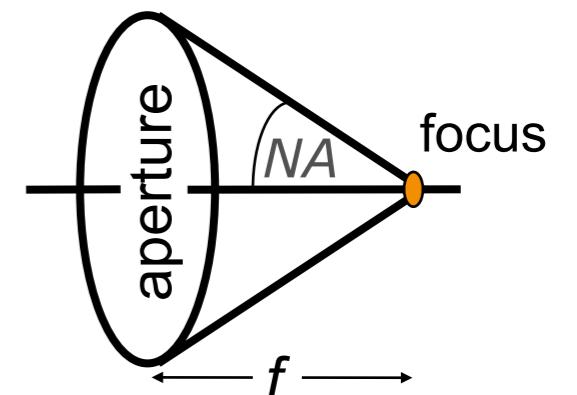
Conventional X-Ray Microscopy

X-ray microscopy as a quantitative local measurement:

- > Full-field microscopy: attenuation and phase contrast
 - measure complex refractive index of sample
- > scanning microscopy:
 - all x-ray analytical techniques can be used as contrast:
 - > x-ray fluorescence (XRF): chemical composition (quantitative analysis)
 - > x-ray absorption spectroscopy (XAS): chemical state of given element (e. g. oxidation)
 - > x-ray diffraction and scattering (SAXS & WAXS): local nanostructure
 - > ...

Full-field and scanning microscopy require x-ray optics

- resolution limited by numerical aperture of optics



Tomorrow: what are the limits and how can we overcome them?