

# Introduction to Accelerator Physics

## Part 3

Pedro Castro / Accelerator Physics Group (MPY)  
Hamburg, 26th July 2022



# Accelerator lectures framework in Summer Student Prog.

18th and 19th Aug.: Future accelerators:

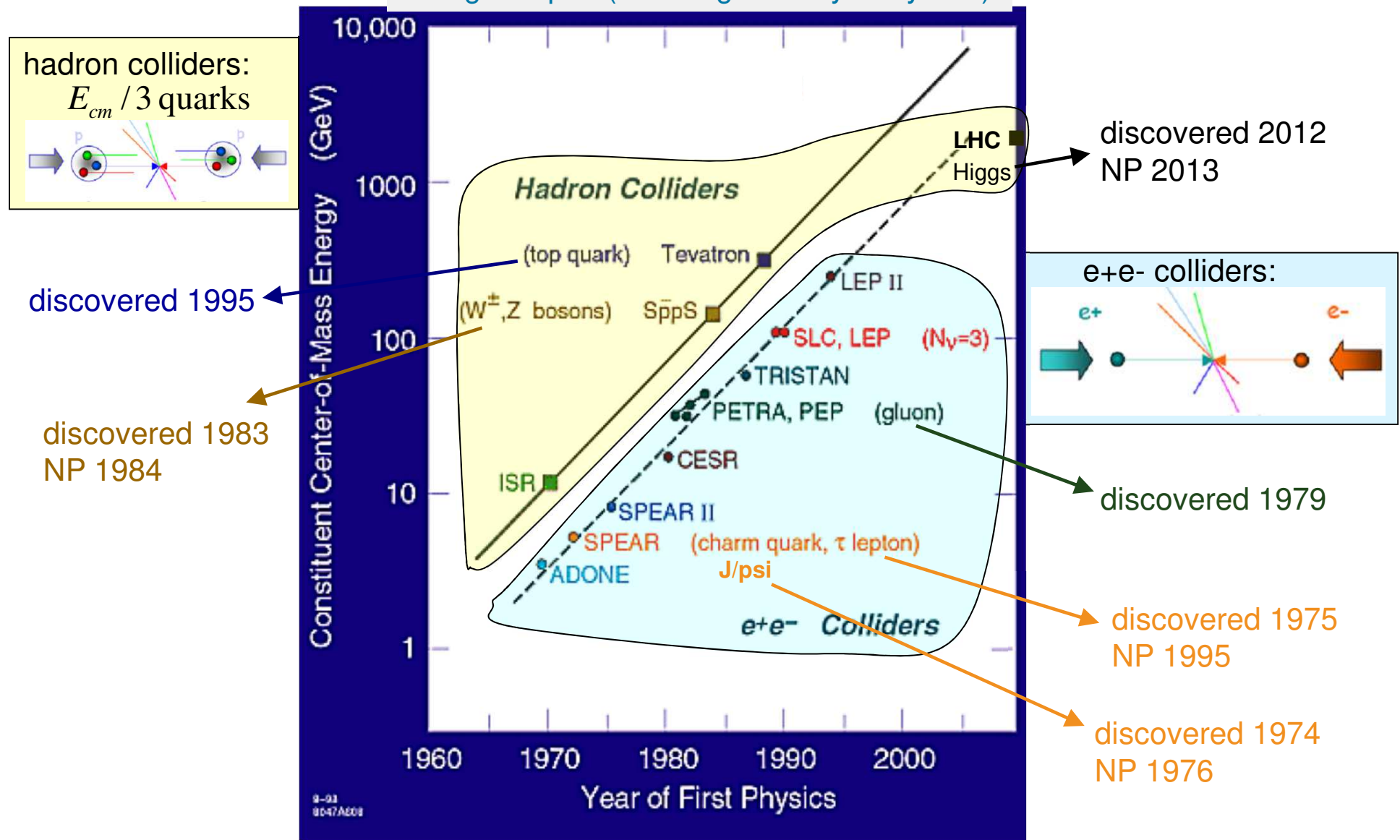
- Future colliders for the energy frontier, K. Buesser
- Plasma accelerators, J. Osterhoff

Today: focus on present day and last 50 years accelerator technology

**synchrotrons: machines for discoveries**

# Main HEP discoveries at synchrotrons in the last 50 years

Livingston plot (doubling E every 3.5 years)



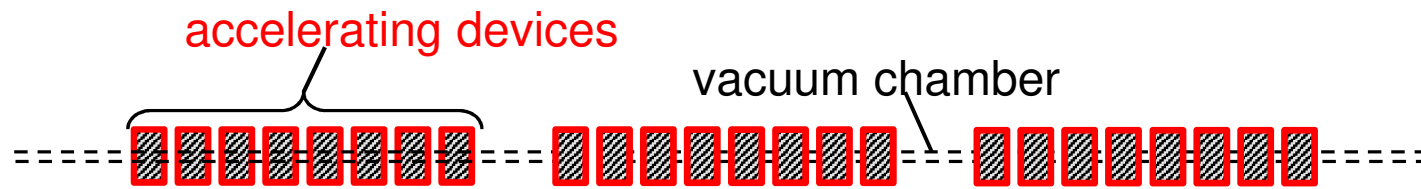
# Scope of this lecture:

## 1. Synchrotrons: key components and their challenges to reach high energies:

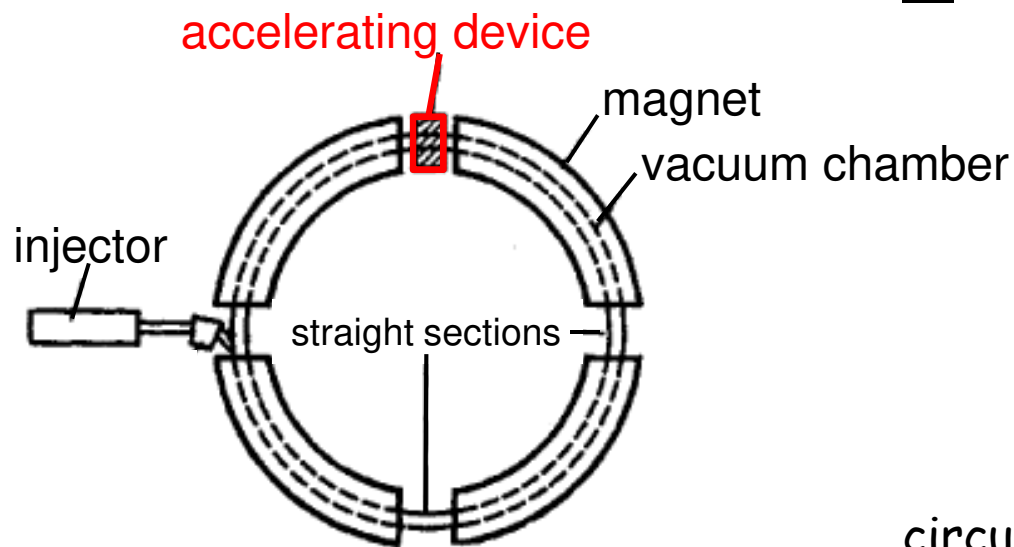
- Dipole magnetic fields
  - Superconducting dipoles
  - Quadrupole magnets to focus beams
- Part 4
- Part 2, yesterday

## 2. Synchrotrons and Linear Accelerators:

- Acceleration using radio-frequency electromagnetic fields
- Part 3



linear accelerator (linac)



circular accelerator: synchrotron

# Motion in electric and magnetic fields

Equation of motion under Lorentz Force

$$\frac{d\vec{p}}{dt} = \vec{F} = q (\vec{E} + \vec{v} \times \vec{B})$$

The diagram shows the Lorentz force equation with arrows pointing from text labels to the corresponding terms in the equation. A bracket under the first three terms is labeled 'of the particle'.

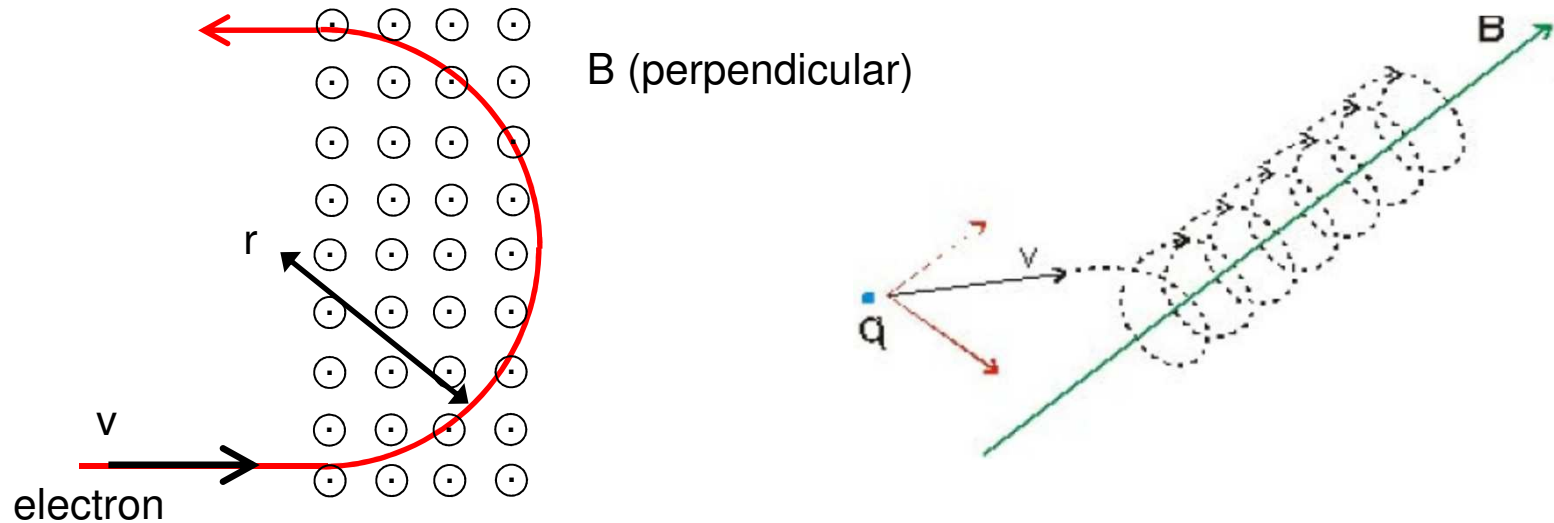
- $\frac{d\vec{p}}{dt}$  is labeled 'momentum'.
- $\vec{F}$  is labeled 'charge'.
- $q$  is labeled 'charge'.
- $\vec{E}$  is labeled 'electric field'.
- $\vec{v}$  is labeled 'velocity'.
- $\vec{B}$  is labeled 'magnetic field'.

of the particle

# Motion in magnetic fields

if the electric field is zero ( $\vec{E} = 0$ ), then

$$\vec{F} = \frac{d\vec{p}}{dt} = q \cdot \vec{v} \times \vec{B} \quad \rightarrow \quad \vec{F} \perp \vec{v}$$



Magnetic fields do not change the particles energy

# Motion in magnetic fields

if the electric field is zero ( $E=0$ ), then

$$\vec{F} = \frac{d\vec{p}}{dt} = q \cdot \vec{v} \times \vec{B}$$

$$E^2 = \vec{p}^2 c^2 + E_0^2$$

energy-momentum relation in special relativity

total energy

momentum

energy at rest


The diagram shows the equation  $E^2 = \vec{p}^2 c^2 + E_0^2$ . Three arrows point from labels below to terms in the equation: one from 'total energy' to  $E^2$ , one from 'momentum' to  $\vec{p}^2$ , and one from 'energy at rest' to  $E_0^2$ . The text 'energy-momentum relation in special relativity' is placed to the right of the equation.




# Motion in magnetic fields

if the electric field is zero ( $E=0$ ), then

$$\vec{F} = \frac{d\vec{p}}{dt} = q \cdot \vec{v} \times \vec{B}$$

$$E^2 = \vec{p}^2 c^2 + E_0^2$$

$$E \frac{dE}{dt} = c^2 \vec{p} \frac{d\vec{p}}{dt} = c^2 q \vec{p} (\vec{v} \times \vec{B}) = c^2 q |\vec{p}| |\vec{v} \times \vec{B}| \cos \phi = 0$$

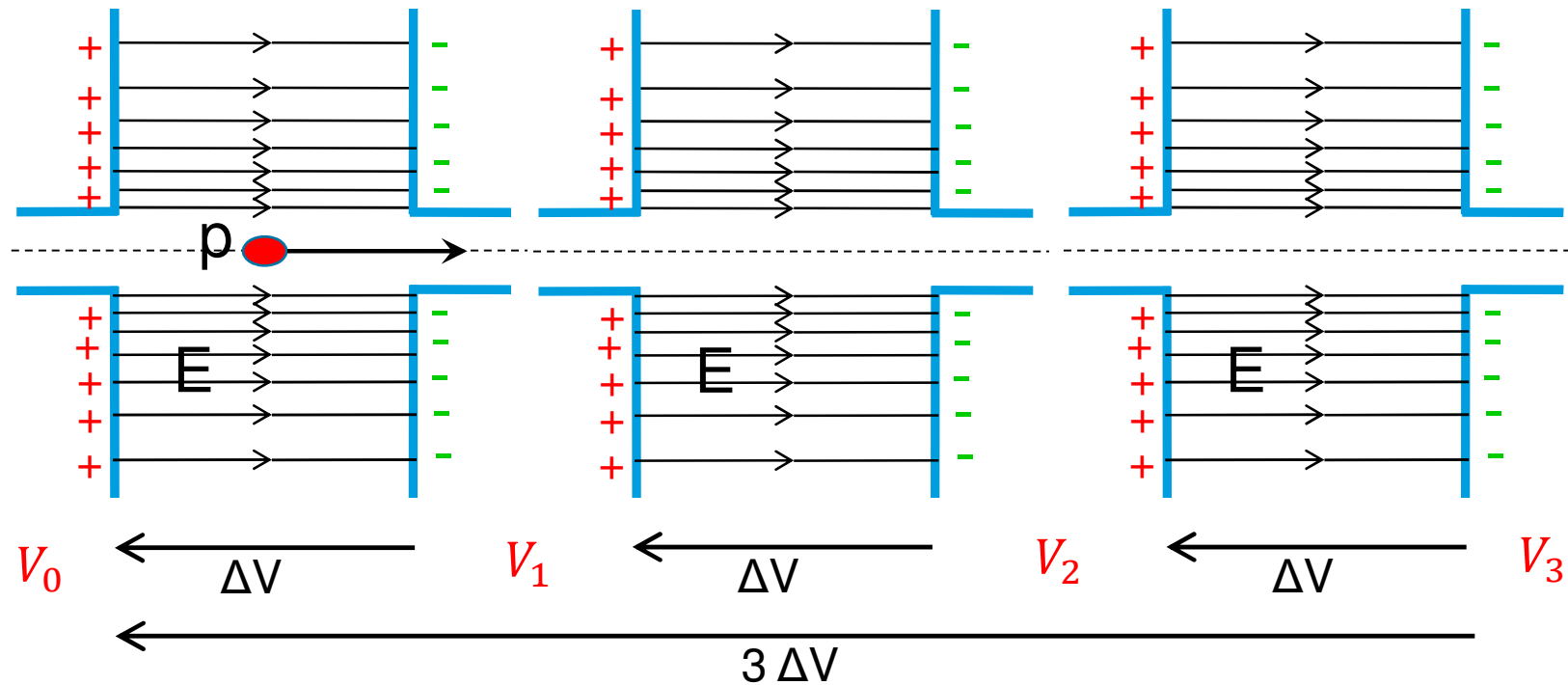
since  $\vec{v} \times \vec{B} \perp \vec{v} \rightarrow \phi = 90^\circ$  

Magnetic fields do not change the particles energy, only electric fields do !

In general:

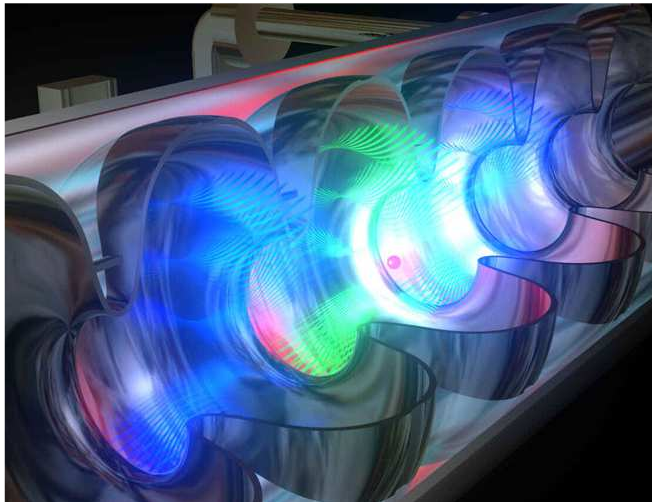
- Static magnetic fields → to guide (bend + focus) particle beams

# acceleration with DC electric fields

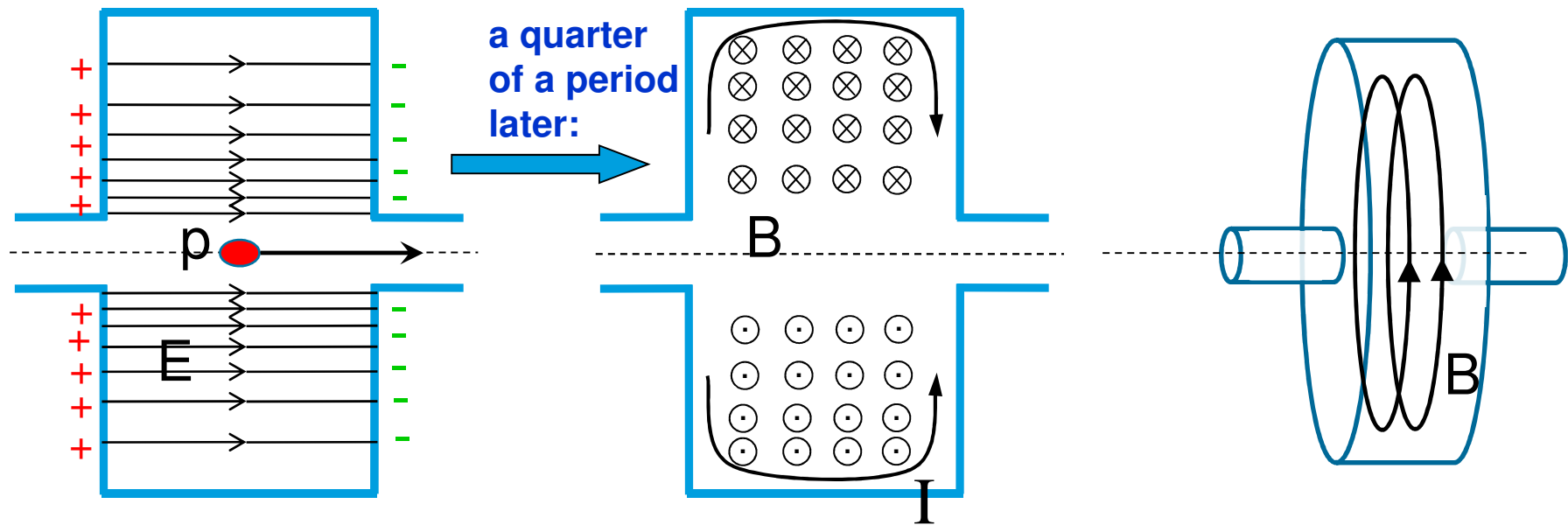


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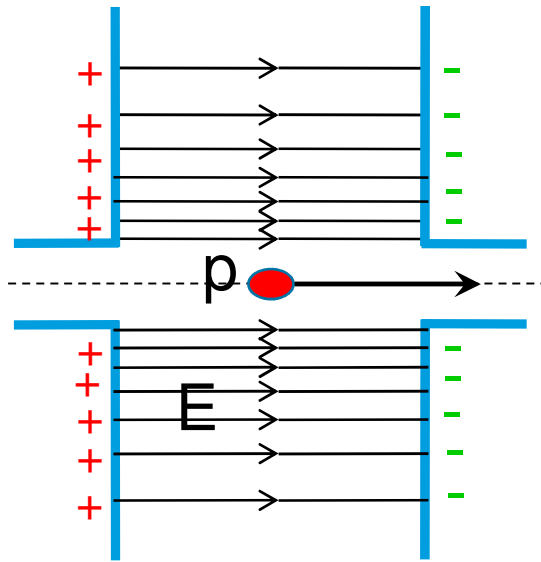
- Static magnetic fields  $\rightarrow$  to guide (bend + focus) particle beams
- Static electric fields  $\rightarrow$  accelerate particle beams (low energy)
- Radio-frequency EM fields  $\rightarrow$  accelerate particle beams (high E)



# RF cavity basics: a cylindrical cavity

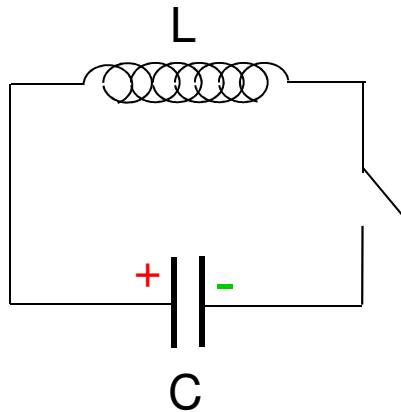


# RF cavity basics: a cylindrical cavity

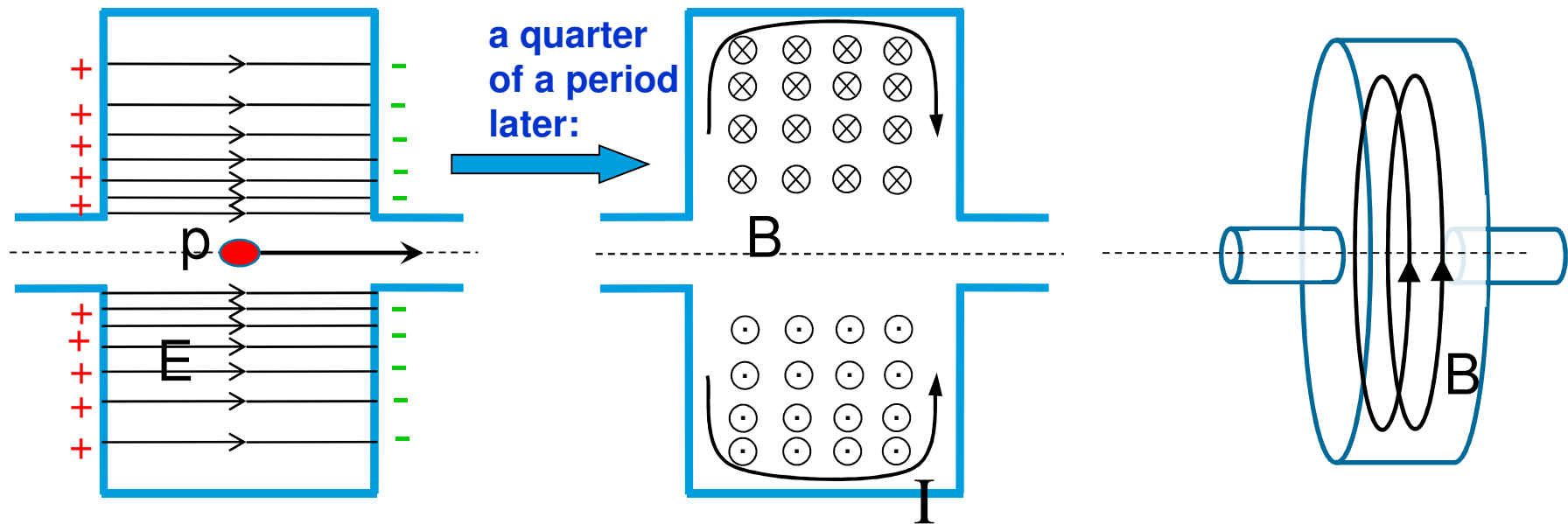


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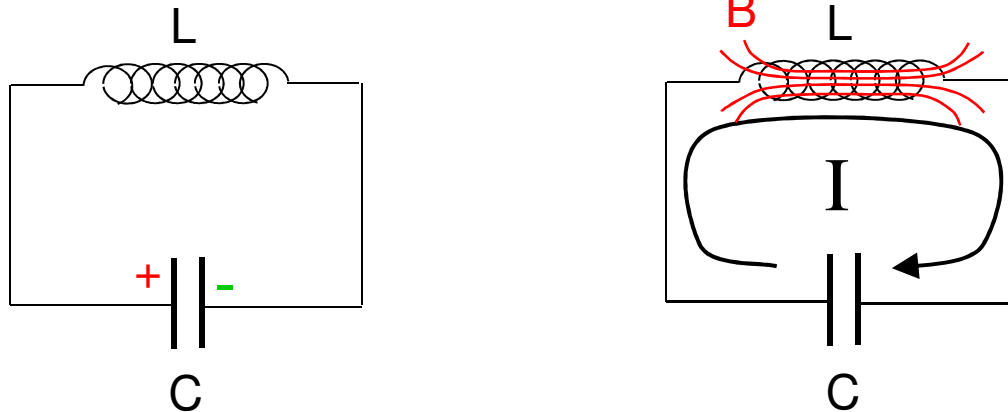
LC circuit (or resonant circuit) analogy:



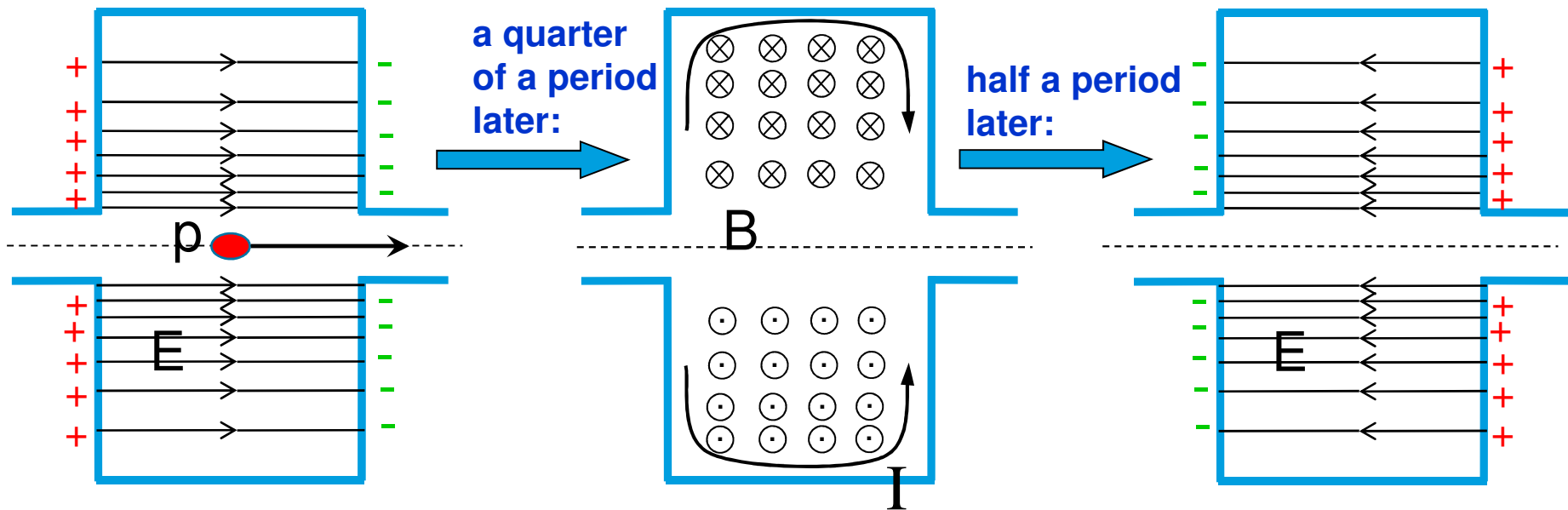
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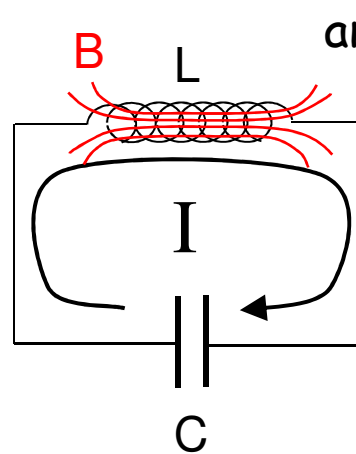
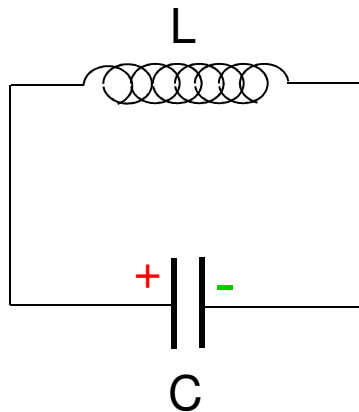
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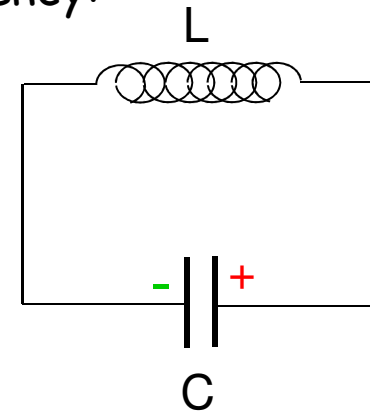


LC circuit (or resonant circuit) analogy:



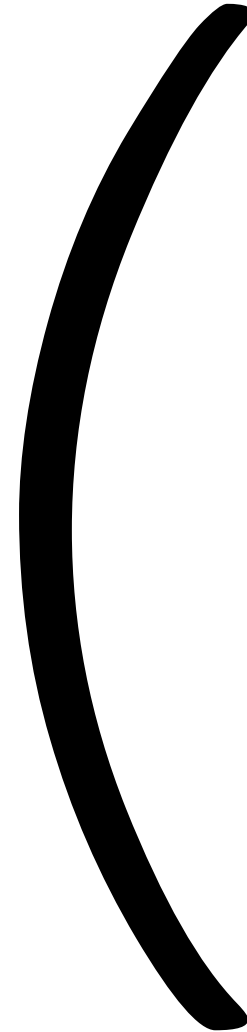
angular frequency:

$$\omega = \frac{1}{\sqrt{LC}}$$





# Equations for the electric and magnetic fields in a pill box cavity



## Maxwell's equations

(differential formulation in SI units)

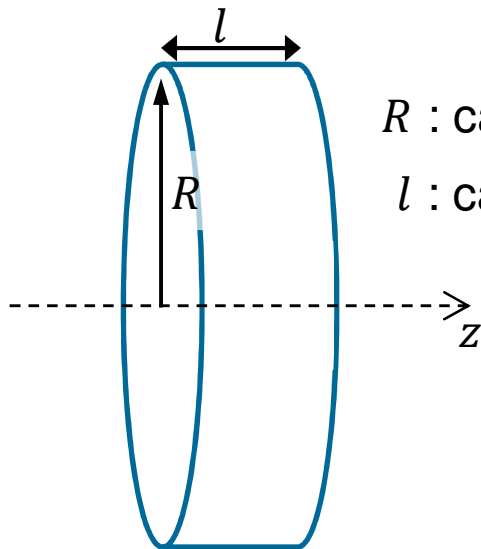
$$\vec{\nabla} \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \times \vec{B} = \mu_0 \vec{J} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

+ boundary conditions



$R$  : cavity radius

$l$  : cavity length

TM modes  
(transverse magnetic modes)

set of solutions with  $B_z = 0$  (that is,  $\vec{B}$  is transverse)

set of solutions with  $E_z = 0$  (that is,  $\vec{E}$  is transverse)

TE modes  
(transverse electric modes)

## Maxwell's equations (differential formulation in SI units)

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set of solutions with  $B_z = 0$  (that is,  $\vec{B}$  is transverse)

$$\left\{ \begin{array}{l} E_z = E_0 J_m \left( x_{mn} \frac{r}{R} \right) \cos m\theta \cos \left( \frac{p\pi}{l} z \right) e^{j\omega t} \\ E_r = -\frac{p\pi}{l} \frac{R}{x_{mn}} E_0 J'_m \left( x_{mn} \frac{r}{R} \right) \cos m\theta \sin \left( \frac{p\pi}{l} z \right) e^{j\omega t} \\ E_\theta = -\frac{p\pi}{l} \frac{mR^2}{x_{mn}^2 r} E_0 J_m \left( x_{mn} \frac{r}{R} \right) \sin m\theta \sin \left( \frac{p\pi}{l} z \right) e^{j\omega t} \\ B_z = 0 \\ B_r = -j\omega \frac{mR^2}{x_{mn}^2 r c^2} E_0 J_m \left( x_{mn} \frac{r}{R} \right) \sin m\theta \cos \left( \frac{p\pi}{l} z \right) e^{j\omega t} \\ B_\theta = -j\omega \frac{R}{x_{mn} c^2} E_0 J'_m \left( x_{mn} \frac{r}{R} \right) \cos m\theta \cos \left( \frac{p\pi}{l} z \right) e^{j\omega t} \end{array} \right.$$

indices:

$m = 0, 1, 2, \dots$  : number of full period variations in  $\theta$  of the fields

$n = 1, 2, \dots$  : number of zeros of the axial field component in  $\vec{r}$

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$J_m$  : Bessel's functions

$x_{mn}$  :  $n$ -th root of  $J_m$  (that is,  $J_m(x_{mn}) = 0$ )

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$$\text{angular frequency : } \omega = c \sqrt{\left( \frac{x_{mn}}{R} \right)^2 + \left( \frac{p\pi}{l} \right)^2}$$

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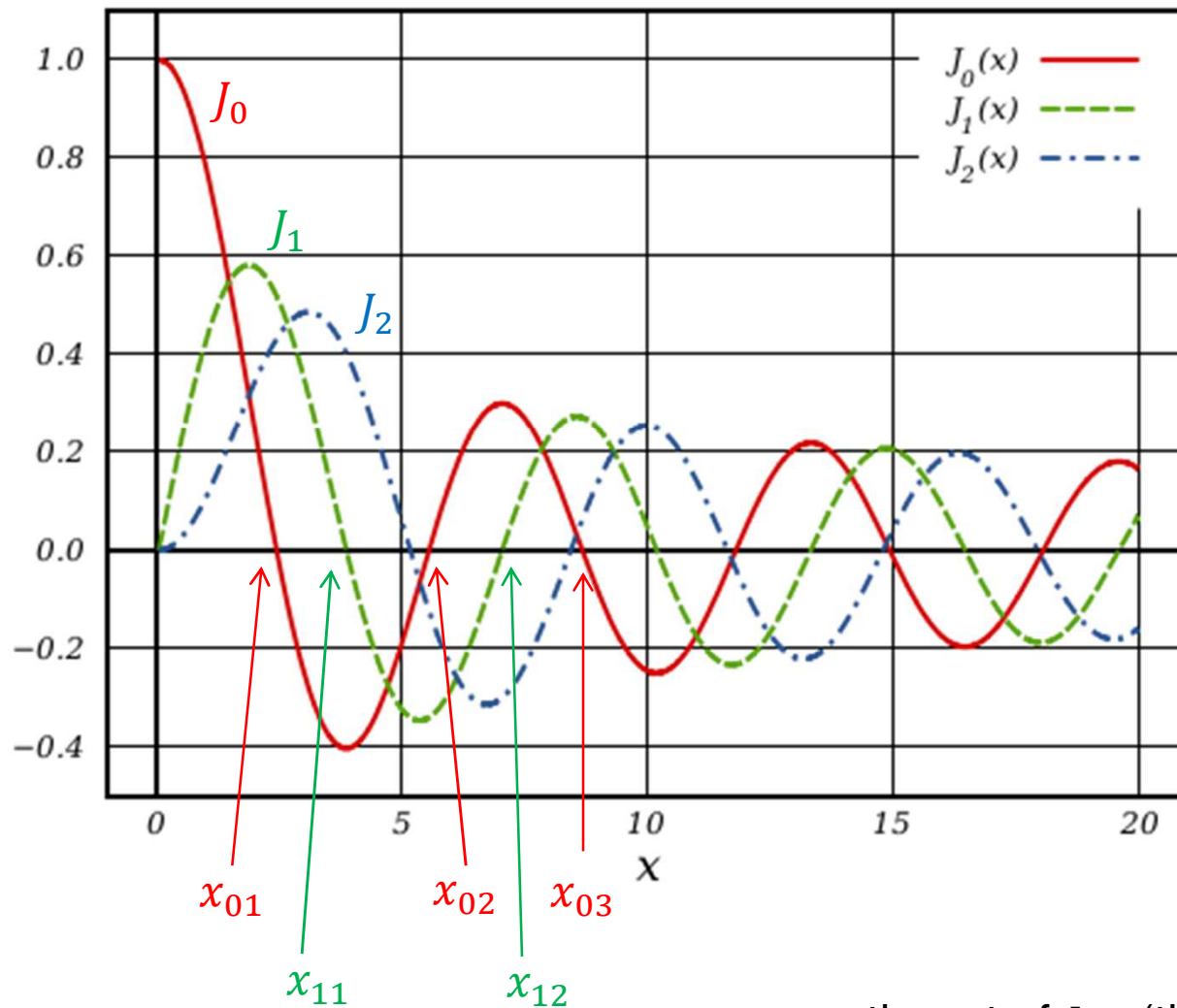
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## $J_m$ : Bessel's functions



$m$	$x_{m1}$	$x_{m2}$	$x_{m3}$
0	2.405	5.520	8.654
1	3.832	7.016	10.173
2	5.136	8.417	11.620

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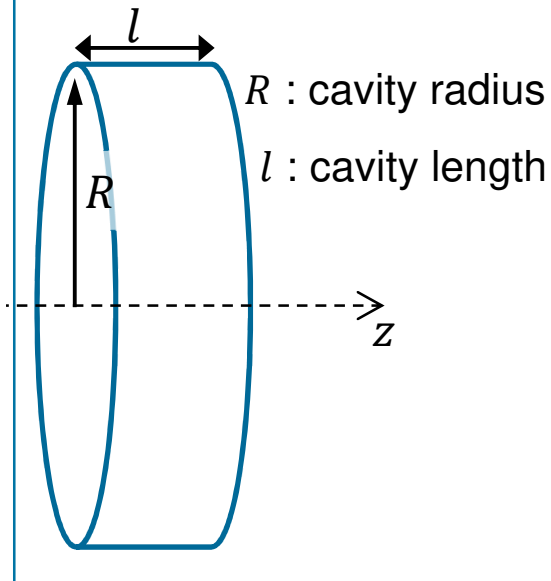
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$$\text{angular frequency : } \omega = c \sqrt{\left( \frac{x_{mn}}{R} \right)^2 + \left( \frac{p\pi}{l} \right)^2}$$



## boundary conditions



fundamental solution with  $B_z = 0$  (that is,  $\vec{B}$  is transverse)

$$E_z = E_0 J_0 \left( x_{01} \frac{r}{R} \right) e^{j\omega t}$$

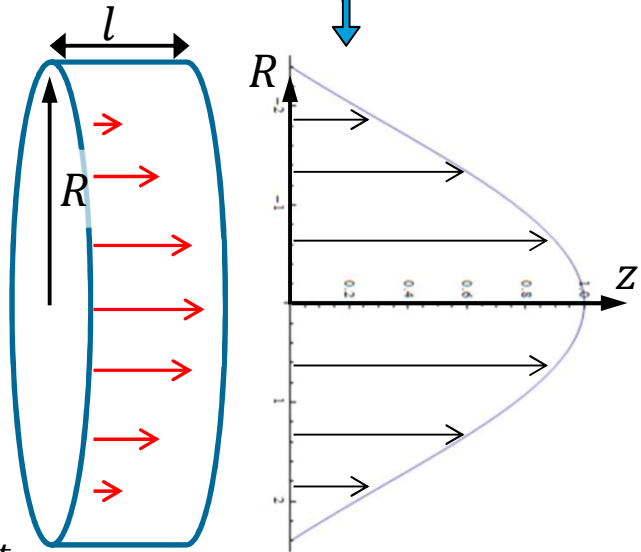
$$E_r = 0$$

$$E_\theta = 0$$

$$B_z = 0$$

$$B_r = 0$$

$$B_\theta = j\omega \frac{R}{x_{01} c^2} E_0 J_1 \left( x_{01} \frac{r}{R} \right) e^{j\omega t}$$



**$m = 0$  : rotation symmetry of the fields**

**$n = 1$  : no zeros of the axial field component in  $\vec{r}$**

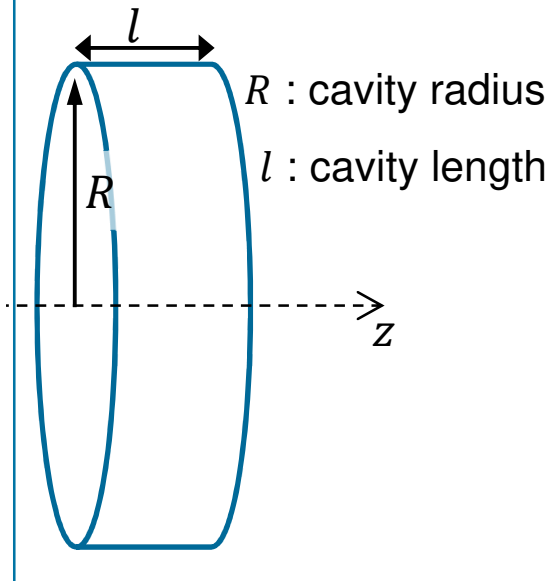
**$p = 0$  : no variation in  $z$  of the fields**

$J_m$  : Bessel's functions

$J'_m$  : derivative of the Bessel's functions

angular frequency :  $\omega = c \frac{x_{01}}{R}$        $x_{01} = 2.405$

## boundary conditions



fundamental solution with  $B_z = 0$  (that is,  $\vec{B}$  is transverse)

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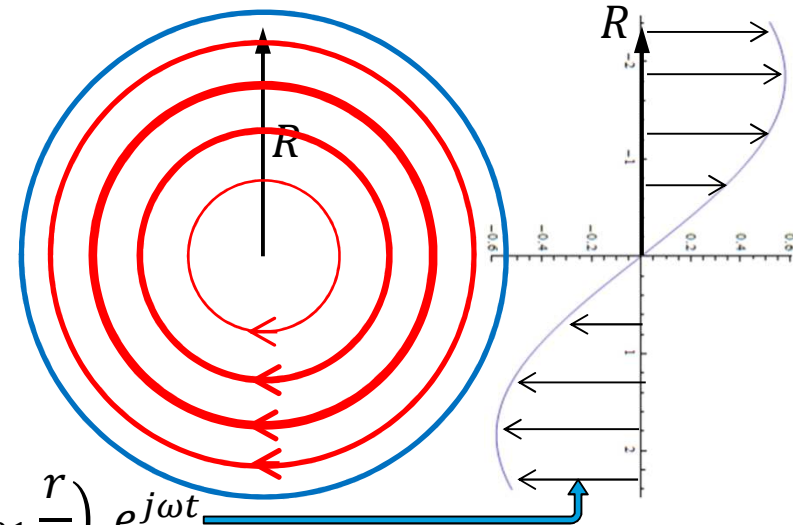
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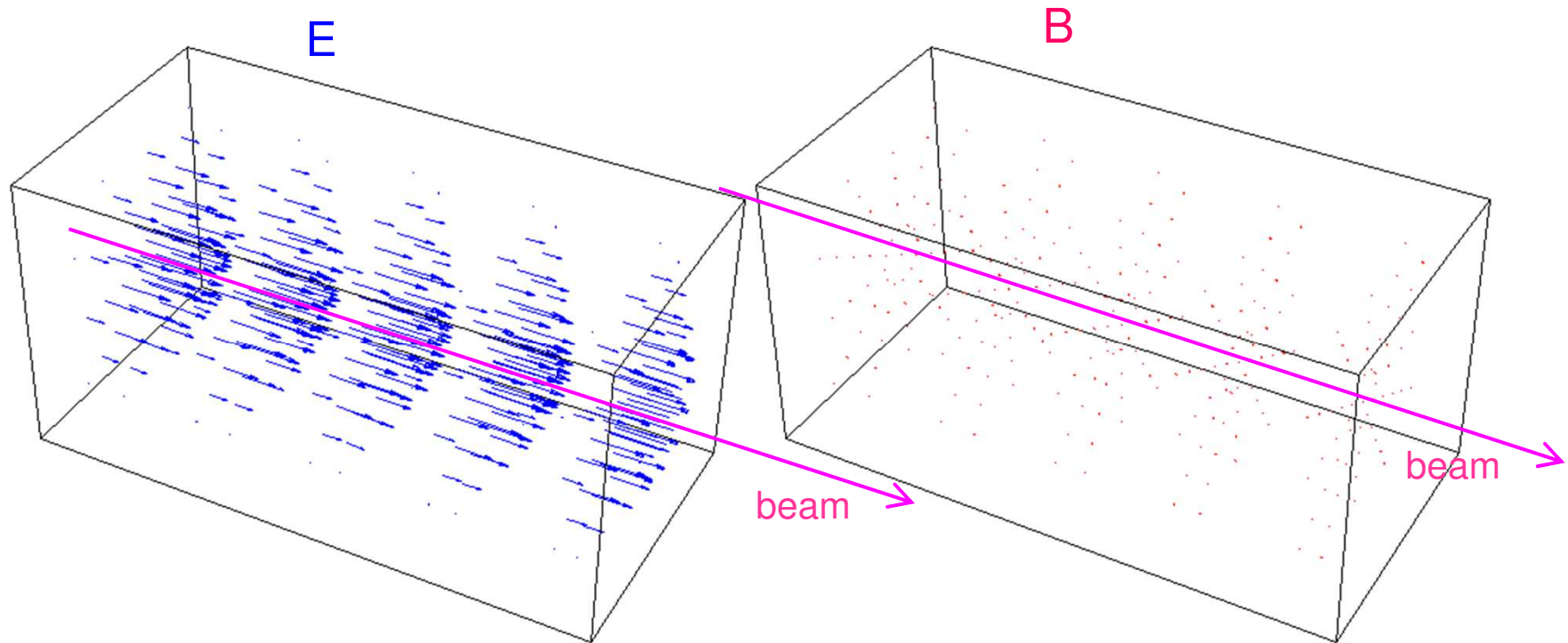
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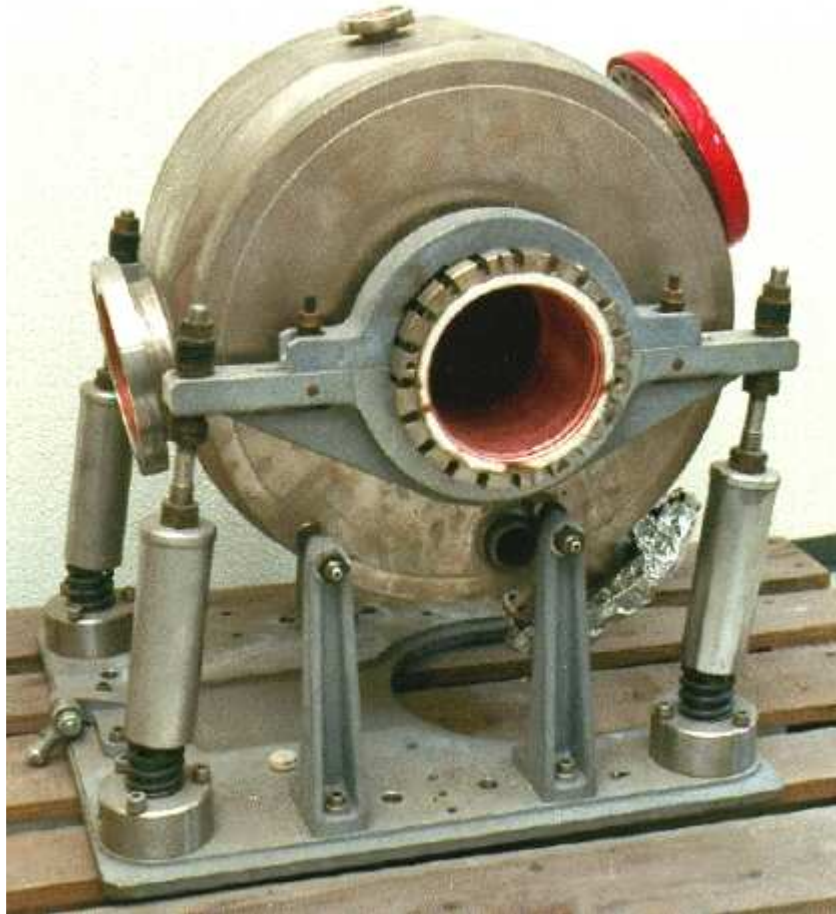
angular frequency :  $\omega = c \frac{x_{01}}{R}$        $x_{01} = 2.405$

# Pill box cavity: 3D visualisation of E and B



## Examples of pill box cavities

DESY cavity (pill box)



ADONE cavity 51 MHz (pill box)  
Frascati lab, Italy

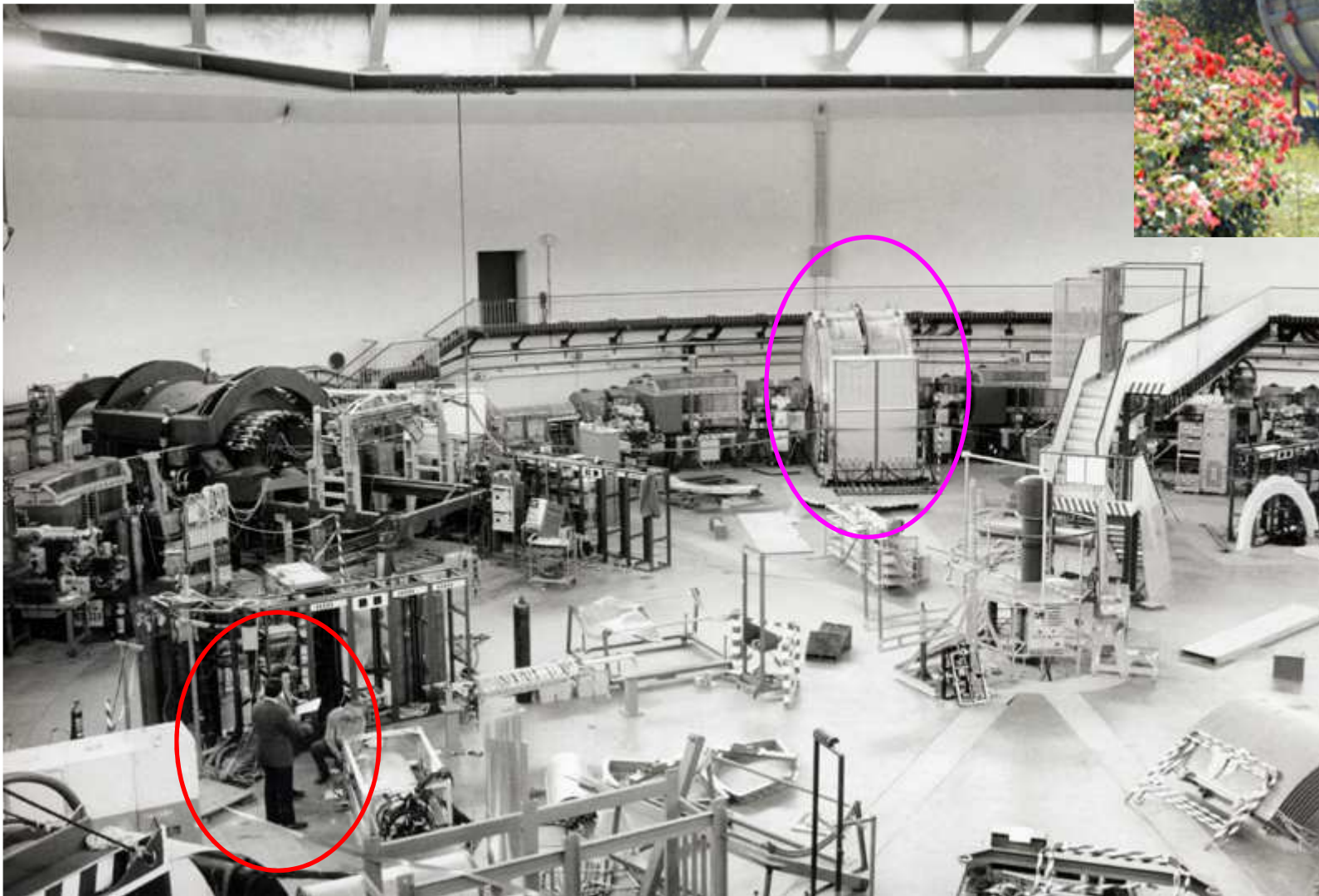




## Examples of pill box cavities

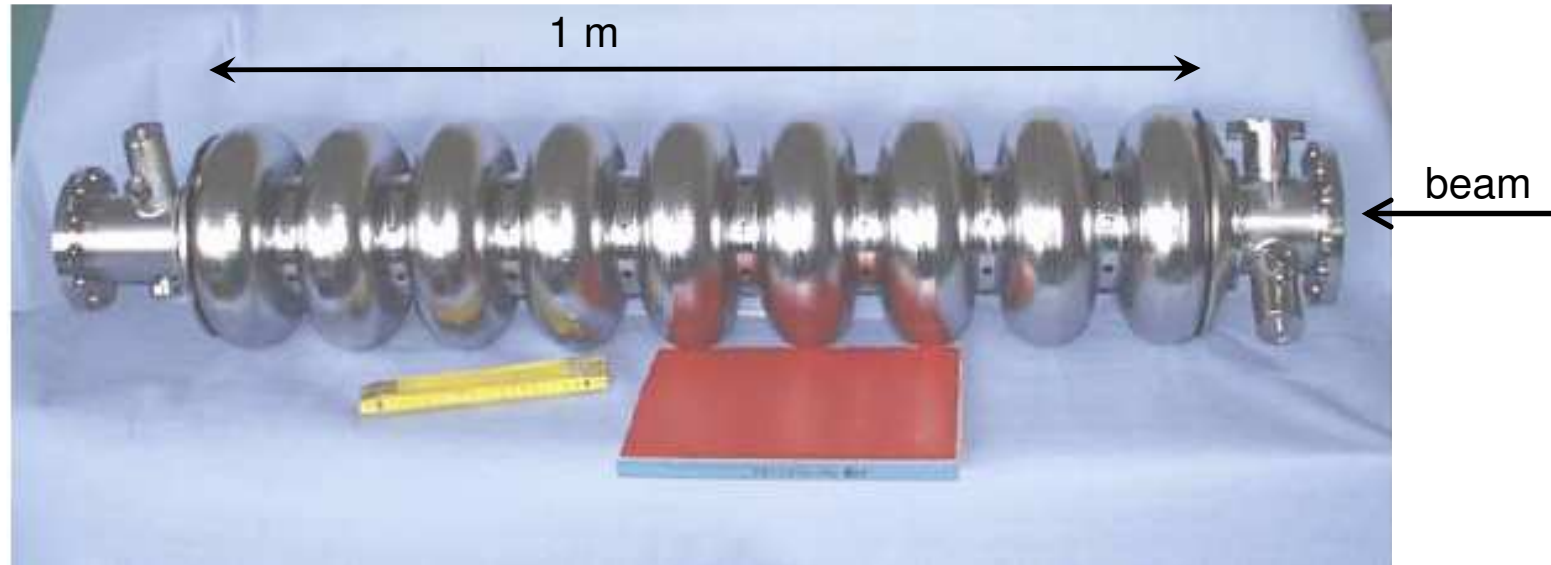
ADONE cavity 51 MHz (pill box)  
Frascati lab, Italy

ADONE in 1963, Laboratori Nazionali di Frascati, Italy



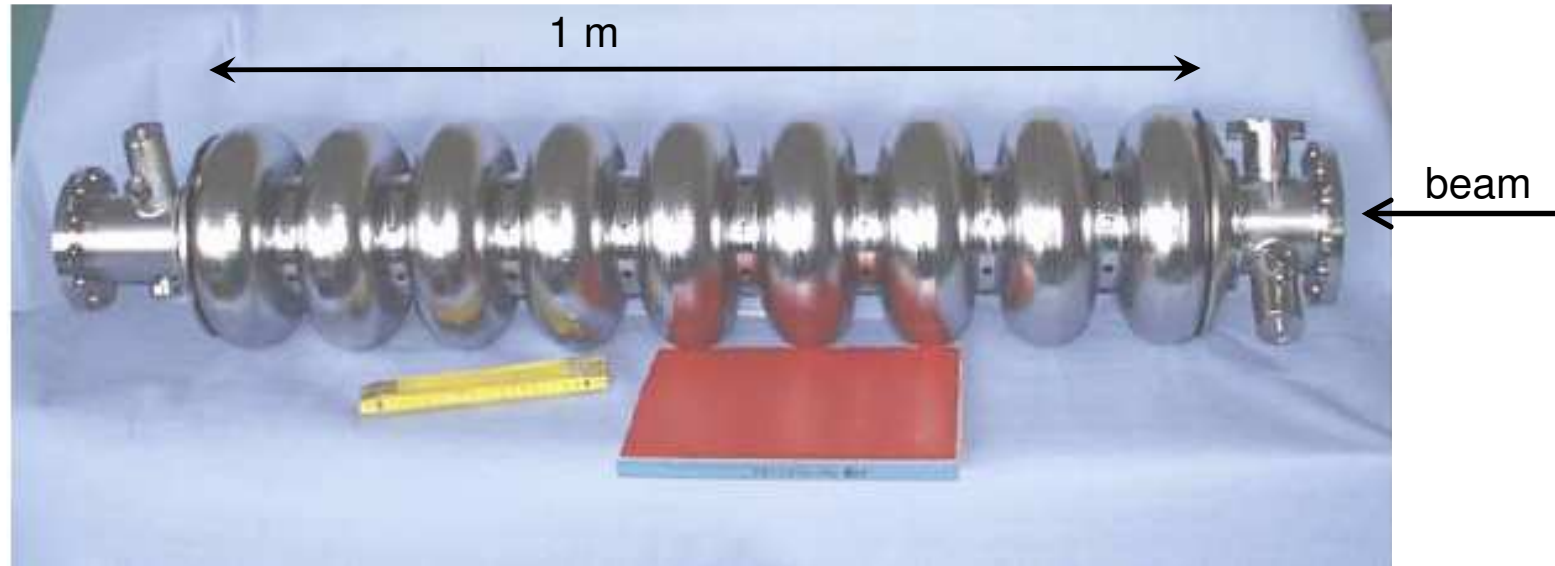
# Superconducting cavity used at DESY

Superconducting cavity used in FLASH (0.3 km) and in XFEL (3 km)



Free-electron <u>L</u> ASer in <u>H</u> amburg	0.3 km	DESY	2004- ?	e-	1.2 GeV
European <u>X</u> -ray <u>F</u> ree- <u>E</u> lectron <u>L</u> aser	3 km	DESY	2016- ?	e-	17.5 GeV
<u>I</u> nternational <u>L</u> inear <u>C</u> ollider	30 km	?	?	e-/e+	2x250 GeV

# Superconducting cavity used at DESY



material: pure Niobium

operating temperature: 2 K

accelerating field gradient: up to 35 MV/m

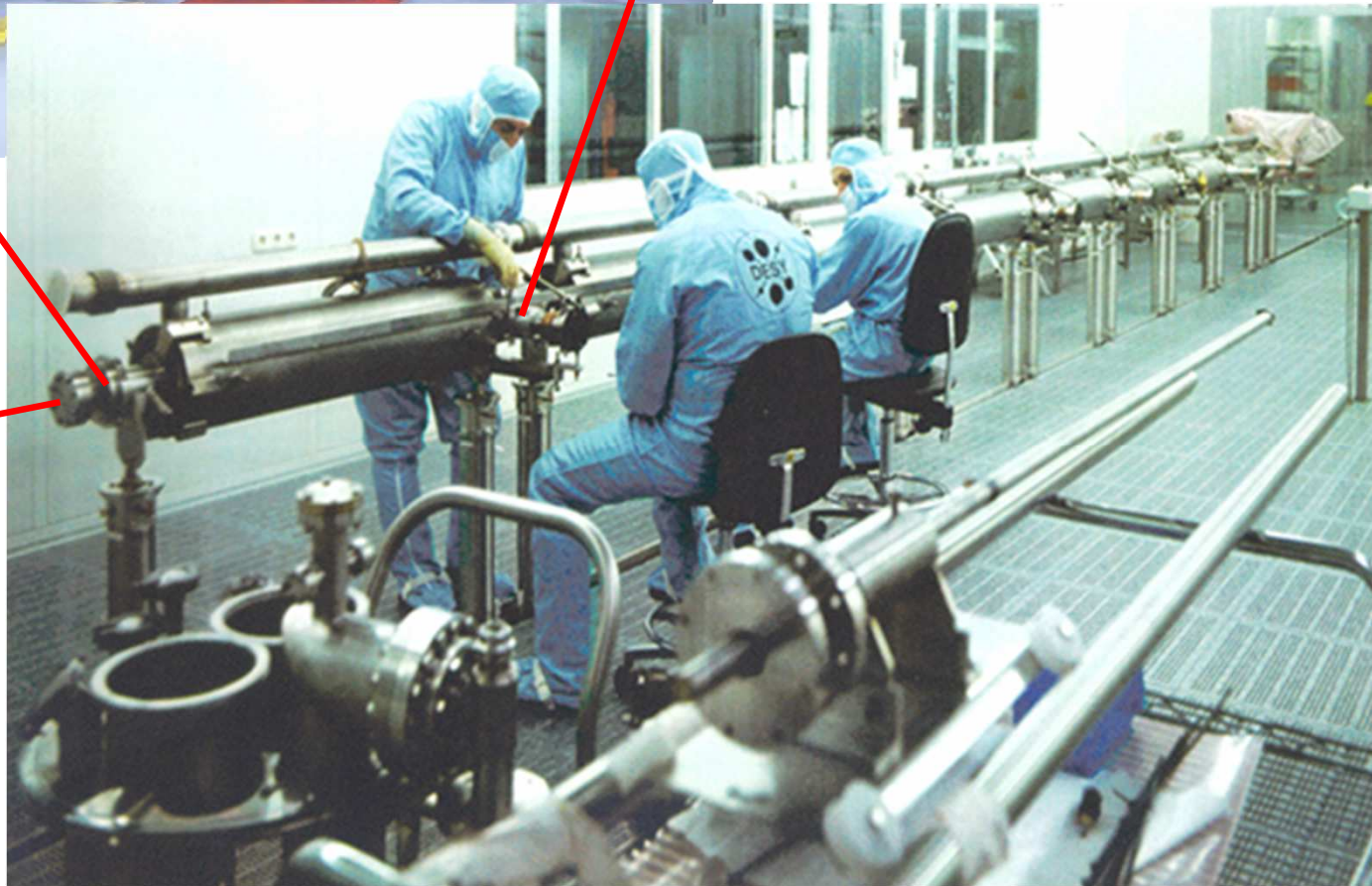


# Cavities inside a cryostat

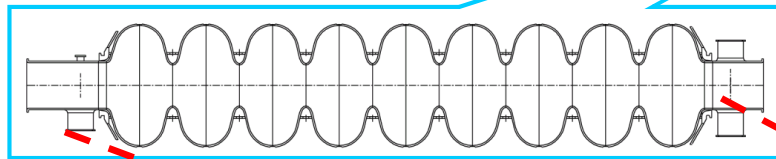
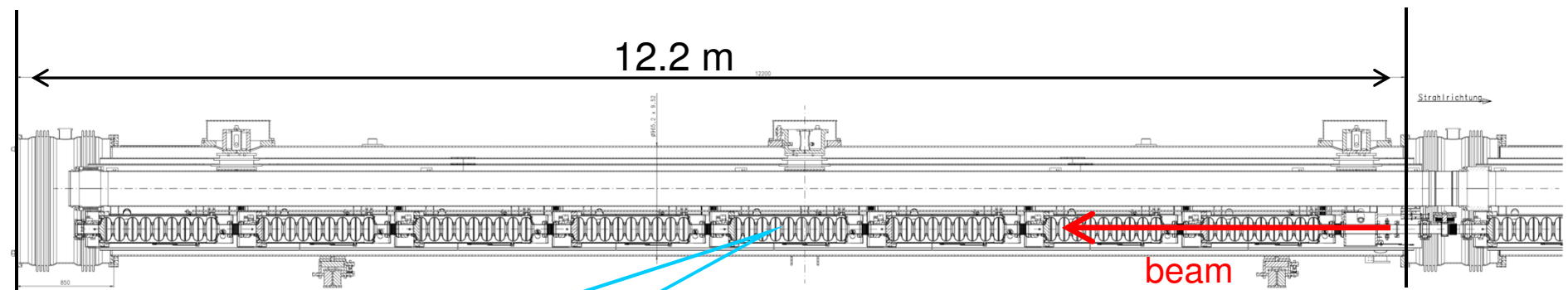


Number of cavities	8
Cavity length	1.038 m
Operating frequency	1.3 GHz
Operating temperature	2 K
Accelerating Gradient	23..35 MV/m

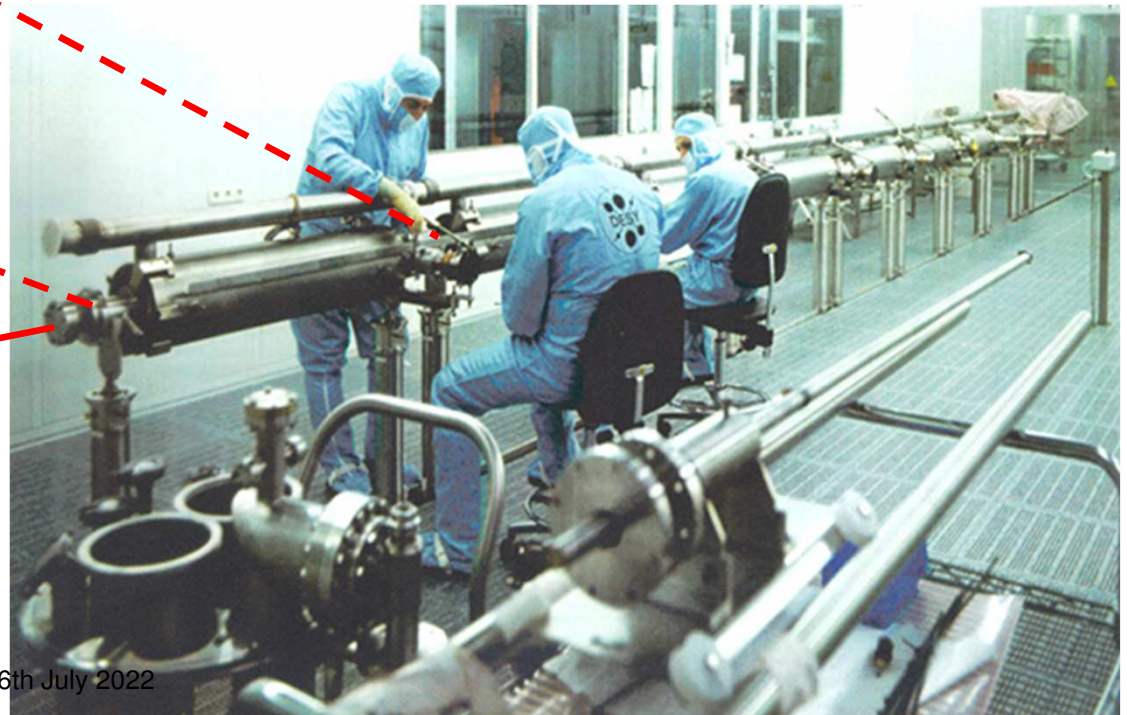
beam







beam ←

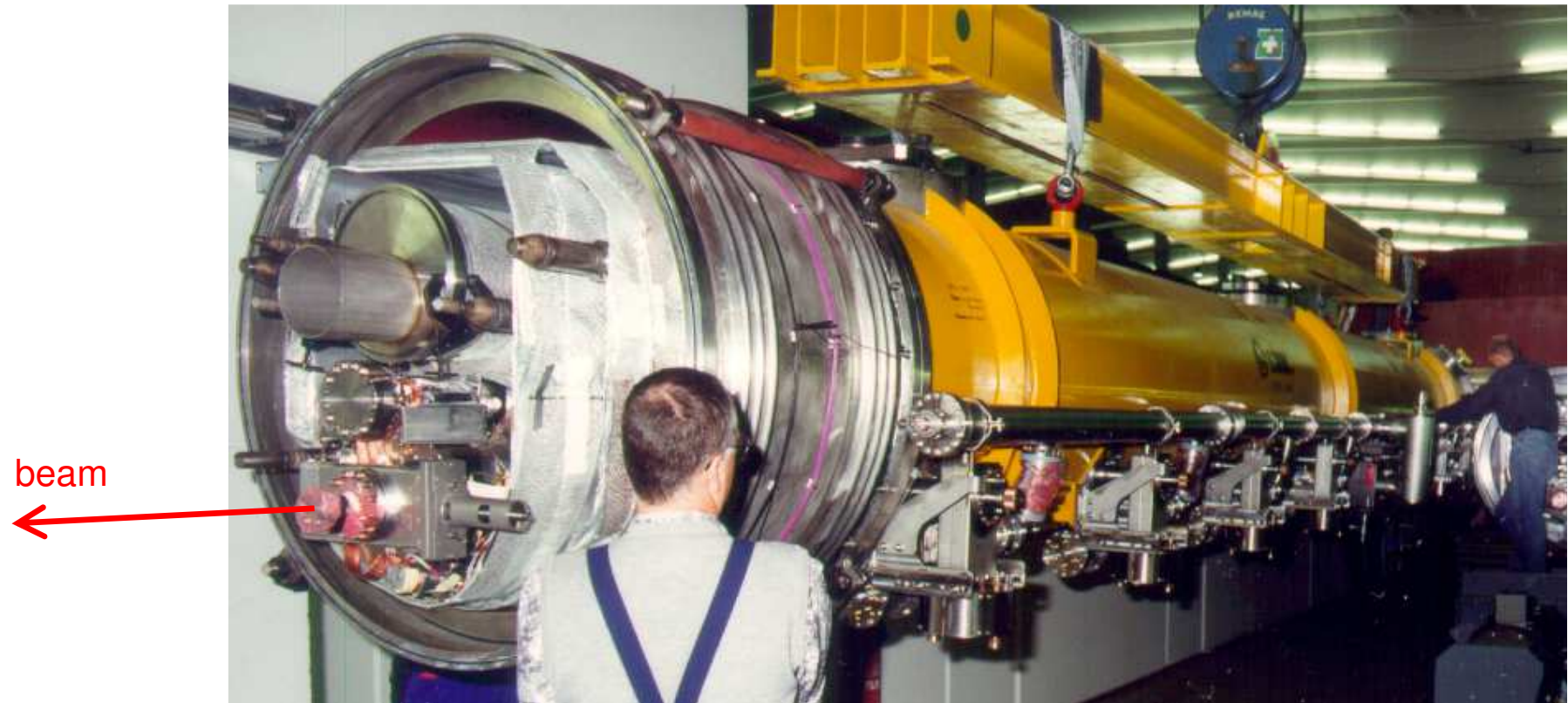


# Cavities inside a cryostat



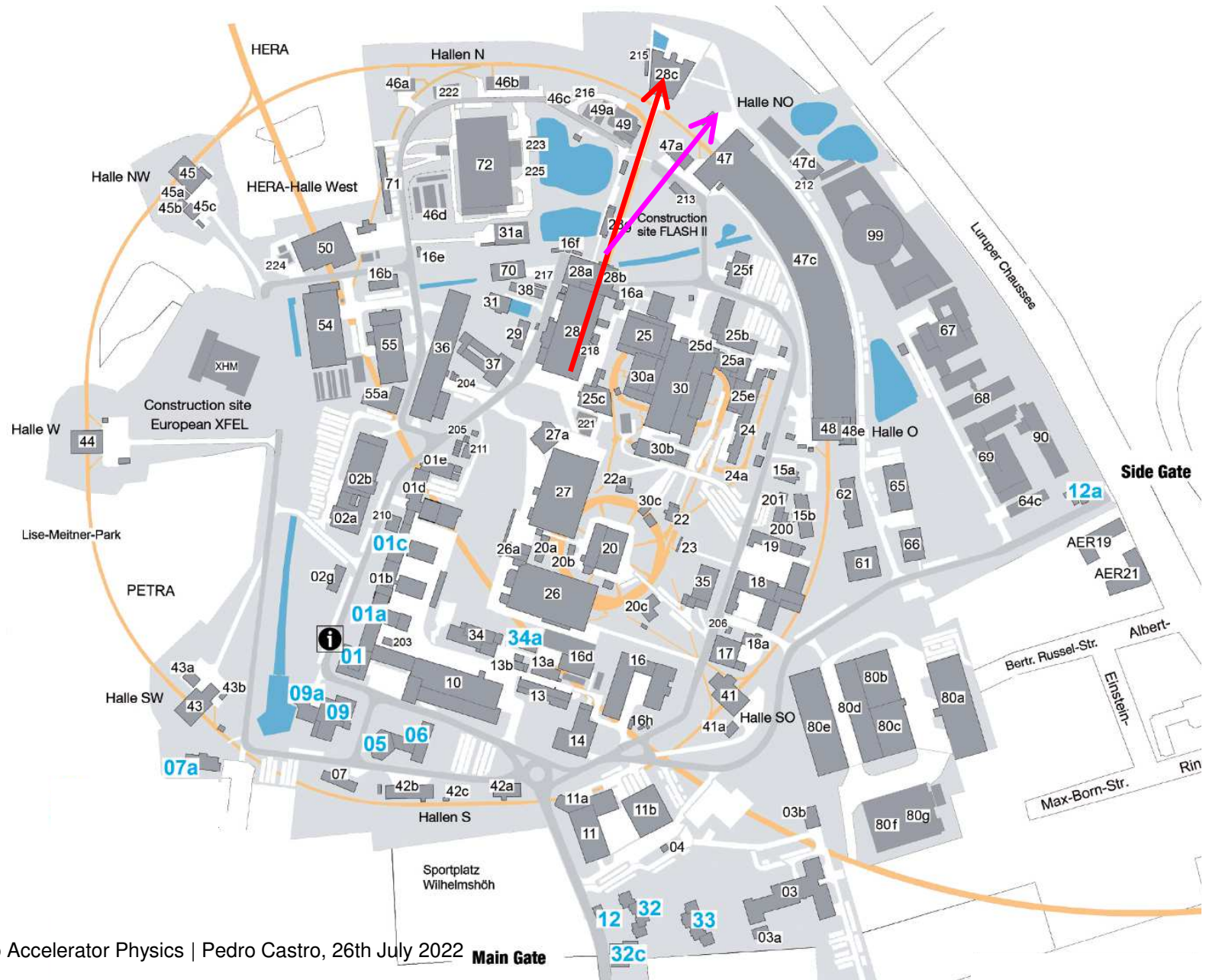


# Cavities inside an accelerator module (cryostat)



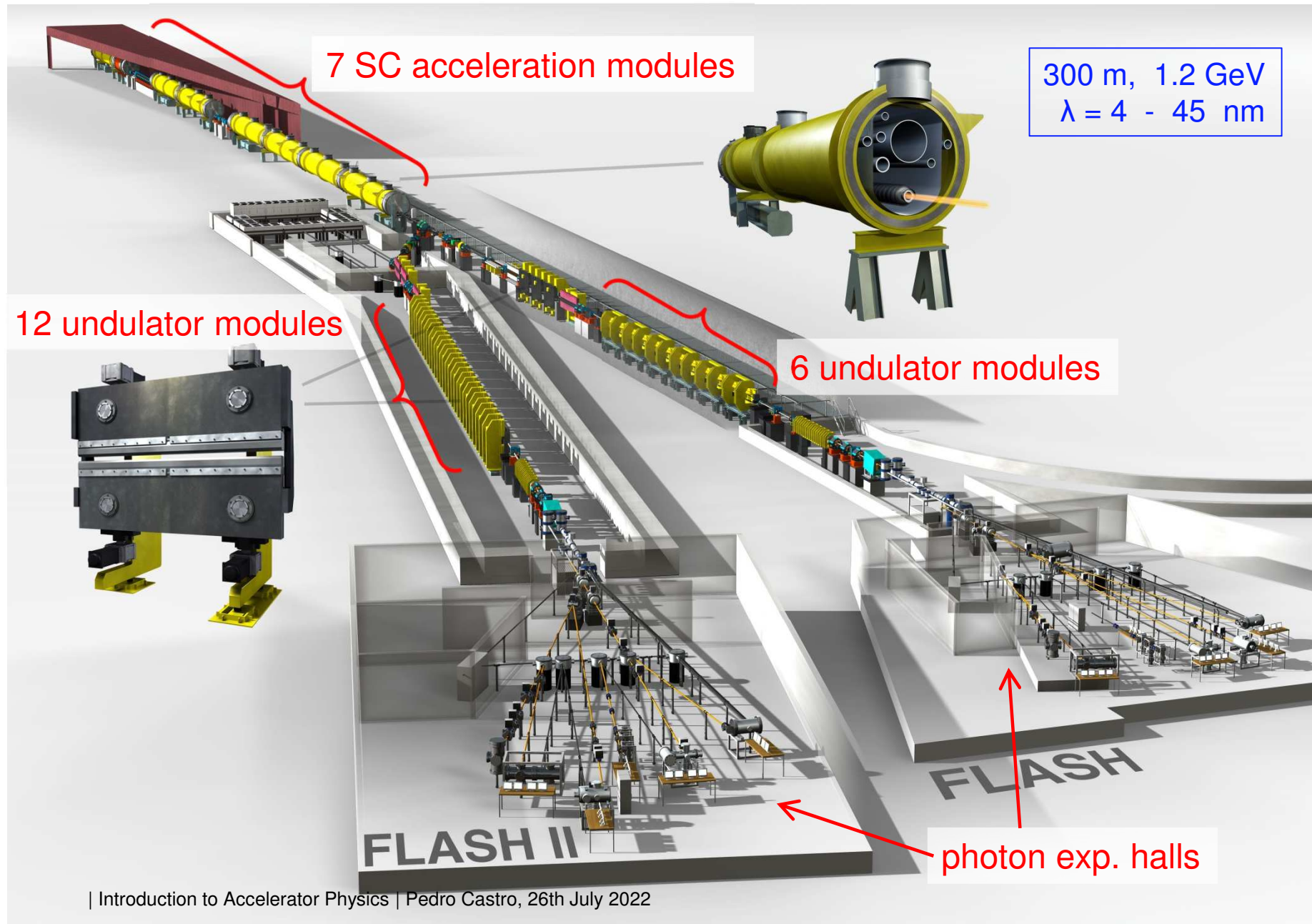
module installation in FLASH (2004)

# Free-electron LASer in Hamburg (FLASH)





# Free-electron LASer in Hamburg (FLASH)



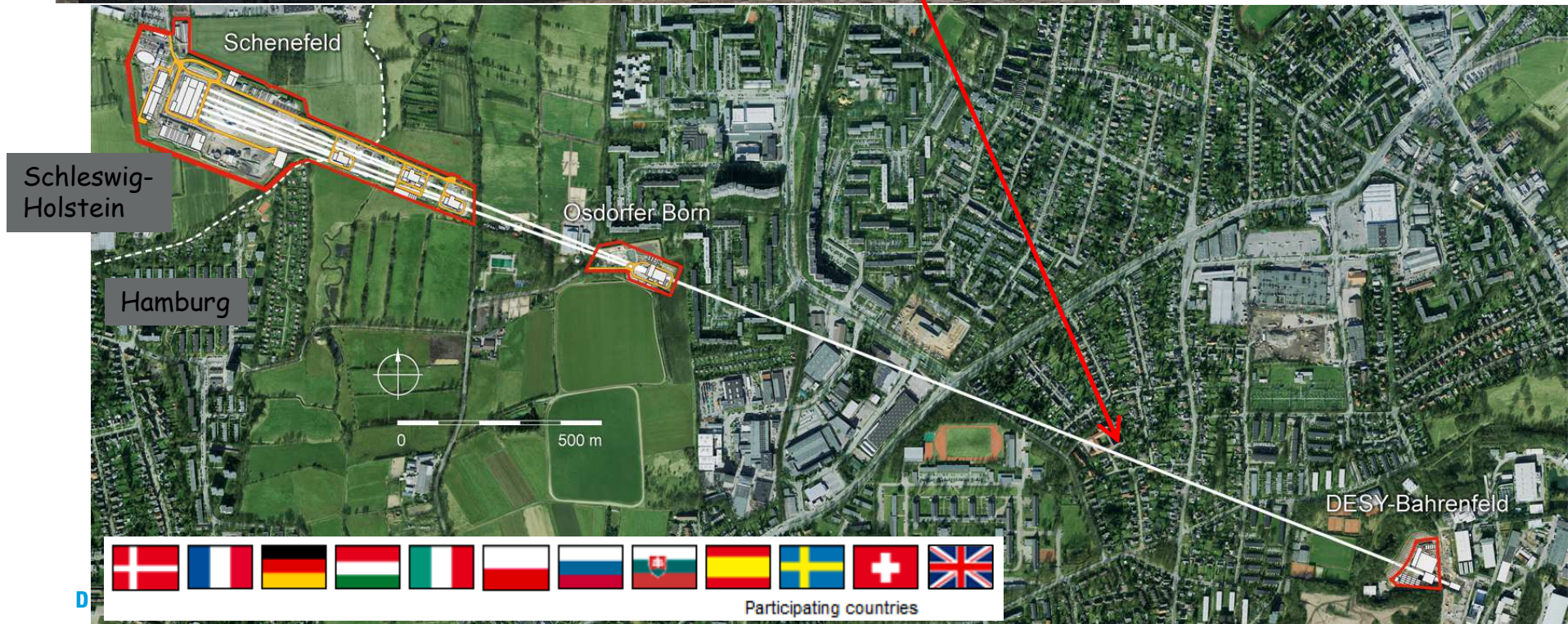


# 100 accelerator modules (cryostats) in XFEL

European X-ray Free-Electron Laser (XFEL)

(3 km, 17.5 GeV)

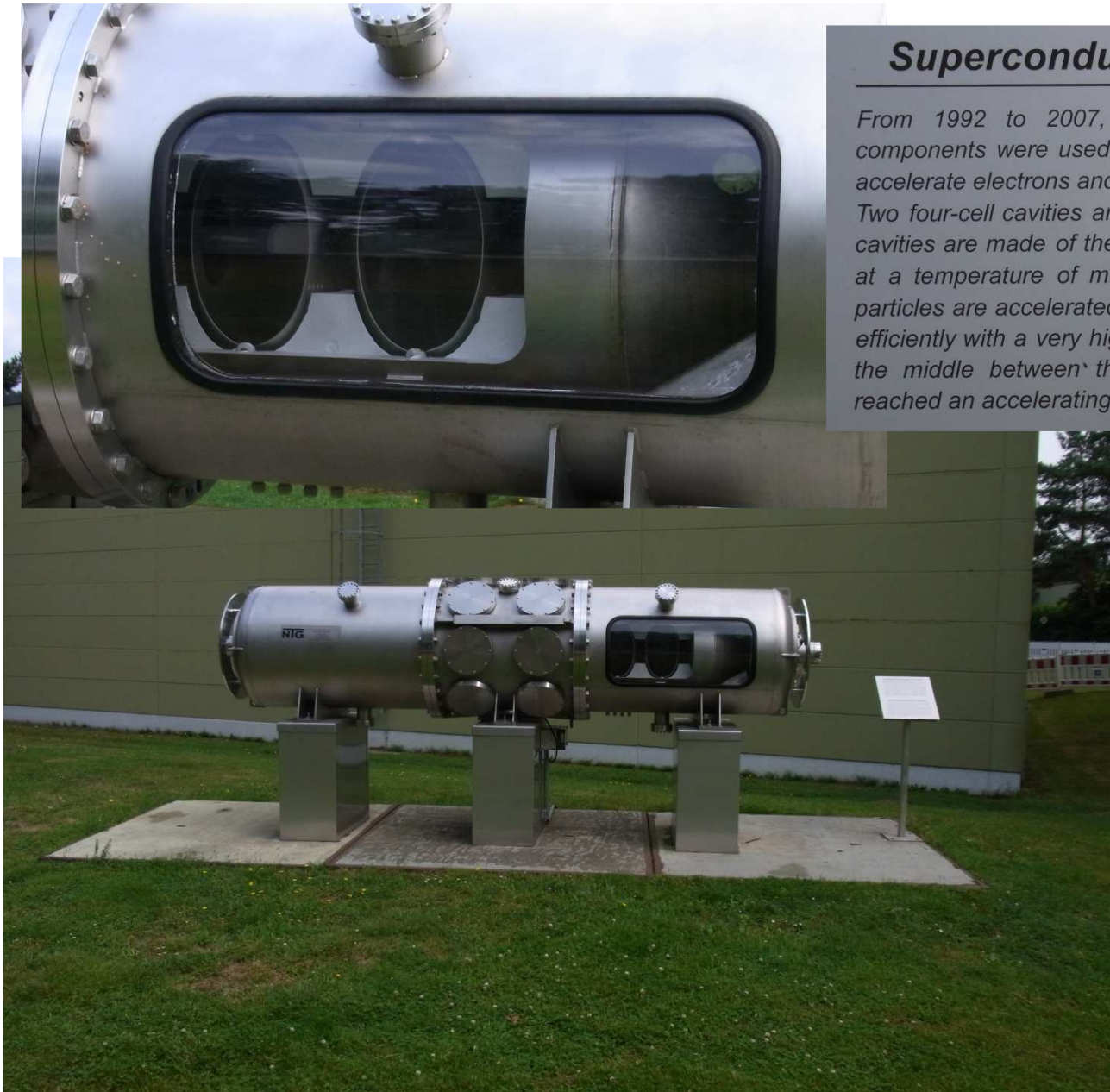
$\lambda = 0.05 - 6 \text{ nm}$





# Superconducting cavities at HERA

16 cavities  
500 MHz



## ***Superconducting Particle Accelerator***

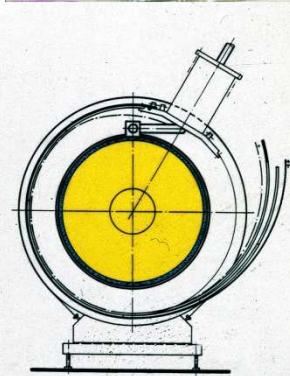
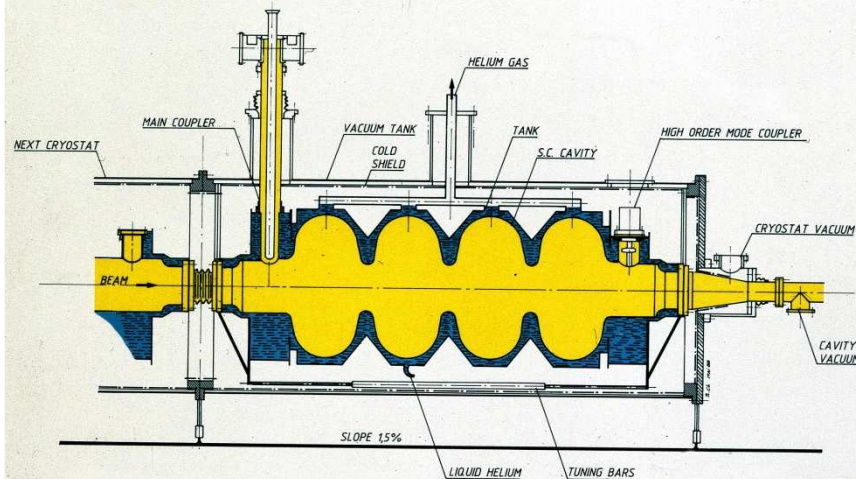
*From 1992 to 2007, eight of these superconducting accelerator components were used in the 6.3-kilometre long storage ring HERA to accelerate electrons and their antiparticles, positrons.*

*Two four-cell cavities are arranged in one thermal vessel (cryostat). The cavities are made of the metal niobium which becomes superconducting at a temperature of minus 269 degrees Celsius. At this temperature, particles are accelerated almost without electric resistance and thus very efficiently with a very high electric alternating voltage which is injected in the middle between the cavities. During HERA operation, this cavity reached an accelerating gradient of 5 million volts per metre.*



# Superconducting cavities at LEP

272 cavities  
352 MHz

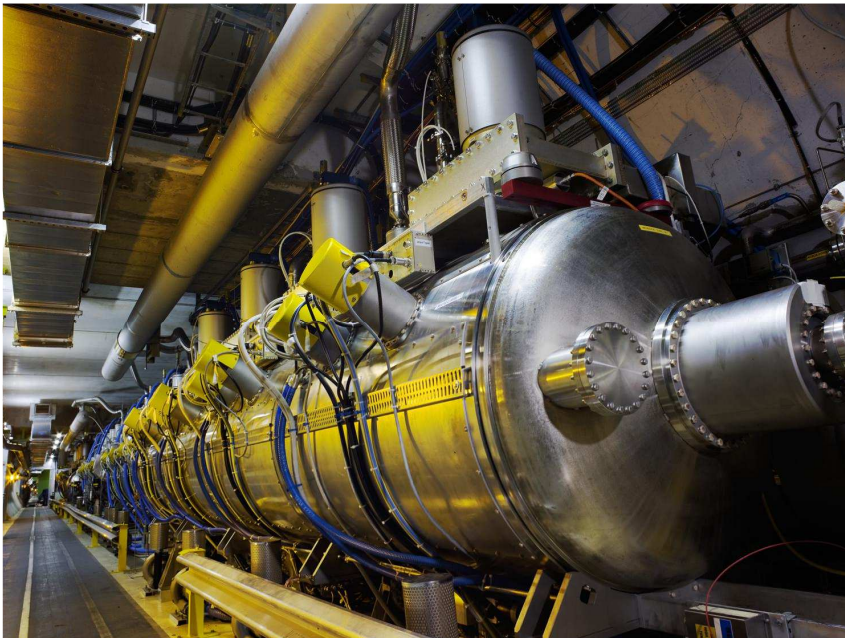


SUPERCONDUCTING CAVITY WITH ITS CRYOSTAT



# Superconducting cavities at LHC

16 cavities  
400 MHz



## Other accelerators using superconducting cavities

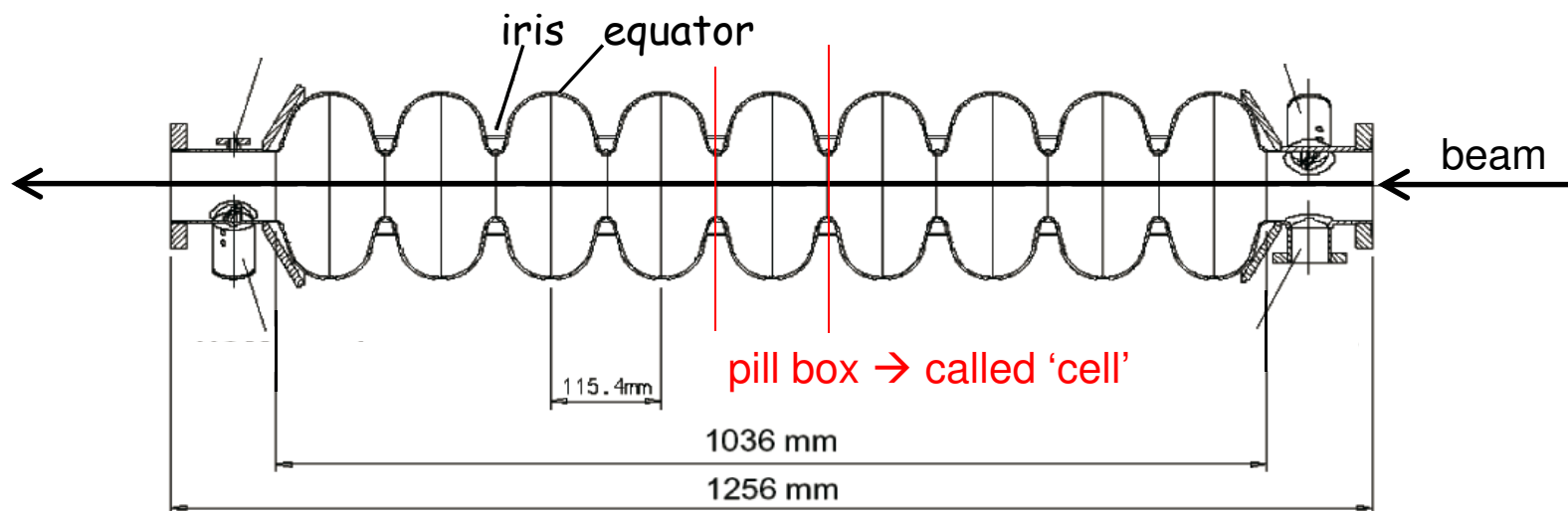
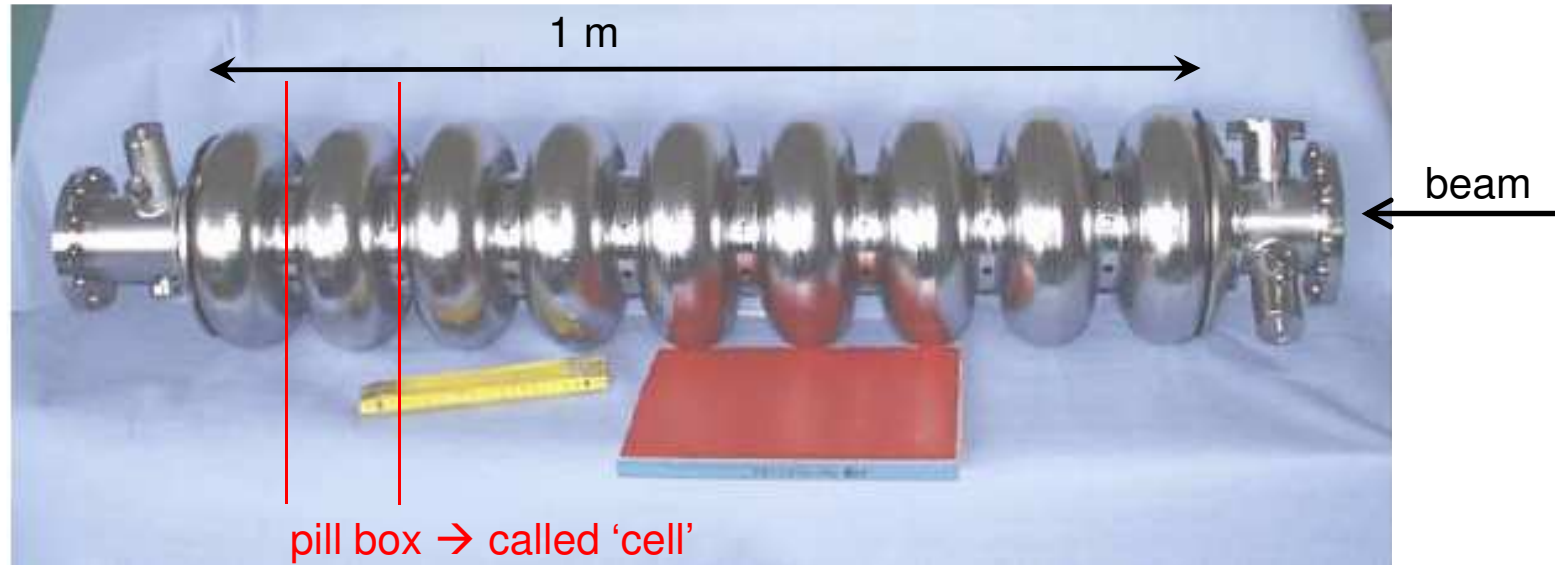
- 5 de-commissioned
- 11 in operation
- 4 in construction
- 9 in design phase

Total = 29

full list: [http://tesla-new.desy.de/srf\\_accelerators](http://tesla-new.desy.de/srf_accelerators)

# Superconducting cavity used in FLASH and in XFEL

Superconducting cavity used in FLASH (0.3 km) and in XFEL (3 km)



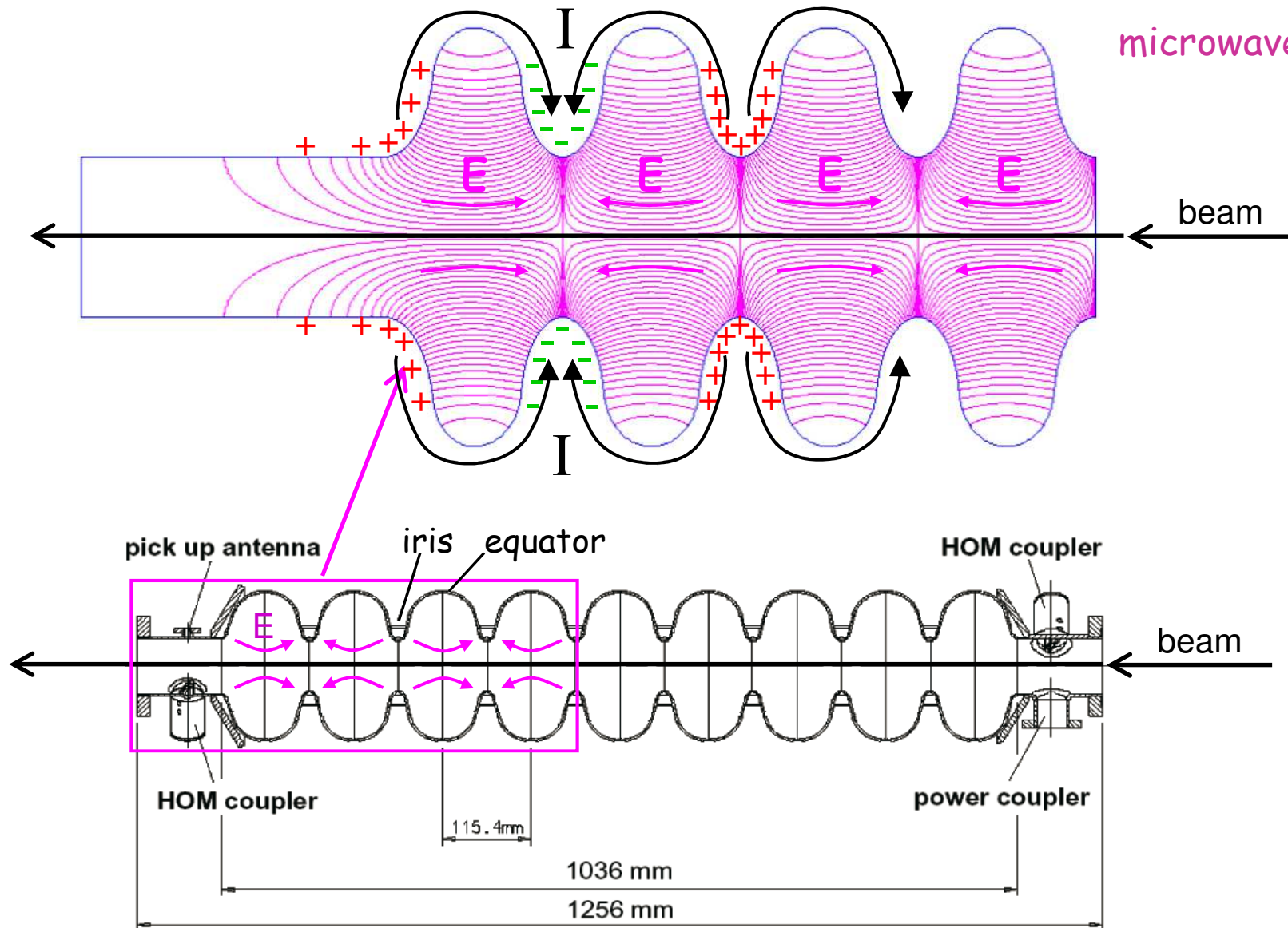


# Accelerating field map

Simulation of the fundamental mode: electric field lines

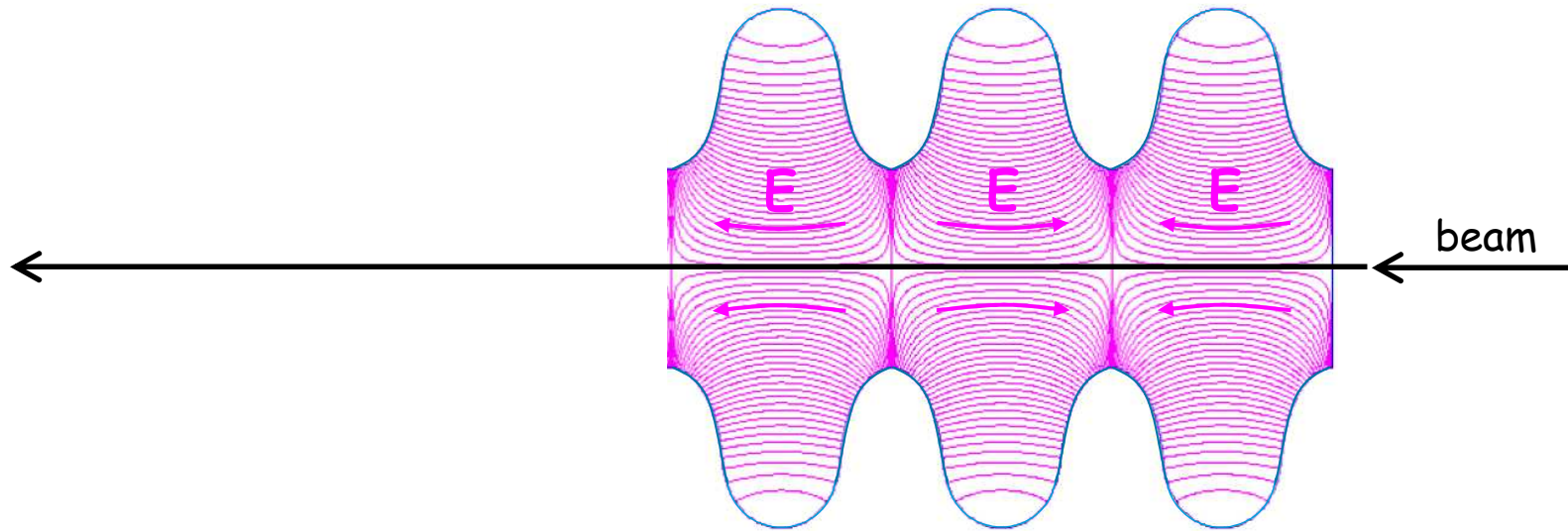
$f_{RF} = 1.3 \text{ GHz}$

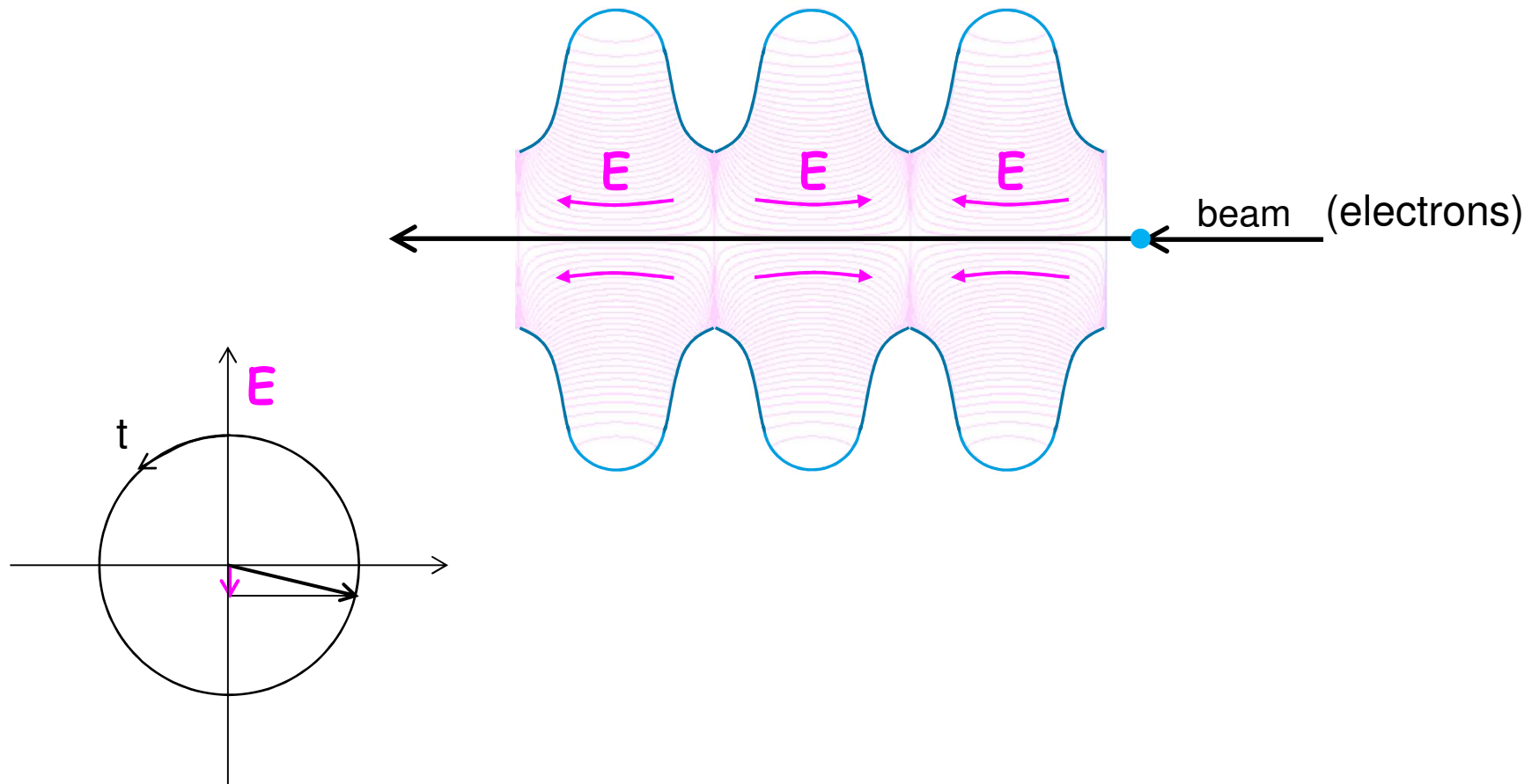
microwaves: (L-band)

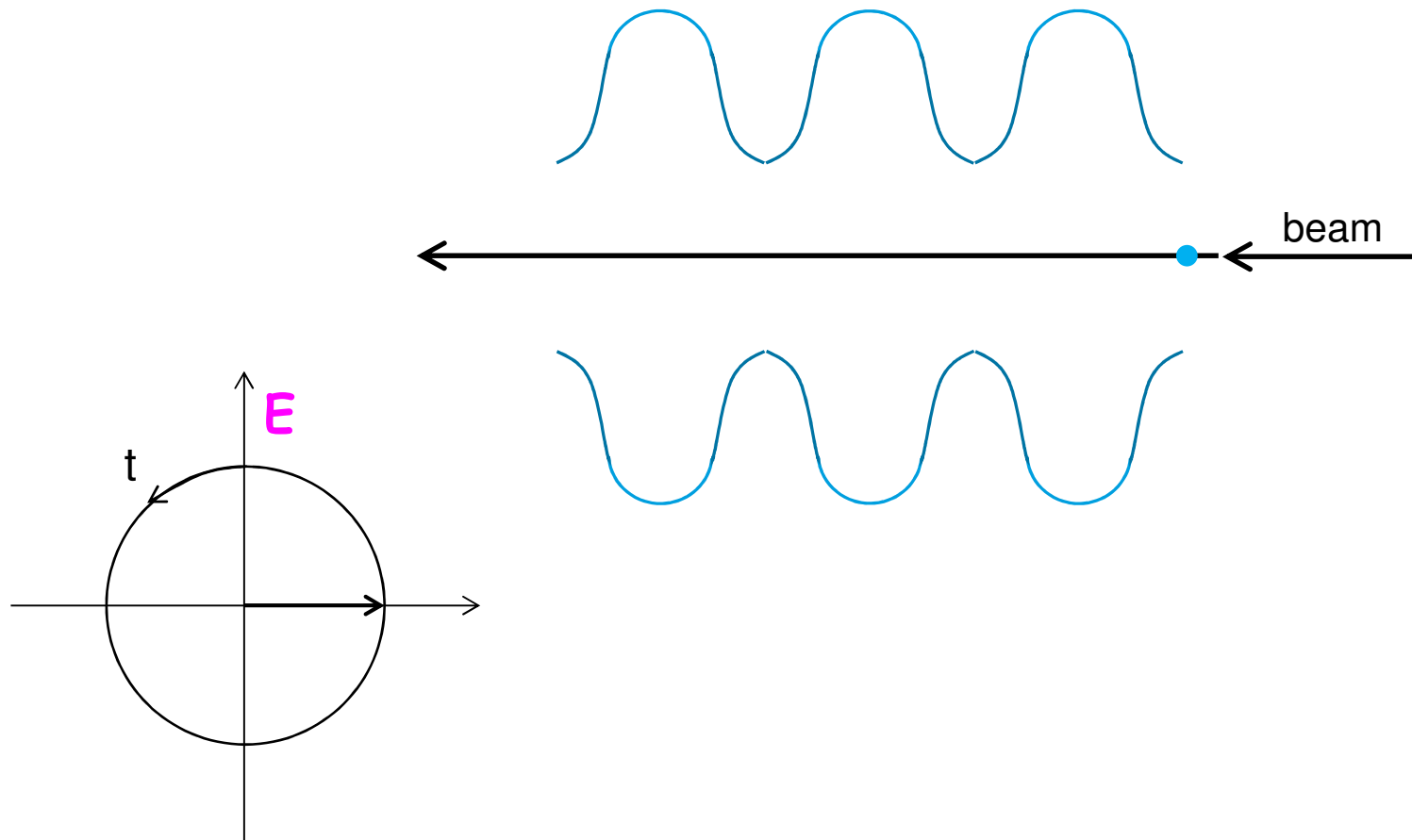


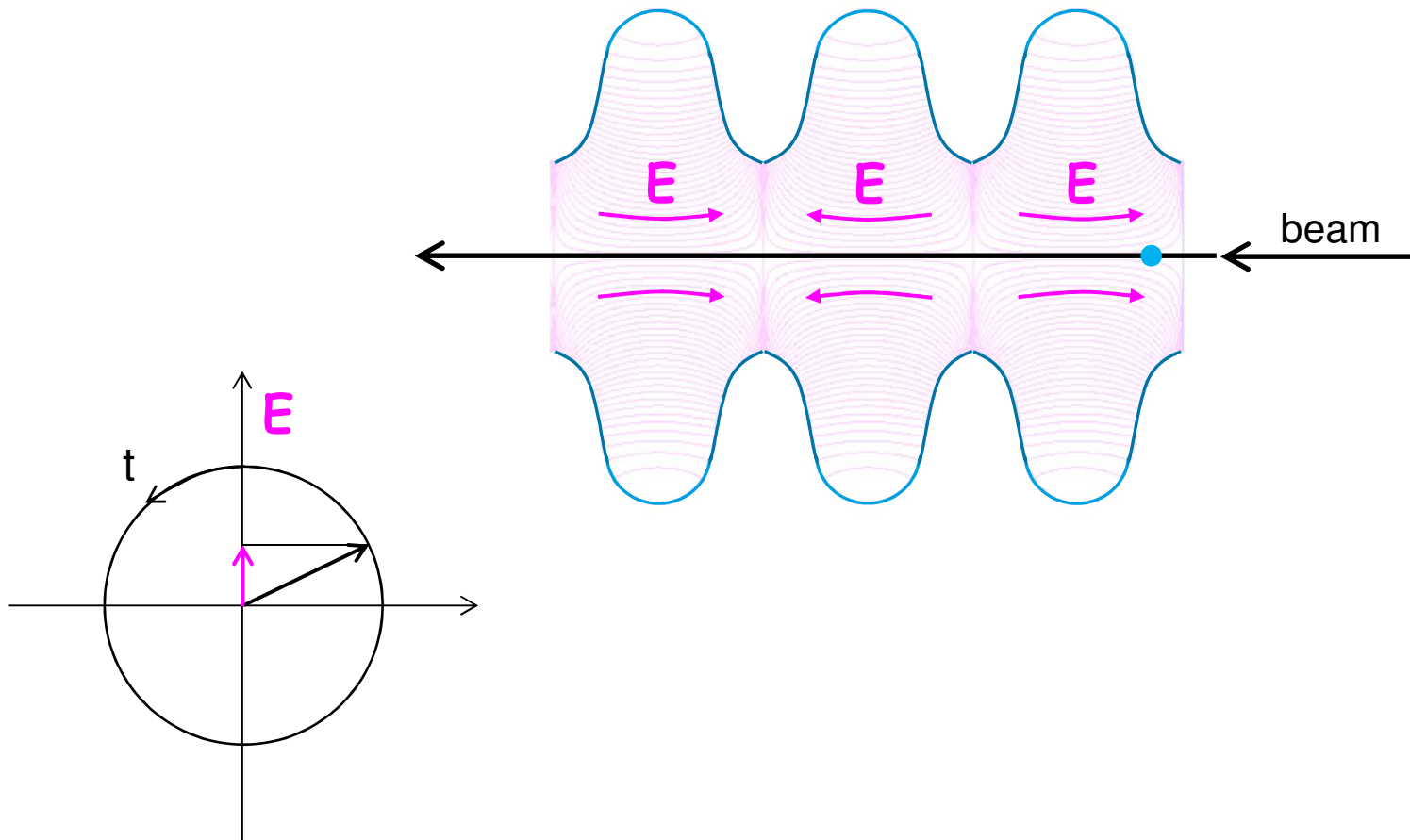
# Is there a net acceleration?

Simulation of the fundamental mode: electric field lines

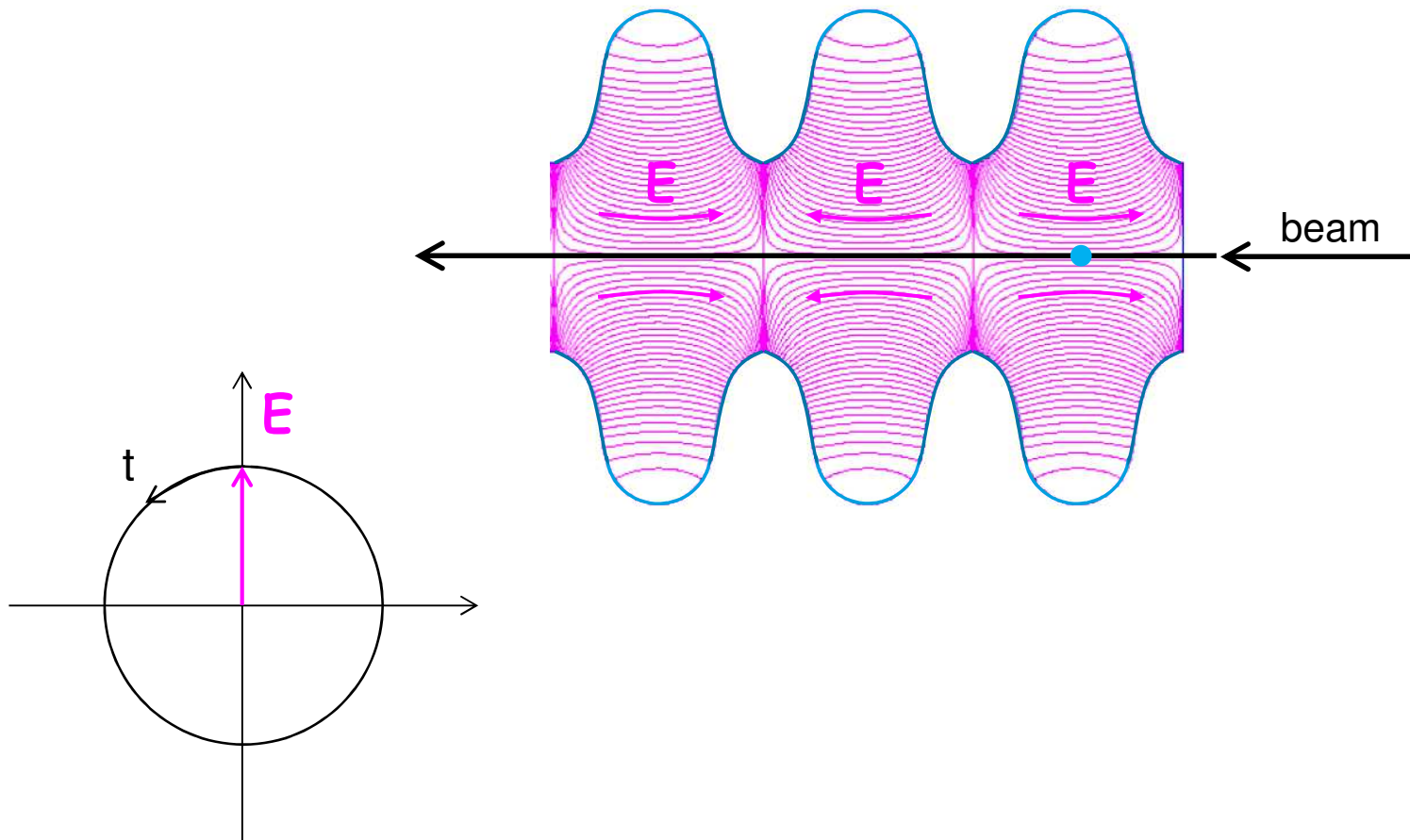


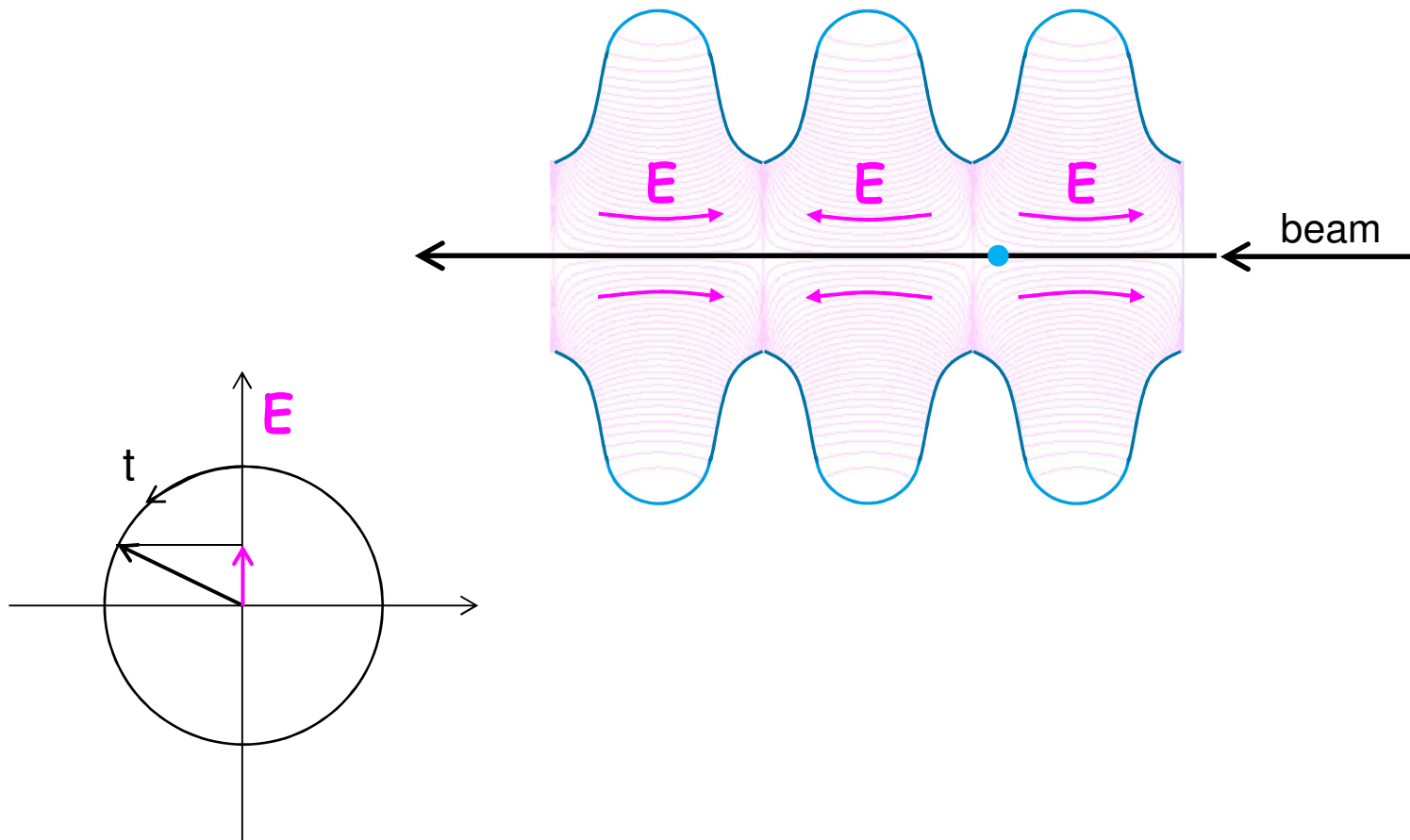


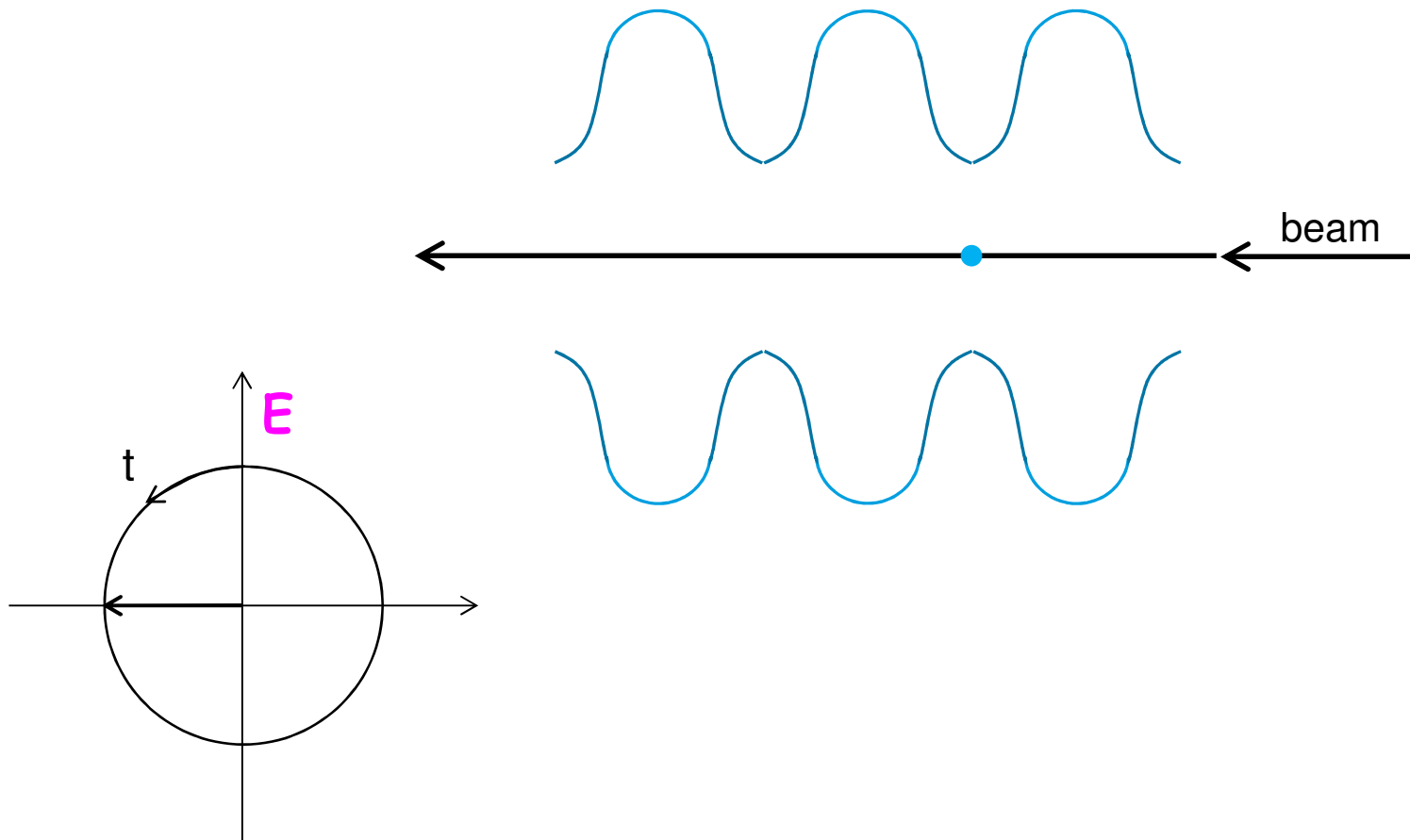


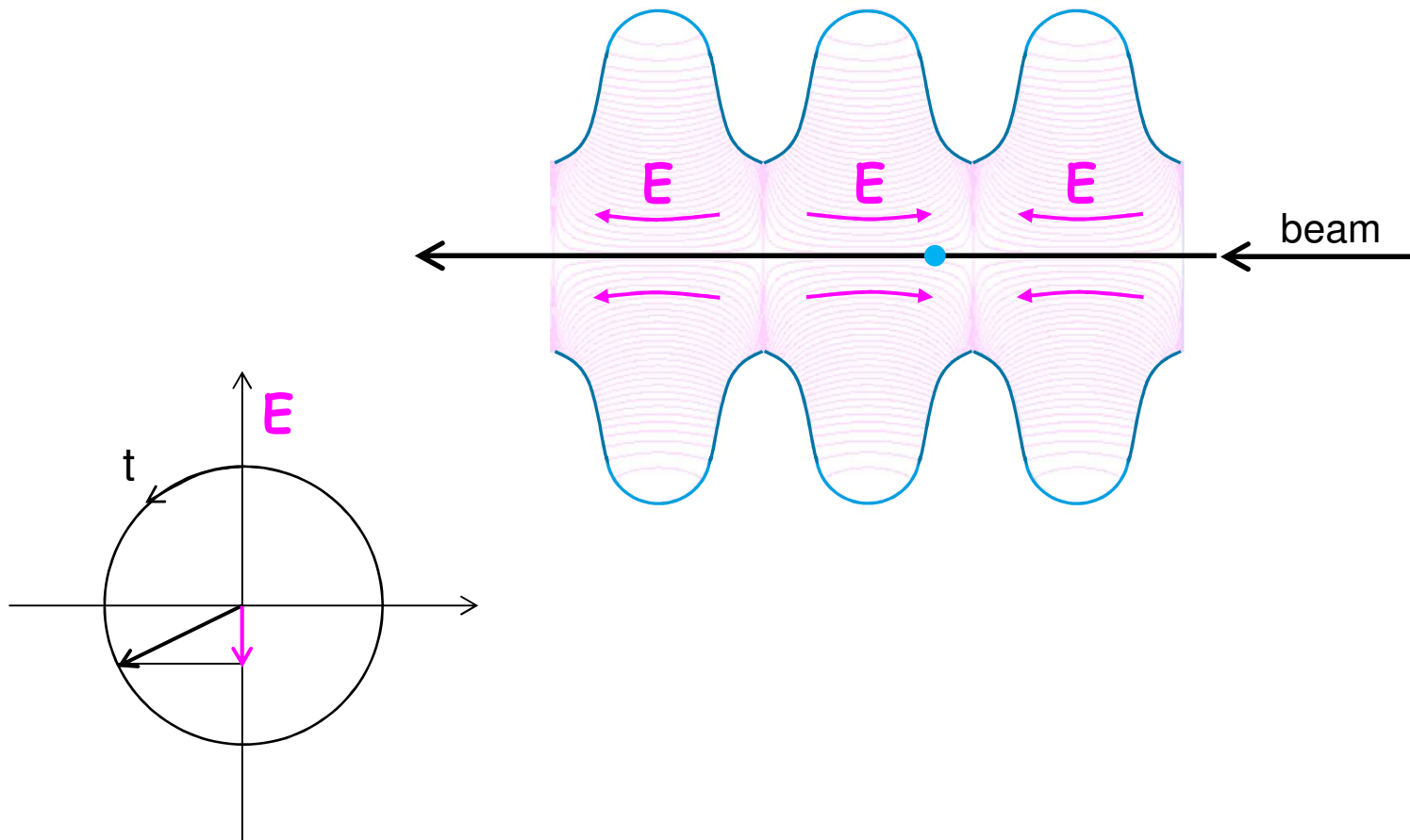


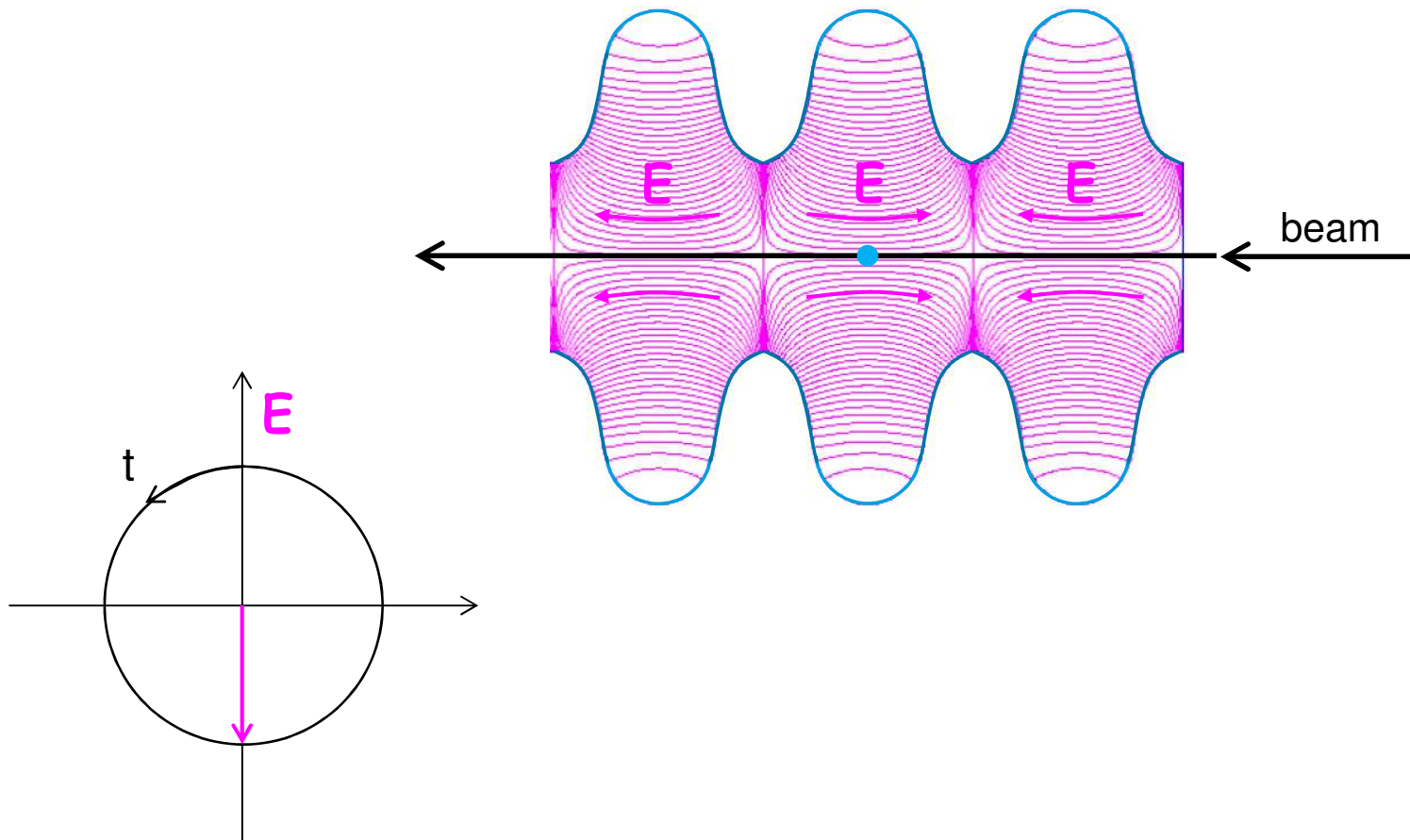


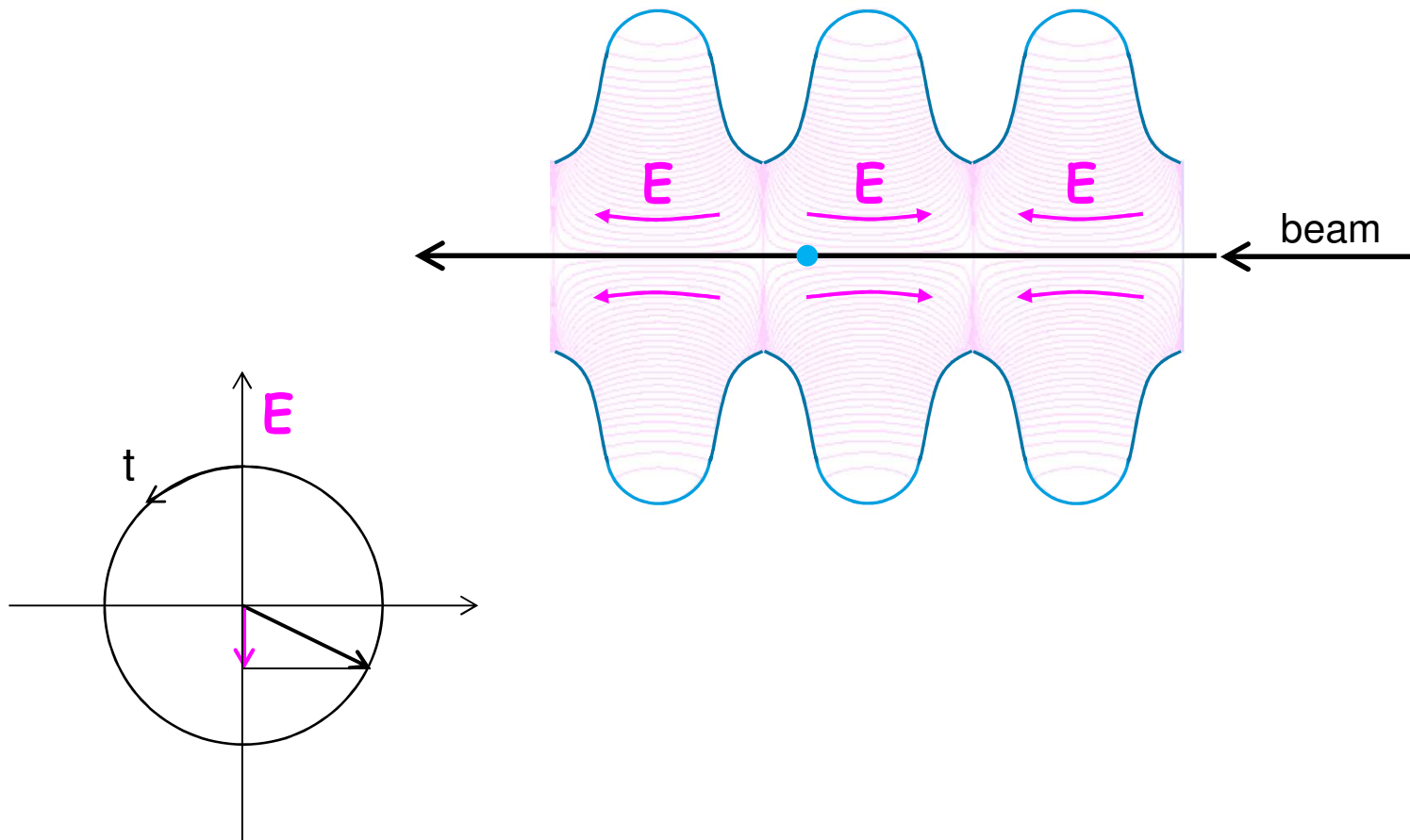


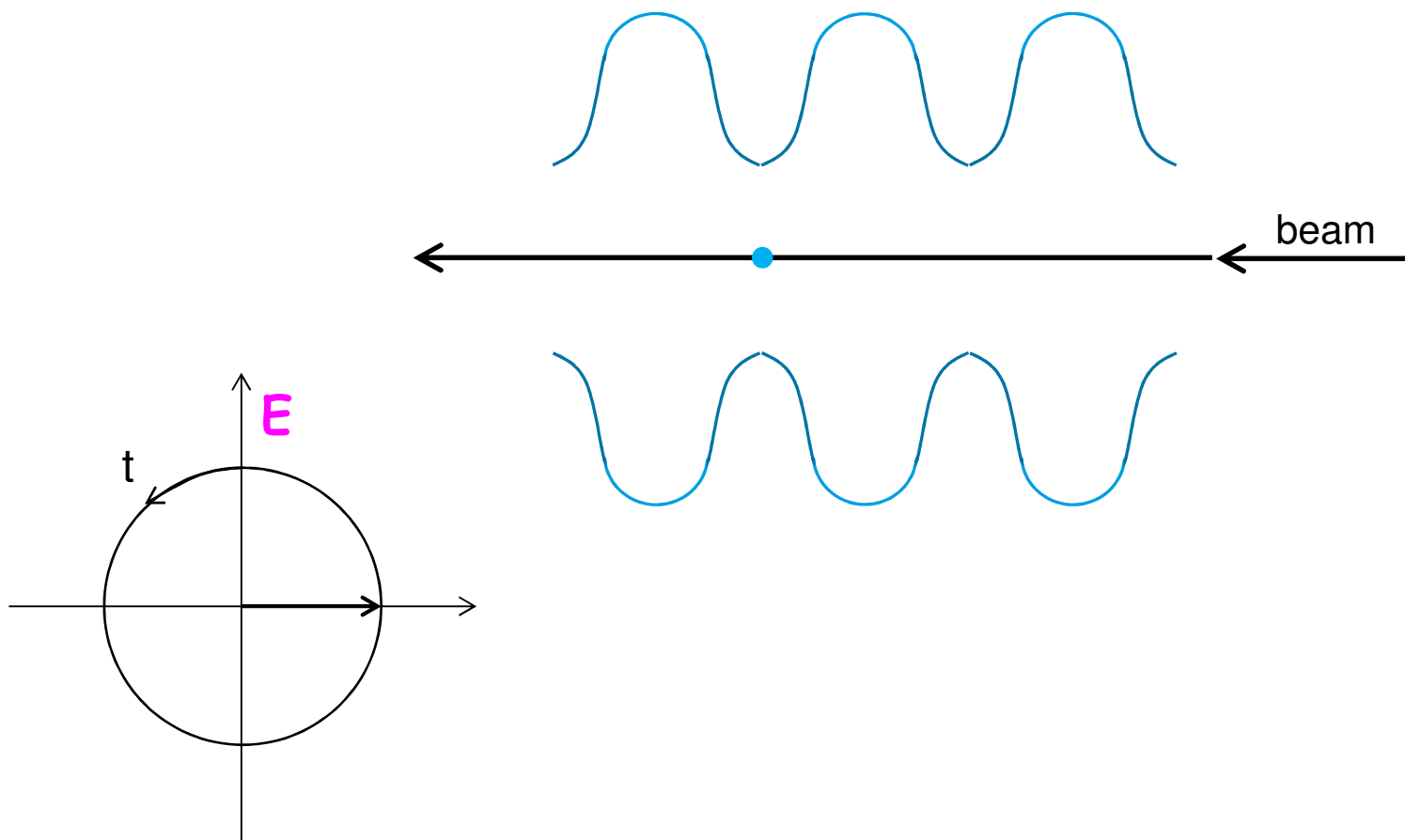


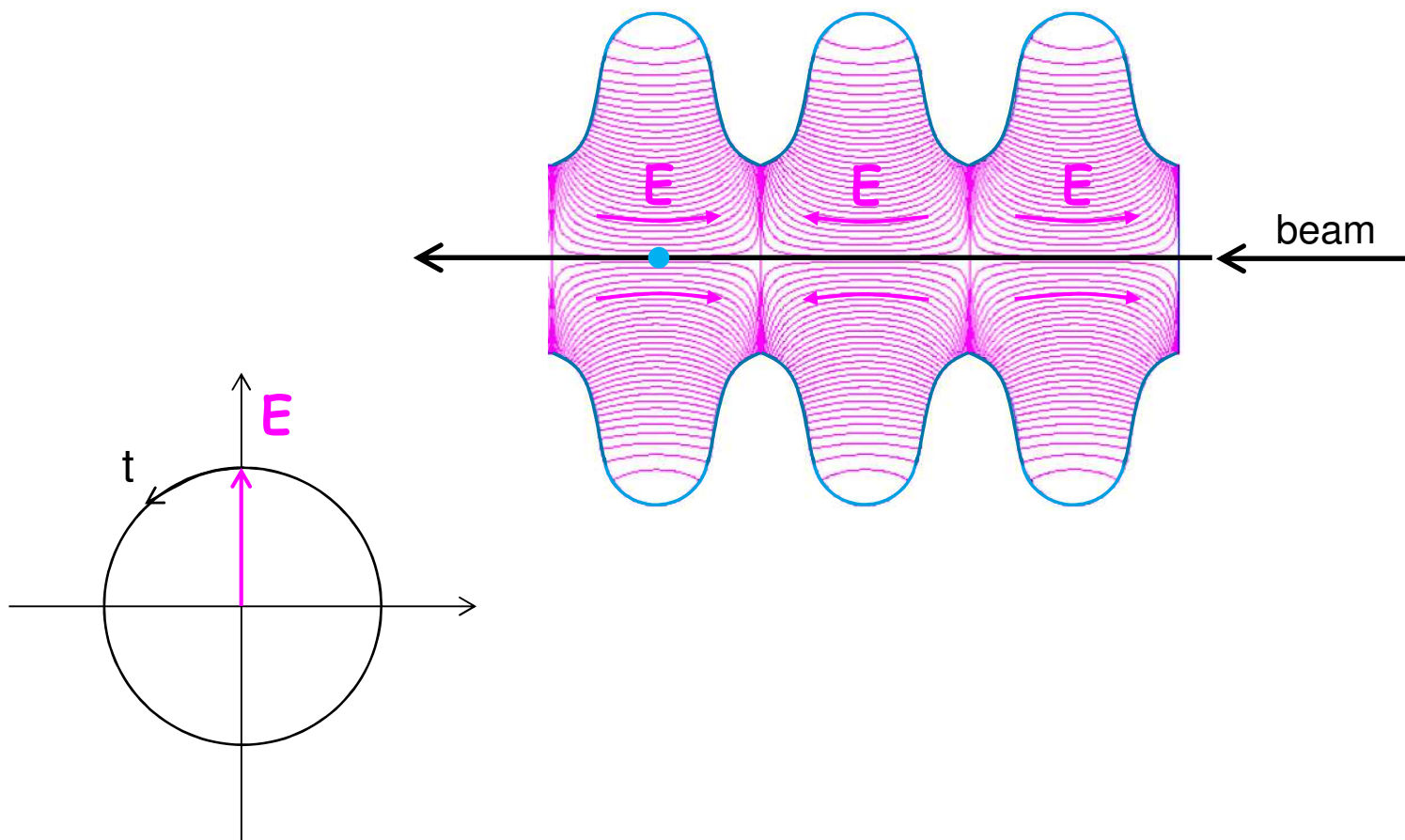




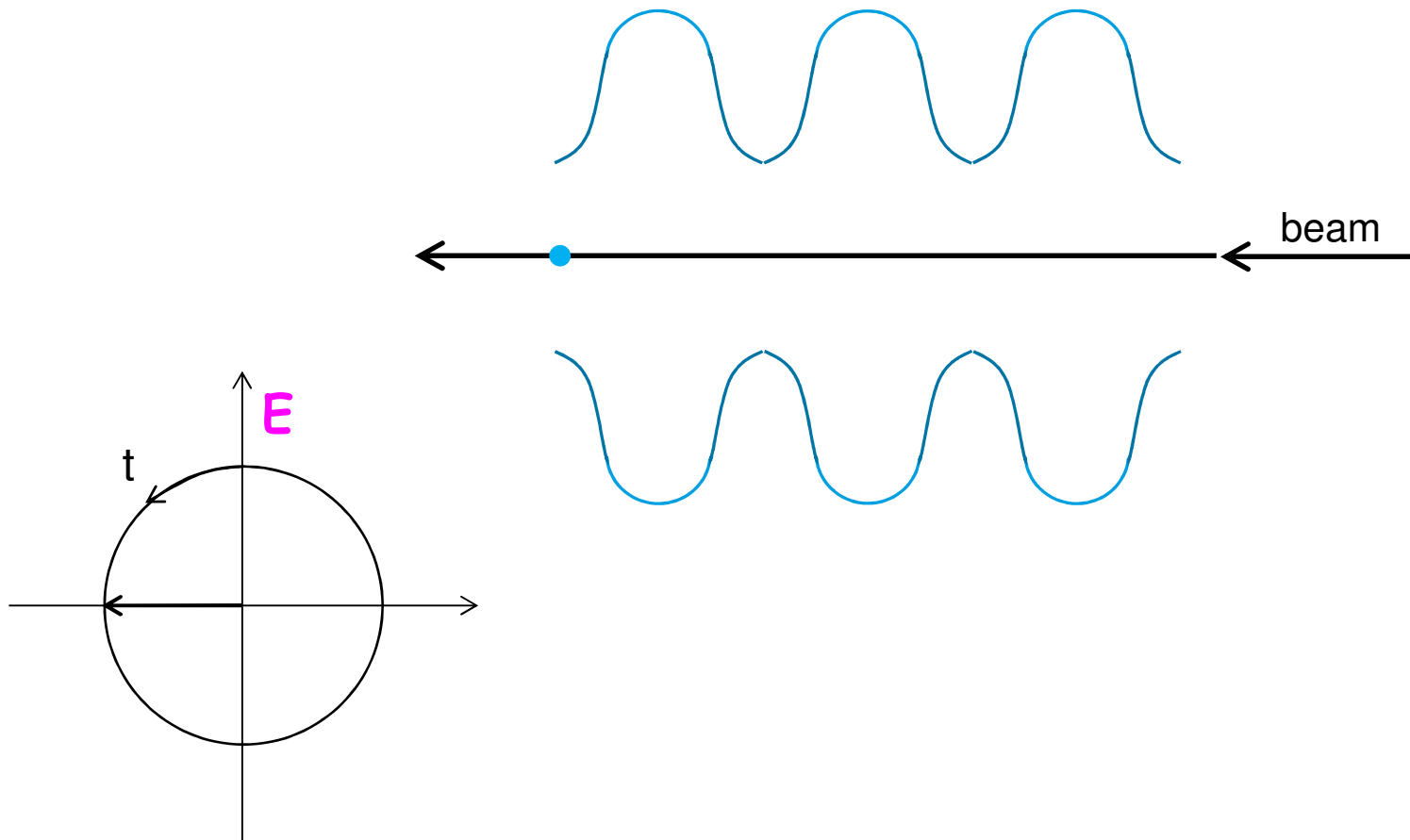






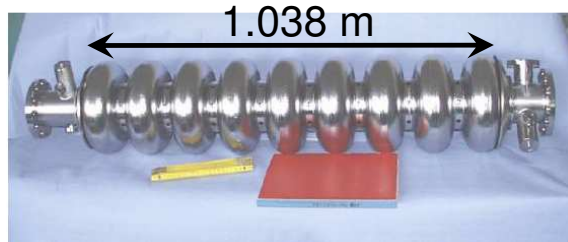
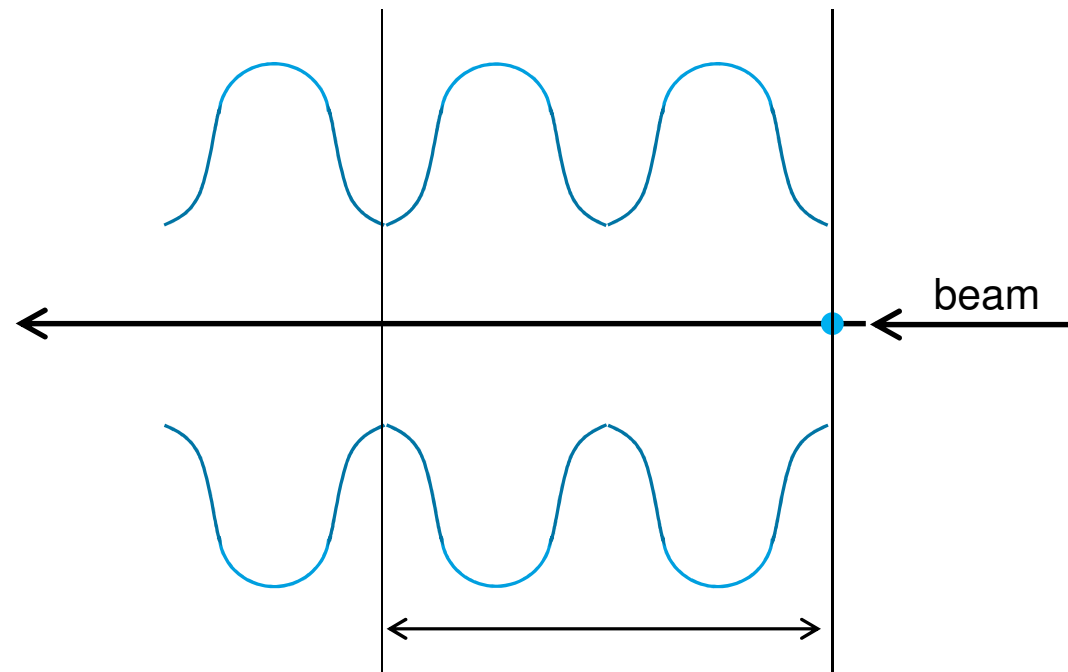






Is there a net acceleration? ..... timing is the key

for electrons,  $\beta \cong 1$



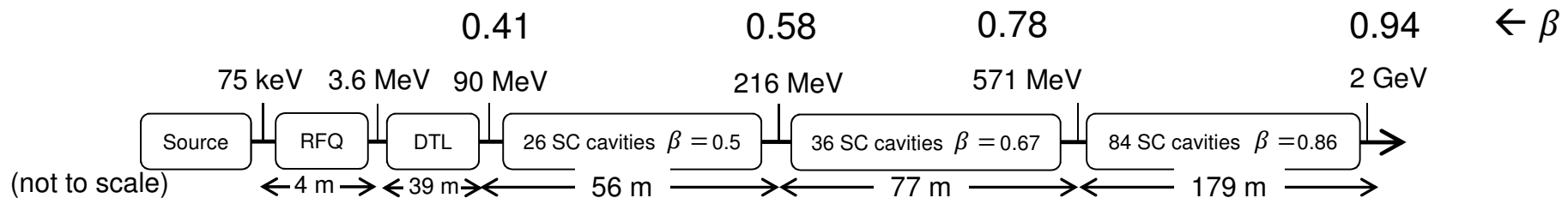
$$l = cT = \frac{c}{f} = \frac{3 \cdot 10^8}{1.3 \cdot 10^9} = 0.23 \text{ m} \quad (2 \text{ cells})$$

$$1 \text{ cavity } (1.038 \text{ m}) / 9 \text{ cells} = 0.115 \text{ m}$$

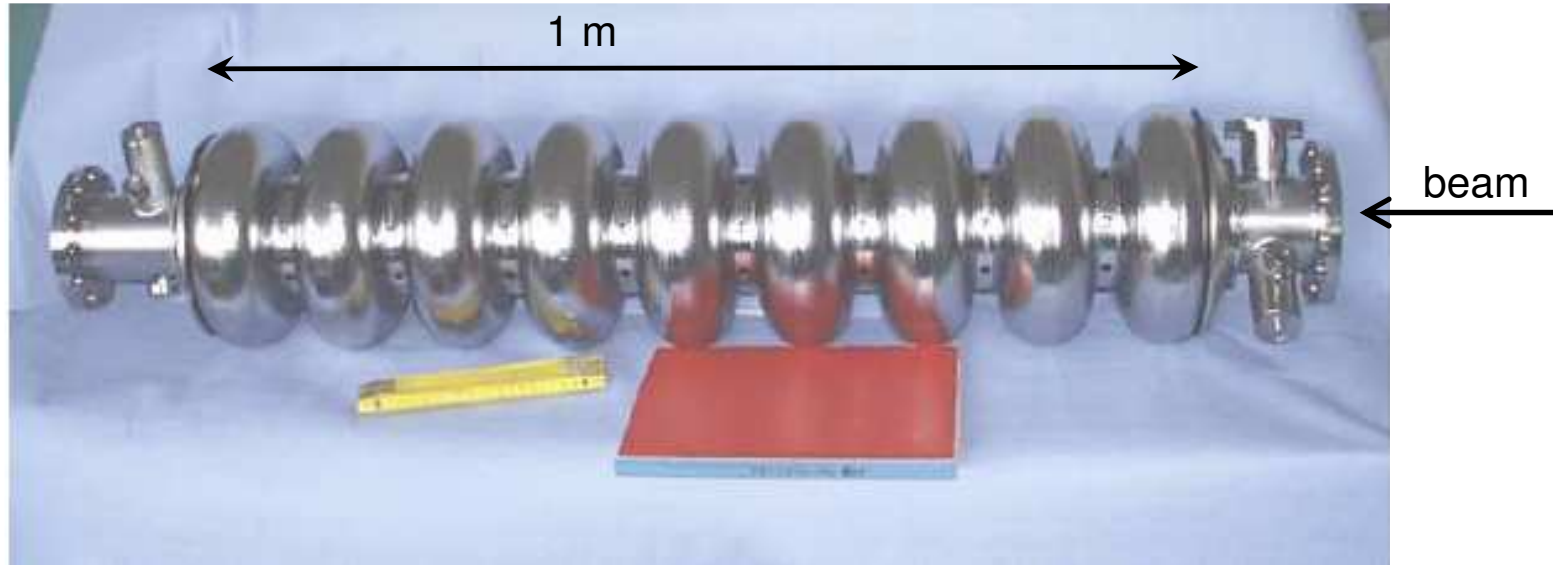
Is there a net acceleration? ..... timing is the key

for protons,  $\beta < 1$

example: ESS (European Spallation Source), Lund, Sweden



# Superconducting cavity used at DESY



# Frequently Asked Questions

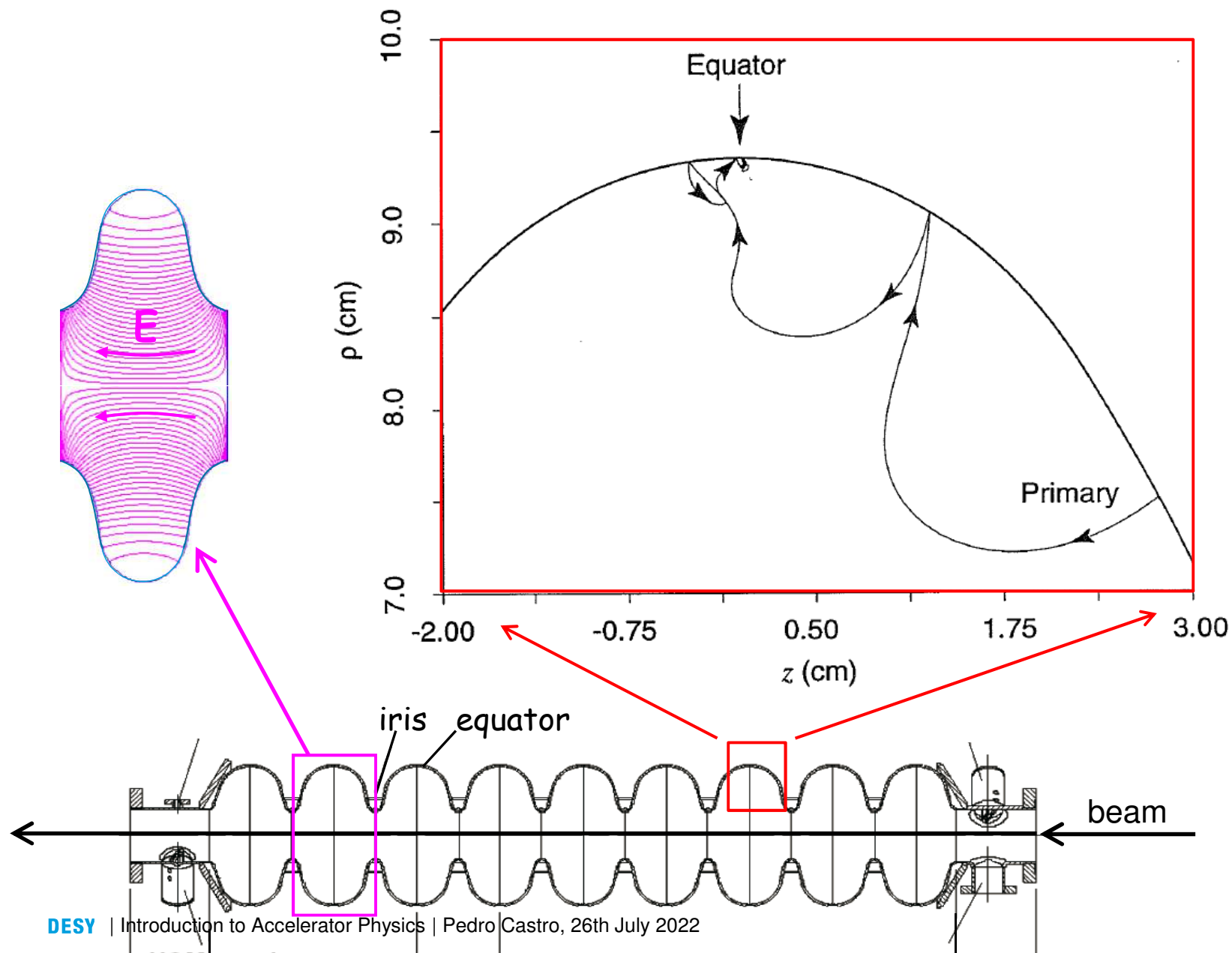
1) Why this shape?

2)

3)

4)

# Multipacting mitigation in superconducting cavities



1) Why this shape? ..... to reduce/avoid multipacting

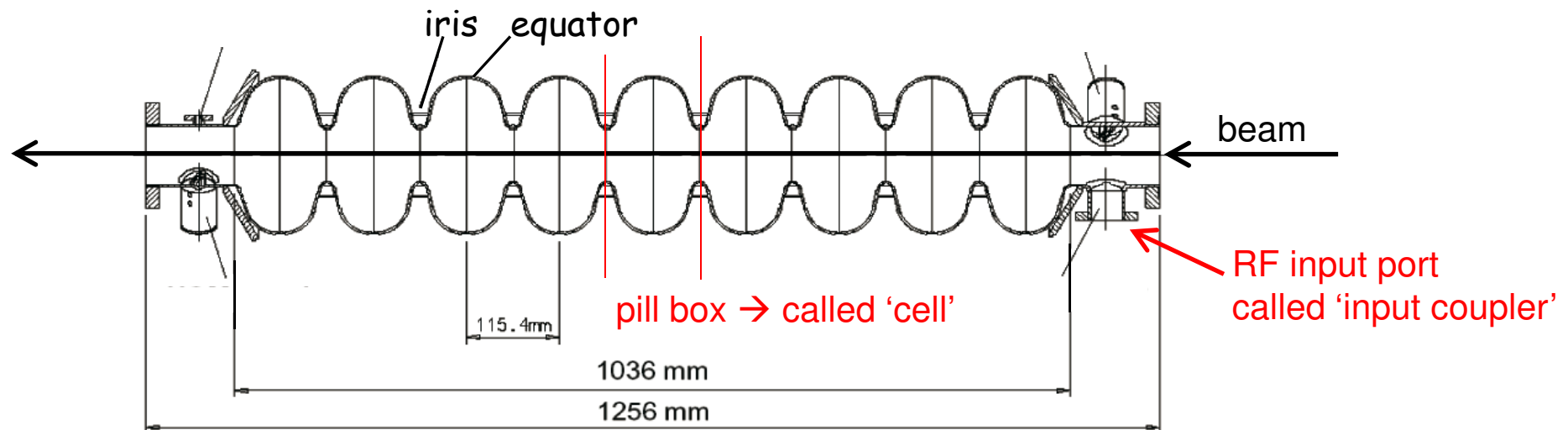
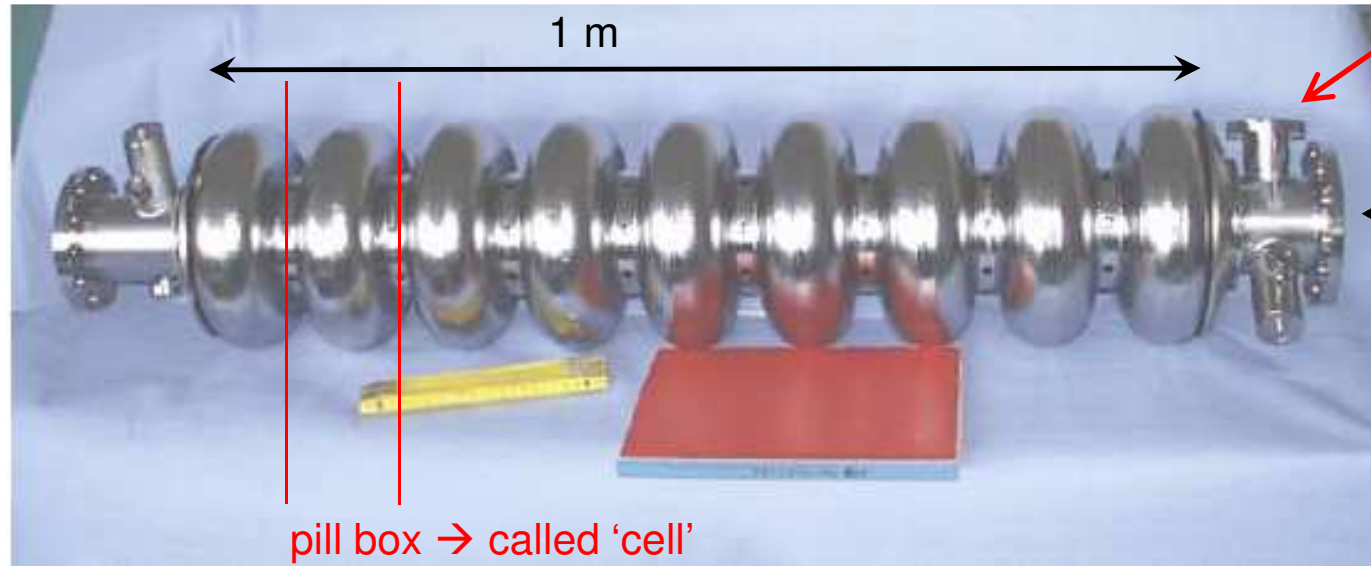
2) How to feed  $\vec{E}$  in?

3)

4)

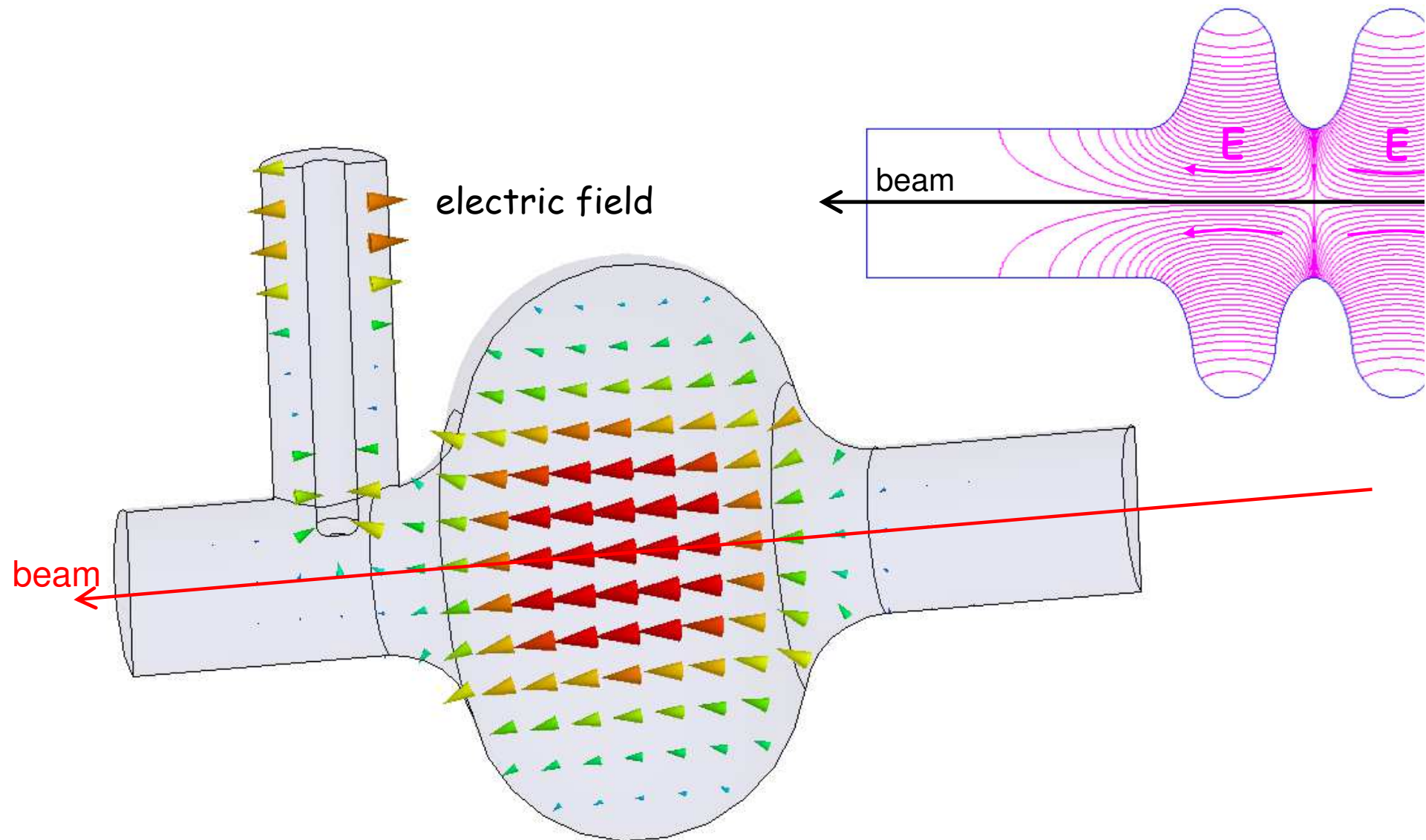
# Superconducting cavity used in FLASH and in XFEL

Superconducting cavity used in FLASH (0.3 km) and in XFEL (3 km)





# Fundamental mode coupler (input coupler)



1) Why this shape? ..... to reduce/avoid multipacting

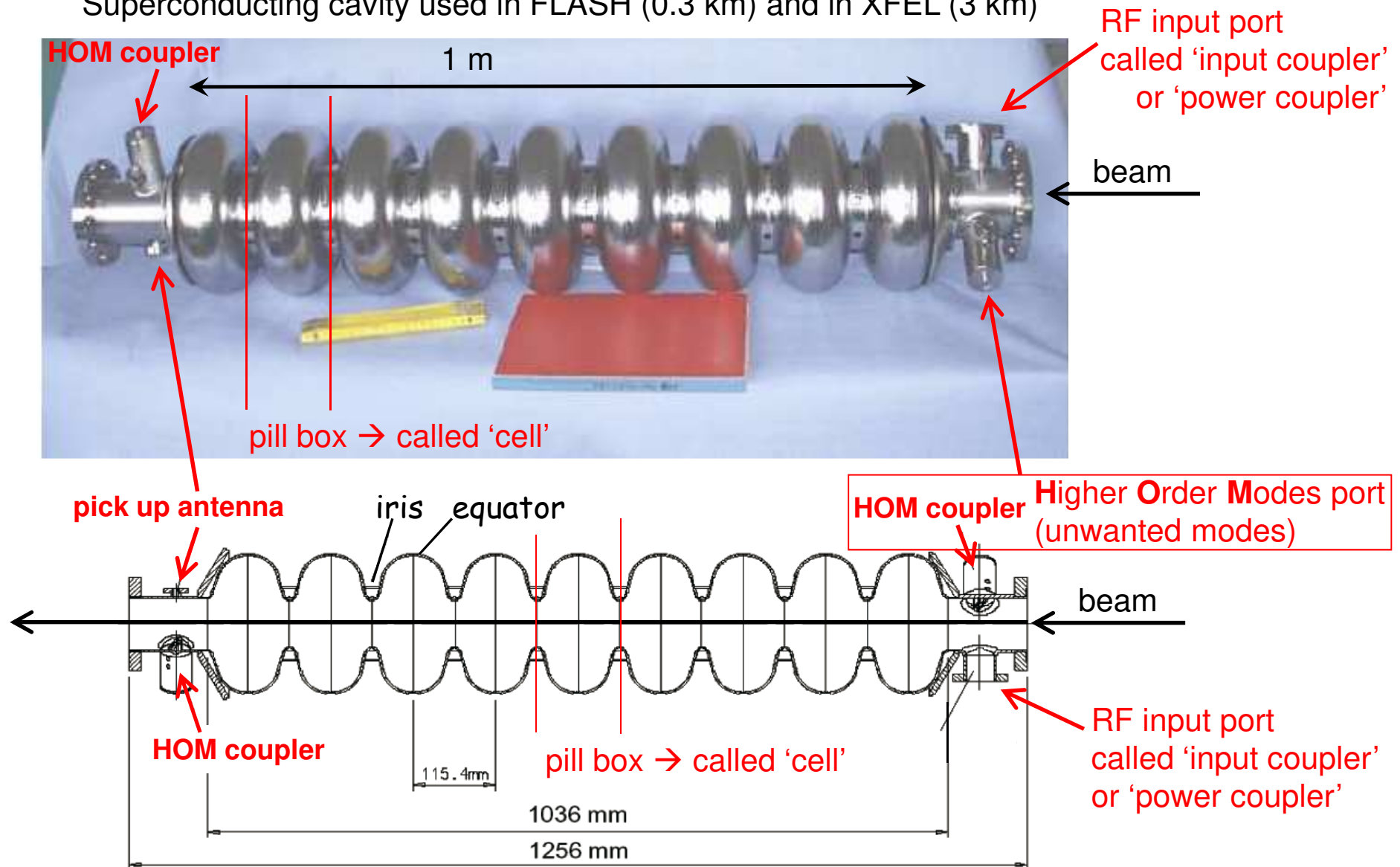
2) How to feed  $\vec{E}$  in? ..... with input couplers

3) How to measure  $\vec{E}$  ?

4)

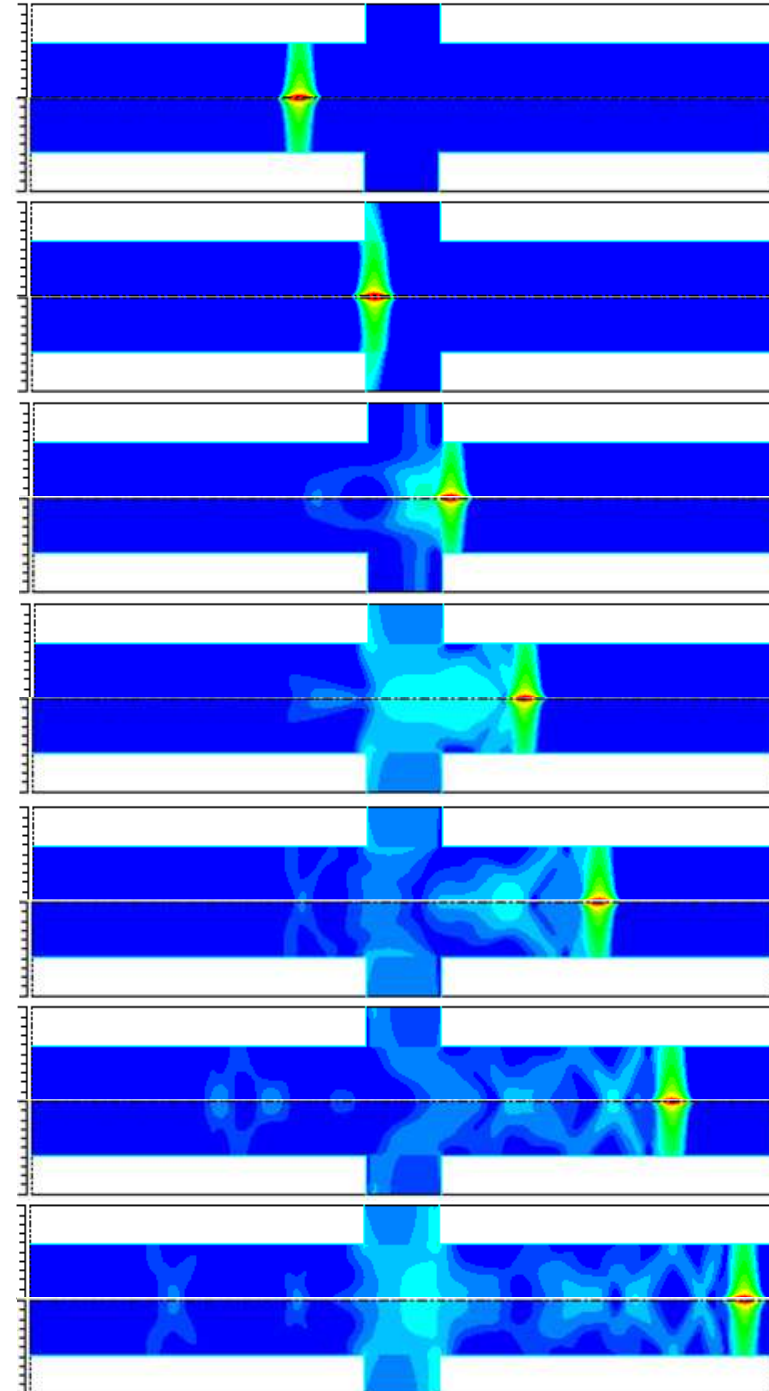
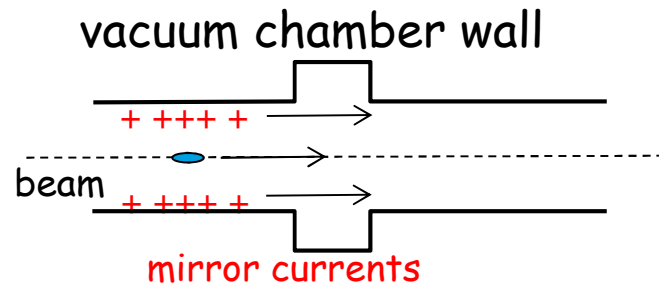
# Superconducting cavity used in FLASH and in XFEL

Superconducting cavity used in FLASH (0.3 km) and in XFEL (3 km)



- 1) Why this shape? ..... to reduce/avoid multipacting
- 2) How to feed  $\vec{E}$  in? ..... with input couplers
- 3) How to measure  $\vec{E}$  ? ..... with pick up antennas
- 4) What are HOM couplers for?

# Wakefields



- 1) Why this shape? ..... to reduce/avoid multipacting
- 2) How to feed  $\vec{E}$  in? ..... with input couplers
- 3) How to measure  $\vec{E}$  ? ..... with pick up antennas
- 4) What are HOM couplers for? ..... to reduce HOM (wakefields)



# Summing-up of this part

Particle acceleration using radio-frequency fields:

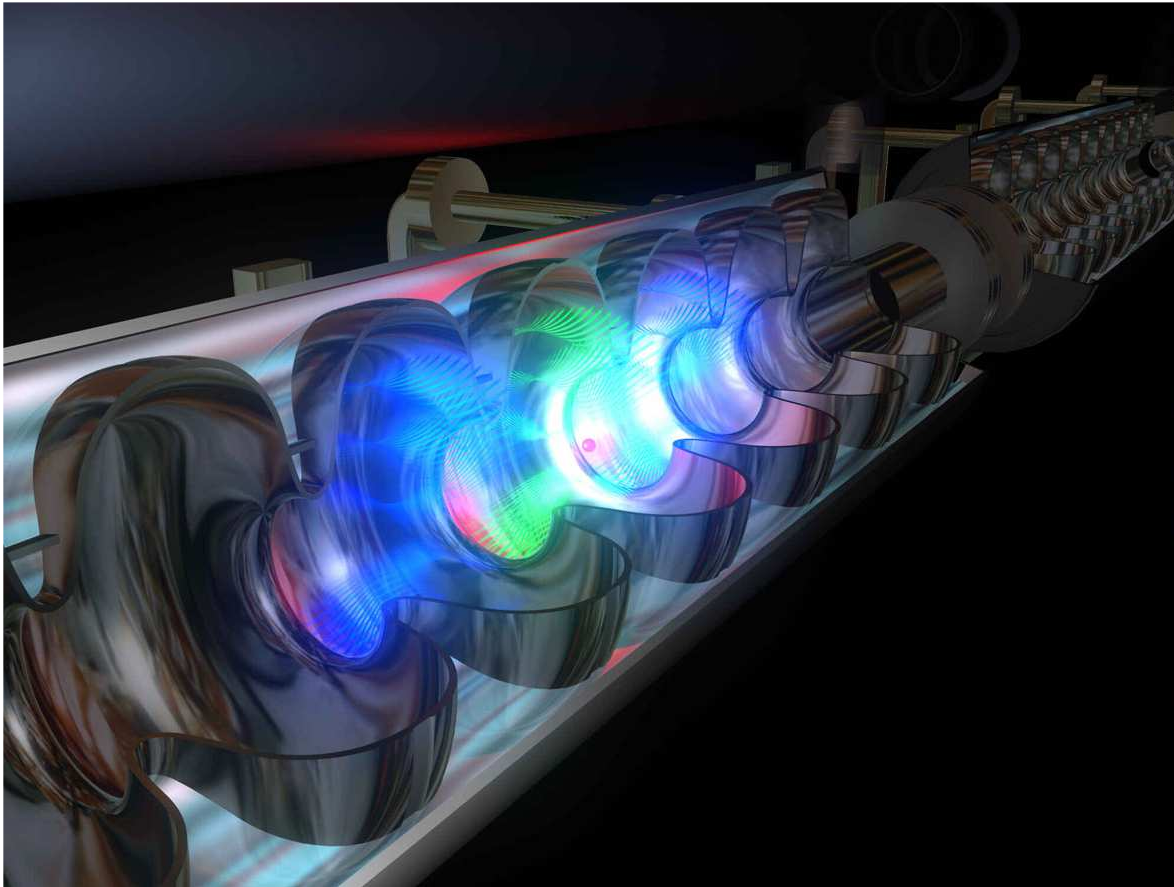
basic cavity:  
pill box

{  
analogy to an LC circuit  
infinite number of solutions for  $\vec{E}$  and  $\vec{B}$   
eq. for the fundamental solution for  $\vec{E}$  and  $\vec{B}$

superconducting  
cavity

{  
multipacting mitigation  
RF couplers and antennas  
wakefields and HOMs  
FLASH and XFEL

## MEDIA DATABASE. “Electron acceleration – a virtual simulation“



DESY → Press → Media database → European XFEL (with filter: media type=movies)

<https://media.desy.de/DESYmediabank/?l=en#l=en&cid=3980&cname=European%20XFEL&f=2165&s=&p=&r=>

YouTube: [https://www.youtube.com/watch?v=FJO\\_DmM4q7M](https://www.youtube.com/watch?v=FJO_DmM4q7M)  
search text: electron acceleration

## Contact

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Elektronen-Synchrotron

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