



LHC projections for the measurement of the Electroweak mixing angle running

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29/11/2022

The Electroweak mixing angle

The Electroweak mixing angle

Casted by Weinberg (1967) in the full EW theory*

$SU(2)_L \times U(1)_Y + \text{Higgs}$

Quantifies **relative strengths** of **electromagnetism** and the **weak force** + ...

... + governs the **Z-boson couplings** to **fermions**

First appearance of a mixing angle between EW boson fields due to Glashow (1961)



Can be used to probe the structure of the EW theory

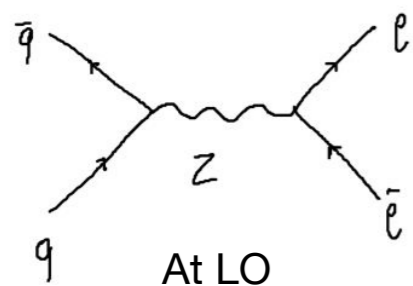
Fundamental **parameter** of the **Standard Model**

$$\sin^2 \theta_W = 1 - \frac{m_W^2}{m_Z^2} = \frac{g'^2}{g^2 + g'^2}$$

*renormalizability of the theory proved by 'tHooft (1971)

Forward-Backward NC DY events

Presence of vector and axial-vector couplings leads to **forward-backward asymmetry** of angular distribution of lepton pairs in DY events



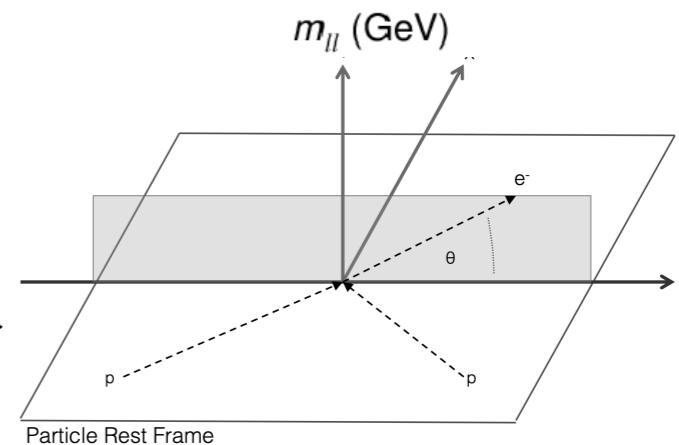
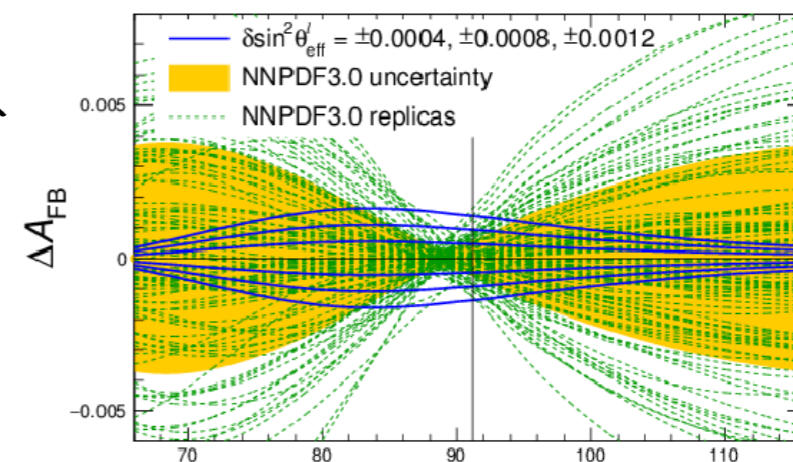
$$\propto 1 + \cos^2 \theta_{ll} + A_4 \cos \theta_{ll}$$

Since $A_4 \propto A_{FB}$ measurement of forward/backward events can be used to determine $\sin^2 \theta_{\text{eff}}^f$

$$A_{FB} = \frac{N_F - N_B}{N_F + N_B}$$

At hadron colliders “dilution effect” → direction of incoming quarks not precisely known:

- ▶ Enhanced sensitivity of A_{FB} to the EW mixing angle at high $|y_{ll}|$
- ▶ Collins-Soper reference frame used

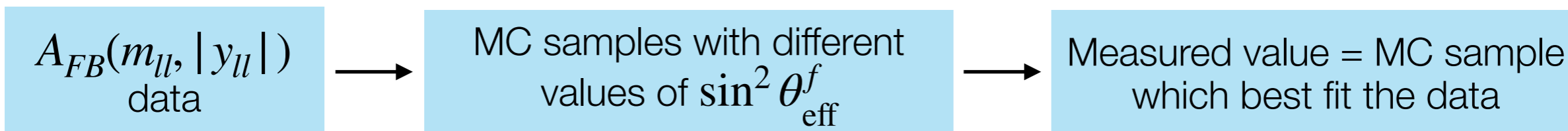


arXiv:1806.00863

arXiv:1902.05142v2

Direct determination of $\sin^2 \theta_{eff}^f$ around the Z pole

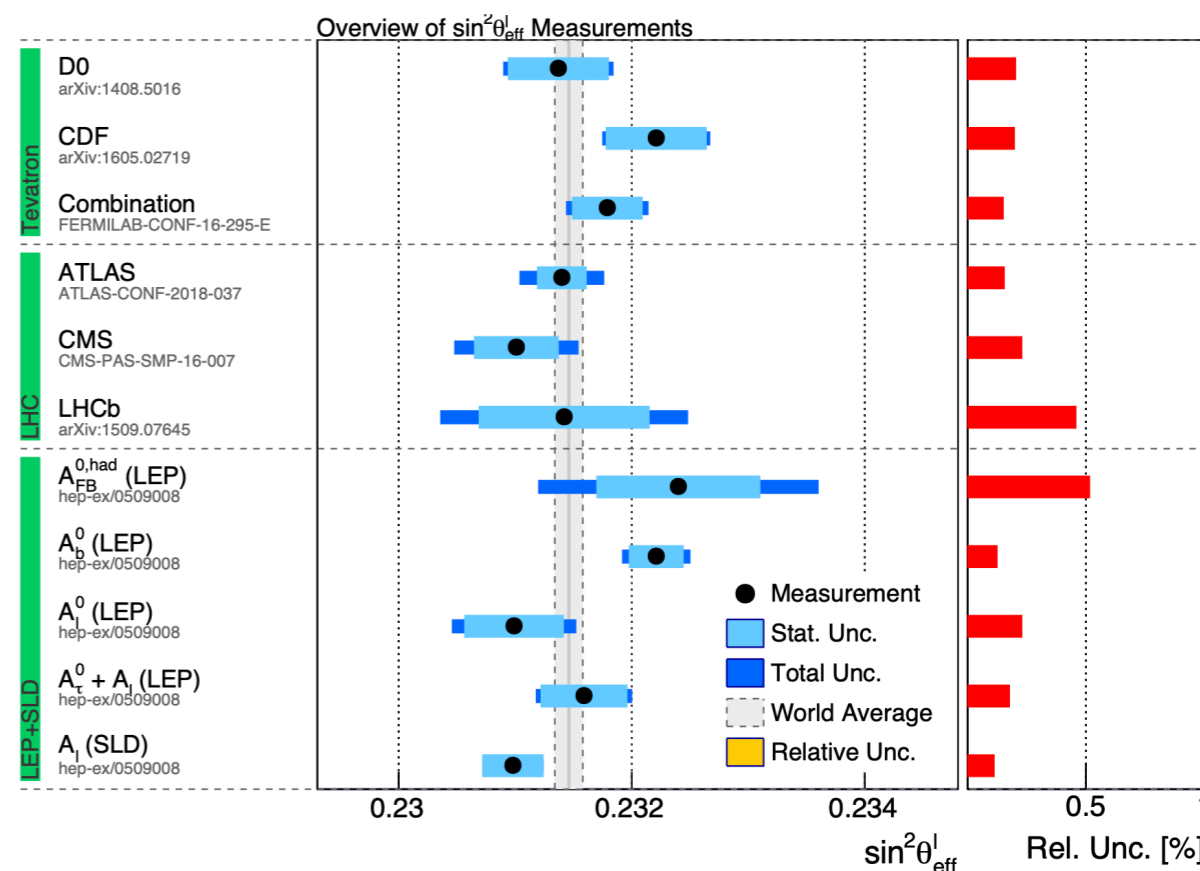
Template fit procedure to measure $\sin^2 \theta_{eff}^f$



Measurements of A_{FB} around the Z pole at lepton (hadron) colliders → relative precision on $\sin^2 \theta_{eff}^f$ of 0.1(0.2) %

Measurements at the LHC has already reached the same precision as the Tevatron → expected big improvement in the nearly future:

- ▶ **More statistics** available (from Run 3 and HL-LHC)
- ▶ **Improved analysis** techniques and **PDF constraining** methods



LEP + SLD + Hadron coll. = 0.23151 ± 0.00014

[arXiv:1902.05142v2](https://arxiv.org/abs/1902.05142v2)

Ongoing work within the **LHCEWWG** to quantify **uncertainties** and **theoretical issues** in the extraction of $\sin^2 \theta_{eff}^f$ (see [EW precision measurements subgroup](#))

The EW mixing angle at high-masses

At lepton/hadron colliders $\sin^2 \theta_{\text{eff}}^f$ measured at the Z boson peak \rightarrow at **high-masses** can be used to **probe extra massive gauge bosons**:

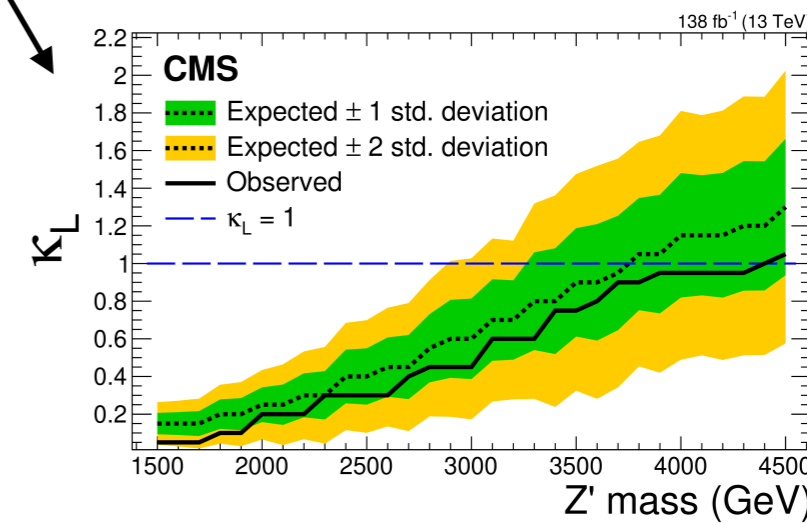
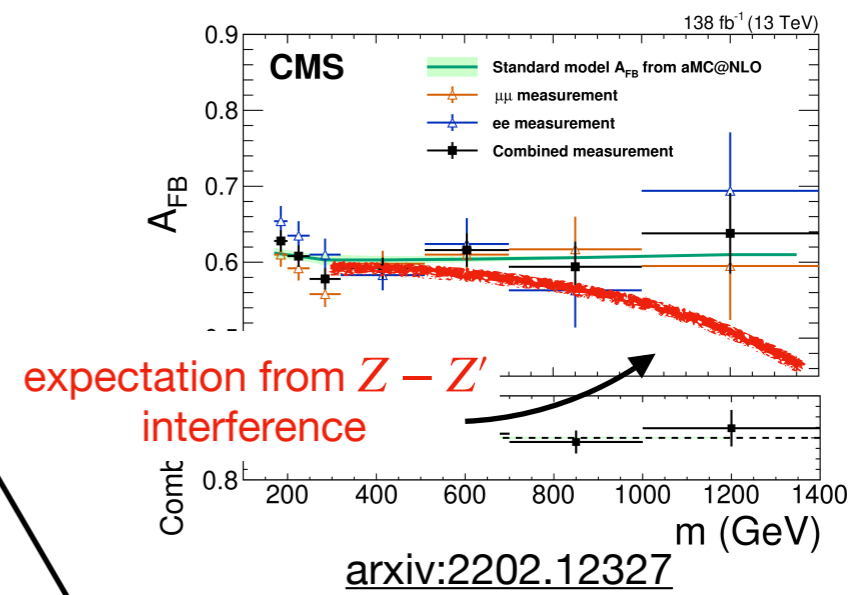
- ▶ New resonances not visible to direct searches if they have large widths...
- ▶ ...but can interfere with SM EW bosons introducing structures in the measured A_{FB}

The CMS Collaboration has recently measured A_{FB} at high-masses \rightarrow extracted exclusion limits For a Z' in the sequential SM

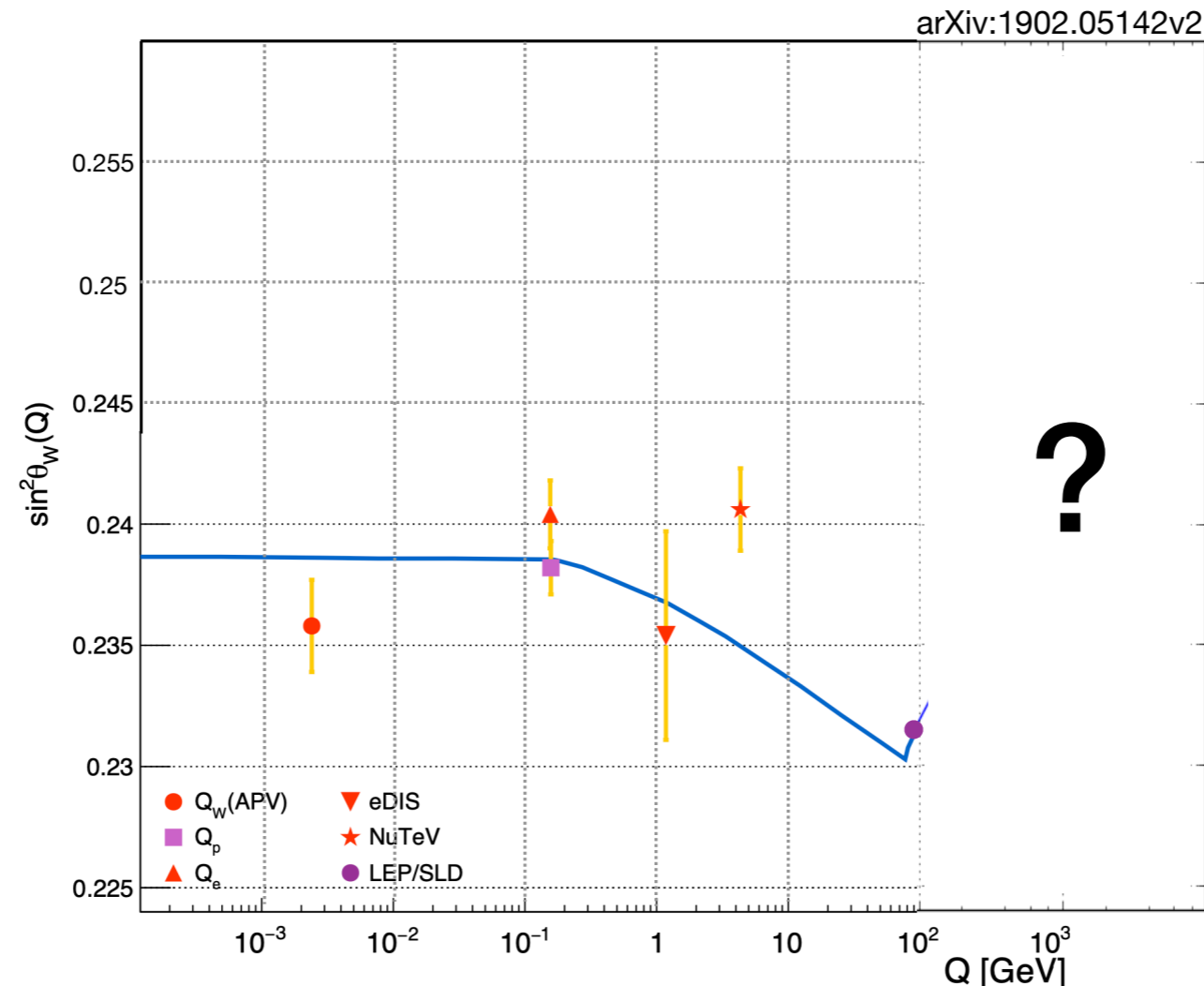
To probe the **presence** of **new physics** outside the Z peak in a **model-independent way**



Need to **compare** the **experimental data** (at high-masses) with theoretical predictions which **include** the **energy dependence of the EW mixing angle**



The energy dependence of $\sin^2 \theta_W$



The EW mixing angle value is expected to show an **energy dependence** which can be **predicted** by the RGE for $\sin^2 \theta_W^{\bar{M}S}(\mu)$ in the $\bar{M}S$ renormalisation scheme (arXiv:hep-ph/0409169v2)

Several measurements at low Q^2 (atomic parity violation) → but **no experimental results** on the running of the EW mixing angle at **high energy**

Will it be possible to test the running of $\sin^2 \theta_W$ @ the LHC?

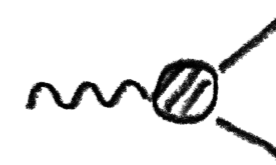
Implementation of $\sin^2 \theta_W^{\overline{MS}}(\mu)$ in POWHEG-BOX

The energy dependence of $\sin^2 \theta_W$ has recently been implemented into POWHEG-BOX
Z_ew BMNNPV:

- ▶ Use an **EW input scheme** where the **EW mixing angle** is **explicit** ($\alpha(\mu), m_Z, \sin^2 \theta_W(\mu)$)
- ▶ Within this “hybrid” scheme the m_Z value is renormalised to its On-Shell value while the **fine structure constant** and the **EW mixing angle** are renormalised in the \overline{MS} scheme, i.e. depend on the energy scale μ
- ▶ Predictions used in this work are obtained at an “**improved LO**” with $\alpha(\mu)$ and $\sin^2 \theta_W(\mu)$ as running parameters \rightarrow the matrix element of the NC DY process is expressed as:

$$|M|^2 \sim \left| \alpha(\mu) \cdot \text{diagram}_\gamma + \frac{\alpha(\mu)}{\sin^2 \theta_W(\mu)} \cdot \text{diagram}_Z \right|^2$$

Here the contributions from higher order expansion are resummed



Analysis strategy

Extract the expected sensitivity on the running of the EW mixing angle at **high energies** up to the **TeV** scale $\rightarrow m_{ll}$ is used as the **dynamic energy scale**

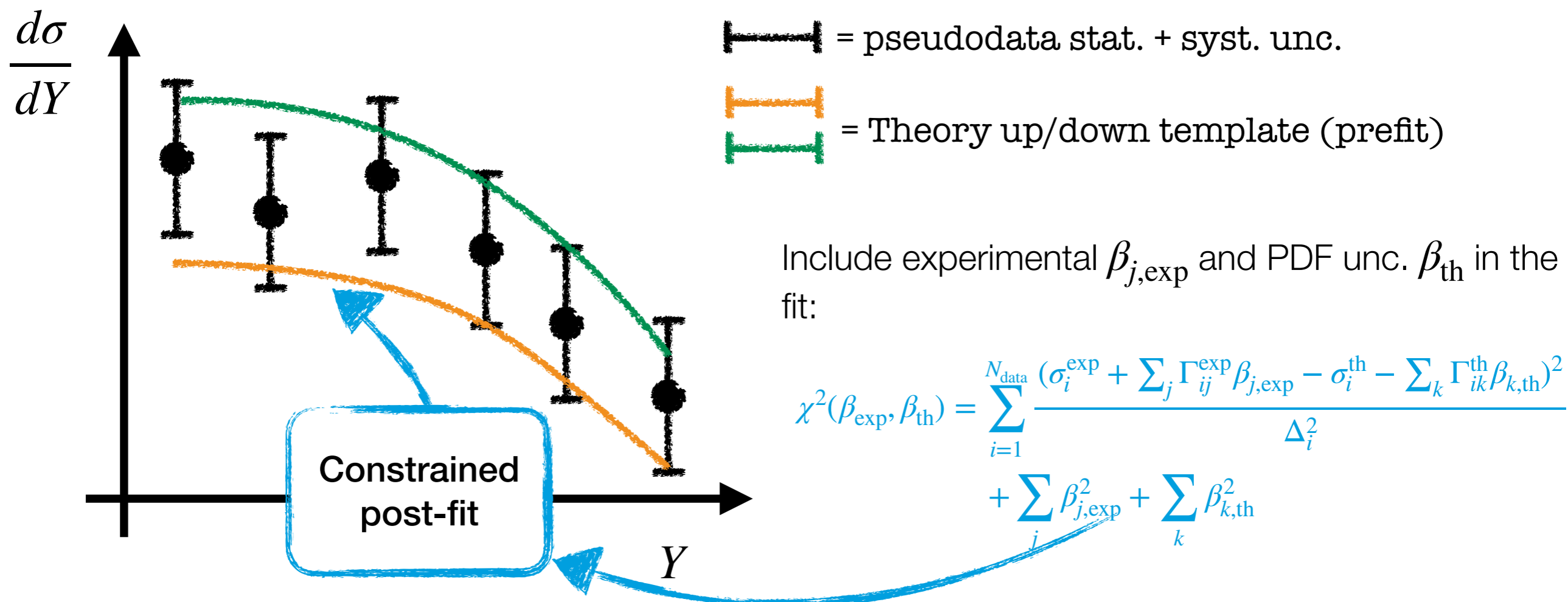
The choice of EW parameters input scheme for theory predictions is **fundamental** \rightarrow scheme where $\sin^2 \theta_W$ can be varied **independently**

Use one billion events calculated @ NLOQCD + improved LOEW with POWHEG-BOX, showered with PYTHIA8 to perform a template fit

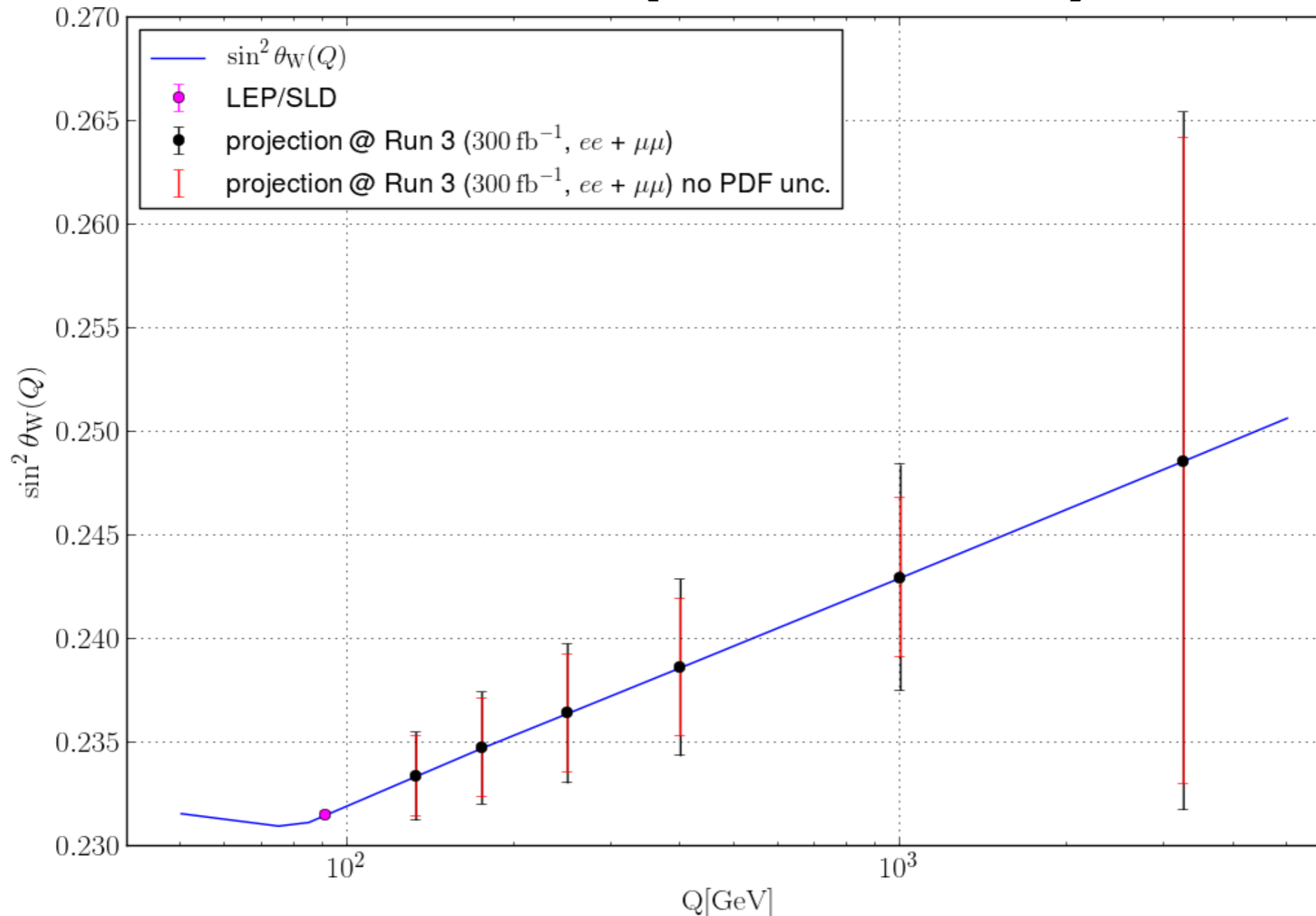
- ▶ Extract the expected sensitivity to $\sin^2 \theta_W^{\bar{M}S}(m_{ll})$ in **several mass bin**
- ▶ Two LHC scenarios considered: **Run 3** (300 fb^{-1}) and **HL-LHC** (3000 fb^{-1})

Analysis strategy

1. Pseudo-data generated using the EW parameters values at the Z peak as inputs
2. Templates obtained by shifting up/down the expected input value of the EW mixing angle by ± 0.01
3. The expected sensitivity $\delta \sin^2 \theta_W^{\overline{MS}}(m_{ll})$ extracted by fitting the pseudo-data using the xFitter fitting tool ([arXiv:1410.4412](https://arxiv.org/abs/1410.4412))



Results @ 300 fb^{-1} (LHC Run 3)

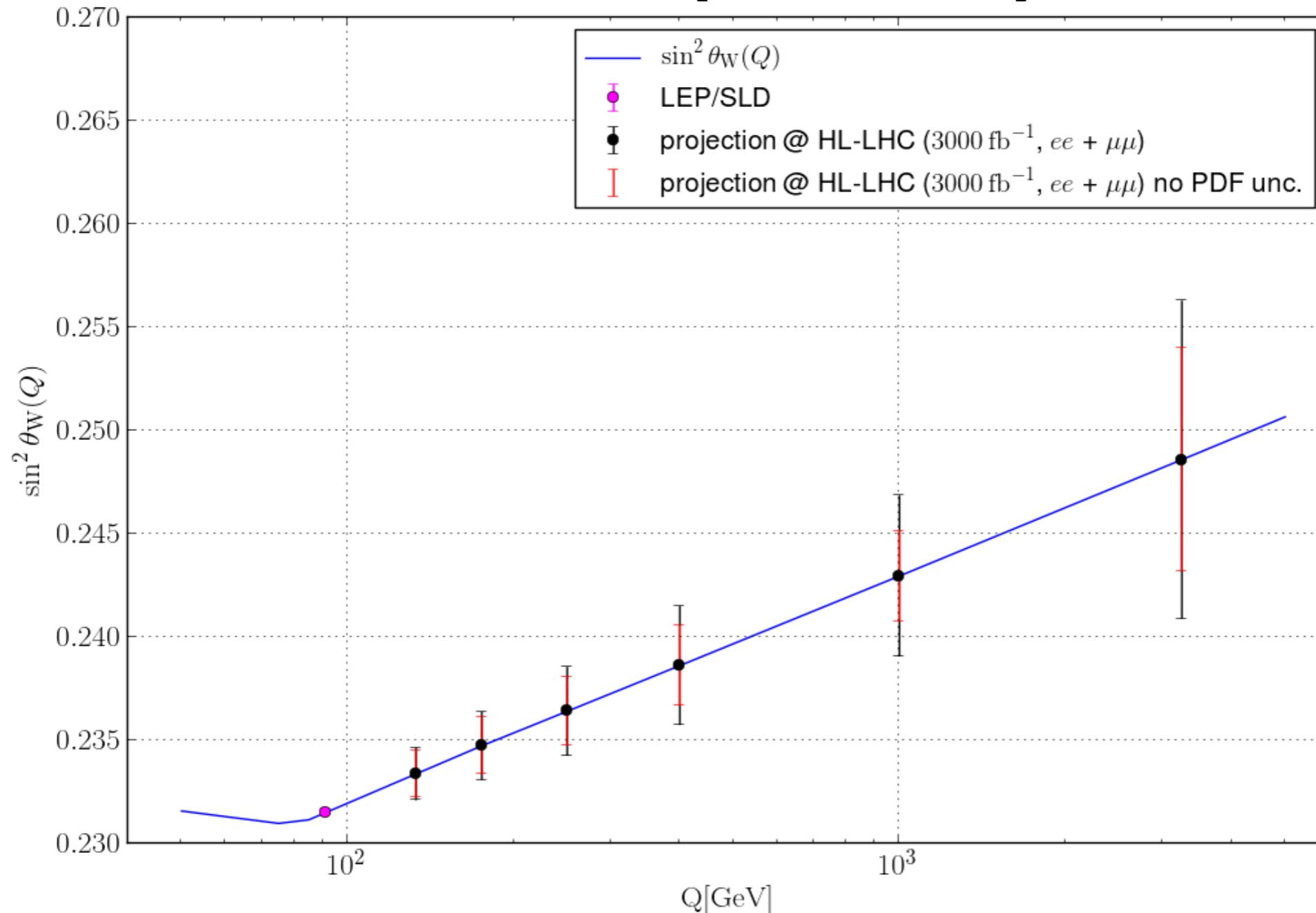


| m_{ll} | $\sin^2 \theta_W(m_{ll})$ | $\delta \sin^2 \theta_W(m_{ll})$ | $\delta \sin^2 \theta_W(m_{ll})$ (%) |
|----------|---------------------------|----------------------------------|--------------------------------------|
| 133 | 0,2334 | 0,0021 | 0,9 |
| 175 | 0,2347 | 0,0027 | 1,2 |
| 250 | 0,2364 | 0,0034 | 1,4 |
| 400 | 0,2386 | 0,0043 | 1,8 |
| 1000 | 0,2430 | 0,0055 | 2,2 |
| 3250 | 0,2486 | 0,0168 | 6,8 |

Expected sensitivity defined as the post-fit uncertainty on $\sin^2 \theta_W^{\overline{MS}}(m_{ll})$



Results @ 3000 fb^{-1} (HL-LHC)



| m_{ll} | $\sin^2 \theta_W(m_{ll})$ | $\delta \sin^2 \theta_W(m_{ll})$ | $\delta \sin^2 \theta_W(m_{ll})$ (%) |
|----------|---------------------------|----------------------------------|--------------------------------------|
| 133 | 0,2334 | 0,0013 | 0,5 |
| 175 | 0,2347 | 0,0017 | 0,7 |
| 250 | 0,2364 | 0,0021 | 0,9 |
| 400 | 0,2386 | 0,0029 | 1,2 |
| 1000 | 0,2430 | 0,0039 | 1,6 |
| 3250 | 0,2486 | 0,0077 | 3,1 |

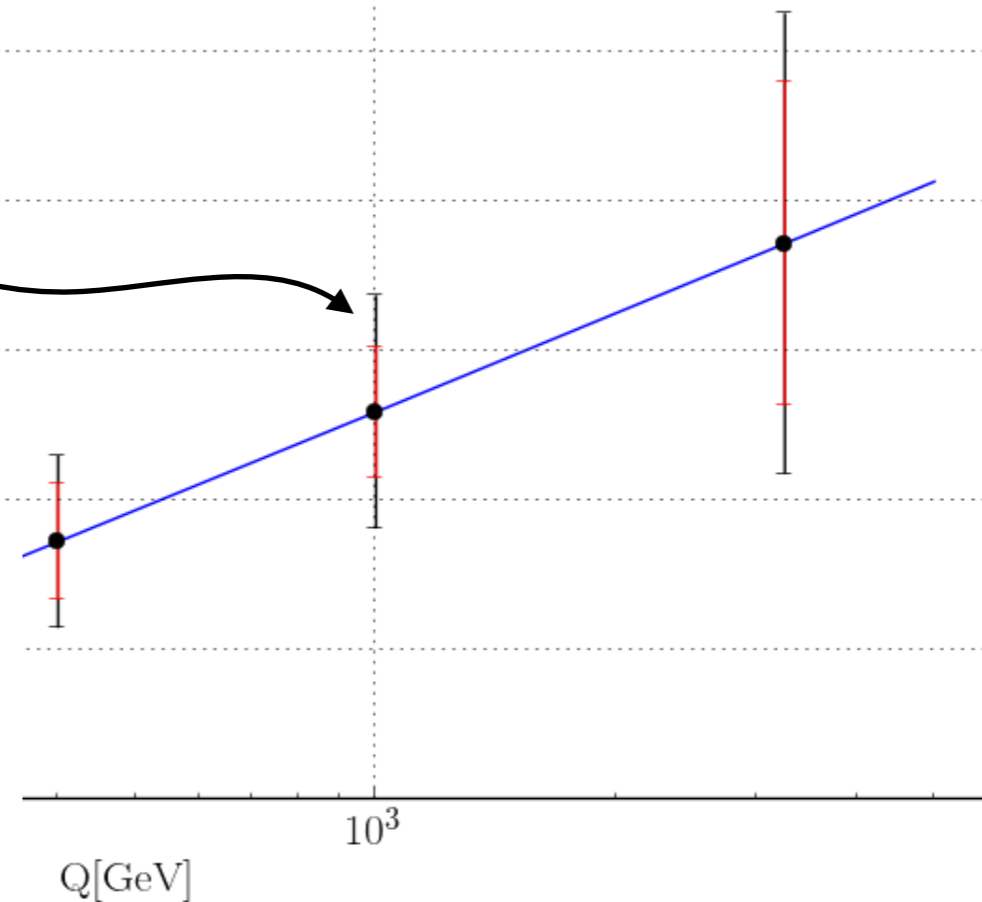
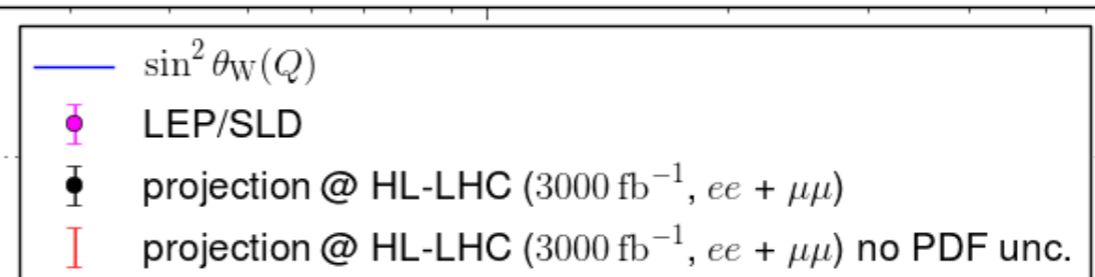
Expected sensitivity defined as the post-fit uncertainty on $\sin^2 \theta_W^{\overline{MS}}(m_{ll})$



Results @ 3000 fb⁻¹ (HL-LHC)

- Impact of PDFs uncertainties not negligible with the current knowledge of PDFs
- The expected sensitivity @ HL-LHC ranges from **0.5 %** to **3 %** (in the higher mass bin)

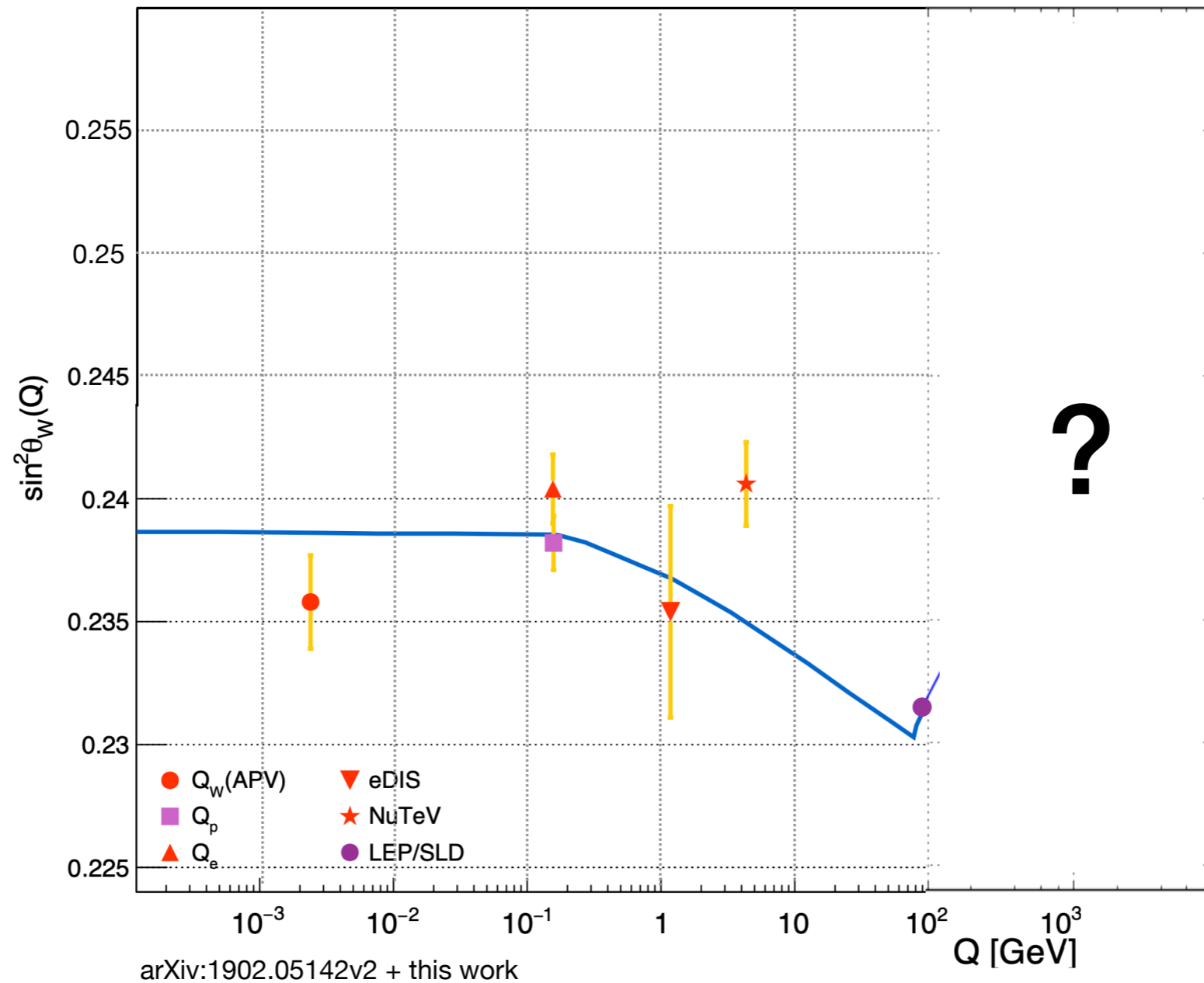
| m_{ll} | $\sin^2\theta_W(m_{ll})$ | $\delta \sin^2\theta_W(m_{ll})$ | $\delta \sin^2\theta_W(m_{ll})$ (%) |
|----------|--------------------------|---------------------------------|-------------------------------------|
| 133 | 0,2334 | 0,0013 | 0,5 |
| 175 | 0,2347 | 0,0017 | 0,7 |
| 250 | 0,2364 | 0,0021 | 0,9 |
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| 3250 | 0,2486 | 0,0077 | 3,1 |



Expected sensitivity defined as the post-fit uncertainty on $\sin^2 \theta_W^{MS}(m_{ll})$

Results

The **expected sensitivity @ HL-LHC** compared to the experimental determinations of $\sin^2 \theta_W^{MS}(\mu)$ at lower energies:



Summary

First projections for the LHC measurement of $\sin^2 \theta_W$ at **high masses!**

Paved the road to **future measurements** of the EW mixing @ the LHC:

- ▶ The **running** of the EW mixing angle is **implemented** in a **public event generator code** (POWHEG-BOX Z_ew_BMNNPV) → allows for extraction of $\sin^2 \theta_W$ at high-energy scale
- ▶ This sensitivity study shows that the **HL-LHC** is expected to measure the **energy dependence** of $\sin^2 \theta_W$ with a **precision of few %** up to $\approx 3 \text{ TeV}$ (conservative estimate)

Future improvements:

- ▶ From a theoretical perspective predictions using full NLO EW calculations → ongoing
- ▶ From the phenomenology point of view the impact and constraints of PDFs uncertainties → under investigation

Stay tuned!



Backup

Analysis strategy

Fitted $\frac{d\sigma}{d|y_{ll}|dm_{ll}}$ simultaneously for **forward** and **backward** events

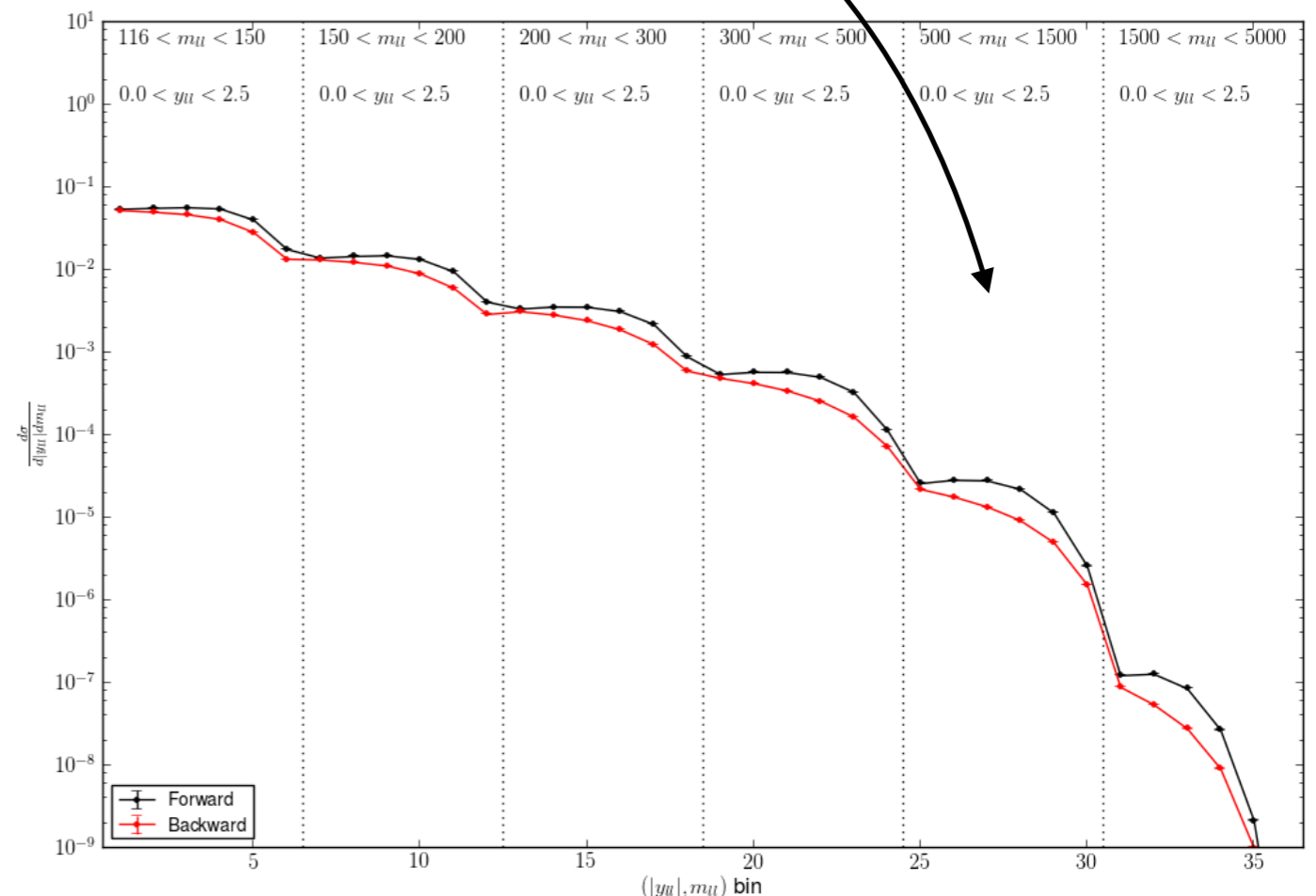
Selection cuts intended to **reproduce** a **realistic** measurement **scenario**:

$$p_T^l > 40 \text{ (30) GeV}, |\eta^l| < 2.5$$

Binning choice to **balance** between **sensitivity** and expected **number of events**

$$m_{ll} : [116, 150, 200, 300, 500, 1500, 5000]$$

$$y_{ll} : [0.0, 0.4, 0.8, 1.2, 1.6, 2.0, 2.5]$$



Emulate detector efficiencies using the in RIVET:

- ▶ ATLAS Run2 ID/reco efficiencies and smearing for electrons ([Eur. Phys. J. C 79 \(2019\) 639](#)) and muons used ([ATL-PHYS-PUB-2015-037](#))
- ▶ Selection efficiencies: $\approx 50\%$ flat as a function of m_{ll} for ee and $\mu\mu$ events

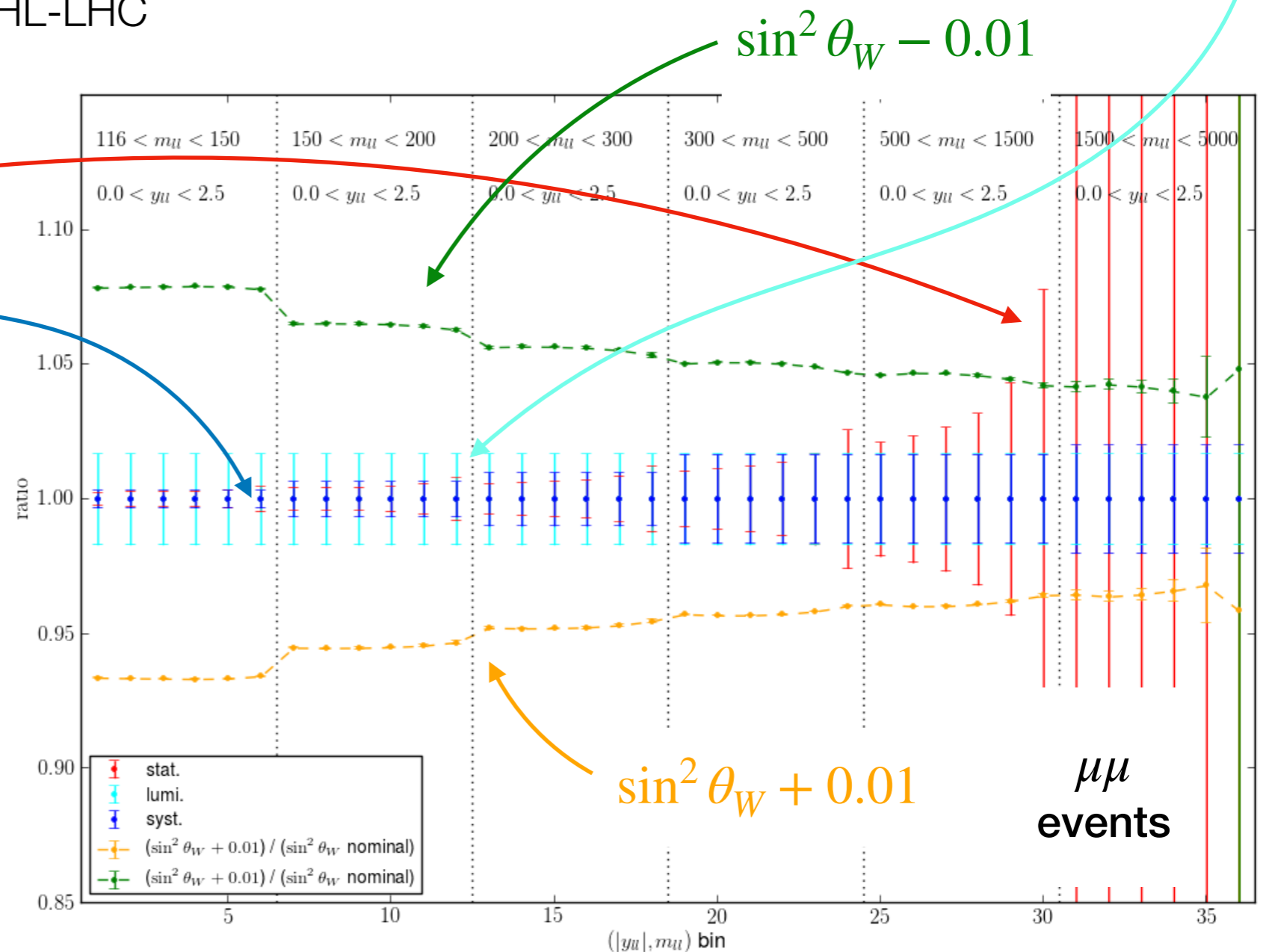
Measurement uncertainties

- ▶ **Expected statistical uncertainties** from reconstructed-level expected number of events (for different luminosities)
- ▶ **Expected systematic uncertainties** from the current measurements projected @ Run 3 (reduced by factor 2) and HL-LHC (reduced by factor 4)
- ▶ **Expected luminosity uncertainty** at HL-LHC → 1% value used

Pre-fit impacts of each uncertainty source on

$$\frac{d\sigma}{d|y_{ll}|dm_{ll}}$$

for **forward events** in the $\mu\mu$ channel



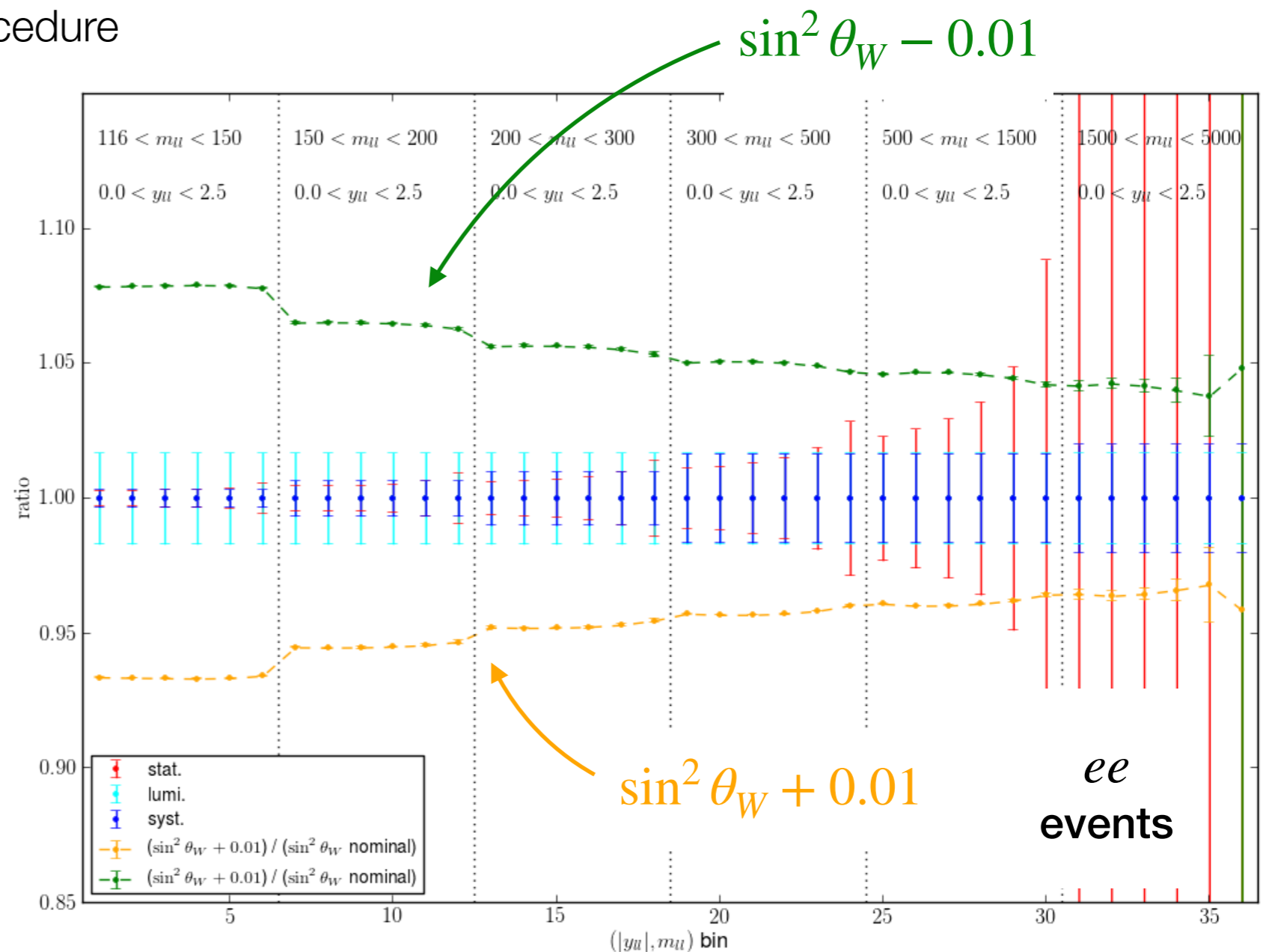
Measurement uncertainties

- ▶ **Expected PDF uncertainties** using aMCFast grids convoluted with the NNPDF31_nnlo_as_0118_hessian PDF set:
 - **not showed** here but included in the fit
 - reduced in the fitting procedure
- ▶ **Scale uncertainties** are **not considered**
 - expected to be $< 0.5\%$ at NNNLO QCD ([JHEP03\(2022\)116](#))

Pre-fit impacts of each uncertainty source on

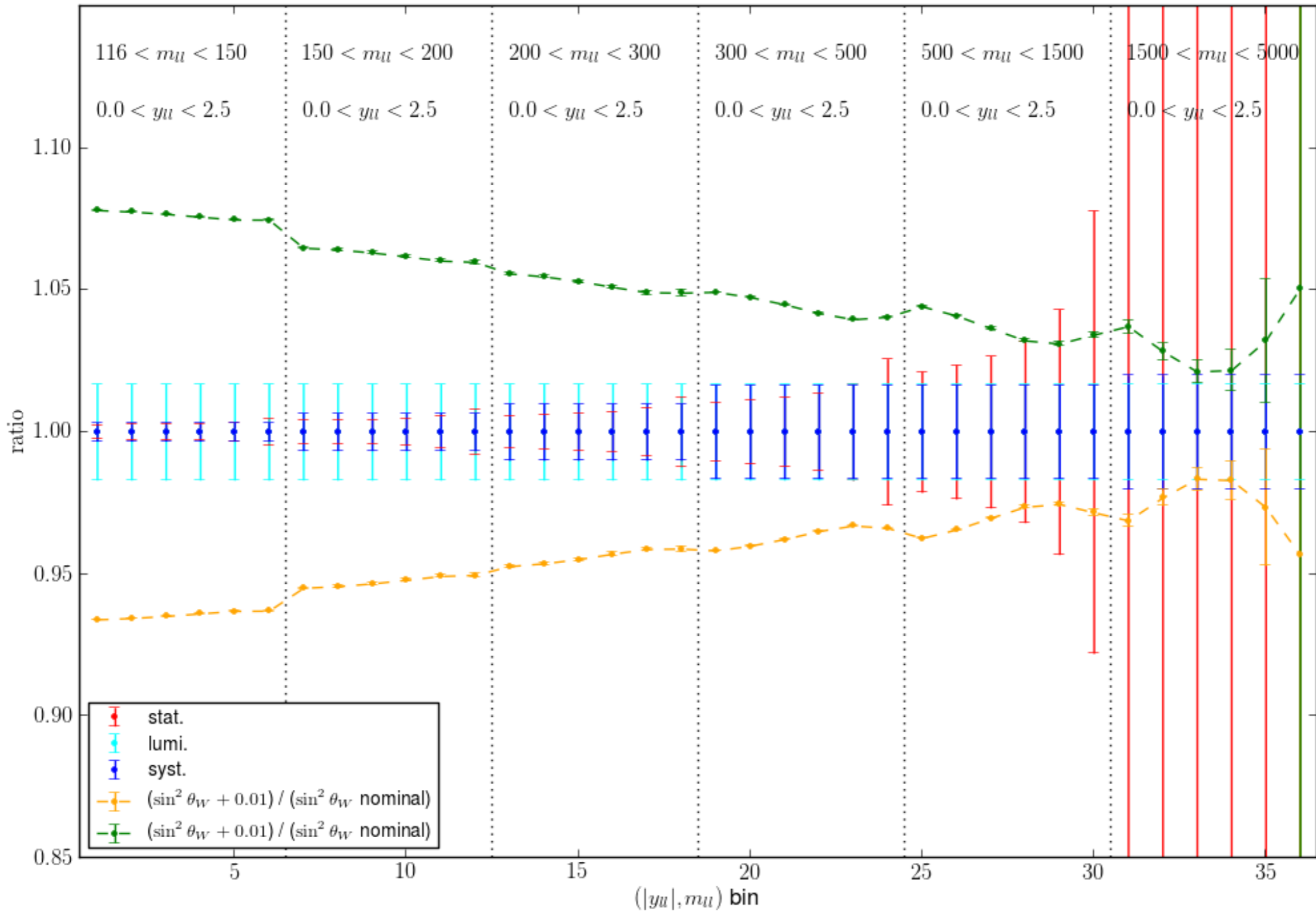
$$\frac{d\sigma}{d|y_{ll}|dm_{ll}}$$

for **forward events** in the ee channel



$$\frac{d\sigma}{d|y_{ll}| dm_{ll}}$$

for backward $\mu\mu$ events



$$\frac{d\sigma}{d|y_{ll}|dm_{ll}}$$

for backward ee events

