

# EXPLORING THE NON-EQUILIBRIUM EARLY UNIVERSE: FROM GRAVITATIONAL WAVES TO SPECTRAL DISTORTIONS

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Particle and Astroparticle Physics  
Colloquium in Hamburg

DESY

January 24, 2023

# Overview

## Messengers from the early Universe

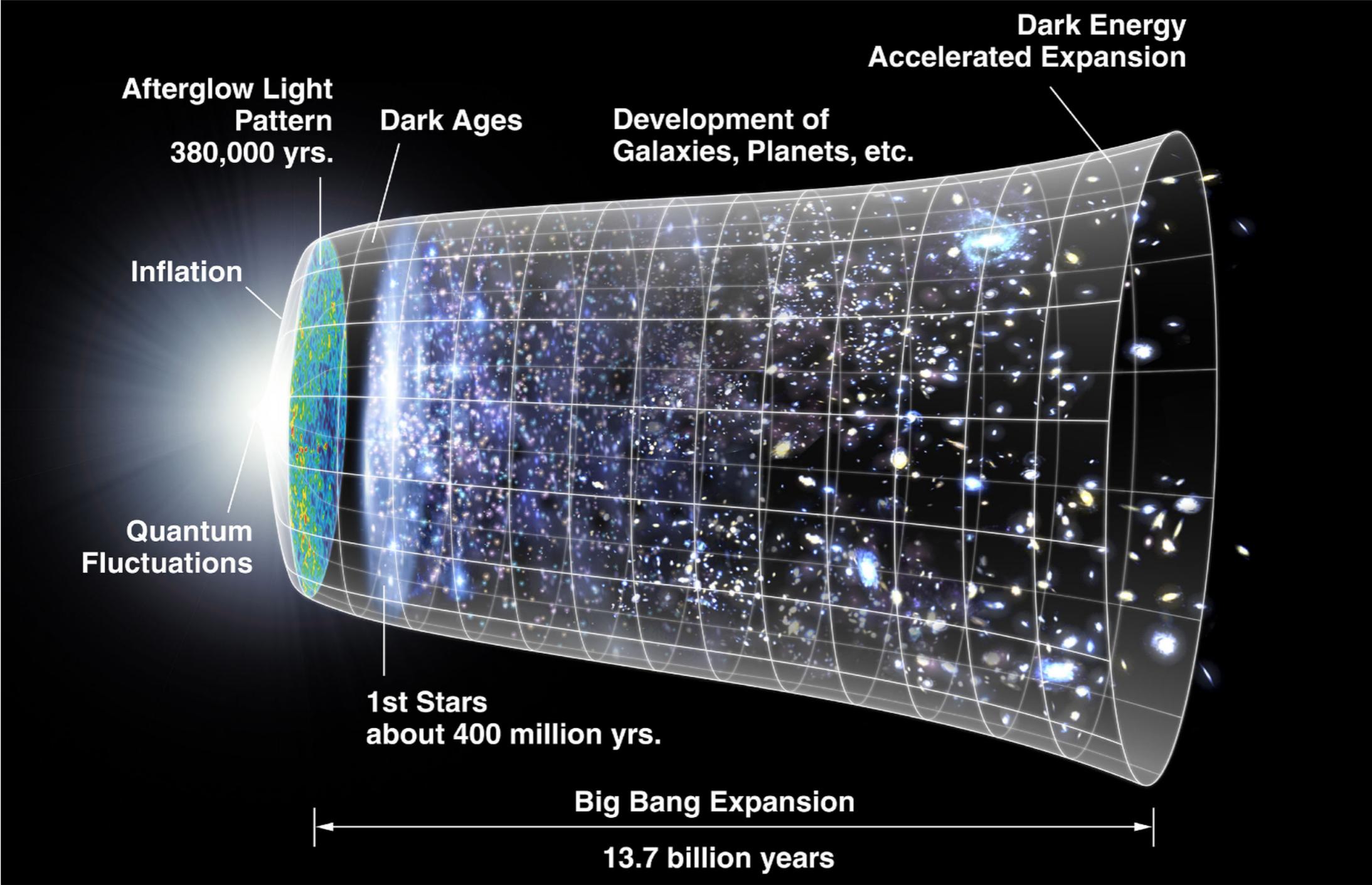
- ▶ Gravitational waves
- ▶ (Distortions of the ) Cosmic microwave background

## Messages from non-equilibrium physics

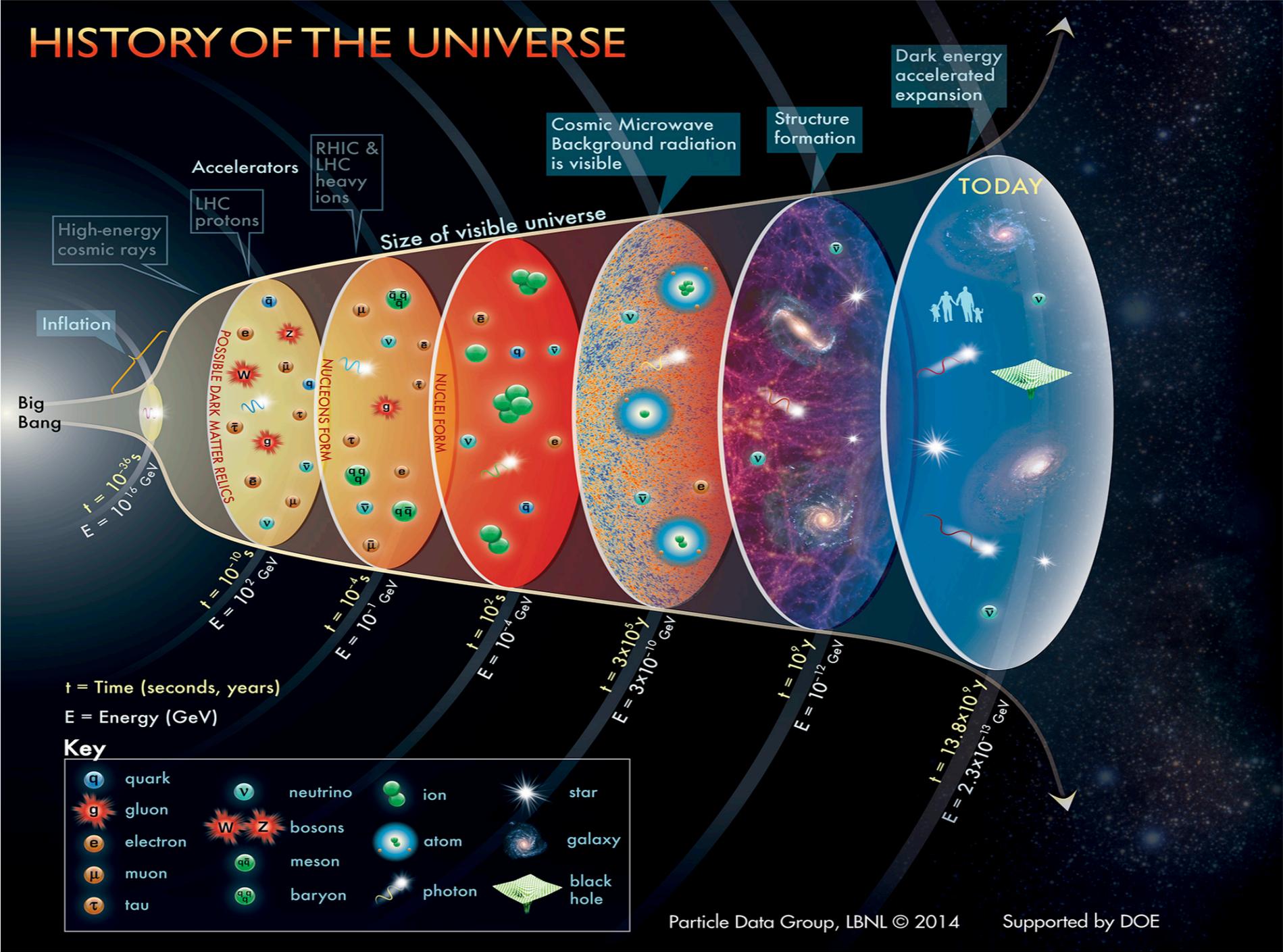
- ▶ Phase transitions
- ▶ Axion/scalar field dynamics, strings, domain walls, ...

What do we know about  
the early Universe?

# Thermal history



# Thermal history and particle physics



# Thermal history and particle physics

Early universe holds the key to many fundamental open questions in particle physics

- What is dark matter, and how is it made
- What is the origin of matter
- What is the dynamics of inflation and reheating

# The early Universe soup



# The early Universe soup



# The early Universe soup

How to identify ingredients

Taste

- ▶ i.e. study Universe today

Smell in kitchen

- ▶ Cosmic microwave background

Splashes in kitchen

- ▶ Gravitational Waves (from phase transitions)



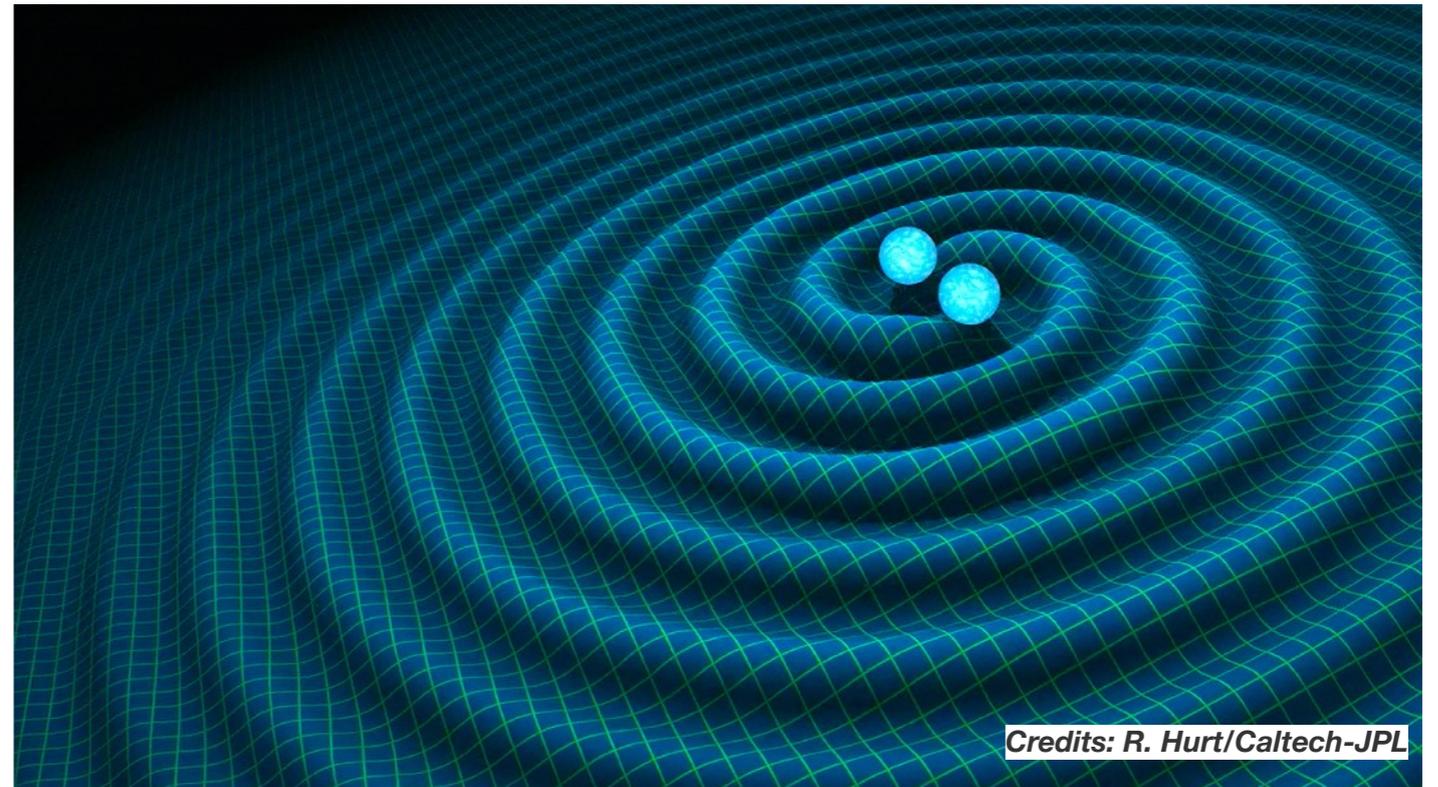
# Messengers I: Gravitational waves

Travel undisturbed  
from earliest times

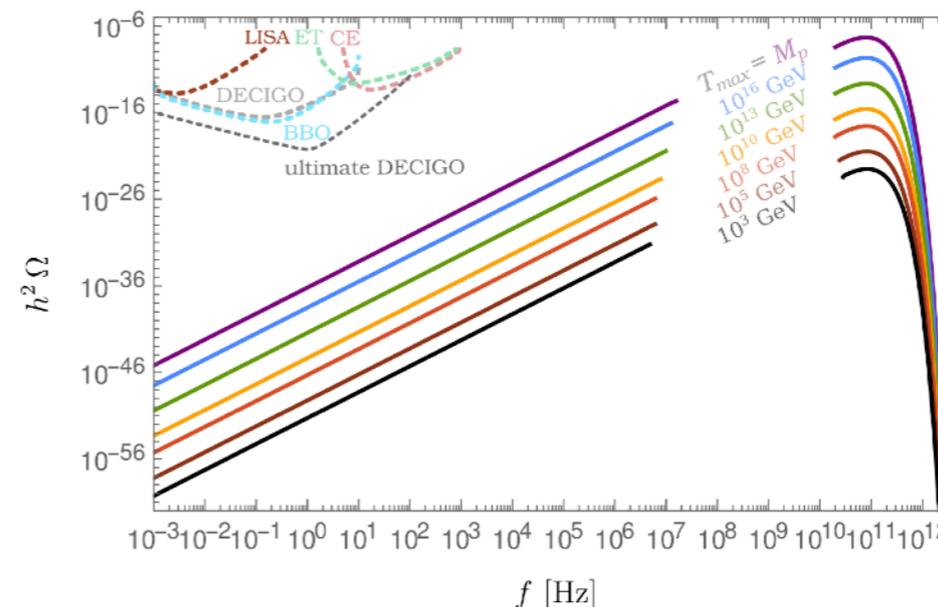
Only produced by  
violent, non-equilibrium  
physics

- ▶ Stochastic GW  
background

Or with very very (very!)  
high temperatures



Credits: R. Hurt/Caltech-JPL



From Ringwald,  
Schütte-Engel,  
Tamarit, 2020

# Messengers II: Photons

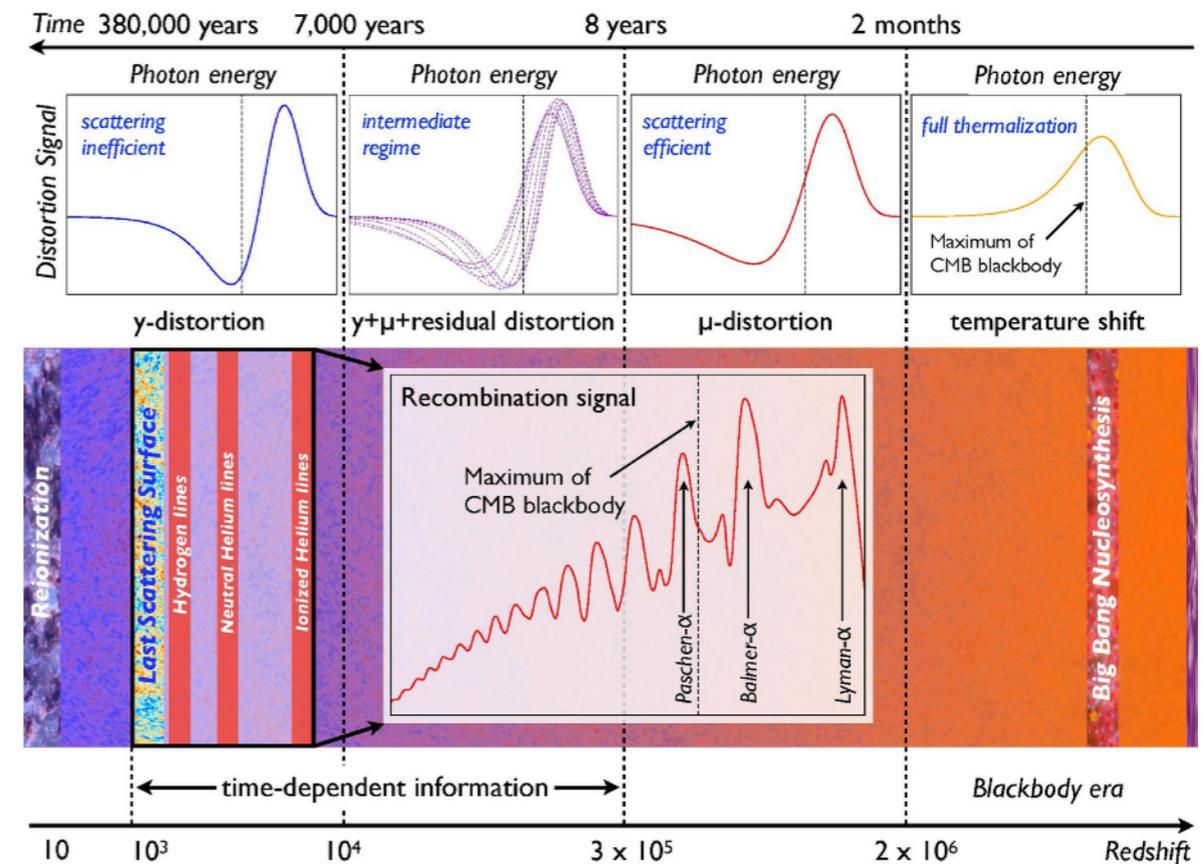
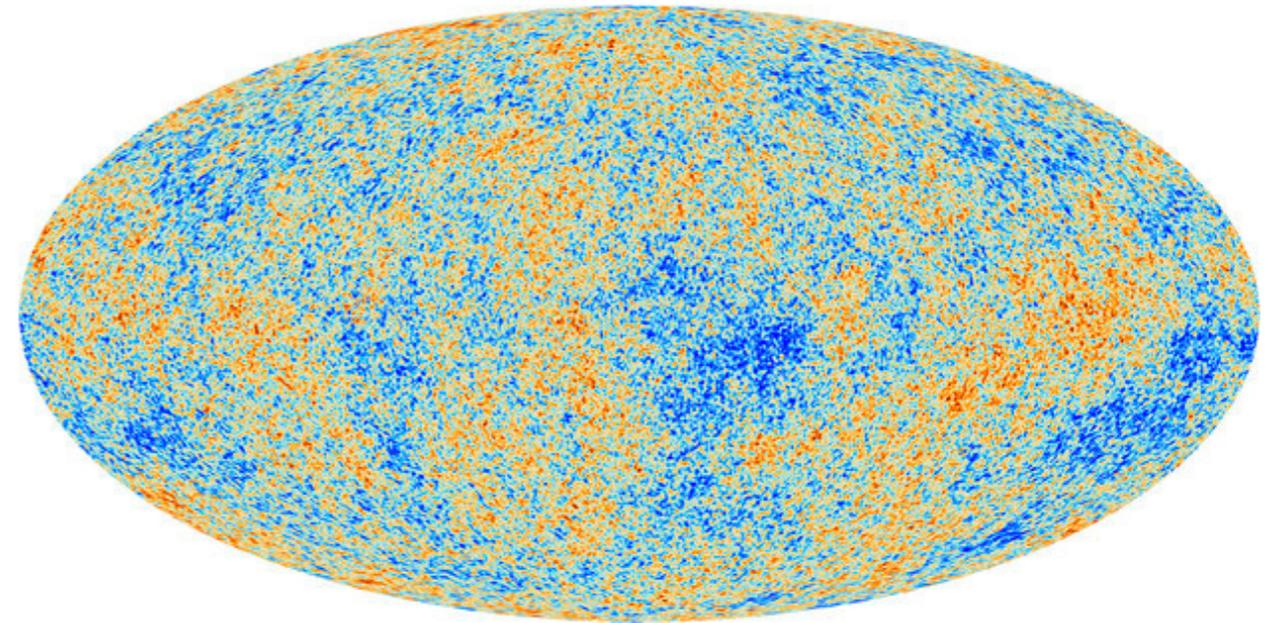
Emitted at  $T \sim 1 \text{ eV}$

Equilibrium physics

- ▶ almost perfect black body spectrum

Non-equilibrium physics can distort the spectrum

- ▶ Probe of keV – MeV temperatures



# Non-equilibrium in the early Universe

# GWs from Phase Transitions

QFT at finite temperature  $\rightarrow$  symmetry restoration

For first order PT

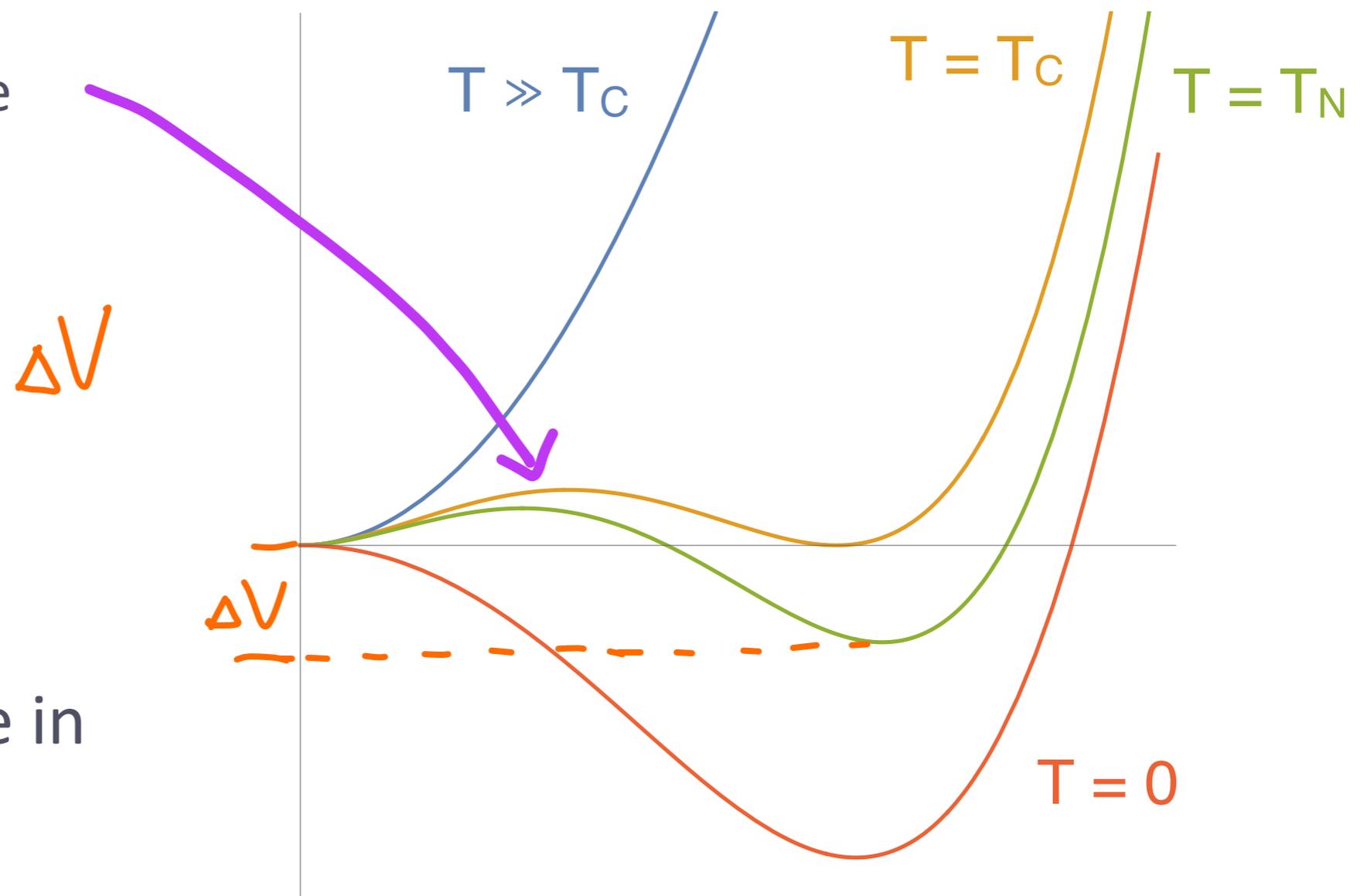
- Need barrier here

PT occurs at  $T_N$

Potential energy

GWs

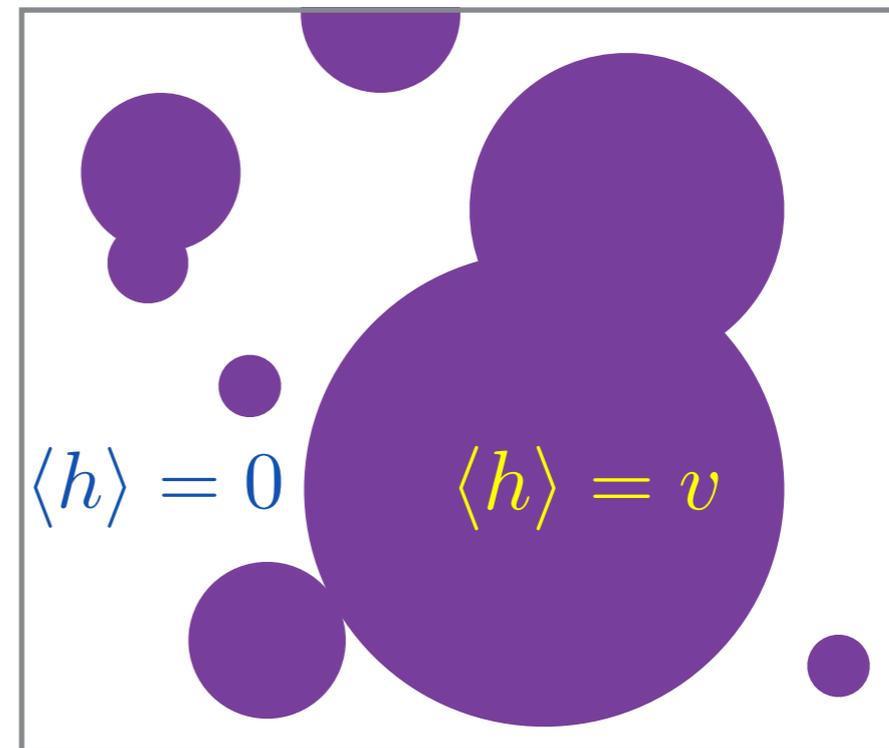
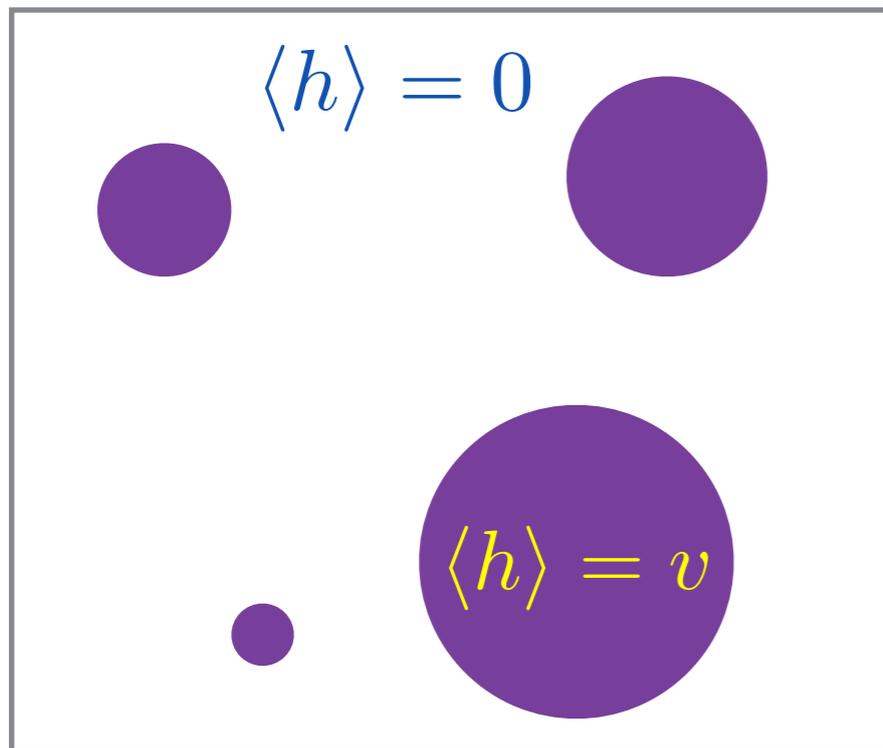
Not in SM! Possible in  
BSM scenarios



# GWs from Phase Transitions

First order PT  $\rightarrow$  Bubbles nucleate, expand

Bubble collisions  $\rightarrow$  Gravitational Waves



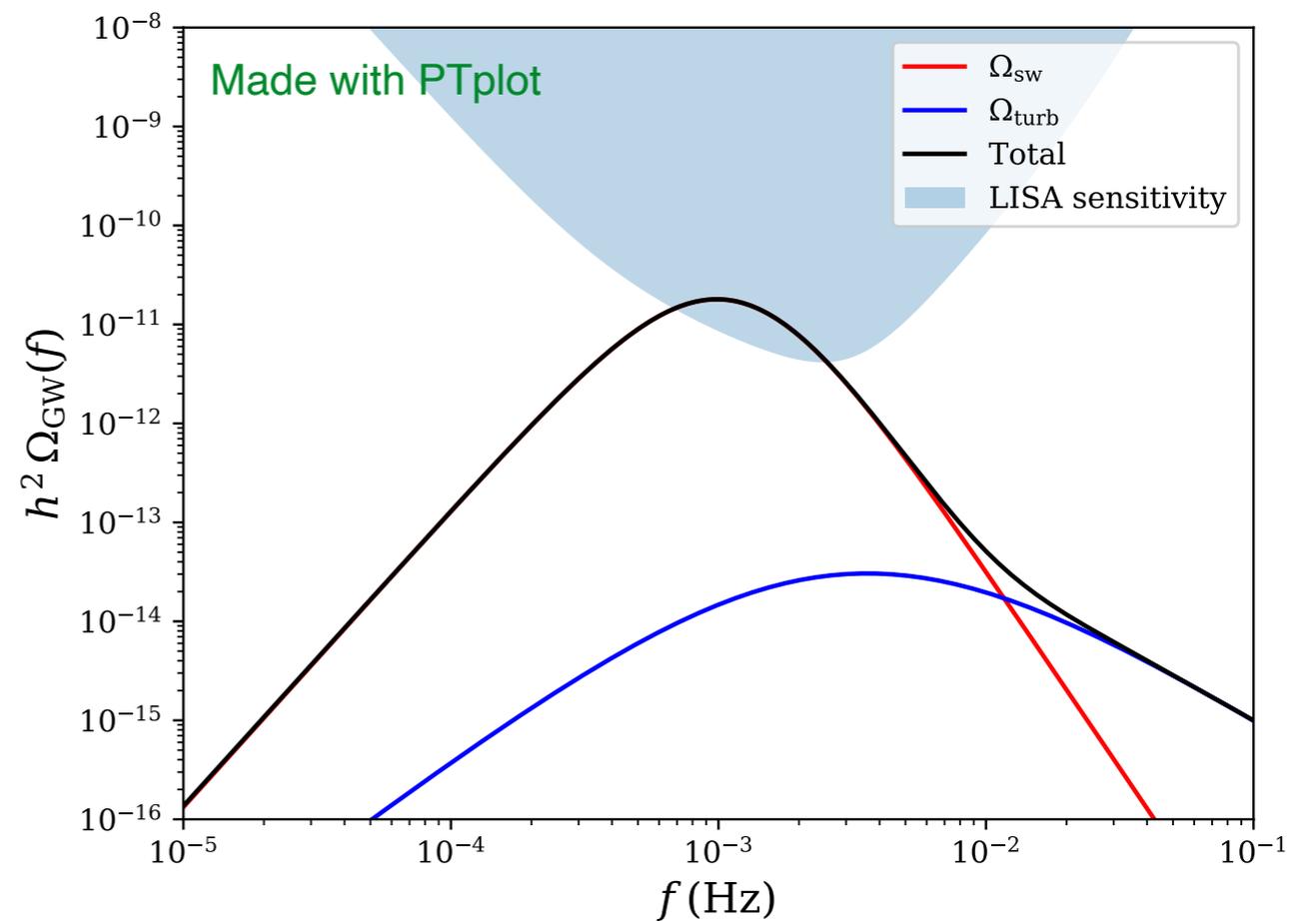
# PT signal

PT characterised by few parameters:

- Latent heat  $\alpha \approx \frac{\Omega_{\text{vacuum}}}{\Omega_{\text{rad}}}$
- Bubble wall velocity  $v$
- Bubble nucleation rate  $\beta$
- PT temperature  $T_*$

More details, see e.g.:

Summary and recommendations:  
1910.13125  
(LISA Cosmology WG)



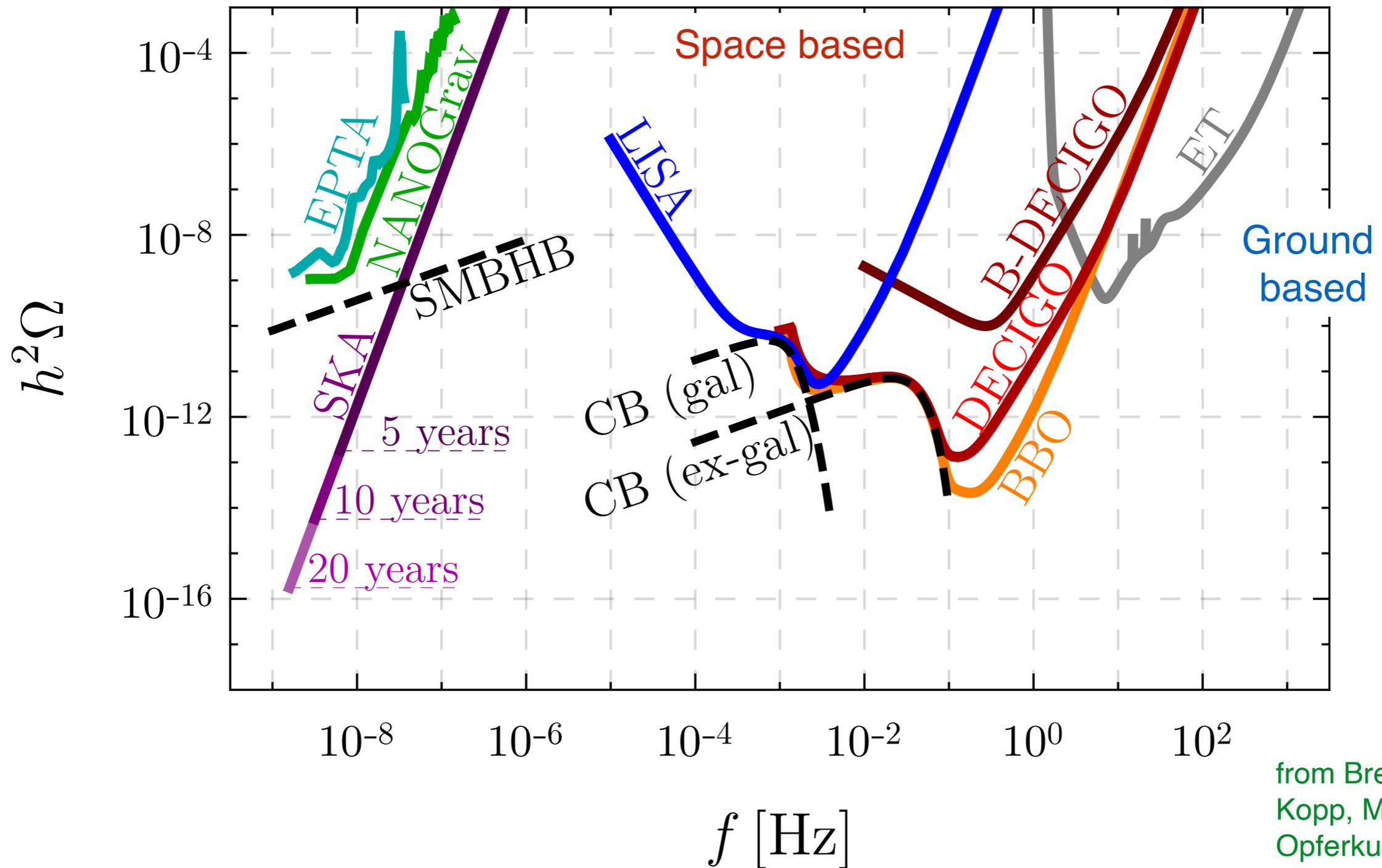
# Frequency ranges

New physics scale

GeV

TeV

PeV

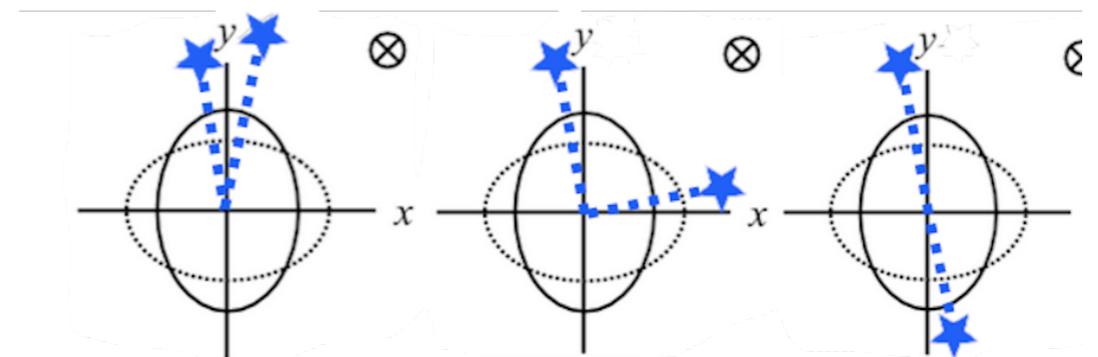
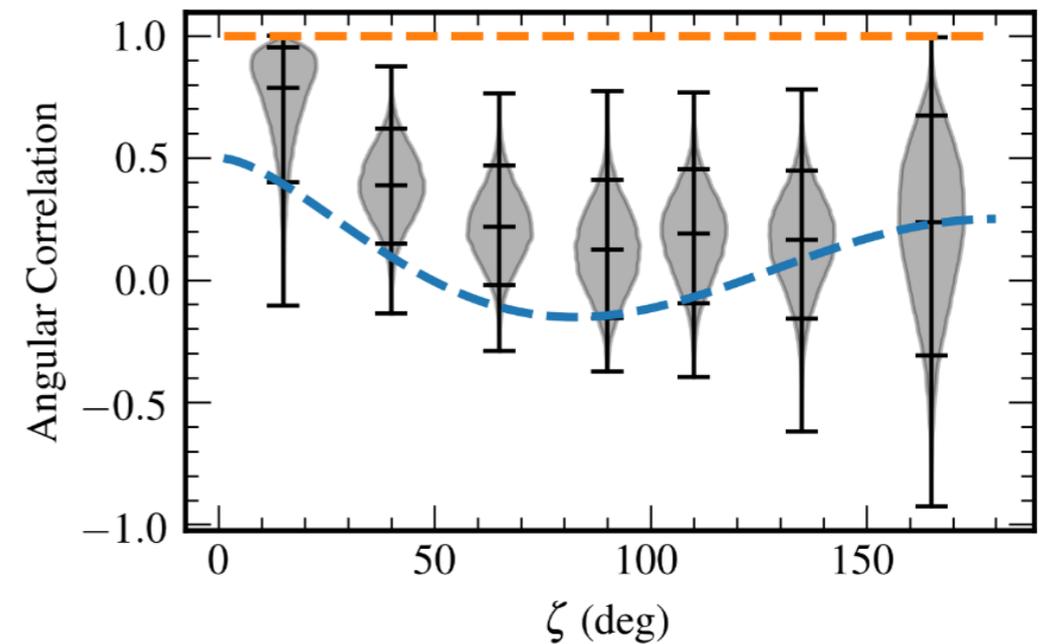
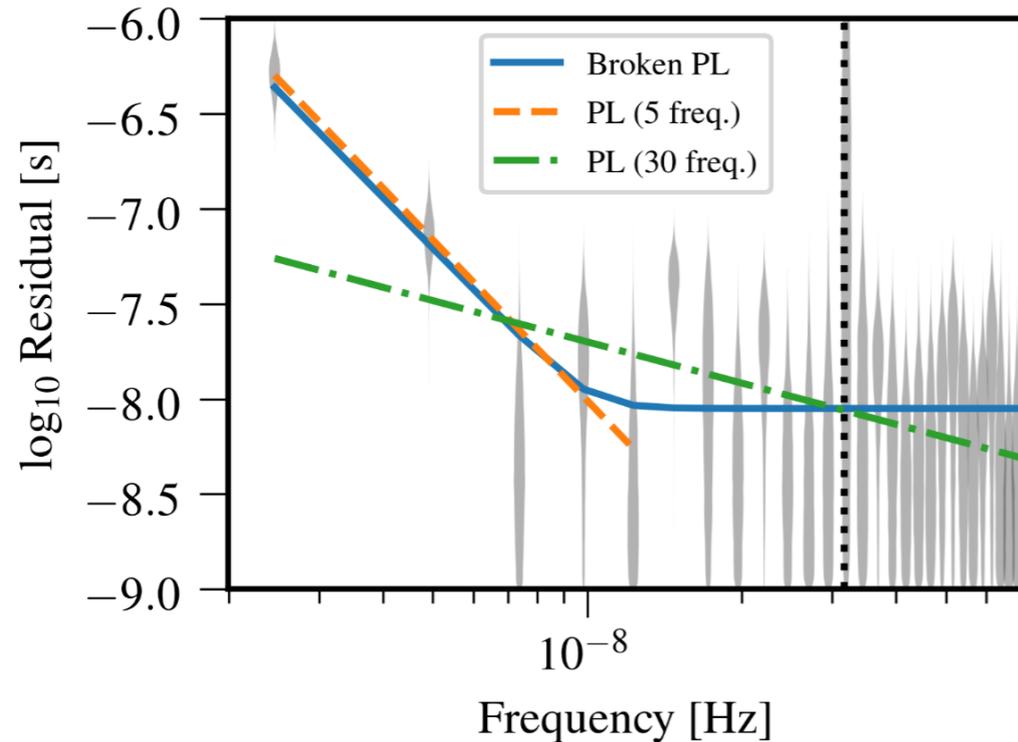


from Breitbach,  
Kopp, Madge,  
Opferkuch, PS  
1811.11175

# NANOGrav saw something!

No  $4\sigma$  evidence for Quadrupole

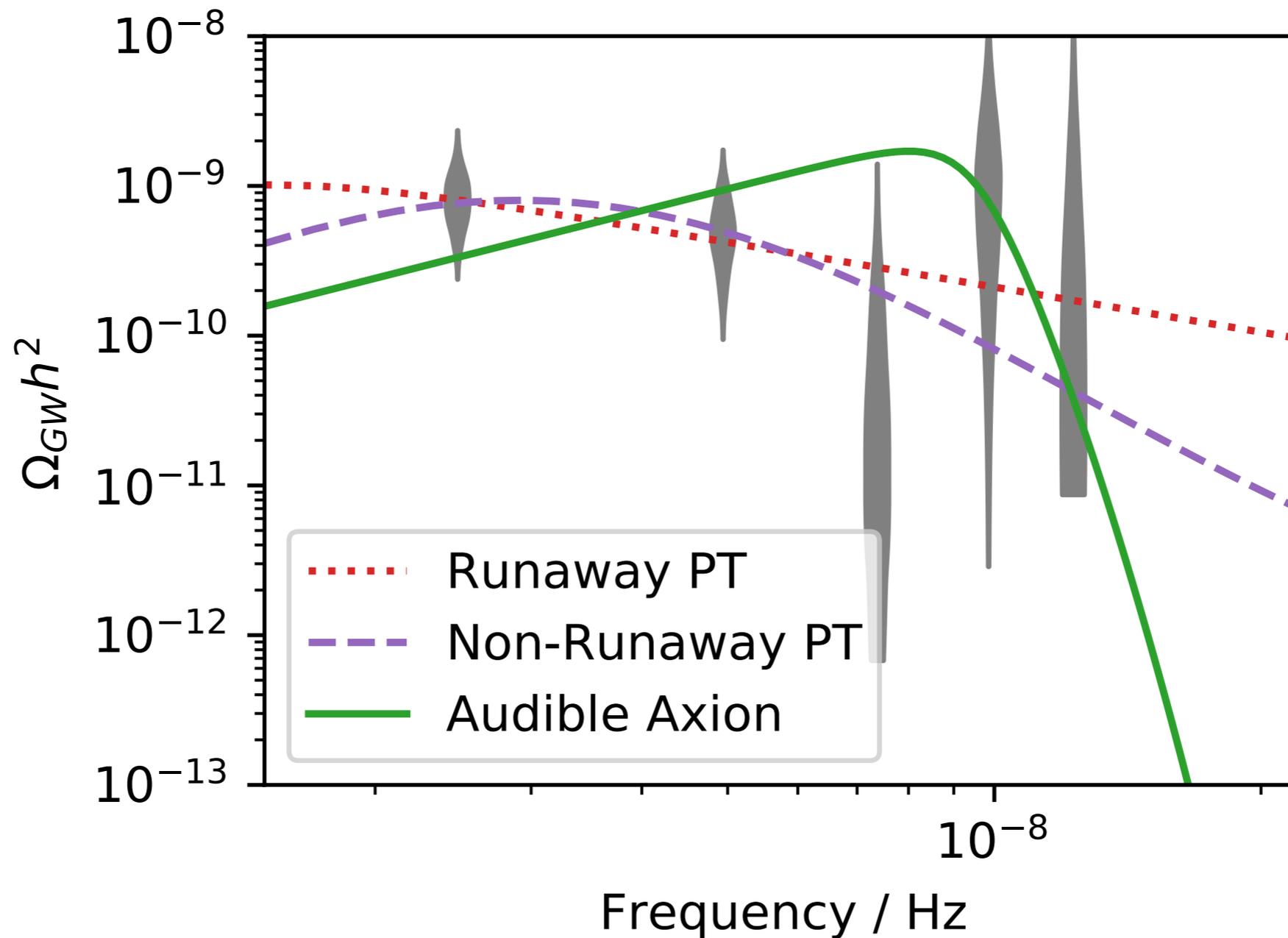
Significant Strain at low frequencies



From NANOGrav collaboration, 2009.04496

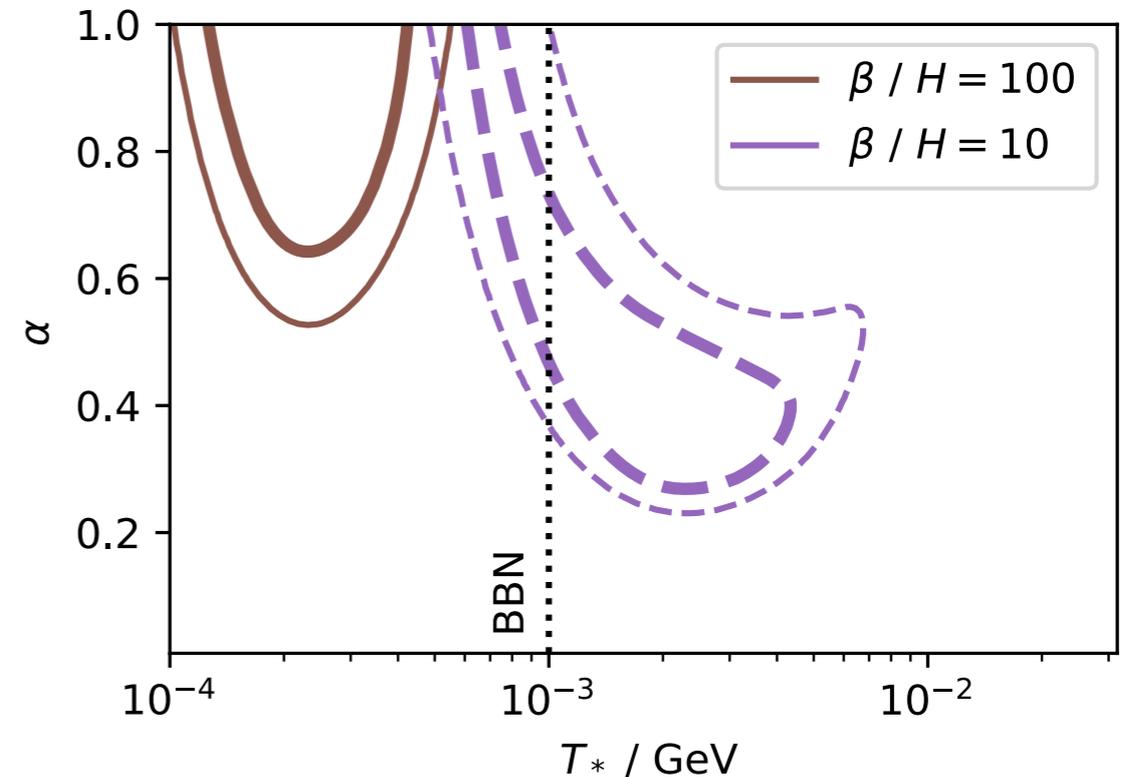
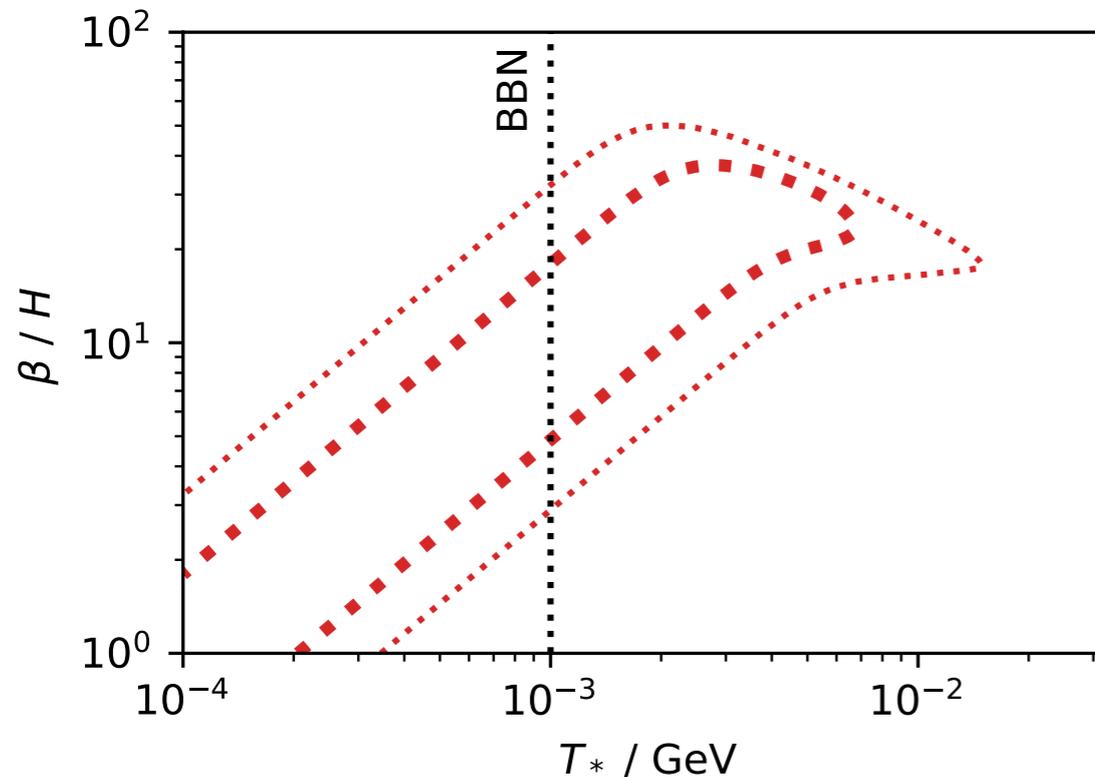
Now also consistent signals in PPTA, EPTA and IPTA - still not fully conclusive though

# Fit with broken power law signals



Wolfram Ratzinger & PS, 2009.11875

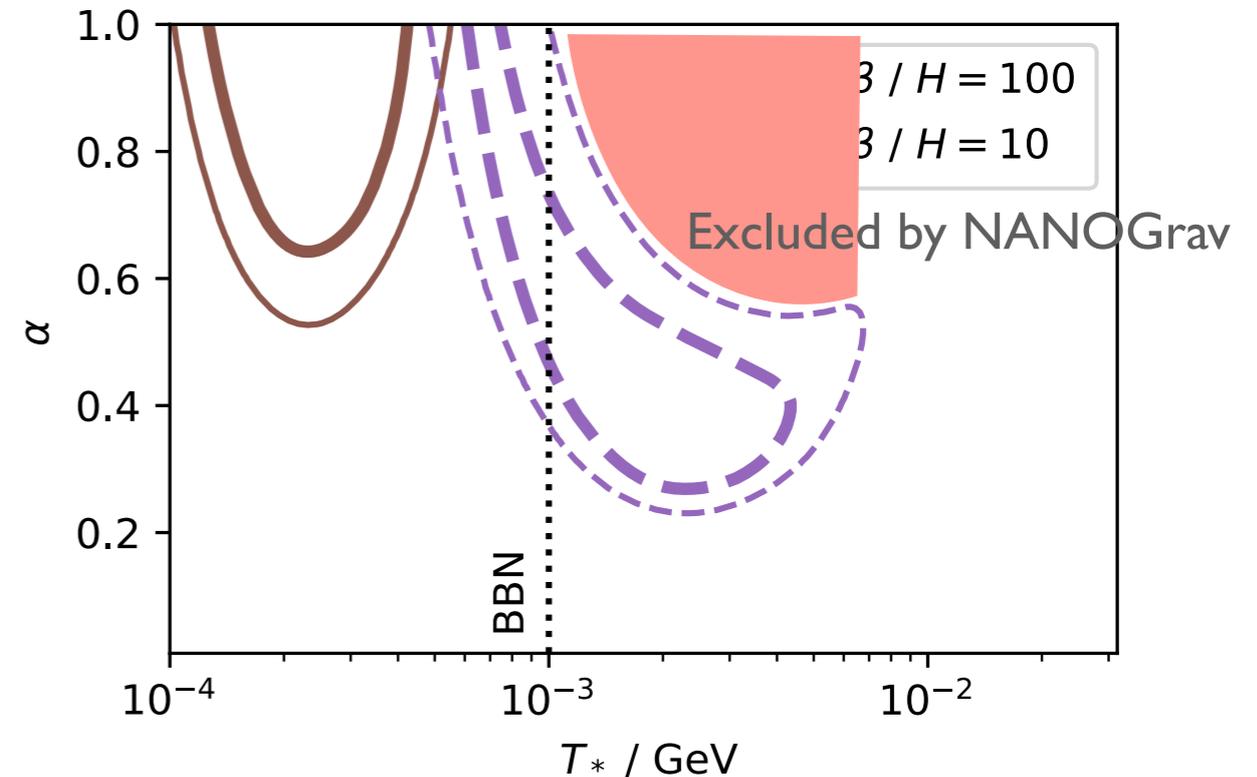
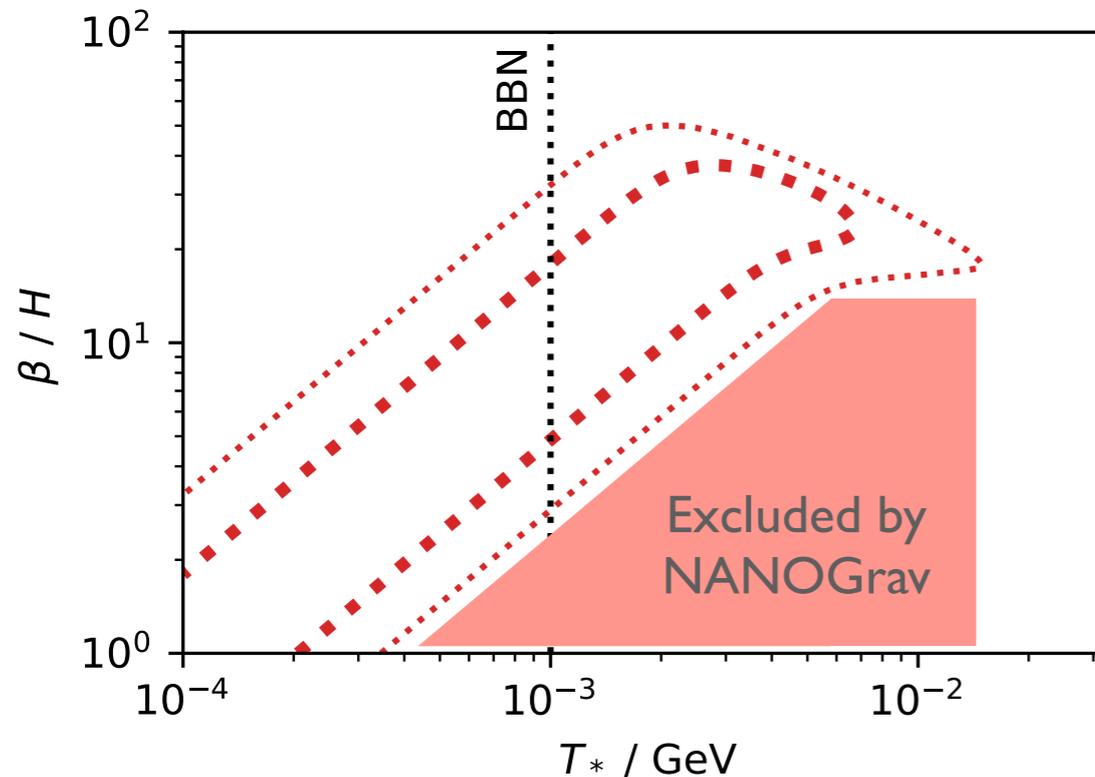
# Fit with Phase Transition



Generic PT parameterisation, best fit with PT at temperatures in few MeV range

Challenge for model building  $\rightarrow$  Hint for dark sector

# Fit with Phase Transition



Generic PT parameterisation, best fit with PT at temperatures in few MeV range

Some model parameters excluded by PTA data now!

# QCD-like dark sectors

The new physics should be light and hidden

QCD-like dark sector can naturally have  $\Lambda_d \sim \text{MeV}$

Confinement PT is first order for

- ▶  $N_d \geq 3$  and  $n_f = 0$
- ▶  $N_d \geq 3$  and  $3 \leq n_f \lesssim 4N_d$

Can this explain the NANOGrav/PTA data?

- ▶ Difficult question in itself due to strong coupling

# Combine lattice and holography

Gürsoy, Kiritsis, Mazzanti, Nitti  
0707.1324, 0707.1349, 0812.0792, 0903.2859, ...

## Improved holographic QCD

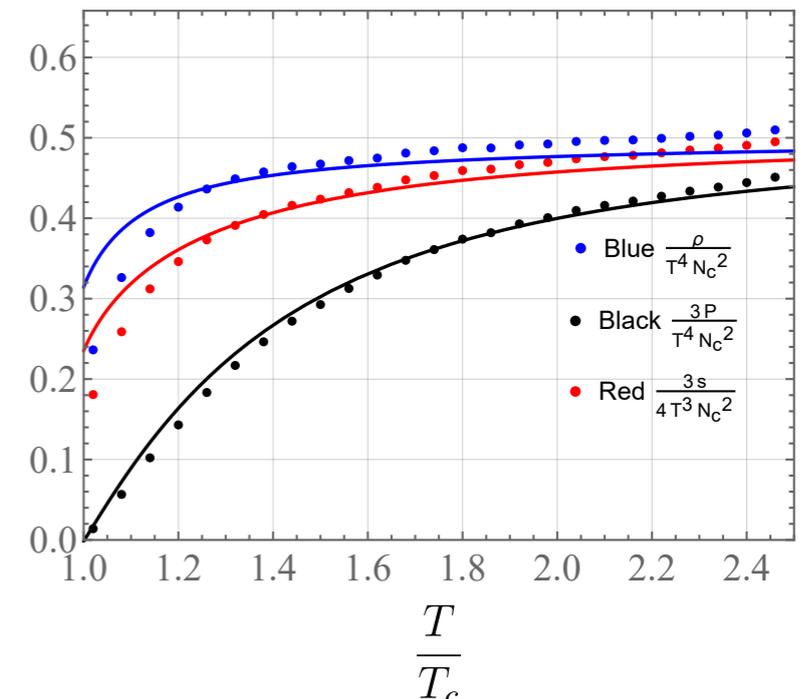
$$\mathcal{S}_5 = -M_P^3 N_c^2 \int d^5x \sqrt{g} \left[ R - \frac{4}{3} (\partial\Phi)^2 + V(\Phi) \right] + 2M_P^3 N_c^2 \int_{\partial M} d^4x \sqrt{h} K$$

## Want this to reproduce SU(N) theories

- ▶ Confinement in IR ( $\lambda \rightarrow \infty$ )
- ▶ Yang Mills beta function in UV ( $\lambda \rightarrow 0$ )

$$V(\lambda) = \frac{12}{\ell^2} \left\{ 1 + V_0 \lambda + V_1 \lambda^{4/3} [\log(1 + V_2 \lambda^{4/3} + V_3 \lambda^2)]^{1/2} \right\}$$

- ▶ Parameters fit to match RGE in UV and lattice in IR!



# Effective potential and bounce action

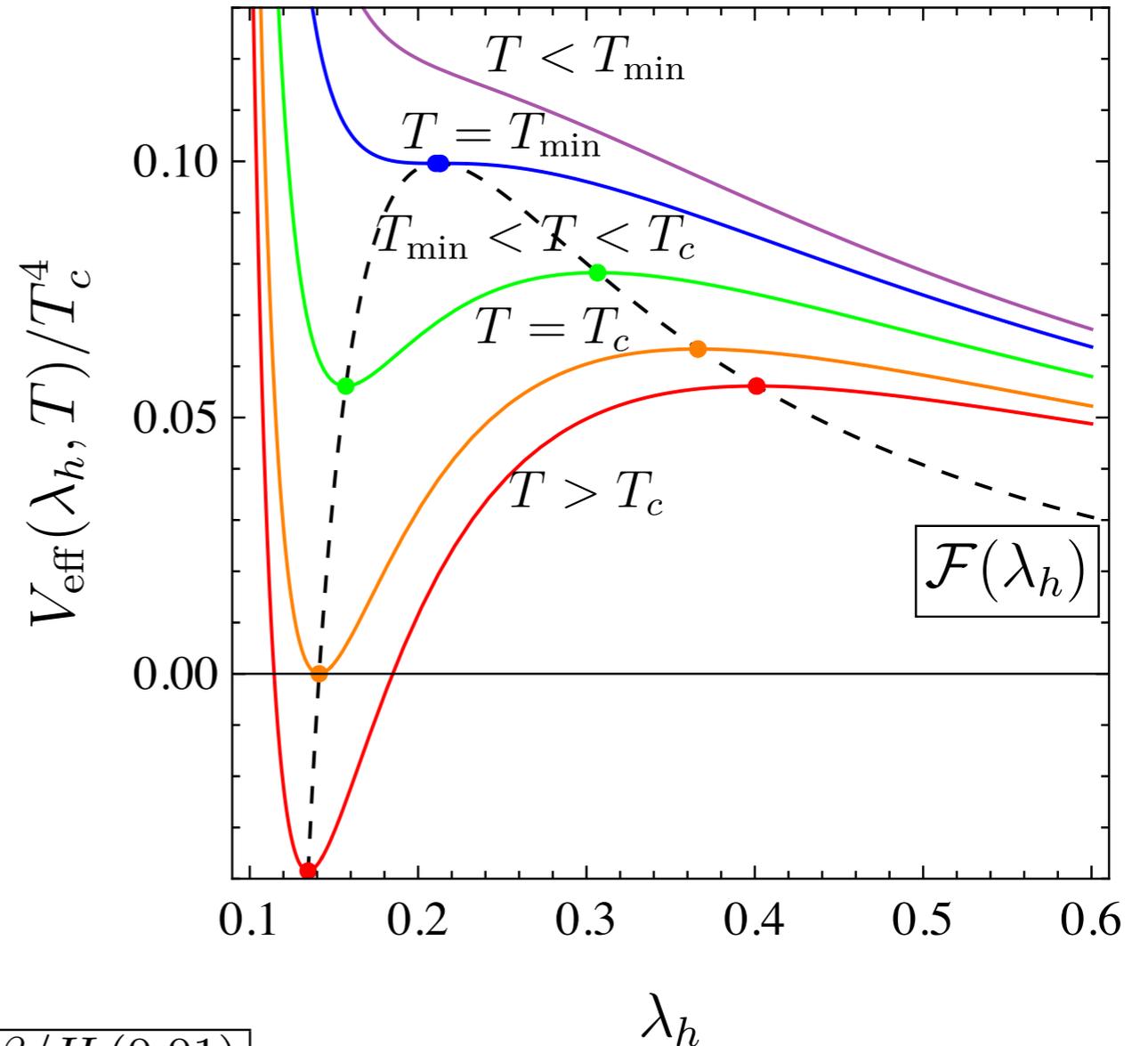
## Bounce action

$$S_{\text{eff}} = \frac{4\pi}{T} \int d\rho \rho^2 \left[ c \frac{N_c^2}{16\pi^2} (\partial_r \lambda_h(r))^2 + V_{\text{eff}}(\lambda_h(r)) \right]$$

## Tunneling decay rate

$$\Gamma = T^4 \left( \frac{S_B}{2\pi} \right)^{3/2} e^{-S_B}$$

Allows us to compute  
 $\alpha$  and  $\beta$



	$\alpha$	$\beta/H (v_w = 1)$	$\beta/H (0.1)$	$\beta/H (0.01)$
$T_c = 50 \text{ MeV}$	0.343	$9.0 \times 10^4$	$8.6 \times 10^4$	$8.2 \times 10^4$
100 GeV	0.343	$6.8 \times 10^4$	$6.4 \times 10^4$	$6.1 \times 10^4$

Morgante, Ramberg, PS, 2210.11821

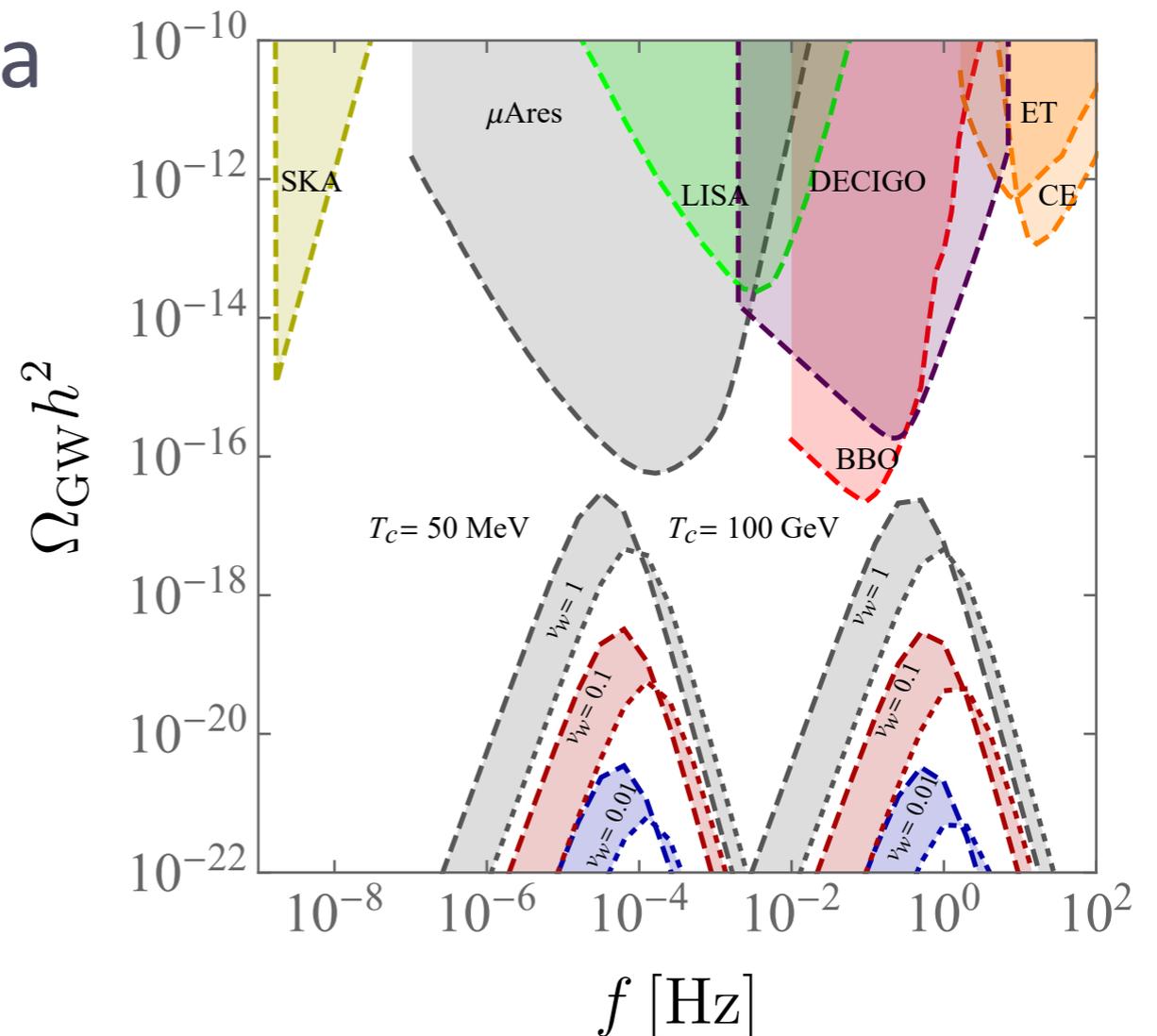
# GW spectrum

First prediction for GW spectra of QCD-like dark sectors from holography

- ▶ for  $N_c = 3, n_f = 0$
- ▶ Some work remains (wall velocity)
- ▶ Larger signal possible for larger  $N_c, n_f$
- ▶ Agrees with estimates based on effective theories and lattice data

(e.g. Halverson+ 2012.04071, Huang+ 2012.11614, March-Russell+ 1505.07109)

Morgante, Ramberg, PS, 2210.11821



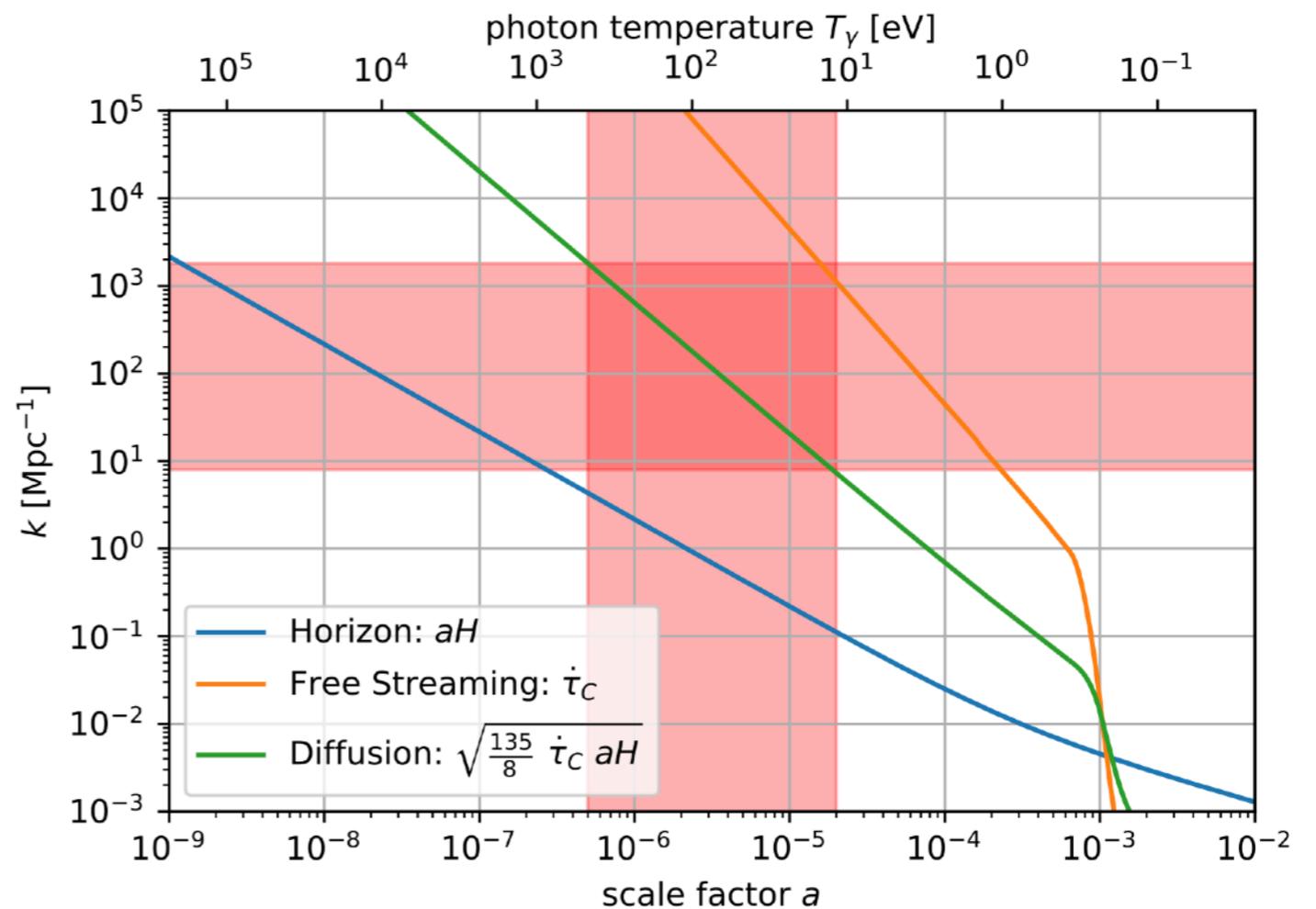
Now what about the  
spectral distortions?

# Spectral distortions?

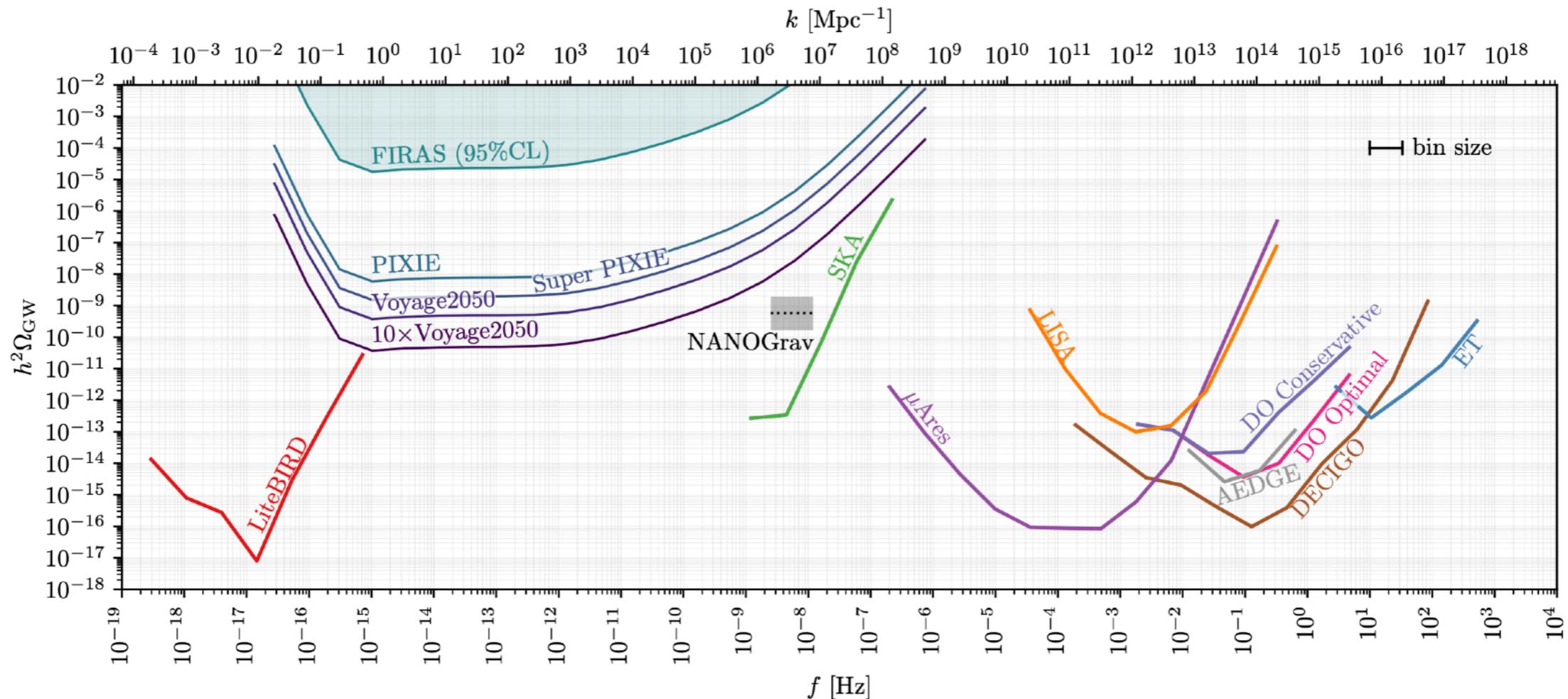
Around  $10^4 \lesssim z \lesssim 10^6$ ,  
photon number is frozen

Any energy added to the  
photons leads to a so  
called  $\mu$  distortion

Energy source we  
consider here:  
Gravitational damping of  
dark sector fluctuations



# Spectral distortions as probes of low scale GWs



From Kite, Ravenni, Patil, Chluba, MNRAS 2021

Tensor fluctuations (GWs) also source  $\mu$  distortions

- But difficult to test. Better to directly go for the scalar fluctuations (that also source the GWs)

# Spectral distortions from dark sector anisotropies

Assume decoupled dark sector,  $\Omega_d \ll 1$

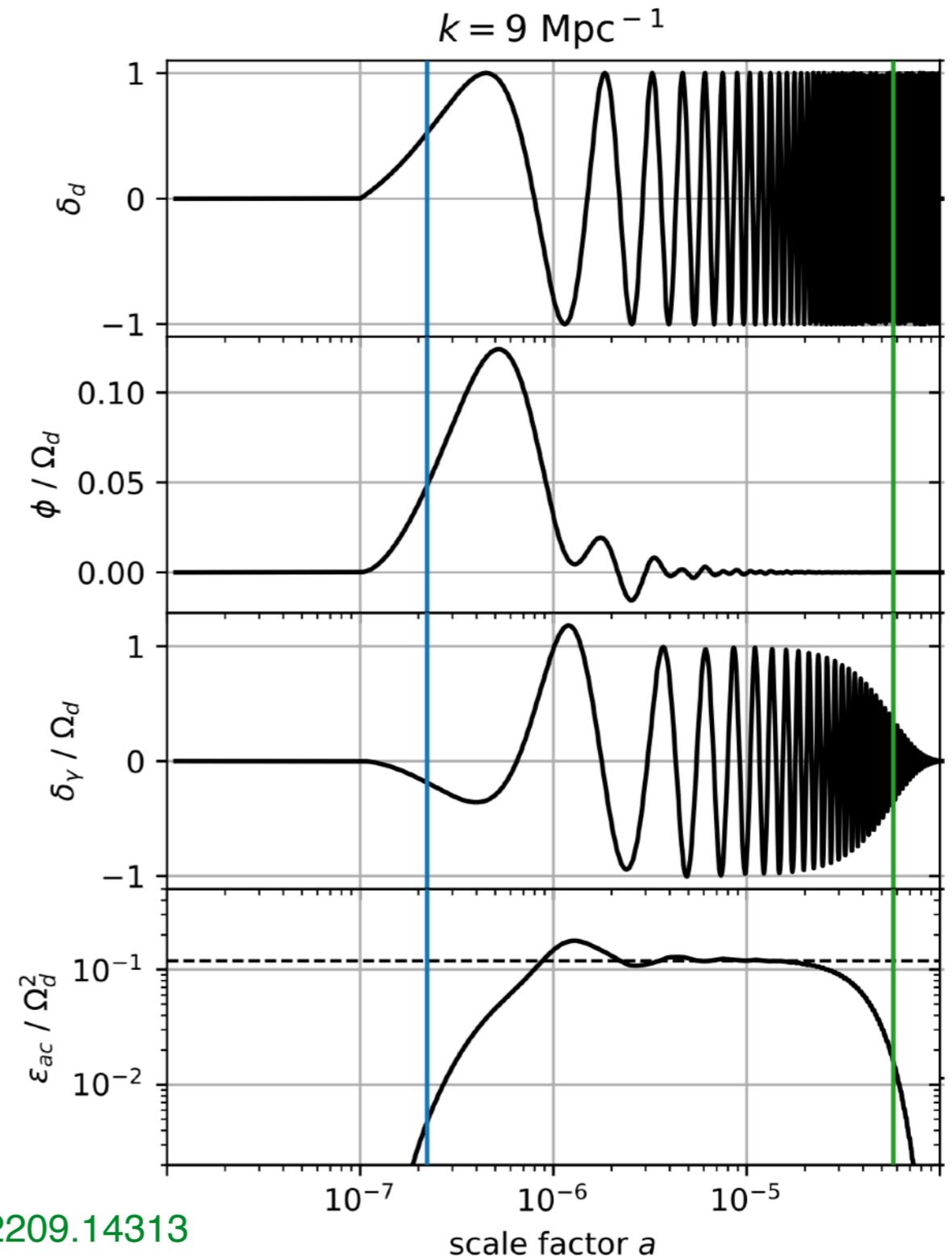
Large fluctuations

$$\delta_d = \delta\rho_d / \rho_d \sim 1$$

- ▶ Gravitationally induced sound waves in photons  $\epsilon_{ac}$

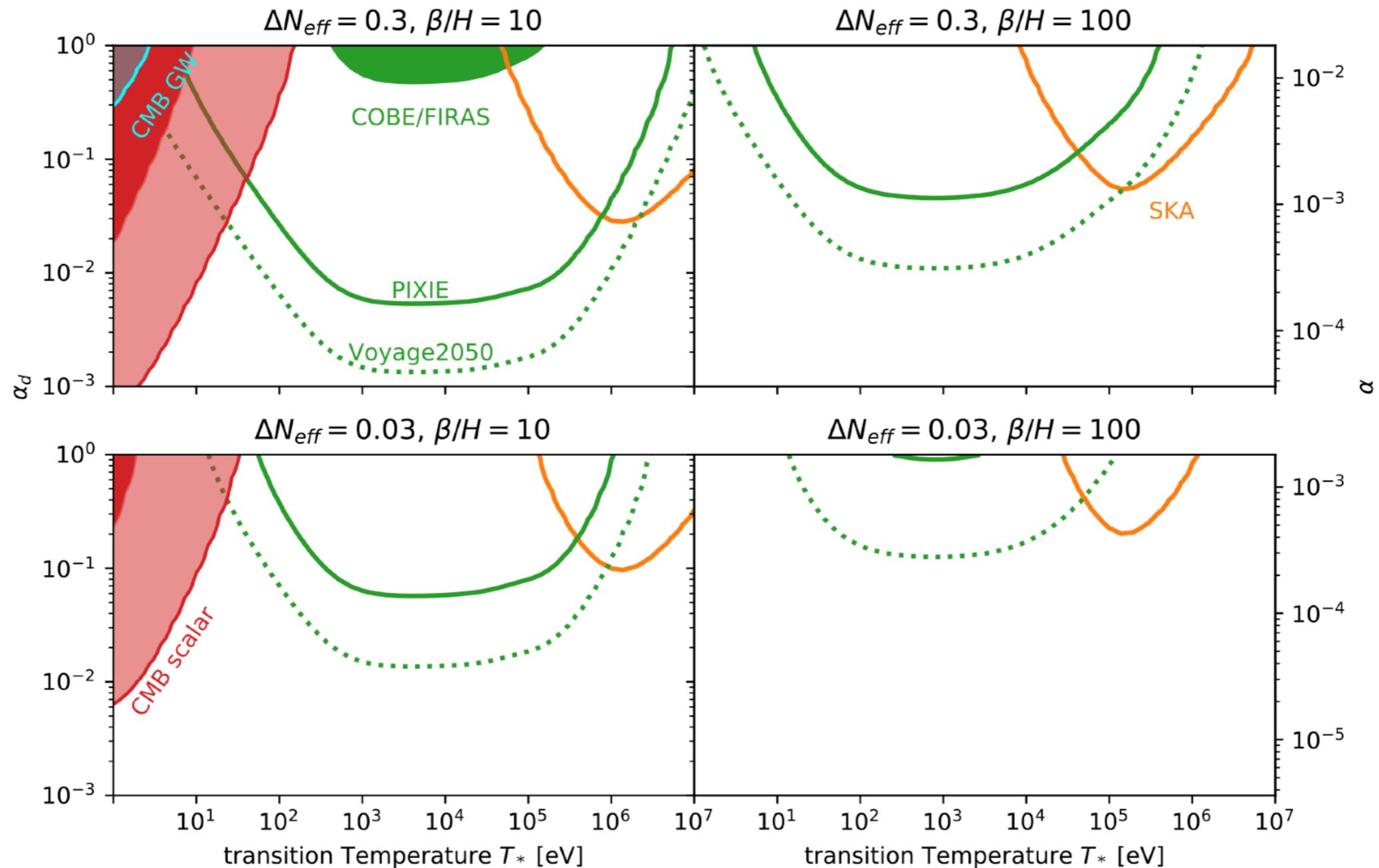
Resulting  $\mu$  distortions

$$\mu = \int d \log k \epsilon_{ac}^{\text{lim}}(k) \mathcal{W}(k),$$



Ramberg, Ratzinger & PS, 2209.14313

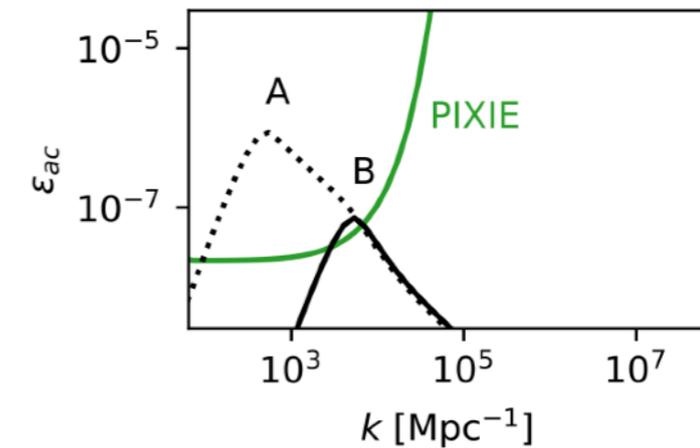
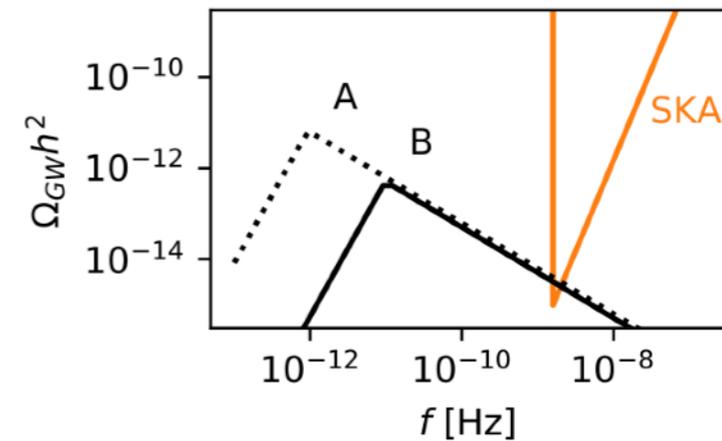
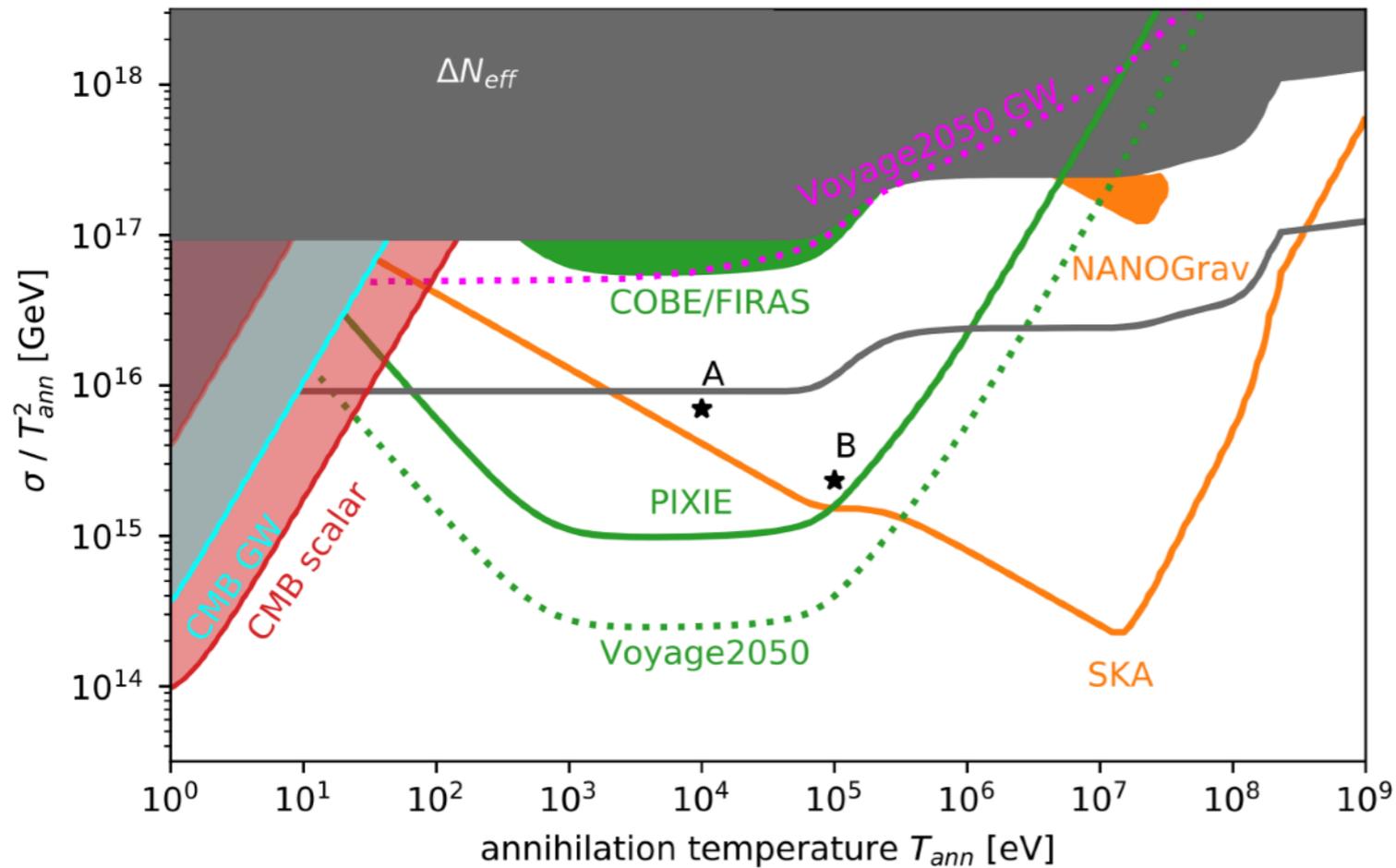
# Example source I: Dark sector phase transition



Note:  $\Omega_d$  fixed to satisfy  $N_{\text{eff}}$  constraints

Ramberg, Ratzinger & PS, 2209.14313

# Example source II: Annihilating domain walls



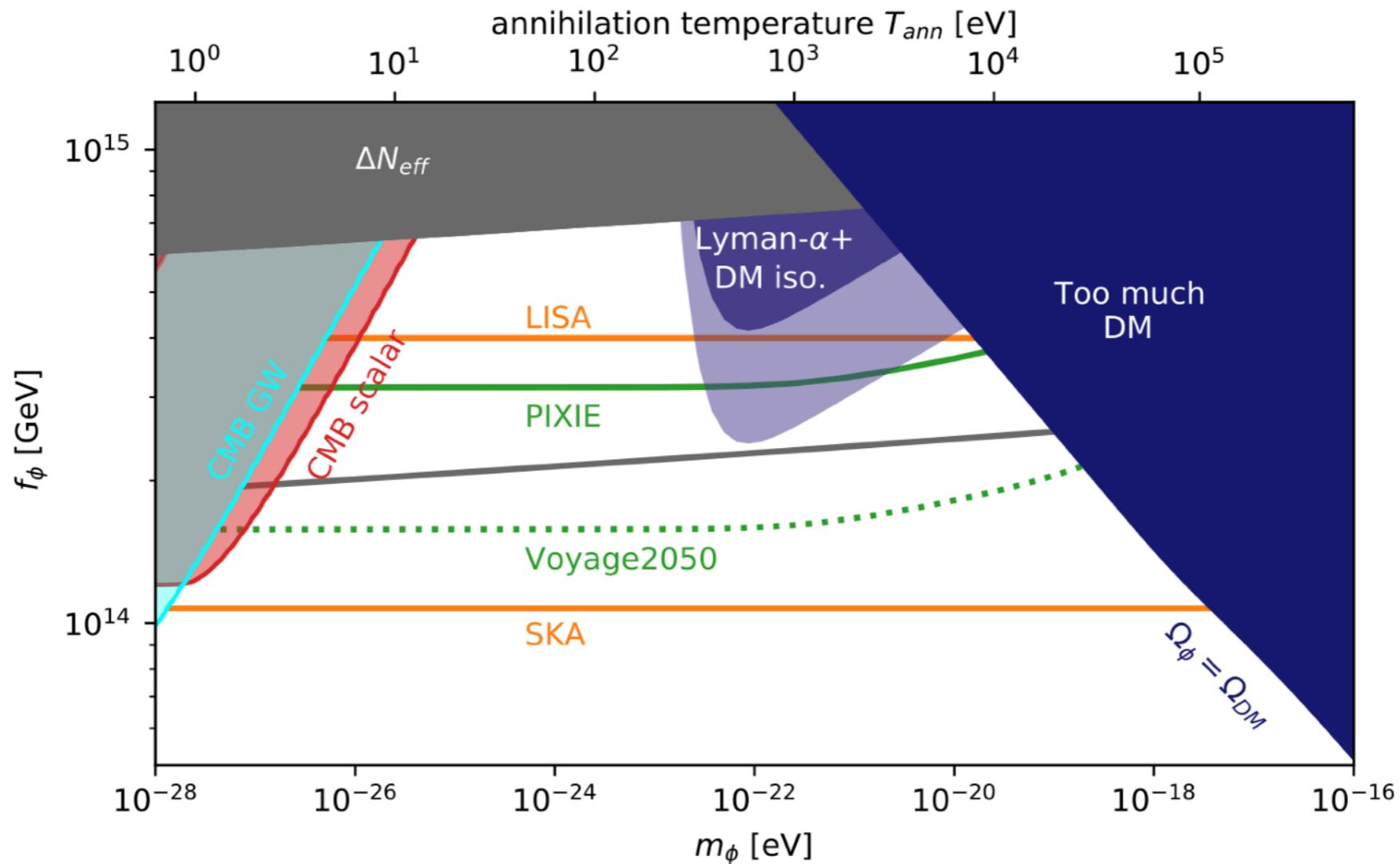
Already probes allowed parameter space

Complementary to GW probes, can break degeneracy

- Multi-messenger cosmology

Ramberg, Ratzinger & PS, 2209.14313

# Source III: (global) cosmic strings



Note: Local strings mainly radiate from small loops and are thus NOT an efficient source of spectral distortions

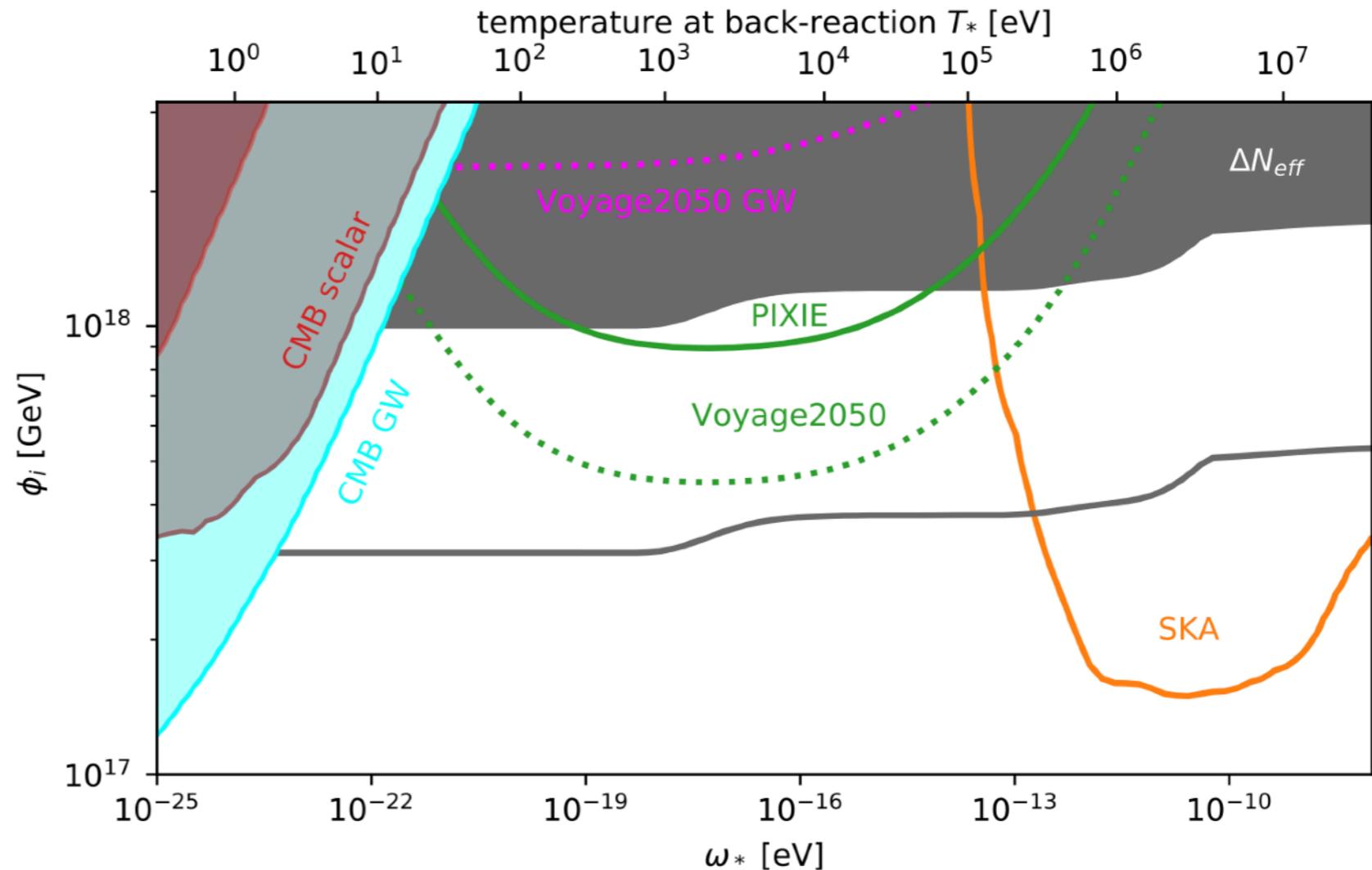
# Example source IV: Audible axions...

Not yet...

Results for scalar toy model

Constraints not as strong since fluctuations are not horizon size

Expect better sensitivity for axion fragmentation



Ramberg, Ratzinger & PS, 2209.14313

# Summary

GWs and CMB spectral distortions (SD) probe non-equilibrium physics in the early Universe

- ▶ Sensitive to otherwise inaccessible (dark) sectors

PTA data hints towards a strong first order PT at the MeV scale, potentially in a dark sector

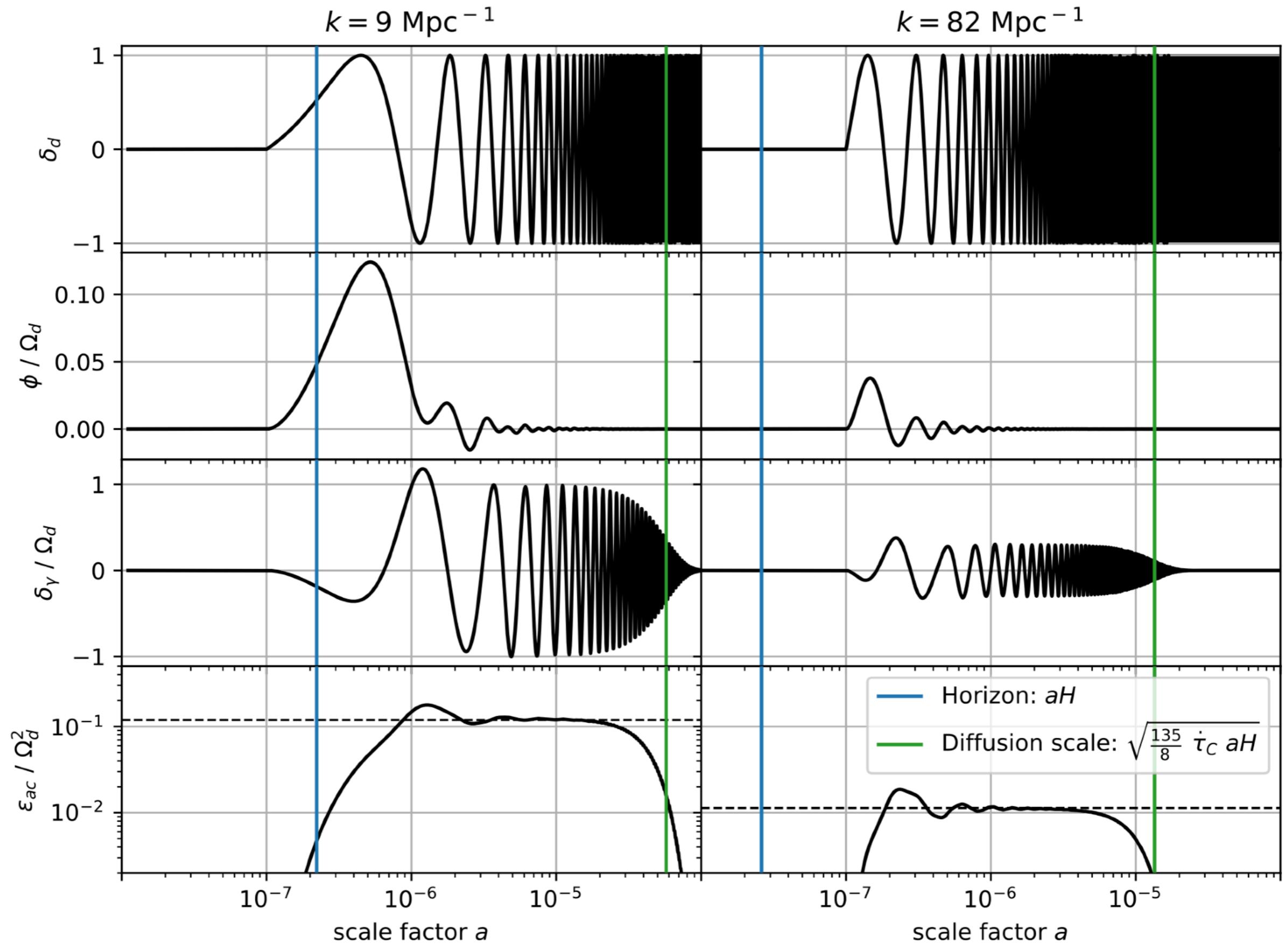
Holography allows computation of PT observables also at strong coupling

Combination of GW and SD

- ▶ multi-messenger probes of early Universe anisotropies

Thank you for your attention!

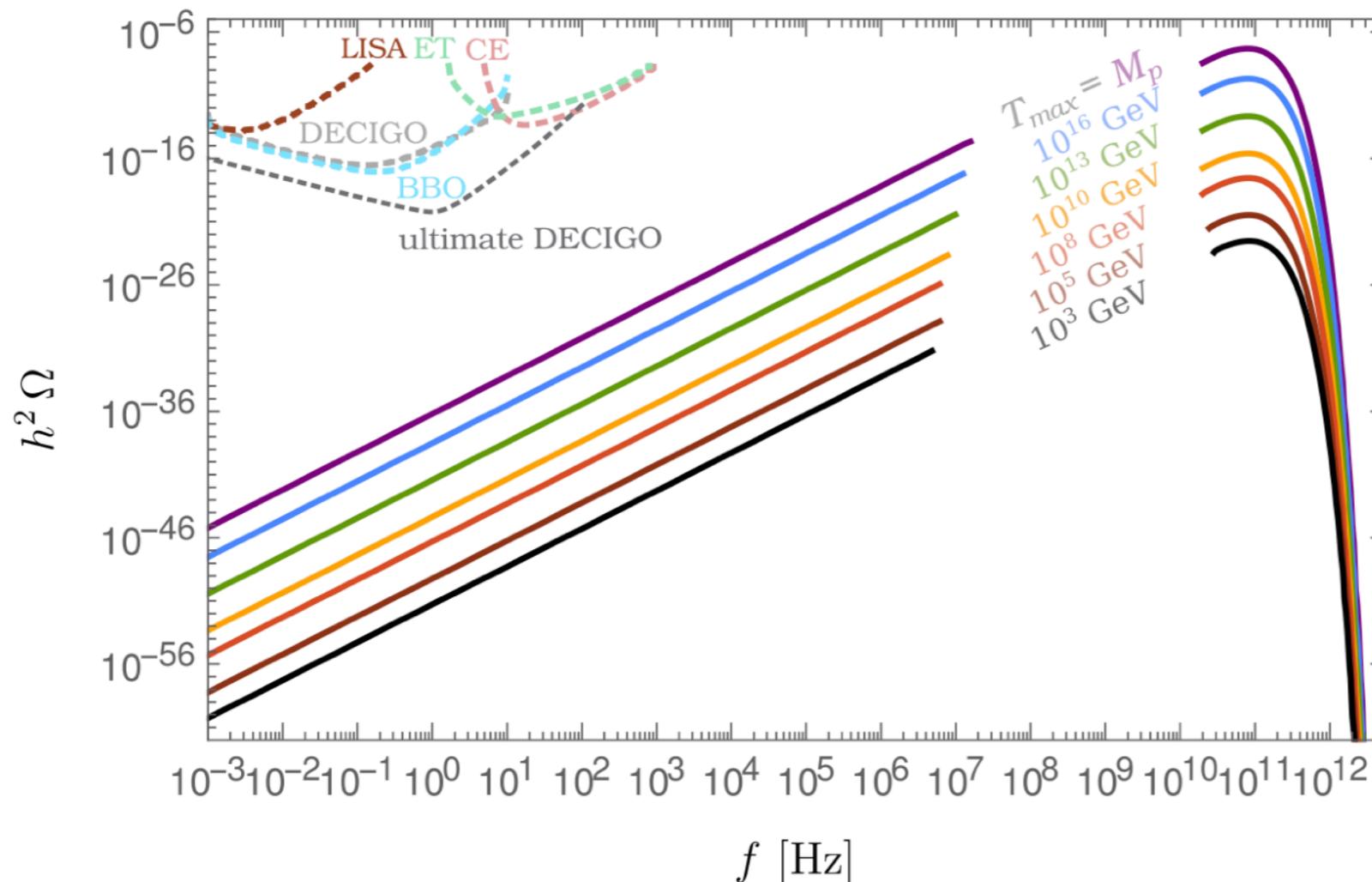




# Standard model

## The hot early Universe sources GWs!

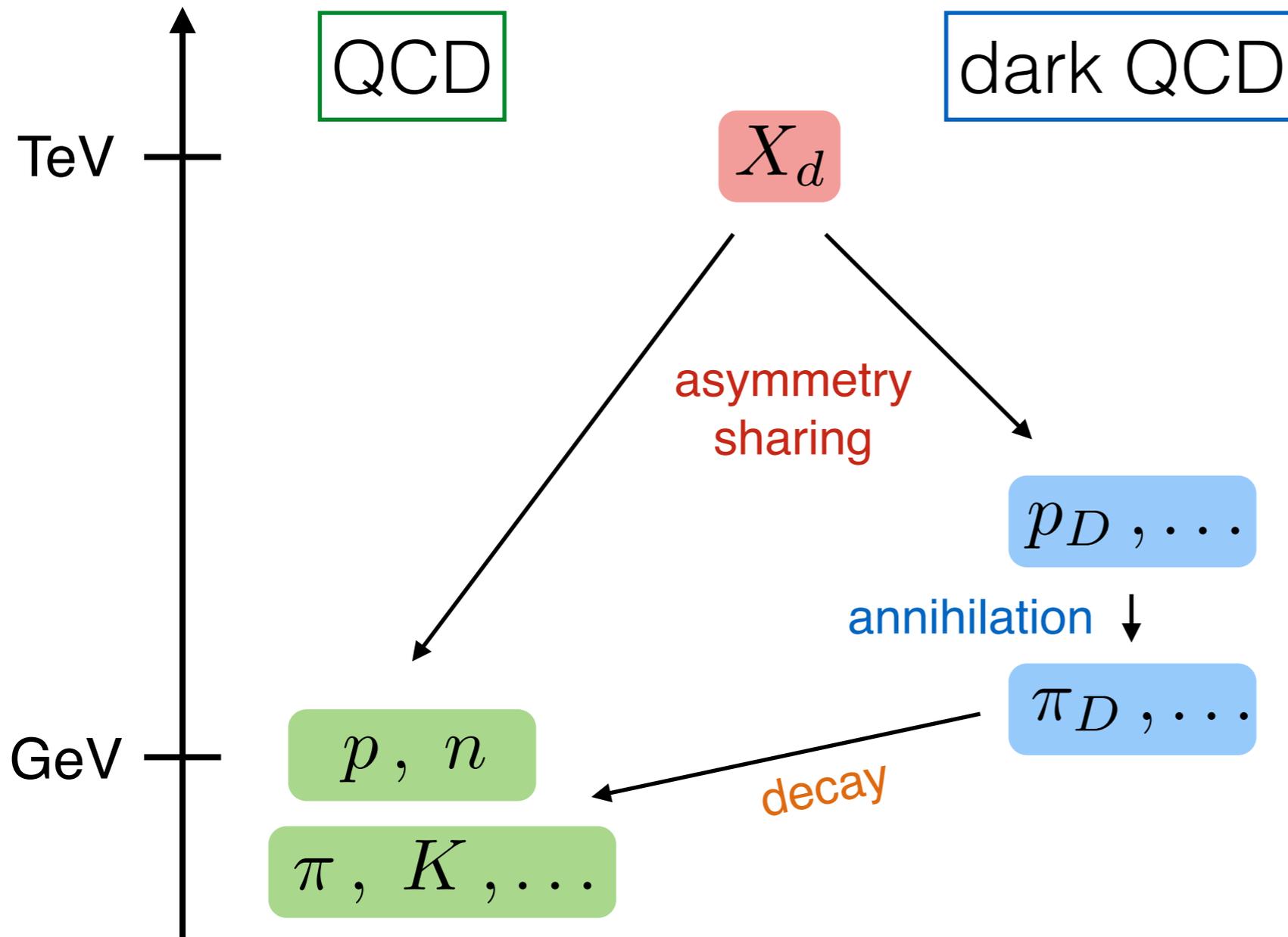
- ▶ Classical picture: thermal fluctuations source tensor fluctuations
- ▶ Quantum picture: gluon + gluon  $\rightarrow$  graviton



From Ringwald,  
Schütte-Engel, Tamarit, 2020

Original computations:  
Ghiglieri, Laine, 2015  
Ghiglieri, Jackson, Laine,  
Zhu, 2020

# Composite DM / Hidden Sector



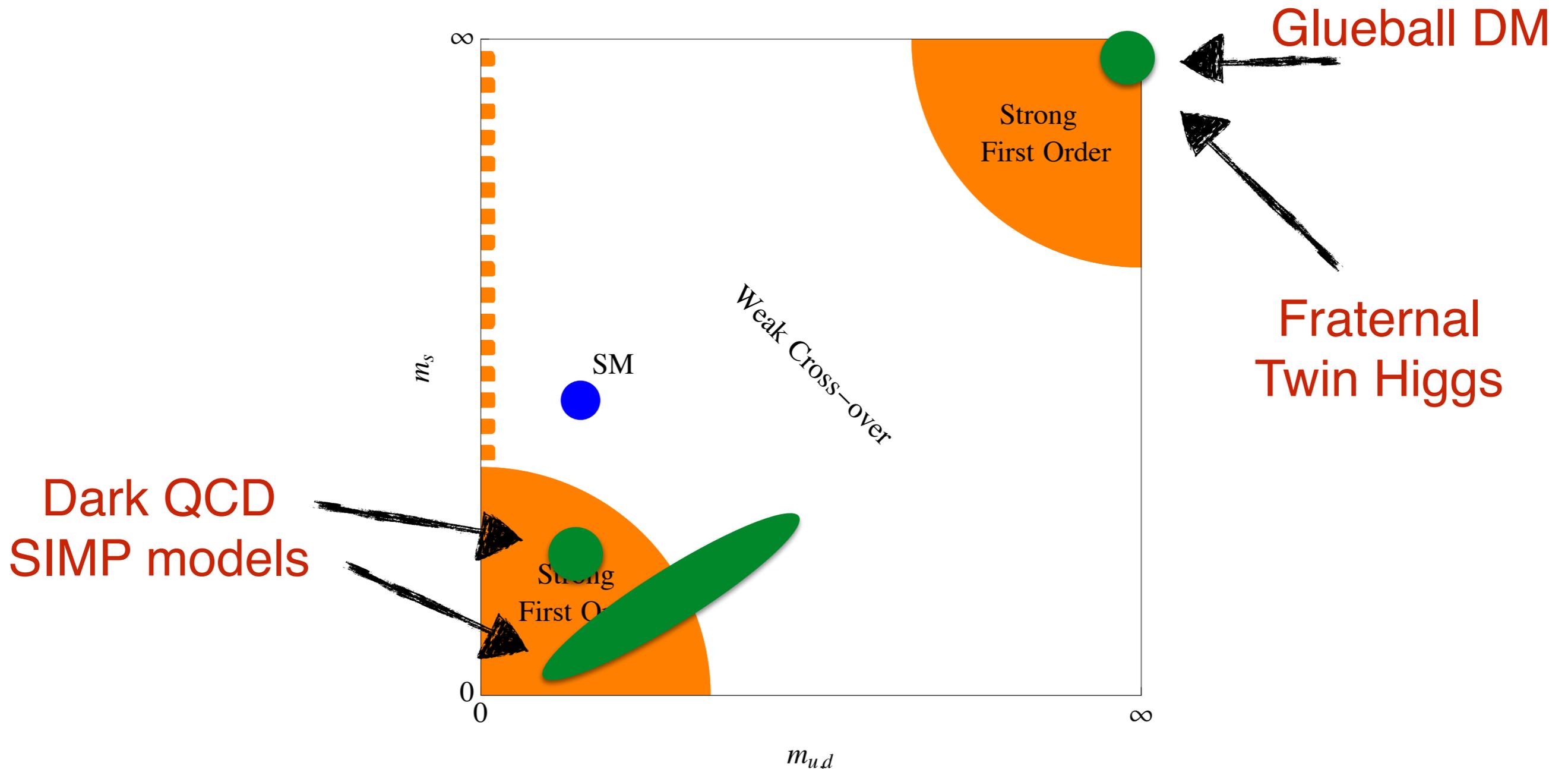
- SU(N) dark sector with neutral "dark quarks"
- Confinement scale  $\Lambda_{\text{darkQCD}}$
- DM is composite "dark proton"

Bai, PS, PRD 89, 2014  
PS, Stolarski, Weiler, JHEP 2015

many other works!

Similar setup e.g.: Blennow et al; Cohen et al; Frandsen et al;  
Hidden Valleys: Strassler, Zurek;...

# Phase Diagram II



PS, 2016

# SU(N) - PT

Consider.  $SU(N_d)$  with  $n_f$  massless flavours

PT is first order for

▶  $N_d \geq 3$  ,  $n_f = 0$

Svetitsky, Yaffe, 1982  
M. Panero, 2009

▶  $N_d \geq 3$  ,  $3 \leq n_f < 4N_d$

Pisarski, Wilczek, 1983

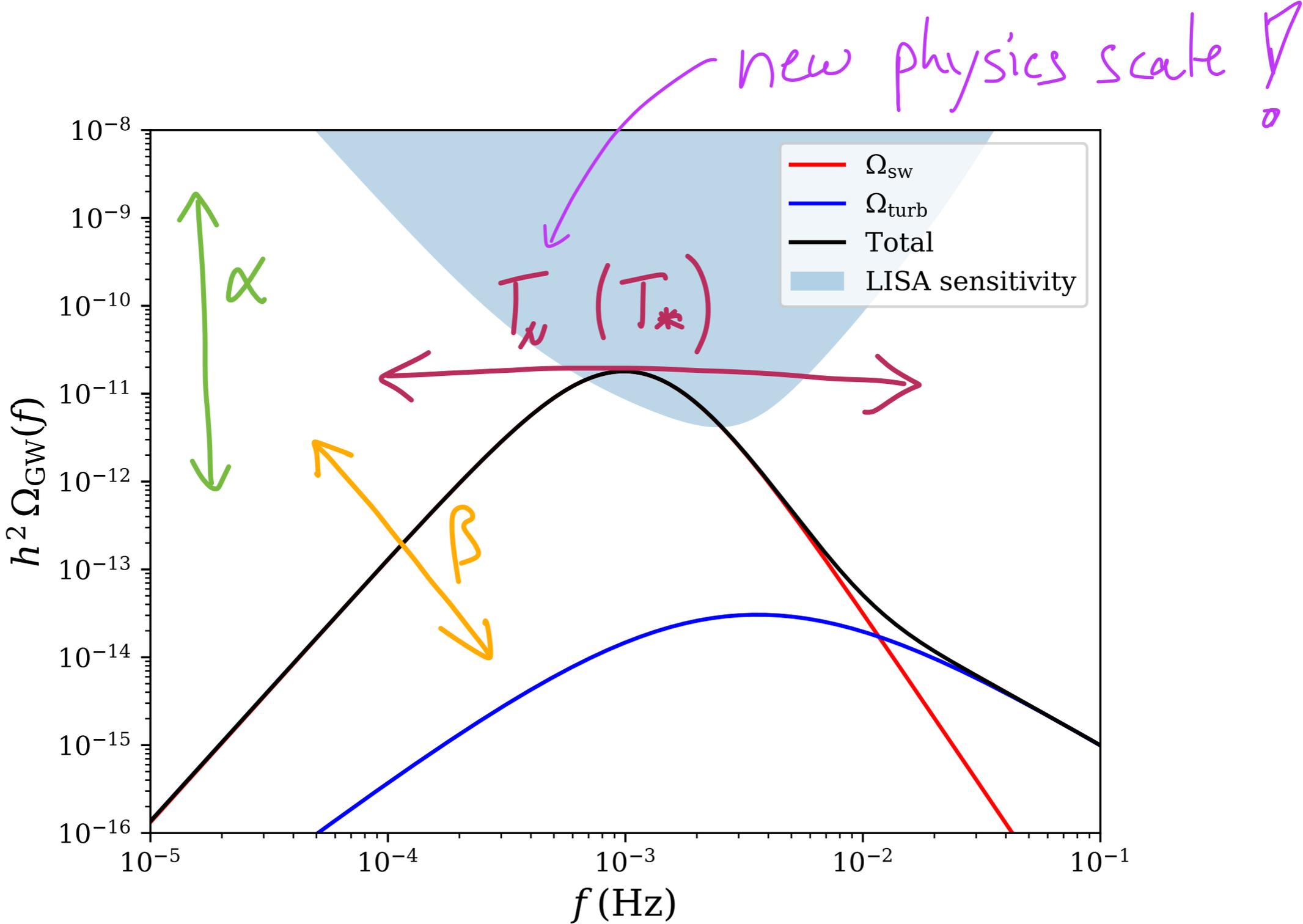
Not for:

▶  $n_f = 1$  (no global symmetry, no PT)

▶  $n_f = 2$  (not yet known)

Note: Nature of the PT does not depend on arbitrary model parameters

# Signal properties



# Combine lattice and holography

## Improved holographic QCD

$$\mathcal{S}_5 = -M_P^3 N_c^2 \int d^5x \sqrt{g} \left[ R - \frac{4}{3} (\partial\Phi)^2 + V(\Phi) \right] + 2M_P^3 N_c^2 \int_{\partial M} d^4x \sqrt{h} K$$

- ▶ AdS Einstein-dilaton gravity  $\leftrightarrow$  4D CFT
- ▶ Dilaton potential  $V(\Phi)$
- ▶ Dilaton  $\lambda = \exp \Phi \leftrightarrow$  't Hooft coupling  $\lambda_t = N_c g_{YM}^2$
- ▶ ...
- ▶ Solutions of EOM  $\leftrightarrow$  phases of SU(N)

Gürsoy, Kiritsis, Mazzanti, Nitti  
0707.1324, 0707.1349, 0812.0792, 0903.2859, ...

# Improved holographic QCD

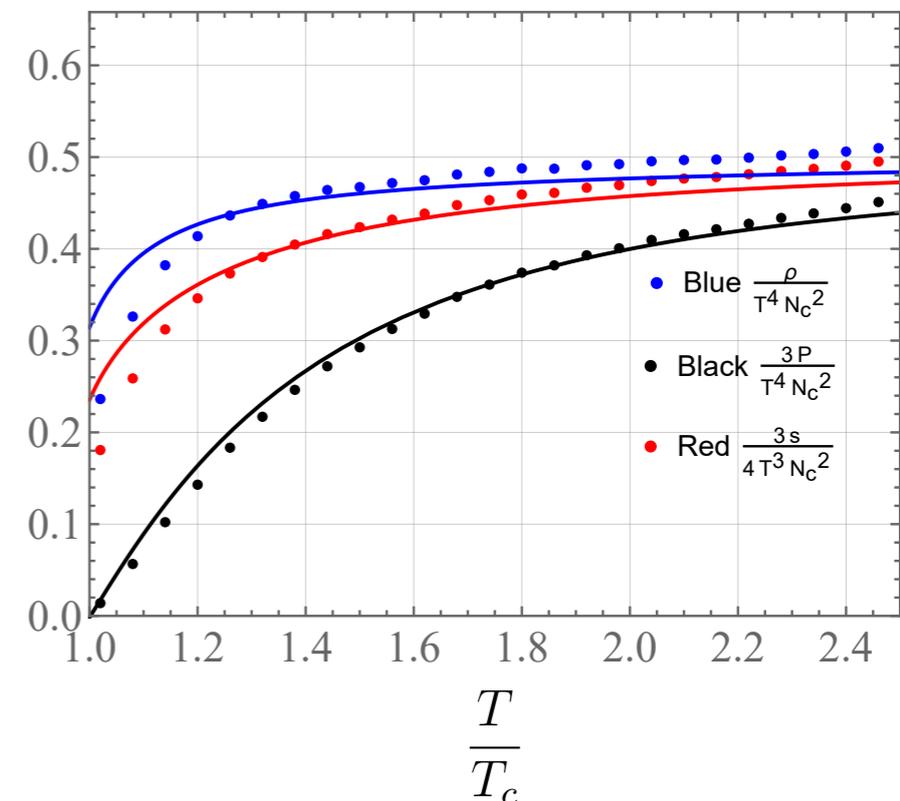
Want this to reproduce SU(N) theories

- ▶ Confinement in IR ( $\lambda \rightarrow \infty$ )
- ▶ Yang Mills beta function in UV ( $\lambda \rightarrow 0$ )

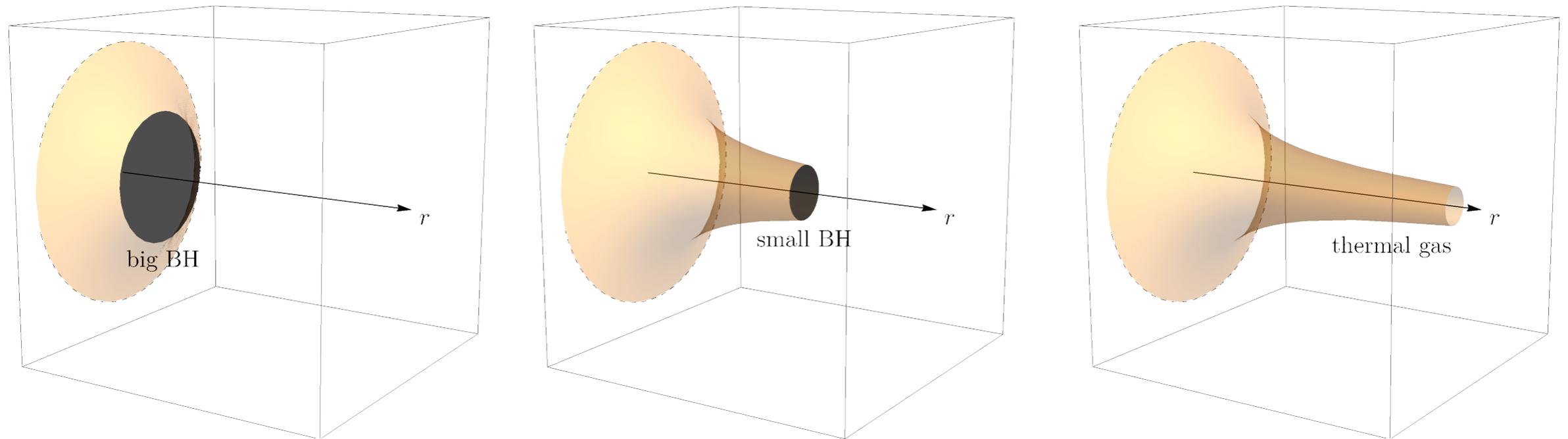
$$V(\lambda) = \frac{12}{\ell^2} \left\{ 1 + V_0 \lambda + V_1 \lambda^{4/3} [\log(1 + V_2 \lambda^{4/3} + V_3 \lambda^2)]^{1/2} \right\}$$

Fix parameters:

- ▶  $V_0, V_2$  to reproduce 2 loop YM running in UV
- ▶  $V_1, V_3$  fit to reproduce SU(3) lattice thermodynamics in IR



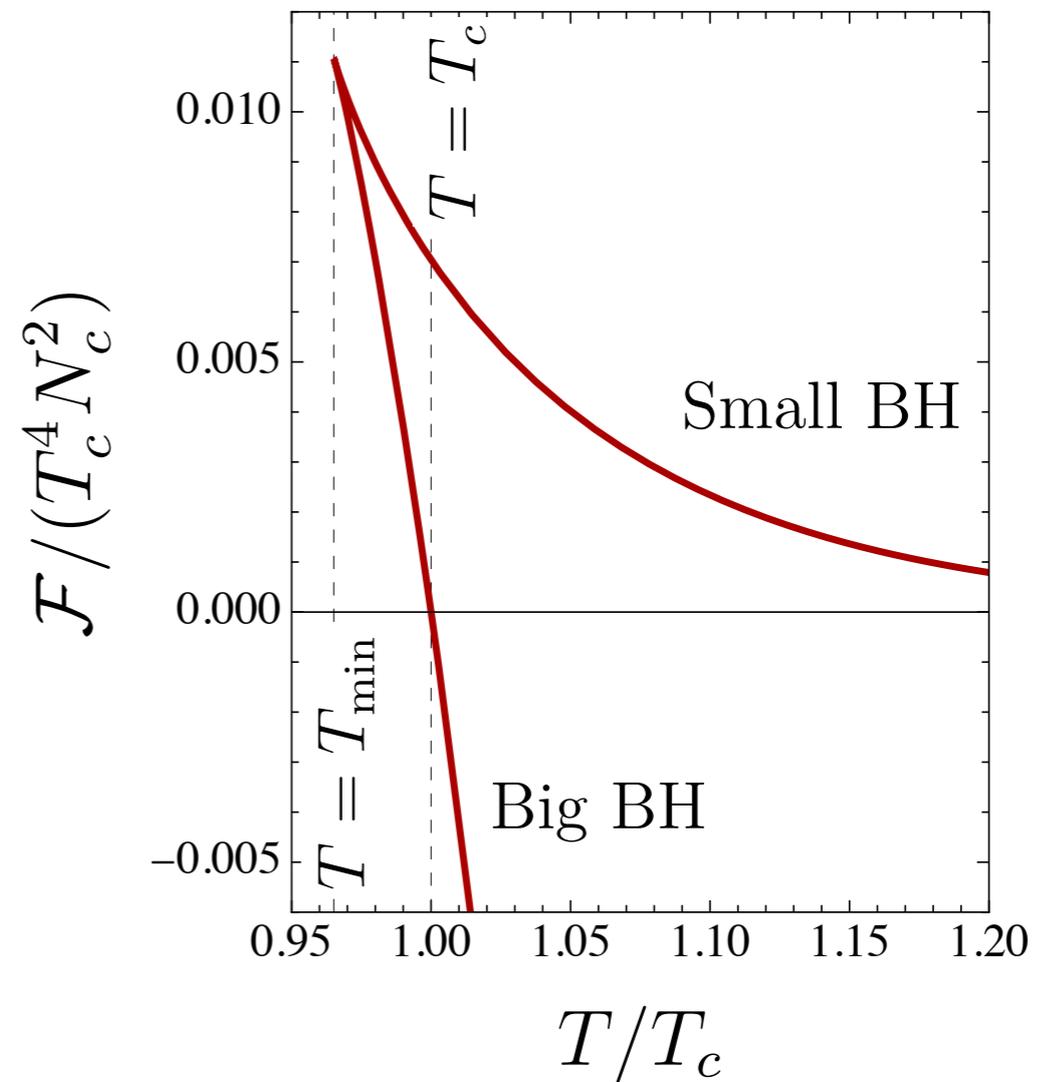
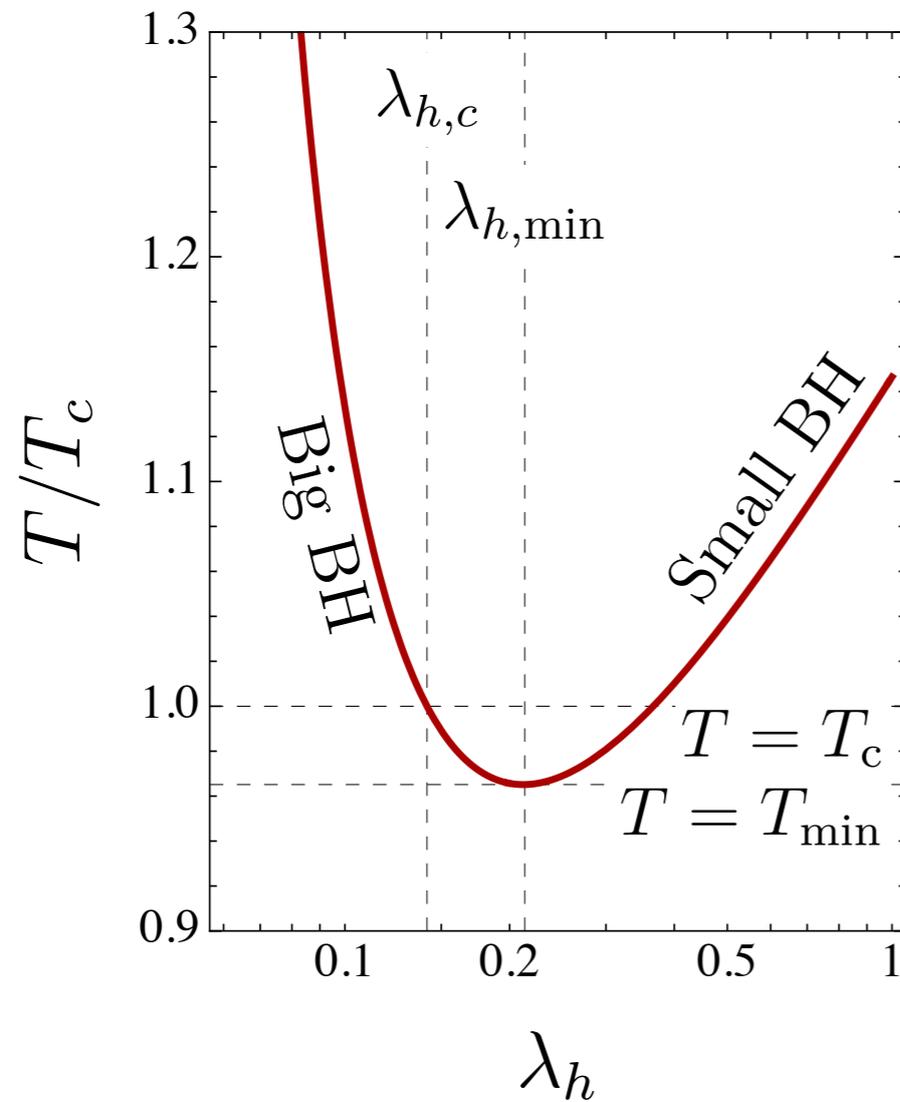
# The phase transition in ihQCD



## Three solutions

- ▶ Big BH: Deconfined phase
- ▶ Small BH: Unstable, saddle point
- ▶ Thermal gas: Confined phase

# The phase transition in ihQCD II



At  $T = T_c$ , deconfined phase becomes meta-stable

Morgante, Ramberg, PS, 2210.11821

# The phase transition in ihQCD III

Hawking Page transition, with small BH acting as instanton

To compute bounce action, need effective action (or free energy) along the full path

Interpolate between big and small BH solutions

- ▶ Do some hard work...
- ▶ Win :)

Morgante, Ramberg, PS, 2210.11821

