



# Experimental Prospects for Fundamental Physics with Muonium

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Reference: Snowmass2021 Whitepaper: Muonium to antimuonium conversion, arXiv:2203.11406

# Content

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- **Motivation**
- **Conceptual Design of MACE**
- **Simulation Result**
- **Summary**



# Content

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- **Motivation**
- Conceptual Design of MACE
- Simulation Result
- Summary



# Searching for cLFV

- Searching for charged lepton flavor violation (cLFV):

- Mu2e }  $\mu$ -e conversion
- COMET }  $\mu$ -e conversion
- Mu3e →  $\mu \rightarrow eee$
- MEGII →  $\mu \rightarrow e\gamma$

- Why cLFV:

- cLFV, as a neutrino-less lepton flavor violating process, is forbidden in SM.
- Precise (high-intensity) experiment searching for cLFV, is an sensitive probe of BSM.
- New scalar or vector particles can be constrained.

Andrew's talk

Jian's talk

COMET  $\mu$   
e

MU2e

Frederik's talk

Luca's talk

$\mu^+$

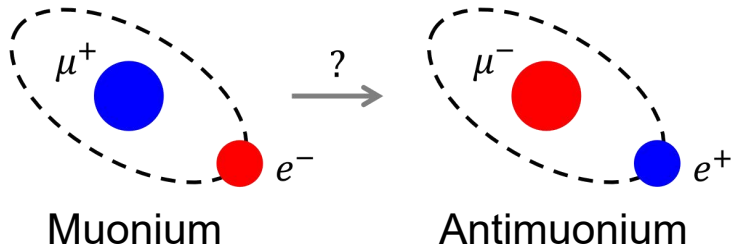
$\gamma$

$e^+$

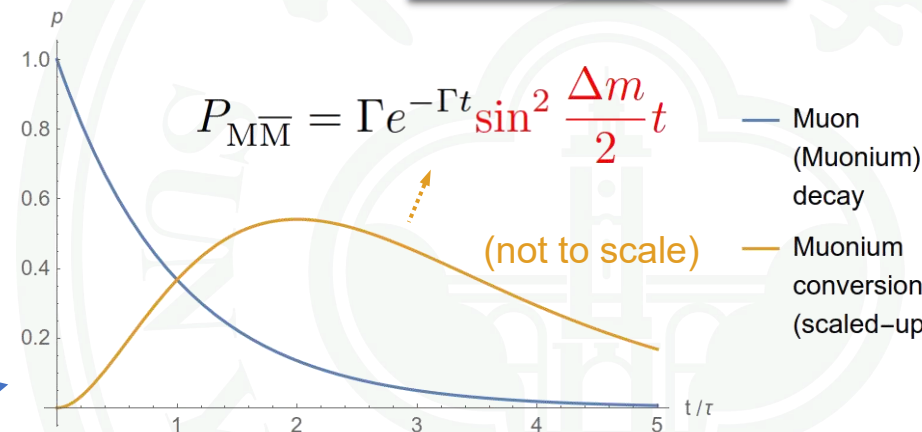
MACE

# Muonium Conversion: a cLFV Process

- Muonium ( $\mu^+e^-$ ): a leptonic isotope of hydrogen;
- Muonium conversion is induced by an interesting phenomenological possibility: **muonium mixing**.



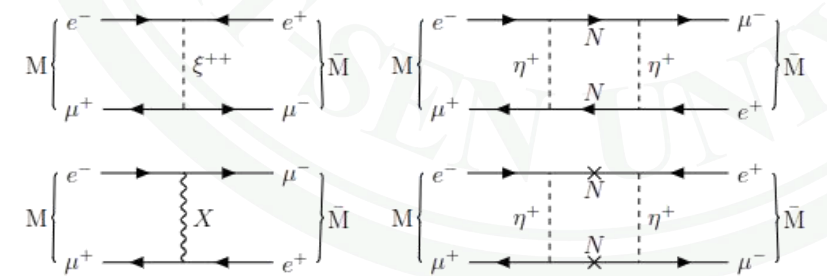
Yuichi Uesaka's talk



$$i \frac{\partial}{\partial t} |\psi\rangle = \mathcal{M} |\psi\rangle \quad |\psi\rangle = \alpha(t) |M\rangle + \beta(t) |\bar{M}\rangle$$

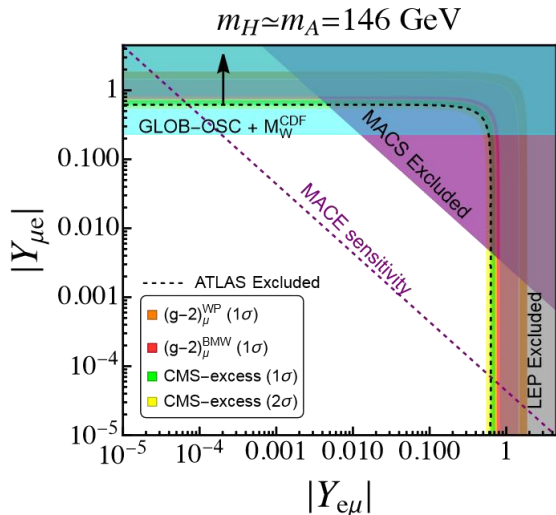
$$\mathcal{M} = \begin{pmatrix} m - i\Gamma/2 & \Delta m/2 - i\Delta\Gamma/4 \\ \Delta m/2 - i\Delta\Gamma/4 & m - i\Gamma/2 \end{pmatrix}$$

$$\mathcal{L} \supset \sum_{i=1}^5 \frac{-G_i(\mathcal{M})}{\sqrt{2}} \langle \bar{M} | Q_i | M \rangle$$



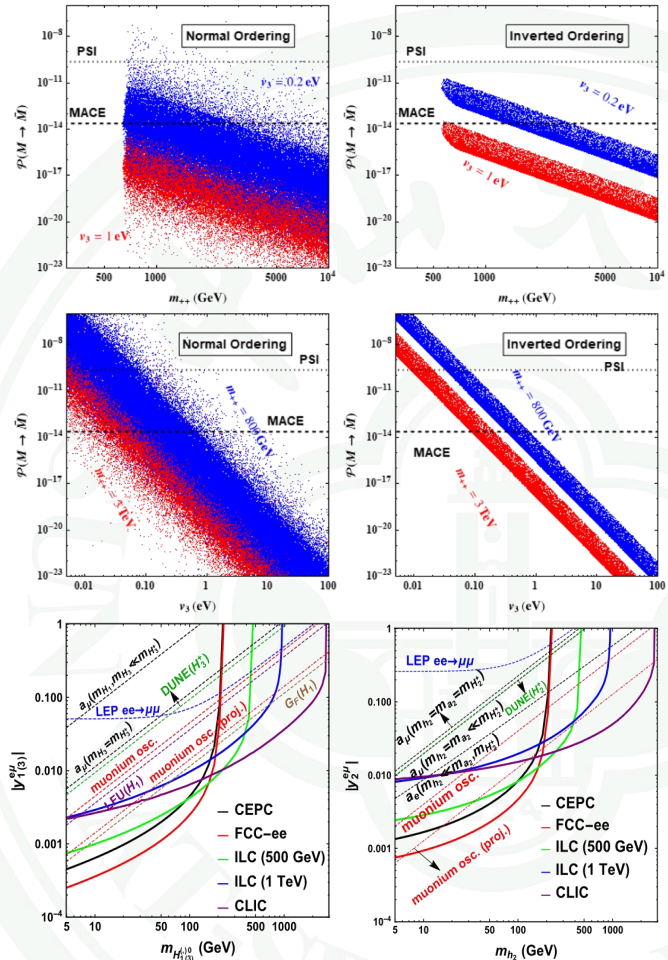
# Why Muonium Conversion?

- Muonium conversion: a  $\Delta L=2$  cLFV process.
- Neutrino mass model: doubly charged TeV Higgs boson can be constrained.
- Complementary to:
  - $\Delta L=1$  cLFV experiments ( $\mu$ - $e$  conversion,  $\mu \rightarrow eee$ ,  $\mu \rightarrow e\gamma$ ).
  - Collider experiments.



Bhupal's talk

Afik, BD, Thapa, Hints of a new leptophilic Higgs sector? arXiv 2305.19314



Chengcheng Han, Da Huang, Jian Tang, Yu Zhang. Probing the doubly charged Higgs boson with a muonium to antimuonium conversion experiment. Phys.Rev.D 103 (2021) 5, 055023

Tong Li, Michael A. Schmidt. Sensitivity of future lepton colliders and low-energy experiments to charged lepton flavor violation from bileptons. Phys.Rev.D 100 (2019) 11, 115007

# What Happened in History?

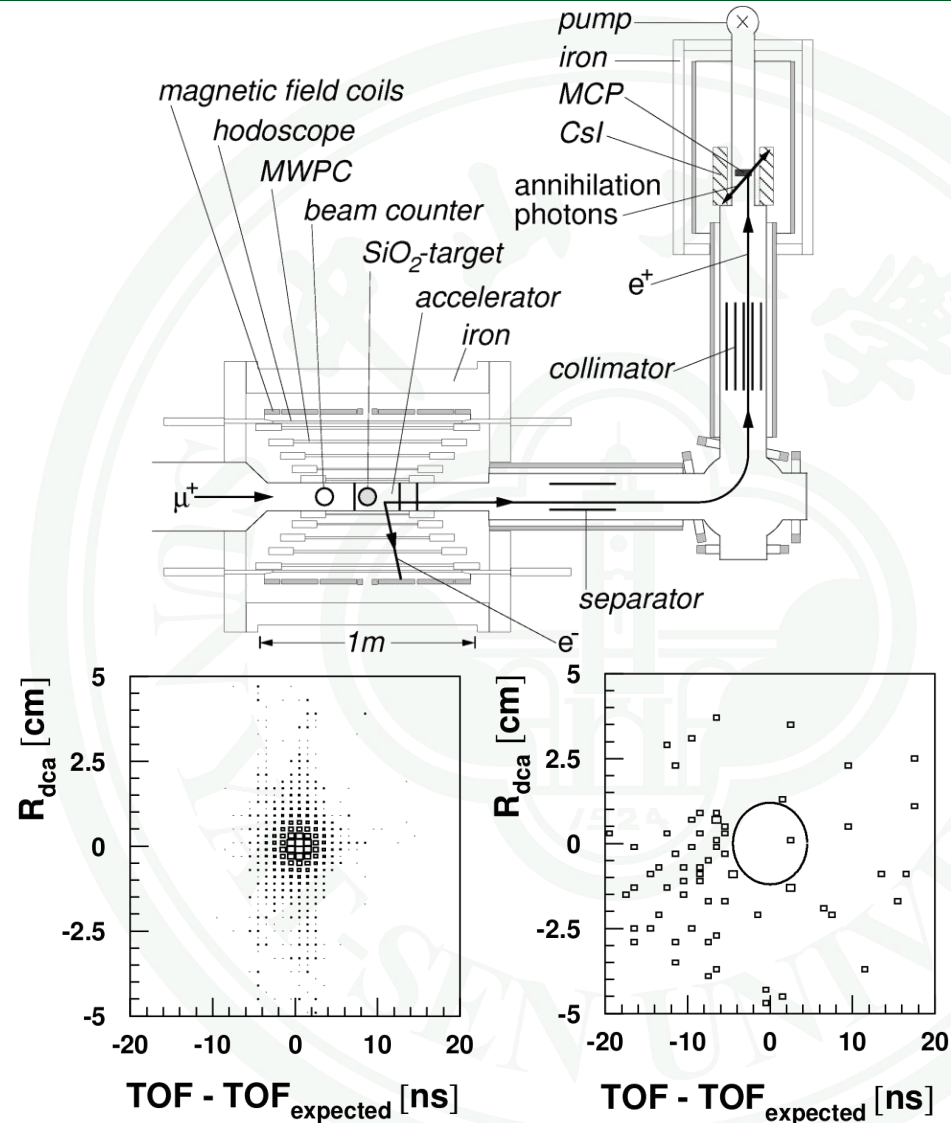
- Current limit (L. Willmann, 1999):

$$P_{M\bar{M}} < 8.3 \times 10^{-11} \text{ (90\% C.L.)}$$

- Can we do substantially better?

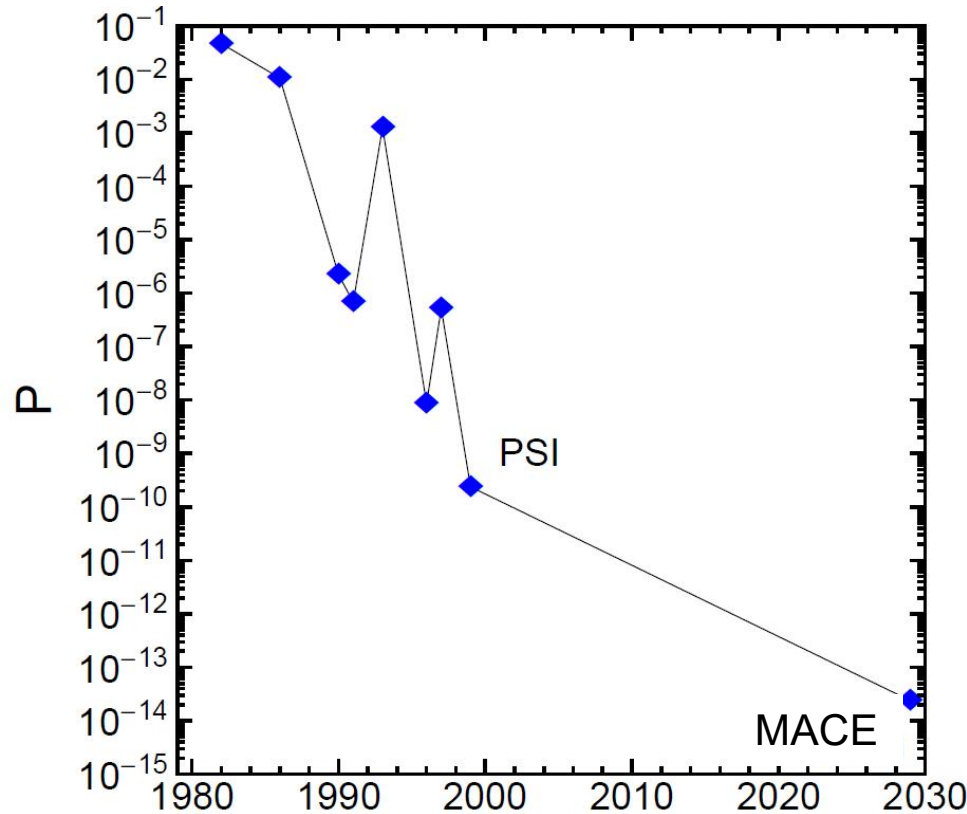
- 20 years later:

- Detector technology and design is improving.
- Muon beam luminosity is much higher.
- Better muonium targetry.



L. Willmann et al. New bounds from searching for muoniumium to anti-muoniumium conversion, Phys.Rev.Lett. 82 (1999), 49-52.

# MACE: Shed Light on New Physics



- **MACE:** The first proposed muonium-to-antimuonium conversion experiment since 1999, we plan to improve the sensitivity by more than two orders of magnitude.
- Together with other flavor and collider searches, we will shed light on the mystery of new physics.

**MACE: Muonium-to-Antimuonium Conversion Experiment**



# Content

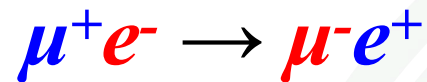
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- Motivation
- **Conceptual Design of MACE**
- Simulation Result
- Summary

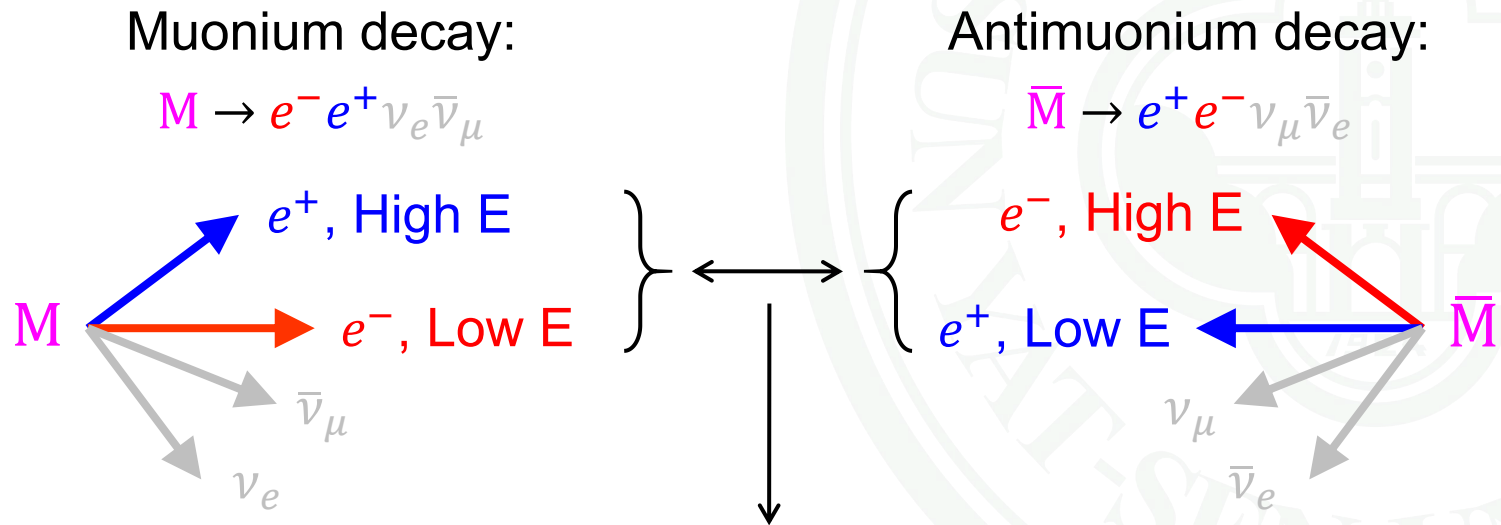


# Conceptual Design of MACE

- How to detect the muonium-antimuonium conversion?



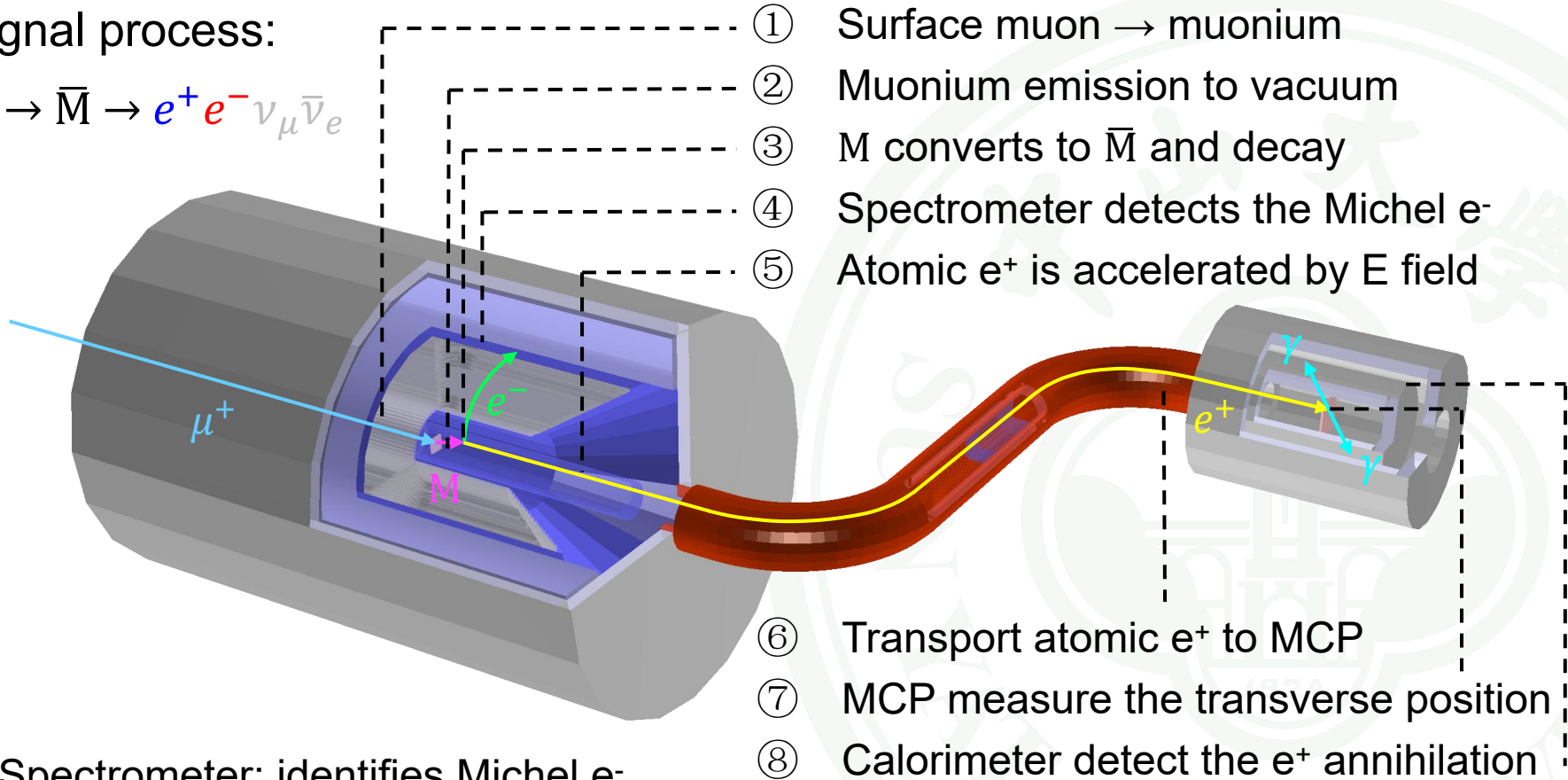
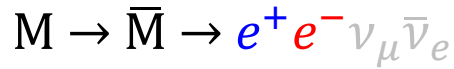
- We can achieve this by identifying the final states:



Search for the conversion by vertex coincidence and charge identification.

# Conceptual Design of MACE

Signal process:



- Spectrometer: identifies Michel  $e^-$ .
- Vertex coincidence: Michel  $e^-$  track and  $e^+$  transverse position projection.
- Calorimeter: identifies atomic  $e^+$ .

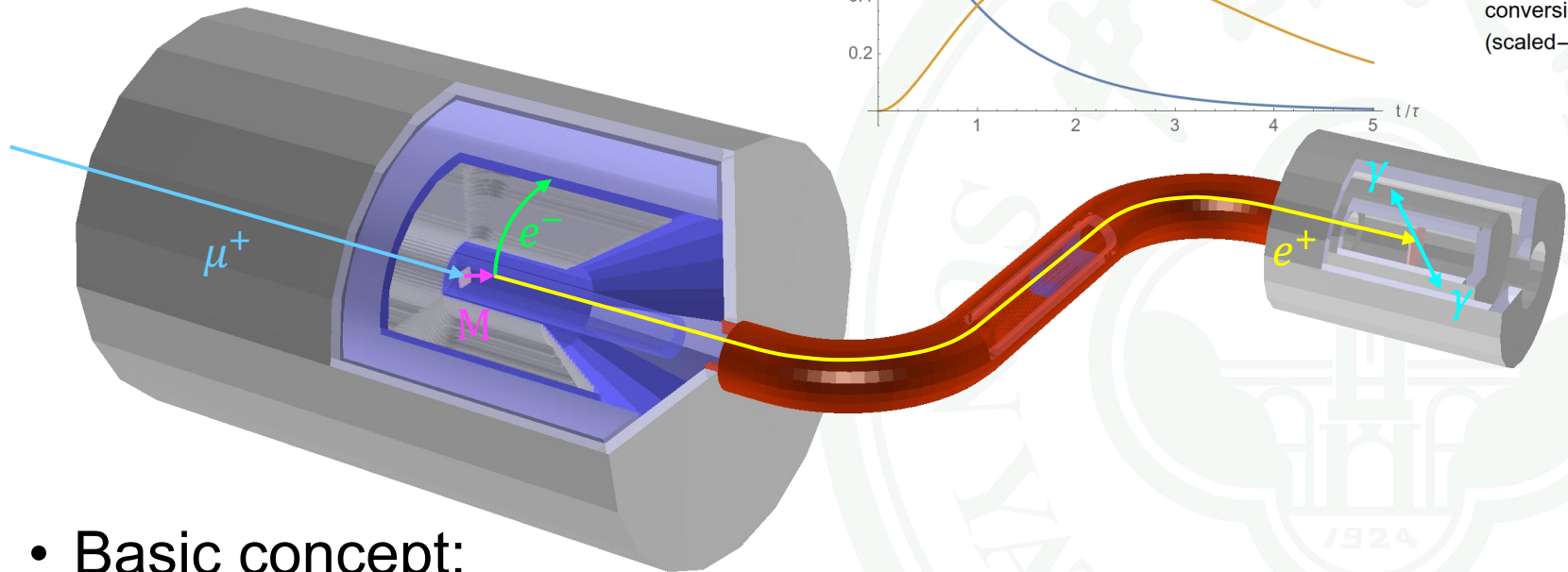
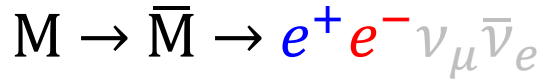
- ① Surface muon  $\rightarrow$  muonium
- ② Muonium emission to vacuum
- ③  $M$  converts to  $\bar{M}$  and decay
- ④ Spectrometer detects the Michel  $e^-$
- ⑤ Atomic  $e^+$  is accelerated by E field
- ⑥ Transport atomic  $e^+$  to MCP
- ⑦ MCP measure the transverse position
- ⑧ Calorimeter detect the  $e^+$  annihilation

**Basic concept:**

**Coincidence of spectrometer, MCP, and calorimeter.**

# Conceptual Design of MACE

- Signal process:



- Basic concept:

- Coincidence of a Michel  $e^-$  and a  $e^+$  from atomic shell:

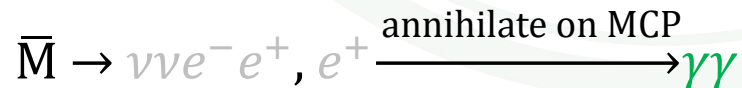
1. Spectrometer



2. MCP



3. Calorimeter



# MACE Upper Bound & Muonium Yield

- As an intensity frontier cLFV experiment, MACE demands as much primary particles as possible:
- A simple estimation: inheriting previous PSI experiment parameters (L. Willmann et al., 1999), we have conversion probability upper bound estimation

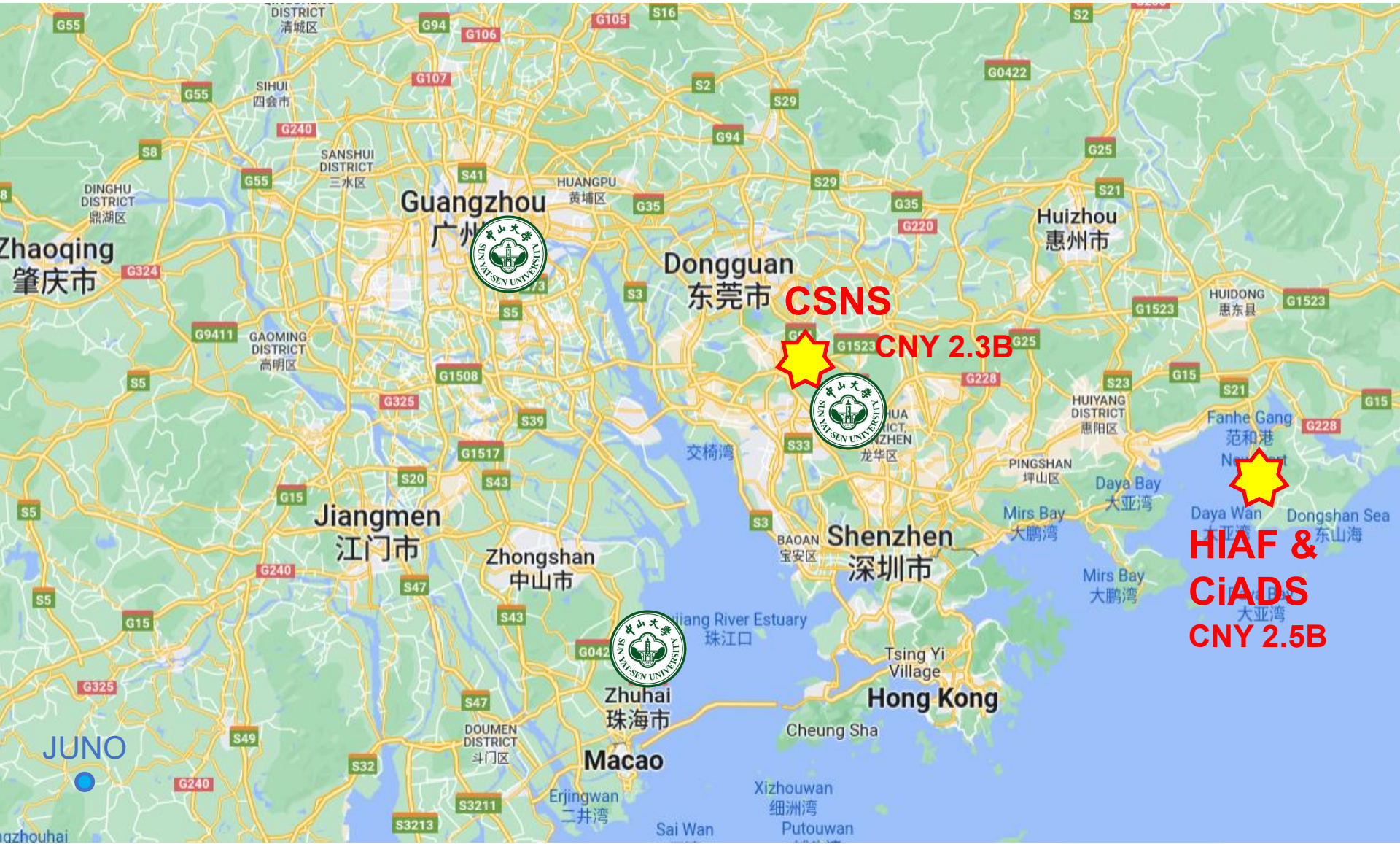
$$P_{M\bar{M}} < \frac{2.30 F_C}{\epsilon_{\text{all}} S_B Y_M L_\mu t}$$

Signal efficiency  
 B field suppression  
 Muonium yield  
 Muon beam luminosity  
 Acquisition time

$$N_M = Y_M L_\mu t$$

- Acquisition time is precious, the upper bound is limited by the number of muoniums ( $N_M$ ), we need more muoniums!
- Two approaches:
  1. Enhance beam luminosity  $L_\mu$ :  
 →  $10^8 \sim 10^{10} \mu^+/\text{s}$  beam
  2. Enhance muonium yield  $Y_M$ :  
 → Optimization of silica aerogel target, or new possibilities (e.g. SF-He).

# Accelerator Muon Source Proposed in China



# Muon Source Proposed at CiADS

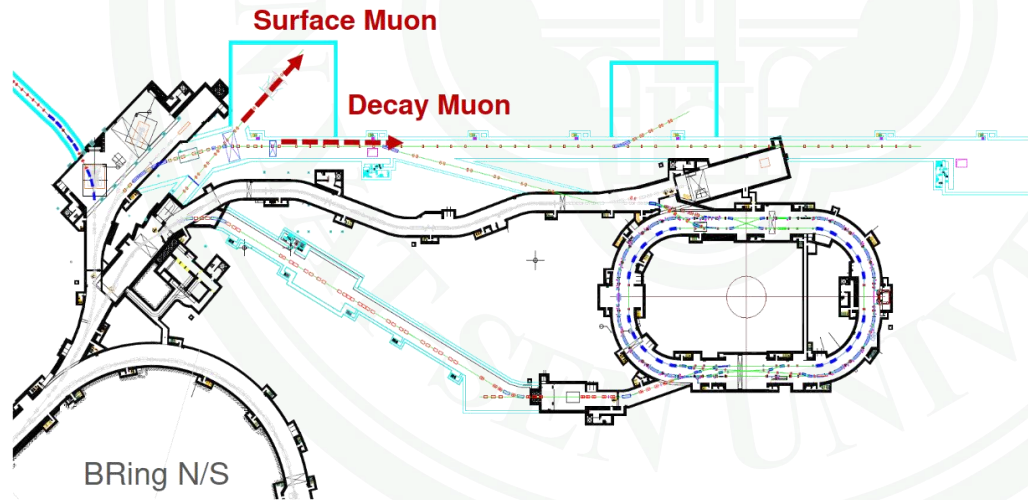
- Proton accelerator.
- Located in Huizhou, Guangdong, PRC.
- Status: constructing (accelerator), conceptual (muon source).
- Intensity:  $10^9 \sim 10^{10} \mu^+/s$
- Beam mode: CW
- Available at ~2030s.

Reference: Jiancheng Yang and He Zhao, MIP2023, 15 Apr. 2023



# Muon Source Proposed at HIAF

- Proton / ion accelerator.
- Located in Huizhou, Guangdong, PRC.
- Status: constructing (accelerator), conceptual (muon source).
- Intensity:  $10^{10} \mu^+/\text{s}$  ?
- Beam mode: CW
- Available at ~2030s.

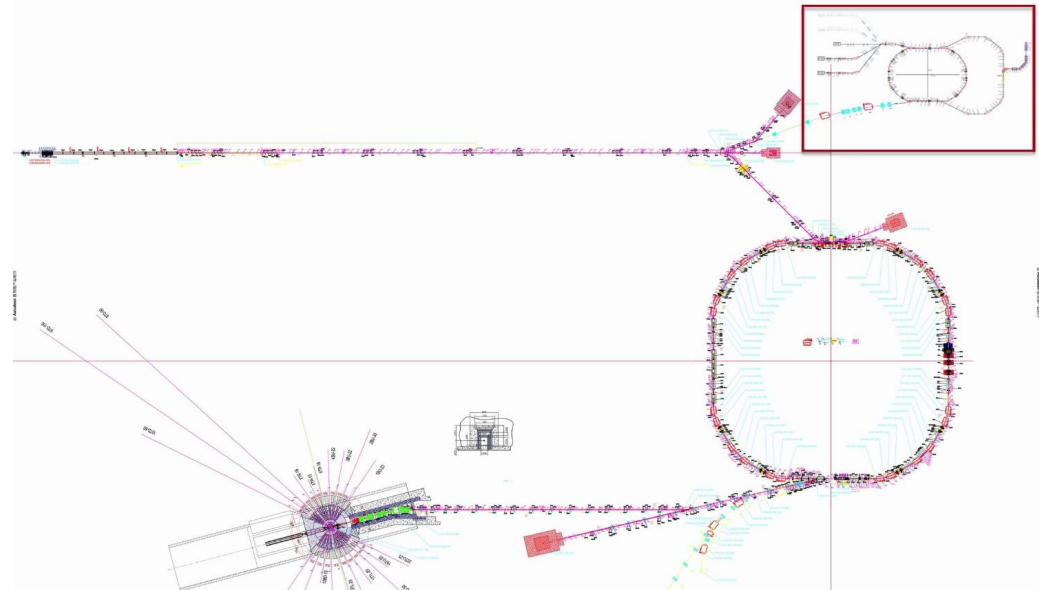
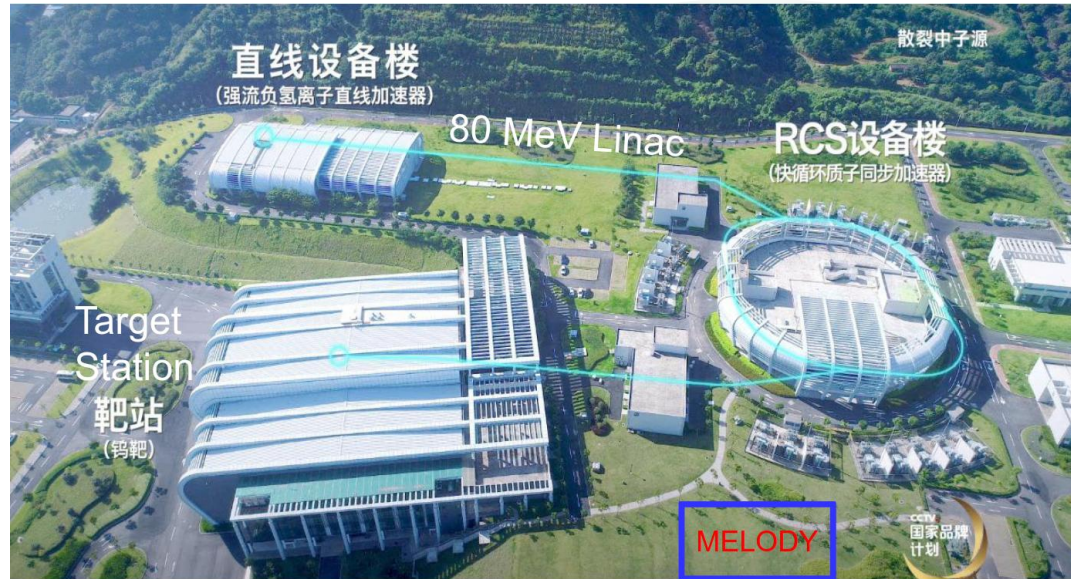


Reference: Yuan He, MIP2023, 15 Apr. 2023



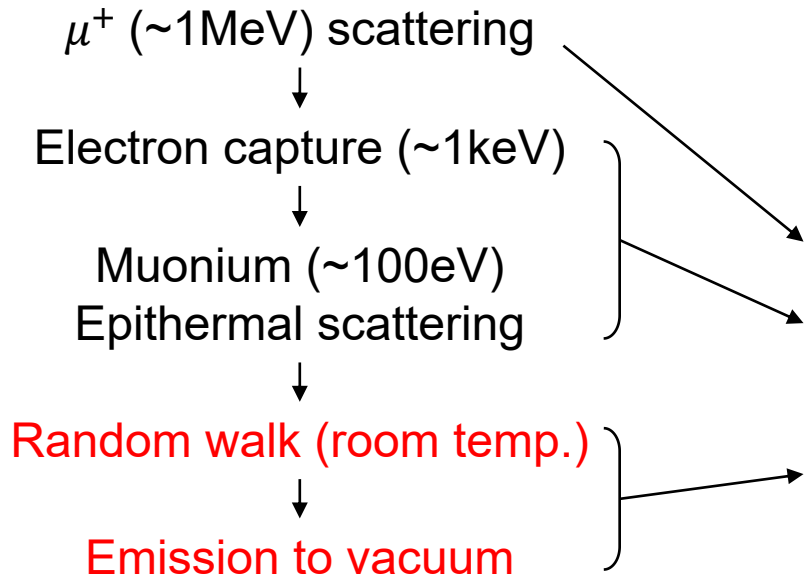
# Muon Source Proposed at CSNS

- Proton accelerator.
- Located in Dongguan, Guangdong, PRC.
- Status: **running** (accelerator), conceptual (EMuS), **approved** (MELODY), conceptual (HEMS).
- Intensity:  $10^5 \sim 10^6 \mu^+/s$
- Beam mode: Pulsed (MELODY: 1Hz, HEMS: 100Hz)
- Available at 2028.



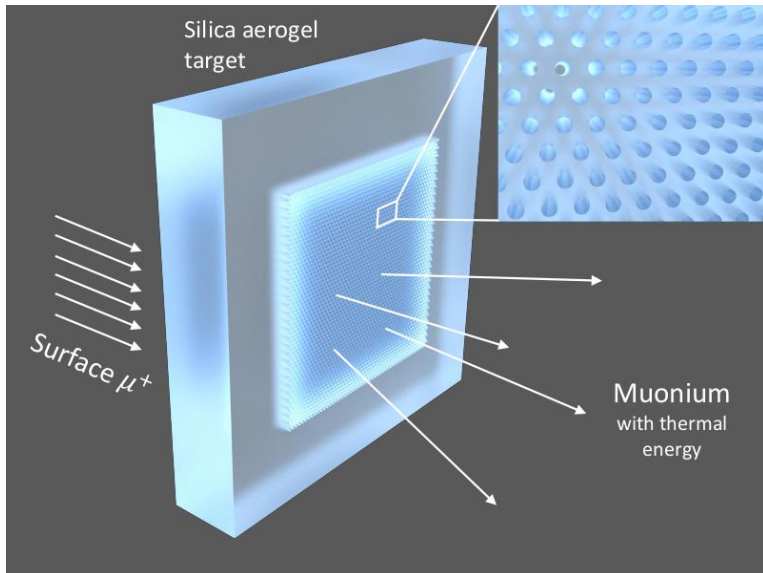
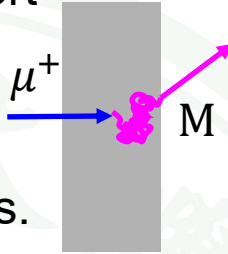
Reference: Yu Bao, MIP2023, 15 Apr. 2023

# Muonium Production and Transport

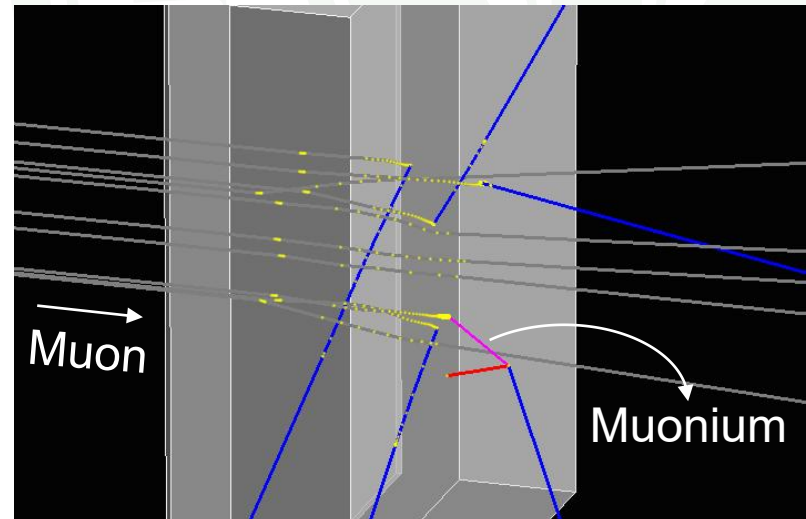


MC simulation for muonium transport has been developed under the MACE offline software framework.

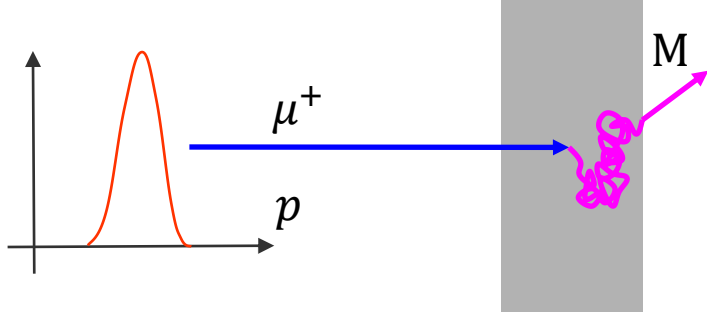
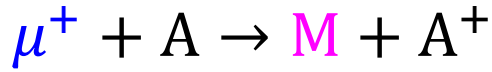
- ① Geant4 low-energy EM process.
- ② Geant4 AtRest process, modeled phenomenologically.
- ③ Random walk approach to thermal muonium tracking.



Simulation:

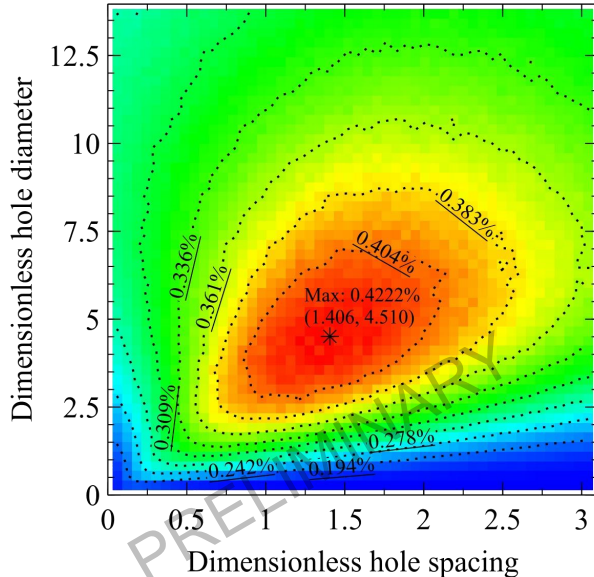


# Muonium Yield Simulation

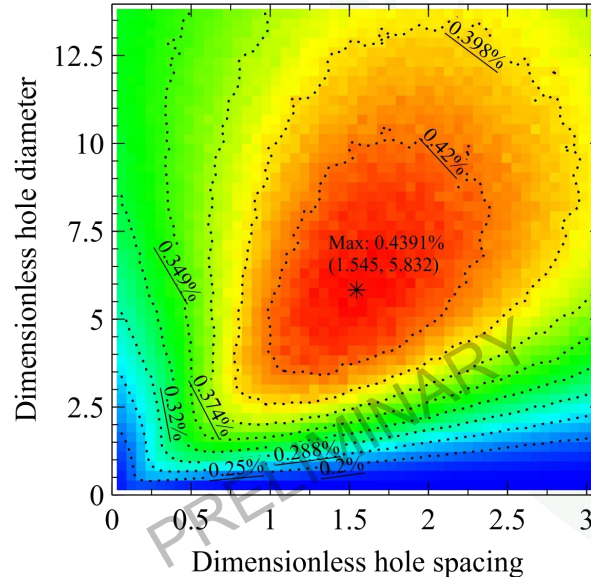


- Surface muon beam momentum spread: 10%
- Muonium mean free path: 200 nm, temp.: 300 K
- Optimal diameter:  $1.55\sqrt{D\tau}$  (50.8  $\mu\text{m}$ )
- Optimal spacing:  $5.83\sqrt{D\tau}$  (191  $\mu\text{m}$ )
- Max vacuum muonium yield: 0.44%

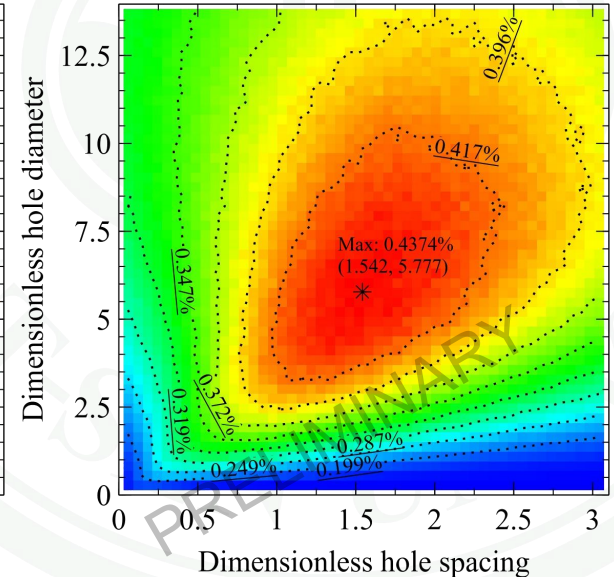
Depth: 1 mm



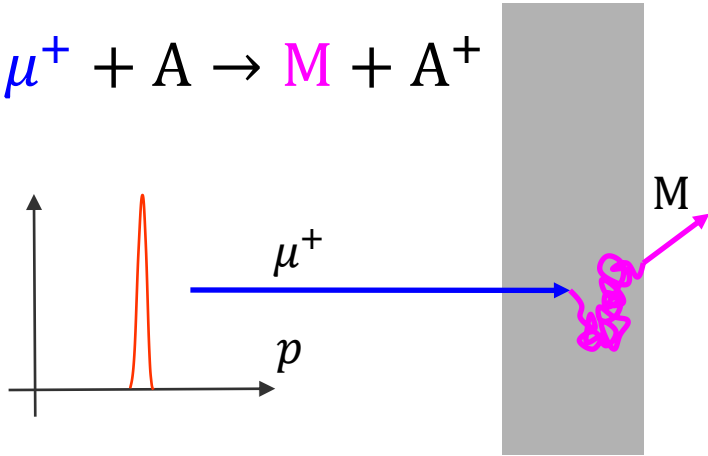
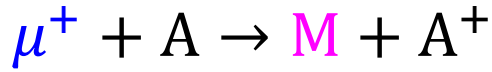
Depth: 3 mm



Depth: 5 mm

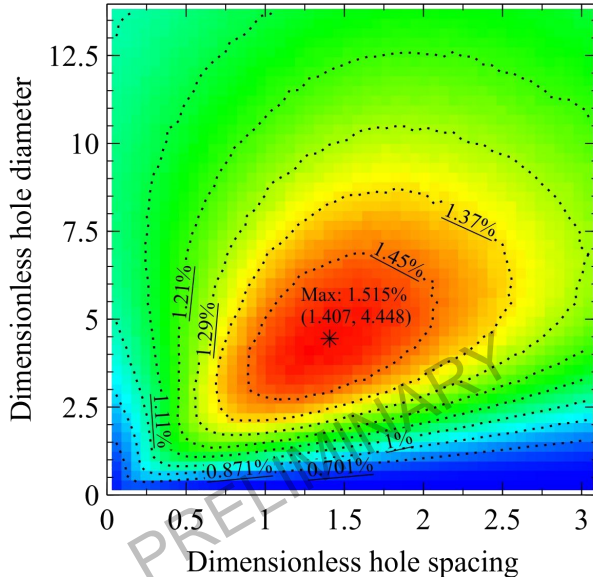


# Muonium Yield Simulation - Low $\sigma_p$ Beam

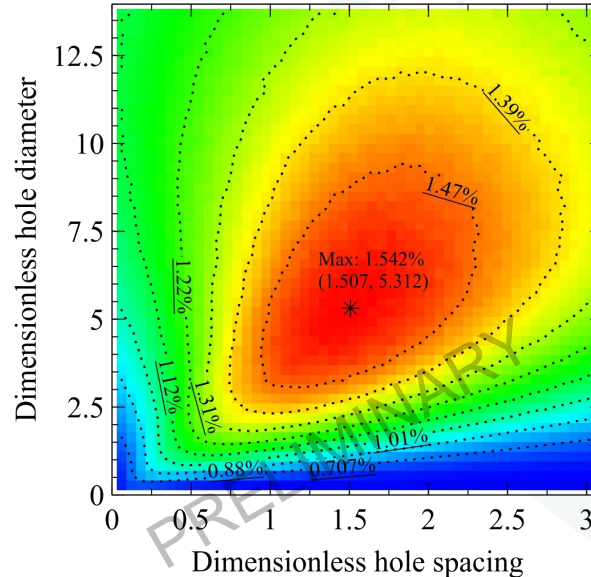


- Surface muon beam momentum spread: 2.5%
- Muonium mean free path: 200 nm, temp.: 300 K
- Optimal diameter:  $1.51\sqrt{D\tau}$  (49.5  $\mu\text{m}$ )
- Optimal spacing:  $5.31\sqrt{D\tau}$  (175  $\mu\text{m}$ )
- Max vacuum muonium yield: **1.54%**

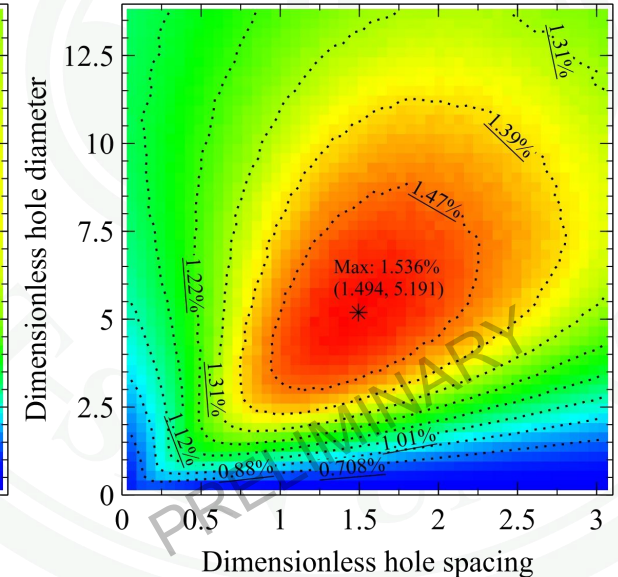
Depth: 1 mm



Depth: 3 mm

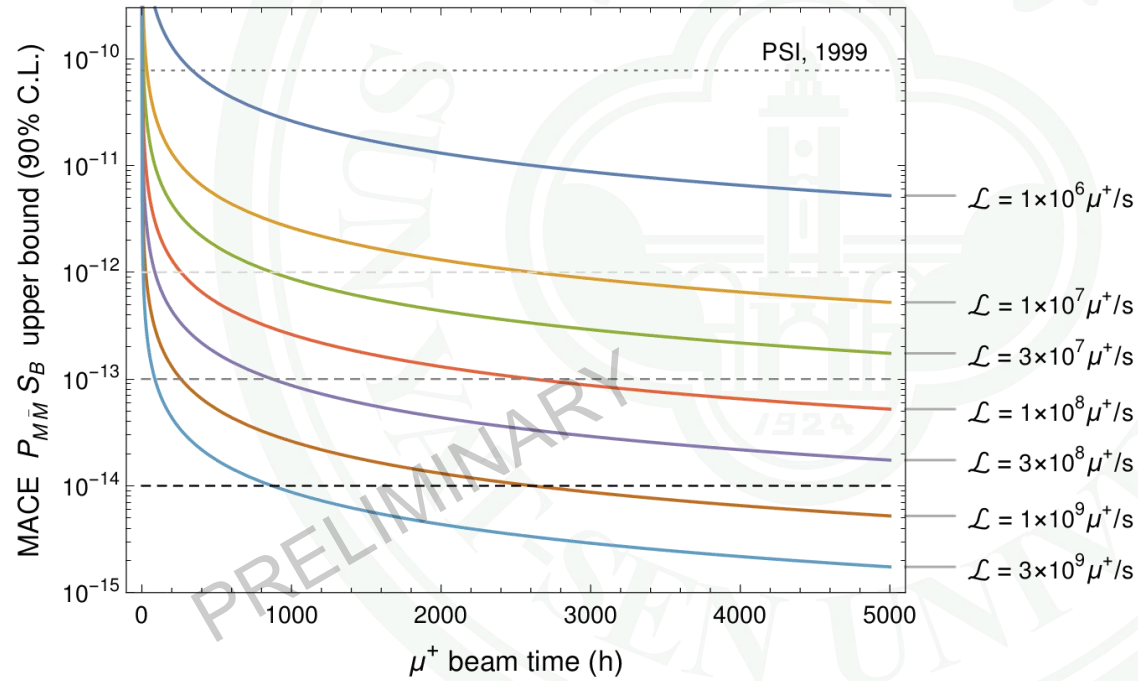


Depth: 5 mm



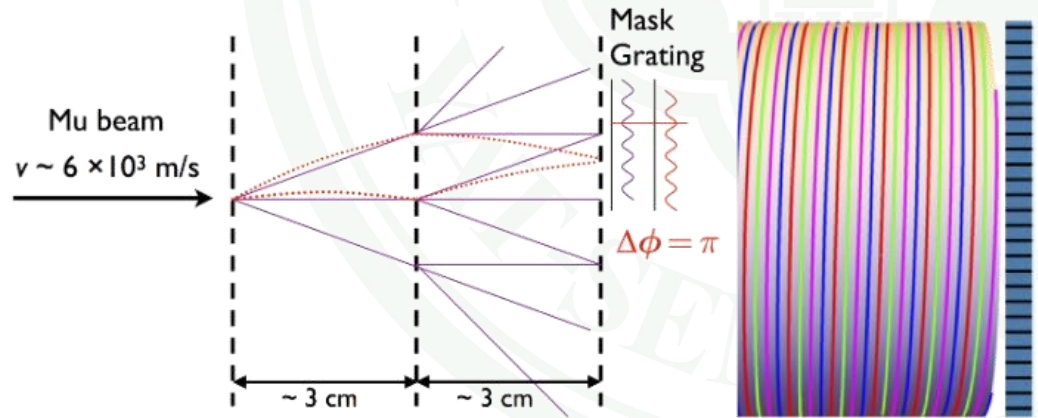
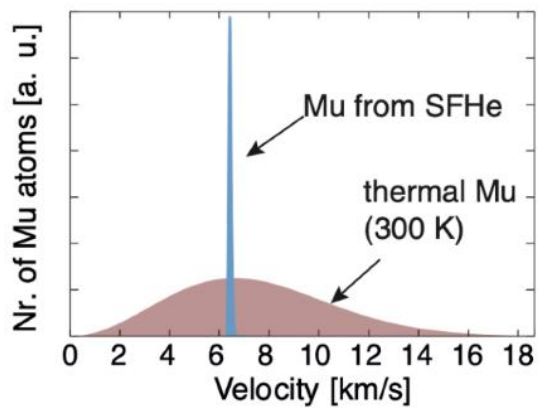
# Muonium Yield and Upper Bound

- Acquisition time is precious, the upper bound is limited by the number of muoniums ( $N_M$ ).
- The more muoniums the merrier.
- If the beam luminosity reaches  $10^8 \mu^+/s$  and the muonium yield increases by 2 orders of magnitude, MACE can improve the upper bound by 3 orders of magnitude.
- The improvement of detector performance will make contributions, correspondingly.



# Muonium Gravity Experiment (MAGE) in US

- Weak equivalence principle of GR is assumed to apply to antimatter.
- However, no direct test of antimatter gravity has been made.
- Challenge: MAGE needs low-divergence source of slow muonium traveling in vacuum.
- Possible solution: SFHe muonium targetry & intensive muon beam.



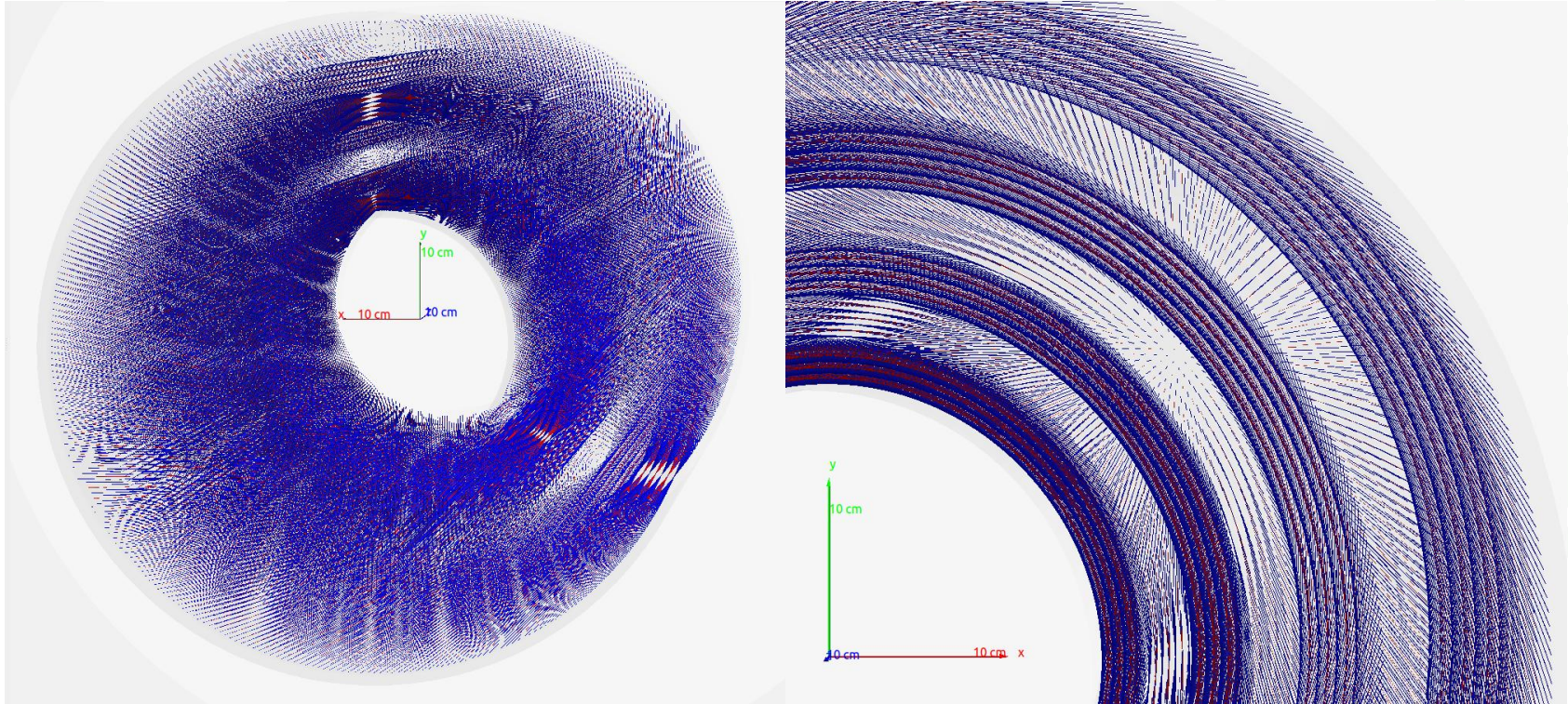
Reference: Daniel Kaplan, Caltech Workshop, 28 Mar. 2023

# Design of Drift Chamber

- The performance of a drift chamber is largely determined by its geometry design, including:
  - Drift cell design
  - Arrangement of wires (stereo/axial)
  - Solid angle coverage, etc.
- To guarantee the required resolution, we design the drift chamber for MACE with following specifications:
  - Square drift cell with minimum cell deformation.
  - Layers of cells are divided into different super layers, cells in the same super layer are twisted identically (all axial, or all stereo with specific stereo angle).
  - Interlaced axial/stereo layer (e.g. VAUAVAU..., A: axial layer, V: stereo layer with positive stereo angle, U: stereo layer with negative stereo angle).

# Design of Drift Chamber

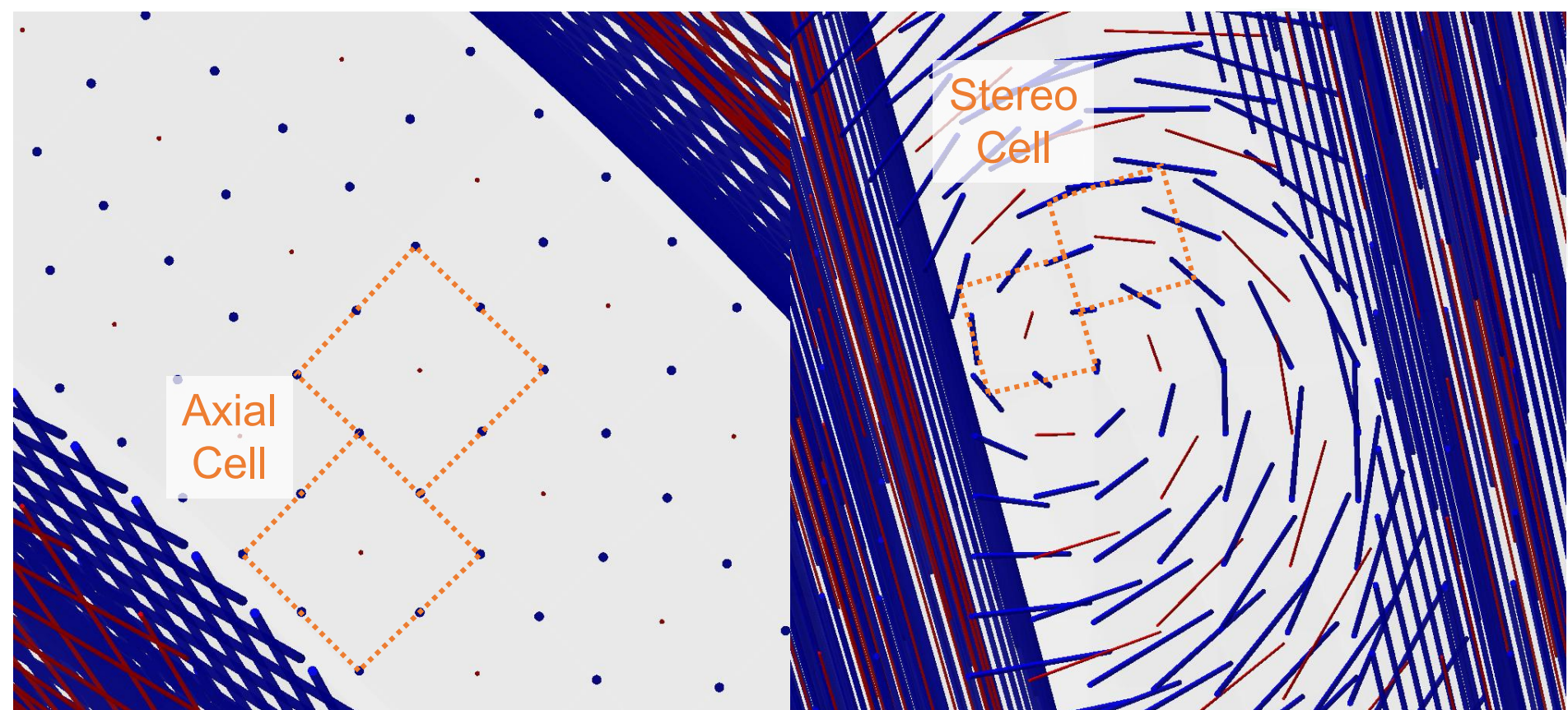
- We have developed an algorithm to generate the drift chamber geometry, allowing us to evaluate and optimize the geometry design of drift chamber.



- Figure: generated Drift chamber geometry.
- This example chamber is consist of 7 super layer, each super layer includes 3 sense layers. They are arranged as VAUVAU. Wires are scaled to be visible (blue: field wire, red: sense wire).



# Design of Drift Chamber



- Left: drift cells in an axial super layer, cells are axial.
- Right: cells in a stereo super layer, cells are twisted.
- Wires are scaled to be clearly visible (blue: field wire, red: sense wire).

# Fast Simulation of Drift Chamber

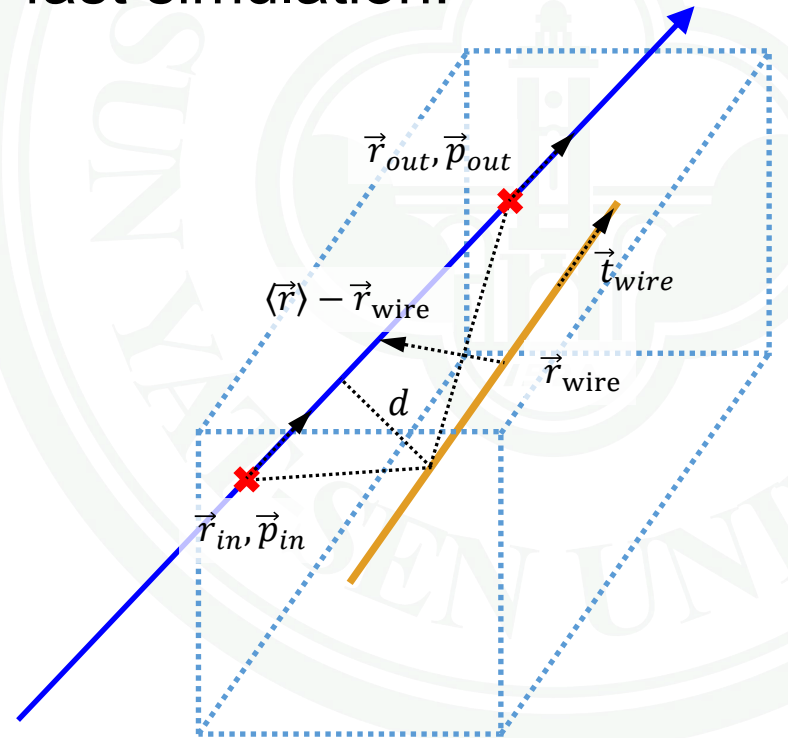
- When a charged particle passes through a drift cell, the drift distance can then be reconstructed.
- Drift distance: distance between the track and the sense wire.
- We use the simple and classical DOCA (distance of closest approach) method to perform the fast simulation:

$$d = (\langle \vec{r} \rangle - \vec{r}_{\text{wire}}) \cdot \frac{\vec{t}_{\text{wire}} \times \langle \vec{p} \rangle}{\| \vec{t}_{\text{wire}} \times \langle \vec{p} \rangle \|}$$

$$\langle \vec{p} \rangle = \frac{\vec{p}_{\text{in}} + \vec{p}_{\text{out}}}{2}$$

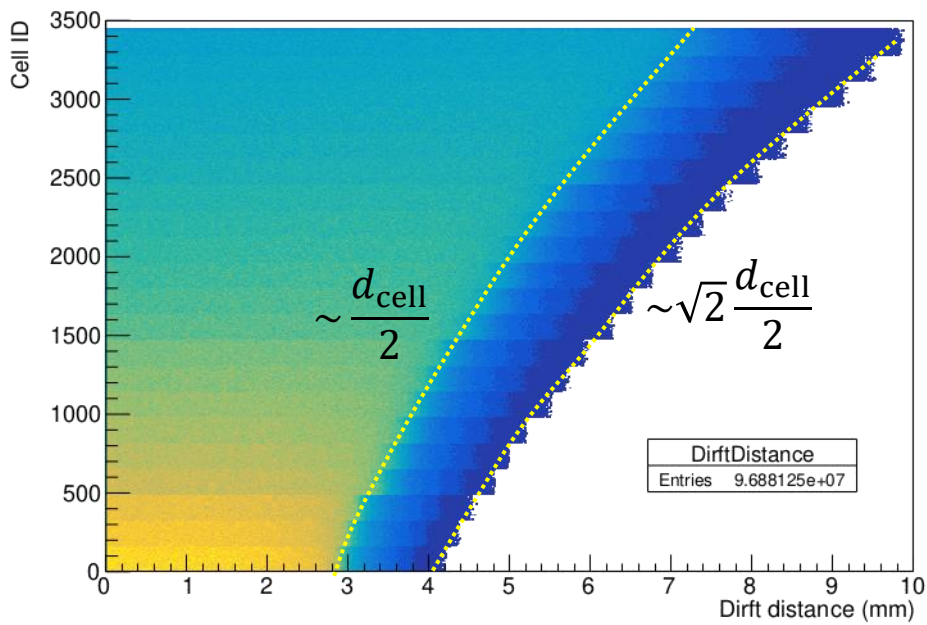
$$\langle \vec{r} \rangle = \frac{\vec{r}_{\text{in}} + \vec{r}_{\text{out}}}{2}$$

- $\vec{r}_{\text{wire}}$ : A point on the sense wire (e.g. the point at  $z=0$ )
- $\vec{t}_{\text{wire}}$ : Direction of the sense wire

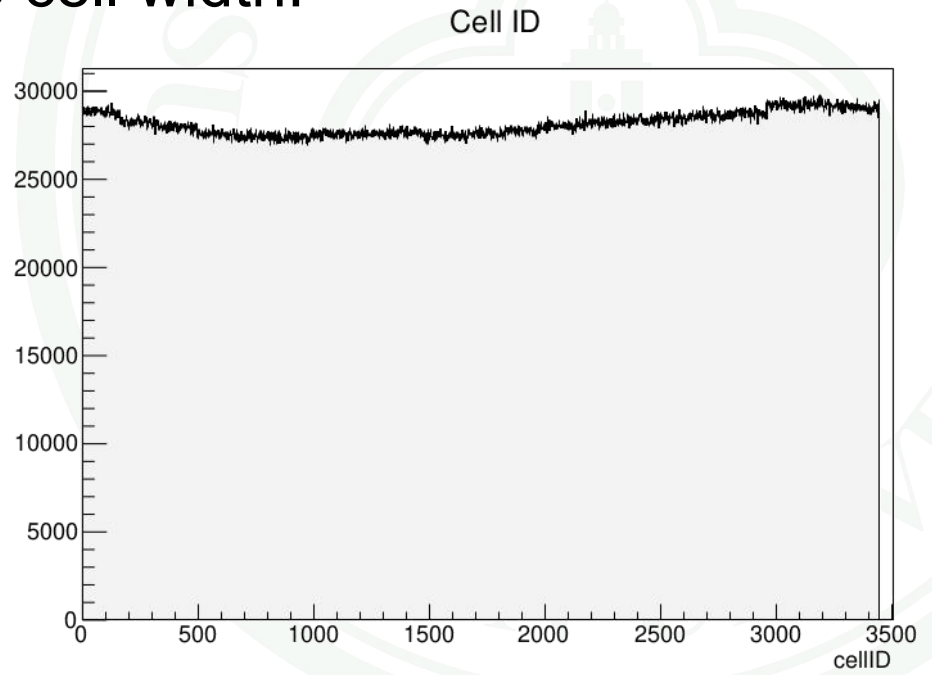


# Fast Simulation of Drift Chamber

- Using the pure geometrical DOCA method, drift distances are directly readout.
- We can check the implementation by drawing its distribution.
- For example, the drift distance and hit rate distribution of a Drift chamber with 10 mm reference cell width:



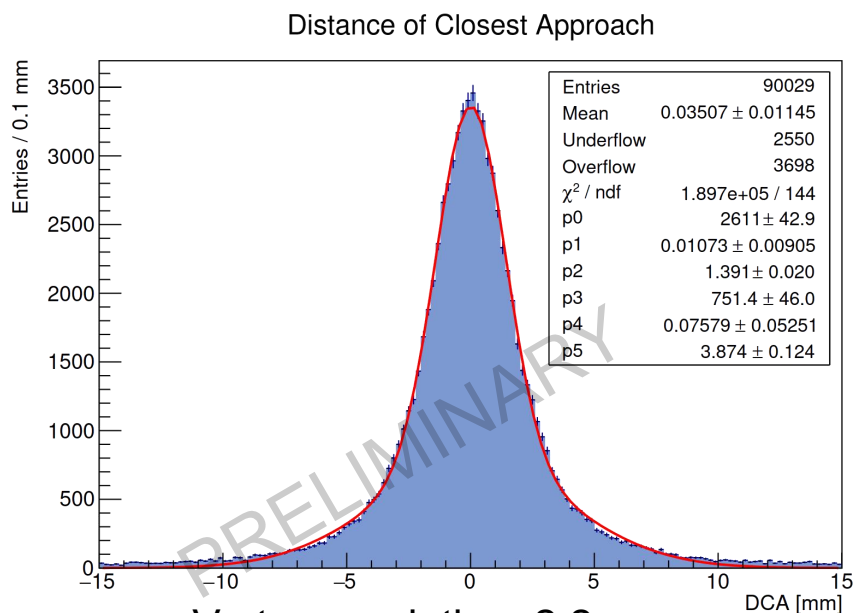
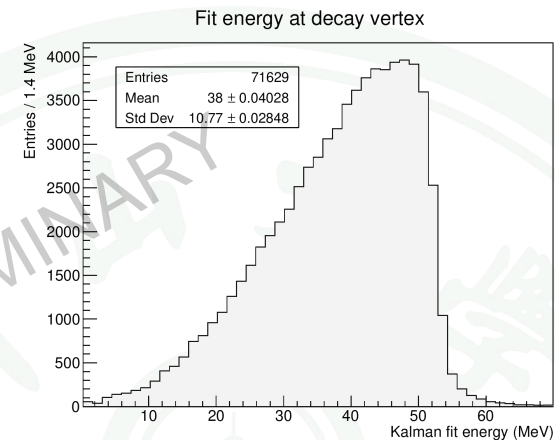
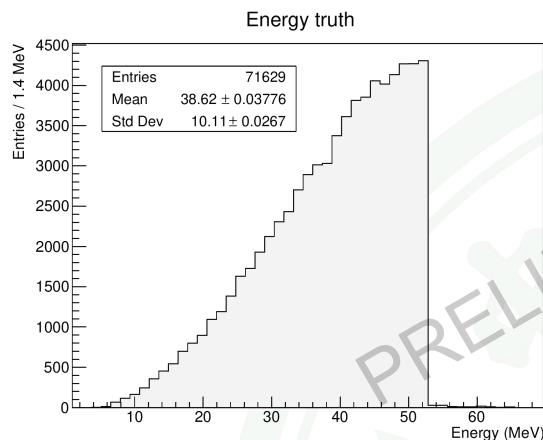
Distribution of drift distance



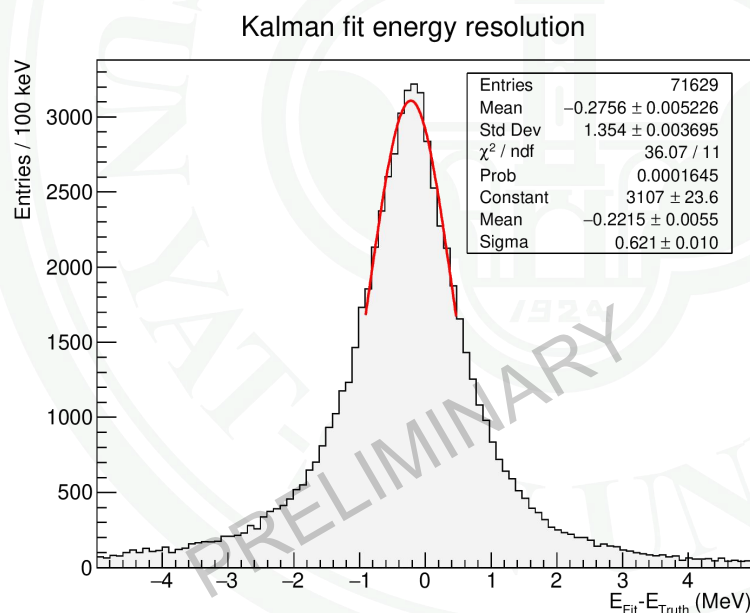
Distribution of hit rate

# Track Reconstruction in Spectrometer

- Kalman-filter-based track reconstruction has been performed, with 100 $\mu\text{m}$  drift distance resolution.
- The resolution of the drift chamber has improved compared with simple least  $\chi^2$ .



Vertex resolution: 2.2 mm  
(double gaussian fit std. dev.)



Momentum (energy) resolution:  $\sim 1.5$  MeV (FWHM)

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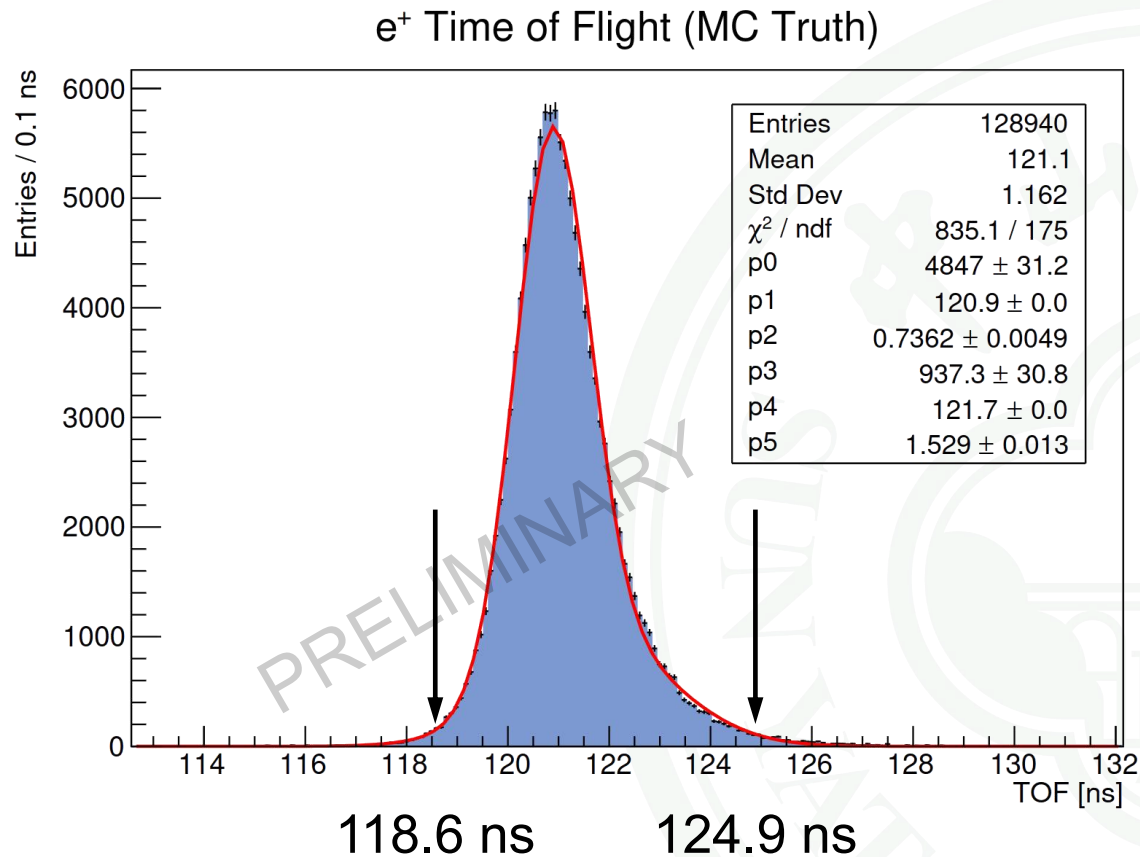


# Event Selection

- A antimuonium decay event is identified by coincident signals of spectrometer, MCP, and EMCal.
- Events are selected as follows:
  1. Find time coincident  $\gamma$  events ( $\geq 2$ ).
  2. Find time coincident  $e^-$  track:
    - Find time coincident drift chamber hits
    - Do track reconstructions
  3. Calculate the distance of closest approach (DCA) of  $e^-/e^+$  tracks.
  4. Calculate  $e^+$  time of flight (TOF) and difference between expected TOF.

Time window?

# Analysis: Time Aspect

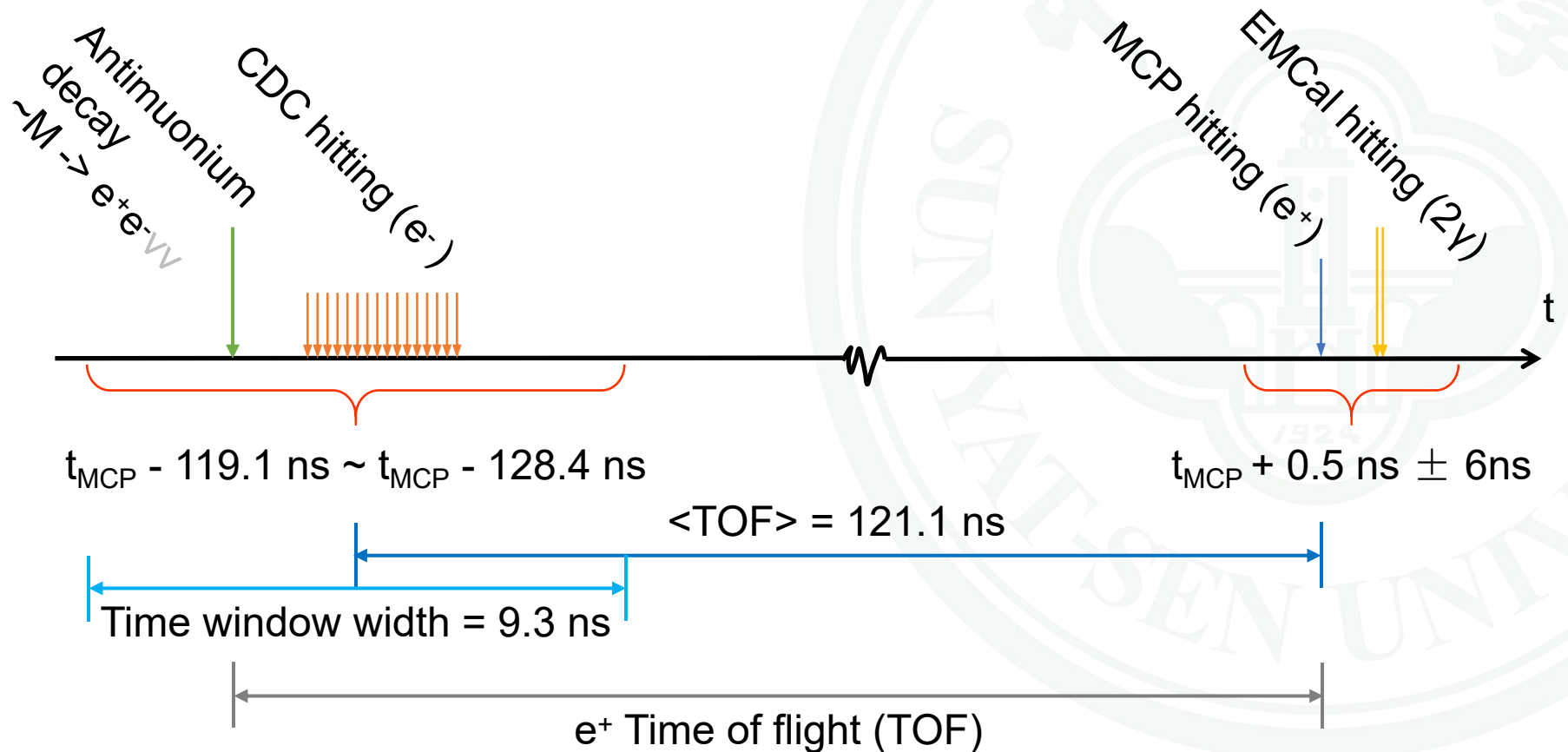


Add e<sup>-</sup> flight time from target to / inside the drift chamber: 0.5 ns / 3.5 ns,

Time window for drift chamber is  $t_{\text{MCP}} - 119.1 \text{ ns} \sim t_{\text{MCP}} - 128.4 \text{ ns}$ .

# Analysis: Time Aspect

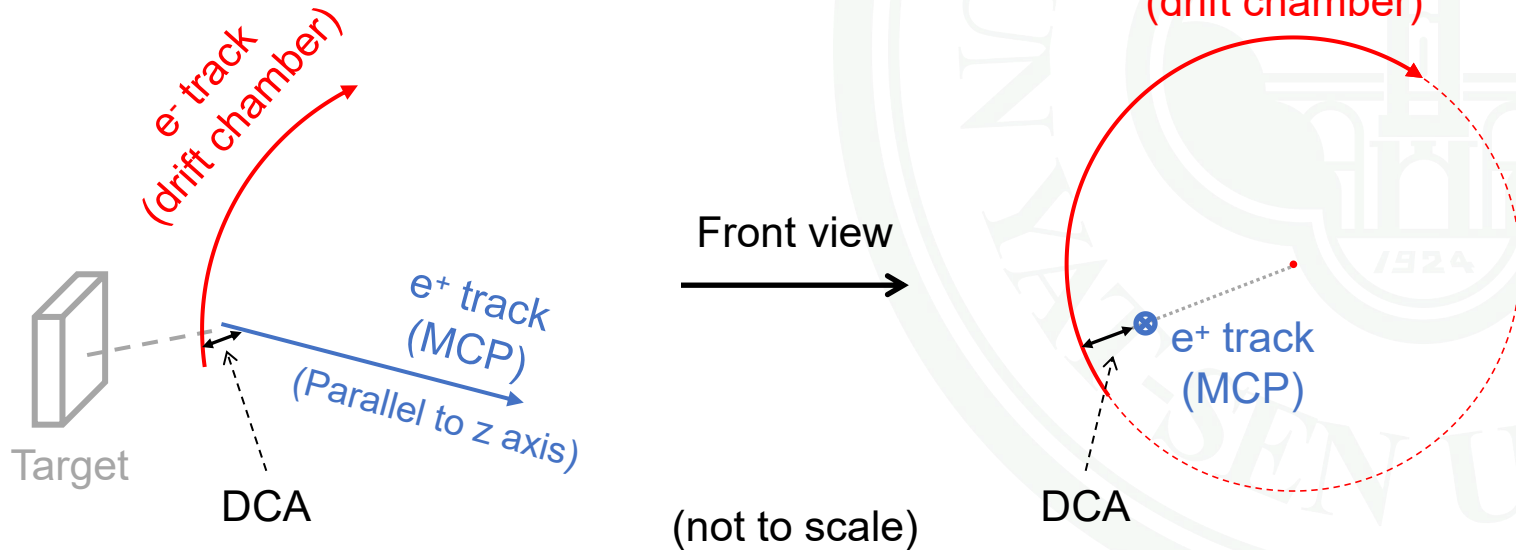
- Time resolution of the drift chamber (2 ns) and EMCal (4.5 ns) have been considered.
- Time window is determined by the simulated TOF spectrum.





# Analysis: Spatial Aspect

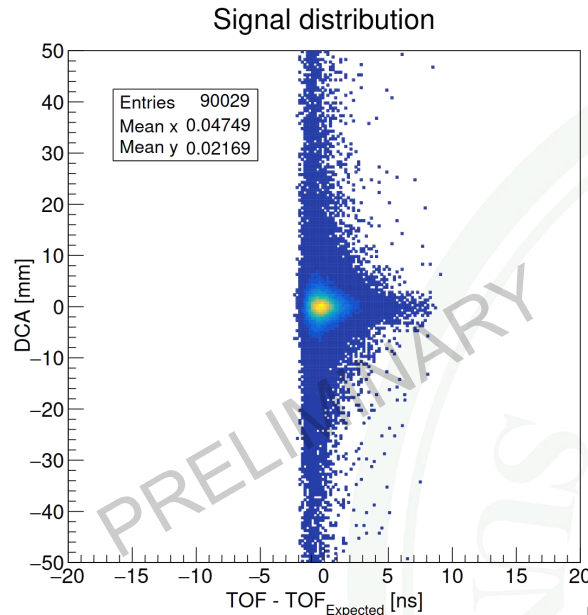
- Spatial resolution of the drift chamber cell ( $100\ \mu\text{m}$ ) has been considered.
- Fitted tracks are extrapolated toward the target by helixes.
- Closest distance between extrapolated tracks and low energy atomic  $e^+$  are calculated.



# Analysis Result

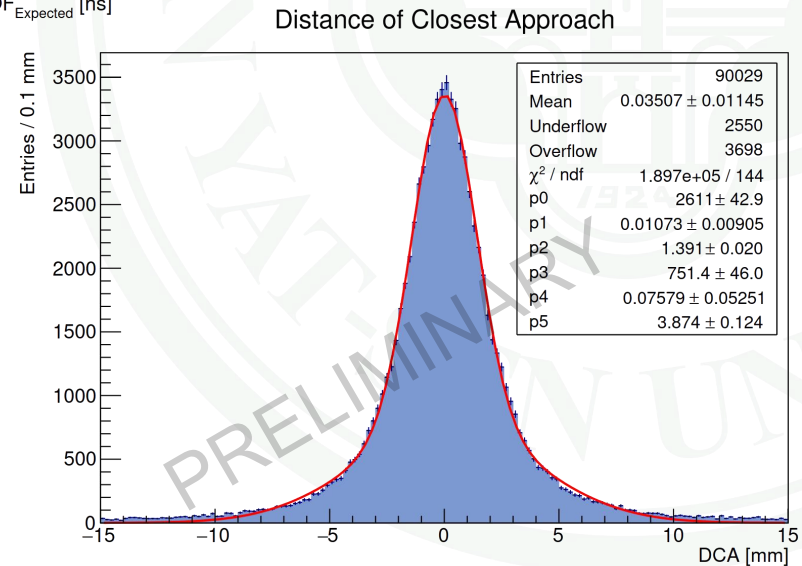
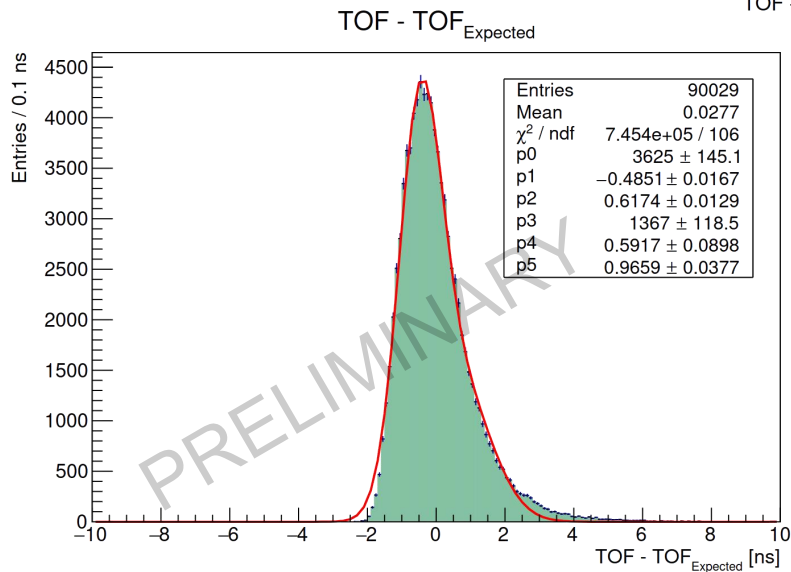
- Following the analysis procedure, the distribution of the signal can be obtained.

$$\sigma_{\Delta\text{TOF}} = 0.58 \text{ ns}$$



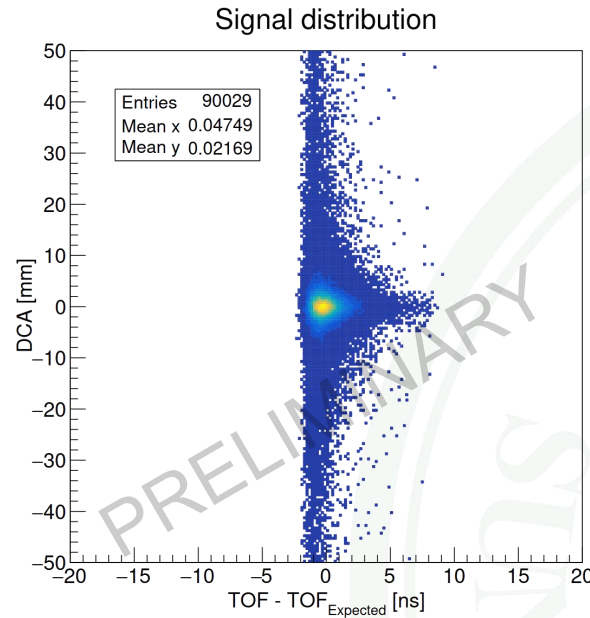
- Space-time resolution improved compared with the previous PSI experiment.

$$\sigma_{\text{DCA}} = 2.2 \text{ mm}$$

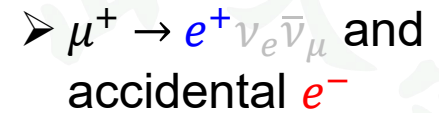


# Analysis Result

- Improved resolution -
- smaller signal region -
- lower background level expected.



- Backgrounds:



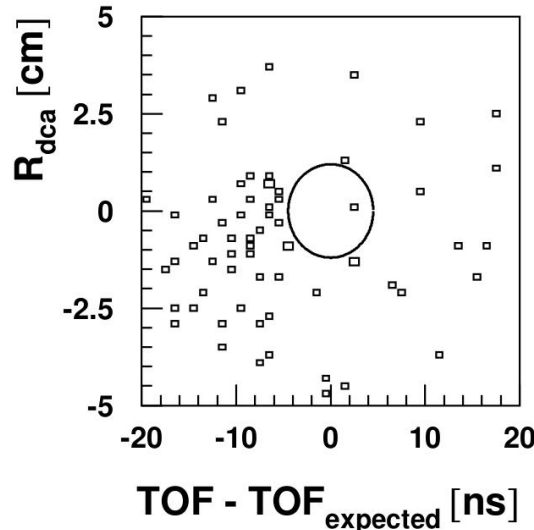
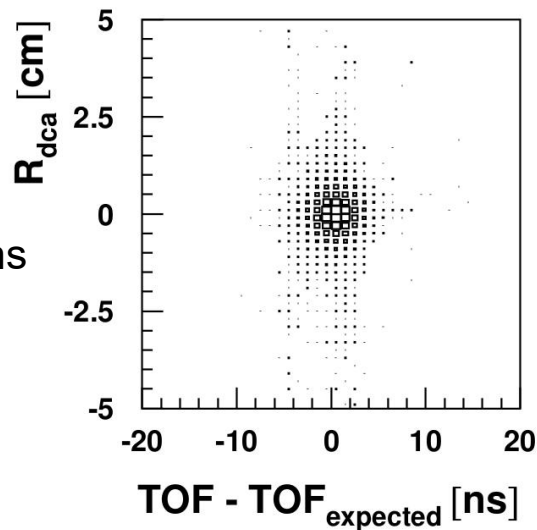
- Background analysis in progress.

$\sigma_{\Delta\text{TOF}} = 0.58 \text{ ns}$

$\sigma_{\text{DCA}} = 2.2 \text{ mm}$

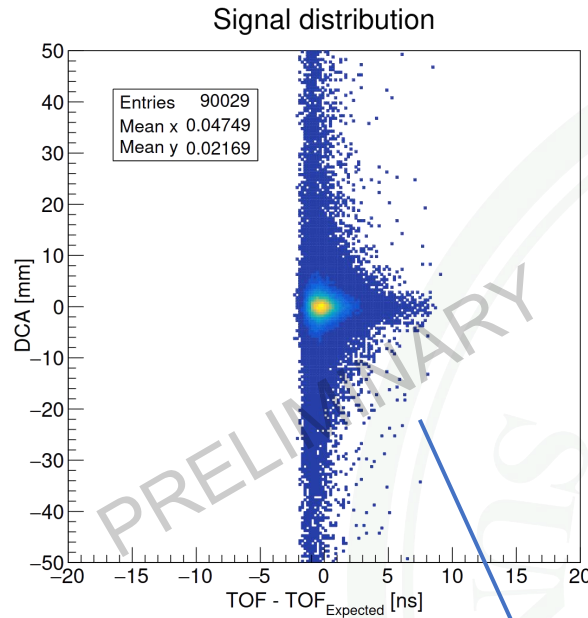
$\sigma_{\Delta\text{TOF}} = 1.5 \text{ ns}$

$\sigma_{\text{DCA}} = 4.0 \text{ mm}$

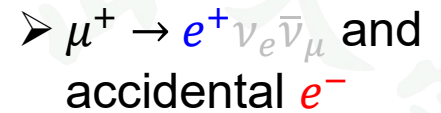


# Analysis Result

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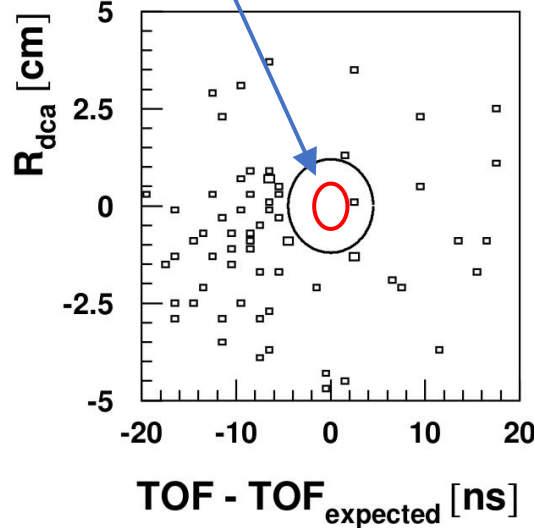
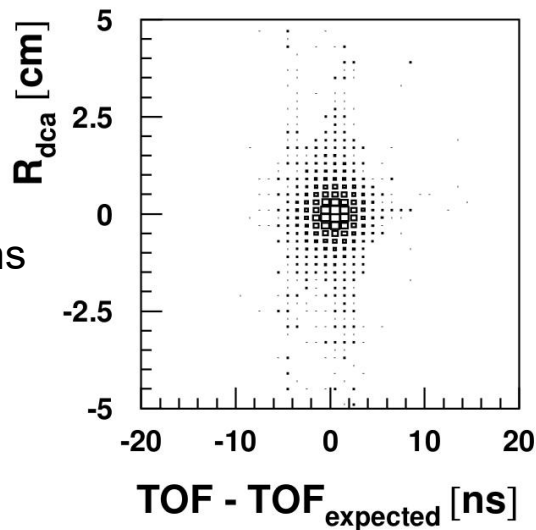
- Backgrounds:



- Background analysis in progress.

$\sigma_{\Delta\text{TOF}} = 0.58 \text{ ns}$

$\sigma_{\Delta\text{TOF}} = 1.5 \text{ ns}$



$\sigma_{\text{DCA}} = 2.2 \text{ mm}$

$\sigma_{\text{DCA}} = 4.0 \text{ mm}$

# Content

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- Motivation
- Conceptual Design of MACE
- Simulation Result
- **Summary**



# Summary

- MACE is the first proposed muonium-to-antimuonium conversion experiment since 1999, with the development of high-intensity muon beam and detector technology, the sensitivity is expected to enhance by more than two orders of magnitude.
  - Together with other flavor and collider searches, MACE will shed light on the mystery of the cLFV and new physics.
- Questions and comments welcome!
- Collaboration welcome!

The background features a large, light green watermark of the Zhejiang University logo. The logo is circular and contains the university's name in Chinese characters '浙江大学' at the top and 'ZHEJIANG UNIVERSITY' at the bottom. In the center of the logo is a depiction of a building with a clock tower, and the year '1924' is inscribed at the bottom of the central emblem. Two dark green rectangular shapes are positioned on the left and right sides of the slide, partially overlapping the watermark.

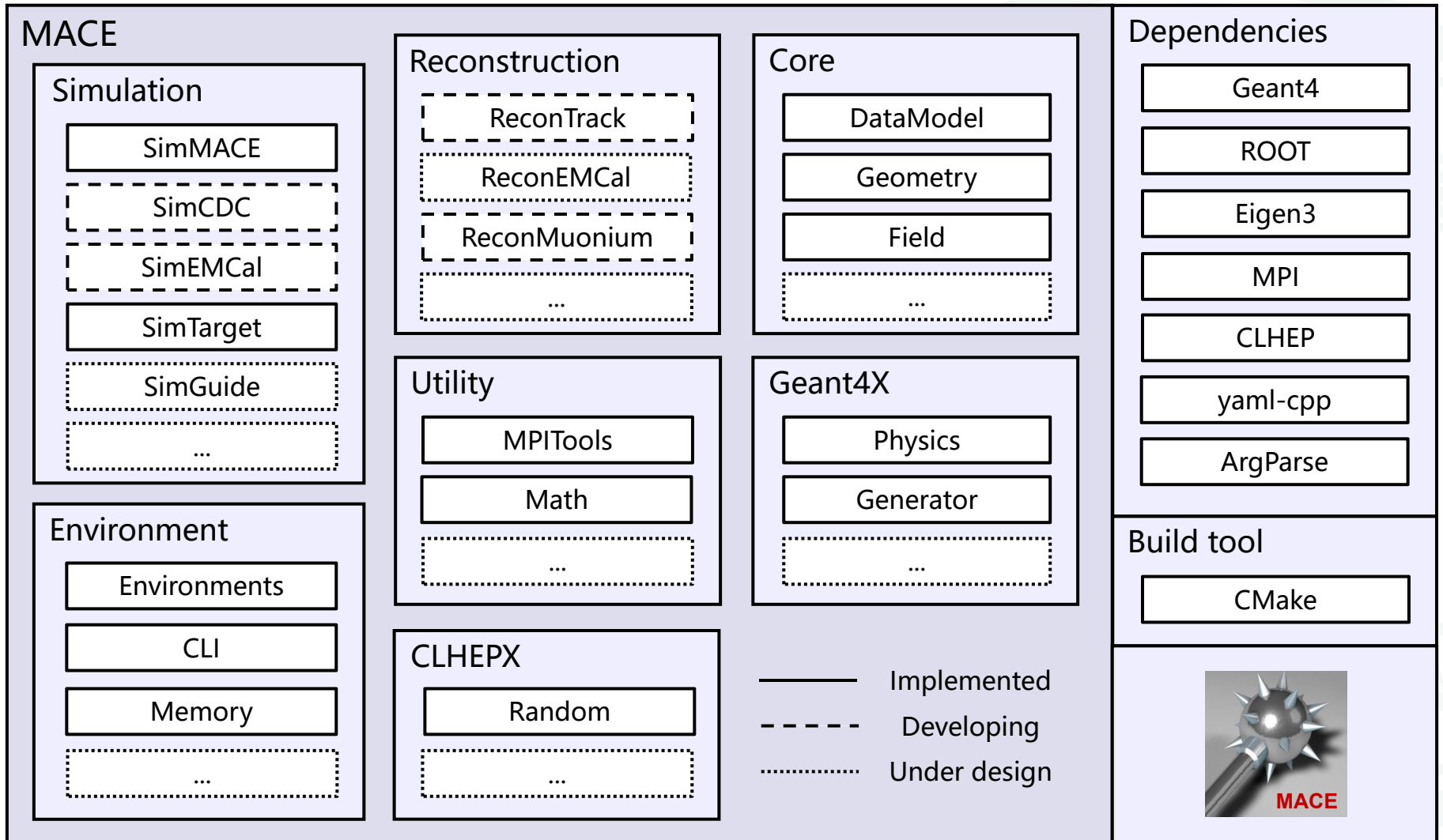
THANK YOU

Backup





# MACE Offline Software



# MACE Offline Software

- MACE offline software: designed for experiment R&D, simulation, and offline reconstruction.
- The software framework has been established, including / allowing:
  - Simulation of the experiment / detectors
  - Large-scale parallel computing with MPI on supercomputer
  - Data model and data I/O
  - Geometry and material interface
  - Detector parameters management and I/O
  - ...
- Designed and programmed with C++ best practice and pattern - design and develop for future.
- Currently, main tasks:
  - Develop offline analysis module.
  - Refine physics processes.
  - Improve and APIs and UIs.