

# Quantum Computing at DESY and the LUXE Experiment

With special focus on arXiv: [2304.01690](https://arxiv.org/abs/2304.01690)

Quantum algorithms for charged particle track  
reconstruction in the LUXE experiment

Arianna Crippa<sup>1,2</sup>, Lena Funcke<sup>3,4</sup>, Tobias Hartung<sup>5</sup>, Beate  
Heinemann<sup>6,7</sup>, Karl Jansen<sup>1,8</sup>, Annabel Kropf<sup>6,7</sup>, Stefan Kühn<sup>1,8</sup>,  
Federico Meloni<sup>6</sup>, David Spataro<sup>6,7</sup>, Cenk Tüysüz<sup>1,2</sup> and Yee Chinn  
Yap<sup>6</sup>

<sup>1</sup> Deutsches Elektronen-Synchrotron DESY, Platanenallee 6, 15738 Zeuthen, Germany

<sup>2</sup> Institut für Physik, Humboldt-Universität zu Berlin, Newtonstr. 15, 12489 Berlin, Germany

<sup>3</sup> Transdisciplinary Research Area “Building Blocks of Matter and Fundamental Interactions”  
(TRA Matter) and Helmholtz Institute for Radiation and Nuclear Physics (HISKP),  
University of Bonn, Nußallee 14-16, 53115 Bonn, Germany

<sup>4</sup> Center for Theoretical Physics, Co-Design Center for Quantum Advantage, and NSF AI  
Institute for Artificial Intelligence and Fundamental Interactions, Massachusetts Institute of  
Technology, 77 Massachusetts Avenue, Cambridge, MA 02139, USA

<sup>5</sup> Northeastern University - London, Devon House, St Katharine Docks, London, E1W 1LP,  
United Kingdom

<sup>6</sup> Deutsches Elektronen-Synchrotron DESY, Notkestr. 85, 22607 Hamburg, Germany

<sup>7</sup> Physikalisches Institut, Albert-Ludwigs-Universität Freiburg, Hermann-Herder-Str. 3a,  
79104 Freiburg, Germany

<sup>8</sup> Computation-Based Science and Technology Research Center, The Cyprus Institute, 20  
Kavafi Street, 2121 Nicosia, Cyprus

Federico Meloni (DESY)

World Quantum Day 2023



# From general methods...

## Increase the reliability of Quantum Computing Calculations

**DESY has a rich (and expanding) set of quantum computing activities**

### Error Mitigation in VQS

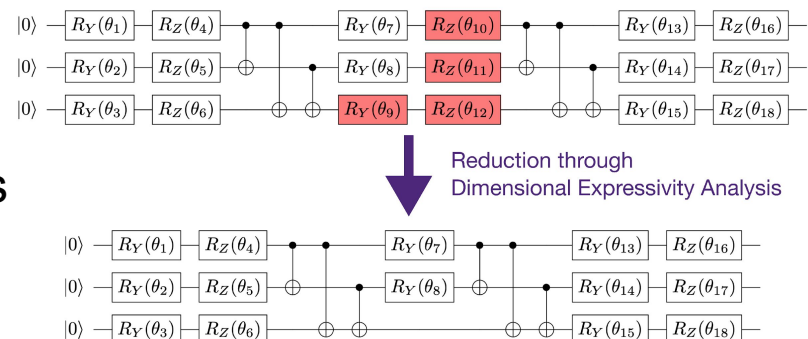
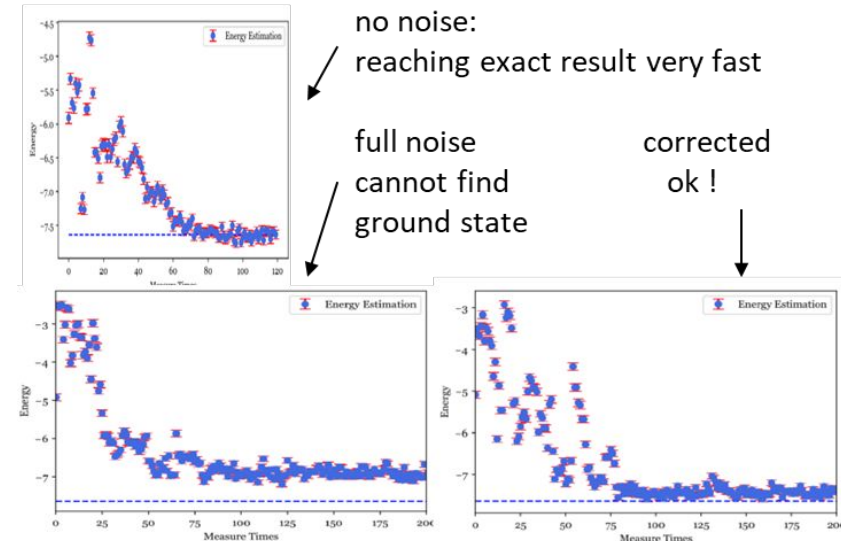
1-Dimensional Heisenberg model

- Very sensitive to QC noise
- Developed error mitigation methods

### Optimization of Dimensional Expressivity of a Quantum Circuit

- Dimensional Expressivity Analysis
- Generate as many/complicated states as possible as little gates as possible

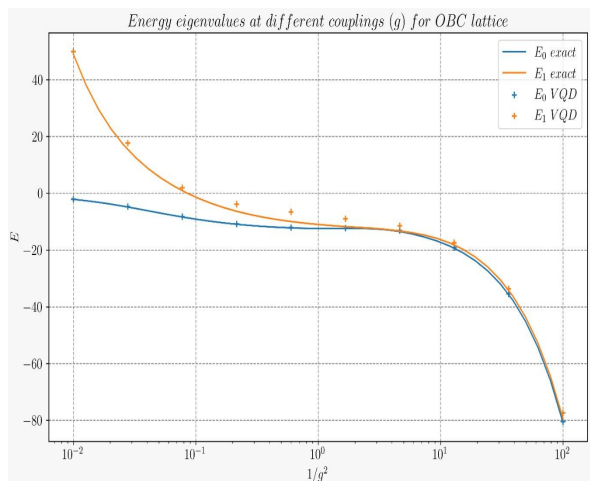
$$H = \sum_{i=1}^N \beta [\sigma_x(i)\sigma_x(i+1) + \sigma_y(i)\sigma_y(i+1) + \sigma_z(i)\sigma_z(i+1)] + J\sigma_z(i)$$



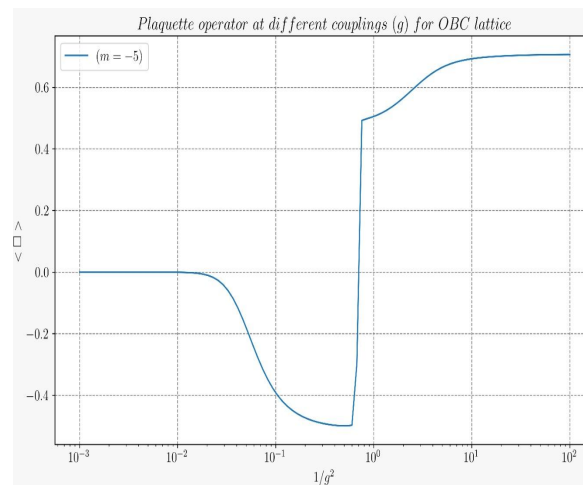
# ... to theory and applications

From QED in 2+1 dimensions to simulations for HEP

## Variational Quantum Simulations (VQCS) for QED



Particle Mass  
 $\Delta = E_1 - E_0$

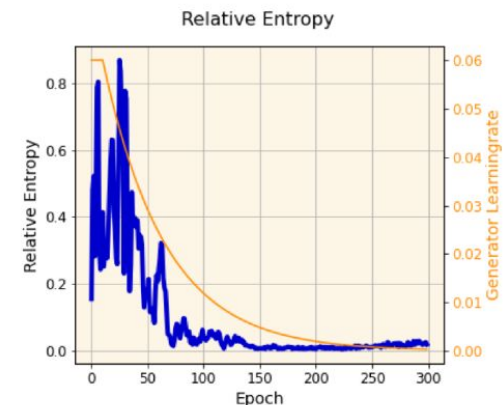
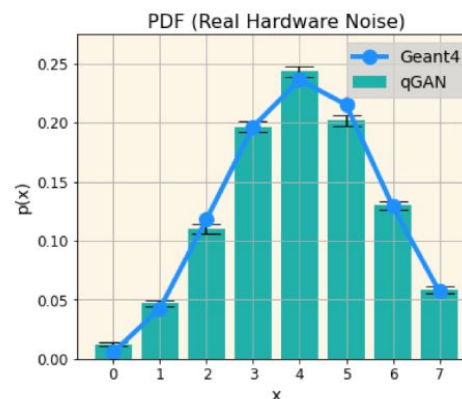


Detecting a phase transition at negative mass

- **not possible with MC methods**

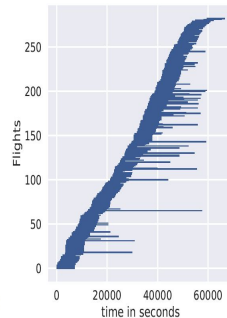
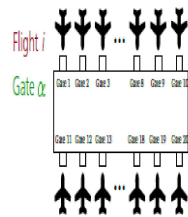
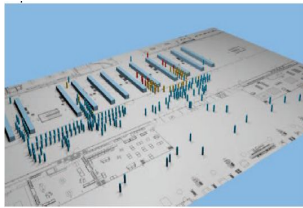
## Methods and Quantum Machine Learning applications

- Robust against noise
- Q-GAN simulations for detectors at High-Luminosity LHC



# Classical optimization problems

## From logistics to particle tracking

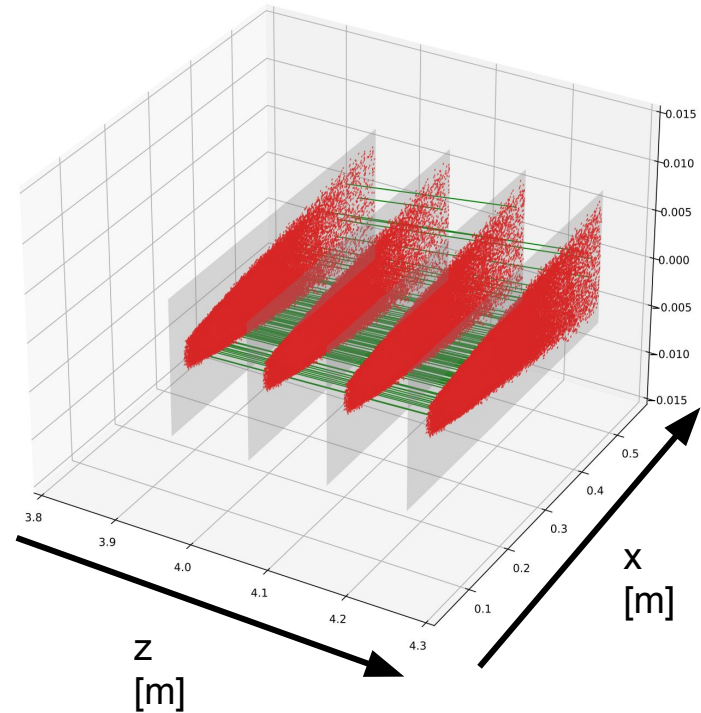


$$H = \sum_{j=1}^n Q_{jj} \sigma_j^z + \sum_{\substack{j,k=1 \\ j < k}}^n Q_{jk} \sigma_j^z \otimes \sigma_k^z$$

### Flight Gate Assignment

find lowest energy  $\Leftrightarrow$  shortest path

- Same mathematics for problems in traffic, logistics, aerospace, ...



### Particle tracking

We only observe particles through their interaction with detectors

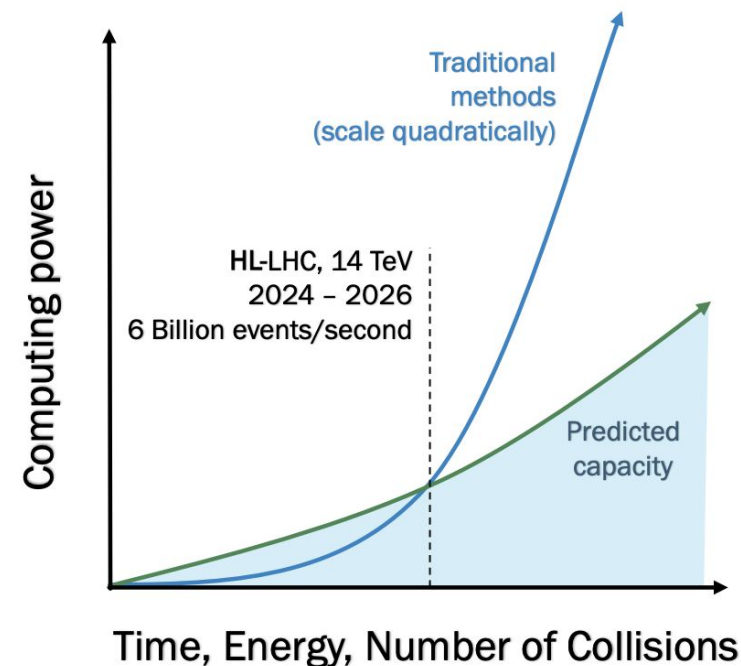
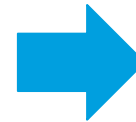
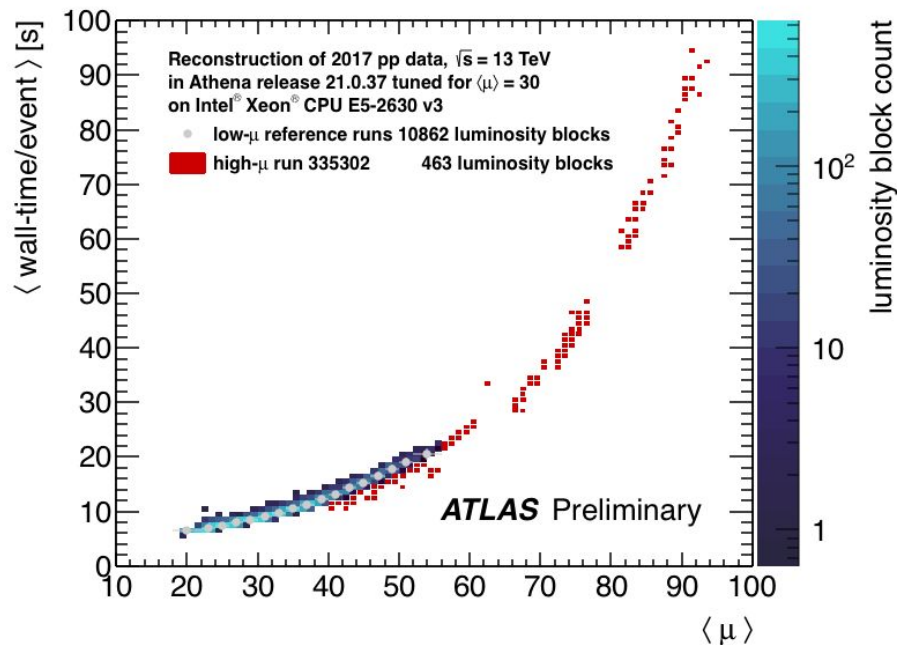
- Need to single out each particle's trajectory from a cloud of hits

# Why study quantum algorithms for tracking?

Tracking is a **hard combinatorial problem**

The CPU needs of HEP will keep growing in the coming years

- We are looking for efficient algorithms and technologies to go forward



Sketch credit: X. Ju, S. Murnane



# The LUXE experiment



**LUXE**

LUXE is a new experiment at DESY and Eu.XFEL

- Collisions of electron beam and a high-power laser
- **First time study non-perturbative QED**

The extreme dynamic range  
( $10^{-4}$  -  $10^6$  particles per event)  
makes LUXE a **good case study**  
**for other colliders**

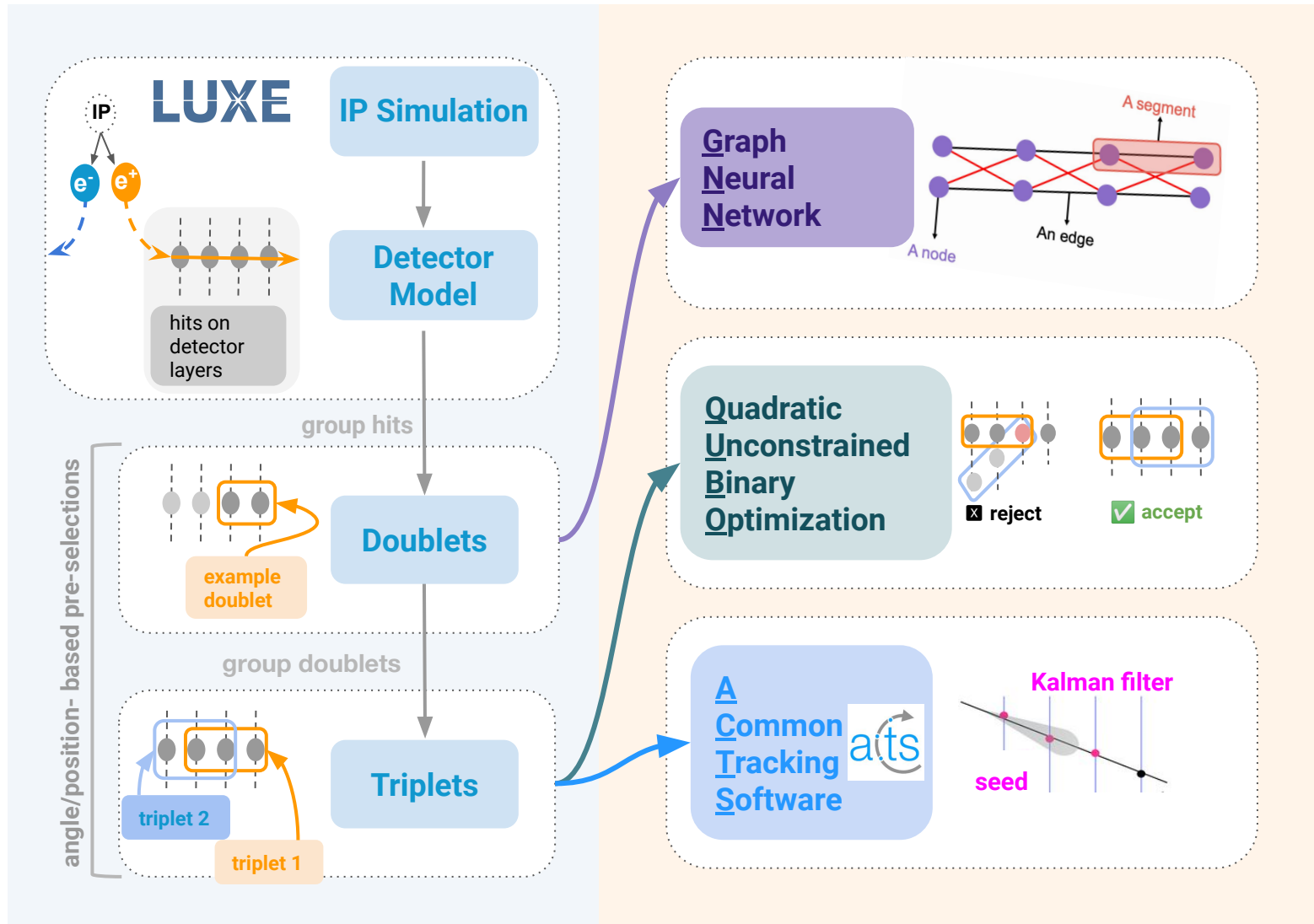
**LUXE (worst case) = 100 hits/mm<sup>2</sup>**

[2303.08533](#)

Detector Reference	Hit Density [mm <sup>-2</sup> ]		
	MCD	ATLAS ITk	ALICE ITS3
Pixel Layer 0	3.68	0.643	0.85
Pixel Layer 1	0.51	0.022	0.51

# Track reconstruction

## Comparing different approaches

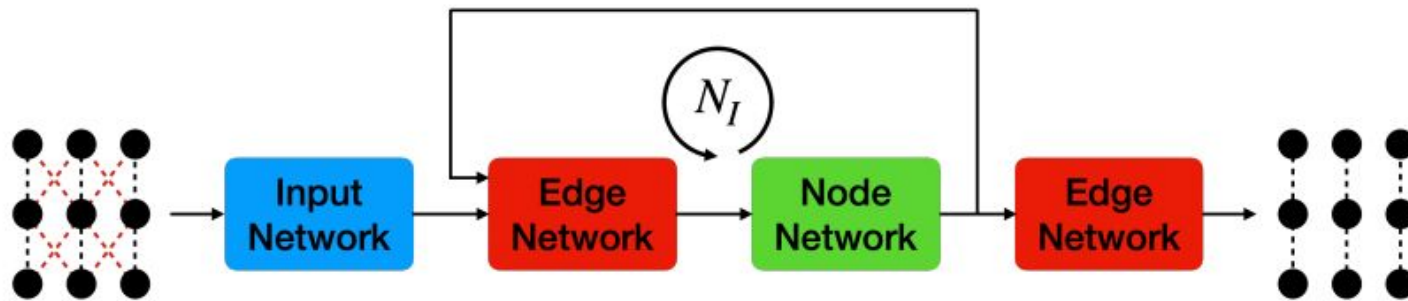


Hep.TrkX  
1810.06111  
Exa.TrkX  
2103.06995  
Q.TrkX  
2109.12636

1902.08324  
2202.06874  
2304.01690

ACTS  
2106.13593

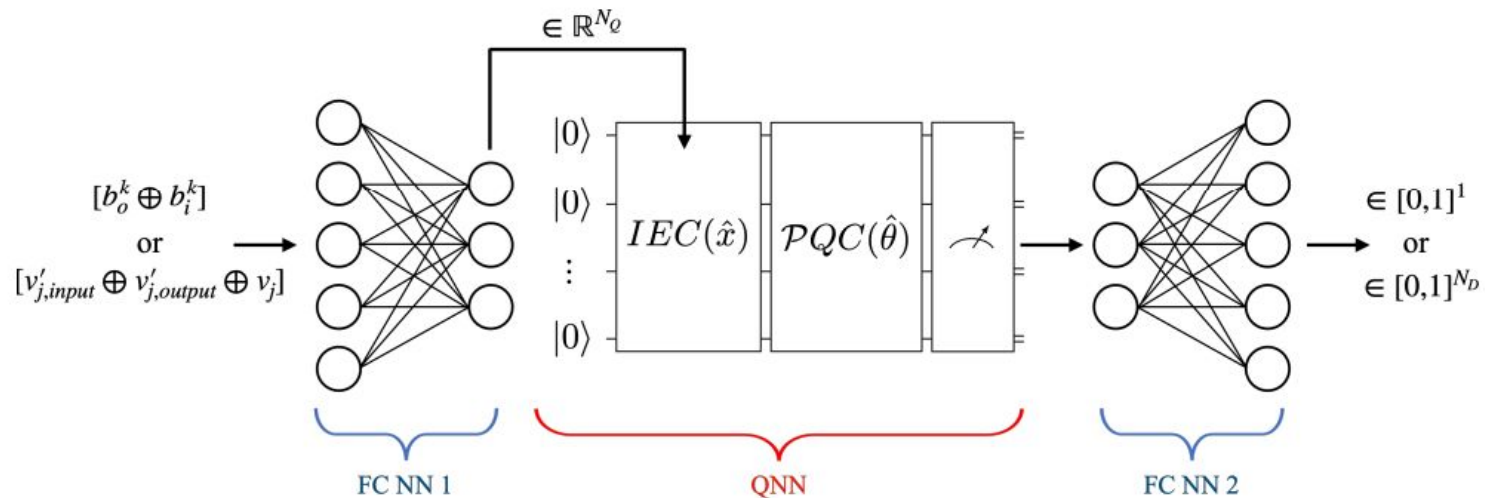
# Quantum Graph Neural Network



Input network encodes information (10 hidden features)

Edge and node nets applied 4 times (as many as the tracker layers)

Retain edges with scores above fixed threshold





# Quadratic Unconstrained Binary Optimisation

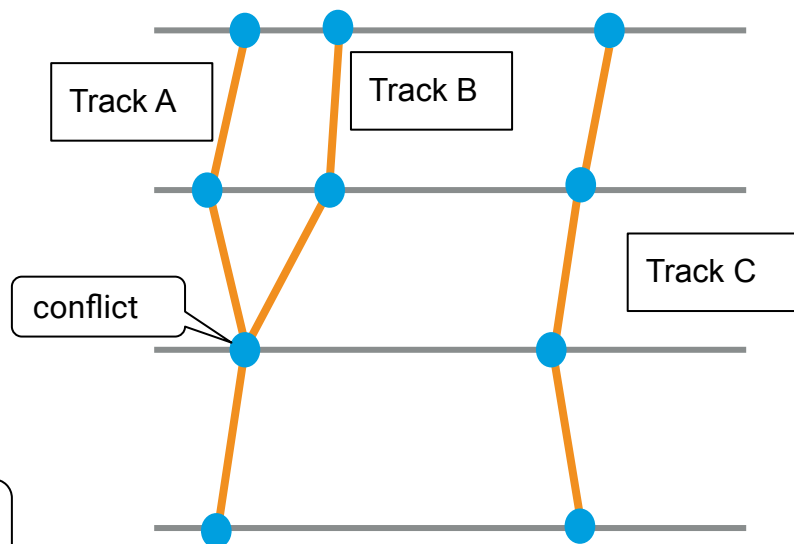
Each triplet is represented as a binary quantity  $T_i, T_j \in \{0, 1\}$

**Minimising an objective function equals to finding the optimal solution**

The selected  $T_i$  are used to form tracks

$$O = \sum_i^N \sum_{j < i} b_{ij} T_i T_j + \sum_{i=1}^N a_i T_i$$

"connection term"
"quality term"



$$b_{ij} = \begin{cases} 0, & \text{if no shared hit} \\ +1, & \text{if in conflict} \\ -S(T_i, T_j) & \text{if forming a track} \end{cases}$$

O can be mapped to an Ising Hamiltonian and evaluated with a quantum computer

$$T_i \rightarrow (1 + Z_i)/2$$

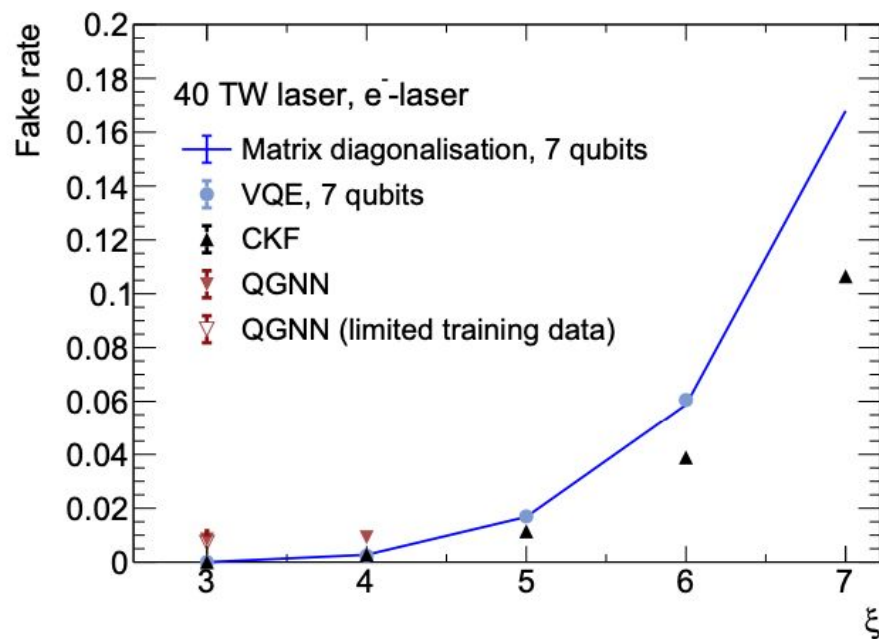
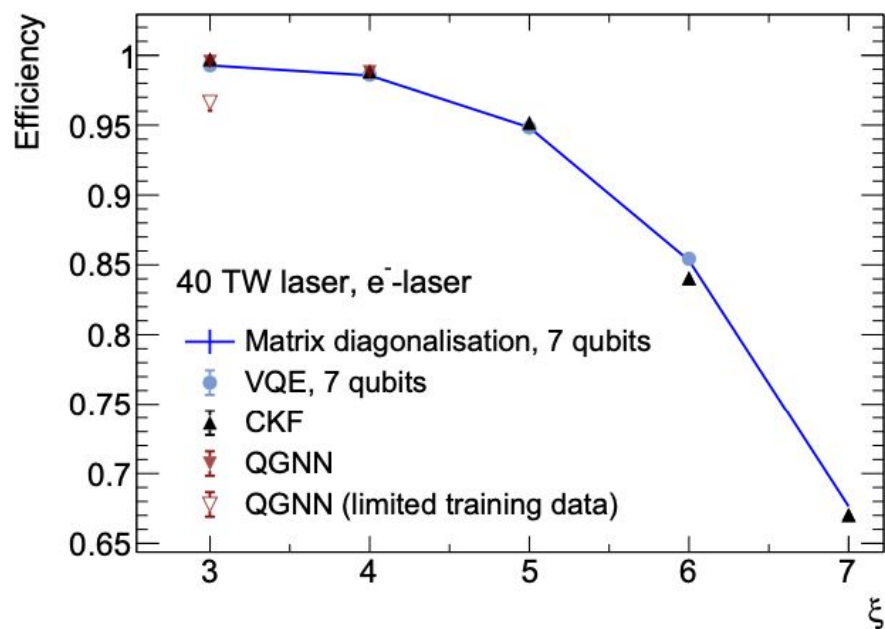
**Find ground state with VQE!**

# Algorithmic performance

Based on ideal classical simulations of quantum circuits

$$\text{Efficiency} = \frac{N_{\text{matched tracks}}}{N_{\text{generated tracks}}}$$

$$\text{Fake rate} = \frac{N_{\text{fake tracks}}}{N_{\text{reconstructed tracks}}}$$



**Excellent performance, in line with state-of-the-art classical tracking**

- Quantum algorithms have higher efficiency but ~2x fakes

Not all methods available for each value of  $\xi$  (due to computational limitations)

Performed also tests with quantum hardware (ibm\_nairobi)

# Summary

LUXE will probe a new regime of quantum physics!

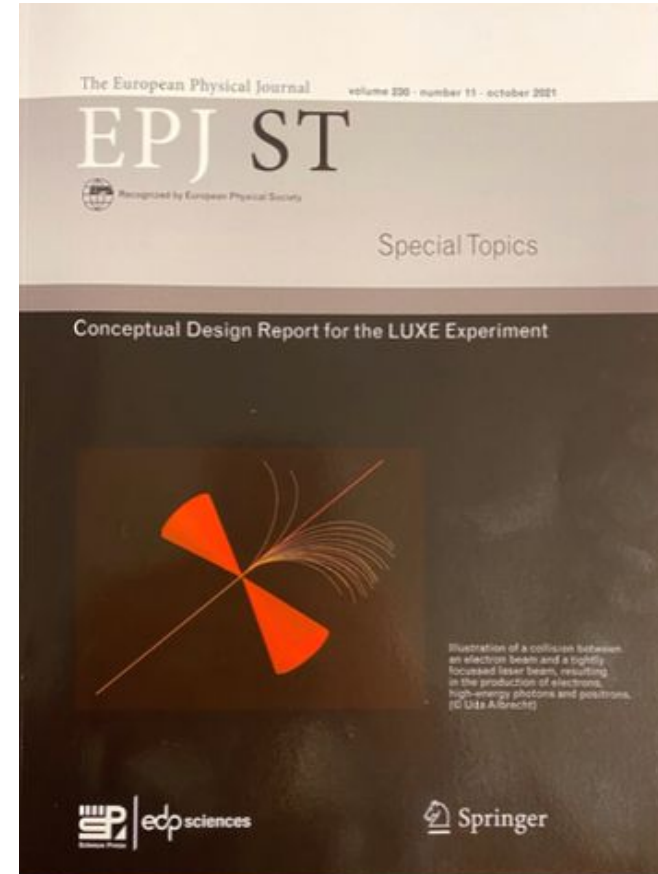
- Huge particle rate range allows to develop and test new reconstruction algorithms

Demonstrated the feasibility of tracking using quantum algorithms

- Similar performance as classical tracking

Next: optimise for larger and real devices

Plenty of space to experiment with new ideas!

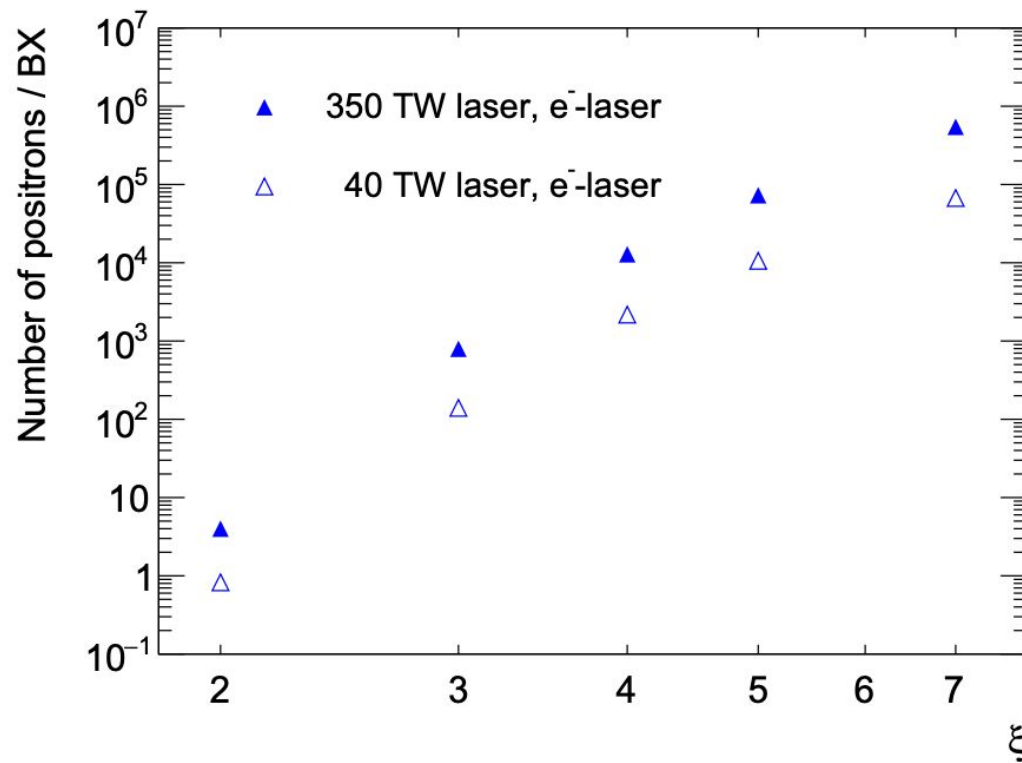
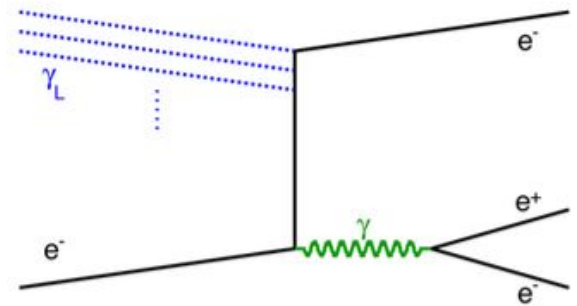


2102.02032

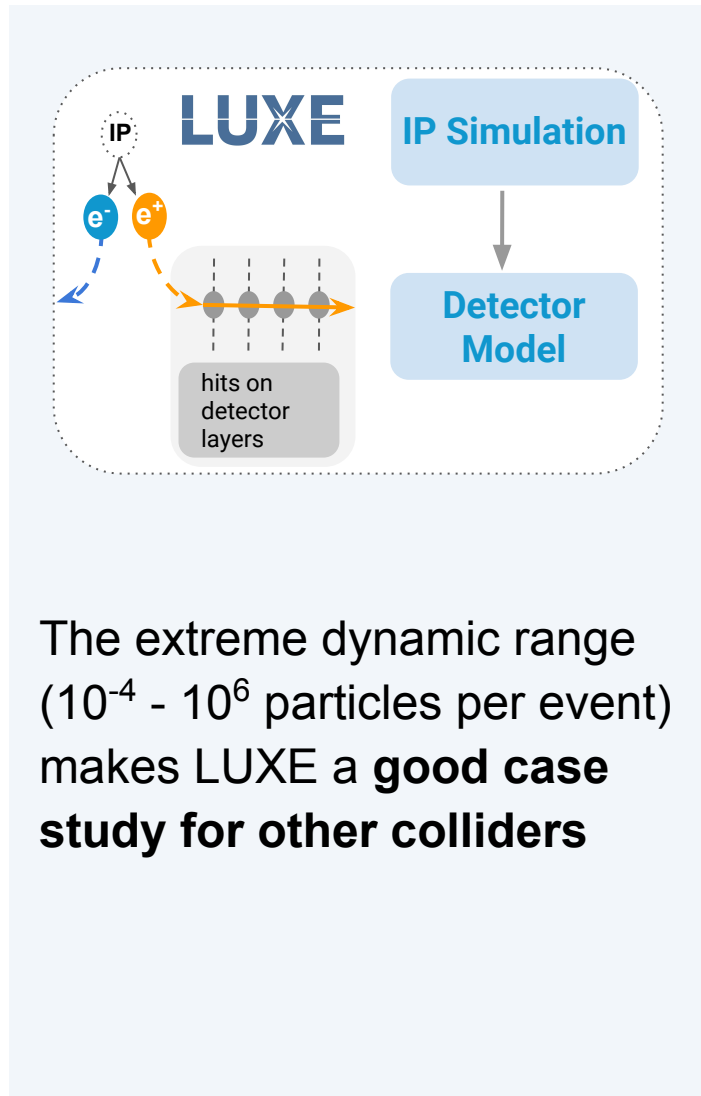
**Thank you!**

# Key observable

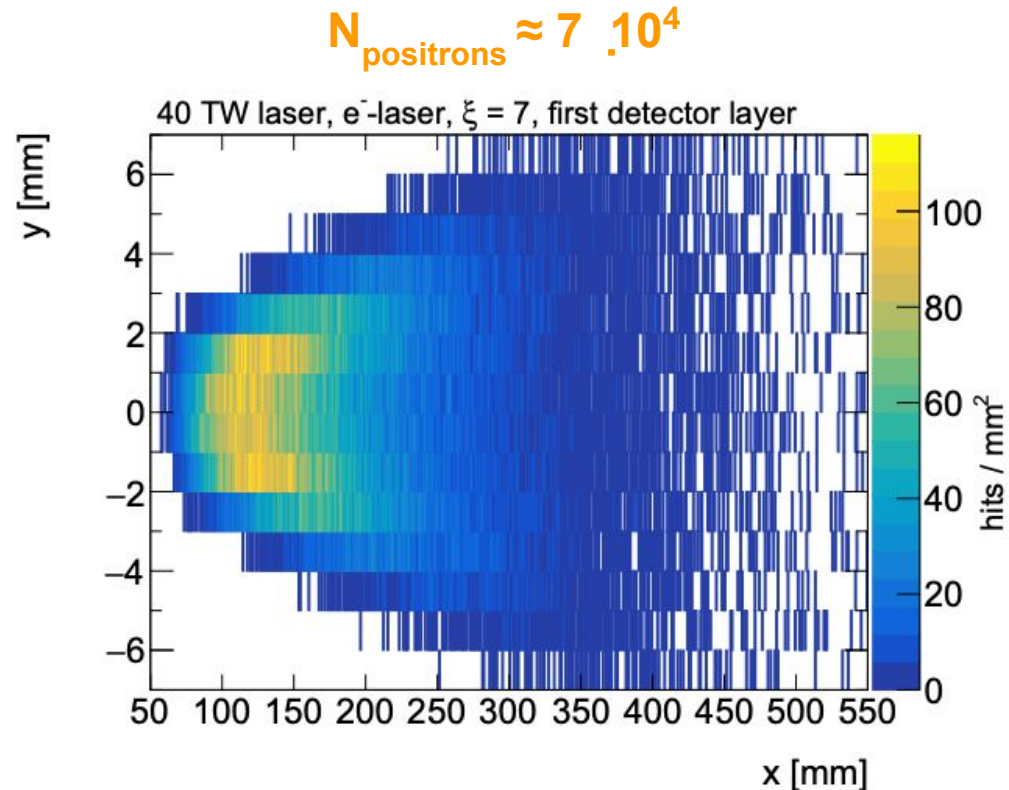
$$e^- + n\gamma_L \rightarrow e^- + e^+ + e^-$$



# LUXE as test-case for other trackers



The extreme dynamic range ( $10^{-4} - 10^6$  particles per event) makes LUXE a **good case study for other colliders**



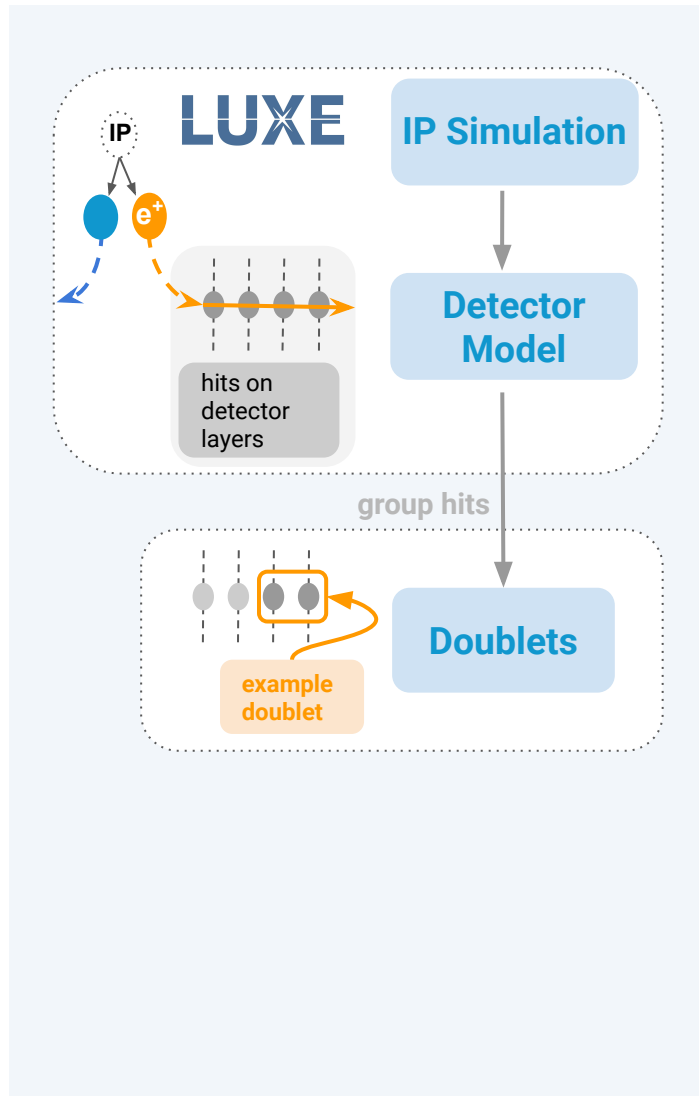
[2303.08533](#)

Detector Reference	Hit Density [mm <sup>-2</sup> ]		
	MCD	ATLAS ITk	ALICE ITS3
Pixel Layer 0	3.68	0.643	0.85
Pixel Layer 1	0.51	0.022	0.51

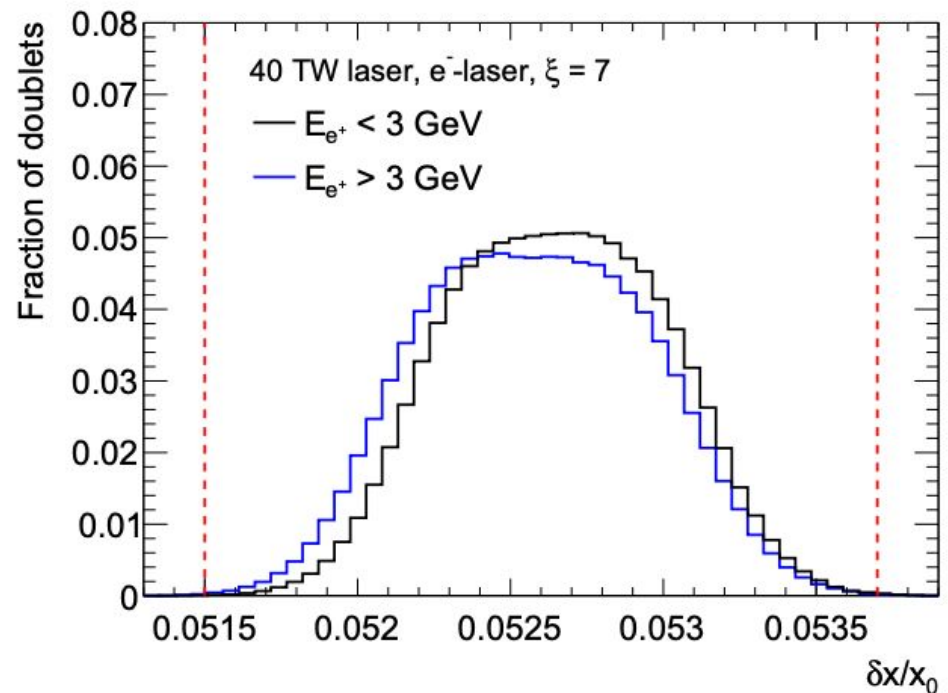


# Track reconstruction

## Selecting the inputs

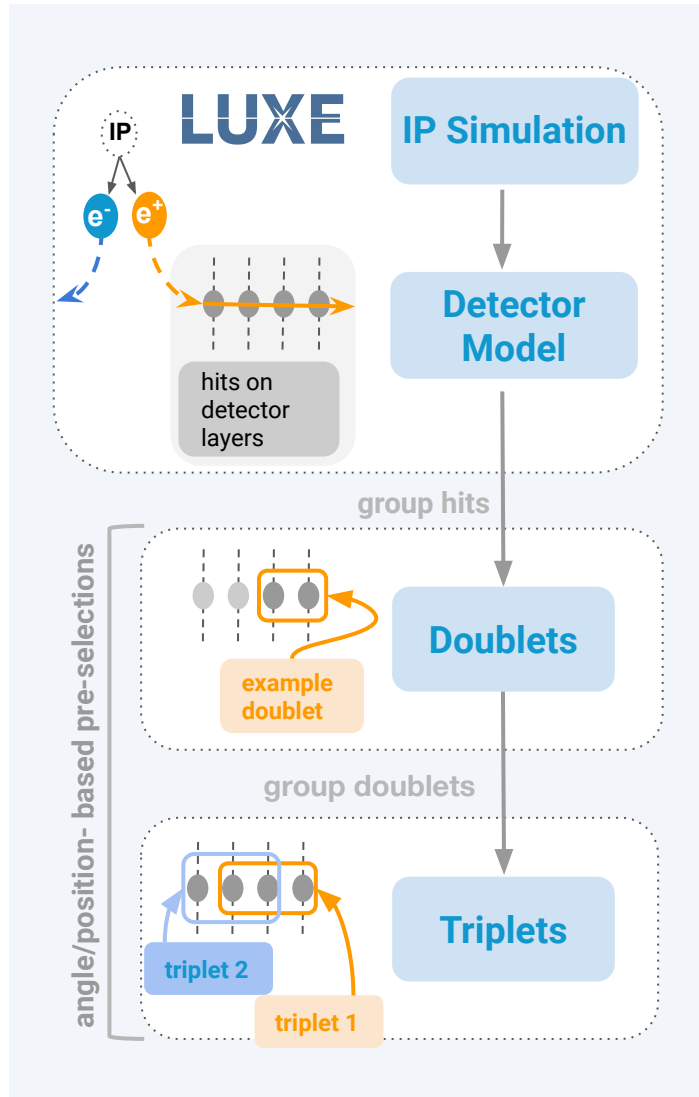


Select doublets based on the ratio  $\delta x/x_0$  where  $\delta x = x_{i+1} - x_i$ , while  $x_0$  indicates the  $x_i$  on the detector layer closest to the IP.



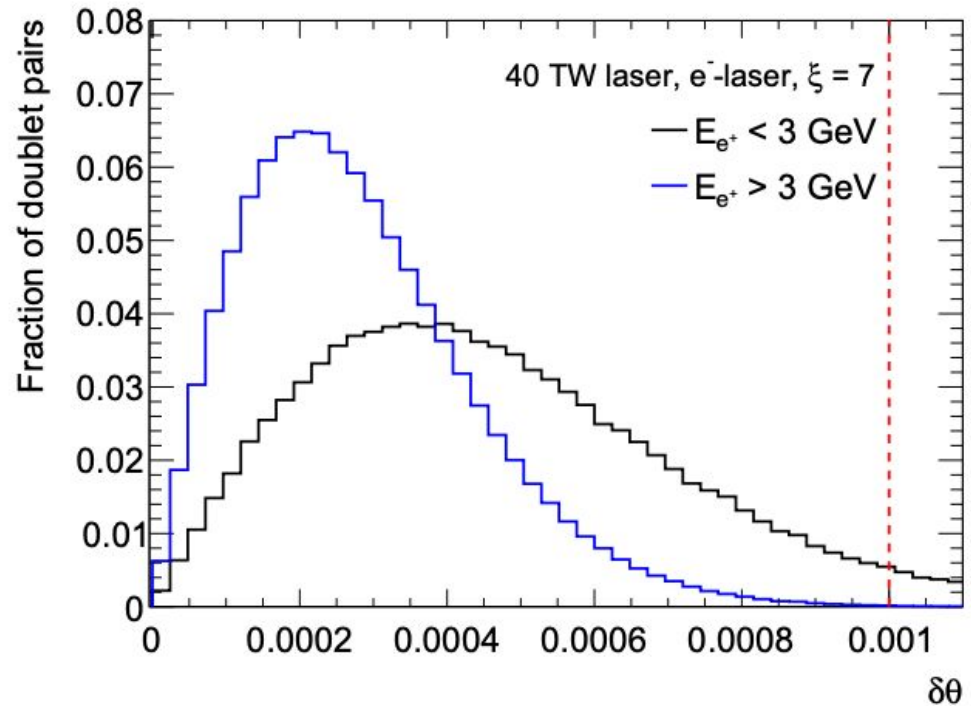
# Track reconstruction

## Selecting the inputs



Select triplets based on the alignment of the constituent doublets

- maximum angle difference  $\delta\theta < 1$  mrad



# Performance

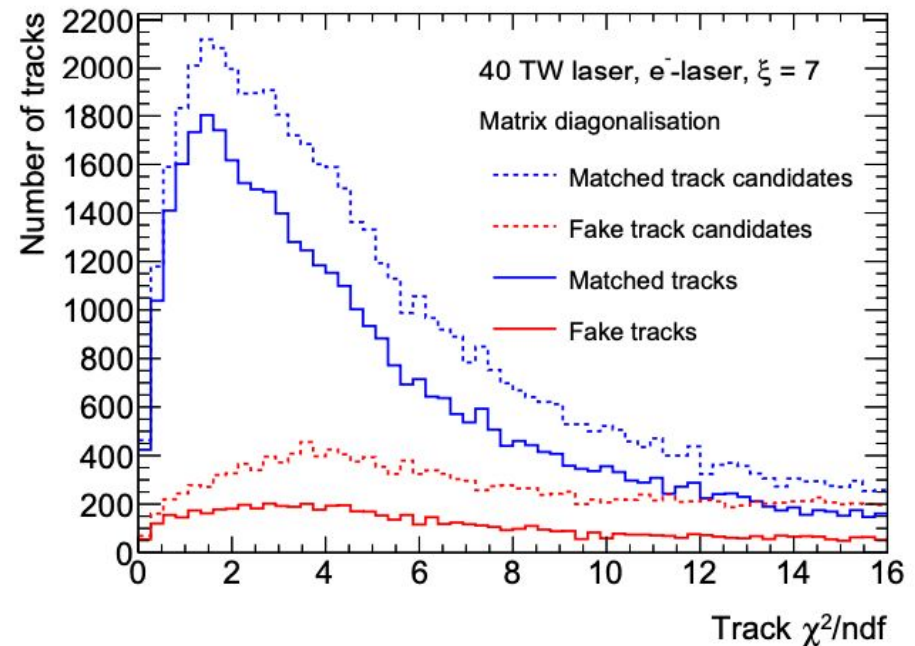
## Track level efficiency and fake rate

The output track candidates from the three methods are fitted

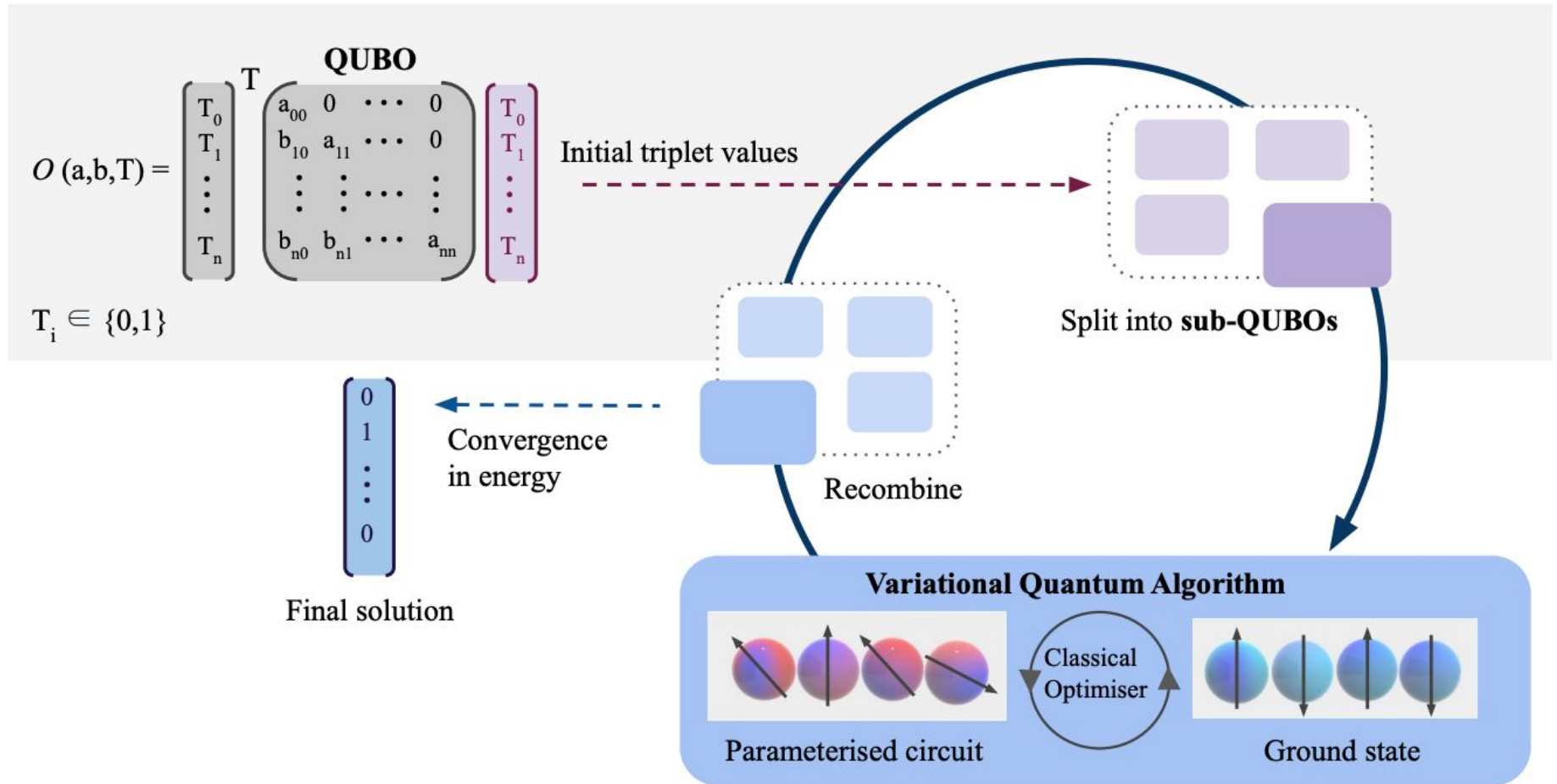
- Track  $\chi^2$  only considered in removal of reconstruction ambiguities

$$\text{Efficiency} = \frac{N_{\text{matched tracks}}}{N_{\text{generated tracks}}}$$

$$\text{Fake rate} = \frac{N_{\text{fake tracks}}}{N_{\text{reconstructed tracks}}}$$



# Variational Quantum Eigensolver



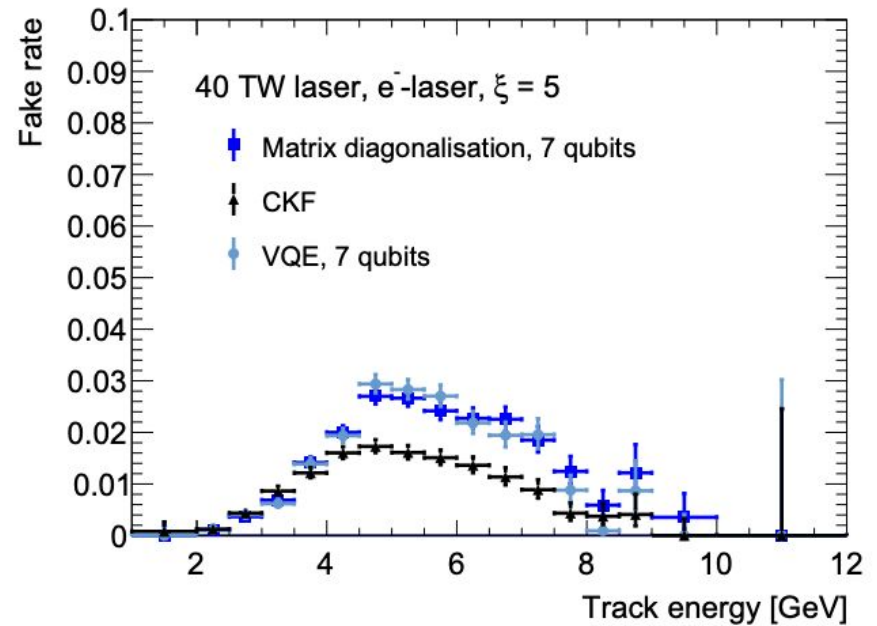
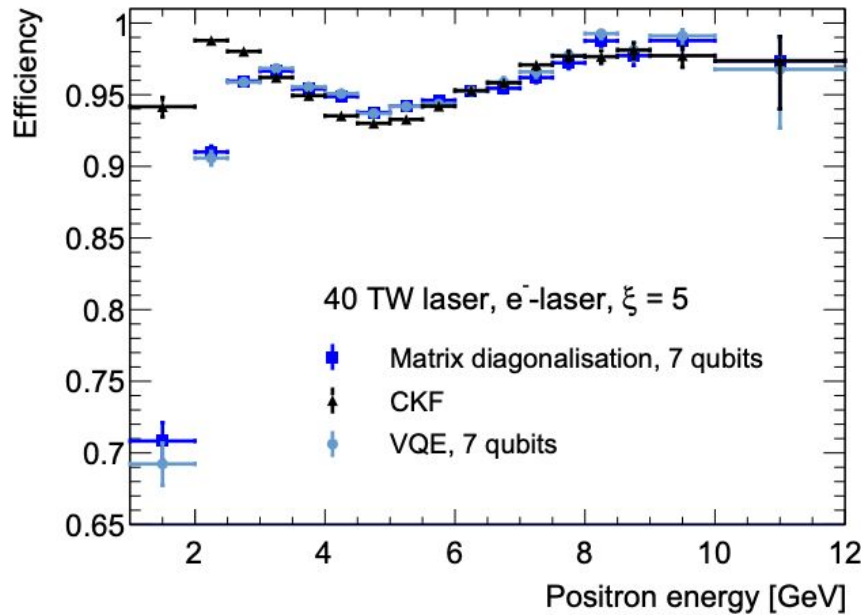
Exact matrix diagonalisation  
used as benchmark

# Algorithmic performance

## Differential efficiency and fake rate

$$\text{Efficiency} = \frac{N_{\text{matched tracks}}}{N_{\text{generated tracks}}}$$

$$\text{Fake rate} = \frac{N_{\text{fake tracks}}}{N_{\text{reconstructed tracks}}}$$



Similar performances across methods

- Difference is maximal in high-density region
- QGNN missing because of choice of  $\xi = 5$

# Tests with quantum hardware

## Tested performance on 7-qubit device (ibm\_nairobi)

Additional complications arising from gate noise, quantum decoherence, readout and state preparation errors

- Adopted calibration matrix-based readout error mitigation

Results relatively stable

- Minimum 10 shots to find correct result

