

#### CLUSTER OF EXCELLENCE QUANTUM UNIVERSE





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Dark Matter Phenomenology in Z'<sub>2</sub> broken Two Higgs Doublet Model with Complex Singlet Extension



#### Extend SM → Two Higgs Doublet Model with Complex Singlet (2HDMS)



## **2HDMS Higgs Sector Potential**

[Notation as in: Baum and Shah, arXiv: 1808.02667]

$$V = V_{2HDM} + V_{S}$$

$$V_{2HDM} = m_{11}^{2} \Phi_{1}^{\dagger} \Phi_{1} + m_{22}^{2} \Phi_{2}^{\dagger} \Phi_{2} - [m_{12}^{2} \Phi_{1}^{\dagger} \Phi_{2} + h.c.] + \frac{\lambda_{1}}{2} (\Phi_{1}^{\dagger} \Phi_{1})^{2} + \frac{\lambda_{2}}{2} (\Phi_{2}^{\dagger} \Phi_{2})^{2} + \lambda_{3} (\Phi_{1}^{\dagger} \Phi_{1}) (\Phi_{2}^{\dagger} \Phi_{2}) + \lambda_{4} (\Phi_{1}^{\dagger} \Phi_{2}) (\Phi_{2}^{\dagger} \Phi_{1}) + \left[ \frac{\lambda_{5}}{2} (\Phi_{1}^{\dagger} \Phi_{2})^{2} + h.c. \right]$$

$$For this study:$$

$$V_{S} = m_{S}^{2} S^{\dagger} S + \left[ \frac{m_{S}'^{2}}{2} S^{2} + h.c. \right]$$

$$For this study:$$

$$\lambda_{2}'' = \lambda_{1}'' + \left[ \frac{\lambda_{11}''}{24} S^{4} + h.c. \right] + \left[ \frac{\lambda_{22}''}{6} (S^{2} S^{\dagger} S) + h.c. \right] + \frac{\lambda_{3}''}{4} (S^{\dagger} S)^{2} + S^{\dagger} S [\lambda_{1}' \Phi_{1}^{\dagger} \Phi_{1} + \lambda_{2}' \Phi_{2}^{\dagger} \Phi_{2}] + [S^{2} (\lambda_{4}' \Phi_{1}^{\dagger} \Phi_{1} + \lambda_{5}' \Phi_{2}^{\dagger} \Phi_{2}) + h.c.]$$

$$\Phi_{i} = \begin{pmatrix} \phi_{i}^{+} \\ \frac{1}{\sqrt{2}}(v_{i} + \rho_{i} + i\eta_{i}) \end{pmatrix} \qquad \langle \Phi_{i} \rangle = \begin{pmatrix} 0 \\ \frac{v_{i}}{\sqrt{2}} \end{pmatrix}$$
$$S = \frac{1}{\sqrt{2}}(v_{S} + \rho_{S} + iA_{S}) \qquad \langle S \rangle = \frac{v_{S}}{\sqrt{2}}$$

DM Candidate

#### **DM Candidate Properties:**

- massive
- electrically neutral
- colourless
- stable

# **2HDMS Higgs Sector Potential** [Notation as in: Baum and Shah, arXiv: 1808.02667]

$$V = V_{2HDM} + V_{S}$$

$$V_{2HDM} = m_{11}^{2} \Phi_{1}^{\dagger} \Phi_{1} + m_{22}^{2} \Phi_{2}^{\dagger} \Phi_{2} - [m_{12}^{2} \Phi_{1}^{\dagger} \Phi_{2} + h.c.] + \frac{\lambda_{1}}{2} (\Phi_{1}^{\dagger} \Phi_{1})^{2} + \frac{\lambda_{2}}{2} (\Phi_{2}^{\dagger} \Phi_{2})^{2} + \lambda_{3} (\Phi_{1}^{\dagger} \Phi_{1}) (\Phi_{2}^{\dagger} \Phi_{2}) + \lambda_{4} (\Phi_{1}^{\dagger} \Phi_{2}) (\Phi_{2}^{\dagger} \Phi_{1}) + \left[ \frac{\lambda_{5}}{2} (\Phi_{1}^{\dagger} \Phi_{2})^{2} + h.c. \right]$$

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$$V_{S} = m_{S}^{2} S^{\dagger} S + \left[ \frac{m_{S}'^{2}}{2} S^{2} + h.c. \right]$$

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$$V_{S} = m_{S}^{2} S^{\dagger} S + \left[ \frac{m_{S}'^{2}}{2} S^{2} + h.c. \right]$$

$$F(\frac{\lambda_{1}''}{24} S^{4} + h.c.) + \left[ \frac{\lambda_{2}''}{6} S^{2} S^{\dagger} S \right] + h.c. + \frac{\lambda_{3}''}{4} (S^{\dagger} S)^{2} + S^{\dagger} S [\lambda_{1}' \Phi_{1}^{\dagger} \Phi_{1} + \lambda_{2}' \Phi_{2}^{\dagger} \Phi_{2}] + [S^{2} (\lambda_{4}' \Phi_{1}^{\dagger} \Phi_{1} + \lambda_{5}' \Phi_{2}^{\dagger} \Phi_{2}) + h.c.]$$

| V <sub>2HDMS</sub> Symmetri   | V <sub>2HDMS</sub> Symmetric Under |  |  |  |  |  |  |  |  |
|---|------------------------------------|--|--|--|--|--|--|--|--|
| $\Phi_j \stackrel{U(1)}{ ightarrow} e^{i	heta} \Phi_j$                  | avoids charge-<br>parity violation |  |  |  |  |  |  |  |  |
| $\Phi_j^\dagger \stackrel{U(1)}{ ightarrow} e^{-i	heta} \Phi_j^\dagger$ |                                    |  |  |  |  |  |  |  |  |
| $\Phi_1 \xrightarrow{Z_2} - \Phi_1$                                     | avoids flavour<br>changing neutral |  |  |  |  |  |  |  |  |
| $\Phi_2 \xrightarrow{Z_2} \Phi_2$                                       | currents                           |  |  |  |  |  |  |  |  |
| (softly broken by m <sub>12</sub> <sup>2</sup> )                        |                                    |  |  |  |  |  |  |  |  |
| $\Phi_j \stackrel{Z'_2}{\to} \Phi_j$                                    | stabilization of DM                |  |  |  |  |  |  |  |  |
| $S \xrightarrow{Z'_2} -S$   |                                    |  |  |  |  |  |  |  |  |

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$$V_{2HDM} = m_{11}^{2} \Phi_{1}^{\dagger} \Phi_{1} + m_{22}^{2} \Phi_{2}^{\dagger} \Phi_{2} - [m_{12}^{2} \Phi_{1}^{\dagger} \Phi_{2} + h.c.] + \frac{\lambda_{1}}{2} (\Phi_{1}^{\dagger} \Phi_{1})^{2}$$

$$+ \frac{\lambda_{2}}{2} (\Phi_{2}^{\dagger} \Phi_{2})^{2} + \lambda_{3} (\Phi_{1}^{\dagger} \Phi_{1}) (\Phi_{2}^{\dagger} \Phi_{2}) + \lambda_{4} (\Phi_{1}^{\dagger} \Phi_{2}) (\Phi_{2}^{\dagger} \Phi_{1})$$

$$+ \left[ \frac{\lambda_{5}}{2} (\Phi_{1}^{\dagger} \Phi_{2})^{2} + h.c. \right]$$
for this study:
$$\lambda_{s} = m_{S}^{2} S^{\dagger} S + \left[ \frac{m_{S}'^{2}}{2} S^{2} + h.c. \right]$$

$$+ \left[ \frac{\lambda_{11}''}{24} S^{4} + h.c. \right] + \left[ \frac{\lambda_{22}''}{6} (S^{2} S^{\dagger} S) + h.c. \right] + \frac{\lambda_{33}''}{4} (S^{\dagger} S)^{2}$$

$$+ S^{\dagger} S [\lambda_{1}' \Phi_{1}^{\dagger} \Phi_{1} + \lambda_{2}' \Phi_{2}^{\dagger} \Phi_{2}] + [S^{2} (\lambda_{4}' \Phi_{1}^{\dagger} \Phi_{1} + \lambda_{5}' \Phi_{2}^{\dagger} \Phi_{2}) + h.c.]$$

| Other Prope                   | Other Properties   |  |  |  |  |  |  |
|-------------------------------|--|--|--|--|--|--|--|
| number of free<br>parameters: | 15   |  |  |  |  |  |  |
| DM mass:                      | $\begin{split}  m_{A_{S}}^{2} &= \frac{\partial^{2} V}{\partial A_{S}^{\dagger} \partial A_{S}}  _{\Phi_{1} = \langle \Phi_{1} \rangle}  _{\Phi_{2} = \langle \Phi_{2} \rangle. S = \langle S \rangle} \\ &= -(2m_{S}^{\prime 2} + v_{S}^{2}(\frac{\lambda_{1}^{\prime \prime}}{3} + \frac{\lambda_{1}^{\prime \prime}}{3}) + 2(\lambda_{4}^{\prime} v_{1}^{2} + \lambda_{5}^{\prime} v_{2}^{2})) \end{split}$ |  |  |  |  |  |  |
| Higgs sector<br>particles:    | 1 charged: $H_{\pm}$ ,<br>1 charged GB: $G_{\pm}$ , SM-like<br>3 scalars: $h_1$ , $h_2$ , $h_3$ ,<br>1 pseudo scalar: A,<br>1 pseudo scalar GB: $G_0$ ,<br>1 pseudo scalar DM: $A_s$   |  |  |  |  |  |  |
| portal<br>couplings:          | $\lambda_1', \lambda_2', \lambda_4', \lambda_5', \lambda_1'' = \lambda_2'', \lambda_3''$   |  |  |  |  |  |  |

### **2HDMS Couplings: DM to Scalar**



$$A_{S} \qquad h_{j} \qquad \lambda_{h_{j}h_{k}A_{S}A_{S}} = \frac{\partial^{4}V}{\partial h_{j}\partial h_{k}\partial A_{S}\partial A_{S}} = -i[(\lambda_{1}' - 2\lambda_{4}')R_{j1}R_{k1} + (\lambda_{2}' - 2\lambda_{5}')R_{j2}R_{k2} - \frac{1}{2}(\lambda_{1}'' - \lambda_{3}'')R_{j3}R_{k3}]$$

$$A_{S}$$

$$\frac{\lambda_{h_{j}A_{S}A_{S}}}{k_{j}} = \frac{1}{v} \frac{\partial^{3}V}{\partial h_{j}\partial A_{S}\partial A_{S}}$$

$$= -i[(\lambda_{1}' - 2\lambda_{4}')c_{\beta}R_{j1} + (\lambda_{2}' - 2\lambda_{5}')s_{\beta}R_{j2} - \frac{v_{S}}{2v}(\lambda_{1}'' - \lambda_{3}'')R_{j3}]$$

## **2HDMS Basis Change**

#### **Interaction Basis Parameters:**

$$\begin{split} \lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5, m_{12}^2, \tan\beta, v_S, m_S^{2\prime}, \\ \lambda_1', \lambda_2', \lambda_4', \lambda_5', \lambda_1'' = \lambda_2'', \lambda_3'' \end{split}$$

#### **Mass Basis Parameters:**

 $m_{h_1}, m_{h_2}, m_{h_3}, m_A, m_{A_S}, m_{H^{\pm}}, \delta'_{14}, \delta'_{25},$  $\tan\beta, v_S, c_{h_1bb}, c_{h_1tt}, \tilde{\mu}^2, m'_S, alignm$ 



## **2HDMS Benchmark Point (BP)**

| $m_{h_1}$    | <i>m</i> <sub><i>h</i><sub>2</sub></sub> | m <sub>h3</sub>   | m <sub>A</sub>    | m <sub>As</sub>                   | m <sub>H<sup>±</sup></sub>        | $\delta_{14}'$ | $\delta'_{25}$ |
|--------------|--|-------------------|-------------------|-----------------------------------|-----------------------------------|----------------|----------------|
| 95 GeV       | 125.09 GeV                               | 900 GeV           | 900 GeV           | 325.86 GeV                        | 900 GeV                           | -9.6958        | 0.2475         |
| $tan(\beta)$ | VS                                       | C <sub>h1bb</sub> | C <sub>h1tt</sub> | $	ilde{\mu}^2$                    | $m_S^{\prime 2}$                  | alignm         |                |
| 10           | 239.86 GeV                               | 0.2096            | 0.4192            | $8.128 \times 10^5 \text{ GeV}^2$ | $-4.809 \times 10^4 \text{GeV}^2$ | 0.9998         | X              |



\*yy channel at CMS (~2.9  $\sigma$ ), bb channel at LEP (~2  $\sigma$ ), investigated in S. Heinemeyer, C. Li, et al, 2021, arxiv:2112.11958



#### Extend SM → Two Higgs Doublet Model with Complex Singlet (2HDMS)



## **DM Phenomenology**



## **DM Phenomenology**

| $m_{h_1}$    | $m_{h_2}$  | m <sub>h3</sub>   | m <sub>A</sub>    | m <sub>As</sub>                   | $m_{H^{\pm}}$                     | $\delta'_{14}$ | $\delta'_{25}$ |
|--------------|------------|-------------------|-------------------|-----------------------------------|-----------------------------------|----------------|----------------|
| 95 GeV       | 125.09 GeV | 900 GeV           | 900 GeV           | 325.86 GeV 900 GeV -              |                                   | -9.6958        | 0.2475         |
| $tan(\beta)$ | VS         | C <sub>h1bb</sub> | C <sub>h1tt</sub> | $	ilde{\mu}^2$                    | $\tilde{\mu}^2$ $m_S^{\prime 2}$  |                |                |
| 10           | 239.86 GeV | 0.2096            | 0.4192            | $8.128 \times 10^5 \text{ GeV}^2$ | $-4.809 \times 10^4 \text{GeV}^2$ | 0.9998         |                |



## **DM Phenomenology**

| $m_{h_1}$    | <i>m</i> <sub><i>h</i><sub>2</sub></sub> | m <sub>h3</sub>   | m <sub>A</sub>    | m <sub>As</sub>                   | m <sub>H<sup>±</sup></sub>        | $\delta'_{14}$ | $\delta'_{25}$ |
|--------------|--|-------------------|-------------------|-----------------------------------|-----------------------------------|----------------|----------------|
| 95 GeV       | 125.09 GeV                               | 900 GeV           | 900 GeV           | / 325.86 GeV 900 GeV              |                                   | -9.6958        | 0.2475         |
| $tan(\beta)$ | VS                                       | C <sub>h1bb</sub> | C <sub>h1tt</sub> | $	ilde{\mu}^2$                    | $m_{S}^{\prime 2}$                | alignm         |                |
| 10           | 239.86 GeV                               | 0.2096            | 0.4192            | $8.128 \times 10^5 \text{ GeV}^2$ | $-4.809 \times 10^4 \text{GeV}^2$ | 0.9998         |                |

#### **Allowed Parameter Space**



- → strongest constraints from:
- bounded from below (bfb)
- unitarity
- LUX-ZEPLIN (LZ)
- Fermi-LAT
- → narrow allowed band around BP

#### Extend SM → Two Higgs Doublet Model with Complex Singlet (2HDMS)



## **Collider Phenomenology**



## Collider Phenomenology HL-LHC

| $m_{h_1}$    | <i>m</i> <sub><i>h</i><sub>2</sub></sub> | m <sub>h3</sub>   | m <sub>A</sub>    | m <sub>As</sub>                   | m <sub>H<sup>±</sup></sub>        | $\delta'_{14}$ | $\delta'_{25}$ |
|--------------|--|-------------------|-------------------|-----------------------------------|-----------------------------------|----------------|----------------|
| 95 GeV       | 125.09 GeV                               | 900 GeV           | 900 GeV           | 00 GeV 325.86 GeV 900 GeV         |                                   | -9.6958        | 0.2475         |
| $tan(\beta)$ | VS                                       | C <sub>h1bb</sub> | C <sub>h1tt</sub> | $	ilde{\mu}^2$                    | $m_{S}^{\prime 2}$                | alignm         |                |
| 10           | 239.86 GeV                               | 0.2096            | 0.4192            | $8.128 \times 10^5 \text{ GeV}^2$ | $-4.809 \times 10^4 \text{GeV}^2$ | 0.9998         |                |





→ very low significance for BP

| Process | <b>C</b> 1 | <b>C</b> 2 | <b>C</b> 3 | <b>C4</b> | <b>C</b> 5 |
|---------|------------|------------|------------|-----------|------------|
| GGF     | 696        | 137        | 114        | 114       | 114        |
| S       |            | 1          | L.356 d    | 7         |            |

| Process | D1   | D2   | D3   | D4   | D5   | D6   |
|---------|------|------|------|------|------|------|
| VBF     | 0.98 | 0.39 | 0.28 | 0.23 | 0.23 | 0.23 |
| S       |      |      | 0.00 | )7 σ |      |      |

## Collider Phenomenology Future Lepton Colliders (e<sup>+</sup>e<sup>-</sup>/µ<sup>+</sup>µ<sup>-</sup>)

| $m_{h_1}$    | $m_{h_2}$  | m <sub>h3</sub>   | m <sub>A</sub>    | $m_{A_S}$ $m_{H^{\pm}}$           |                                   | $\delta'_{14}$ | $\delta'_{25}$ |
|--------------|------------|-------------------|-------------------|-----------------------------------|-----------------------------------|----------------|----------------|
| 95 GeV       | 125.09 GeV | 900 GeV           | 900 GeV           | 325.86 GeV                        | 900 GeV                           | -9.6958        | 0.2475         |
| $tan(\beta)$ | VS         | C <sub>h1bb</sub> | C <sub>h1tt</sub> | $	ilde{\mu}^2$                    | $m_S^{\prime 2}$                  | alignm         | -              |
| 10           | 239.86 GeV | 0.2096            | 0.4192            | $8.128 \times 10^5 \text{ GeV}^2$ | $-4.809 \times 10^4 \text{GeV}^2$ | 0.9998         | ×              |

h1.2.3  $e^{-}/\mu^{-}$ → AcAc  $10^{-2}$ AcAc AcAcv 10<sup>0</sup> → AsAsV  $10^{-2}$ [q] ه 10<sup>-4</sup>  $10^{-6}$  $10^{-8}$ 103  $2 \times 10^{3}$  $3 \times 10^{3}$ √*s* [GeV]

 $e^{+}/\mu^{+}$ 





#### Dark Matter (DM) Phenomenology

(Relic Density, Indirect Detection, Direct Detection)



- can fit 95 GeV excess in 2HDMS
- strong constraints from: bfb, unitarity, LZ, Fermi-LAT

Collider

#### Phenomenology (HL-LHC,

HIUMI)

**Future Lepton Colliders)** 

- significance at HL-LHC rather low
  - $\rightarrow$  can be improved with machine learning
  - → comprehensive parameter scans planned
- potentially promising prospects at Future Lepton Colliders
  - → further improvement with polarized beams
  - → further parameter scans planned
- muon collider shows best prospects of production cross section

| m    | <i>n</i> 1 | m <sub>h2</sub> | m <sub>h3</sub>   | m <sub>A</sub>    | m <sub>As</sub>                   | m <sub>H<sup>±</sup></sub>        | $\delta'_{14}$ | $\delta'_{25}$ |
|------|------------|-----------------|-------------------|-------------------|-----------------------------------|-----------------------------------|----------------|----------------|
| 95 G | eV         | 125.09 GeV      | 900 GeV           | 900 GeV           | 325.86 GeV 900 GeV                |                                   | -9.6958        | 0.2475         |
| tan( | β)         | VS              | C <sub>h1bb</sub> | C <sub>h1tt</sub> | $\tilde{\mu}^2$ $m_S^{\prime 2}$  |                                   | alignm         |                |
| 10   | )          | 239.86 GeV      | 0.2096            | 0.4192            | $8.128 \times 10^5 \text{ GeV}^2$ | $-4.809 \times 10^4 \text{GeV}^2$ | 0.9998         | $\mathbf{X}$   |

| Decay Modes                 | Branching Ratio (BR) |
|-----------------------------|----------------------|
| $h_3 \rightarrow b\bar{b}$  | 0.412                |
| $h_3 \rightarrow A_S A_S$   | 0.247                |
| $h_3 \rightarrow t\bar{t}$  | 0.106                |
| $h_3 \rightarrow \tau \tau$ | 0.064                |
| $h_3 \rightarrow h_2 h_2$   | 0.061                |
| $h_3 \rightarrow h_1 h_2$   | 0.035                |
| $h_3 \rightarrow h_1 h_1$   | 0.022                |



#### 

We generated the gluon gluon fusion process with  $h_3$  successively decaying into a pair of DM candidates in Madgraph\_aMC\_v3.4.1. For **BP1**,  $\sigma_{GGF} \times BR(h_3 \times A_S A_S) =$ 0.232 fb. We perform the signal analyses using the following cuts successively from Ref. [58] on the benchmark **BP1**,

- C1: The final state consists of up to four jets with  $p_T > 30$  GeV and  $|\eta| < 2.8$ .
- C2: We demand a large  $\not\!\!\!E_T > 250$  GeV.
- C3: The hardest leading jet has  $p_T > 250$  GeV with  $|\eta| < 2.4$ .
- C4: We demand  $\Delta \Phi(j, \not\!\!\!E_T) > 0.4$  for all jets and  $\Delta \Phi(j, \not\!\!\!E_T) > 0.6$  for the leading jet.
- C5: A lepton-veto is imposed for electrons with  $p_T > 20$  GeV and  $|\eta| < 2.47$  and muons with  $p_T > 10$  GeV and  $|\eta| < 2.5$ .

| Process | C1  | C2  | <b>C3</b> | <b>C4</b> | C5  |
|---------|-----|-----|-----------|-----------|-----|
| GF      | 696 | 137 | 114       | 114       | 114 |
| S       |     | 1   | .356 a    | 7         |     |

**Table 9.** The cut flow table for the number of signal events for **BP1** at leading order (LO) and signal significance S at  $\sqrt{s} = 14$  TeV and  $\mathcal{L} = 3000$  fb<sup>-1</sup>. The SM background is obtained from Ref. [58].

#### 

- **D1**: The final state consists of at least two jets with  $p_T(j_1) > 80$  and  $p_T(j_2) > 40$  GeV and  $\Delta \Phi(j_i, \not \!\!\!E_T) > 0.5$ .
- **D2**: We demand  $\eta j_1 j_2 < 0$  and  $\Delta \Phi j_1 j_2 < 1.5$ .
- **D3**: We demand  $|\Delta \eta|_{jj} > 3.0$ .
- D4: The invariant mass of the two forward jets is required to be large, i.e,  $M_{jj} > 600$  GeV.
- **D5**: We demand  $\not\!\!\!E_T > 200$  GeV.
- D6: Furthermore, a lepton veto is imposed for electrons with p<sub>T</sub> > 20 GeV or muons with p<sub>T</sub> > 10 GeV.

| Process | D1             | D2   | D3   | D4   | D5   | D6   |
|---------|----------------|------|------|------|------|------|
| VBF     | 0.98           | 0.39 | 0.28 | 0.23 | 0.23 | 0.23 |
| S       | $0.007 \sigma$ |      |      |      |      |      |

**Table 10.** The cut flow table for the signal cross-sections for **BP1** at LO and signal significance S at  $\sqrt{s} = 14$  TeV and  $\mathcal{L} = 3000$  fb<sup>-1</sup>. The SM background is obtained from Ref. [58].

Future Lepton Colliders: Event generation with WHIZARD, cuts:

• Photon cuts:  $E_{\gamma} > 10$  GeV,  $\Theta > 7^{\circ}$ 













Ωh<sup>2</sup>











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