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# Investigating the Higgs selfcouplings through HHH production

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based on work in collaboration with Georg Weiglein



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# Introduction: the Higgs potential

 Crucial questions about Electroweak Symmetry Breaking: What is the form of the Higgs potential?



**SM Potential:** 
$$V(\Phi) = \lambda (\Phi^{\dagger} \Phi)^2 - \mu^2 \Phi^{\dagger} \Phi$$
  
 $\supset -\lambda v H^3 - \frac{\lambda}{4} H^4$   
**BSM theories**  $\rightarrow$  more complicated shapes

Very challenging experimentally

requires trilinear and quartic Higgs self-couplings

## **Trilinear Higgs coupling: experimental status**

• Experimental bounds on signal strength from HH production:  $\mu_{HH} < 2.4$ 





# **Triple Higgs production**

- Additional source of information  $\rightarrow$  HHH production Dependence on both trilinear  $\kappa_3$  and quartic  $\kappa_4$   $H = \frac{\kappa_3}{H}$   $H = \frac{\kappa_4}{H}$   $H = \frac{\kappa_4}{H}$
- Is it possible to obtain bounds on  $\kappa_3$  and  $\kappa_4$  from HHH production beyond theoretical bounds from perturbative unitarity?
- How big can deviations in  $\kappa_4$  be in BSM theories from SM value ( = 1)
- Is there potential to improve  $\kappa_3$  constraints from HH production?

## Perturbative unitarity and Higgs couplings

- Process relevant for  $\kappa_3$ ,  $\kappa_4$  is  $HH \rightarrow HH$  scattering (see also [Liu et al `18])
- Jacob-Wick expansion allows to extract partial waves



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 $\kappa_3$ 

## Extension of SM potential by operators



Contributions to  $\kappa_3$ ,  $\kappa_4$ :



# **Extension of SM potential by operators**



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 $\kappa_3$ 

#### **BSM example: 2HDM**

- Consider the 2HDM as an example
- Prediction for  $\kappa_3$  up to two-loop level: [Bahl, Braathen, Weiglein 22]



### Model example: 2HDM - trilinear vs quartic

- Same benchmark Point of [Bahl, Braathen, Weiglein 22]  $\rightarrow$  cross-check  $\kappa_3$  result
- Expectedly deviations in  $\kappa_3$  induce sizeable deviations in  $\kappa_4$



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 $\kappa_i =$ 

 $i \in \{3H, 4H\}$ 

#### **Prospects for the HL-LHC**

• Small rates at LHC

Need dominant production & decays

gluon fusion

$$BR(H \to b\bar{b}) = 0.584$$

• <u>BRs</u>:  $BR(H \to \tau^+ \tau^-) = 6.627 \times 10^{-2}$ 

 $BR(H \to \gamma \gamma) = 2.26 \times 10^{-3}$ 

 $2b4\tau$  and  $4b2\gamma$ produce relatively few events even for large  $\kappa_3 \gtrsim 4.5, \ \kappa_4 \gtrsim 30$ 

• Focus on 6b and  $4b2\tau$  final states with 5 and 3 tagged b-quarks, respectively

#### **Backgrounds:**

<u>6b</u>: dominant QCD contributions (see also [Papaefstathiou, Robens, Xolocotzi`21]) <u>4b2</u> $\tau$ :  $W^+W^-b\bar{b}b\bar{b}$ ,  $Zb\bar{b}b\bar{b}$ ,  $t\bar{t}(H \to \tau\tau)$ ,  $t\bar{t}(H \to b\bar{b})$ ,  $t\bar{t}(Z \to \tau\tau)$ ,  $t\bar{t}(Z \to b\bar{b})$ ,  $t\bar{t}t\bar{t}$ 

## **Event generation and pre-selection**

- Events generated with MadGraph5\_aMC@NLO
- Higgs states decayed with MadSpin

(conservative) background K-factor of 2

signal K-factor of 1.7 [Florian, Fabre, Mazzitelli`20]



#### **Pre-selection cuts:**

 $\begin{array}{ll} \mbox{Invariant mass of final states:} \gtrsim 350 \mbox{ GeV} \\ \mbox{At least one pair of tagged states with} \\ m_{ij} \in [110, 140] \\ \mbox{$p_T(b) > 30 \mbox{ GeV}$} \quad p_T(\tau) > 10 \mbox{ GeV} \\ |\eta(\tau)| < 2.5 \quad |\eta(b)| < 2.5 \end{array}$ 

## **Graph Neural Network**

- Add nodes for tagged  $b,\,\tau$  and Missing Transverse Momentum
- Consider combinations of *b*-quarks and  $\tau$  with reconstructed four-momentum  $(p_i + p_j)$
- If  $m_{ij} \in [100, 150]$  (GeV) add extra node  $H_i$
- Features for each node:  $[p_T, \eta, \phi, m, PDGID]$



Dataset with signal & 
$$\blacksquare$$
 **GNN**  
background graphs **Converse**  $E = \left\{ P(\mathbf{S}), P(\mathbf{B}_1), \dots, P(\mathbf{B}_N) \right\}$ 

- GNN trained on  $(\kappa_3, \kappa_4) = (1,1)$  sample
- Signal regions selected with cuts on background scores

# **Graph Neural Network**

• Consider combinations of *b*-quarks and  $\tau$  with reconstructed four-momentum  $(p_i + p_j)$ 

If  $m \in [100, 150]$  (CoVA add ovtra pada

- **Assumption:** Same GNN efficiency for other values of  $(\kappa_3, \kappa_4)$
- Flat optimistic 80% b-tagging and  $\tau$ -tagging efficiency
- Significance:  $Z = \sqrt{2\left((S+B)\ln\left(1+\frac{S}{B}\right) S\right)}$

from [Cowan, Cranmer, Gross, Vitells `10]

- GNN trained on  $(\kappa_3, \kappa_4) = (1,1)$  sample
- Signal regions selected with cuts on background scores

#### **Showered and reconstructed results** 5*b*

- Showering and reconstruction of events: Pythia, FastJet, Rivet
- HL-LHC luminosity of 3/ab and ATLAS-CMS combined luminosity of 6/ab



#### Showered and reconstructed results $3b2\tau$

•  $3b2\tau$  more complicated due to multiple backgrounds —

multi-class classification

- Train on backgrounds:  $W^+W^-b\overline{b}b\overline{b}$ ,  $Zb\overline{b}b\overline{b}$ ,  $t\overline{t}(H \to \tau^+\tau^-)$ 
  - Impose cuts on NN scores to reduce backgrounds:

 $P[W^+W^-b\bar{b}b\bar{b}] < 0.03, \ P[Zb\bar{b}b\bar{b}] < 0.1, \ P[t\bar{t}(H \to b\bar{b})] < 0.3$ 

	$\sigma(\text{gen.})(\text{fb})$	$\sigma({ m sel.})({ m fb})$	$\sigma({ m NN})({ m fb})$
$tt(H \to \tau\tau)$	3.8	0.17	0.011
WWbbbb	31	4.6	$8.1 \times 10^{-3}$
$tt(H \rightarrow bb)$	3.5	0.89	$3.8 \times 10^{-3}$
Zbbbb	4.3	0.45	$3.3 \times 10^{-4}$
$tt(Z \rightarrow bb)$	0.77	0.15	$3.1 \times 10^{-4}$
$tt(Z \to \tau \tau)$	4.7	0.080	$2.2 \times 10^{-4}$
tttt	0.38	0.091	$2.1 \times 10^{-4}$

#### Showered and reconstructed results $3b2\tau$

•  $3b2\tau$  more complicated due to multiple backgrounds •

multi-class classification

• Train on backgrounds:  $W^+W^-b\overline{b}b\overline{b}$ ,  $Zb\overline{b}b\overline{b}$ ,  $t\overline{t}(H \to \tau^+\tau^-)$ 



#### **Combined Results**

- Assumption: No correlations
- Simplified combination of significances (Stouffer method)

$$Z_{\text{comb.}} = \frac{Z_{3b2\tau} + Z_{5b}}{\sqrt{2}}$$

<u>Combination</u> of further channels and improvements of <u>tagging/reconstruction</u> methods could enhance results further



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#### Understanding the 'black box': NN interpretations

Which features are more important? Investigate with 'Integrated Gradients' method

- Tagged b-jets and  $\tau$  nodes ordered by  $p_T$
- 'Roughly' reconstructed Higgs nodes ordered by 'closeness' to 125 GeV
- $p_T$ , E and PID more important than angular observables
- Higgs masses most important







#### **Lepton Colliders**

- Complete picture of  $(\kappa_3, \kappa_4) \rightarrow$  lepton colliders?
- Inclusive  $\ell \ell \to HHH + X$  analysis with  $H \to b\bar{b}$ 
  - At least 5 tagged *b*-quarks with  $p_T(b) > 30$  GeV
  - ► Tagging efficiency: 80 %

- Important: For high energies b-quarks are not only in the central part of detector → requires extended tagging capabilities
- Negligible background from other SM processes



#### **Lepton Collider Results**

- Poissonian analysis:  $\mu_{up} = \frac{1}{2} F_{\chi^2}^{-1} \left[ 2(n+1); CL \right]$
- Results similar to other works with dedicated analyses for 1 and 3 TeV, e.g. [Maltoni, Pagani, Zhao `18]



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# **HL-LHC vs. future lepton colliders**

- HL-LHC can provide competitive results compared to  $1\ {\rm TeV}$  collider
- High energy lepton collisions way more sensitive



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**BUT** such machines

## Conclusions

• If there is a sizeable deviation in  $\kappa_3$ , an even larger deviation in  $\kappa_4$  is not unreasonable sizeable  $\kappa_4$  deviations allowed by unitarity

- **<u>GNNs</u>** provide enhanced results at HL-LHC
  - HL-LHC should be able to probe regions allowed by unitarity
  - HHH not powerful enough to constrain  $\kappa_3$  as well as di-Higgs bounds

**BUT** can provide complementary information and be used in combination with di-Higgs

HL-LHC competitive with 1 TeV lepton colliders but higher energies more sensitive



# Backup

[ATLAS 2211.01216]

Combination assumption	Obs. 95% CL	Exp. 95% CL	Obs. value $^{+1\sigma}_{-1\sigma}$
HH combination	$-0.6 < \kappa_\lambda < 6.6$	$-2.1 < \kappa_\lambda < 7.8$	$\kappa_{\lambda} = 3.1^{+1.9}_{-2.0}$
Single- <i>H</i> combination	$-4.0 < \kappa_\lambda < 10.3$	$-5.2 < \kappa_\lambda < 11.5$	$\kappa_{\lambda} = 2.5^{+4.6}_{-3.9}$
HH+H combination	$-0.4 < \kappa_\lambda < 6.3$	$-1.9 < \kappa_\lambda < 7.5$	$\kappa_{\lambda} = 3.0^{+1.8}_{-1.9}$
<i>HH</i> + <i>H</i> combination, $\kappa_t$ floating	$-0.4 < \kappa_\lambda < 6.3$	$-1.9 < \kappa_\lambda < 7.6$	$\kappa_{\lambda} = 3.0^{+1.8}_{-1.9}$
<i>HH</i> + <i>H</i> combination, $\kappa_t$ , $\kappa_V$ , $\kappa_b$ , $\kappa_\tau$ floating	$-1.3 < \kappa_\lambda < 6.1$	$-2.1 < \kappa_\lambda < 7.6$	$\kappa_{\lambda} = 2.3^{+2.1}_{-2.0}$

## **Two-Higgs Doublet Model (2HDM)**

• Two-Higgs Doublet Model (2HDM)  $\rightarrow$  a second doublet:  $\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \rho_1 + i\eta_1) \end{pmatrix}, \ \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \rho_2 + i\eta_2) \end{pmatrix}$ 

$$V_{2\text{HDM}} = m_{11}^2 (\Phi_1^{\dagger} \Phi_1) + m_{22}^2 (\Phi_2^{\dagger} \Phi_2) - m_{12}^2 (\Phi_1^{\dagger} \Phi_2 + \Phi_2^{\dagger} \Phi_1) + \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 (\Phi_1^{\dagger} \Phi_1) (\Phi_2^{\dagger} \Phi_2) + \lambda_4 (\Phi_1^{\dagger} \Phi_2) (\Phi_2^{\dagger} \Phi_1) + \frac{\lambda_5}{2} \left( (\Phi_1^{\dagger} \Phi_2)^2 + (\Phi_2^{\dagger} \Phi_1)^2 \right)$$

• Free parameters:  $m_H, m_{H'}, m_A, m_{H^{\pm}}, m_{12}^2, v, \cos(\beta - \alpha), \tan\beta$ 

Scalar Particle content:Neutral scalars: H',  $H(m_H = 125 \text{ GeV})$ Neutral pseudoscalars: ACharged scalars:  $H^{\pm}$ 

Alignment limit  $\rightarrow$  couplings of light Higgs same as SM  $\cos(\beta - \alpha) = 0$ 

#### Model example: 2HDM - calculation

• 1-loop calculation for  $\kappa_3$ ,  $\kappa_4$  with FeynArts, FormCalc, LoopTools in alignment limit



#### **Edge Convolution**

**Input features:**  $\vec{x}_{i}^{(0)} \rightarrow$  update iteratively with **Edge Convolution** operation:

#### **Edge Convolution operation**



# **Graph Embedding**

- Fully-connected nodes for b and  $\tau$  final states
- **Input features**:  $[p_T, \eta, \phi, E, m, PDGID]$ 
  - Additional node for Missing Transverse Momentum (MTM) in showered & reconstructed events



- Consider combinations of *b*-quarks and  $\tau$ with reconstructed four-momentum
- 2.
- $(p_i + p_i)$
- If  $m_{ii} \in [100, 150]$  (GeV) add extra node  $H_i$



**RN: Reconstructed Nodes** 

# **Embedding performance**

Dataset with signal &  $\blacksquare$  **GNN** background graphs **Calculate Converses**  $\bullet$   $\left\{ P(\mathbf{S}), P(\mathbf{B}_1), \ldots, P(\mathbf{B}_N) \right\}$ 

- GNN trained on  $(\kappa_3, \kappa_4) = (1,1)$  sample
- Evaluate performance with Receiver Operating Characteristic (ROC) curves



# **Training loss and accuracy**



#### **Score distributions**



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## **Integrated Gradients**

- $\rightarrow$  Integrated Gradients: [Sundararajan, Taly, Yan 1703.01365]
  - axiomatic method
  - uses Neural Network gradients  $\rightarrow$  **fast!**
  - suitable for requires a differentiable model **Neural Networks!**
  - input baseline Definition:  $I_{i}(x) = (x_{i} - x_{i}') \int_{0}^{1} d\alpha \frac{\partial F(x' + \alpha(x - x'))}{\partial x_{i}}$ Gradient of Neural Attribution scores Network F  $\rightarrow$  importance of feature
- Easy to implement for Graph Neural Networks as well

Does **not** take into account graph structures

work in progress in Deep Learning community

Viable to understand important features

expect mass of reconstructed Higgs to be important

#### • <u>Axioms:</u>

- <u>Completeness</u>: sum of attributions equal to difference of network output for input and baseline values
- <u>Sensitivity</u>: when baseline and input have different values and different NN outputs, attributions should also be different
- **Dummy**: A zero input should yield no attribution
- Implementation Invariance: If two methods are equivalent (i.e. yield same scores for all inputs despite being different) then attributions should be identical
- **Linearity**: Attributions should be linear for linear combinations of networks  $aF_1 + bF_2$
- **<u>Symmetry</u>**: For a network symmetric for two variables F(x, y) = F(y, x), the attributions should be the same

# **Reconstructed Higgs Mass**

- Interpretation as expected: If a Higgs close to 125 GeV can be found  $\implies$  signal
- Complete understanding would require to study correlations between observables → <u>future work</u>



## Attribution vs. nodes

- E and  $p_T$  from leading order particles is more important
- *m* is more important for the reconstructed Higgs closest to the SM mass value





#### Lepton collider cross sections

- Inclusive  $\ell \ell \to HHH + X$  analysis with  $H \to b\bar{b}$
- Cross sections small below 1 TeV
- Note:  $\mu^+\mu^-$  vs.  $e^+e^-$  collider at 10 TeV has difference of less than 5 % on cross sections

