

Track reconstruction of charged particles using a 4D quantum algorithm

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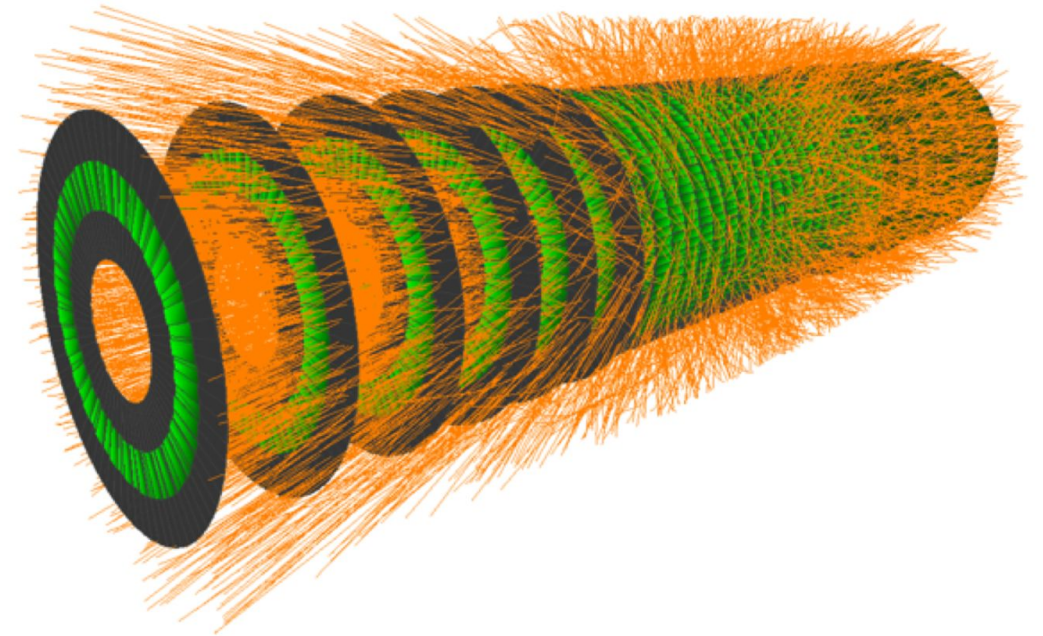
HELMHOLTZ



Track reconstruction

Reconstruct full events:

- Measuring particle energy
- Determine particle type
- Projection to/through other detector parts
- Identify/reconstruct secondary decays



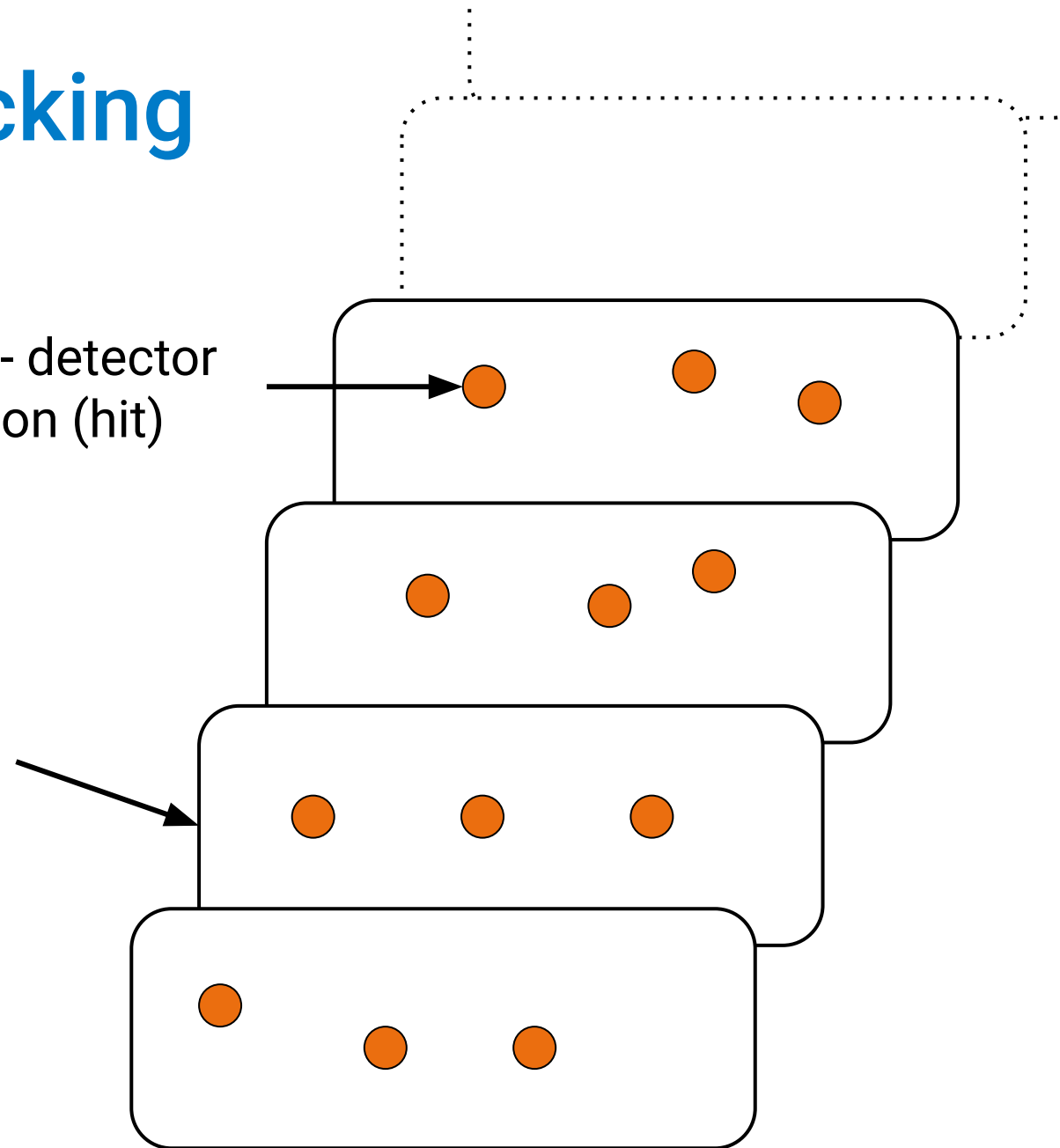
Source: TrackML Challenge
<https://www.kaggle.com/competitions/trackml-particle-identification/overview/description>

... but can become computationally very costly!

Pattern recognition for tracking

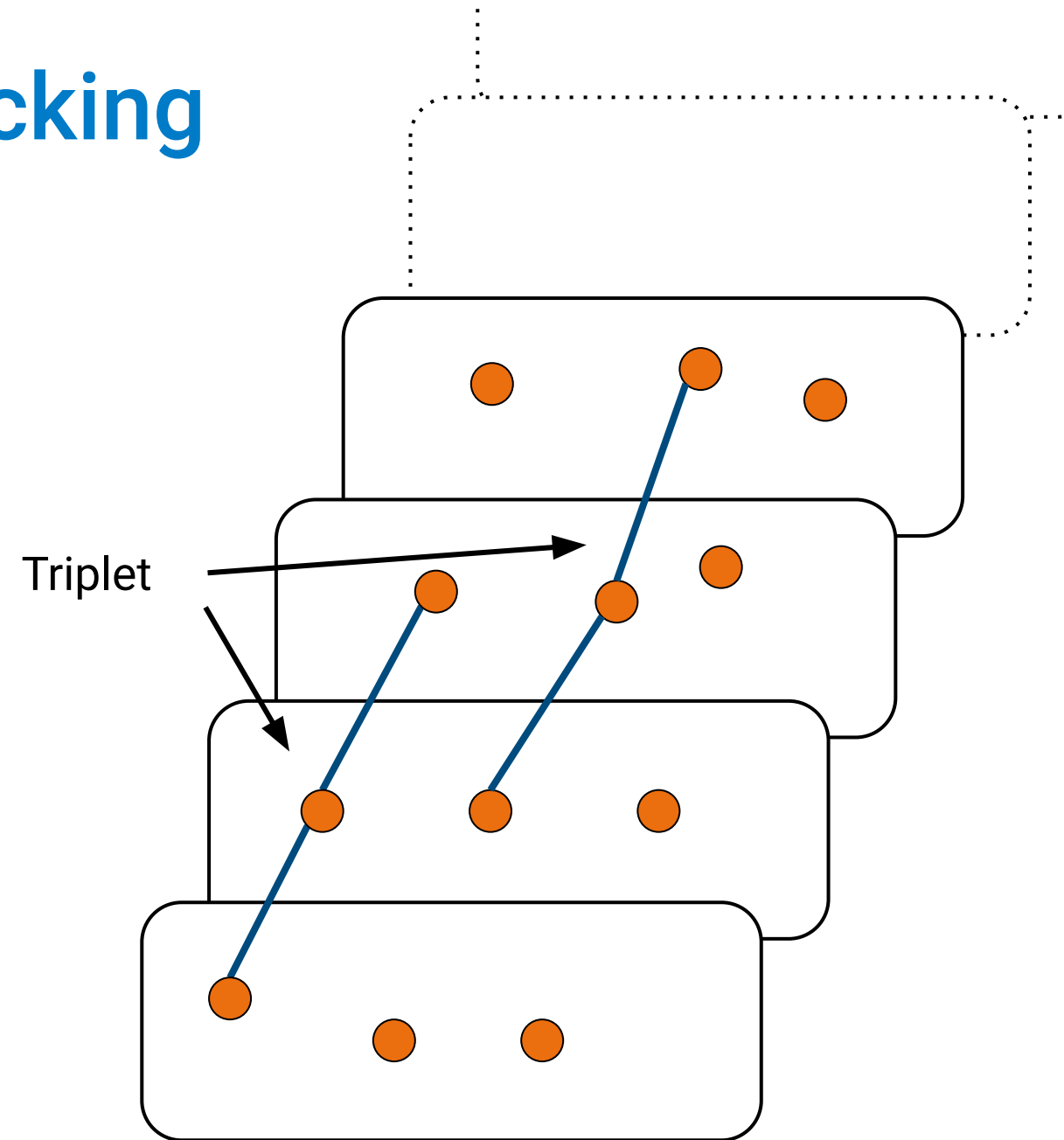
particle - detector
interaction (hit)

detector
layer



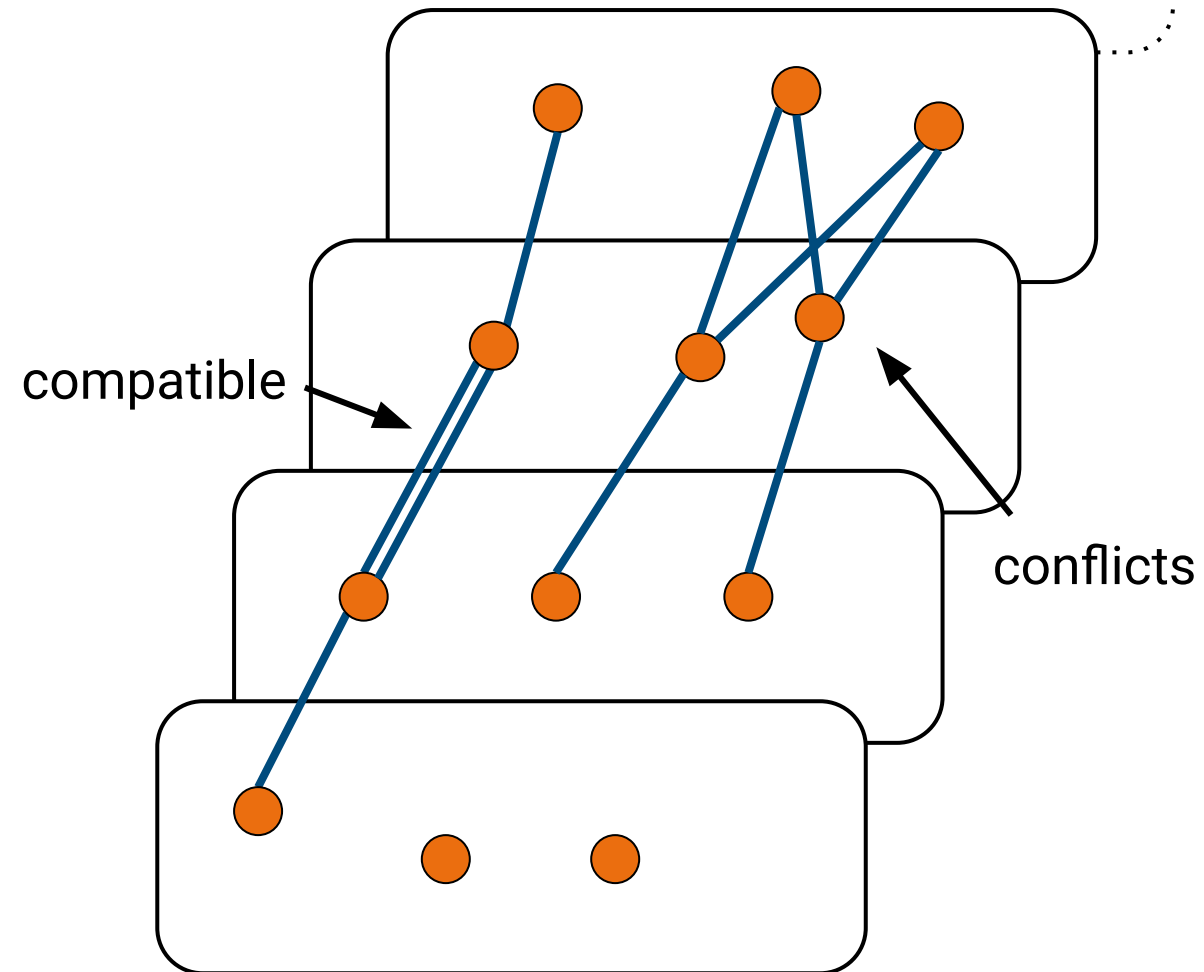
Pattern recognition for tracking

- **Triplets** as elementary patterns



Pattern recognition for tracking

- **Triplets** as elementary patterns
- **Interactions** between triplets

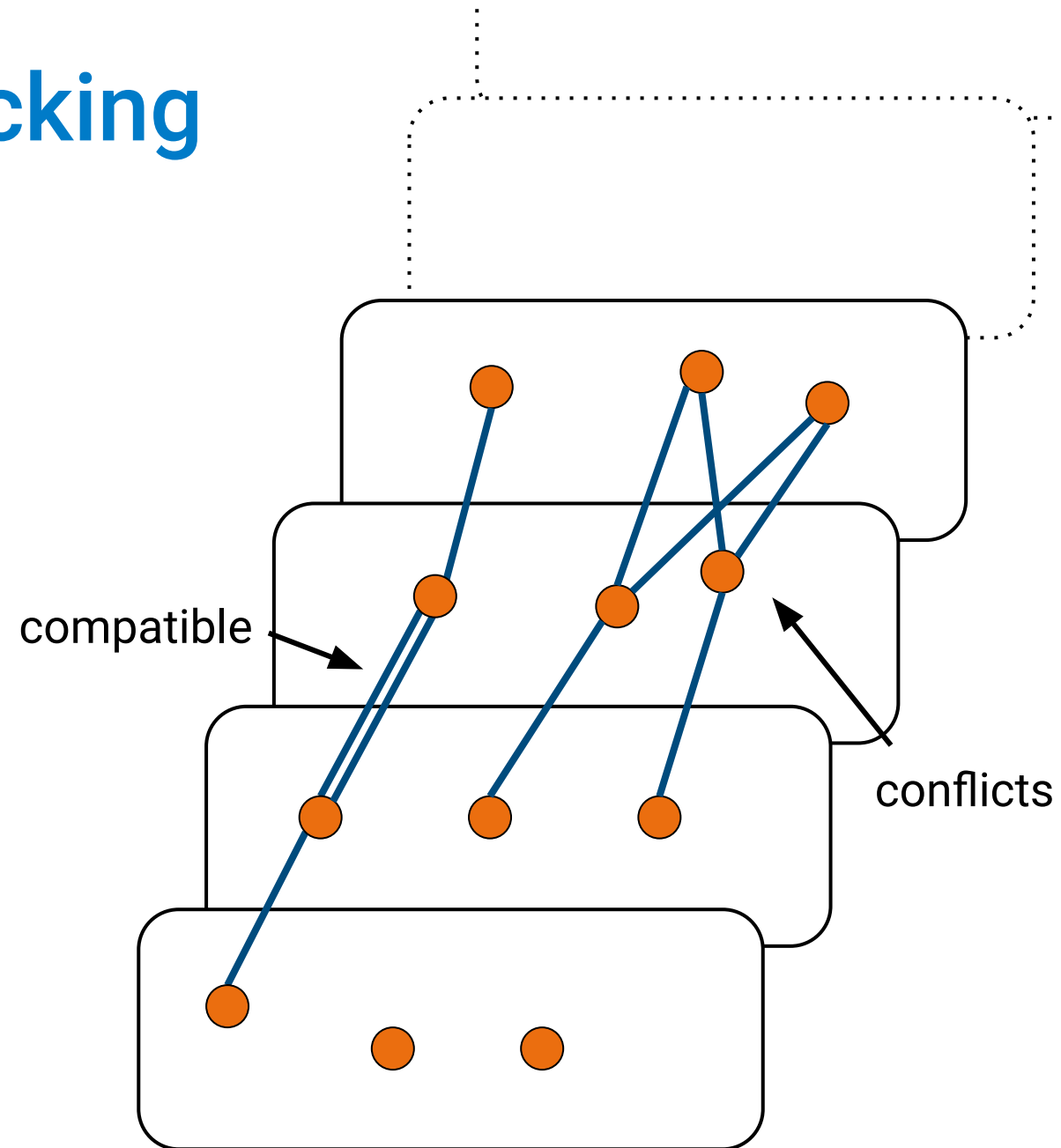


Pattern recognition for tracking

- **Triplets** as elementary patterns
- **Interactions** between triplets

Goal:

Identify triplets stemming from a single particle
→ build tracks from kept triplets

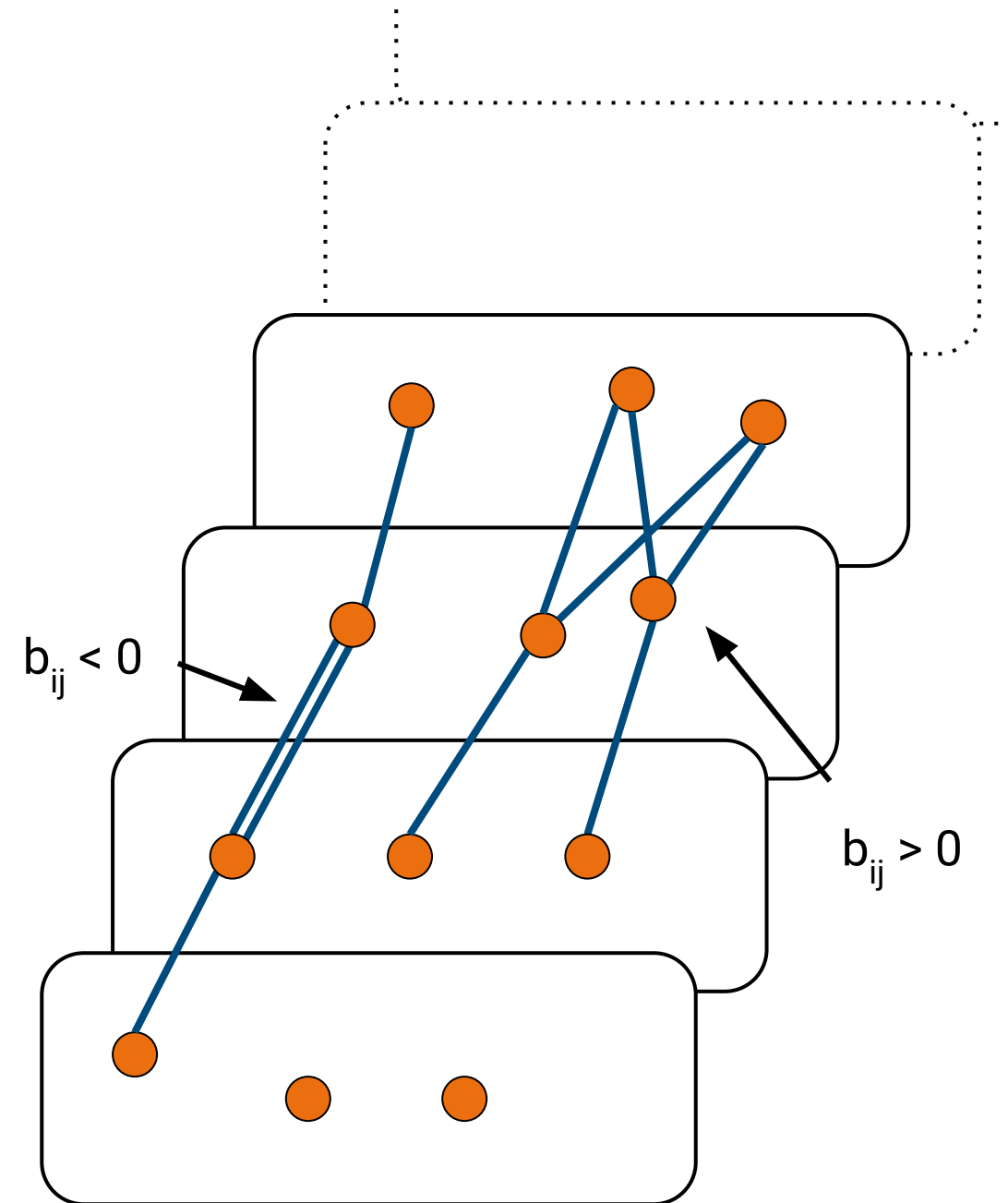


QUBO

Quadratic Unconstrained Binary Optimisation

$$\hat{H} = \sum_i^N \sum_{j<i} b_{ij} T_i T_j + \sum_{i=1}^N a_i T_i \quad (\text{QUBO})$$

- $T_i \in \{0, 1\}$
- b_{ij} : interaction
- a_i : quality
- $\mathbf{v}_{\text{binary}}: [T_1, T_2, T_3, \dots, T_N] \rightarrow [0, 1, 1, \dots, 0]$



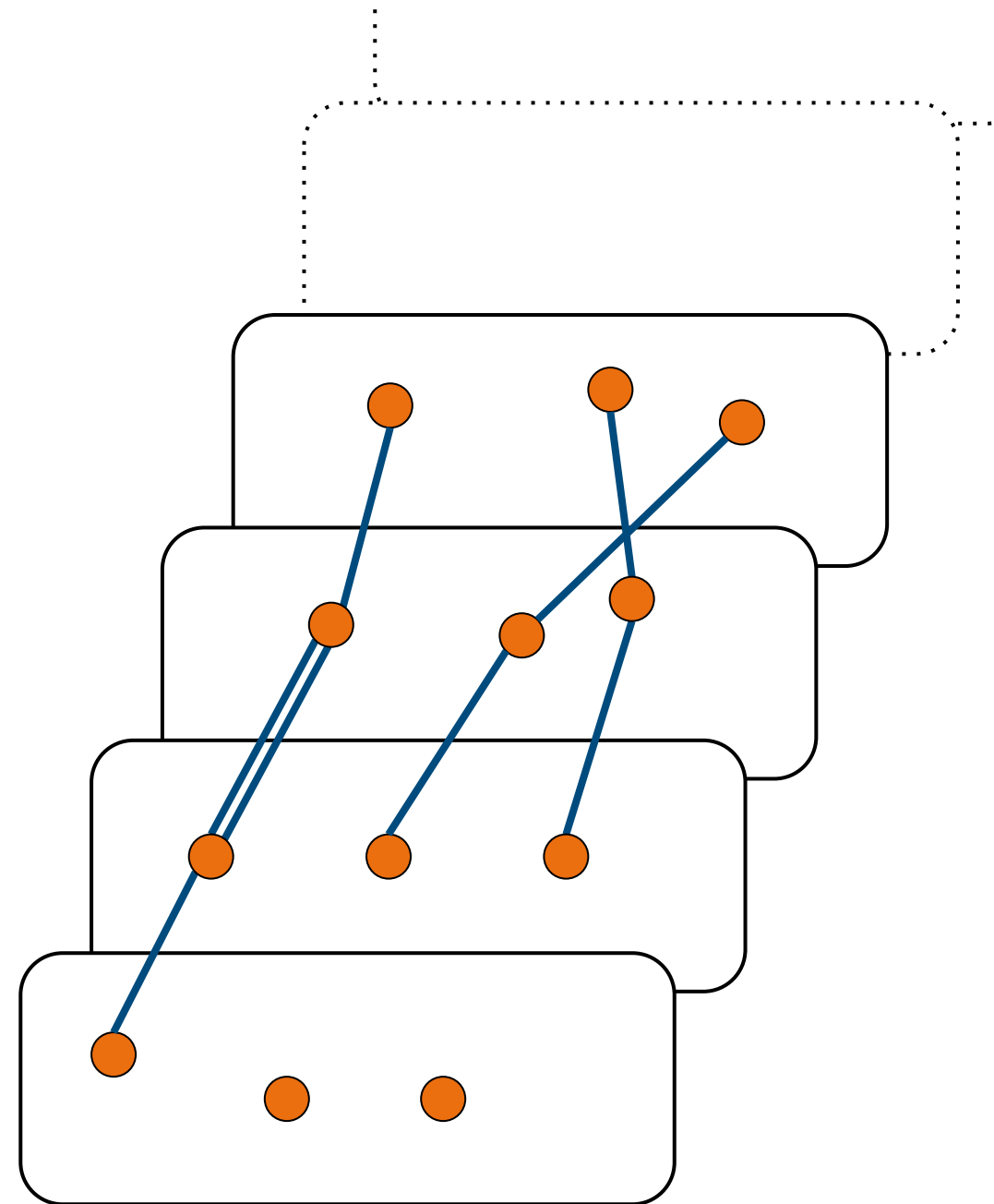
QUBO

$$\hat{H} = \sum_i^N \sum_{j<i} b_{ij} T_i T_j + \sum_{i=1}^N a_i T_i \quad (\text{QUBO})$$

- $T_i \in \{0, 1\}$
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- $\mathbf{v}_{\text{binary}}: [T_1, T_2, T_3, \dots, T_N] \rightarrow [0, 1, 1, \dots, 0]$

Ground state of the Hamiltonian

→ **optimal set of triplets**



QUBO

$$\hat{H} = \sum_i^N \sum_j^N b_{ij} T_i T_j + \sum_i^N a_i T_i \quad (\text{QUBO})$$

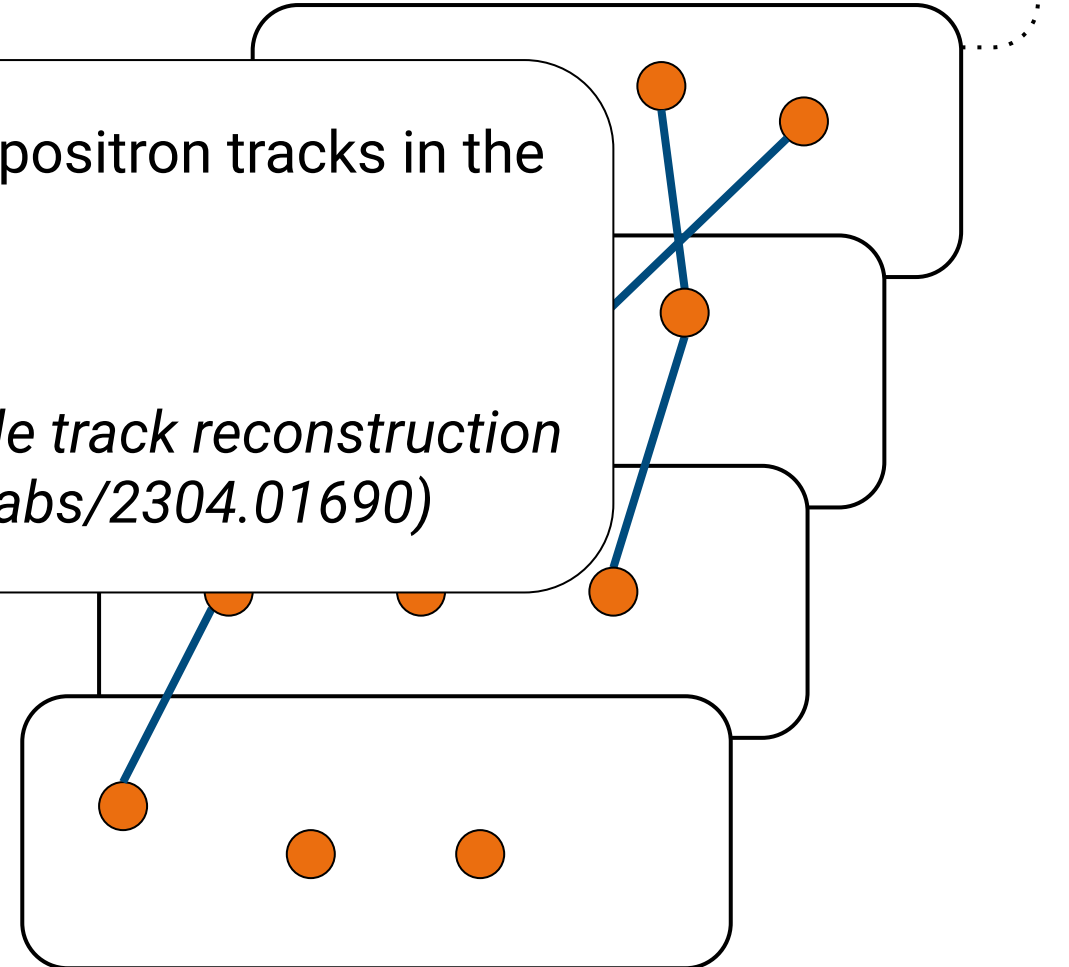
- $T_i \in \{0, 1\}$
- \mathbf{v} binary
- b_{ij} : int
- a_i : quantity

Approach investigated for reconstructing positron tracks in the Laser Und XFEL Experiment (LUXE):

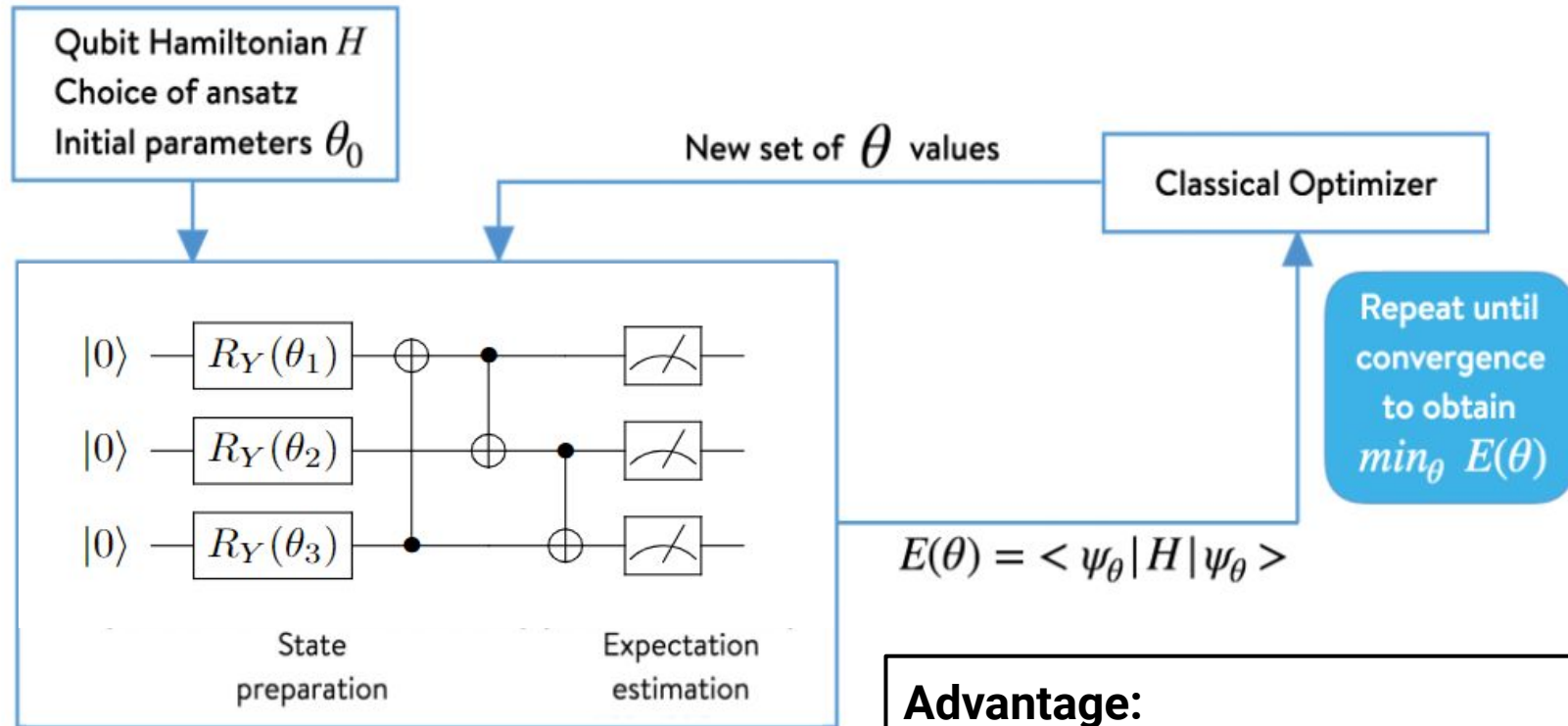
→ Yee Chinn Yap's talk

→ "Quantum algorithms for charged particle track reconstruction in the LUXE experiment" (<https://arxiv.org/abs/2304.01690>)

Minimise Hamiltonian → optimal set of triplets



VQE - Variational Quantum Eigensolver



Source: edited from <http://openqemist.1qbit.com/>

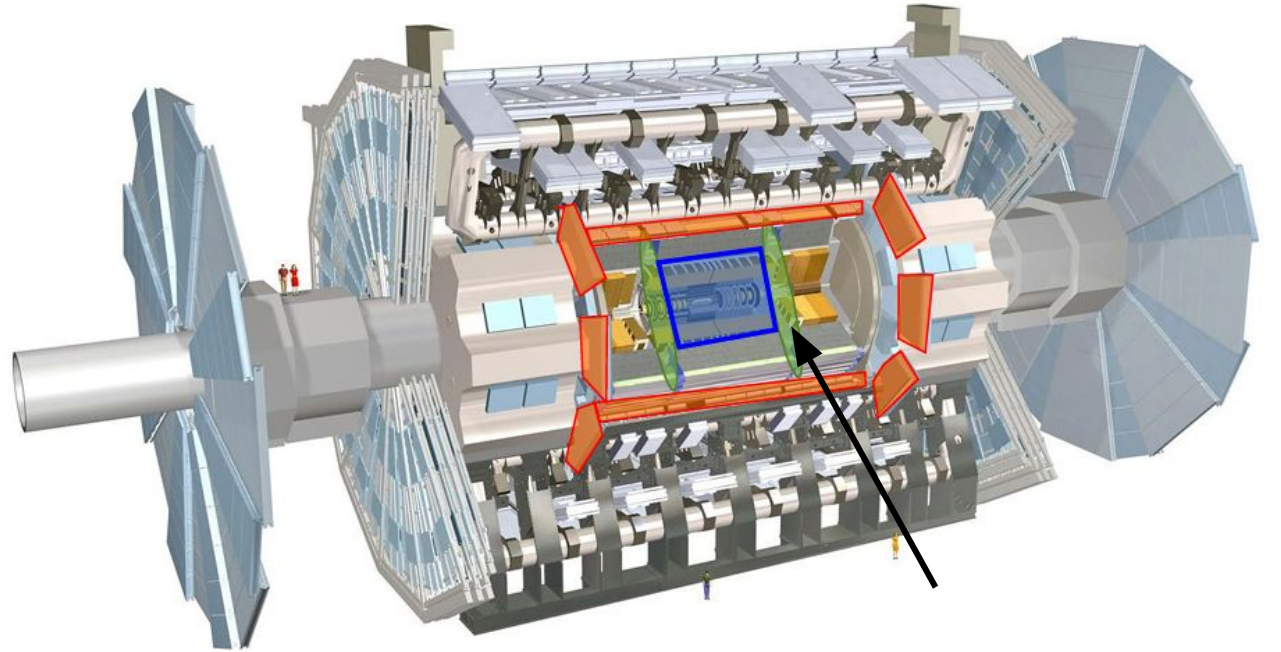
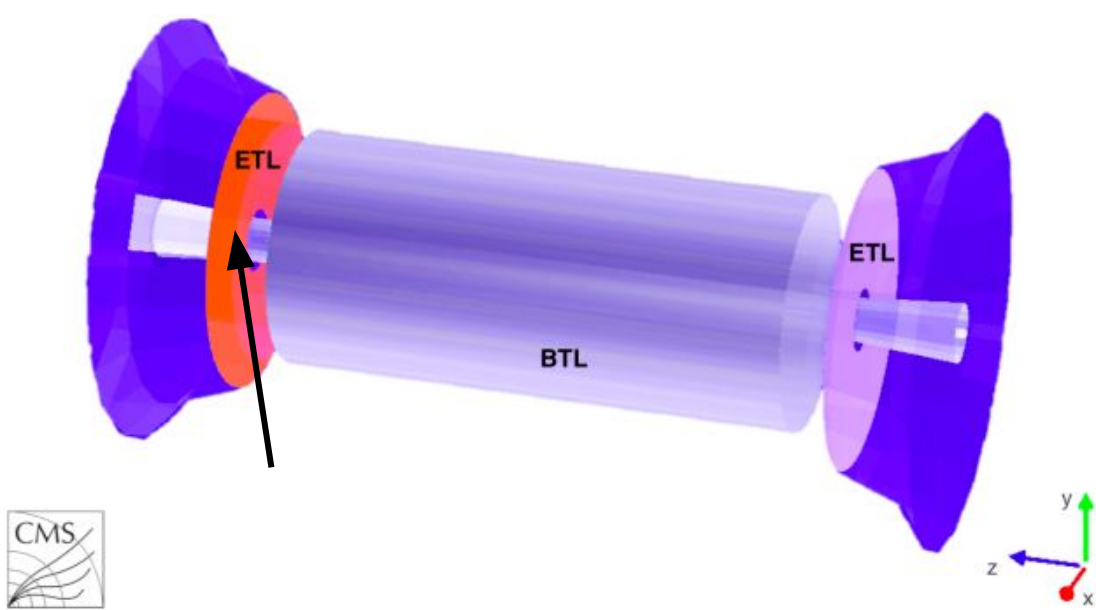
Advantage:

$\dim(H) = 2^n \times 2^n$, then $\langle \psi | H | \psi \rangle$ needs

- $O(2^{2n})$ operations classically
- $O(\text{Poly}(n))$ operations with a quantum computer

Timing information used for particle tracking

- Reduce background and sharpening resolution
- ATLAS: High Granularity Timing Detector
- CMS: Minimum Ionising Particle Detector



Source: <https://cds.cern.ch/record/2667167?ln=de>

Source: https://cds.cern.ch/record/2799535/files/Affolder-ATLAS_upgrade-v6.pdf

Timing information used for particle tracking

- Reduce background and sharpening resolution
- ATLAS: High Granularity Timing Detector
- CMS: Minimum Ionising Particle Detector
- Next generation of detectors will (probably) have timing in every layer

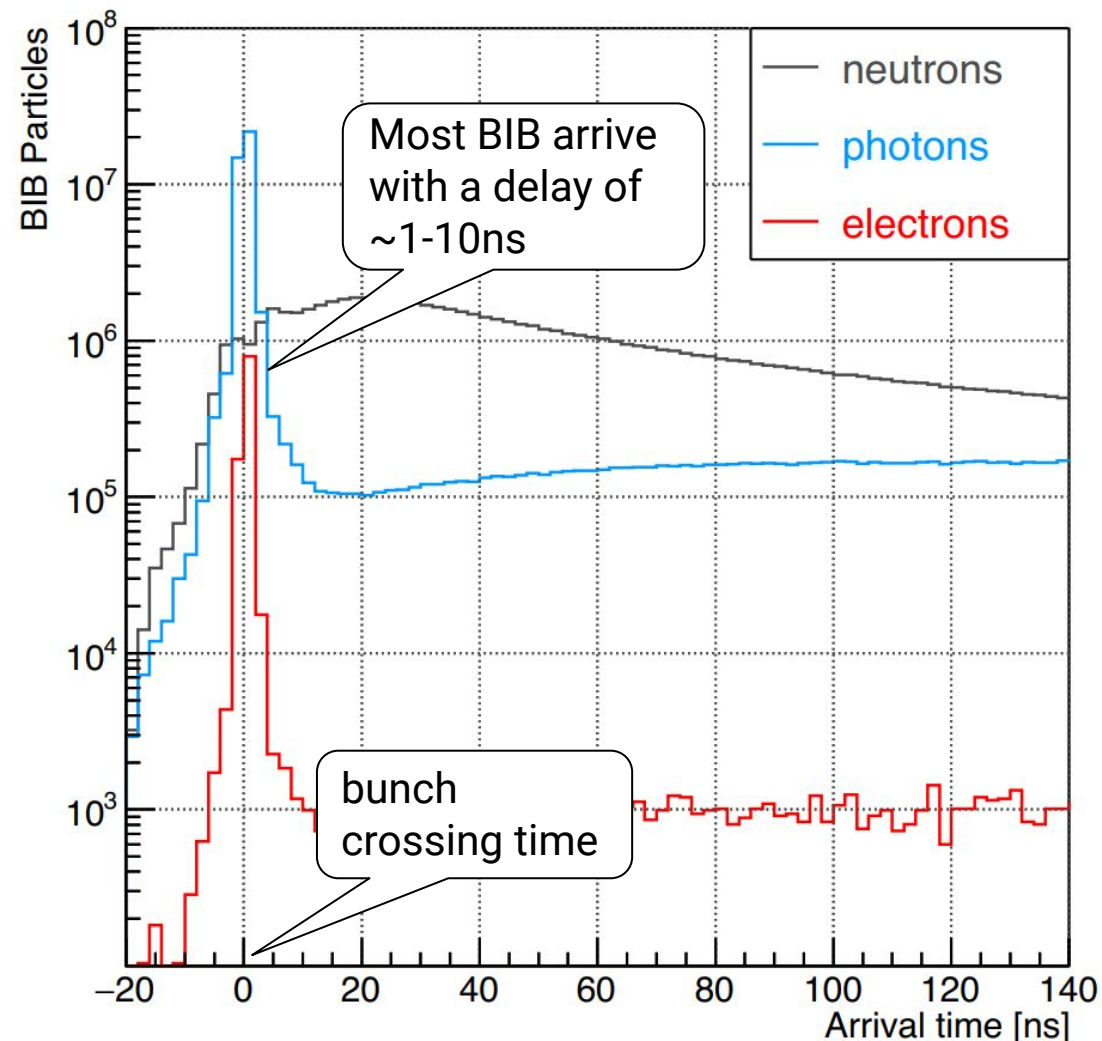
Pattern recognition in Muon Colliders

Beam muons decays induce secondary particle showers that reach the detector
(**B**eam-**I**nduced-**B**ackground)

Time information as a crucial component to suppress BIB particles

4D tracking with QUBO:

Include time information directly into pattern recognition



Source: <https://doi.org/10.1007/s41781-021-00067-x>

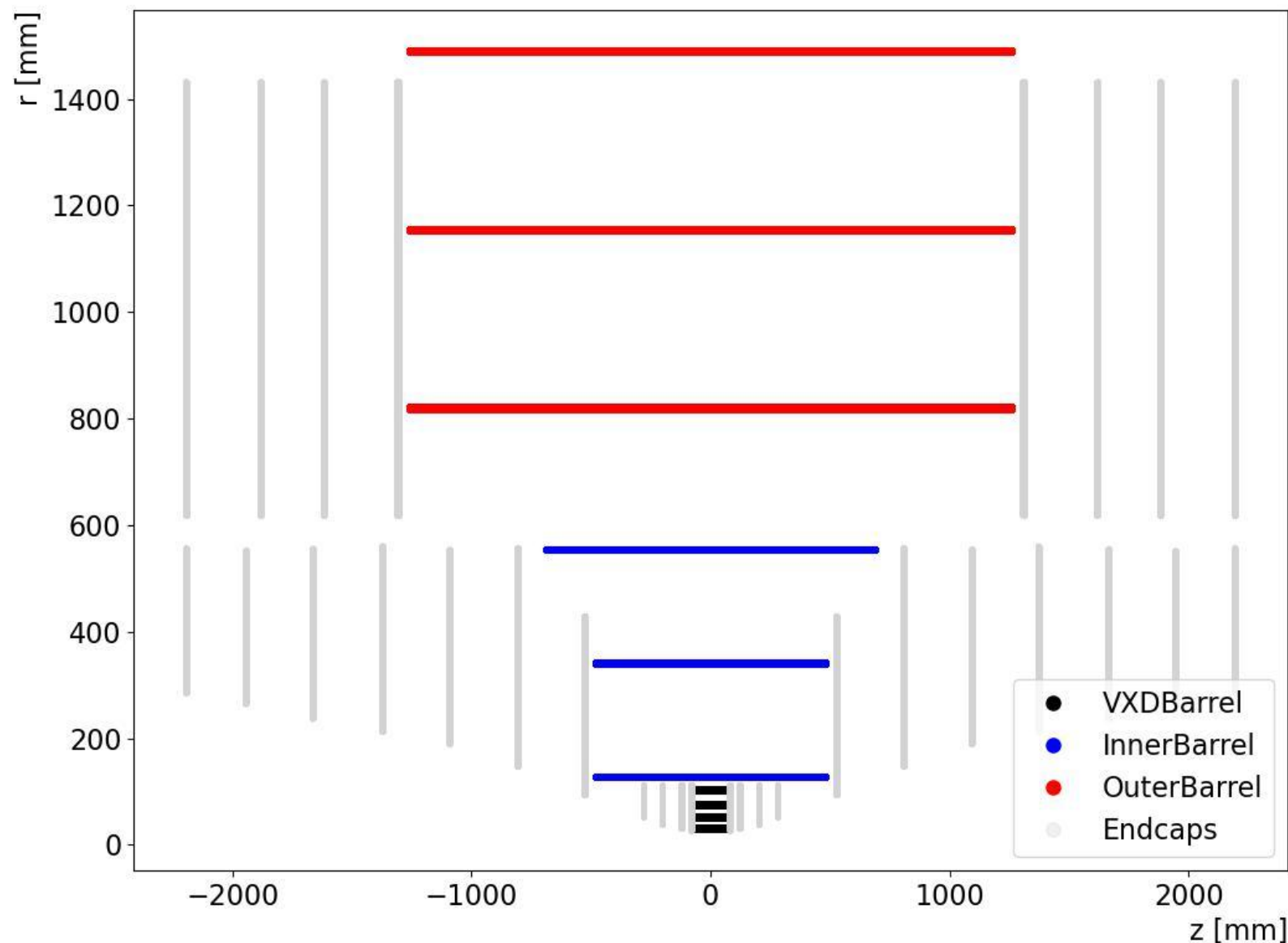
4D QUBO

$$\hat{H} = \sum_i^N \sum_{j<i} b_{ij} T_i T_j + \cancel{\sum_{i=1}^N a_i T_i}$$

Interaction $b_{ij, \text{total}}$:

- curvature
- scattering
- time

→ 4D modeling of interactions



Time component of b_{ij}

Raw time from data



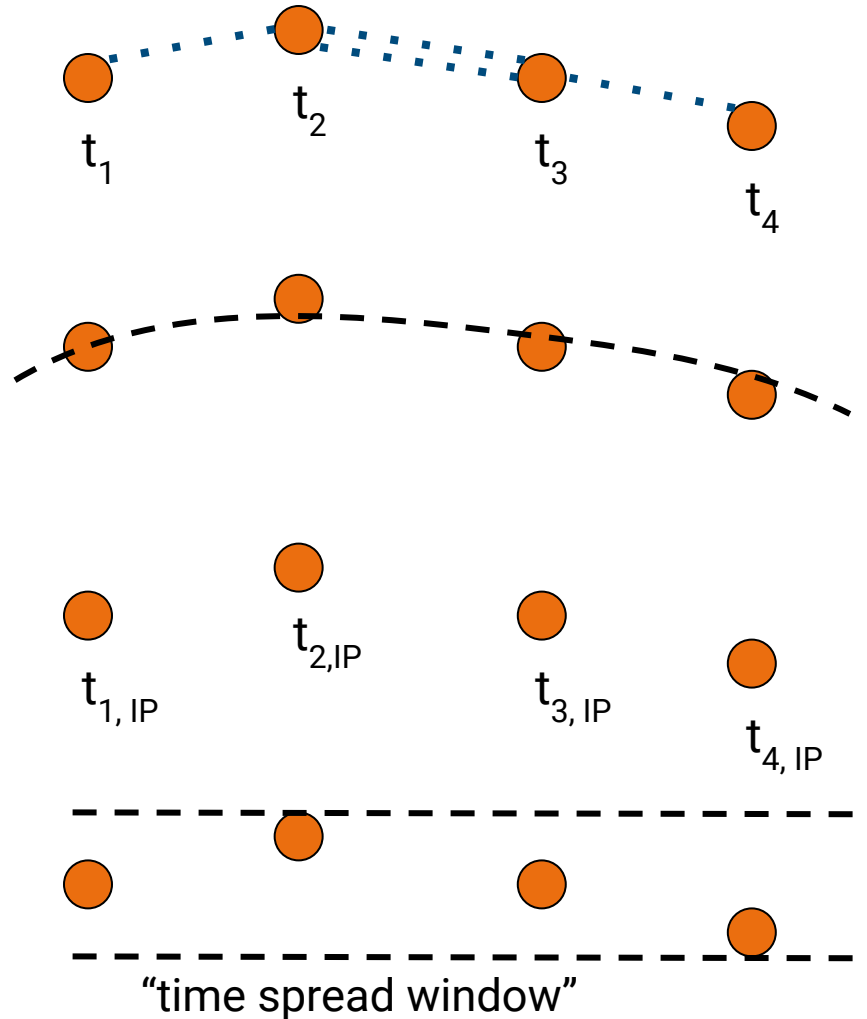
p_T / curvature



Time of hits at IP



Time compatibility



Time component of b_{ij}

Raw time from data



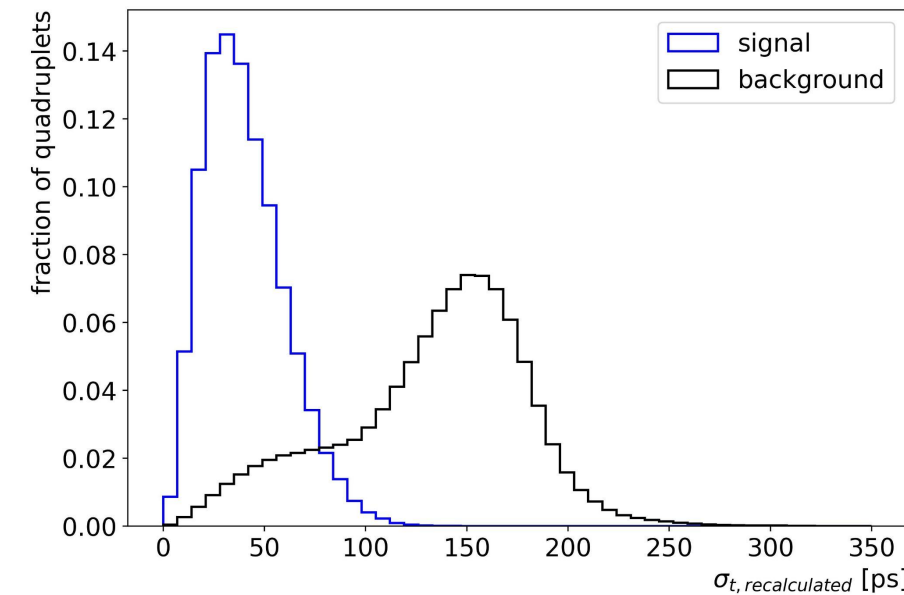
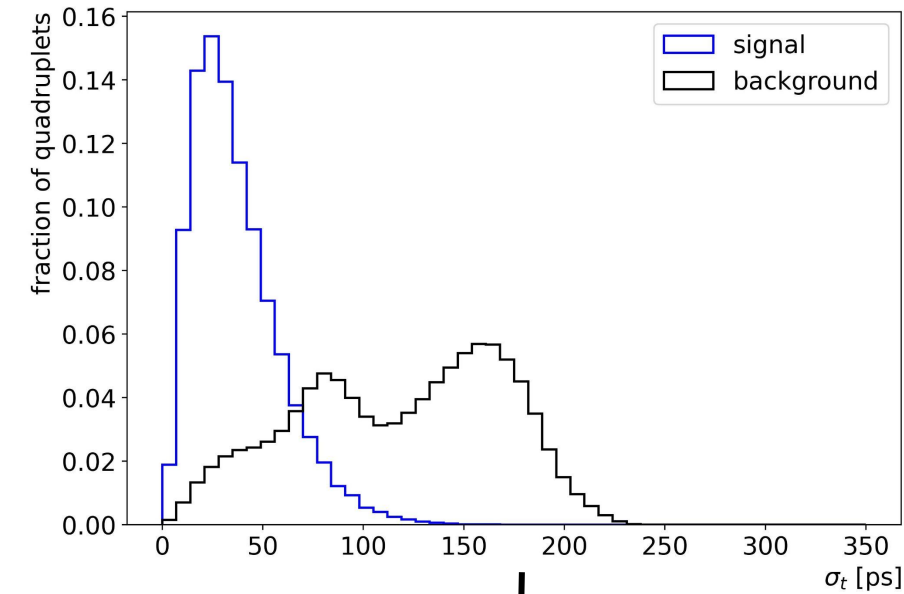
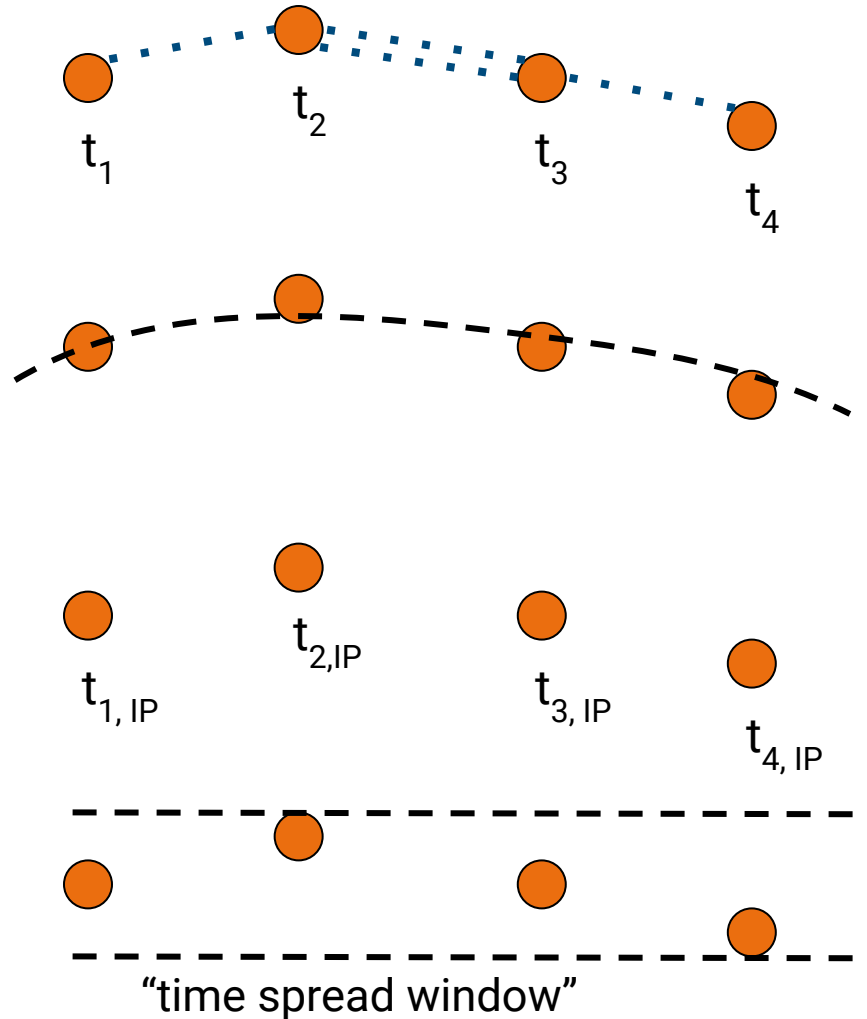
p_T / curvature



Time of hits at IP



Time compatibility



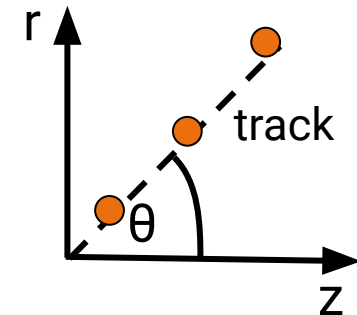
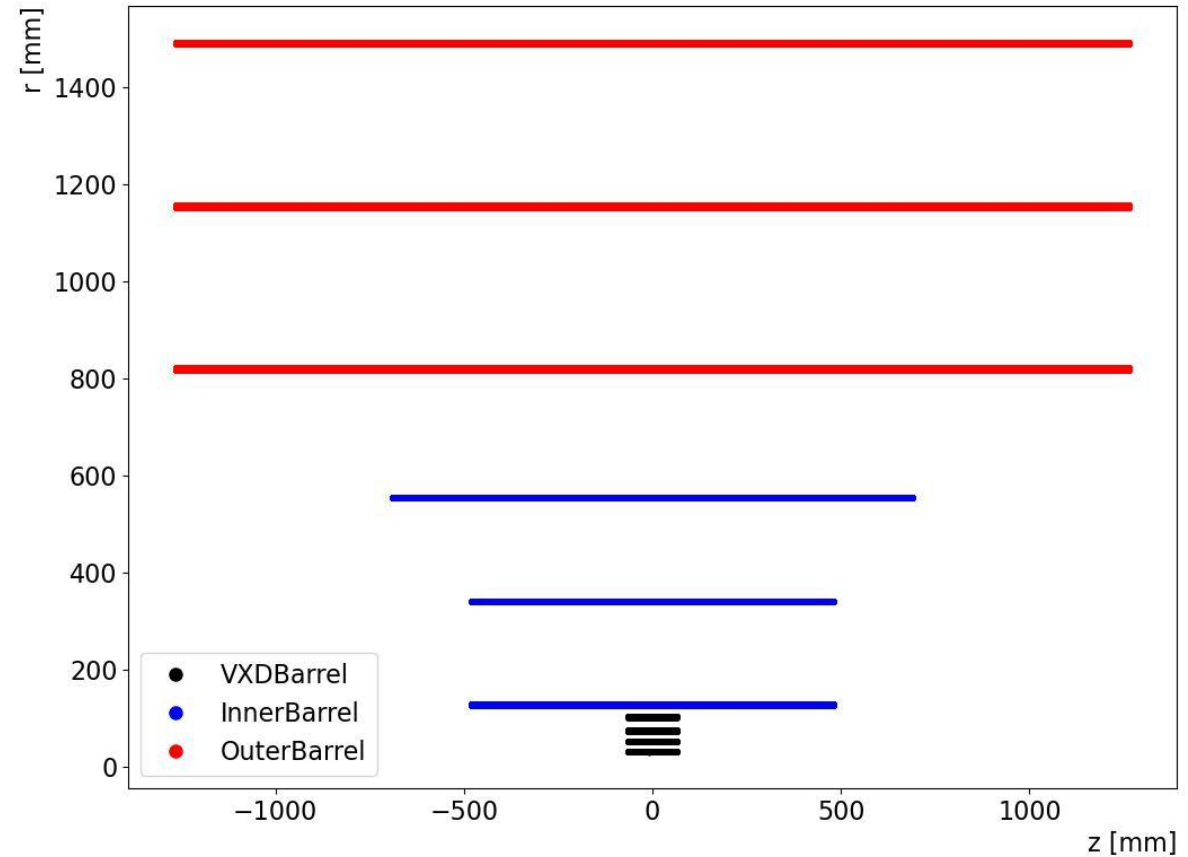
Single muon track within a large BIB

Pre-selection + QUBO coefficients

- Signal-only events to determine pre-selection values
- QUBO coefficients studied on single muon events overlaid with BIB

Tracking:

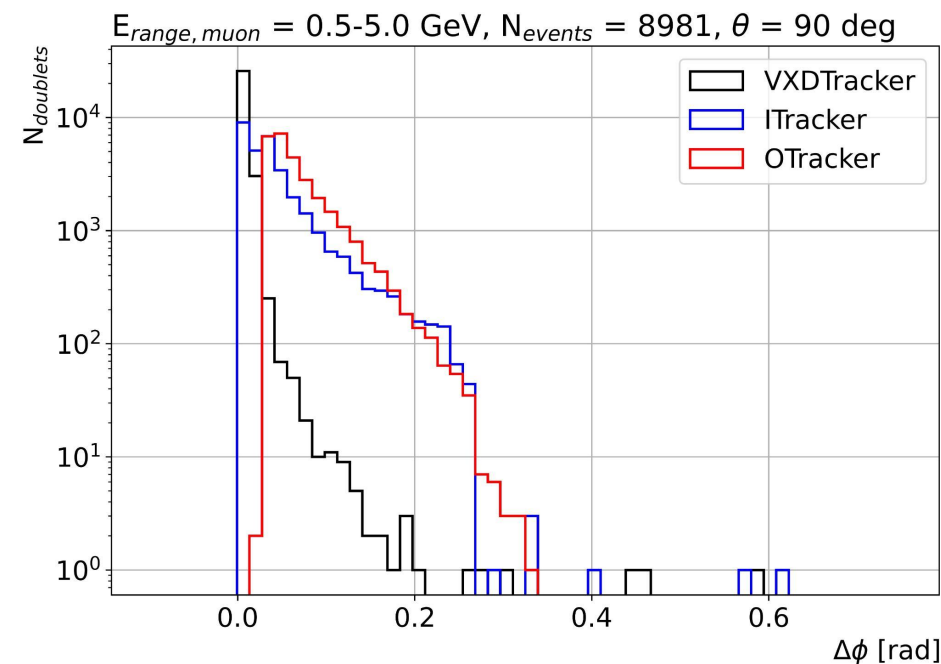
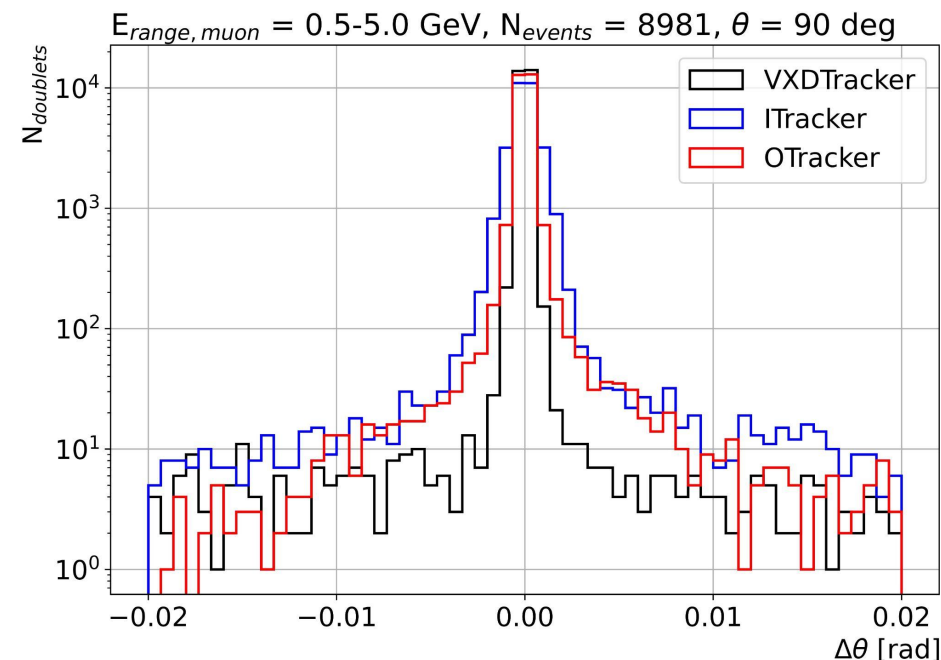
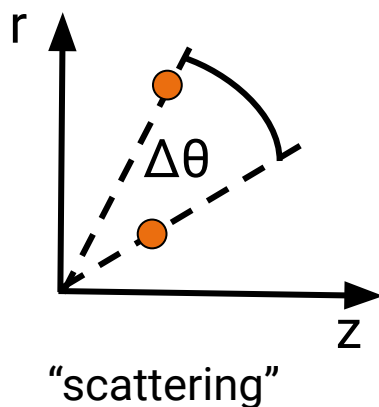
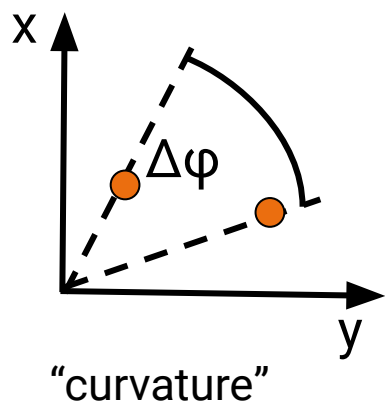
- Focus on barrel region
- $O(10^6)$ background hits
- $\theta = 90^\circ$, $\varphi \in [0, 2\pi]$



Preselection

Pre-selection

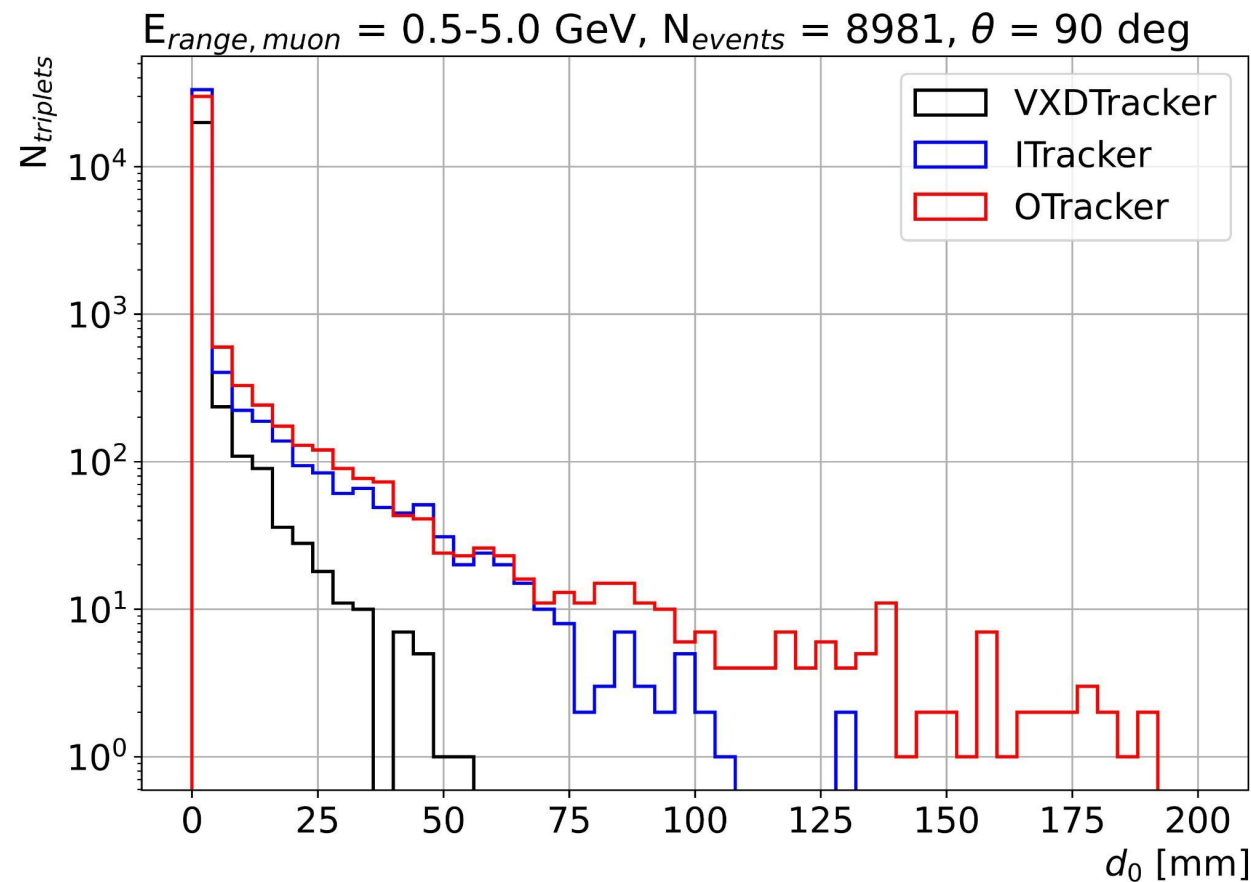
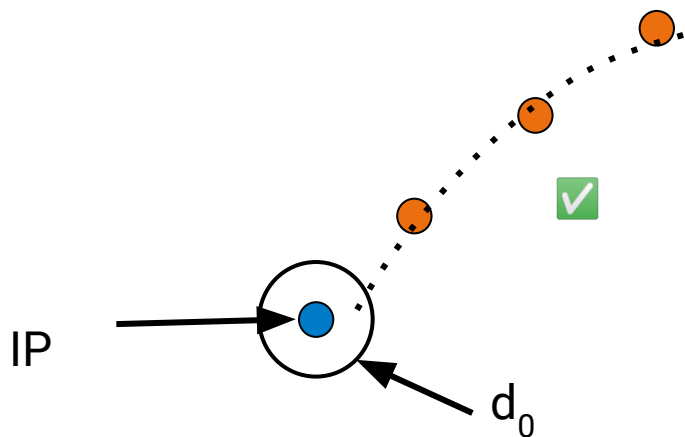
- **Doublet** pre-selection on $\Delta\theta$ and $\Delta\phi$



Preselection

Pre-selection

- **Doublet** pre-selection on $\Delta\theta$ and $\Delta\varphi$
- **Triplet** pre-selection on trajectories having a small $|d_0|$ w.r.t. the IP



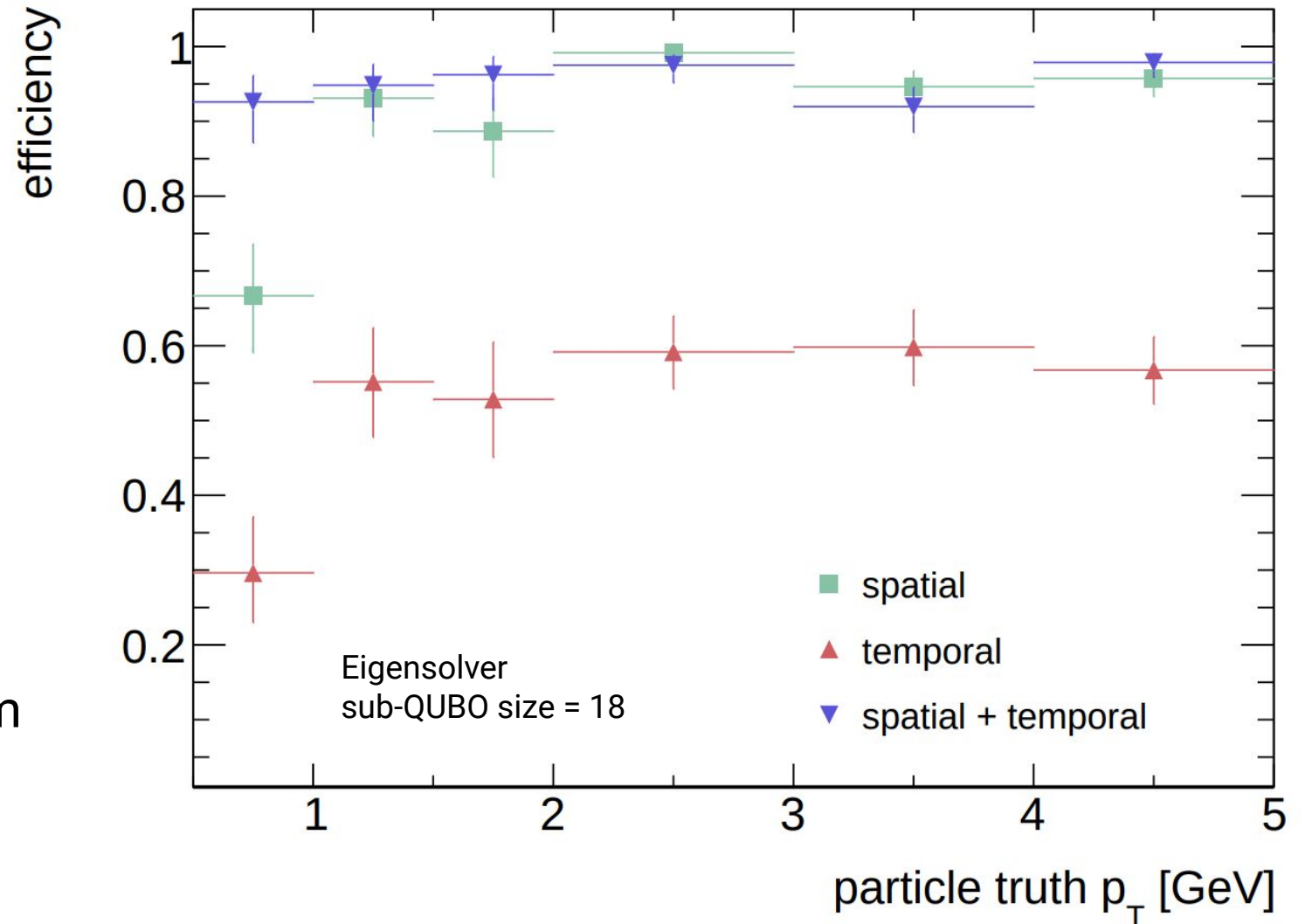
Efficiency vs. p_T

Reconstruction mode

- Pattern building in a θ -slice around muon track

Track selection

- At least 6 hits in a row
- Matched if majority of hits from signal else fake



Summary

- First implementation of a 4D-QUBO is in place
- Focus on barrel region of the Muon Collider detector
- Adding time information to the QUBO parameters b_{ij} is likely to improve track reconstruction efficiency especially at low p_T

Thank You!

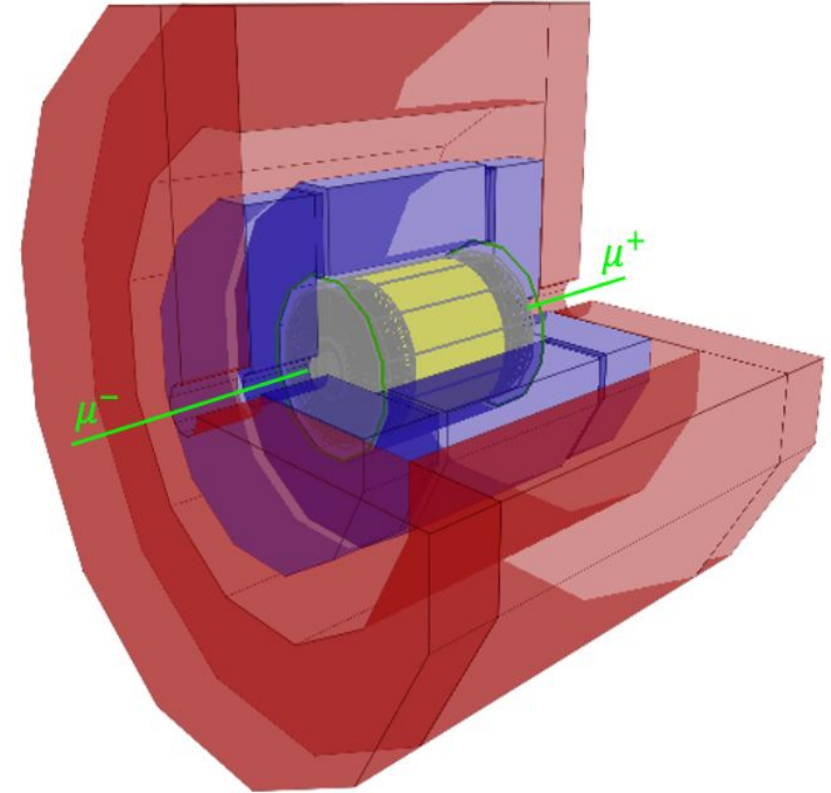
Next steps

- Performance vs θ , additionally including endcap regions
- Optimise QUBO parameter modelling, e.g. weighting of time/spatial parts
- Optimise track selection and fitting, e.g. number of hits required:
 χ^2 , p_T reconstruction...
- Number of fake tracks per event before / after χ^2

Muon Collider

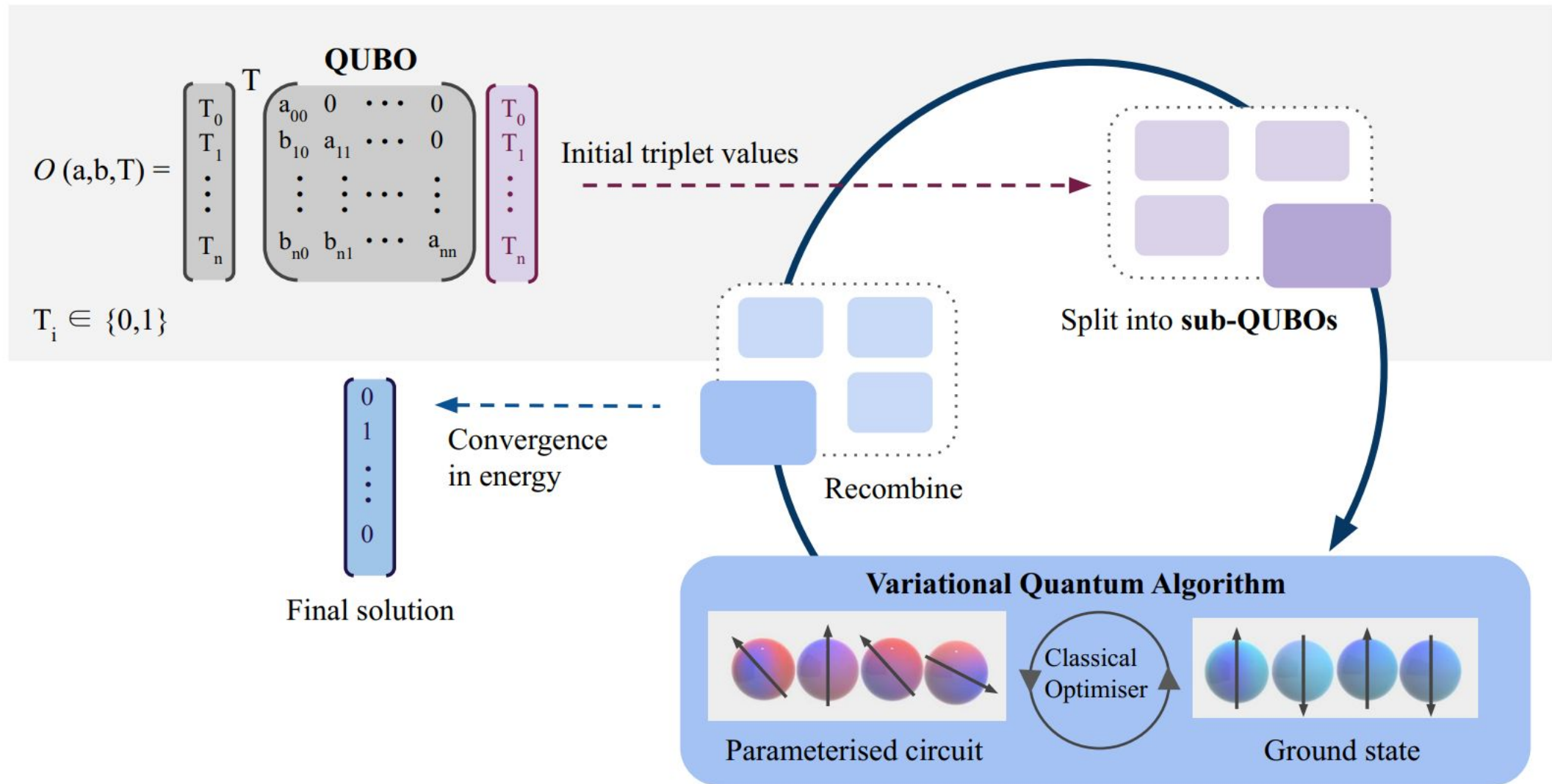
Why Muon Colliders?

- Muons are heavier than electrons
→ higher energy reach, less synchrotron radiation,
- Higgs precision measurements
- Complementary research on pp and e^+e^- colliders



Source: <https://muoncollider.web.cern.ch>

Sub-QUBOs



Source: <https://arxiv.org/pdf/2304.01690.pdf>

Appendix: QUBO parameter settings

Trivial

- -1 if connection possible

compatible curvature: $c=1$
contrary curvature: $c=2$

Spatial

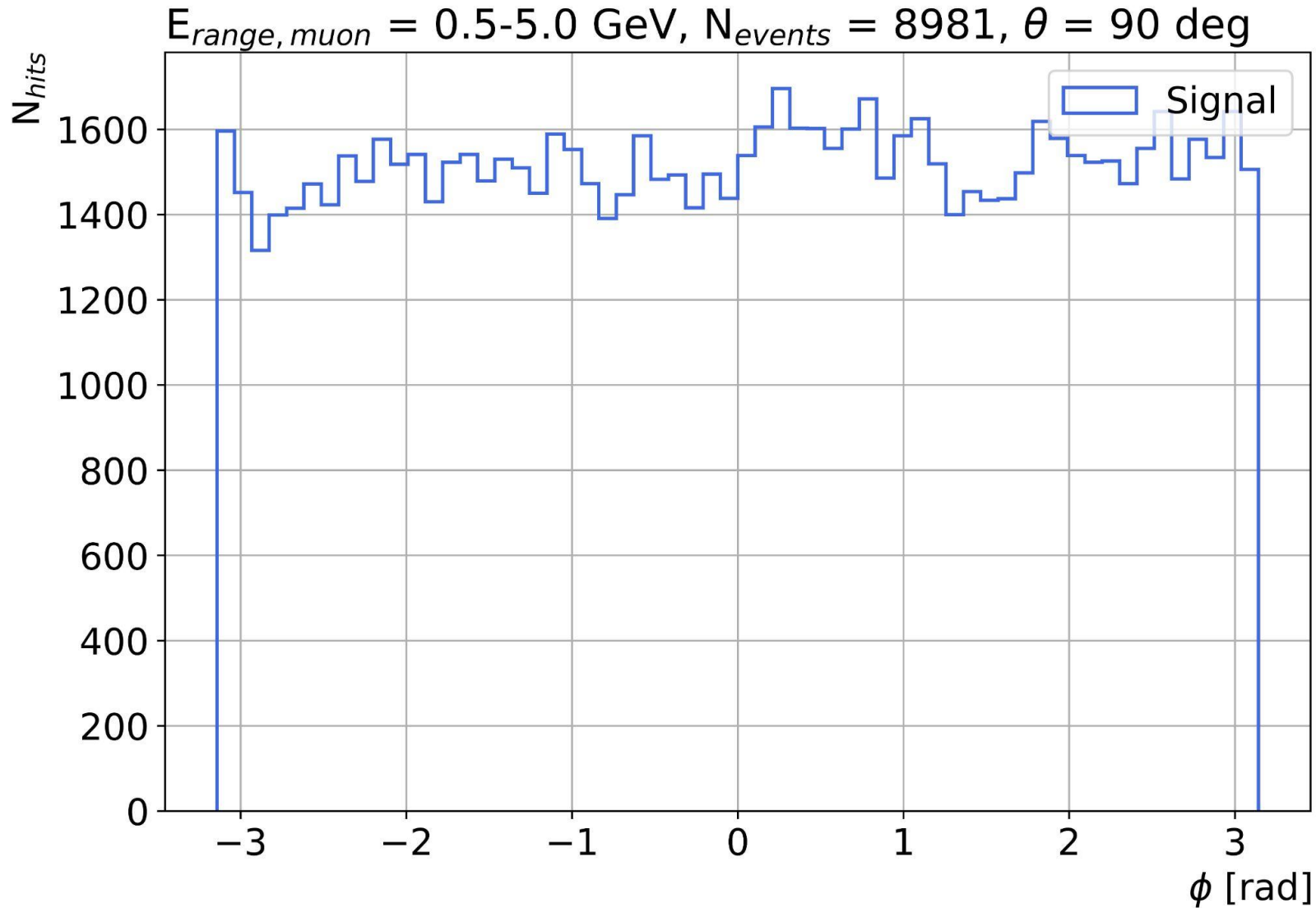
- $f(q/p_T) : 0.5 \cdot (c - \min([pT_{\text{triplet } 1} \ pT_{\text{triplet } 2}]) / \max([pT_{\text{triplet } 1} \ pT_{\text{triplet } 2}])) \rightarrow [0, 1]$
- $\max(\Delta\theta / 0.01) \rightarrow [0, 1]$
- average of both is spatial value

Temporal

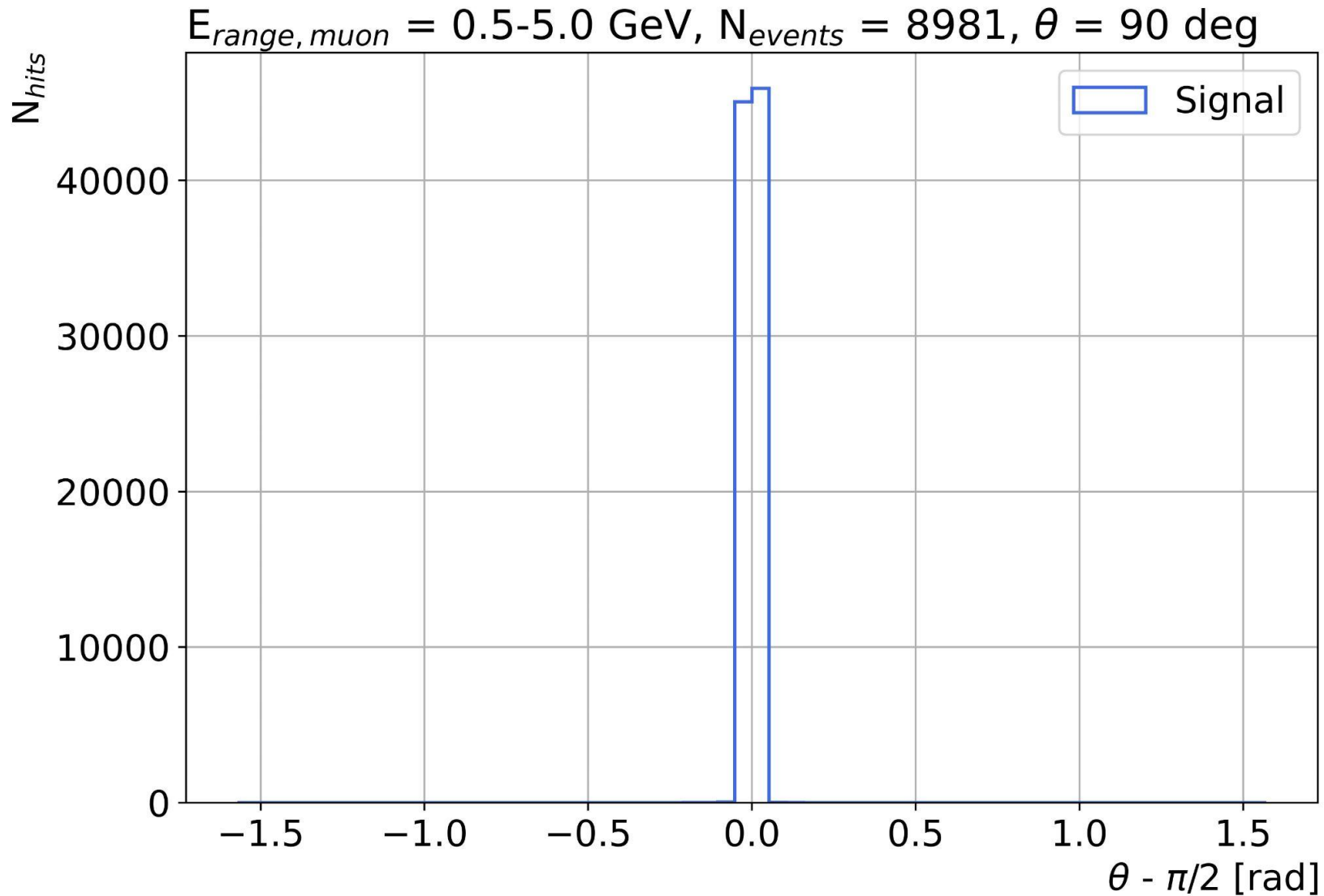
- $\min(\sigma(t_{\text{hits}}) / 250 \text{ [ps]}, 1) \rightarrow [0, 1]$

Connections are rescaled
to be inside $[-1.0, -0.9]$

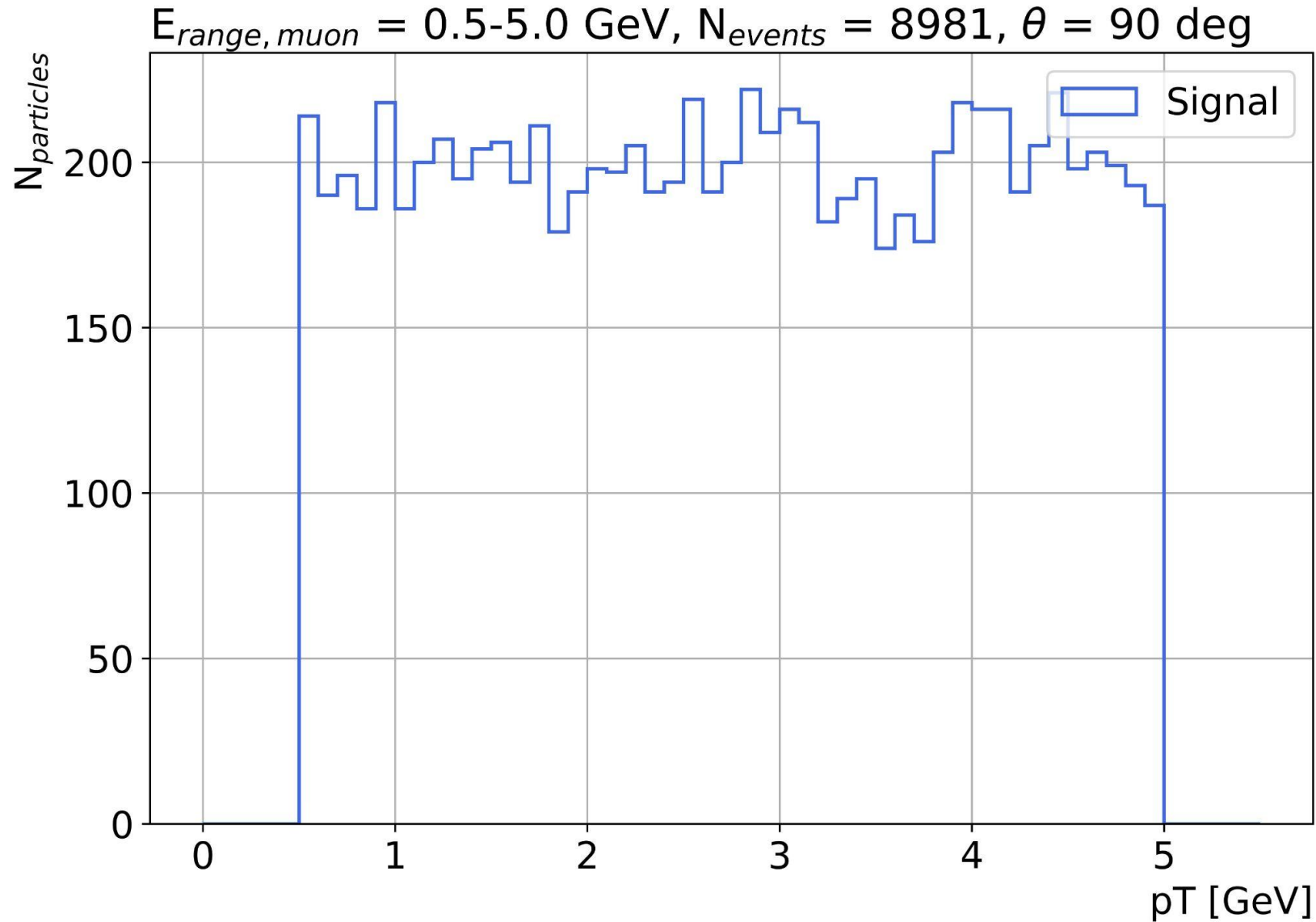
Appendix: Signal only - ϕ



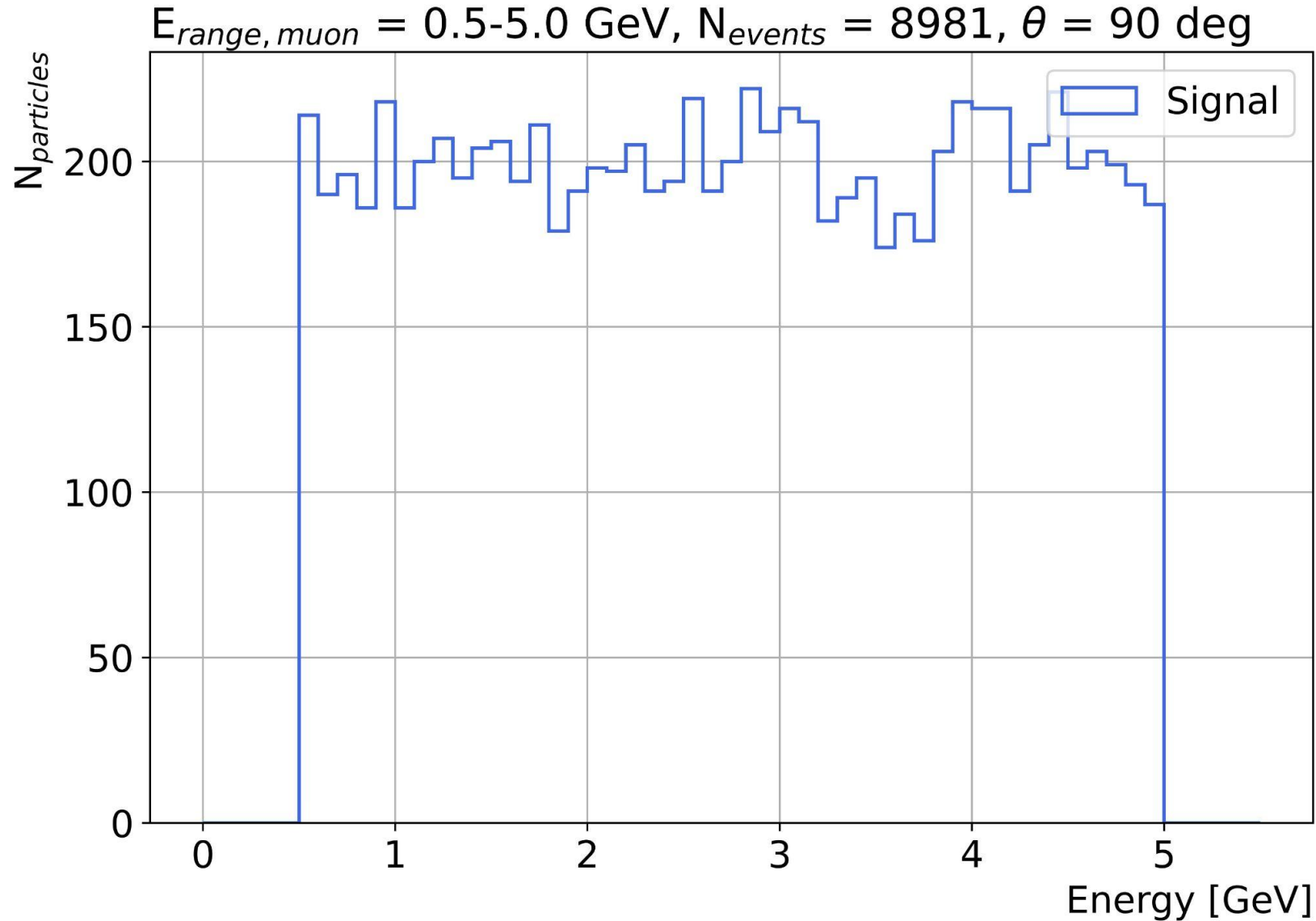
Appendix: Signal only - θ



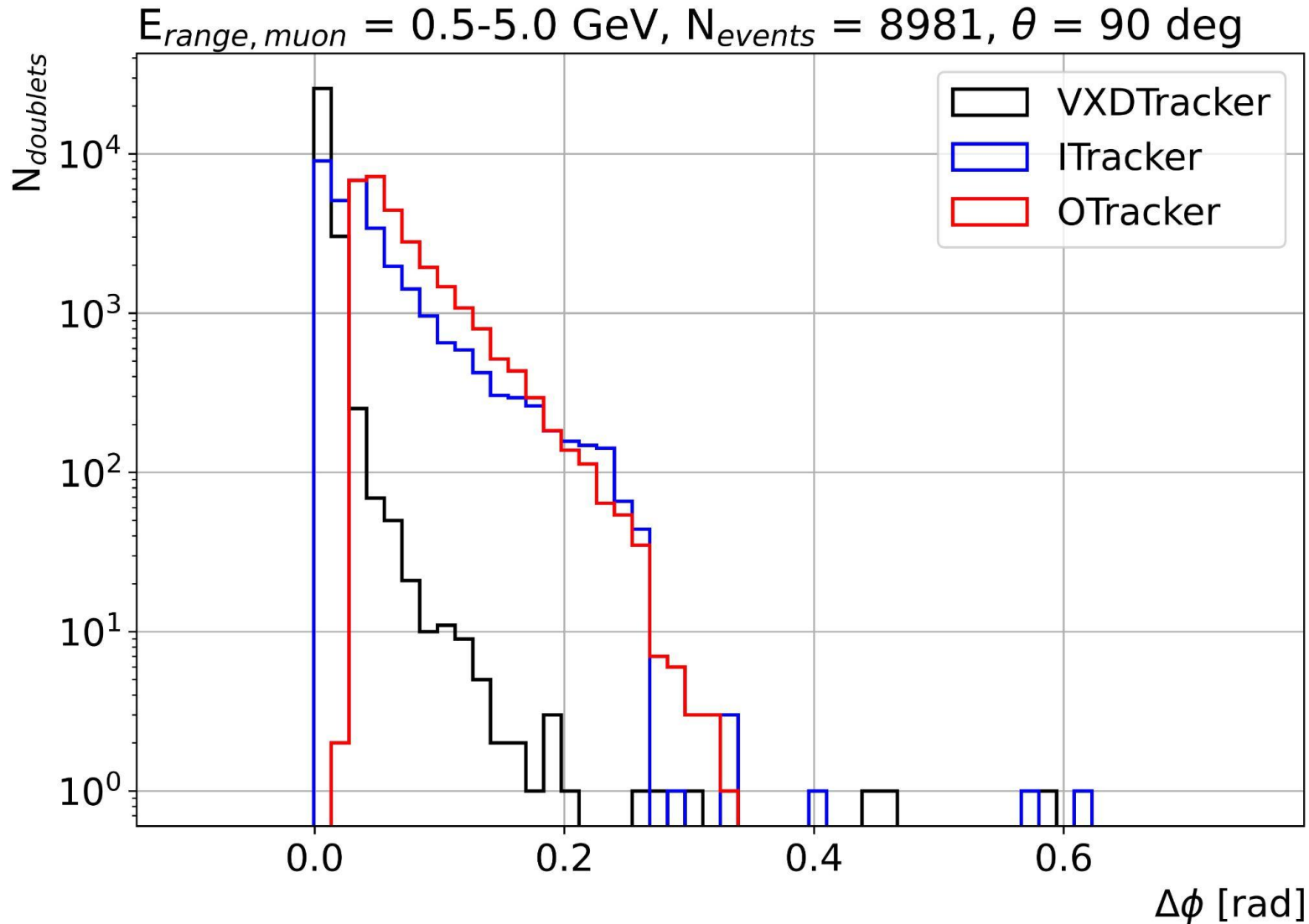
Appendix: Signal only - p_T



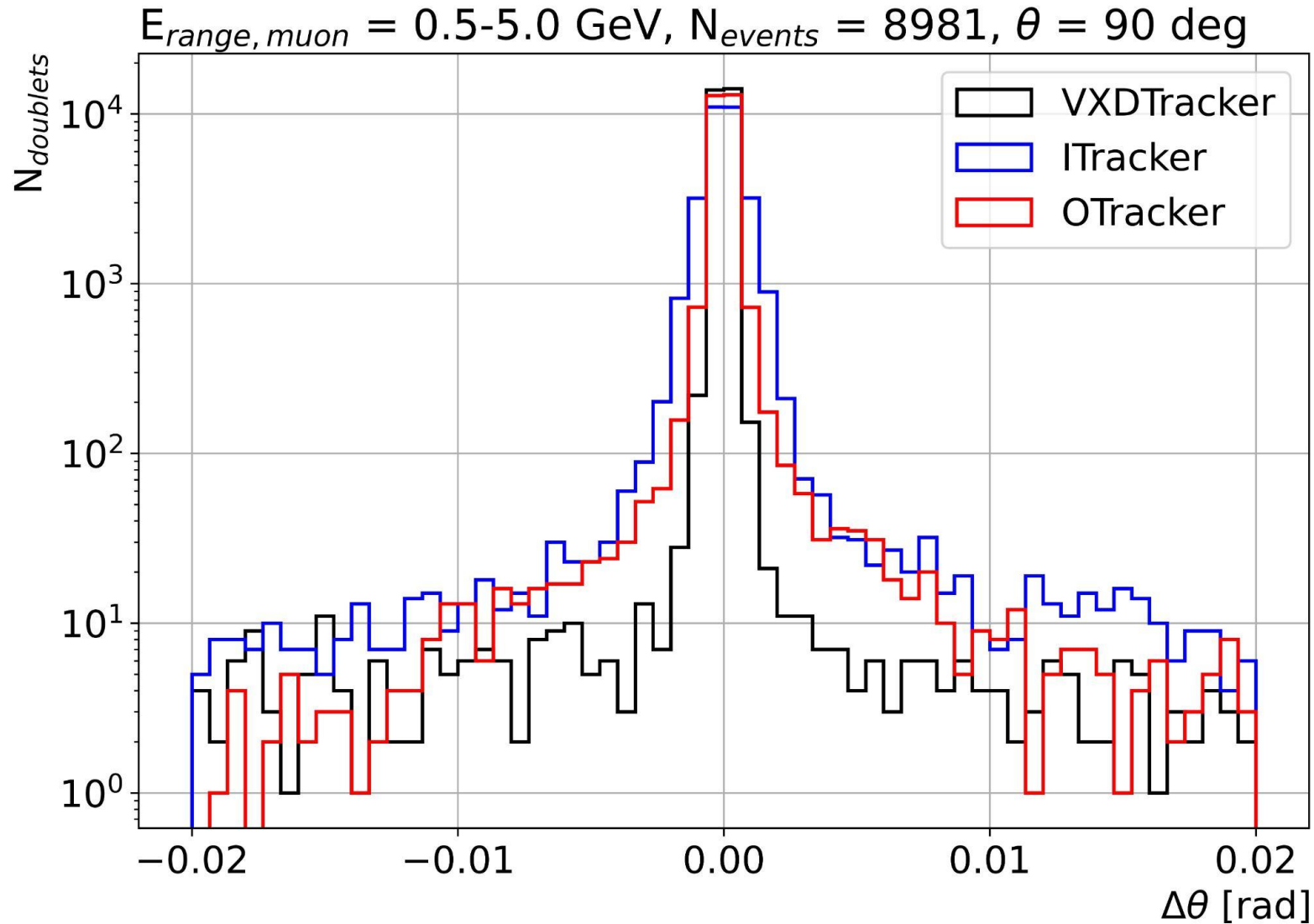
Appendix: Signal only - energy



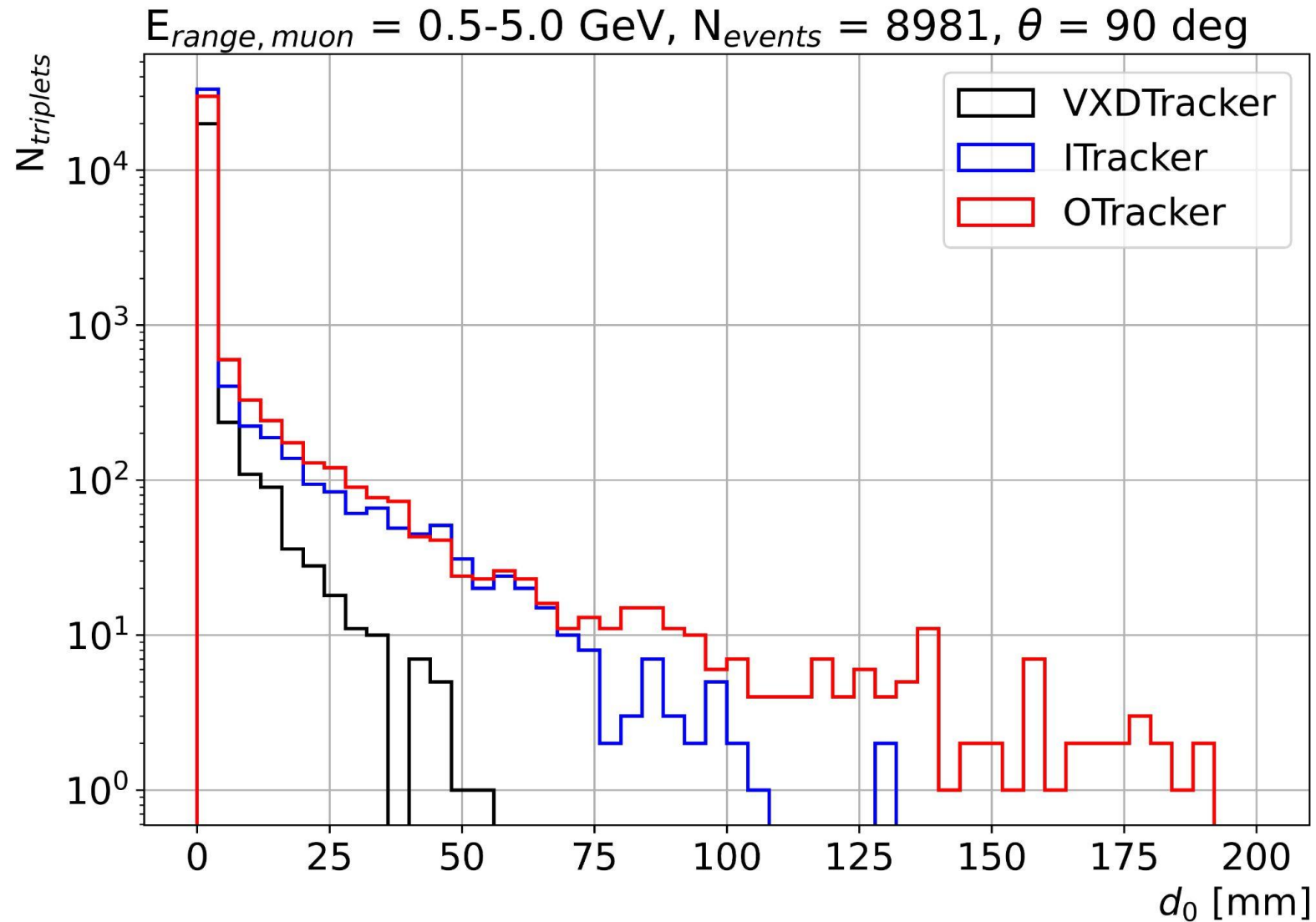
Appendix: Signal only - $\Delta\phi$



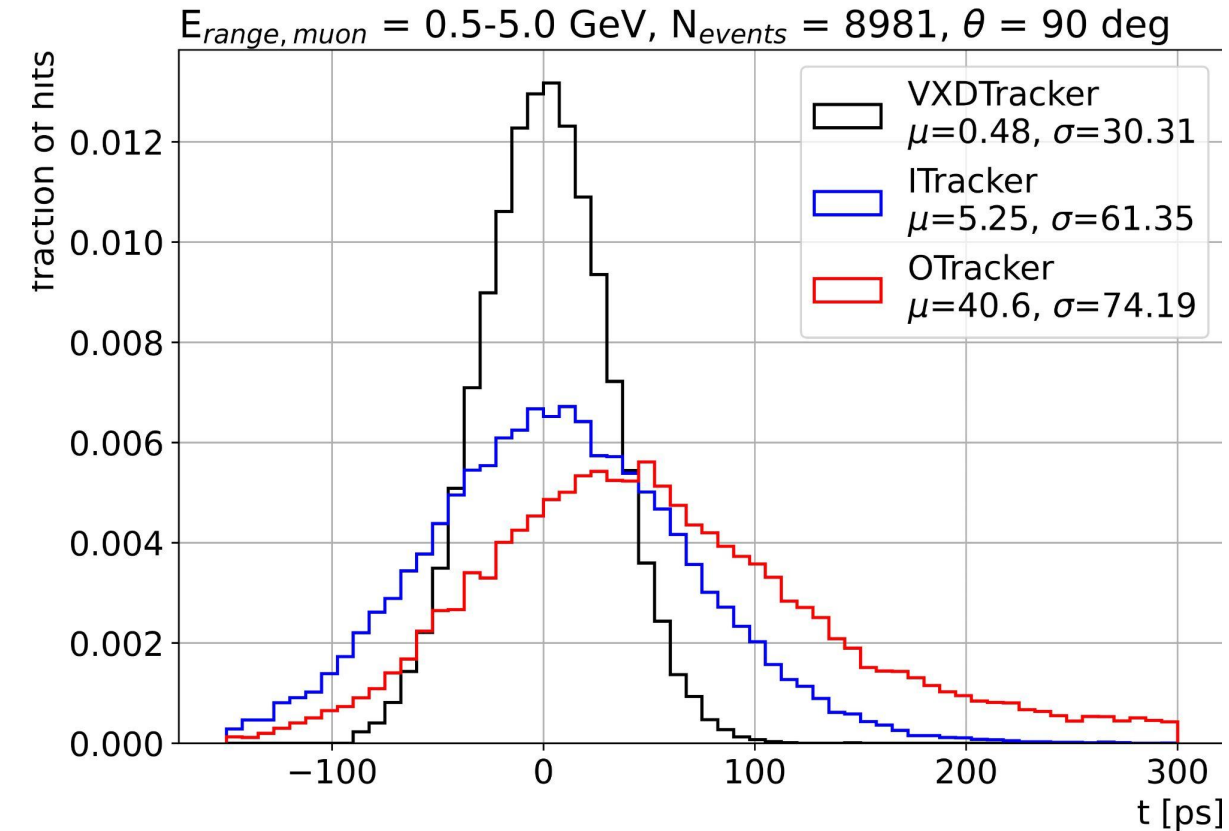
Appendix: Signal only - $\Delta\theta$



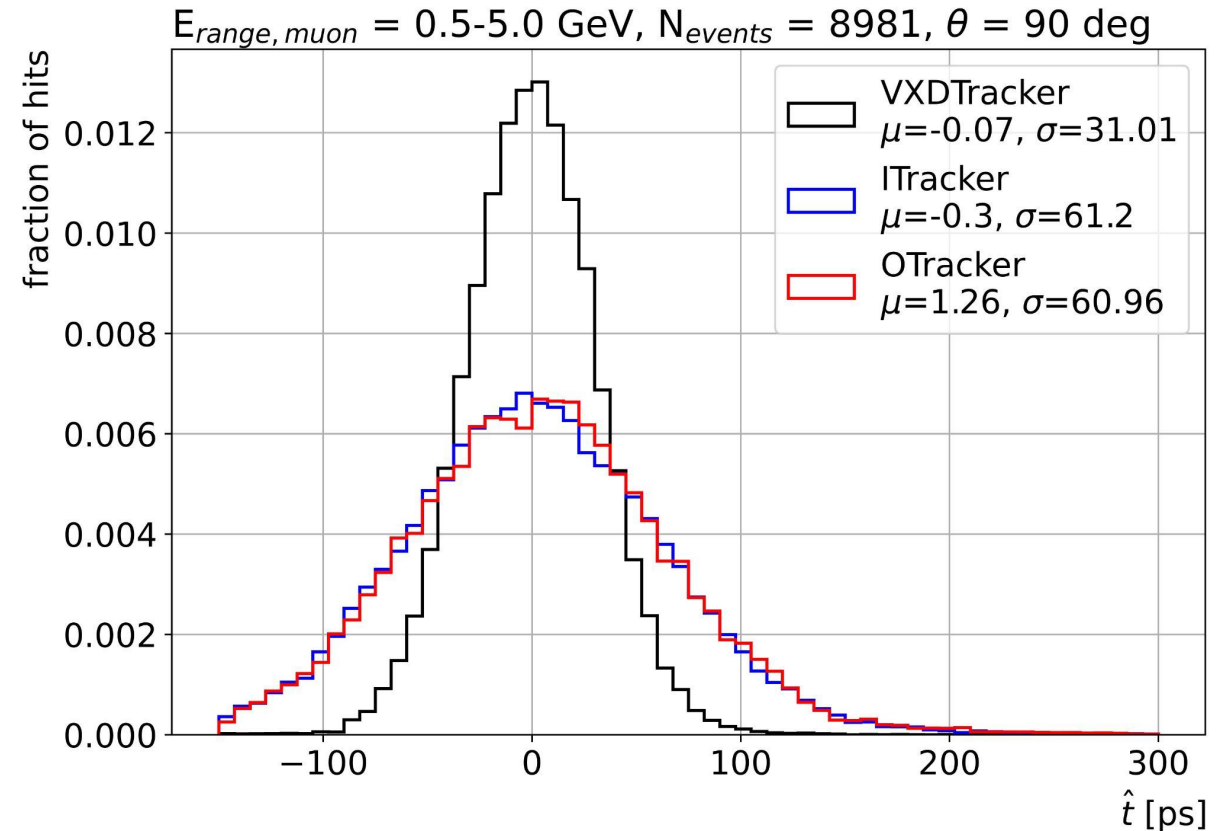
Appendix: Signal only - d_0



Appendix: Signal only - t_{hits}

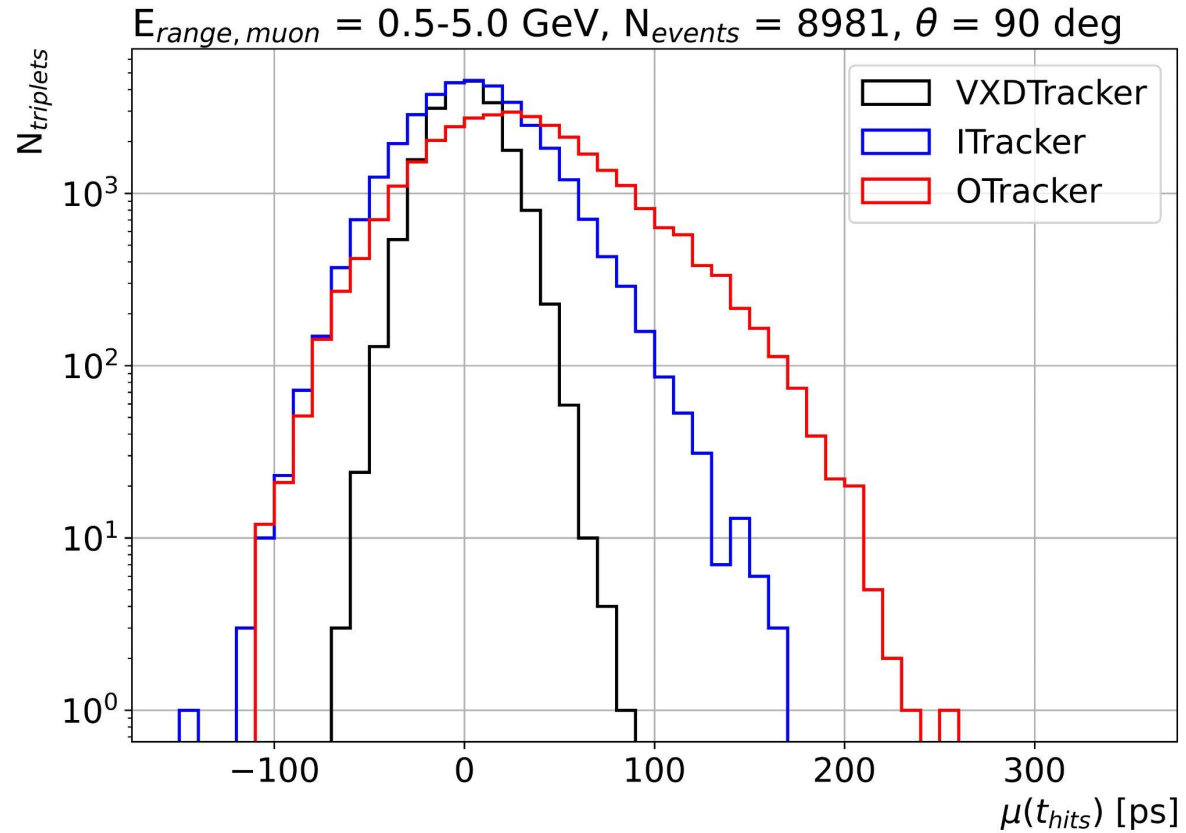


$t - \text{tof}_{\text{photon}}$

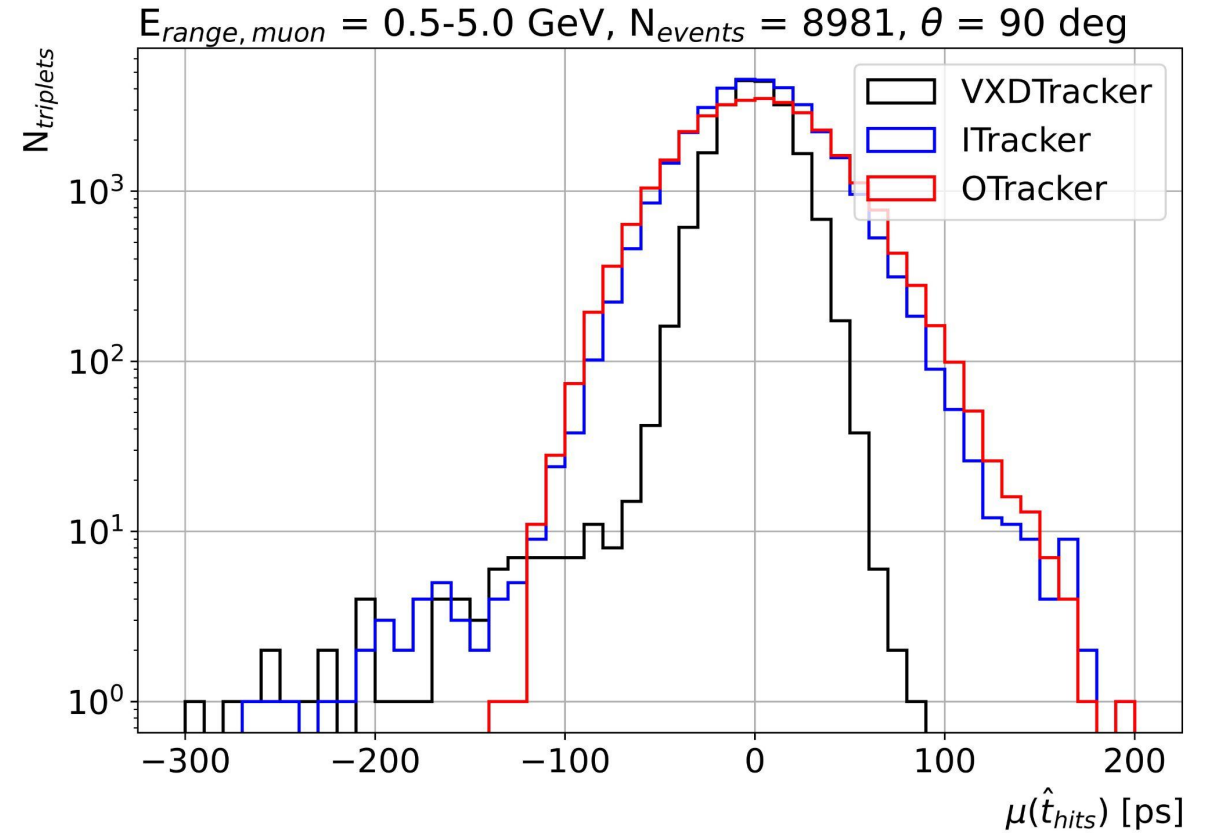


$t - \text{tof}_{\text{curvature}}$

Appendix: Signal only - $\mu(t_{\text{hits, triplet}})$

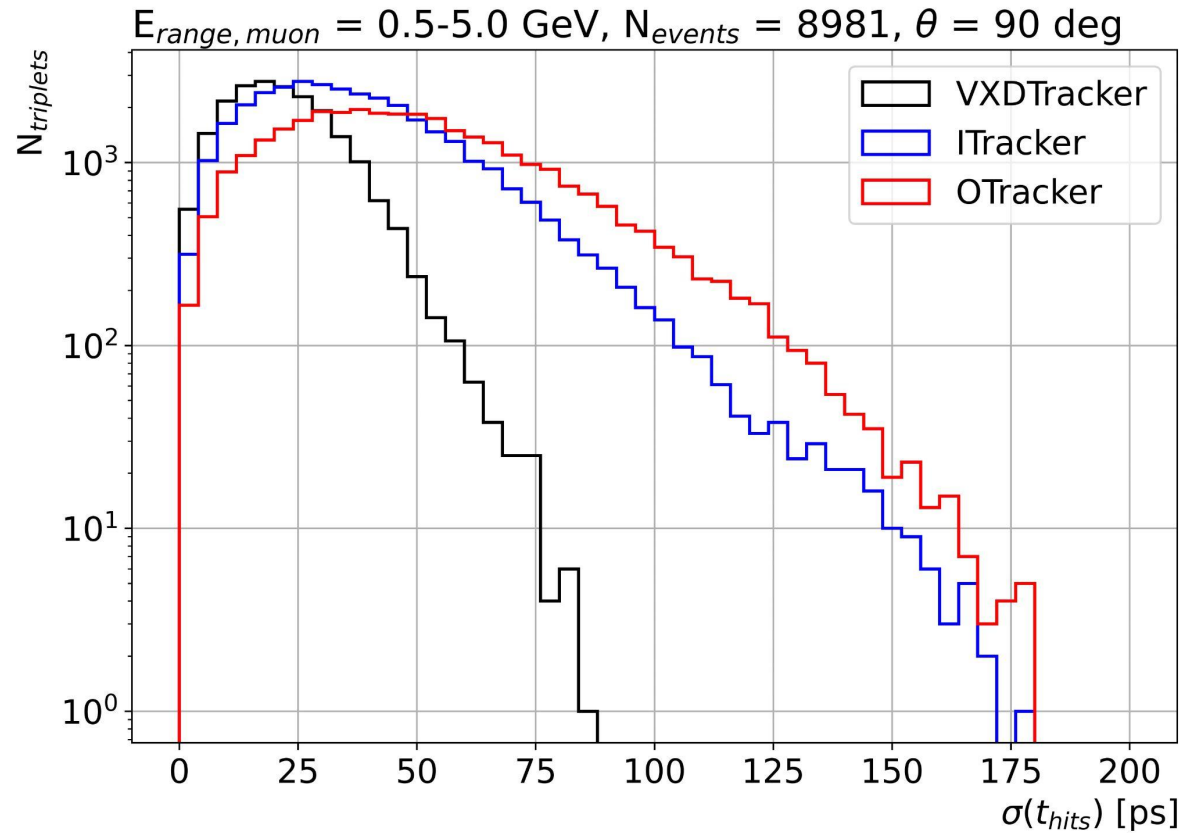


t - tof_{photon}

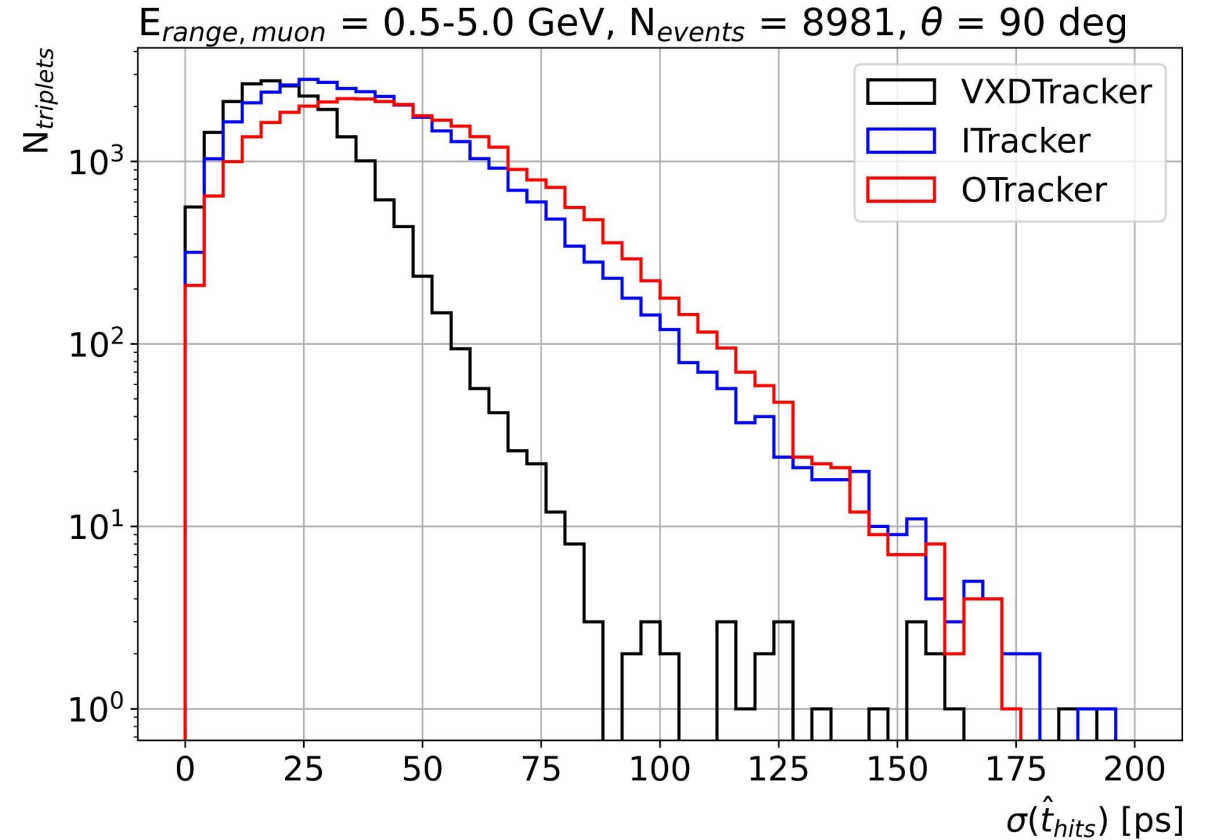


t - tof_{curvature}

Appendix: Signal only - $\sigma(t_{\text{hits, triplets}})$

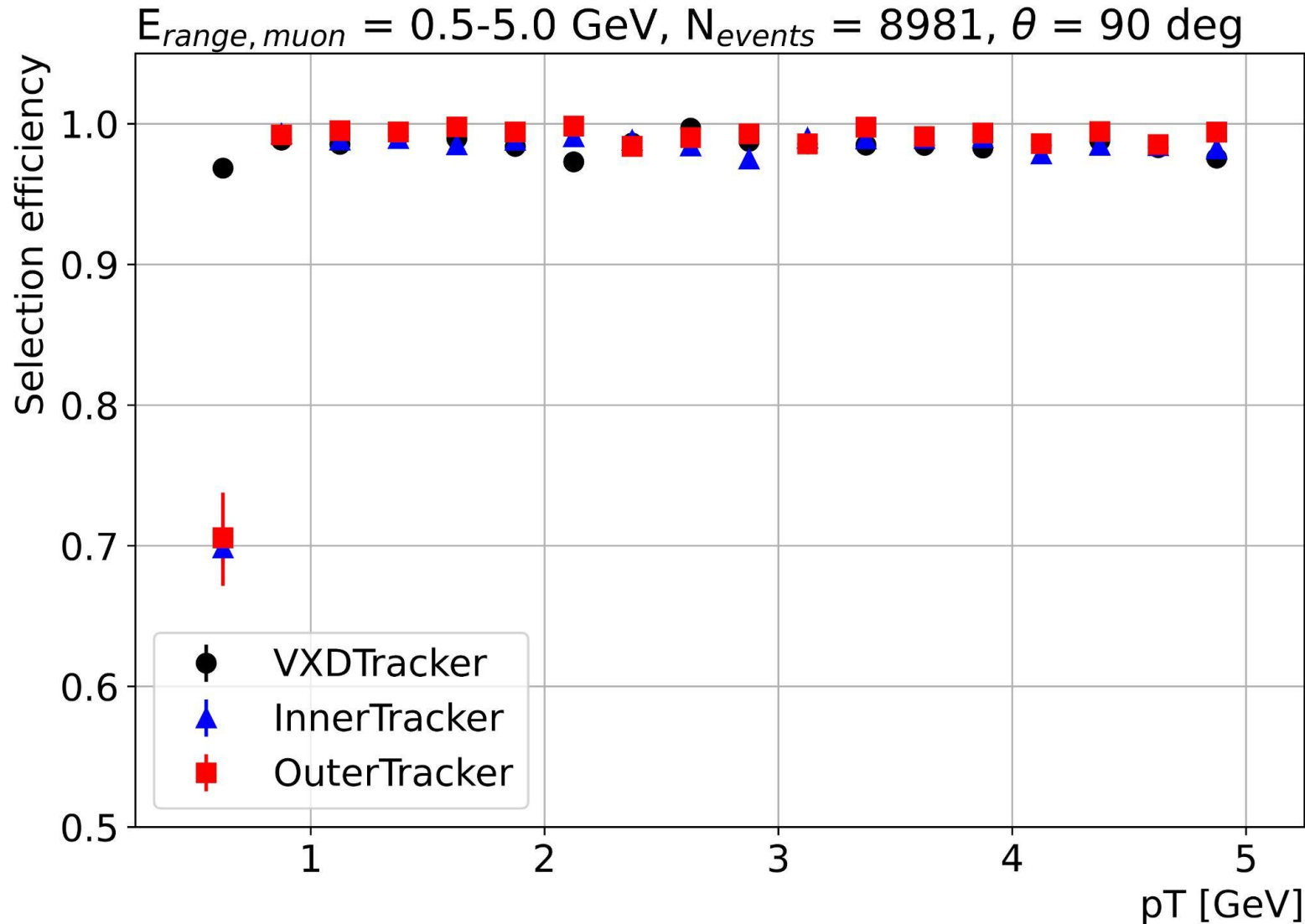


t - tof_{photon}

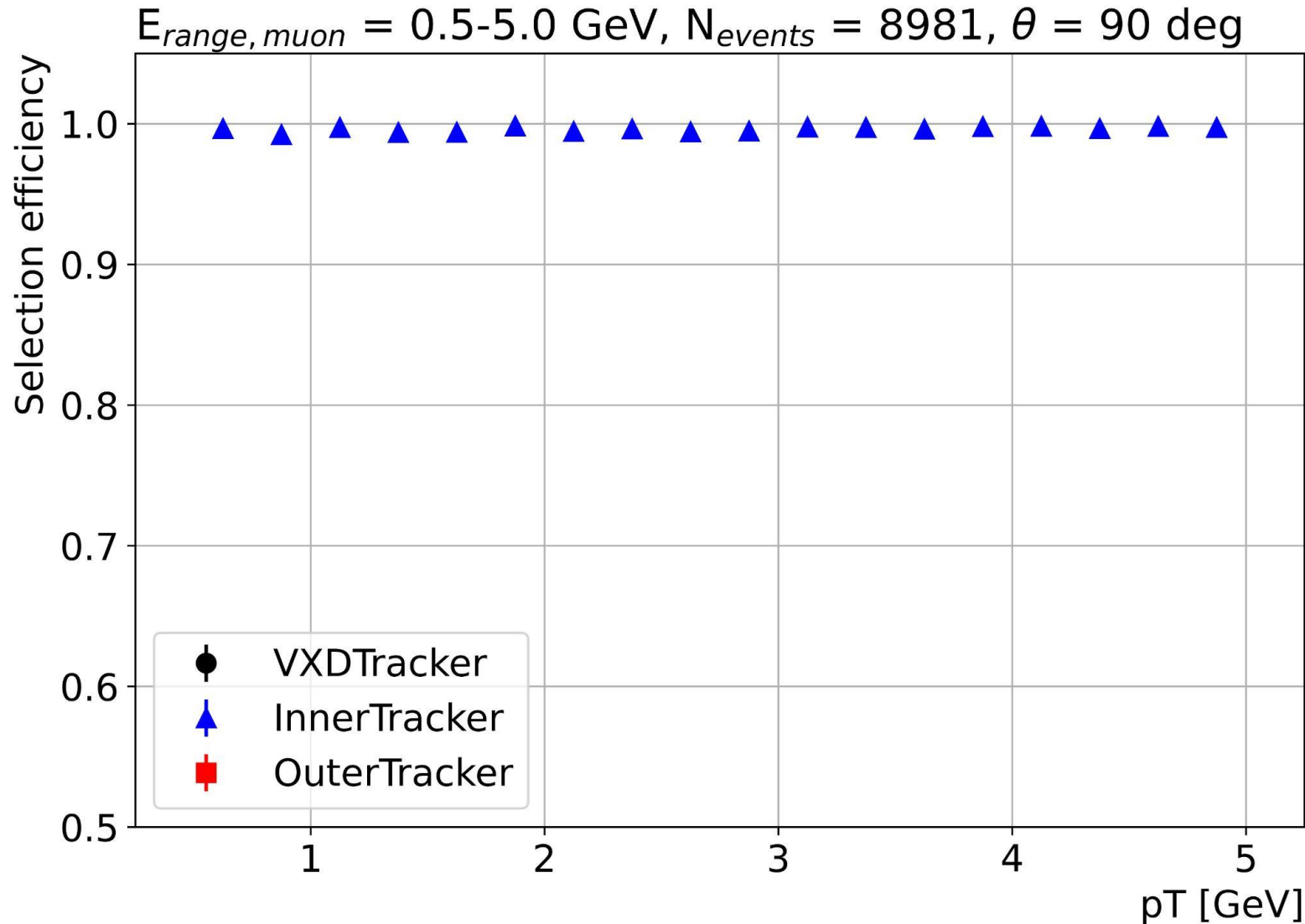


t - tof_{curvature}

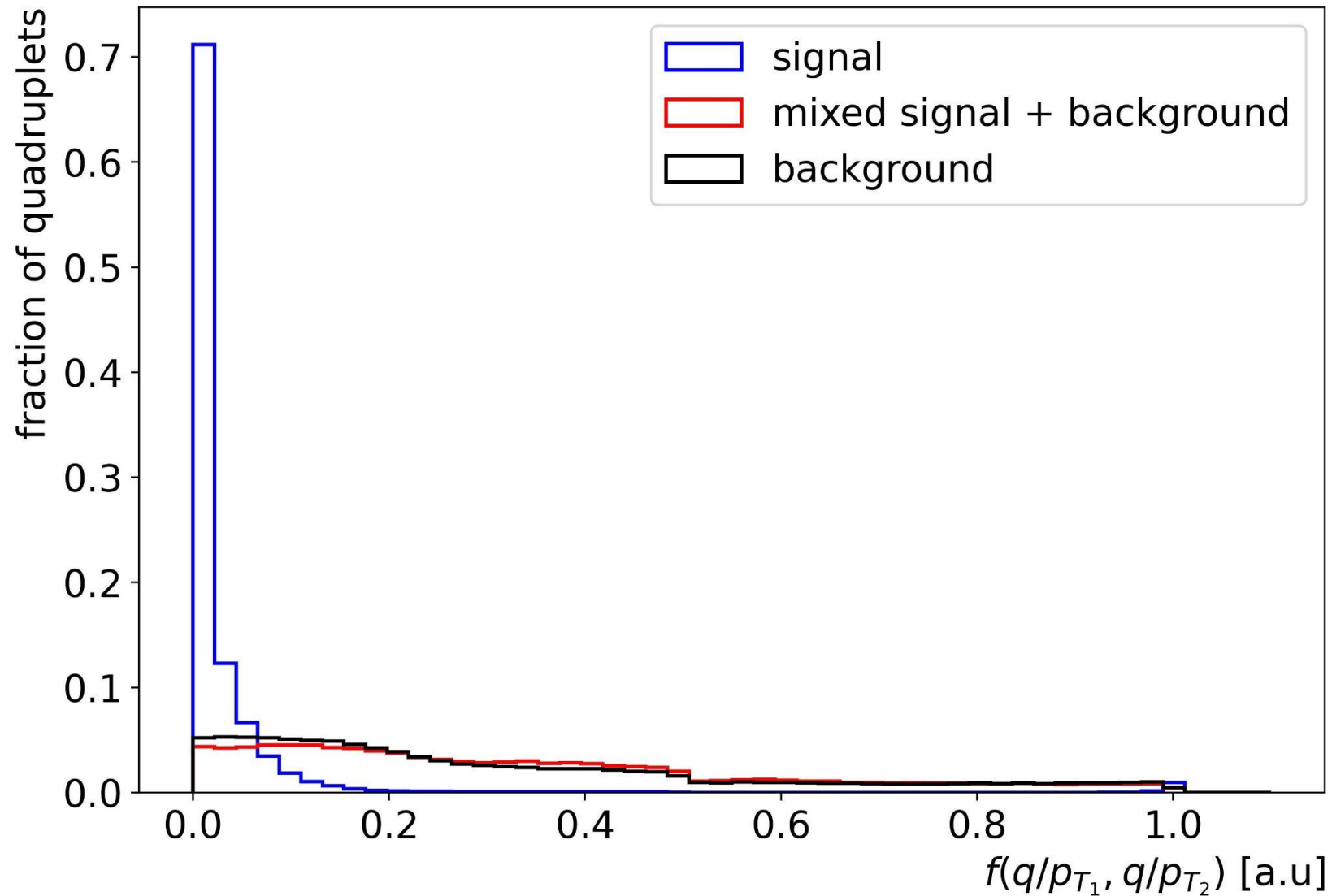
Appendix: Signal only - doublet pre-selection



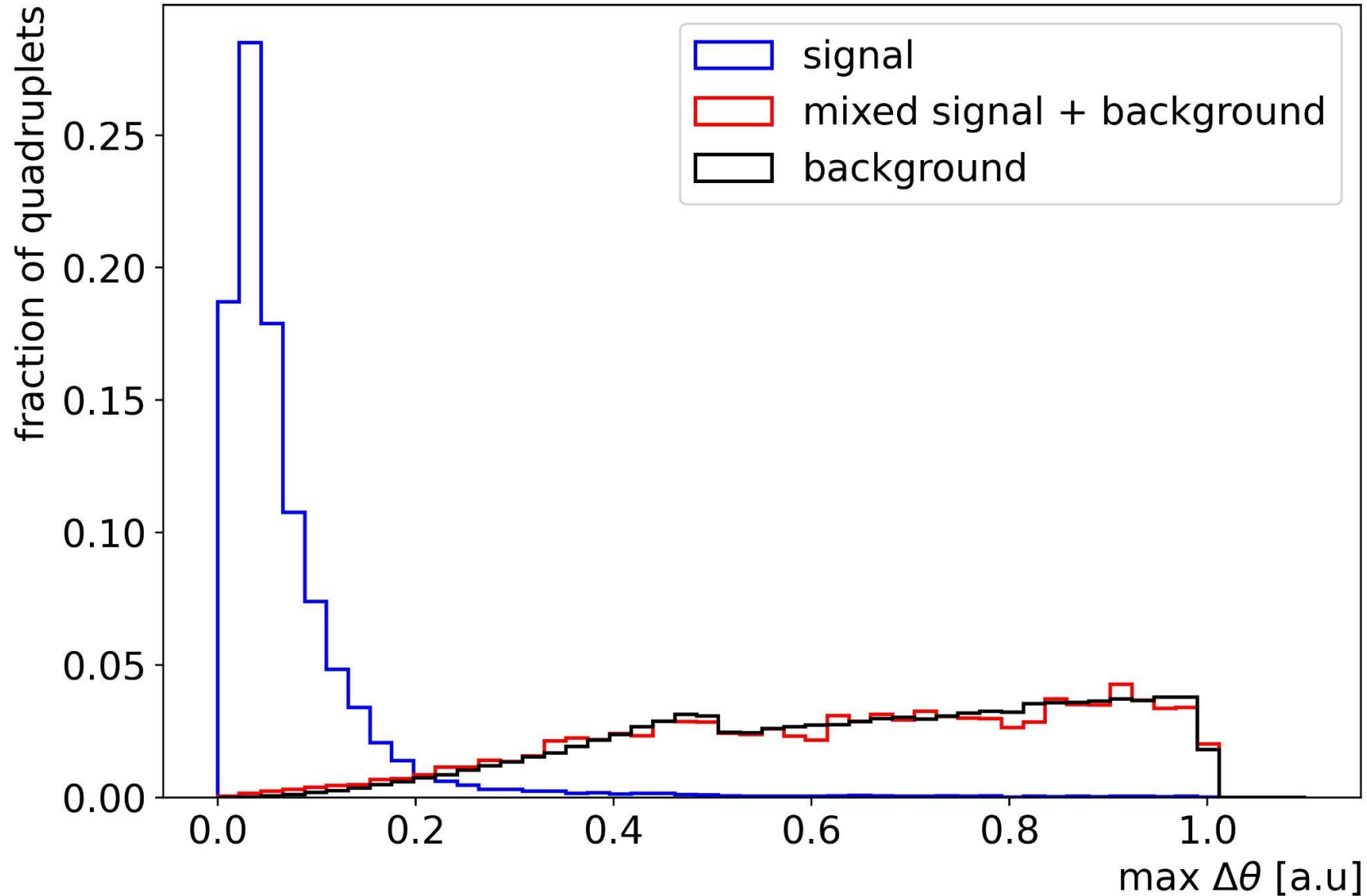
Appendix: Signal only - triplet pre-selection



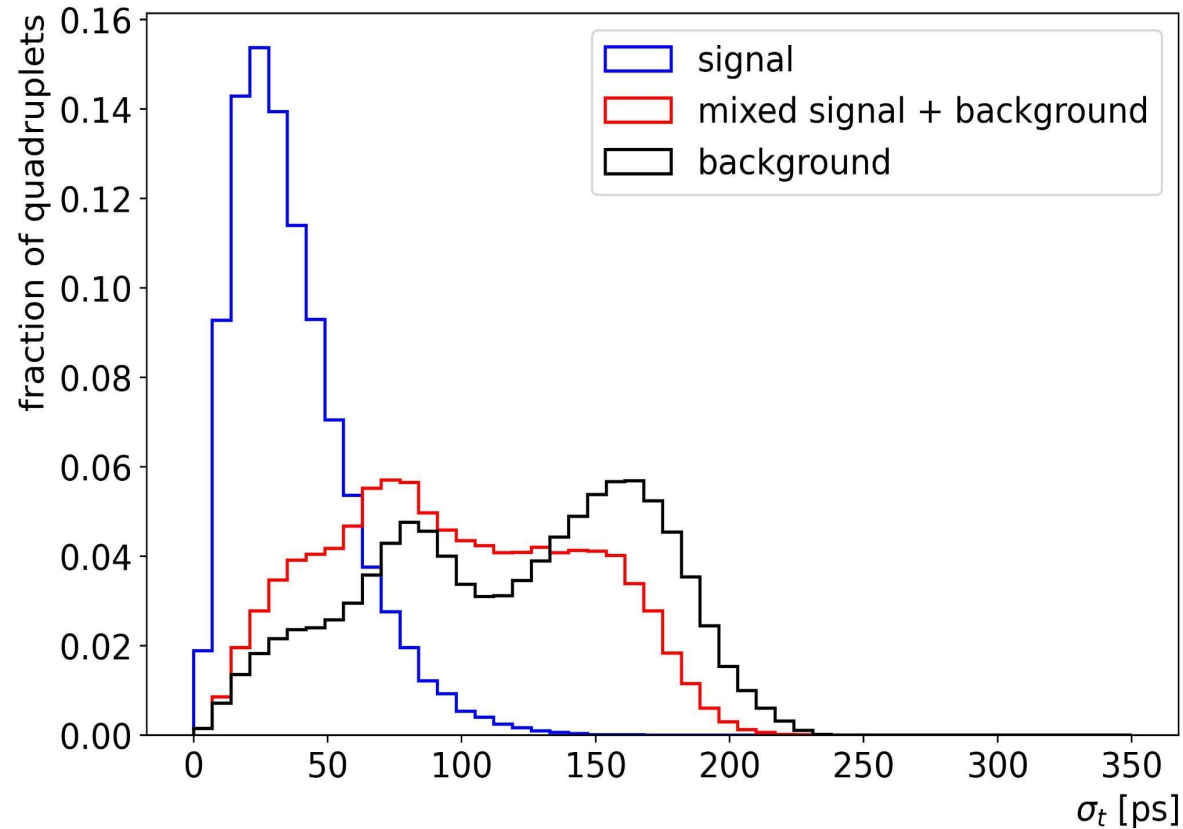
Appendix: QUBO-coefficients - curvature



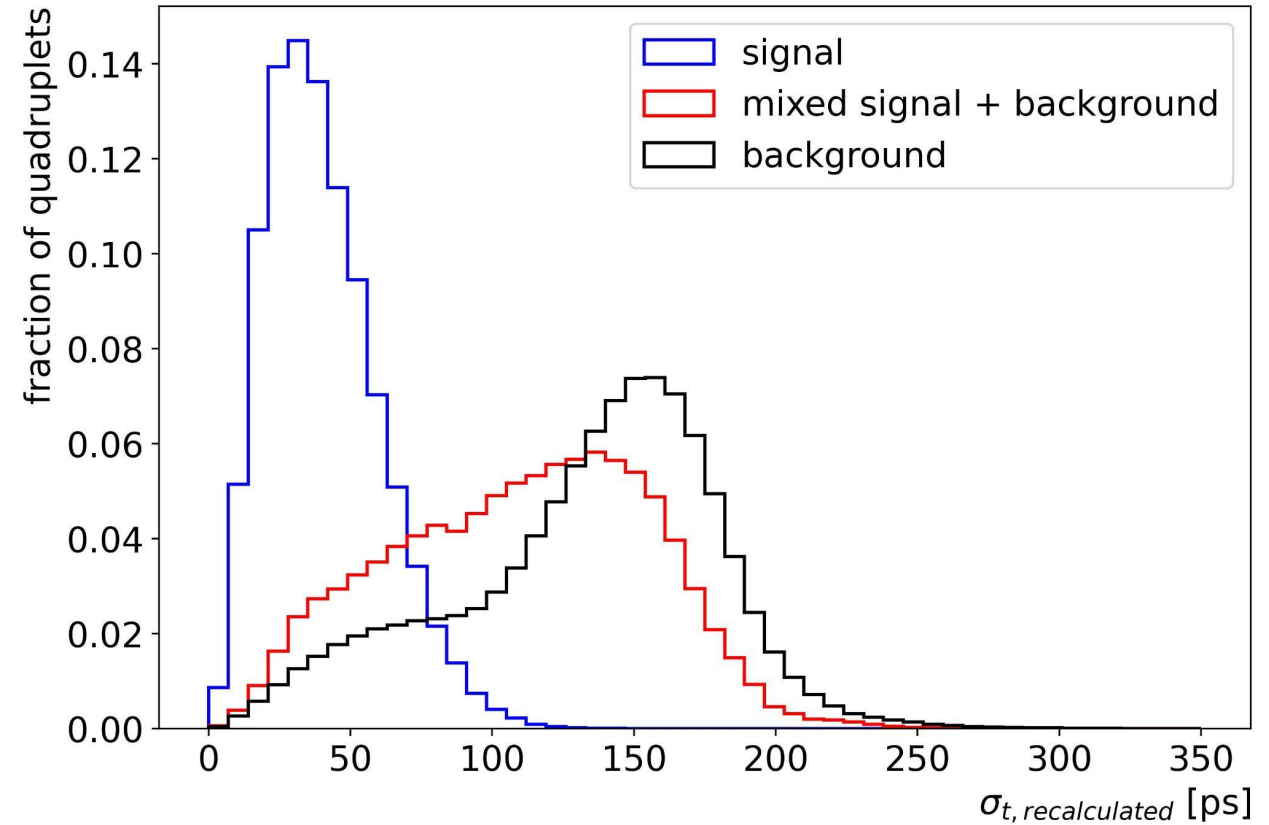
Appendix: QUBO-coefficients - $\max(\Delta\theta)$



Appendix: QUBO-coefficients - $\sigma(t_{\text{hits, quadruplet}})$



t - tof_{photon}



t - tof_{curvature}

Appendix: Preselection values

VXD: $\Delta\varphi = 0.05$ $\Delta\theta = 0.01$ $d_0 = 15\text{mm}$

ITracker: $\Delta\varphi = 0.2$ $\Delta\theta = 0.01$ $d_0 = 50\text{mm}$

OTracker: $\Delta\varphi = 0.25$ $\Delta\theta = 0.005$ $d_0 = 50\text{mm}$

Appendix: Triplet statistics

$$N_{\text{events}} = 538,$$

$$N_{\text{triplets}} = 15087781 \rightarrow 28044 / \text{event}$$

$$N_{\text{triplets, signal}} = 5048 \rightarrow 9 / \text{event}$$

$$N_{\text{triplets, majority signal}} = 40137 \rightarrow 75 / \text{event}$$

$$N_{\text{triplets, majority background}} = 278561 \rightarrow 518 / \text{event}$$

$$N_{\text{background}} = 14764025 \rightarrow 27442 / \text{event}$$

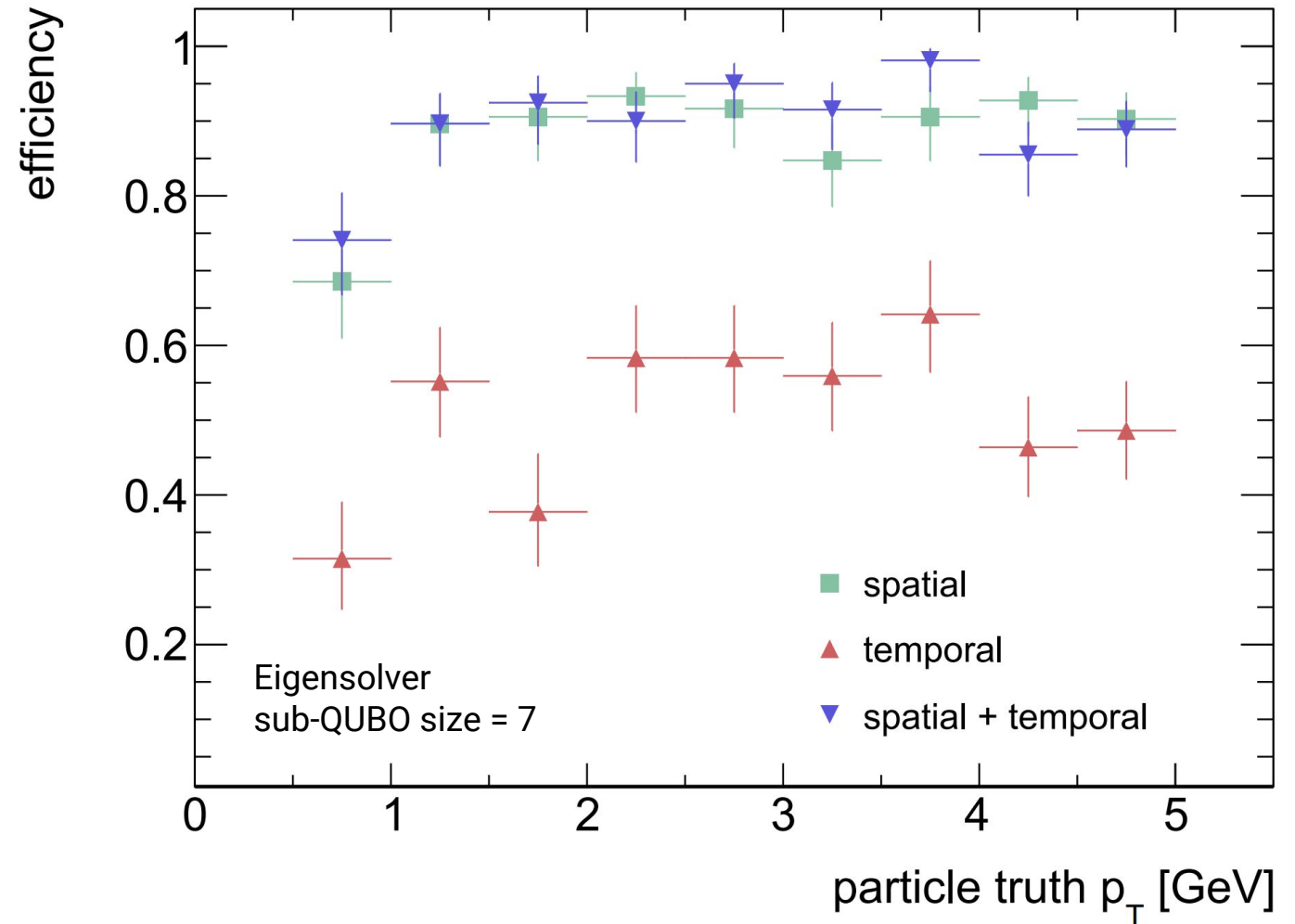
Efficiency vs. p_T

Reconstruction mode

- Pattern building in a θ -slice around muon track

Track selection

- At least 6 hits in a row
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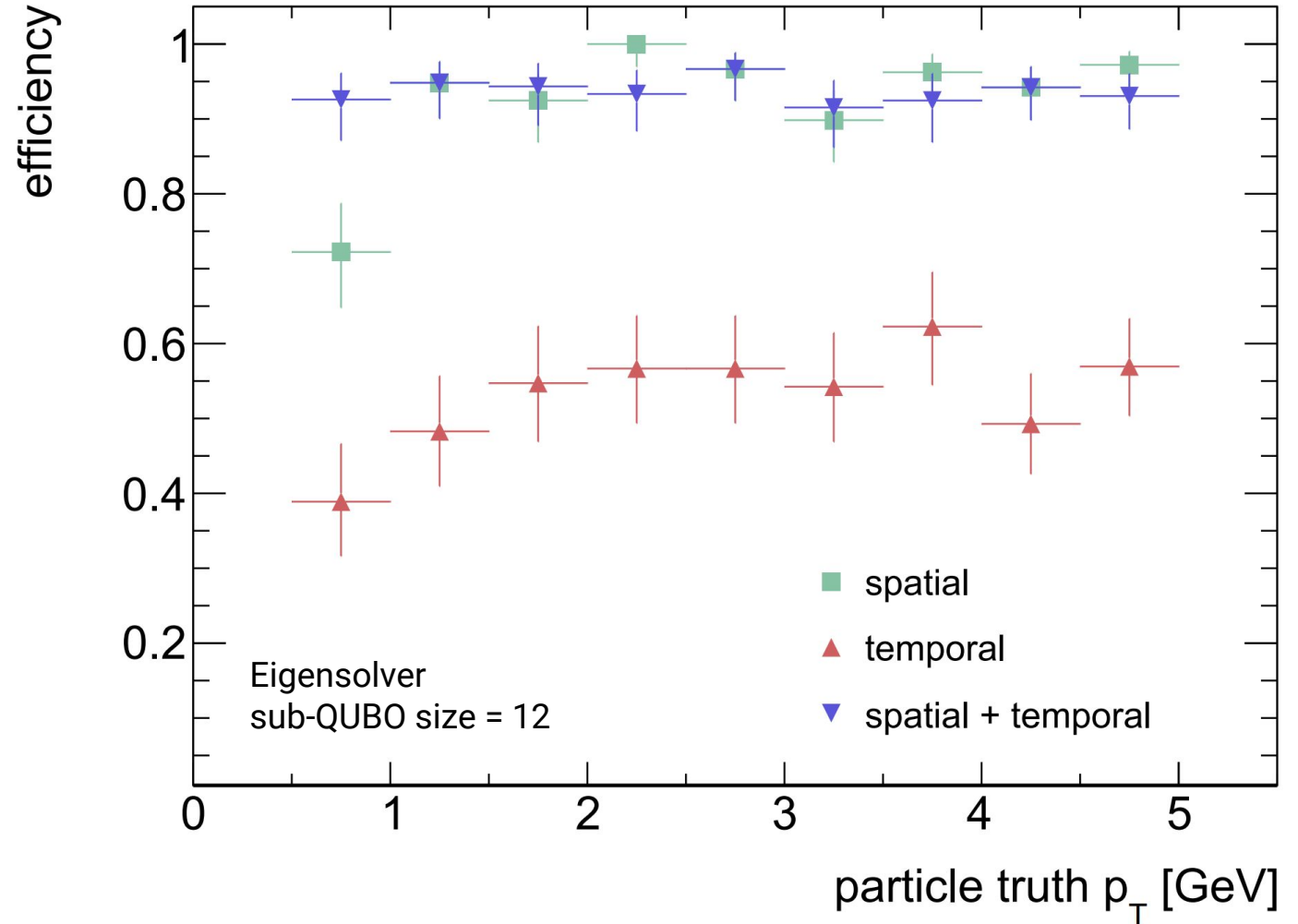
Efficiency vs. p_T

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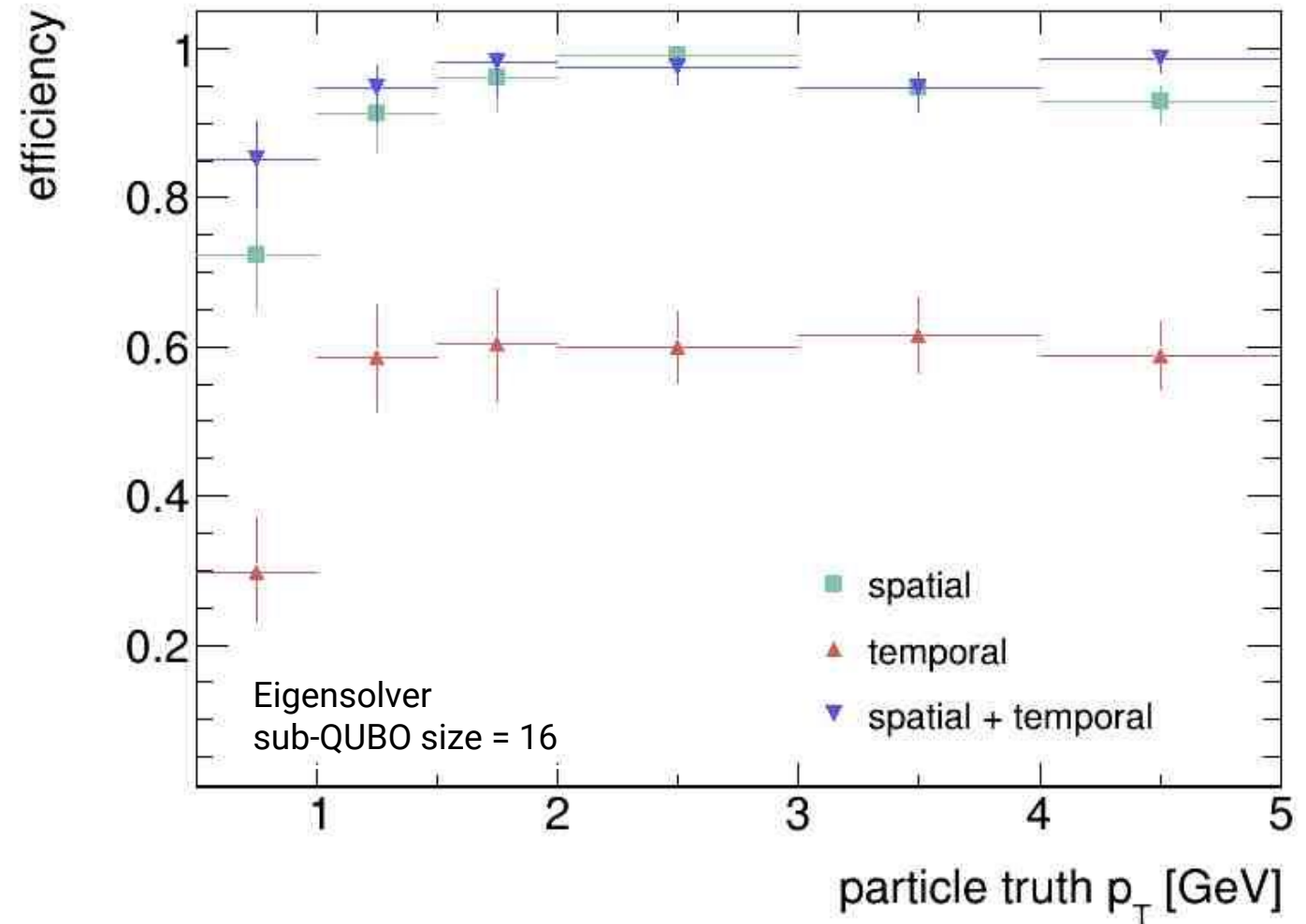
Efficiency vs. p_T

Reconstruction mode

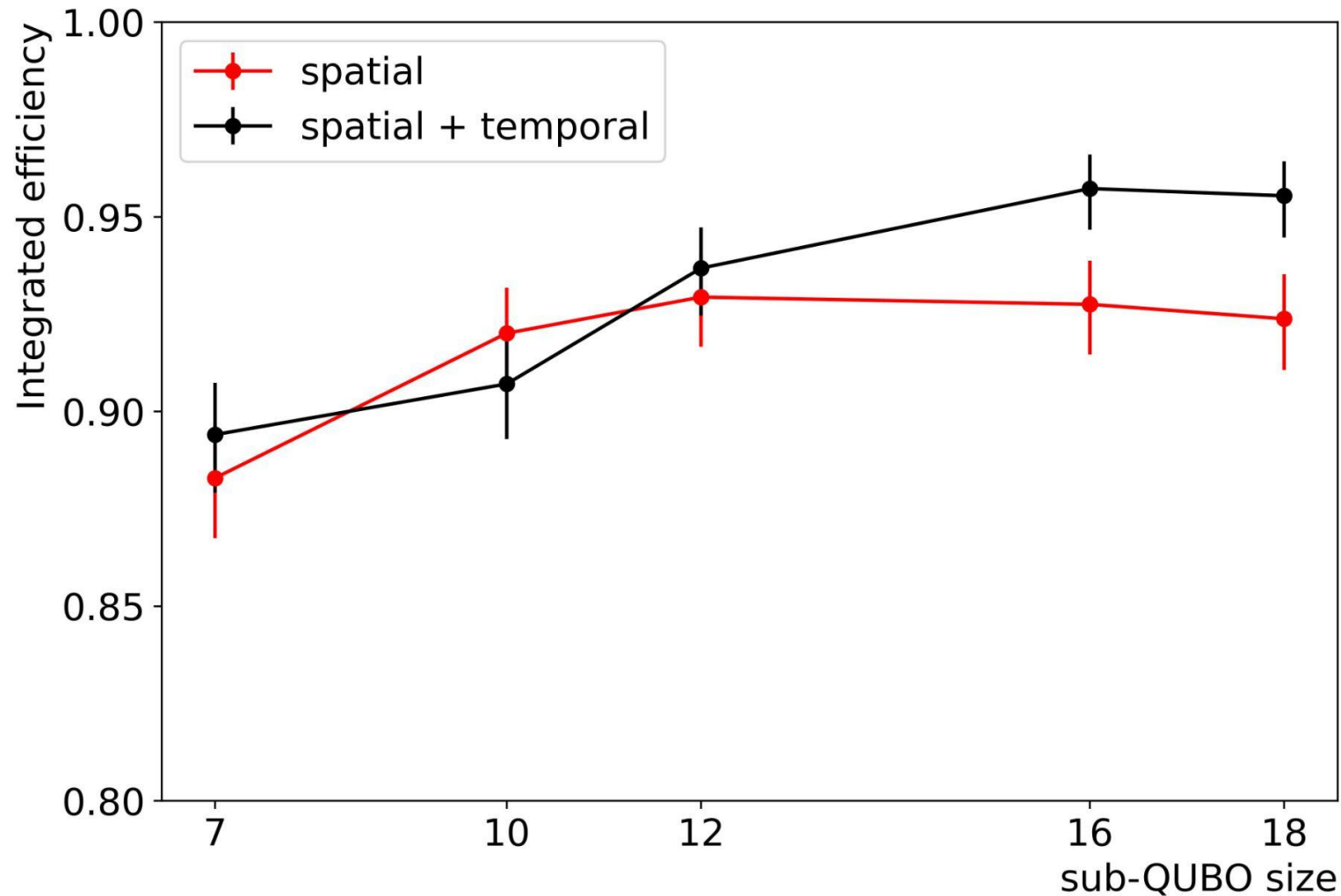
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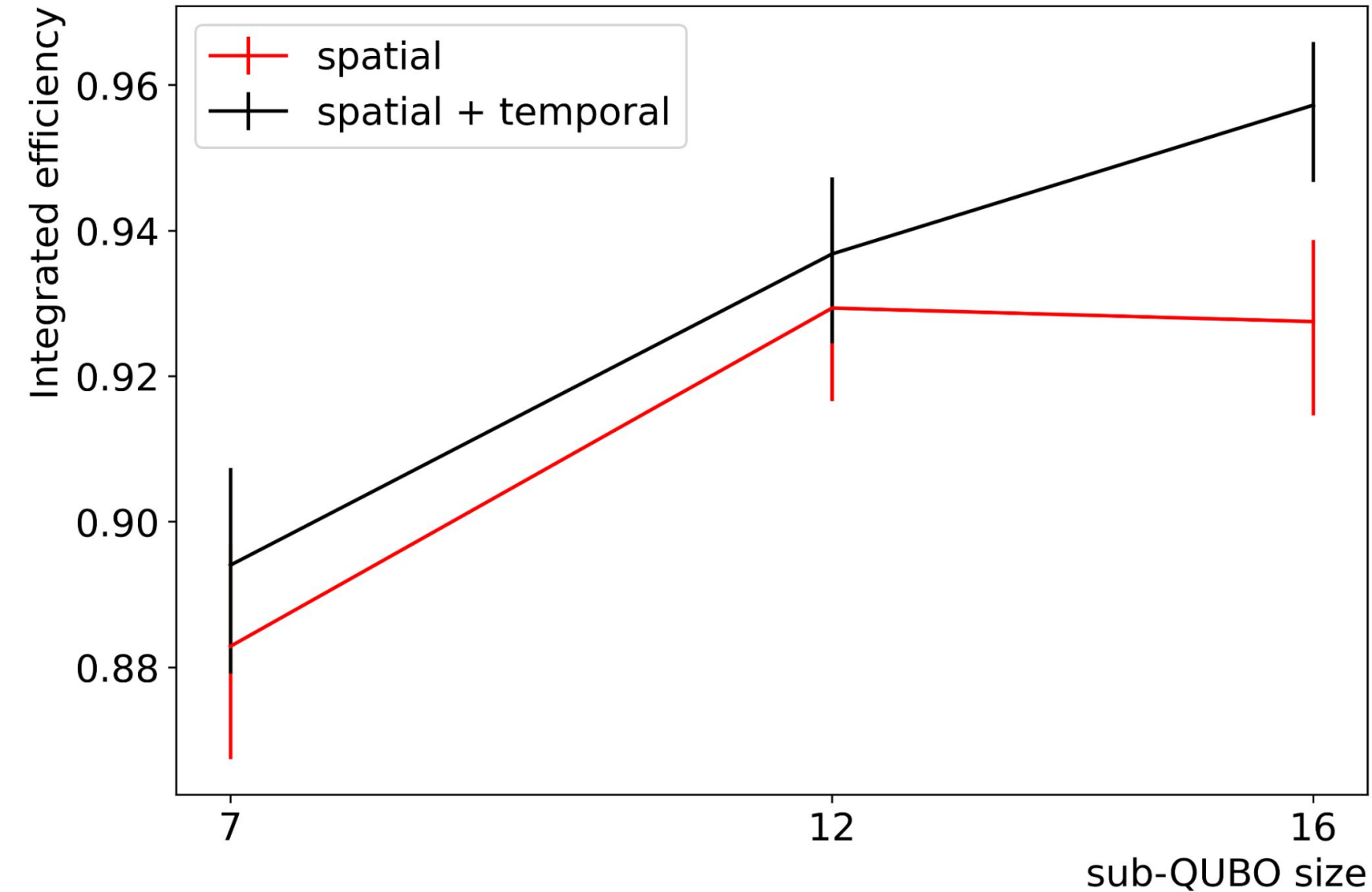


Efficiency vs. sub-QUBO size

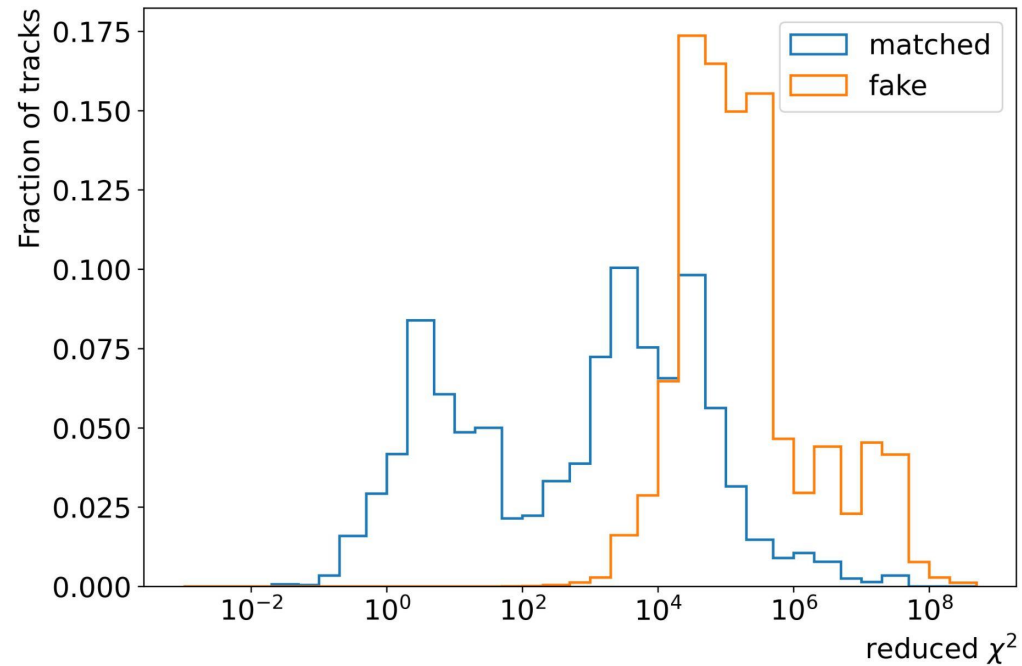


**Not finished plots and
not understood results**

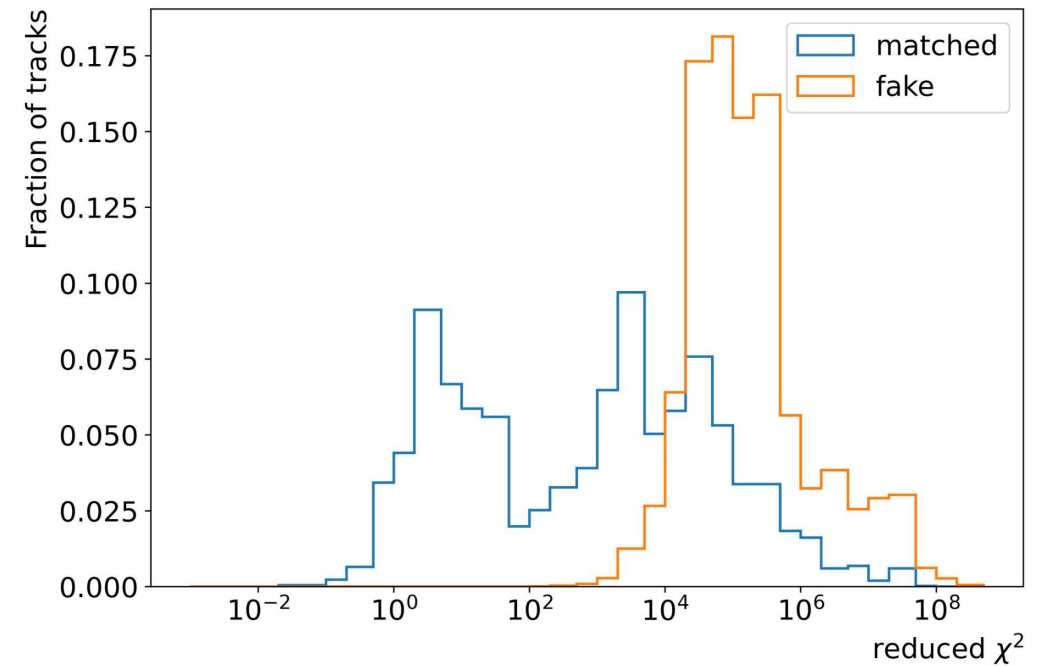
Integrated efficiency vs sub-QUBO size



Appendix: χ^2 - before final track selection



spatial



spatial + temporal