

# BSM perspectives in four-top final states at the LHC

---

**Panagiotis Stylianou**

based on work with Anisha, O. Atkinson,  
A. Bhardwaj, C. Englert and W. Naskar  
(2302.08281)



**FH discussion**  
**10 July 2023**

No BSM signal discovered at LHC



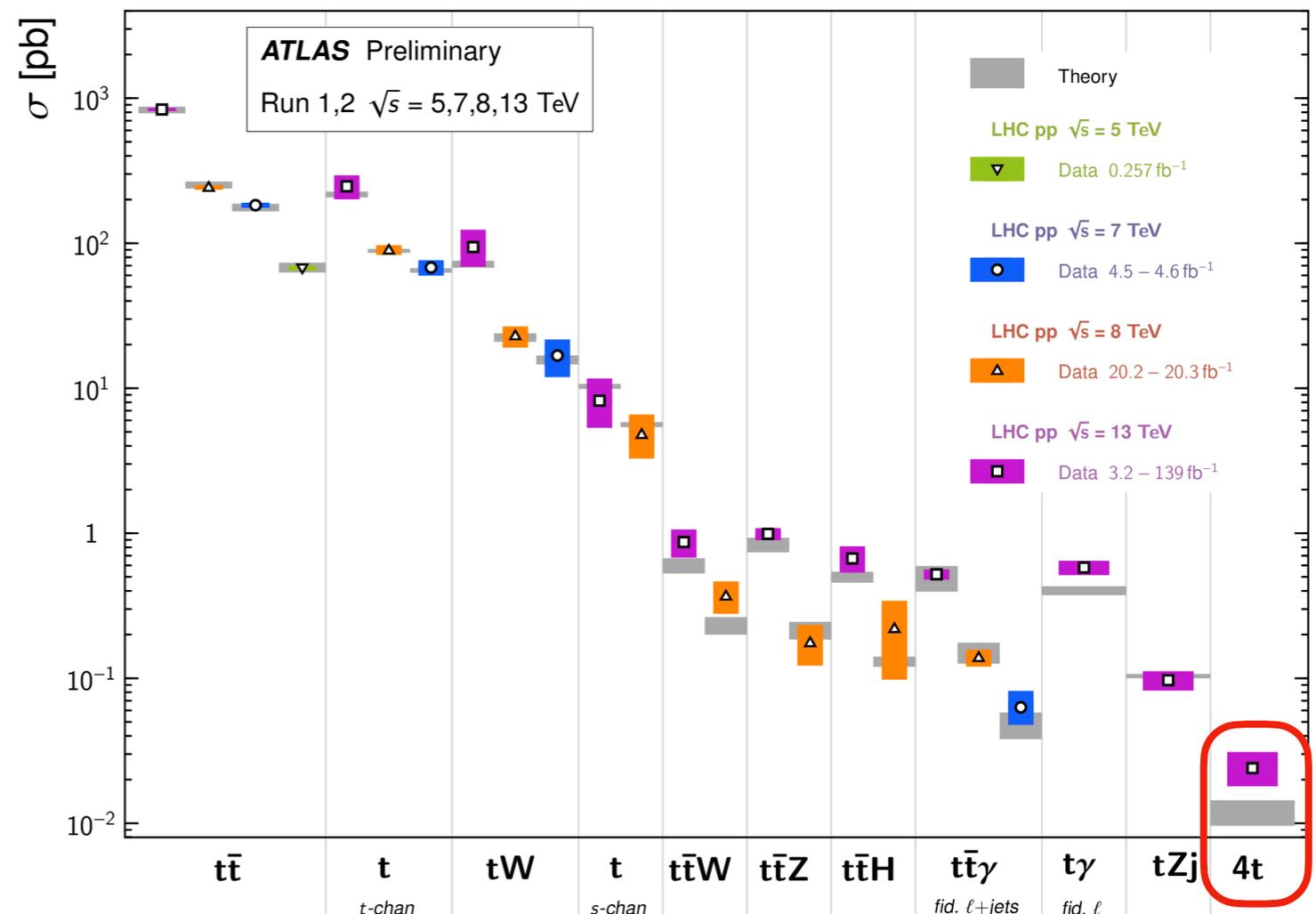
- Turn to less abundant processes for new-physics searches
- Efficient exploitation of correlations in data required
- Model-independent techniques

## Content:

- Focus on 4-top production  
→ GNN analysis
- BSM resonances in 4-top  
→ 2HDM example
- Non-resonant searches  
→ Higgs-philic ALP

Top Quark Production Cross Section Measurements

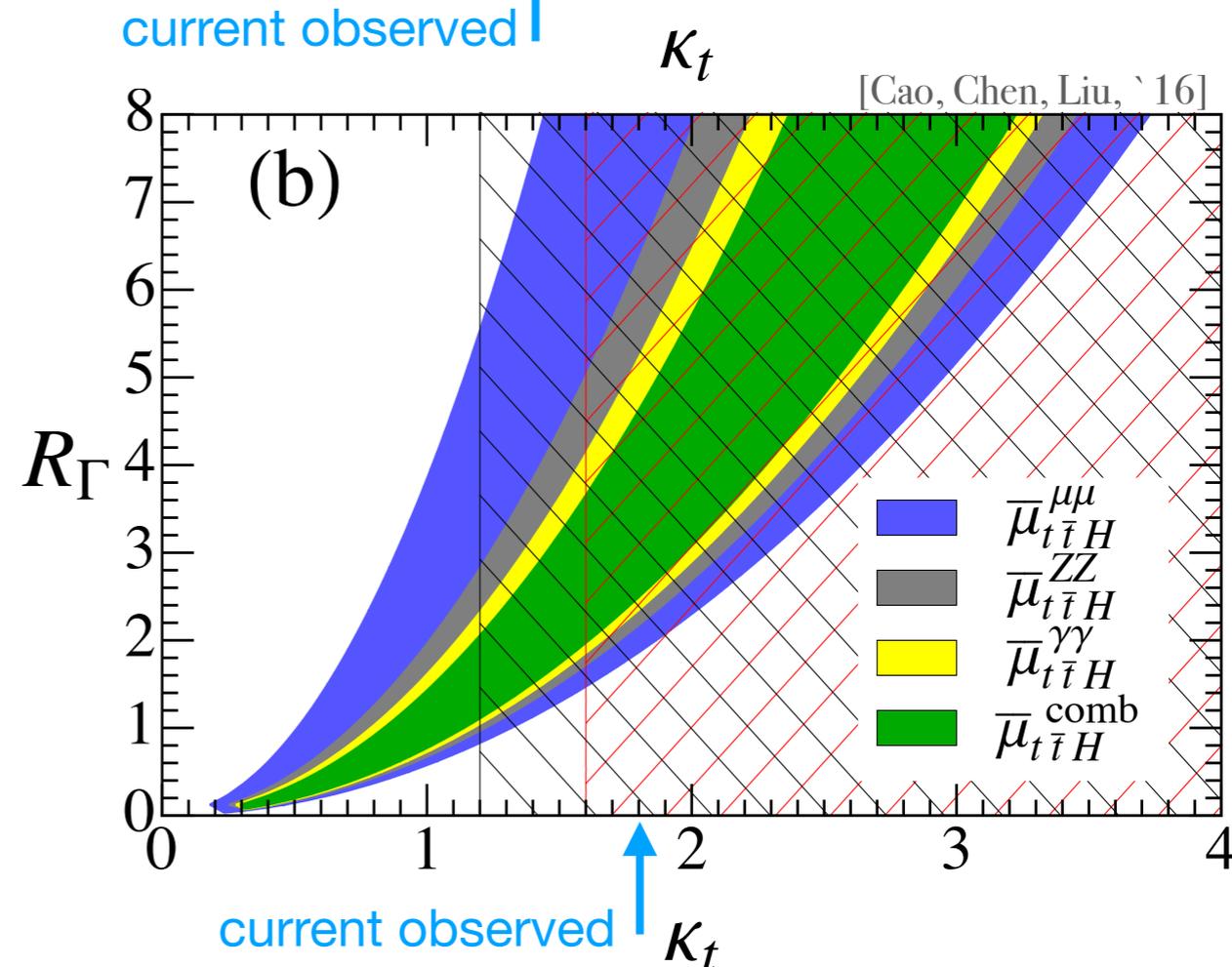
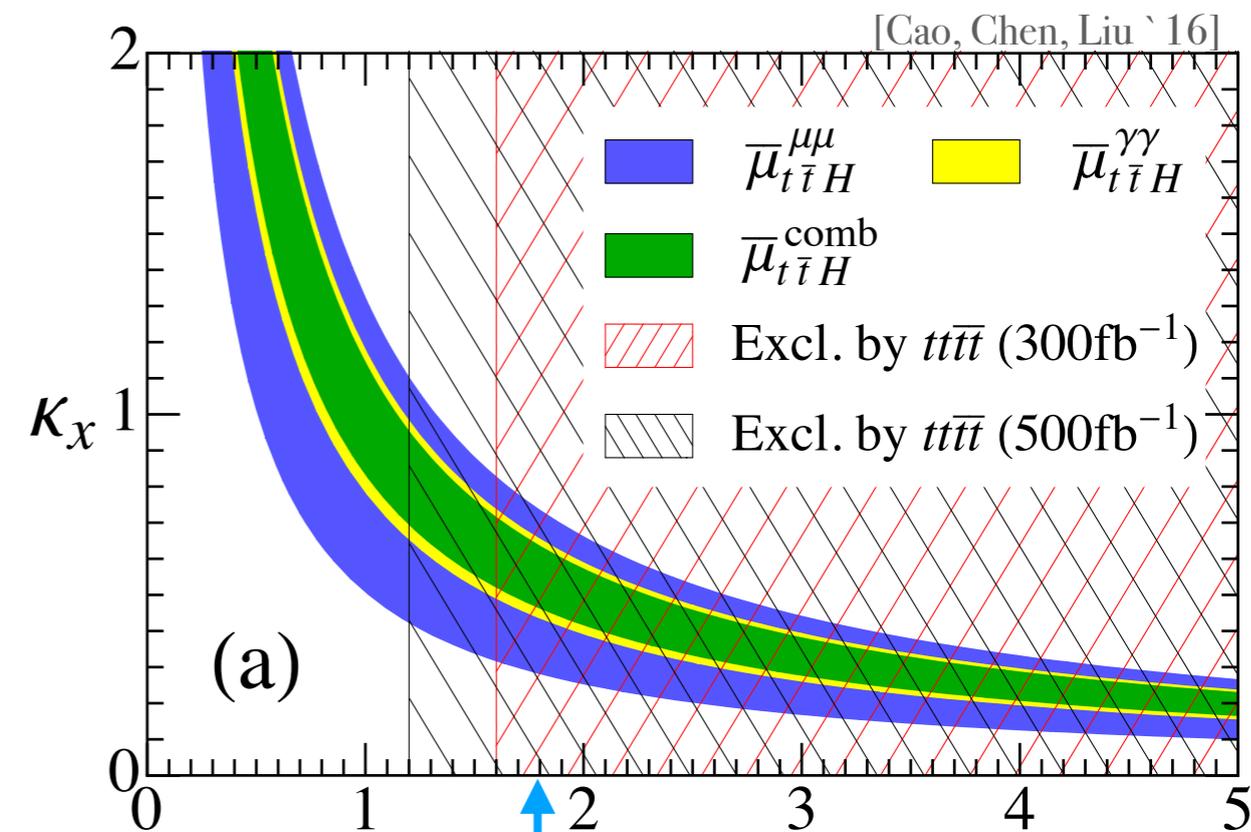
Status: November 2022



# 4-top at the LHC

## $t\bar{t}t\bar{t}$ production

- Rare process, but recently observed by ATLAS, CMS  
[ATLAS 2303.15061]  
[CMS 2305.13439]
- SM cross section at NLL accuracy  
[Beekveld, Kulesza, Valero `22]
- Access to Yukawa coupling  $y_t$
- Independent of Higgs width
- Combine with  $t\bar{t}H$  for insights on other couplings / width [Cao, Chen, Liu `16]



# Considered Processes for SM

- Two same-sign di-lepton (2SSDL) final state:

$$pp \rightarrow t\bar{t}t\bar{t} \rightarrow \ell^+\ell^+/\ell^-\ell^- + \text{jets} + \text{b-quarks}$$

- Three leptons (3L):

$$pp \rightarrow t\bar{t}t\bar{t} \rightarrow \ell\ell\ell + \text{jets} + \text{b-quarks}$$

Multiple final states with rich kinematics



Exploit correlations in data with Machine Learning

## Pre-selection:

- $p_T(\ell) > 10 \text{ GeV} \ \& \ |\eta(\ell)| < 2.5$
- $p_T(b) > 20 \text{ GeV} \ \& \ |\eta(b)| < 2.5$
- $p_T(j) > 20 \text{ GeV} \ \& \ |\eta(j)| < 4.5$
- At least 20 GeV of missing energy

70% tagging efficiency



nowadays pessimistic, but we neglect mis-tagging

# Simulated SM Backgrounds

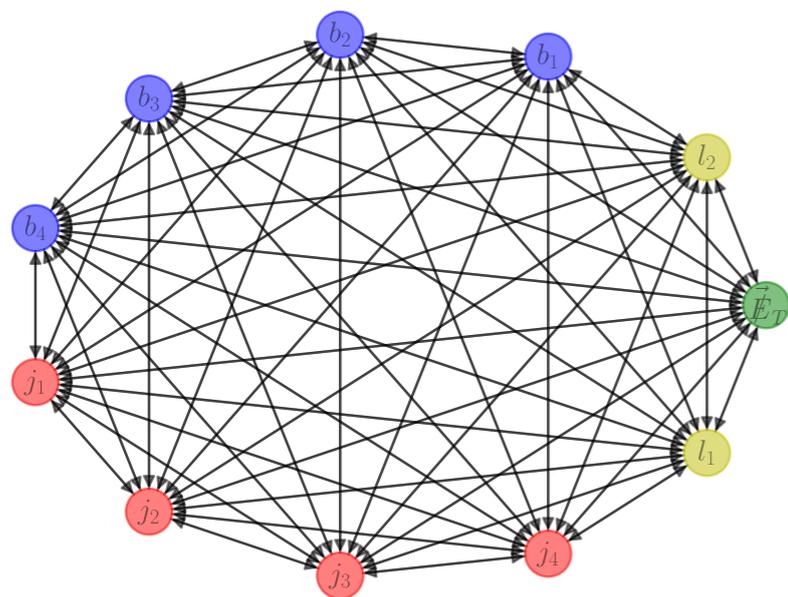
- 2SSDL backgrounds:

Processes	Cross Section (fb)
$pp \rightarrow t_{\ell^+} \bar{t}_h W_{\ell^+}^+ + t_h \bar{t}_{\ell^-} W_{\ell^-}^-$	$57.67 \pm 0.06$
$pp \rightarrow t_{\ell^+} \bar{t}_h Z_{\ell^+ \ell^-} + t_h \bar{t}_{\ell^-} Z_{\ell^+ \ell^-} + t_{\ell^+} \bar{t}_{\ell^-} Z_{\ell^+ \ell^-}$	$10.65 \pm 0.01$
$pp \rightarrow (W_{\ell^+}^+ W_h^- W_{\ell^+}^+ + W_h^+ W_{\ell^-}^- W_{\ell^-}^-) b \bar{b}$	$43.29 \pm 0.05$
$pp \rightarrow (W_{\ell^+}^+ W_h^- Z_{\ell^+ \ell^-} + W_h^+ W_{\ell^-}^- Z_{\ell^+ \ell^-} + W_{\ell^+}^+ W_{\ell^-}^- Z_{\ell^+ \ell^-}) b \bar{b}$	$12.65 \pm 0.02$

- 3L backgrounds:

Processes	Cross Section (fb)
$pp \rightarrow t_{\ell^+} \bar{t}_{\ell^-} W_{\ell^\pm}^\pm$	$3.421 \pm 0.004$
$pp \rightarrow t_{\ell^+} \bar{t}_h Z_{\ell^+ \ell^-} + t_h \bar{t}_{\ell^-} Z_{\ell^+ \ell^-} + t_{\ell^+} \bar{t}_{\ell^-} Z_{\ell^+ \ell^-}$	$10.65 \pm 0.01$
$pp \rightarrow Z_{\ell^+ \ell^-} W_{\ell^\pm}^\pm b \bar{b}$	$3.296 \pm 0.003$
$pp \rightarrow W_{\ell^+}^+ W_{\ell^-}^- W_{\ell^\pm}^\pm b \bar{b}$	$3.614 \pm 0.004$
$pp \rightarrow (W_{\ell^+}^+ W_h^- Z_{\ell^+ \ell^-} + W_h^+ W_{\ell^-}^- Z_{\ell^+ \ell^-} + W_{\ell^+}^+ W_{\ell^-}^- Z_{\ell^+ \ell^-}) b \bar{b}$	$12.65 \pm 0.02$

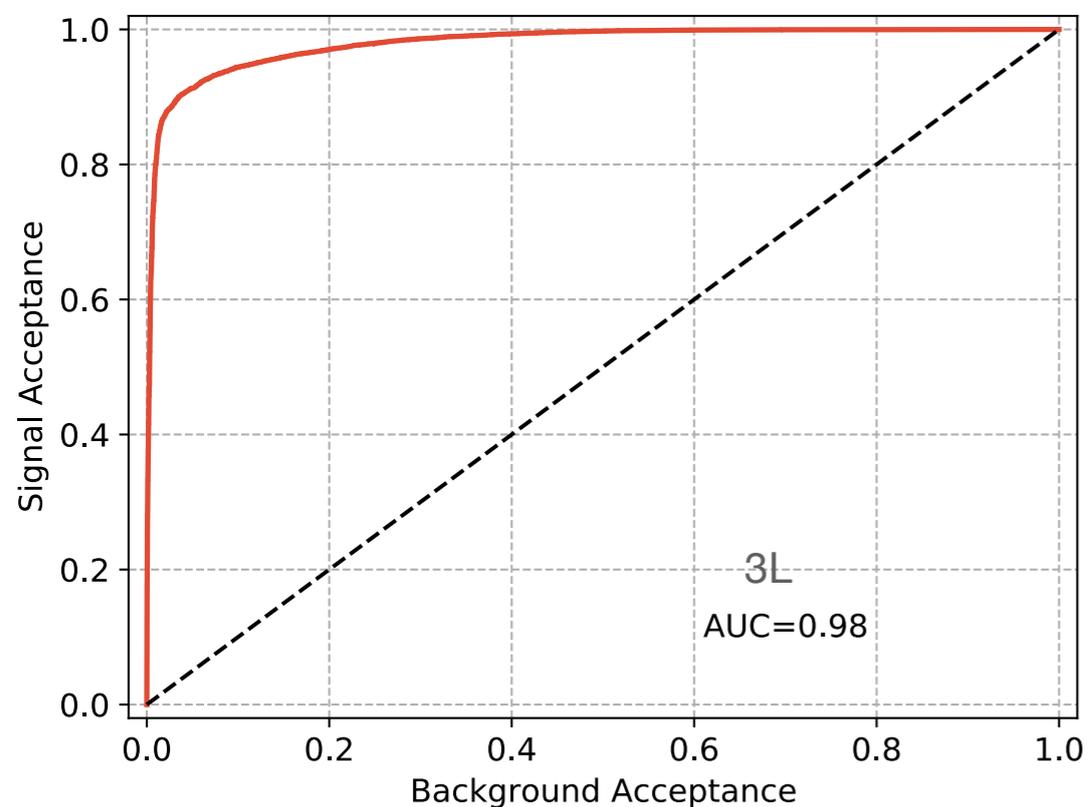
# SM Significance



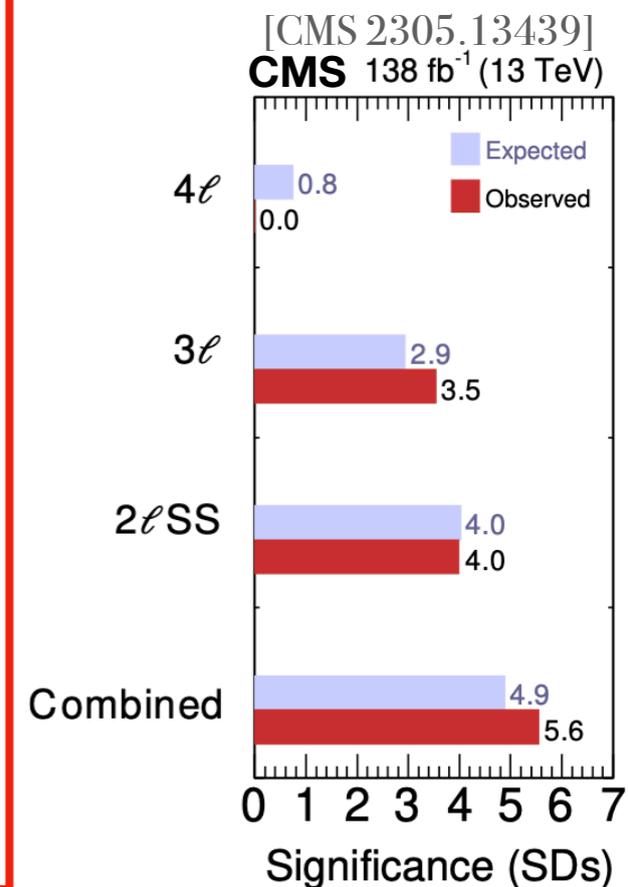
$\left\{ P(\text{Signal}), P(\text{Background}) \right\}$

Input feature vector for node  $i$ :

$$x_i^{(0)} = [p_{T,i}, \eta_i, \phi_i, E_i, m_i, \text{PID}_i]$$



- Use ROC curves to obtain optimal working point → gives score threshold to accept event
- ‘Simplified’ significance  $N_S / \sqrt{N_B + N_S}$  for our simulated gives  $\sim 4.6$  for 2SSDL and  $\sim 3$  for 3L
- Reasonable estimates for BSM expected with our analysis



# Scalar resonances - why 4-top?

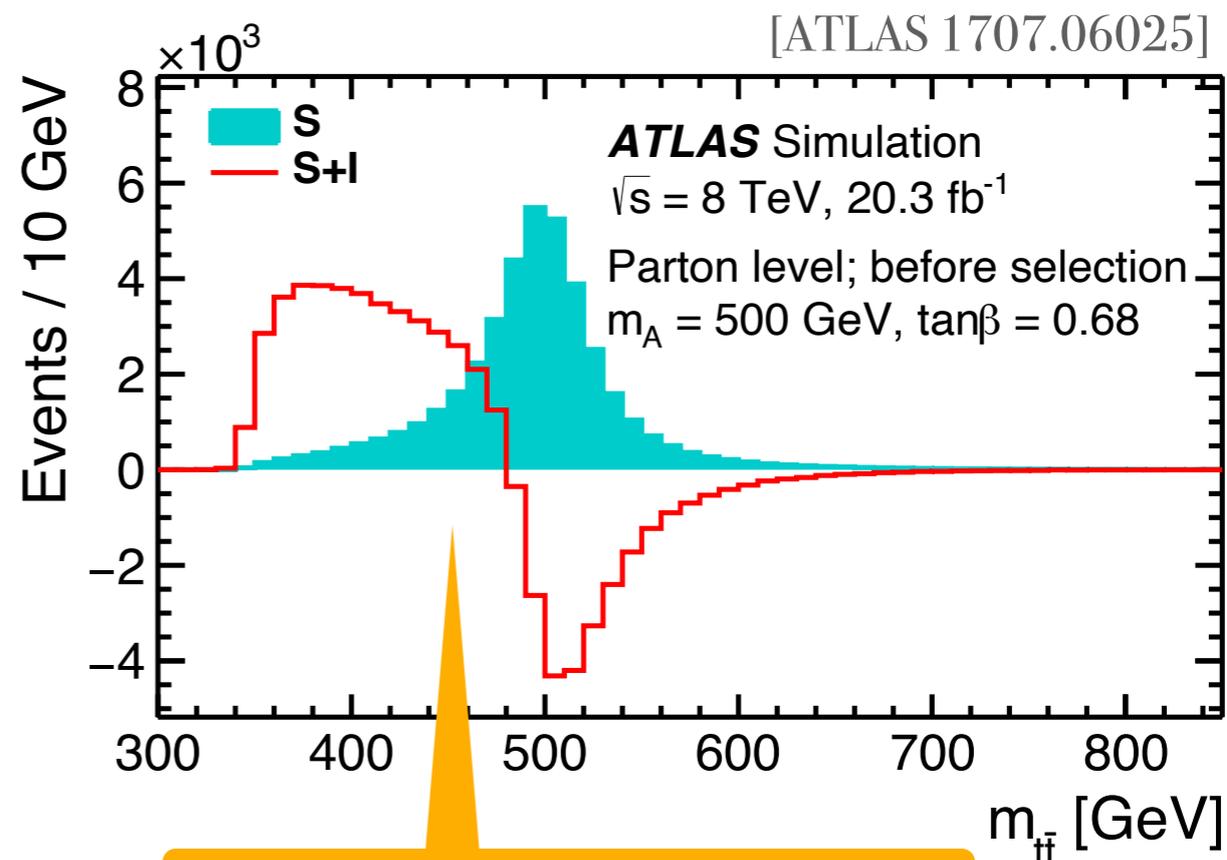
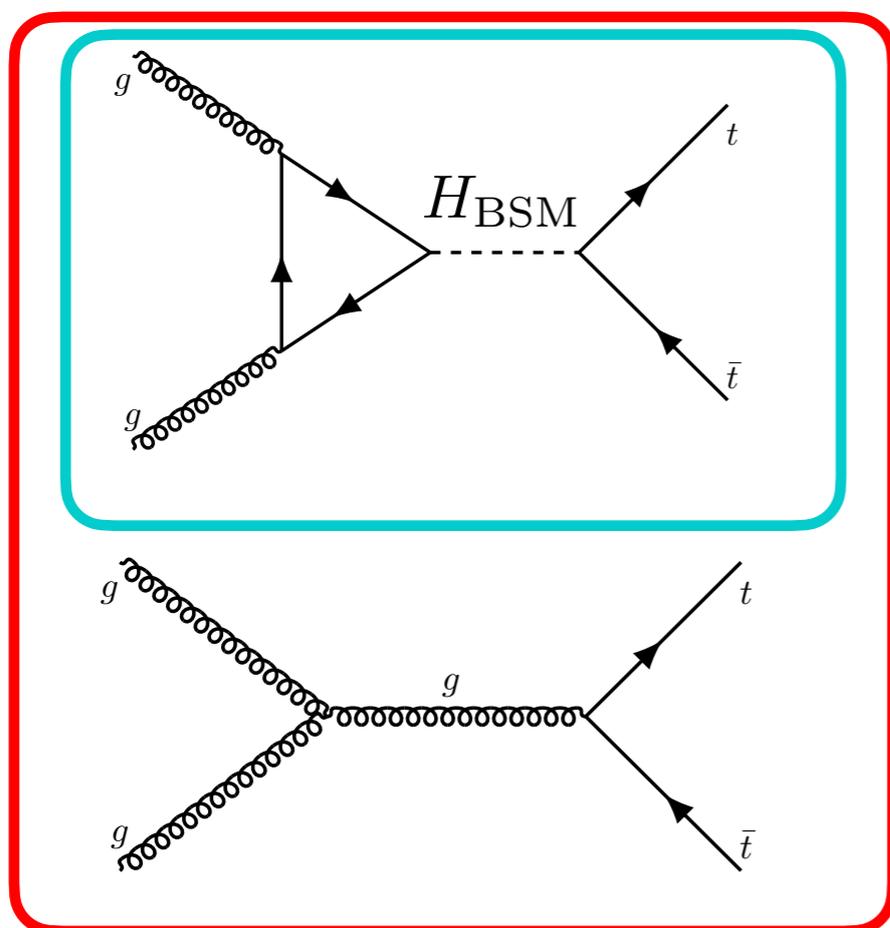
- Many works focus on different types of resonances (e.g. [Darme, Fuks, Maltoni `21], [Cao et al `21]) → **focus on scalar resonances**

Fermion Yukawa couplings:  
 $g_{ffh} \sim m_f$

Heavier? ➔

BSM scalars dominant coupling to tops?  
⇒ **Resonances in  $t\bar{t}$ !**

- However:



Distortion of peak from signal-background

# Scalar Resonance searches

- Simplified Lagrangian:

$$\mathcal{L}_{\text{simp}} = \frac{1}{2} (\partial S)^2 - \frac{M_S^2}{2} S^2 - \frac{m_t}{v} [\xi_S \bar{t}_L t_R S + \text{h.c.}]$$

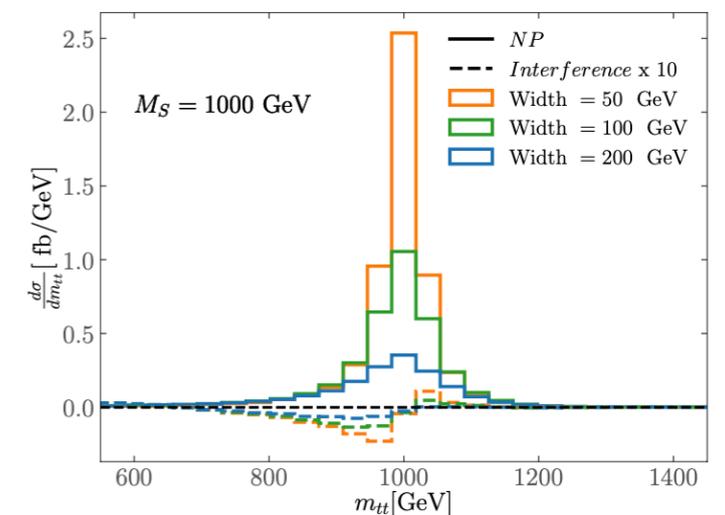
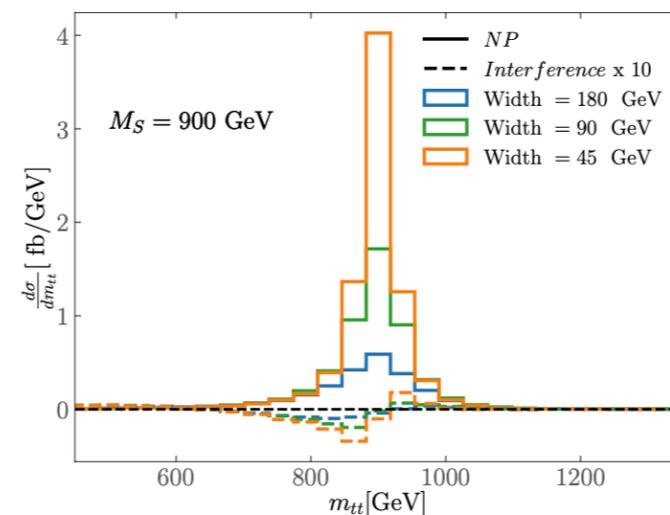
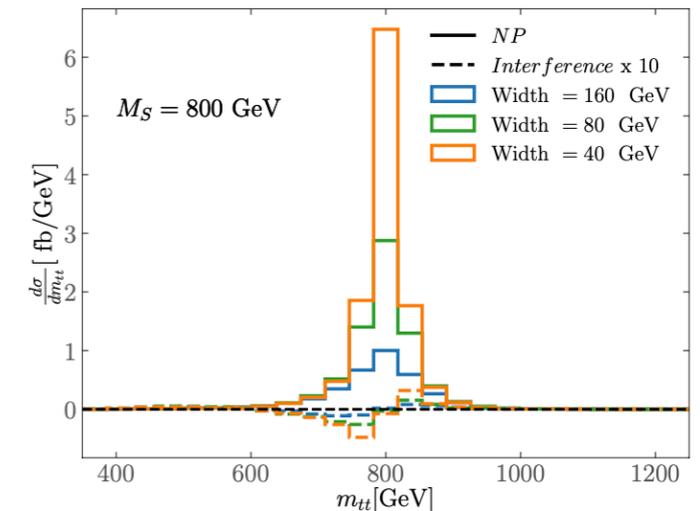
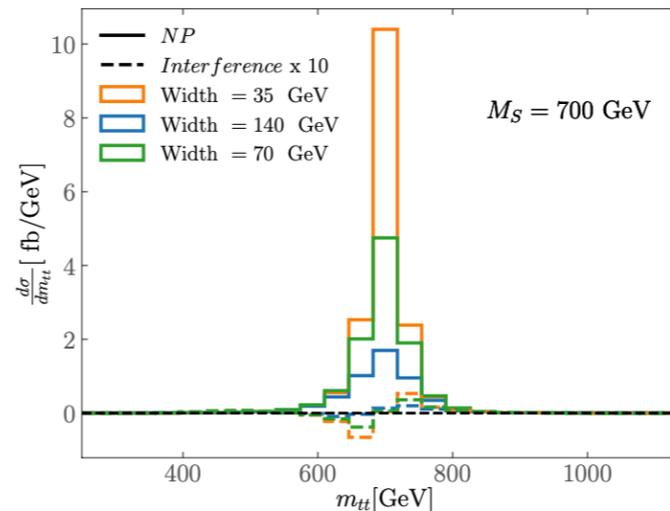
## Resonant Contributions:

$$d\sigma^{\text{new}} \sim |\mathcal{M}_{\text{res}}|^2 d\text{LIPS}$$

## Interference Contributions:

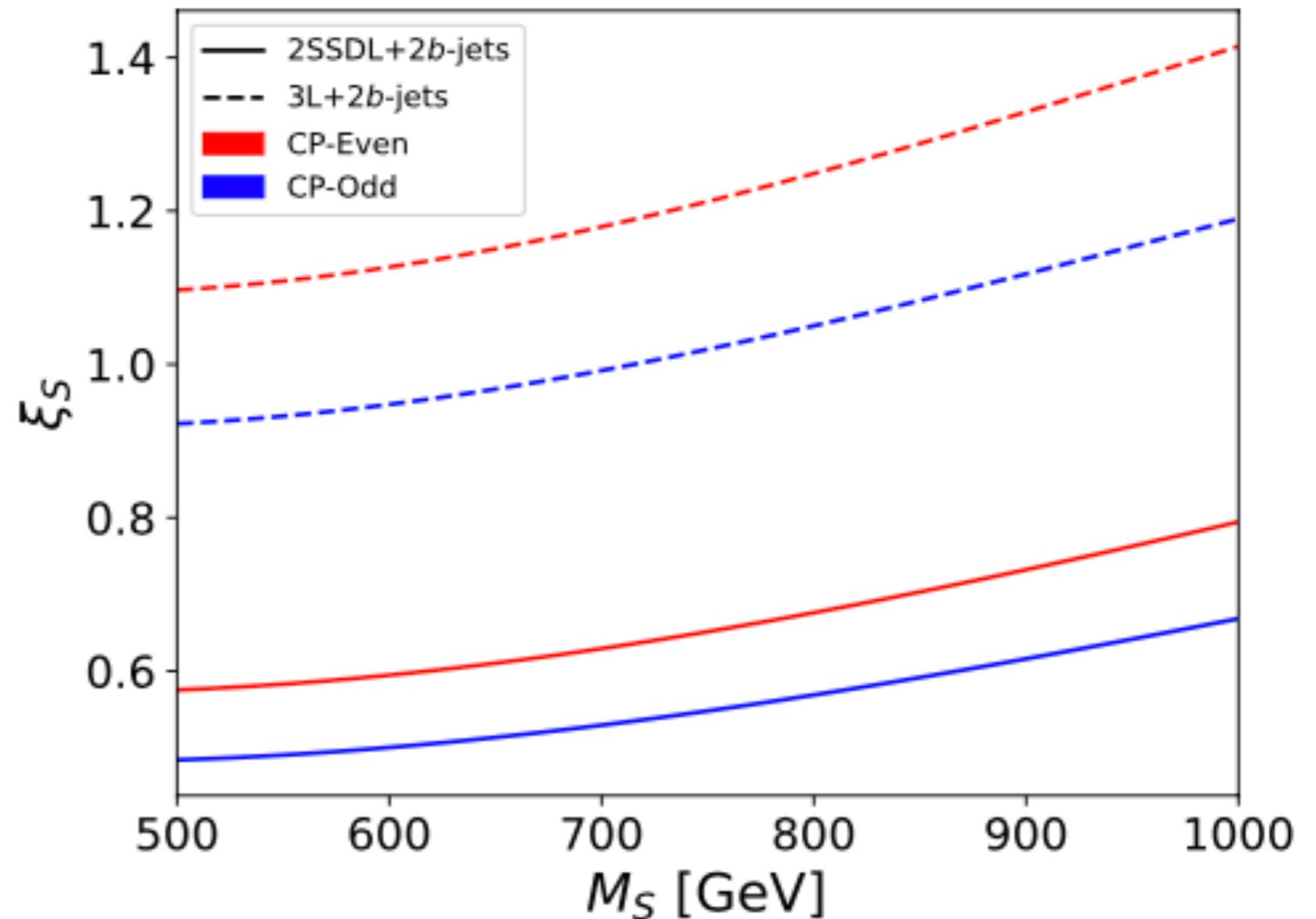
$$d\sigma^{\text{inf}} \sim 2\text{Re}(\mathcal{M}_{\text{bkg}} \mathcal{M}_{\text{res}}^*) d\text{LIPS}$$

- Interference effects that can distort mass peak are relatively small
- More significant for  $\xi_S \rightarrow 0$  but in this case sensitivity is also limited
- For CP-odd case interference should be vanishing when studying CP-even observables



# Results with GNN

- Train GNN for different masses  $M_S$  for fixed width ratios  $\Gamma_S/M_S = 0.1$  and  $\xi_S = 1$
- Can in principle set constraints on  $\xi_S < 1$ , however sensitivity is limited
- $2\sigma$  confidence limits on scalar mass with CP-even and CP-odd couplings (3/ab for 13TeV collisions)



# Mapping to 2HDM

- Map to type-2 2HDM with particle content:

- CP even:  $h$  (SM-like Higgs),  $H$  and  $H^\pm$

- CP odd:  $A$

$$\mathcal{L}_{2\text{HDM}} \supset -\frac{m_t}{v} (\xi_h \bar{t} t h + \xi_H \bar{t} t H - i \xi_A \bar{t} \gamma^5 t A)$$

- Parameters in terms of 2HDM couplings:

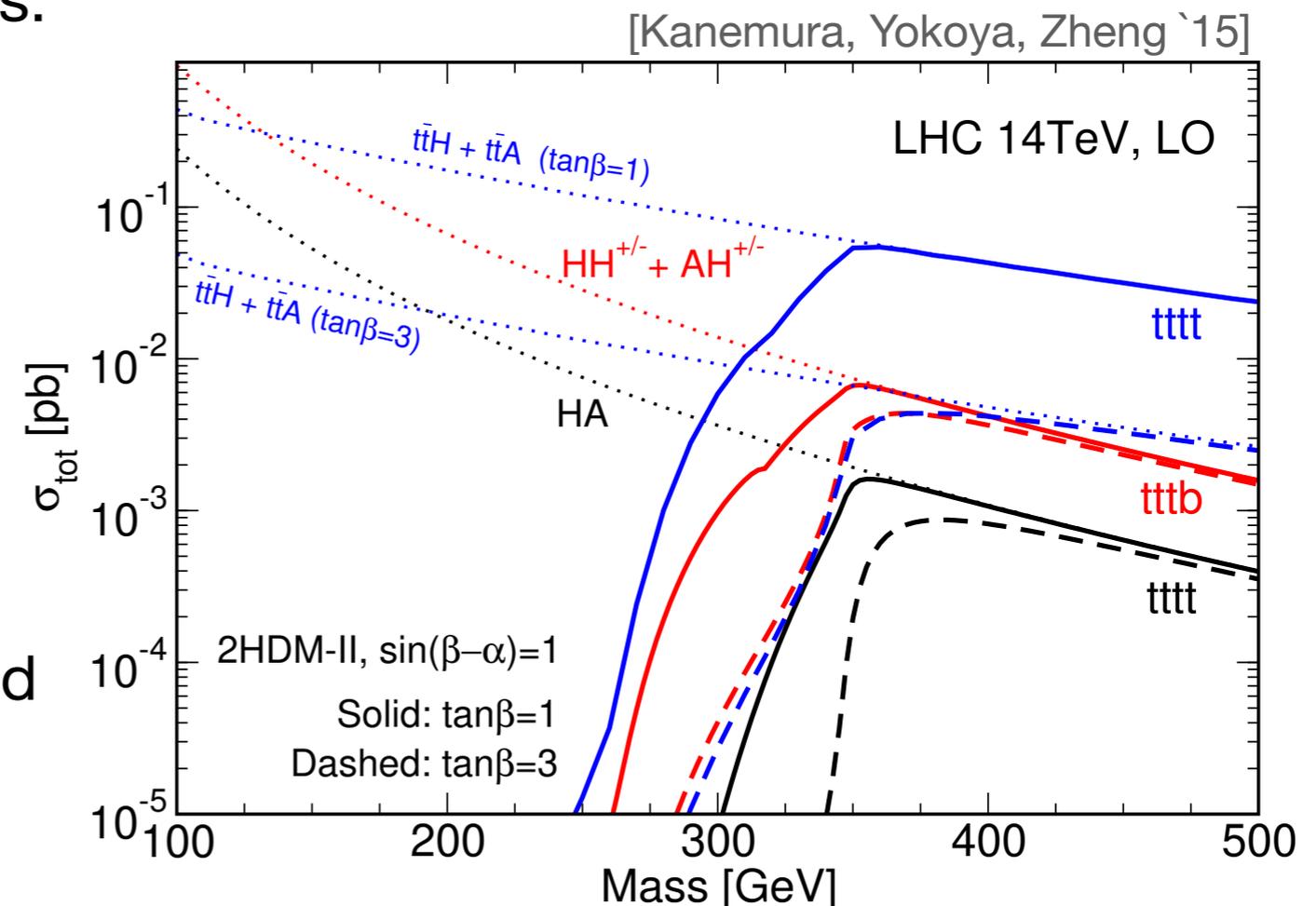
$$\xi_h = \sin(\beta - \alpha) + \cos(\beta - \alpha)$$

$$\xi_H = \cos(\beta - \alpha) - \sin(\beta - \alpha)$$

$$\xi_A = \cot(\beta)$$

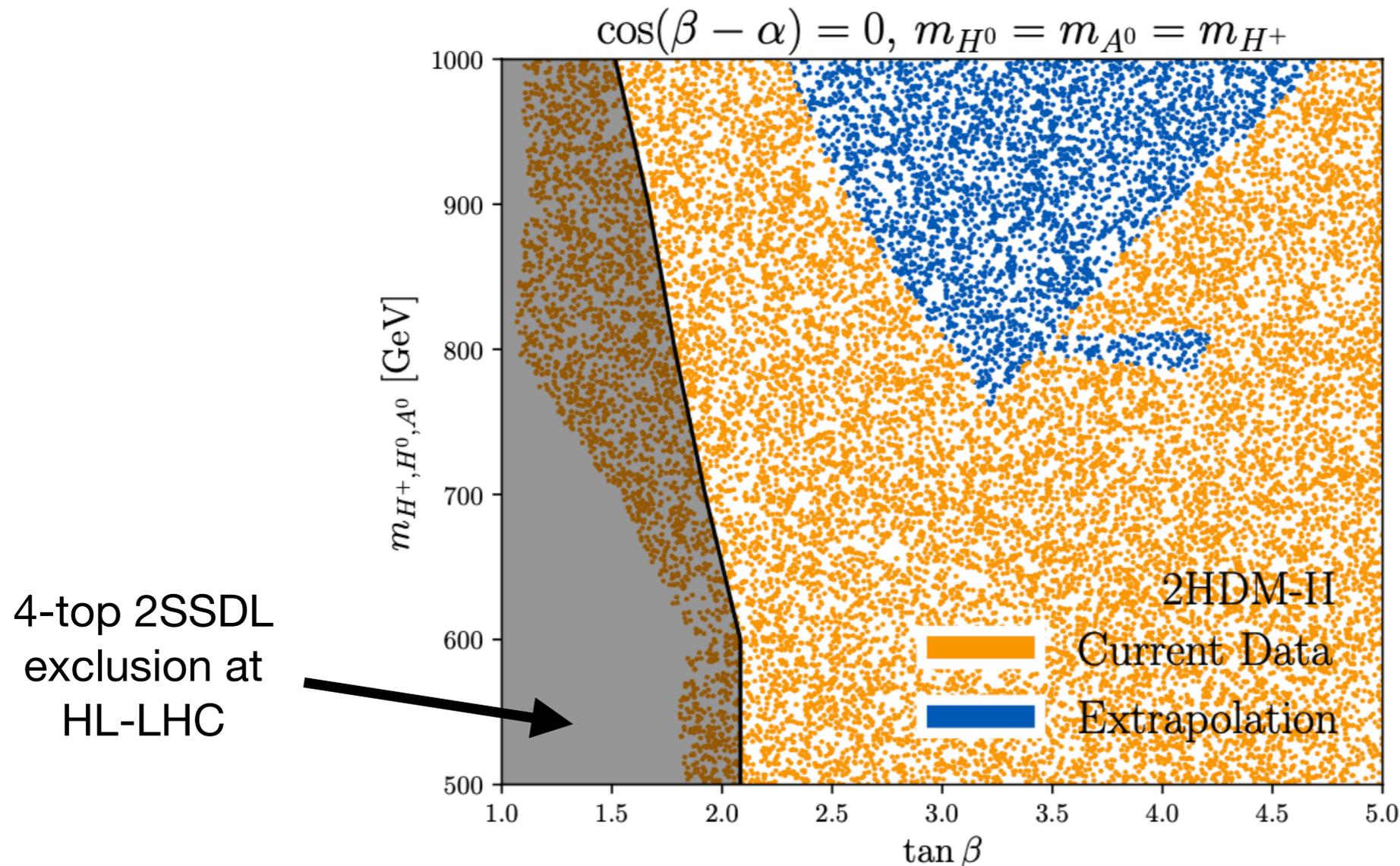
Alignment limit:  
 $\cos(\beta - \alpha) = 0$

- Sizeable multi-top interactions expected



# Exclusions

- Scan parameter space (2HDecay and HiggsBounds) for current data and extrapolated
- Sensitivity improvements mostly lead by  $H^+ \rightarrow t\bar{b}$  and  $H \rightarrow \tau^+\tau^-$
- Overlay 2SSDL resonance search results



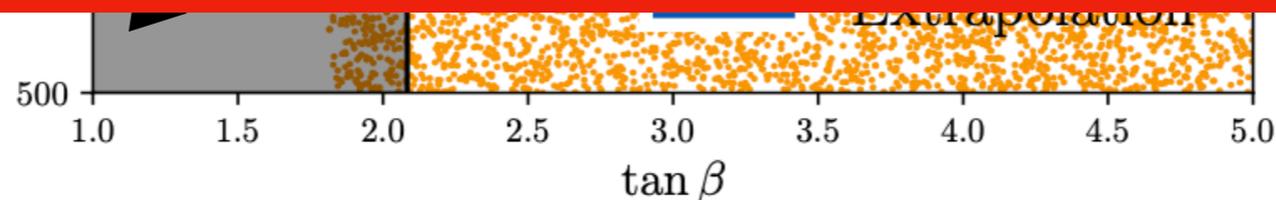
# Exclusions

- Scan parameter space (2HDecay and HiggsBounds) for current data and extrapolated
- Sensitivity improvements mostly lead by  $H^+ \rightarrow t\bar{b}$  and  $H \rightarrow \tau^+\tau^-$
- Overlay 2S
- Effects from signal-signal interference?
- Possible mixing effects from BSM states?



- Currently investigating for Two-Higgs Doublet Models
- Collaborative effort with ATLAS experimentalists at DESY

4-top 2SSD  
exclusion at  
HL-LHC



# SMEFT Prospects from four-tops

- SMEFT Lagrangian

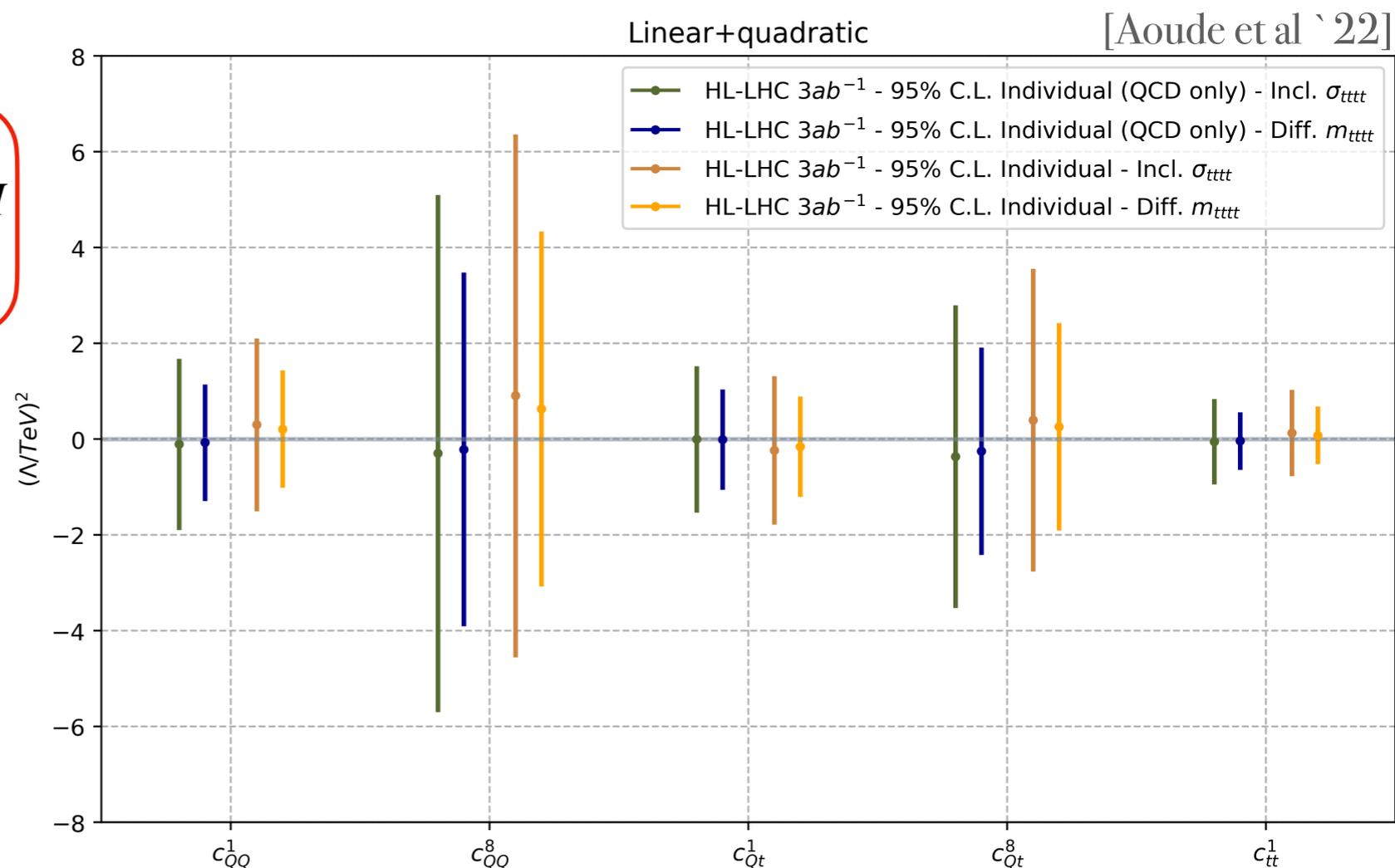
$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{n \geq 5} \sum_i \frac{C_i^{(n)}}{\Lambda^{n-4}} \mathcal{O}_i^{(n)}$$

- Sensitivity to 4-heavy 4-fermion operators in SMEFT [Aoude et al `22]
- Complements top-fits from top-pair production

Care needed! Significant  $\alpha_S^2 \alpha_{EM}$  and  $\alpha_S^2 \alpha_t$  contributions



Not unexpected, sizeable EW even at NLO [Frederix, Pagani, Zaro `18]



# Non-resonant new interactions

- Motivated EFT-related example:  $\hat{H}$  parameter [Englert et al `19]

- Can be understood as an oblique correction:

$$\hat{H} = -\frac{M_H^2}{2} \Sigma_H''(M_H^2)$$

- Introduce through  $\mathcal{L}_{\hat{H}} = \frac{\hat{H}}{m_H^2} |D_\mu D^\mu \Phi|^2$

Higgs propagator modification

$$-i\Delta(p^2, m_H^2) = \frac{1}{p^2 - m_H^2} - \frac{\hat{H}}{m_H^2}$$

- Associated modifications of couplings

$$\frac{g_{VVH}^{\hat{H}}(p^2)}{g_{VVH}^{\text{SM}}} = 1 - \hat{H} \left(1 - \frac{p^2}{m_H^2}\right), \quad \frac{g_{t\bar{t}H}^{\hat{H}}}{g_{t\bar{t}H}^{\text{SM}}} = 1 - \hat{H}$$

- Note:  $\left(\frac{1}{p^2 - M_H^2} - \frac{\hat{H}}{M_H^2}\right) \left[1 - \hat{H} \left(1 - \frac{p^2}{M_H^2}\right)\right] = \frac{1}{p^2 - M_H^2} + \mathcal{O}(p^2 - M_H^2)$

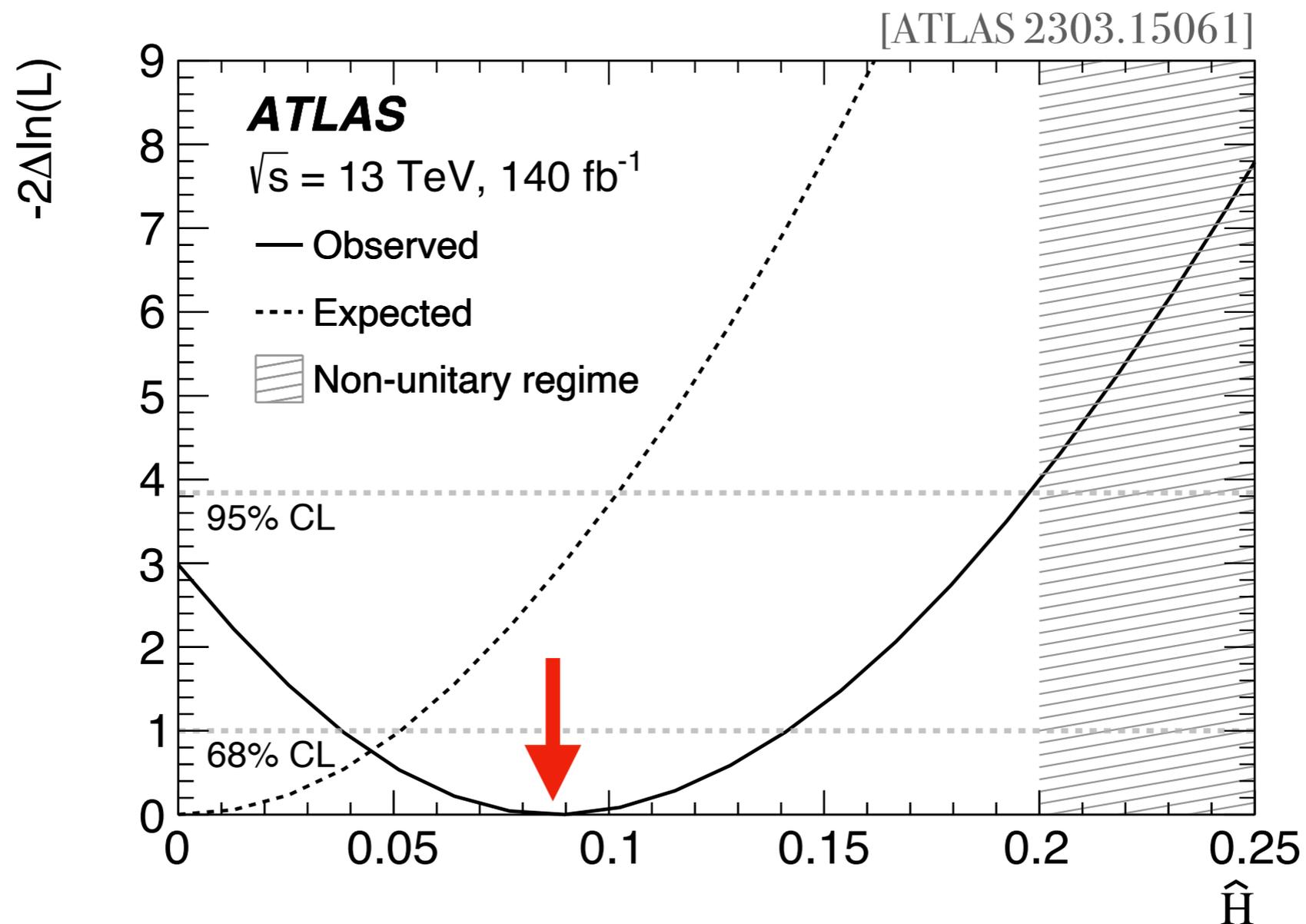


Effect of  $\hat{H}$  can be more important in 4-top

# $\hat{H}$ bounds from experiments

- Previous CMS 95% upper limit:  $\hat{H} < 0.12$  [CMS 1908.06463]
- Recent ATLAS paper also placed bounds on  $\hat{H}$

Small excess from SM!



# An example: 4-top for Higgs-philic ALP

[Anisha, Das Bakshi, Englert, PS '22 (preprint)]

- Chiral Electroweak Lagrangian (HEFT):

$$U = \exp(i\pi^a \tau^a / v)$$

$$\mathcal{L} = -\frac{1}{4} W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + \mathcal{L}_{\text{ferm}} + \mathcal{L}_{\text{Yuk}}$$

$$+ \frac{v^2}{4} \mathcal{F}_H \text{Tr}[D_\mu U^\dagger D^\mu U] + \frac{1}{2} \partial_\mu H \partial^\mu H - V(H) + \mathcal{L}_{\text{GF}} + \mathcal{L}_{\text{FP}}$$

[Buchalla, Cata, Krause '14]

[Brivio et al '14]

[Herrero, Morales '20, '21, '22]

**Non-linear construction, Higgs is a singlet**

$$\mathcal{F}_H = \left( 1 + 2(1 + \zeta_1) \frac{H}{v} + (1 + \zeta_2) \left( \frac{H}{v} \right)^2 + \dots \right)$$

## Non-linear introduction of an Axion-Like Particle (ALP):

$$\mathcal{L}_{\text{LO}}^{\text{ALP}} = \frac{1}{2} \partial_\mu \mathcal{A} \partial^\mu \mathcal{A} - \frac{1}{2} M_{\mathcal{A}}^2 \mathcal{A}^2 + a_{2D} \left( i v^2 \text{Tr}[U \tau^3 U^\dagger \mathcal{V}_\mu] \frac{\partial_\mu \mathcal{A}}{f_A} \mathcal{F}_{2D} \right)$$

ALP field

$$\mathcal{V}_\mu = (D_\mu U) U^\dagger$$

How to constrain new couplings and mass?

$$\mathcal{F}_{2D} = \left( 1 + 2\zeta_{12D} \frac{H}{v} + \zeta_{22D} \left( \frac{H}{v} \right)^2 + \dots \right)$$

[Brivio et al '17]

# An example: 4-top for Higgs-philic ALP

[Anisha, Das Bakshi, Englert, PS '22 (preprint)]

- Chiral Electroweak Lagrangian (HEFT):

$$U = \exp(i\pi^a \tau^a / v)$$

$$\mathcal{L} = -\frac{1}{4} W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + \mathcal{L}_{\text{ferm}} + \mathcal{L}_{\text{Yuk}}$$

[Buchalla, Cata, Krause '14]

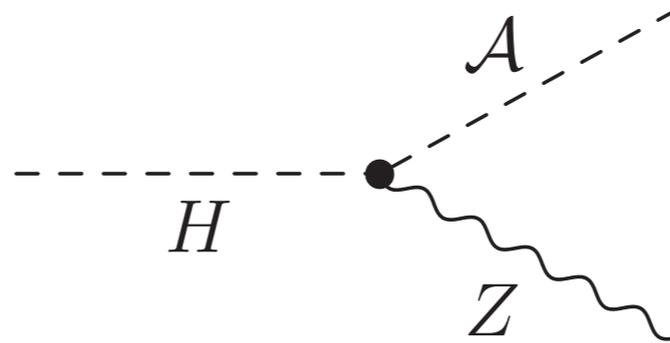
[Brivio et al '14]

[Herrero, Morales '20, '21, '22]

$\mathcal{L}_{\text{GF}} + \mathcal{L}_{\text{FP}}$

$\dots$ )

**In non-linear case ALP-Higgs-Z coupling is leading order**



Non-  
constr  
Higgs is

Non-linear i

$\mathcal{L}_{\text{LC}}^{\text{ALP}}$

ALP FIELD

$$V_\mu = (D_\mu U) U^\dagger$$

How to  
constrain new  
couplings and  
mass?

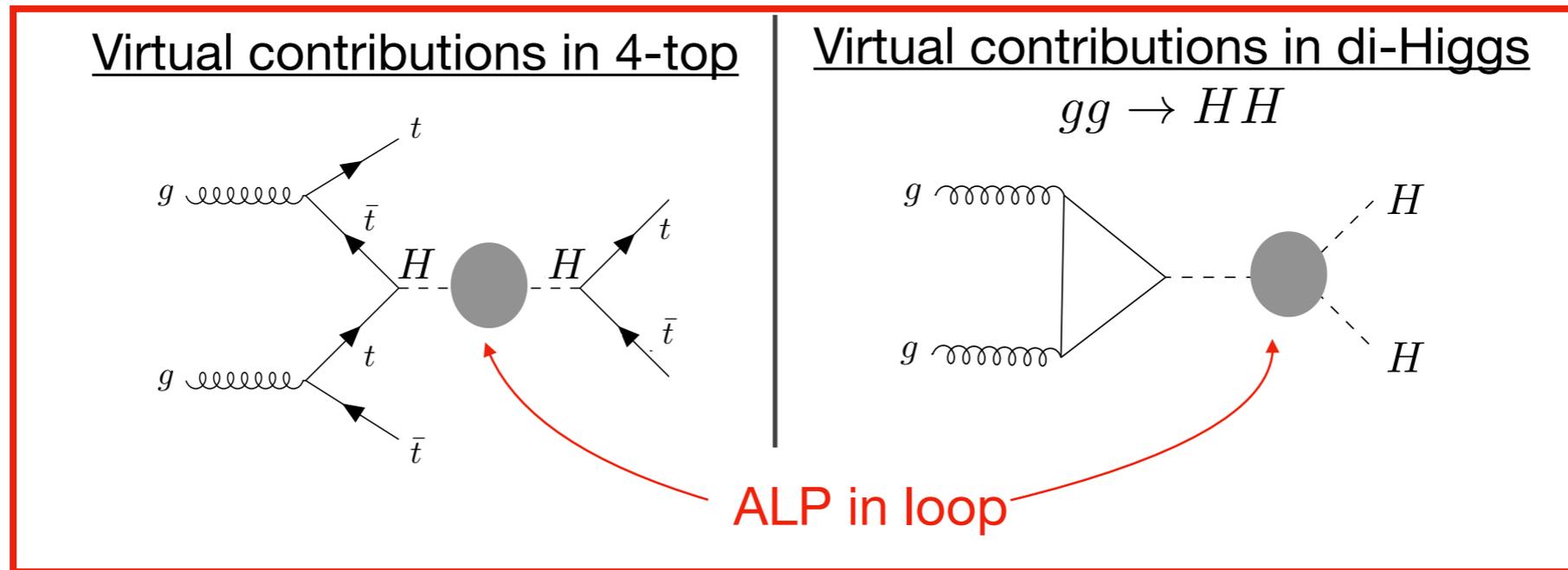
$$\mathcal{F}_{2D} = \left( 1 + 2\zeta_{12D} \frac{H}{v} + \zeta_{22D} \left( \frac{H}{v} \right)^2 + \dots \right)$$

[Brivio et al '17]

# An example: 4-top for Higgs-philic ALP

[Anisha, Das Bakshi, Englert, PS '22 (preprint)]

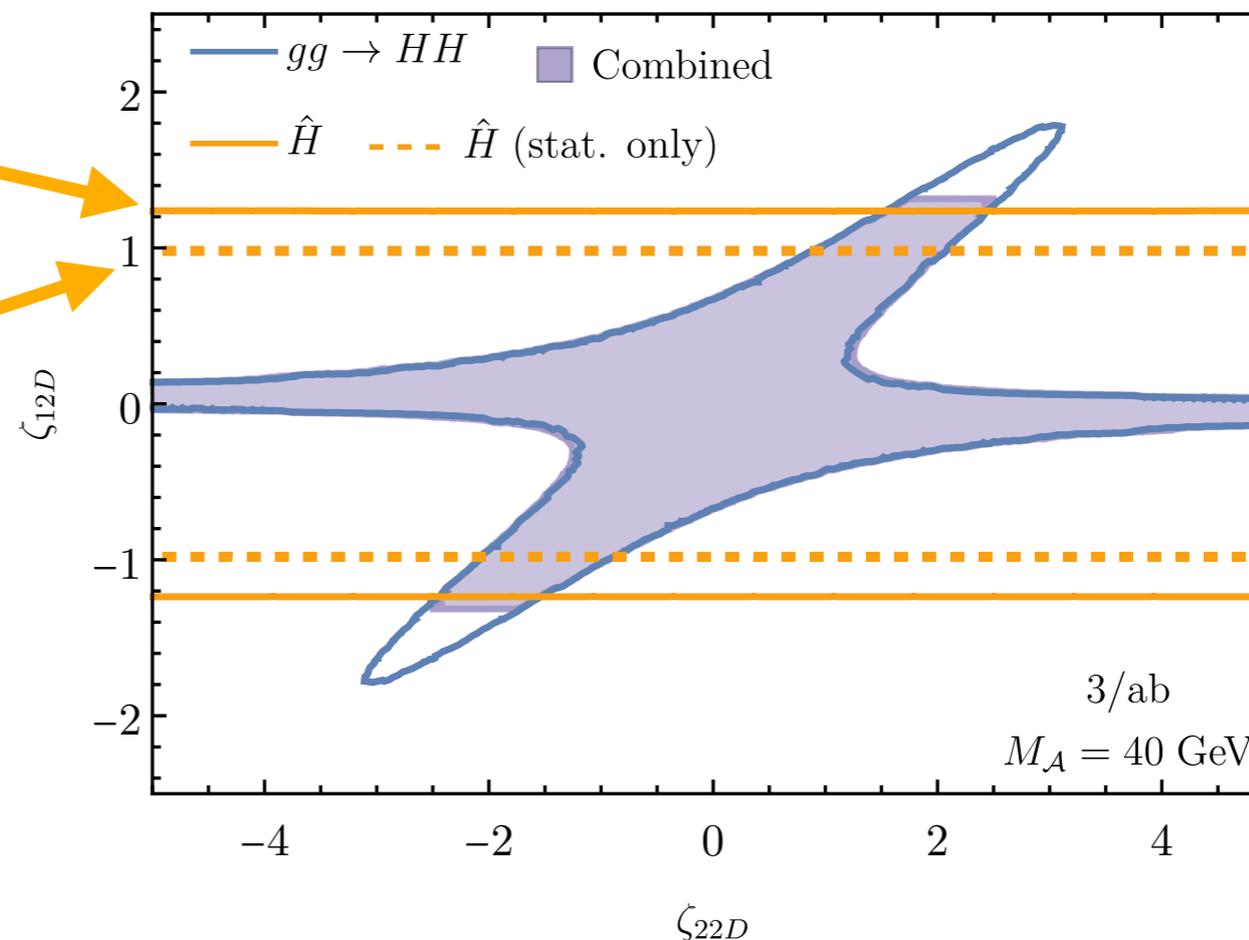
- Main probes for ALP mass  $\gtrsim 34$  GeV:



**3/ab extrapolation**

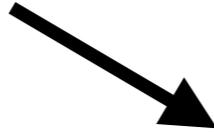
**Projection with only statistics**

[CMS-PAS-FTR-18-03]



# Conclusions

- **ML techniques** enhance sensitivity to SM 4-top production



utilised by experiments

- Sensitivity to resonances → 4-top can complement searches of top-pair production suffering from destructive signal-SM interference
- Complementary information to parameter models of UV-complete models (e.g. representative 2HDM type II)
- Measurement of  $\hat{H}$  can provide insights on non-resonant interactions: small deviation in observed data from ATLAS
- $\hat{H}$  particularly useful for models with new states coupled to Higgs

*Thank you!*

# Backup: Edge Convolution

- Signal Region Selection:
  - represent events as fully-connected bidirectional graphs
  - Graph Neural Network (GNN) for signal-background discrimination
  - Supervised learning: background  $\rightarrow$  0, signal  $\rightarrow$  1
- Each node is assigned node features  $\vec{x}_i^{(0)}$  as input
- Node features updated for each ‘message passing layer’ with Edge Convolution

$$\vec{x}_i^{(l+1)} = \frac{1}{|\mathcal{N}(i)|} \sum_{j \in \mathcal{N}(i)} \text{RELU} \left( \Theta \cdot (\vec{x}_j^{(l)} - \vec{x}_i^{(l)}) + \Phi \cdot (\vec{x}_i^{(l)}) \right)$$

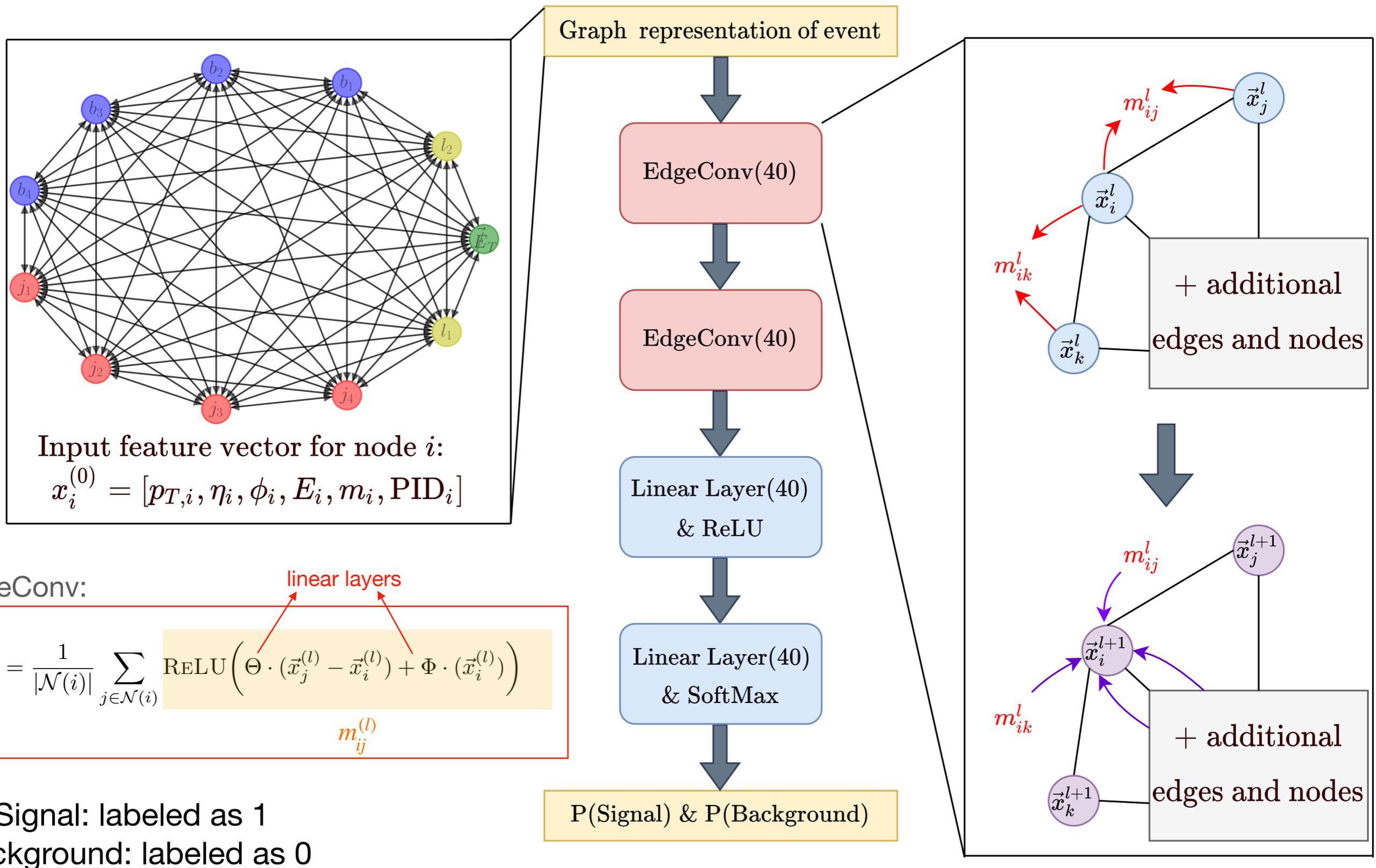
Linear Layers

Nodes in ‘neighbourhood’ of  $i$  (connected)

$m_{ij}^{(l)}$

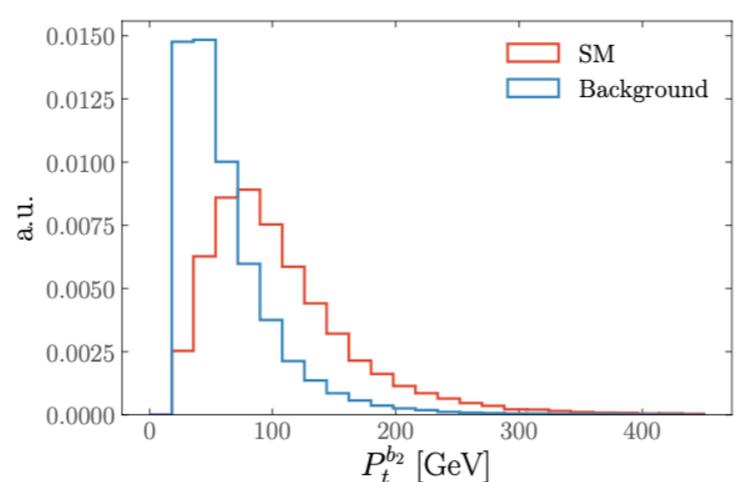
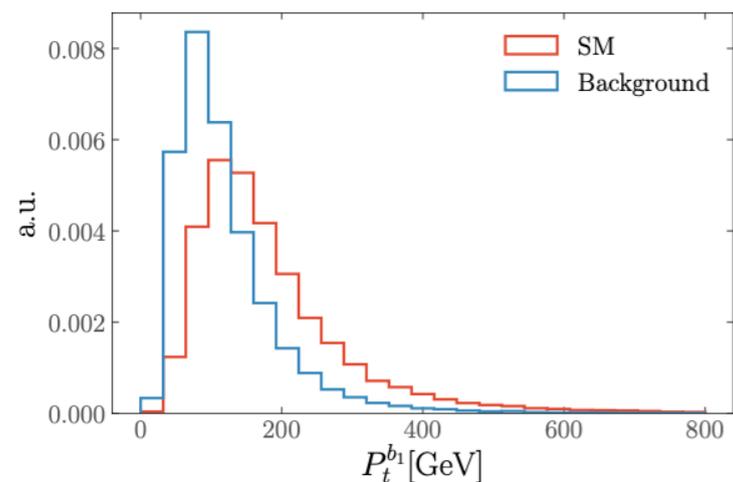
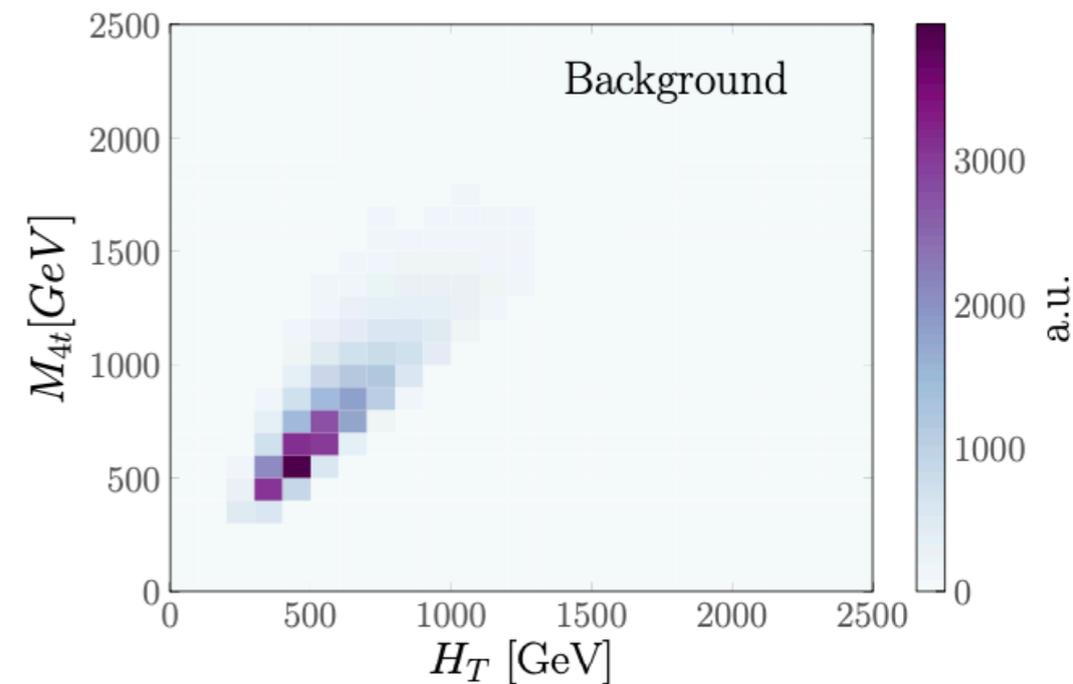
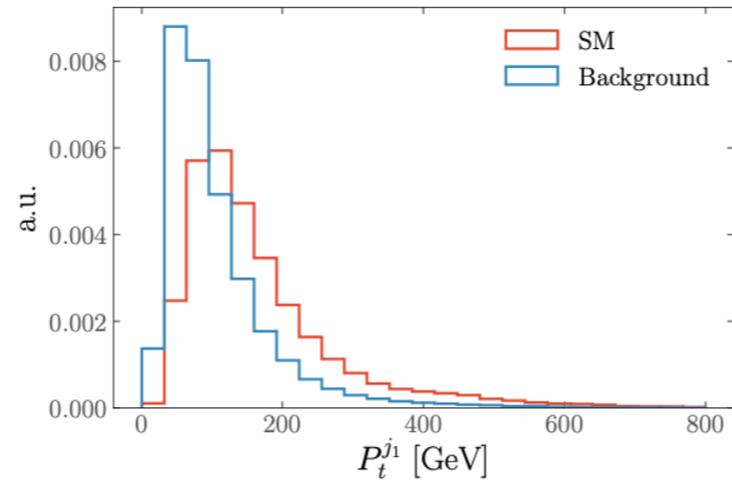
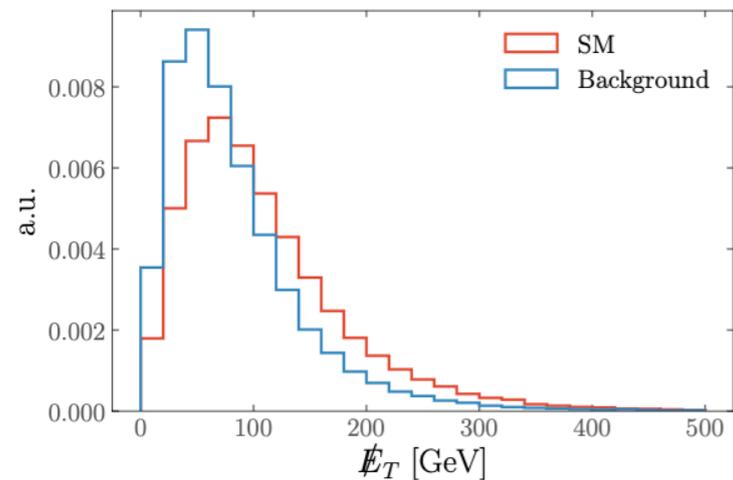
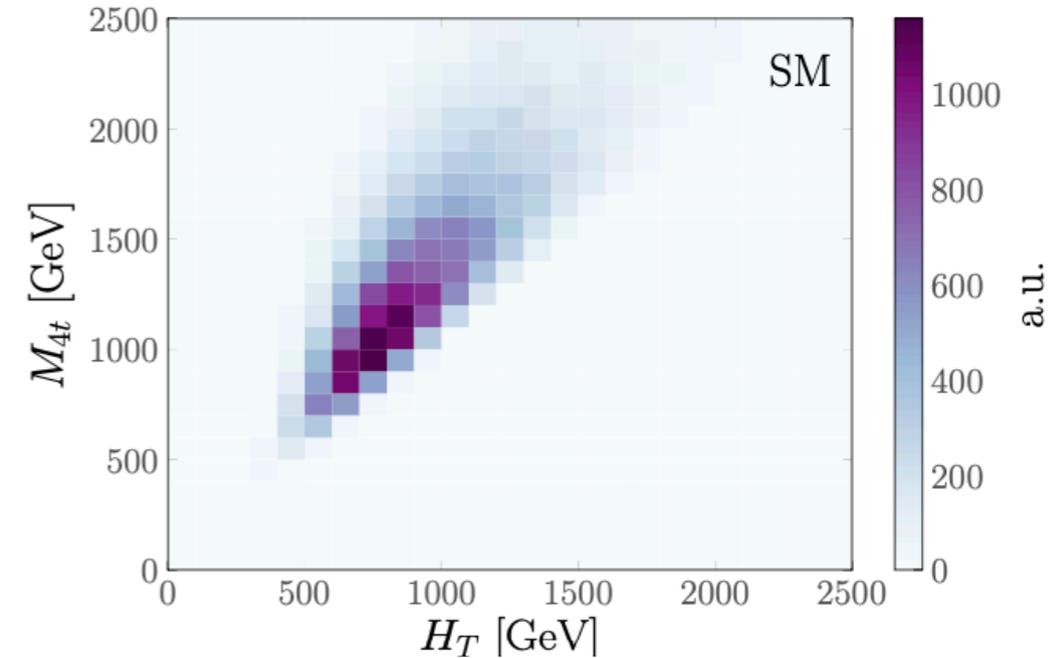
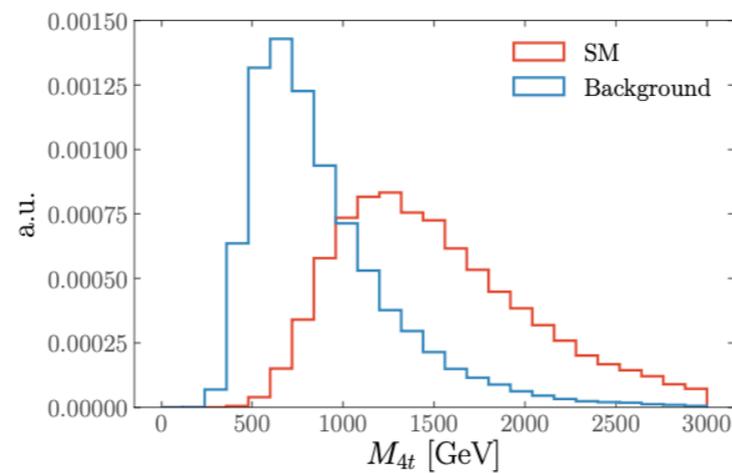
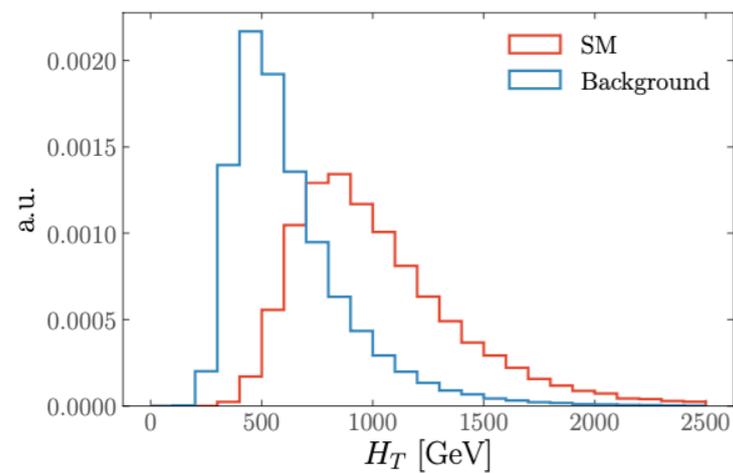
- ‘Graph Readout Operation’: mean  $\rightarrow$  gives a vector for ‘graph properties’

# Backup: Network Architecture



# Backup: Representative Distributions

- Total visible invariant mass and  $H_T$  show the best discriminative features between SM signal and SM background for 2SSDL



# Backup: Resonances vs EFT in 4-top

- Simplified Lagrangians with scalars, pseudoscalars and vector resonances (e.g. [Darme, Fuks, Maltoni '21], [Cao et al '21])

- Scalar to EFT matching



Need dim-8 operators, e.g.

$$\mathcal{O}_S^1 = \bar{t}t\bar{t}t$$

- Differences between EFT and resonances **for small couplings and masses**

