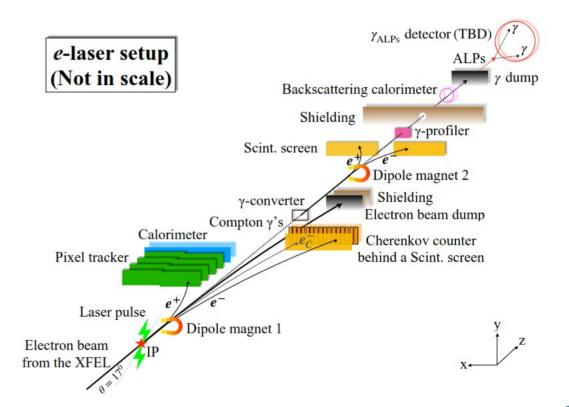
Tracking in the LUXE experiment

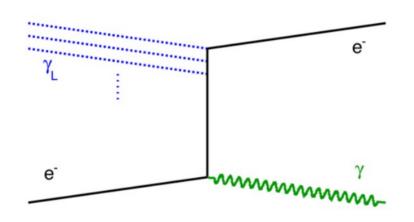
The Laser Und XFEL Experiment (LUXE)

LUXE main goals:

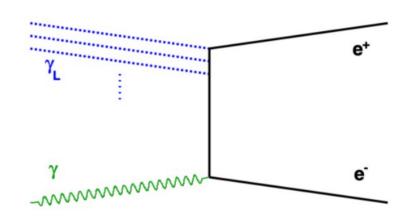
- Precision measurements in the non-pertubative regime of QED
- Search for new particles beyond the SM



The Laser Und XFEL Experiment (LUXE)



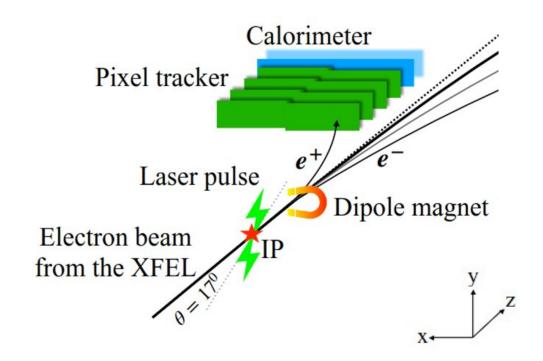
Non-linear Compton scattering



Breit-Wheeler process

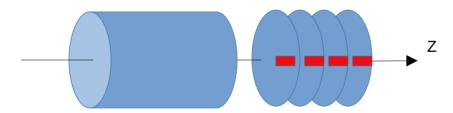
Tracking

- 4 Layers, 100 mm apart
- Each layer 2 sensors slightly overlapping
- Hits position is currently given in global coordinates: (x, y, z)
- No magnetic field in the tracker
 → Trajectories are straight lines
 (up to scattering)



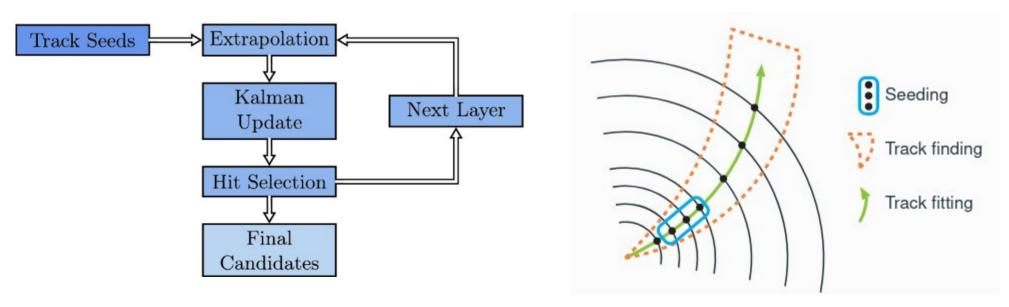
A common tracking software (ACTS)

- Experiment-independent toolkit for track reconstruction in HEP
- Assumes a barrel-shaped detector with end-cap disks
- The 4 layers are mapped to a rectangle in 4 end-cap disks:



Combinatorial Kalman Filter (CKF)

- Preforms the track finding and track fitting altogether.
- If more than one hit is found, the procedure splits for both possibilities



Kalman Filter

- Preforms track fitting only, thus, requires track candidates
- At each step adds the next hit and updates the fit
- The code is written based on the CKF for LUXE
- ACTS requires a propagator, updater, and a smoother
- Currently assume a single particle and consider all hits as a track candidate
- Next step get multiple track candidates and loop over them

Global to local coordinates

- Current given coordinates are global (x, y, z) where (0, 0, 0) is the interaction point (IP).
- ACTS requires a surface + local coordinates (u, v).
- The variance is given in term of du, dv.
- Conversion required:

```
u, v + surface \rightarrow x, y, z \rightarrow \rho, z
```

```
// compute Jacobian from global coordinates to rho/z
          rho = sqrt(x^2 + v^2)
// drho/d\{x,y\} = (1 / sqrt(x^2 + y^2)) * 2 * \{x,y\}
              = 2 * \{x,y\} / r
      dz/dz = 1 (duuh!)
double x = globalPos[Acts::ePos0];
double y = globalPos[Acts::ePos1];
double scale = 2 / std::hypot(x, y);
Acts::ActsMatrix<2, 3> jacXyzToRhoZ = Acts::ActsMatrix<2, 3>::Zero();
jacXvzToRhoZ(0, Acts::ePos0) = scale * x;
jacXyzToRhoZ(0, Acts::ePos1) = scale * y;
jacXyzToRhoZ(1, Acts::ePos2) = 1;
// compute Jacobian from local coordinates to rho/z
Acts::ActsMatrix<2, 2> jac =
    jacXyzToRhoZ * rotLocalToGlobal.block<3, 2>(Acts::ePos0, Acts::ePos0);
// compute rho/z variance
Acts::ActsVector<2> var = (jac * localCov * jac.transpose()).diagonal();
```

Quadratic unconstrained binary optimization (QUBO)

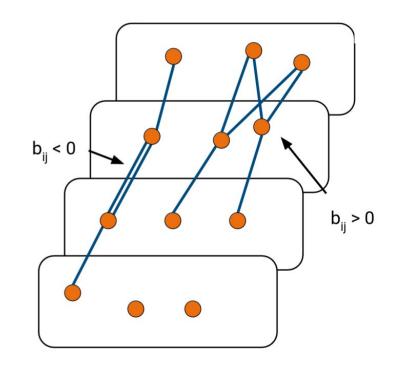
- Input for the Kalman Filter is the output of the QUBO
- The objective function to minimize:

$$O = \sum_{i}^{N} \sum_{j < i} b_{ij} T_i T_j + \sum_{i=1}^{N} a_i T_i,$$

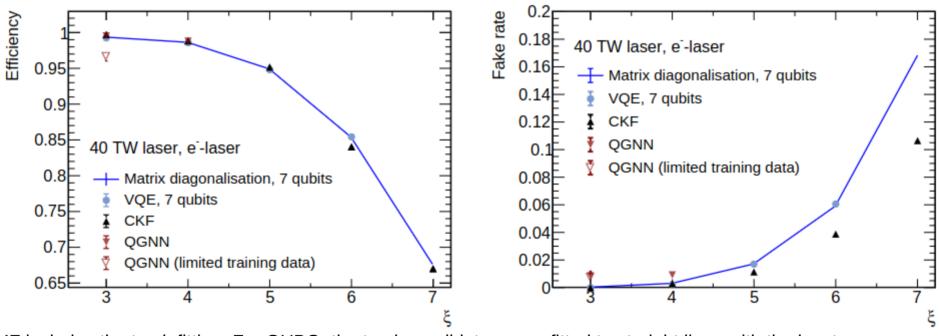
 T_i – triplets of consecutive hits, assume binary values.

b_{ij} – compatibility of triplets

a_i – quality of the triplet



CKF efficiency and fake rate



CKF includes the track fitting. For QUBO, the track candidates were fitted to straight lines with the least-square method. Current aim is to fit using the Kalman filter and compare the results. Image taken from: https://arxiv.org/pdf/2304.01690.pdf