

Dark Goo:

Bulk viscosity as an alternative to dark energy

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- 1 Motivation and Objectives
- 2 Theoretical Concepts and Presentation of the Model
 - Bulk Viscosity and Expansion
 - The “Dark Goo” Model
 - Validity of the Hydrodynamic Approximation
- 3 Results
 - Preliminaries
 - Background Evolution
 - Linear Perturbations
 - Compatibility with Observations

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Motivation and Objectives

- Experimental: Results from SNIa, CMB peaks, BAO, LSS
 - Universe accelerates now
 - Universe is made of 70% of a dark “something”
- Theoretical: Many models/mechanisms on the market (cosmological constant, quintessence, etc)
 - None seems satisfactory
 - Either suffer from severe fine tuning problems, lead to instabilities, are ruled out or are waiting further analysis
- Bottom line: Door is opened for new models to explain the acceleration
- Objective: Focus on a model that includes bulk viscosity

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Bulk Viscosity and Expansion

- Hydrodynamics is a theory of “fluid cells” (effective theory)
- Bulk viscosity characterizes deviations from local equilibrium → Modifies the energy-momentum tensor
- Effect of bulk viscosity on a FRW expansion¹

$$\dot{\rho} = -\frac{3\dot{a}}{a}(\rho + p_{\text{eff}})$$

where $p_{\text{eff}} = p - 3\zeta \frac{\dot{a}}{a}$ and $\zeta > 0$ is the bulk viscosity

- Remarks:
 - Shift between EOS and measured pressures
 - Gives a negative contribution to the pressure
→ May act as dark energy
 - ζ must be computed from a more fundamental theory

¹Weinberg, “Gravitation and Cosmology” (1972)

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The “Dark Goo” Model (1)

- Need some microscopic physics to “personify” ζ
- SM particles cannot produce any ζ in the late universe
→ Need to add a new energy component to the universe
- The model:
 - Add self-interacting scalar particles with Lagrangian:

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - \frac{1}{2} m_0^2 \phi^2 - \frac{\lambda}{4!} \phi^4$$

- Assumptions:
 - Scalar and SM particles are in thermal equilibrium in the early universe, and decouple from each other afterward
 - Hydrodynamics is valid until the present time
 - Weak coupling (technical necessity)
- Free parameters: $\lambda, m_0, \epsilon \equiv T_s/T_\gamma$
- Remark: Very different from quintessence or (generalized) Chaplygin gas models²

²Fabris et al. (2006), Colistete et al. (2007), Li and Barrow (2009), Velten and Schwach (2011)

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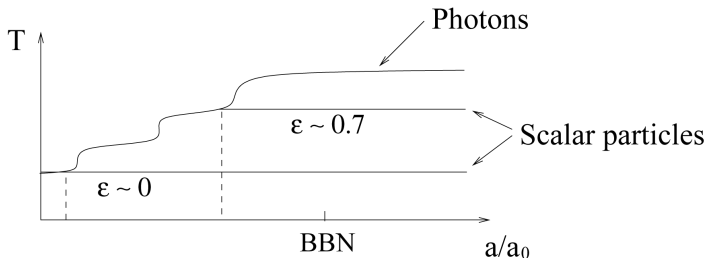
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The “Dark Goo” Model (2)



- ϵ controls the scalar-photon decoupling time
- Decoupling before BBN $\rightarrow \epsilon < 0.7$
- Scalars add relativistic degrees of freedom (N_{eff})
 \rightarrow Might affect the physics of the CMB

The “Dark Goo” Model (3)

- Pressure and density for the scalar component are:

$$\begin{aligned} p_s &= \frac{m_0^2 T_s^2}{2\pi^2} K_2 \left(\frac{m_0}{T_s} \right) + O(\lambda T_s^4) \\ \rho_s &= \frac{m_0^2 T_s}{2\pi^2} \left[T_s K_2 \left(\frac{m_0}{T_s} \right) - \frac{m_0}{2} \left(K_1 \left(\frac{m_0}{T_s} \right) + K_3 \left(\frac{m_0}{T_s} \right) \right) \right] \end{aligned}$$

- Bulk viscosity for the scalar component is³:

$$\zeta = \left(\frac{\tilde{m}^4}{\lambda^4 m_{\text{th}}} \right) \left(\frac{m_{\text{th}}}{T_s} \right)^{\kappa_3} e^{\kappa_1} e^{\kappa_2 m_{\text{th}}/T_s}$$

where $m_{\text{th}}^2 = m_0^2 + \lambda T_s^2/24$ and $\tilde{m}^2 = m_0^2 - \beta(\lambda) T_s^2/48$

- Physics of bulk viscosity:
 - Proportional to the mean free time
 - Proportional to breaking of conformal invariance

³ Jeon (1995)

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Validity of the Hydrodynamic Approximation

- For the concept of bulk viscosity to make sense, hydrodynamics must be valid
- The assumptions of hydrodynamics are:
 - Local equilibrium:

$$\frac{\Gamma_s}{H} > 1 \rightarrow \frac{m_0 \lambda^4 e^{-3m_0/T_s}}{H} > 1$$

- Small inhomogeneities and gravitational instabilities:
→ Results show that linear perturbations are well behaved
- No cavitation:

$$p_{b \max} > \rho_{\text{DE}} \rightarrow \lambda^{3/2} m_0^3 T_s > \left(\frac{3}{16\pi} \right)^{1/2} \rho_{\text{DE}}$$

where $p_{b \max}$ is the tensile strength of the scalar fluid

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- New public code (written by J. Lesgourgues) that computes cosmological perturbations and CMB physics:

C *osmic*

L *inear*

A *nisotropy*

S *olving*

S *ystem*

- All numerical results presented here are obtained using this code, slightly modified to take into account bulk viscous effects
- Website: <http://lesgourg.web.cern.ch/lesgourg/class.html>
- Go get it, it's FREE!⁴

⁴Limited time offer. Available while supplies last.

Not responsible for misuse of the code. Do physics responsibly.

Parameters in CLASS

- Parameters used in CLASS:

$$\left(\underbrace{\epsilon, \lambda, m_0}_{\text{Scalar sector}}, \underbrace{\Omega_b, h, A_s, n_s, \tau}_{\text{CDM sector}} \right)$$

where Ω_b : Baryon density fraction
 h : Reduced Hubble parameter
 A_s : Primordial spectrum amplitude
 n_s : Primordial spectrum tilt
 τ : Reionization optical depth

- More convenient to use:

$$(\epsilon, \lambda, \Omega_m, \Omega_b, h, A_s, n_s, \tau)$$

where $\Omega_b + \Omega_{\text{CDM}} + \Omega_s = 1$, $\Omega_m \equiv 1 - \Omega_s$ and Ω_s is the scalar density fraction

- Remark: m_0 can be viewed as a function of $(\epsilon, \lambda, \Omega_m, h)$

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Results for the Background Evolution (1)

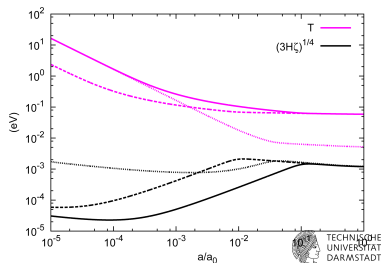
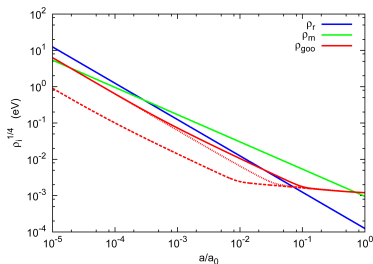
- Integrate the Friedmann equations (including bulk viscosity)
- Parameters ($\epsilon, \lambda, \Omega_m, \Omega_b, h$):
 - Full: (0.7, 0.25, 0.28, 0.05, 0.72)
 - Dashed: (0.1, 0.25, 0.28, 0.05, 0.72)
 - Dotted: (0.7, 10^{-4} , 0.28, 0.05, 0.72)
 (correspond to $m_0 = 1.0, 1.0, 0.027$ eV)

• Evolution of densities:

- $T_s \gg m_0$: $\rho_s \propto a^{-4}$, $3H\zeta \ll \rho_s$
- $T_s \sim m_0$: $\rho_s \propto a^{-3}$
- $T_s \ll m_0$: $3H\zeta \sim \rho_s$

• Remarks:

- Tend to a fixed point with $p_{\text{eff}} = -|w|\rho_s$
- Fixed point not reached immediately



Results for the Background Evolution (2)

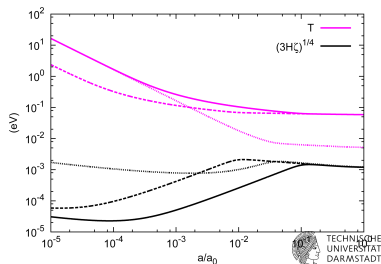
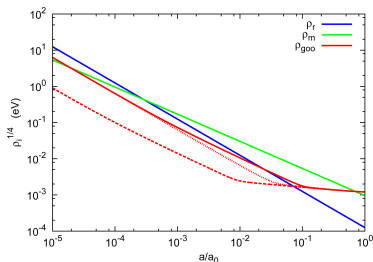
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 (correspond to $m_0 = 1.0, 1.0, 0.027$ eV)

Varying ϵ :

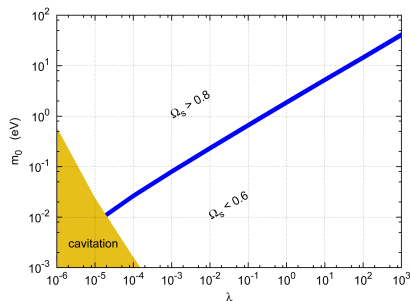
- $\epsilon \searrow \Rightarrow T_s \searrow$
 \Rightarrow DE domination happens sooner
- ϵ has effects only at high T
 \rightarrow Increases relativistic d.o.f.

Varying λ (and thus m_0):

- $\lambda \searrow \Rightarrow m_0 \searrow$
 \Rightarrow DE domination happens later
- $\lambda \nearrow \Rightarrow$ Matter-like period \nearrow
 \rightarrow Unified model of DM and DE?



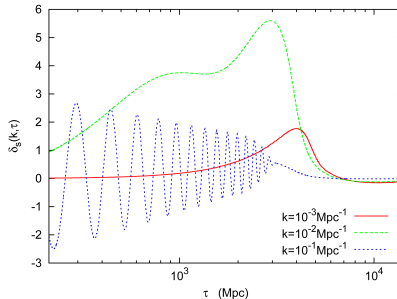
Results for the Background Evolution (3)



- m_0 can be viewed as a function of $(\epsilon, \lambda, \Omega_m, h)$
- Can check that m_0 is independent of ϵ
- Explore parameter space:
($\Omega_m \in [0.2, 0.4]$, $h \in [0.65, 0.75]$) (thin blue band)
- Results with hydro constraints:
 $\lambda > 2 \times 10^{-5}$ and $m_0 > 0.01$ eV
 $\lambda \in [2 \times 10^{-5}, 1]$ and $m_0 \in [0.01, 2]$ eV

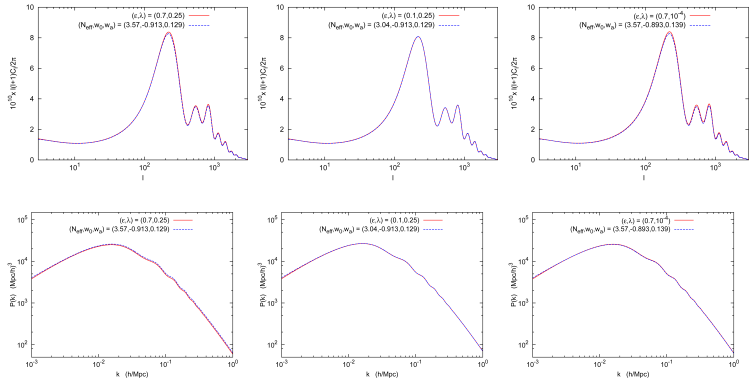
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Results for Perturbations (1)



- Density perturbations for 3 modes with $(\epsilon, \lambda) = (0.7, 0.25)$
- All modes are damped out at $\tau \approx 3000$ Mpc
→ Equations are stable
- Dark Goo model is similar to any model with negligible perturbations at late times (e.g. Λ CDM)

Results for Perturbations (2)



- Rad. domination: Extra scalar d.o.f. evolve differently than decoupled neutrinos (i.e. no anisotropic stress tensor)
- Expect larger oscillation amplitudes \rightarrow Higher CMB peaks
- For large $\epsilon = 0.7$: Dark Goo peaks $>$ w CDM peaks
- For small $\epsilon = 0.1$: No significant difference

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Summary of Results

- Effective neutrino number (at early times):

$$N_{\text{eff}} = 3.04 + 2.2\epsilon^4$$

Model can account for any value in the range
 $3.04 < N_{\text{eff}} < 3.62$ (or $0 < \epsilon < 0.7$)

- Equation of state parameter:

$$w_0 = -0.9085 + 0.21(\Omega_m - 0.3) + 3\lambda^{-0.4}10^{-4}$$

- Time dependence of the dark energy component:

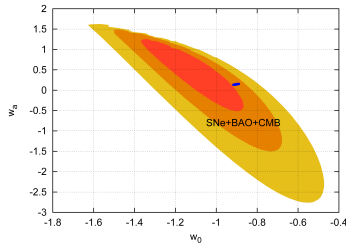
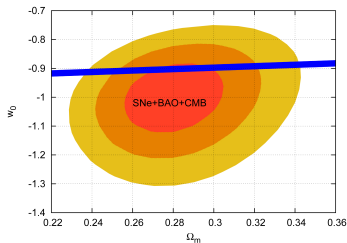
$$w_a = 0.129 + 0.02(\Omega_m - 0.3) + \lambda^{-0.5}10^{-4}$$

where the wCDM parametrization used is⁵

$$w(a) = w_0 + w_a(1 - a/a_0)$$

⁵Chevallier and Polarski (2000), Linder (2002)

Compatibility with Observations



- Left panel: Vary $h \in [0.714, 0.724]$, $\lambda \in [2 \times 10^{-5}, 1]$
- Right panel: Vary h, λ in same range, $\Omega_m \in [0.245, 0.306]$
- Bottom line:
 - Dark Goo model compatible with current data
 - Dark Goo model predicts $(w_0, w_a) \sim (-0.9, 0.13)$

- Features of the Dark Goo model:
 - First principles computation of bulk viscosity
 - Discussion in terms of physical properties of particles
 - Model is falsifiable (parameter space bounded)
 - Less fine tuning (compared to quintessence, for example)
- Future work:
 - More rigorous study of hydro assumptions (cavitation in particular)
 - Extend the model to include Dark Matter?

But really, what is Dark Goo?

Example of a Dark Goo filled universe...



THANK YOU!!!