

Odderon at the EIC from exclusive production of C-even quarkonia

Sanjin Benić (University of Zagreb)

SB, Dumitru, Kaushik, Motyka, Stebel, in preparation

SB, Horvatić, Kaushik, Vivoda, Phys. Rev. D **108** (2023) 7, 074005

Synergies between the EIC and the LHC, Hamburg, Germany, December 15, 2023



HRZZ
Croatian Science
Foundation

Odderon in QCD

. odderon is state with vacuum quantum numbers which is C-odd

Lukaszuk, Nicolescu (1973)

-> In QCD at least **three gluons** contracted with d_{abc} color factor

. **is pp and $p\bar{p}$ scattering same at high energy?**

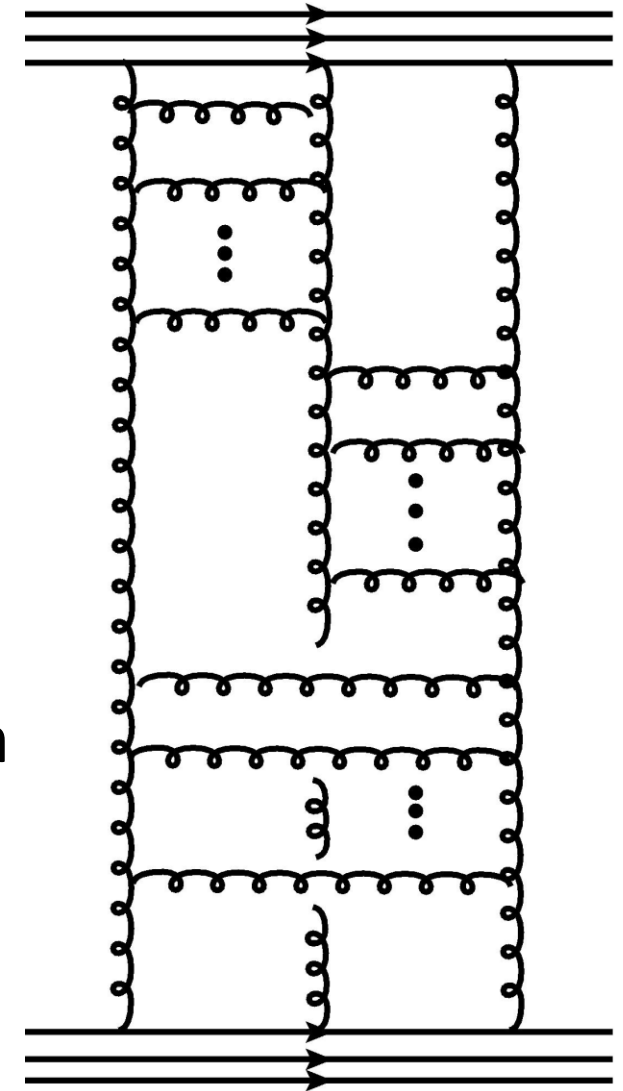
. Bartels-Jaroszewicz-Kwiecinski-Praszalowicz (BJKP) equation was constructed

-> pairwise BFKL ladders between three (reggeized) gluons

Bartels (1979)

Jaroszewicz (1980)

Kwiecinski, Praszalowicz (1980)



Odderon searches

. recent exciting news by the 5 sigma odderon discovery in pp vs p \bar{p}

. interpretation in terms of a hard (p)QCD odderon?

➡ turn to DIS for better control

. odderon exchange guaranteed

by C=+1 meson/quarkonia in the final state

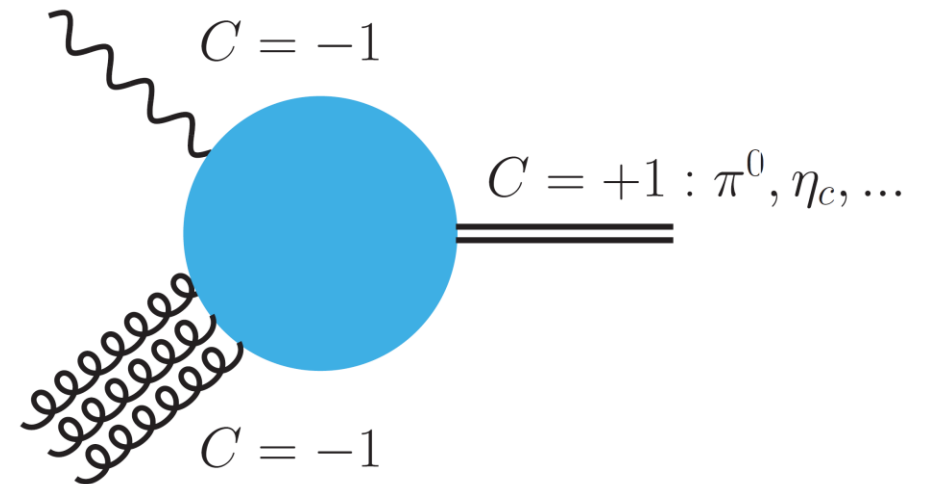
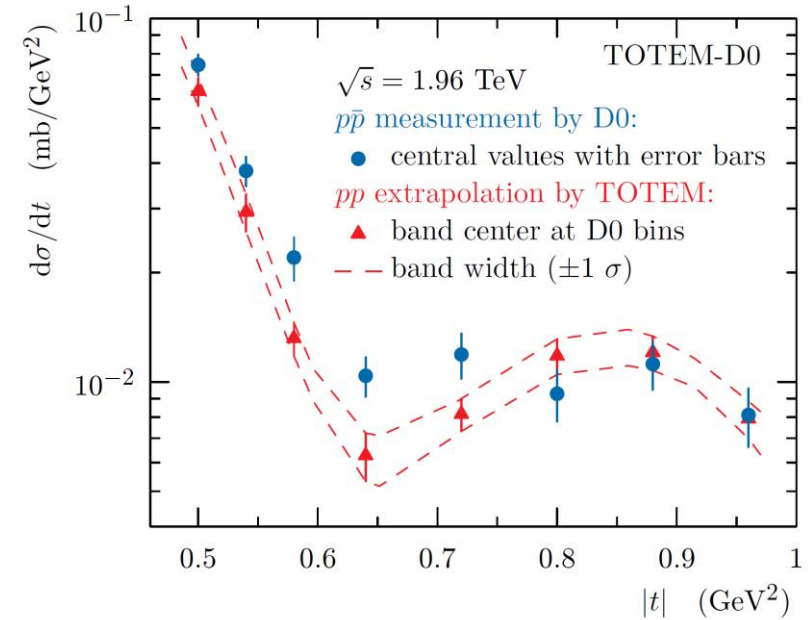
. HERA: null result from H1 collaboration

H1 (2002)

$\sigma(\gamma^* p \rightarrow \pi^0 N^*) < 49$ nb

. similar for a₂ and f₂ tensor mesons Ewerz (2003)

TOTEM, D0 (2021)



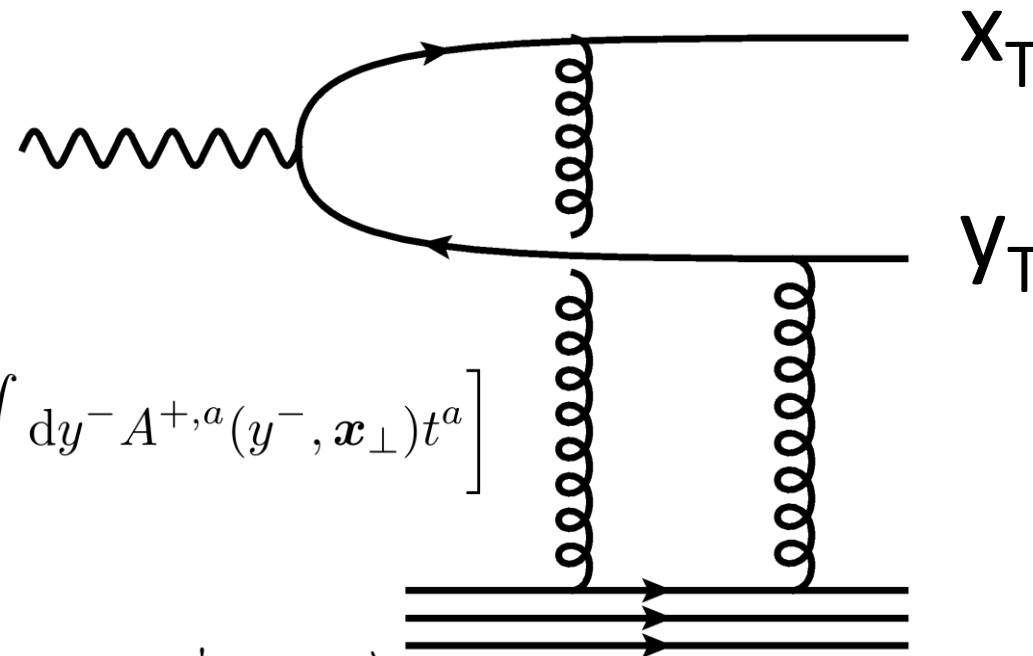
Odderon: a modern perspective

Kovchegov, Szymanowski, Wallon (2004)
Hatta, Iancu, Itakura, McLerran (2005)

. dipole S-matrix

$$\mathcal{D}(\mathbf{x}_\perp, \mathbf{y}_\perp) = \frac{1}{N_c} \text{tr} \langle V(\mathbf{x}_\perp) V^\dagger(\mathbf{y}_\perp) \rangle$$

$$V(\mathbf{x}_\perp) = \mathcal{P} \exp \left[-ig \int dy^- A^{+,a}(y^-, \mathbf{x}_\perp) t^a \right]$$



. odderon as the imaginary part

$$\mathcal{O}(\mathbf{x}_\perp, \mathbf{y}_\perp) = -\frac{1}{2iN_c} \text{tr} \langle V(\mathbf{x}_\perp) V^\dagger(\mathbf{y}_\perp) - V(\mathbf{y}_\perp) V^\dagger(\mathbf{x}_\perp) \rangle$$

. expand the
Wilson line

$$\mathcal{O}(\mathbf{x}_\perp, \mathbf{y}_\perp) = -\frac{g^3}{24N_c} d^{abc} (\alpha^a(\mathbf{x}_\perp) - \alpha^a(\mathbf{y}_\perp)) (\alpha^b(\mathbf{x}_\perp) - \alpha^b(\mathbf{y}_\perp)) (\alpha^c(\mathbf{x}_\perp) - \alpha^c(\mathbf{y}_\perp))$$

. charge conjugation $\mathbf{x}_\perp \leftrightarrow \mathbf{y}_\perp \rightarrow$ **odderon flips sign (C-odd)**

Odderon: a modern perspective

Kovchegov, Szymanowski, Wallon (2004)
 Hatta, Iancu, Itakura, McLerran (2005)
 Motyka (2006)

$$\mathbf{r}_\perp = \mathbf{x}_\perp - \mathbf{y}_\perp \text{ (dipole size)} \qquad \mathbf{b}_\perp = \frac{1}{2}(\mathbf{x}_\perp + \mathbf{y}_\perp) \text{ (impact parameter)}$$

- > odderon linear in \mathbf{r}_\perp -> need another vector: $\mathbf{r}_\perp \cdot \mathbf{b}_\perp$
- > **odderon as a GTMD** (generalized transverse momentum distribution)
- > **vanishes at $b_T=0$**

$$\mathcal{D}(\mathbf{r}_\perp, \mathbf{b}_\perp) = 1 - \mathcal{N}(\mathbf{r}_\perp, \mathbf{b}_\perp) + i\mathcal{O}(\mathbf{r}_\perp, \mathbf{b}_\perp)$$

. non-linear (Balitsky-Kovchegov) evolution equation

$$\frac{\partial \mathcal{O}(\mathbf{r}_\perp, \mathbf{b}_\perp)}{\partial Y} = \frac{\alpha_S N_c}{2\pi^2} \int_{\mathbf{r}_{1\perp}} \frac{\mathbf{r}_\perp^2}{\mathbf{r}_{1\perp}^2 \mathbf{r}_{2\perp}^2} \left[\mathcal{O}(\mathbf{r}_{1\perp}, \mathbf{b}_\perp) + \mathcal{O}(\mathbf{r}_{2\perp}, \mathbf{b}_\perp) - \mathcal{O}(\mathbf{r}_\perp, \mathbf{b}_\perp) \right. \\ \left. - \mathcal{N}(\mathbf{r}_{1\perp}, \mathbf{b}_\perp) \mathcal{O}(\mathbf{r}_{2\perp}, \mathbf{b}_\perp) - \mathcal{O}(\mathbf{r}_{1\perp}, \mathbf{b}_\perp) \mathcal{N}(\mathbf{r}_{2\perp}, \mathbf{b}_\perp) \right]$$

linear piece:
equivalent to BJKP

saturation corrections:
acts to suppress the
odderon at high energy

$$Y = \log(1/x)$$

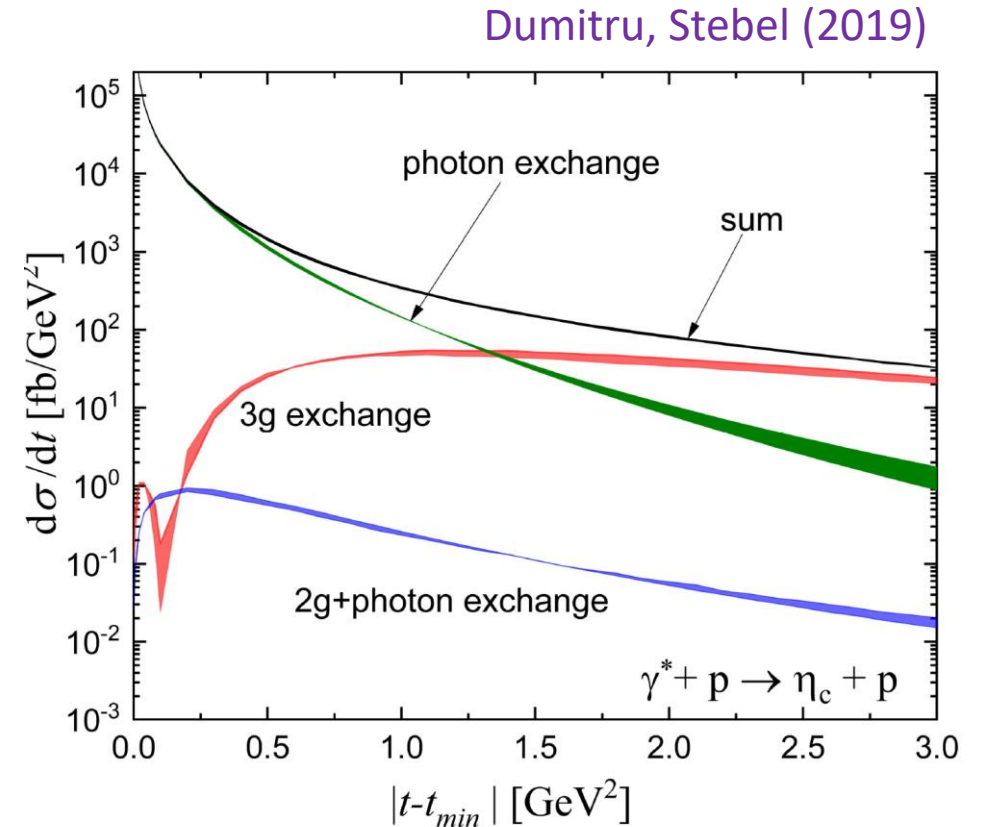
Theory status (with η_c)

Czyzewski, Kwiecinski, Motyka, Sadzikowski (1997)
Bartels, Braun, Colferai, Vacca (2001)
Dumitru, Stebel (2019)

- . no experimental detection so far -> EIC, LHC (UPC)?
- . from late 90's theorists start to explore exclusive production of C-even quarkonia -> focus is on η_c

-> prominent feature: almost flat cross section (Donnachie-Landshoff mechanism)

1. issues with η_c detection
(small branching ratios, $J/\psi \rightarrow \eta_c \gamma$ feed-down)
2. odderon cross sections in general small
 $\sim 10^2 \text{ fb/GeV}^2$ for moderate x ($x = 0$).
3. no quantum evolution



Motivations

1. issues with η_c detection

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

→ consider other $C=+1$ quarkonia: χ_{cJ} ($J = 0, 1, 2$) family

. decay mode $\chi_{cJ} \rightarrow J/\psi \gamma$ (χ_c is a P-wave, BR $\sim 30\%$ for χ_{c1} !) Pentchev, DIS2023, GHP 2023

. about 56 χ_{c1} 's and ~ 12 χ_{c2} 's **detected** (!) near threshold with GlueX

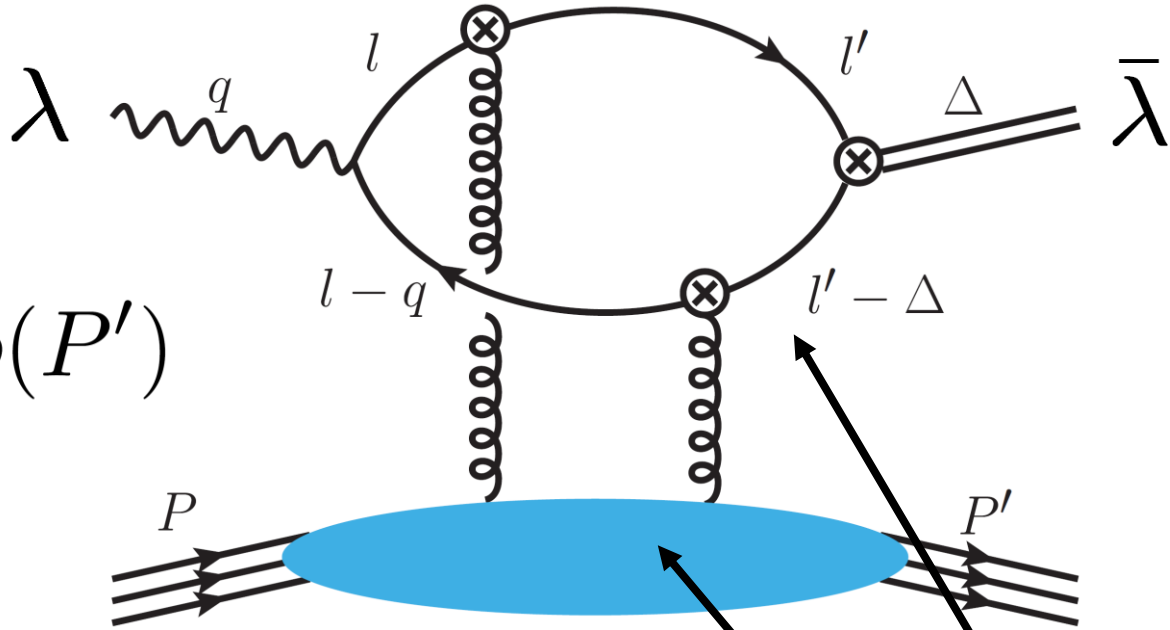
2. odderon cross sections **in general small**

→ **utilize** high luminosity at the EIC

3. **no quantum evolution effects** -> solve the BK evolution for the odderon

Amplitude

$$\gamma^*(q)p(P) \rightarrow \mathcal{H}(\Delta)p(P')$$



$$\langle \mathcal{M}_{\lambda\bar{\lambda}} \rangle = 2q^- N_c \int_{\mathbf{r}_\perp \mathbf{b}_\perp} e^{-i\Delta_\perp \cdot \mathbf{b}_\perp} \boxed{i\mathcal{O}(\mathbf{r}_\perp, \mathbf{b}_\perp)} \mathcal{A}_{\lambda\bar{\lambda}}(\mathbf{r}_\perp, \Delta_\perp)$$

. reduced amplitude $\mathcal{A}_{\lambda\bar{\lambda}}(\mathbf{r}_\perp, \Delta_\perp) = \int_z \int_{l_\perp l'_\perp} \sum_{h\bar{h}} \Psi_{\lambda, h\bar{h}}^\gamma(l_\perp, z) \Psi_{\bar{\lambda}, h\bar{h}}^{\mathcal{H}*}(l'_\perp - z\Delta_\perp, z) e^{i(l_\perp - l'_\perp + \frac{1}{2}\Delta_\perp) \cdot \mathbf{r}_\perp}$

. perturbative photon wave function $\Psi_{\lambda, h\bar{h}}^\gamma(\mathbf{k}_\perp, z) \equiv \sqrt{z\bar{z}} \frac{\bar{u}_h(k) e q_c \not{\epsilon}(\lambda, q) v_{\bar{h}}(q-k)}{\mathbf{k}_\perp^2 + \varepsilon^2}$ $\varepsilon \equiv \sqrt{m_c^2 + z\bar{z}Q^2}$
 $z = \frac{k^-}{q^-}$ $\bar{z} \equiv 1 - z$

Charmonia wave functions

scalar function: **boosted Gaussian ansatz**

$$\Psi_{\bar{\lambda}, h \bar{h}}^{\mathcal{H}}(\mathbf{k}_{\perp}, z) \equiv \frac{1}{\sqrt{z \bar{z}}} \underbrace{\bar{u}_h(k) \Gamma_{\bar{\lambda}}^{\mathcal{H}}(k, k') v_{\bar{h}}(k')}_{\text{spin structure}} \phi_{\mathcal{H}}(\mathbf{k}_{\perp}, z)$$

Forshaw, Sandapen, Shaw (2004)
Kowalski, Motyka, Watt (2006)

. covariant ansatz

spin structure

$$\Gamma_{\bar{\lambda}}^{\mathcal{H}}(k, k') = \begin{cases} i\gamma_5, & \mathcal{H} = \mathcal{P} \\ 1, & \mathcal{H} = \mathcal{S} \\ i\gamma_5 \not{E}(\bar{\lambda}, \Delta_0), & \mathcal{H} = \mathcal{A} \\ \frac{1}{4} (\gamma_{\mu}(k_{\nu} - k'_{\nu}) + \gamma_{\nu}(k_{\mu} - k'_{\mu})) E^{\mu\nu}(\bar{\lambda}, \Delta_0), & \mathcal{H} = \mathcal{T} \end{cases}$$

polarization vector for spin 1

η_c (Dumitru, Stebel (2019))

χ_c

spin 2 -> coupling to the energy momentum tensor

spin 2 polarization tensor: in terms of $E^{\mu}(\bar{\lambda}, \Delta_0)$ via Clebsch-Gordan coeffs

. transversality condition

$$\Delta_0 \cdot E(\bar{\lambda}, \Delta_0) = 0 \quad \Delta_0 = k + k'$$

Berger, Donnachie, Dosch, Nachtmann (2000)
SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

Final amplitudes: scalar charmonia

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

. reduced amplitudes

off-forward phase $\delta_{\perp} = \frac{1}{2}(z - \bar{z})\Delta_{\perp}$

$$\mathcal{A}_0(\mathbf{r}_{\perp}, \Delta_{\perp}) = eq_c \int_z e^{-i\delta_{\perp} \cdot \mathbf{r}_{\perp}} \mathcal{A}_L(r_{\perp})$$

$$\mathcal{A}_{\lambda=\pm 1}(\mathbf{r}_{\perp}, \Delta_{\perp}) = eq_c \lambda e^{i\lambda\phi_r} \int_z e^{-i\delta_{\perp} \cdot \mathbf{r}_{\perp}} \mathcal{A}_T(r_{\perp})$$

$$\mathcal{A}_L(r_{\perp}) \equiv -\frac{2}{\pi} m_c Q(z - \bar{z}) K_0(\varepsilon r_{\perp}) \phi_S(r_{\perp}, z)$$

$$\mathcal{A}_T(r_{\perp}) \equiv \frac{i\sqrt{2} m_c}{2\pi z\bar{z}} \left[(z - \bar{z})^2 \varepsilon K_1(\varepsilon r_{\perp}) \phi_S(r_{\perp}, z) - K_0(\varepsilon r_{\perp}) \frac{\partial \phi_S}{\partial r_{\perp}} \right]$$

spin 1 to spin 0 transition -> quark spin flip: only from mass in the eikonal approximation

. full amplitudes (after removing overall phase)

odderon harmonics

$$\tilde{\mathcal{M}}_L = 8\pi N_c eq_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_L(r_{\perp}) \operatorname{sgn}(z - \bar{z}) J_{2k+1}(r_{\perp} \delta_{\perp})$$

$$\tilde{\mathcal{M}}_T = 4\pi i N_c eq_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_T(r_{\perp}) [J_{2k}(r_{\perp} \delta_{\perp}) - J_{2k+2}(r_{\perp} \delta_{\perp})]$$

Final amplitudes: axial vector harmonia

$$\mathcal{A}_{LL}(r_{\perp}) = 0 \quad \longrightarrow \quad \text{no contribution when photon and axial harmonia are longitudinally polarized}$$

$$\mathcal{A}_{LT}(r_{\perp}) \equiv \frac{\sqrt{2}}{\pi} Q K_0(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{A},T}}{\partial r_{\perp}}$$

$$\mathcal{A}_{TL}(r_{\perp}) \equiv \frac{\sqrt{2}}{\pi} \frac{1}{z\bar{z}} \frac{1}{M_{\mathcal{A}}} \left[-m_c^2 K_0(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{A},L}}{\partial r_{\perp}} + \varepsilon K_1(\varepsilon r_{\perp}) \nabla_{\perp}^2 \phi_{\mathcal{A},L} \right]$$

$$\mathcal{A}_{TT}(r_{\perp}) \equiv -\frac{i}{\pi} \frac{z - \bar{z}}{z\bar{z}} \left[\frac{\partial \phi_{\mathcal{A},T}}{\partial r_{\perp}} \varepsilon K_1(\varepsilon r_{\perp}) - m_c^2 K_0(\varepsilon r_{\perp}) \phi_{\mathcal{A},T} \right] \quad \text{only polarization preserving transition}$$

$$\tilde{\mathcal{M}}_i = 4\pi i N_c e q_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_i(r_{\perp}) [J_{2k}(r_{\perp} \delta_{\perp}) - J_{2k+2}(r_{\perp} \delta_{\perp})], \quad i = TL, LT$$

$$\tilde{\mathcal{M}}_{TT} = 8\pi N_c e q_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_{TT}(r_{\perp}) \operatorname{sgn}(z - \bar{z}) J_{2k+1}(r_{\perp} \delta_{\perp})$$

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

Final amplitudes: tensor harmonia

$$\widetilde{\mathcal{M}}_i = -4\pi N_c e q_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_i(r_{\perp}) \text{sign}(z - \bar{z}) [J_{2k+3}(r_{\perp} \delta_{\perp}) + J_{2k-1}(r_{\perp} \delta_{\perp})], \quad i = LT2, TTf$$

$$\widetilde{\mathcal{M}}_i = 4\pi i N_c e q_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_i(r_{\perp}) [J_{2k}(r_{\perp} \delta_{\perp}) - J_{2k+2}(r_{\perp} \delta_{\perp})], \quad i = TT2p, LT, TL,$$

$$\widetilde{\mathcal{M}}_i = 8\pi N_c e q_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_i(r_{\perp}) \text{sgn}(z - \bar{z}) J_{2k+1}(r_{\perp} \delta_{\perp}), \quad i = TTp, LL$$

$$\widetilde{\mathcal{M}}_{TT2f} = 4\pi i N_c e q_c \sum_{k=0}^{\infty} (-1)^k \int_z \int_0^{\infty} r_{\perp} dr_{\perp} \mathcal{O}_{2k+1}(r_{\perp}, \Delta_{\perp}) \mathcal{A}_{TT2f}(r_{\perp}) [J_{2k+4}(r_{\perp} \delta_{\perp}) - J_{2k-2}(r_{\perp} \delta_{\perp})],$$

$$\mathcal{A}_{LT2}(r_{\perp}) \equiv \frac{1}{\pi} (z - \bar{z}) Q K_0(\varepsilon r_{\perp}) \left(\frac{\partial^2 \phi_{\mathcal{T}, T2}}{\partial r_{\perp}^2} - \frac{1}{r_{\perp}} \frac{\partial \phi_{\mathcal{T}, T2}}{\partial r_{\perp}} \right),$$

$$\mathcal{A}_{TT2,p}(r_{\perp}) \equiv -\frac{i}{\sqrt{2\pi}} \frac{1}{z\bar{z}} \left((z^2 + \bar{z}^2) \varepsilon K_1(\varepsilon r_{\perp}) \left(\frac{\partial^2 \phi_{\mathcal{T}, T2}}{\partial r_{\perp}^2} - \frac{1}{r_{\perp}} \frac{\partial \phi_{\mathcal{T}, T2}}{\partial r_{\perp}} \right) + m_c^2 K_0(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{T}, T2}}{\partial r_{\perp}} \right),$$

$$\mathcal{A}_{TT2,f}(r_{\perp}) \equiv \frac{i\sqrt{2}}{\pi} \varepsilon K_1(\varepsilon r_{\perp}) \left(\frac{\partial^2 \phi_{\mathcal{T}, T2}}{\partial r_{\perp}^2} - \frac{1}{r_{\perp}} \frac{\partial \phi_{\mathcal{T}, T2}}{\partial r_{\perp}} \right),$$

$$\mathcal{A}_{LT}(r_{\perp}) \equiv -\frac{i}{2\pi} Q M_{\mathcal{T}} (3 - 4(z^2 + \bar{z}^2)) K_0(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{T}, T}}{\partial r_{\perp}},$$

$$\mathcal{A}_{TT,p}(r_{\perp}) = -\frac{\sqrt{2} M_{\mathcal{T}}}{4\pi} \frac{z - \bar{z}}{z\bar{z}} \left[m_c^2 K_0(\varepsilon r_{\perp}) \phi_{\mathcal{T}, T}(r_{\perp}, z) - (z - \bar{z})^2 \varepsilon K_1(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{T}, T}}{\partial r_{\perp}} \right],$$

$$\mathcal{A}_{TT,f}(r_{\perp}) = -\frac{\sqrt{2} M_{\mathcal{T}}}{\pi} (z - \bar{z}) \varepsilon K_1(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{T}, T}}{\partial r_{\perp}},$$

$$\mathcal{A}_{LL}(r_{\perp}) = -\frac{\sqrt{2} Q}{\sqrt{3\pi}} (z - \bar{z}) K_0(\varepsilon r_{\perp}) (3\nabla_{\perp}^2 - 2m_c^2) \phi_{\mathcal{T}, L}(r_{\perp}, z),$$

$$\mathcal{A}_{TL}(r_{\perp}) = \frac{i}{2\pi\sqrt{3}} \frac{1}{z\bar{z}} \left[\varepsilon K_1(\varepsilon r_{\perp}) (z - \bar{z})^2 (3\nabla_{\perp}^2 - 2m_c^2) \phi_{\mathcal{T}, L} - m_c^2 K_0(\varepsilon r_{\perp}) \frac{\partial \phi_{\mathcal{T}, L}}{\partial r_{\perp}} \right].$$

all overlaps calculated, all amplitudes found

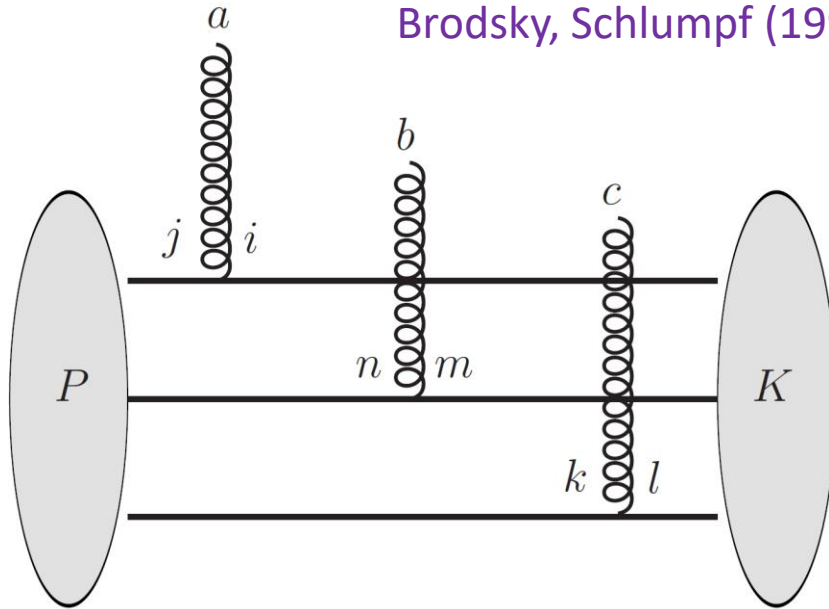
SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

Odderon initial condition

- . a microscopic quark model of the proton

Dumitru, Miller, Venugopalan (2018)

Brodsky, Schlumpf (1994)



- . a key element in incorporating the **Donnachie-Landshoff mechanism**

even a high- t three gluon exchange may not break up the proton

Donnachie, Landshoff (1979)

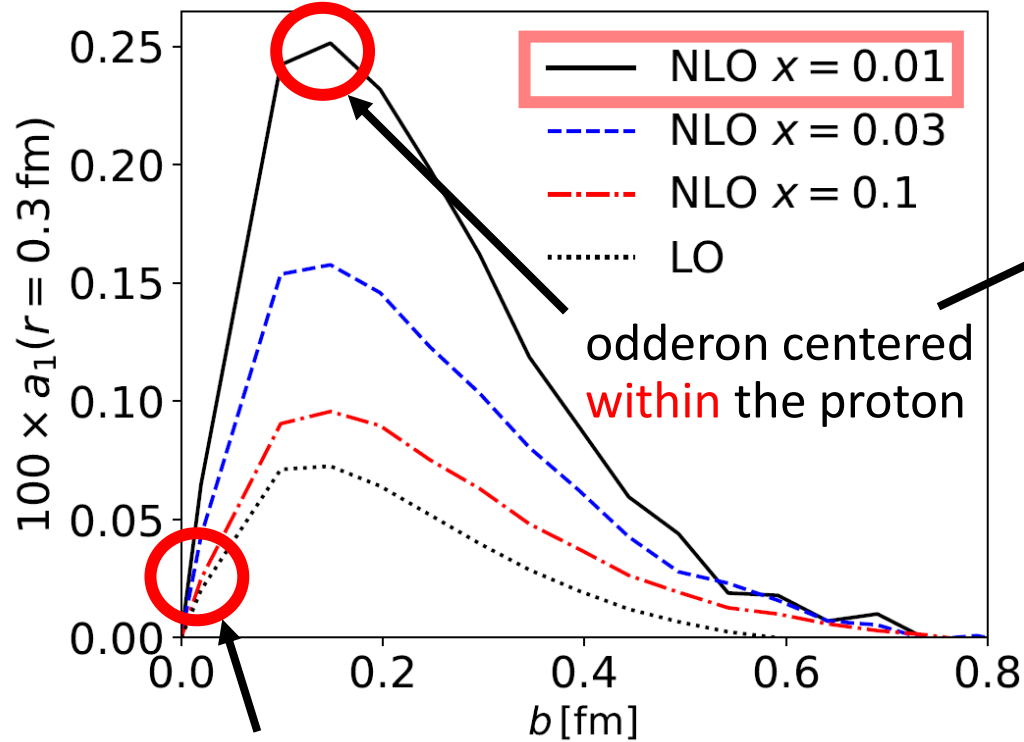
- . model computation **fixes overall sign of the odderon**
- . evolution linear in O -> **odderon sign not changed by evolution**

Odderon evolved

. initial condition from NLO computation by Dumitru, Mantysaari and Paatelainen

- > proton made up of three valence quarks + gluon
- > 100+ diagrams!

we take $\alpha_s(2m_c) \sim 0.25$

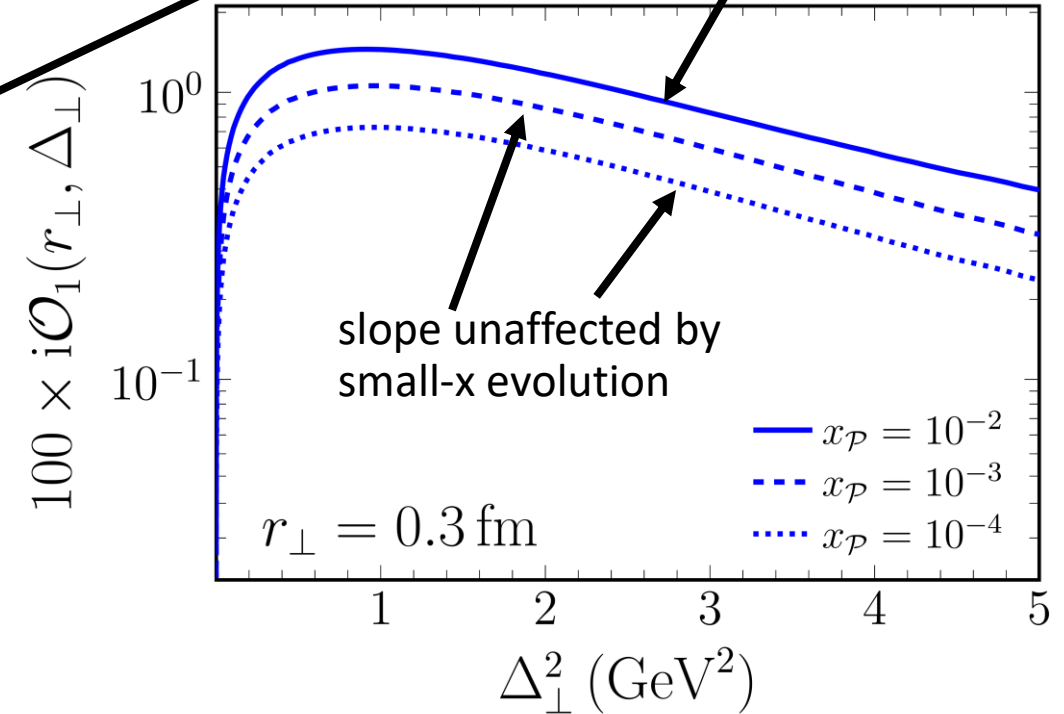


odderon centered within the proton

➔

Fourier transform

Donnachie-Landshoff mechanism



vanishes at the origin

Dumitru, Mantysaari, Paatelainen (2022)
Dumitru, Mantysaari, Paatelainen (2023)

SB, Horvatic, Kaushik, Vivoda (2023)
SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

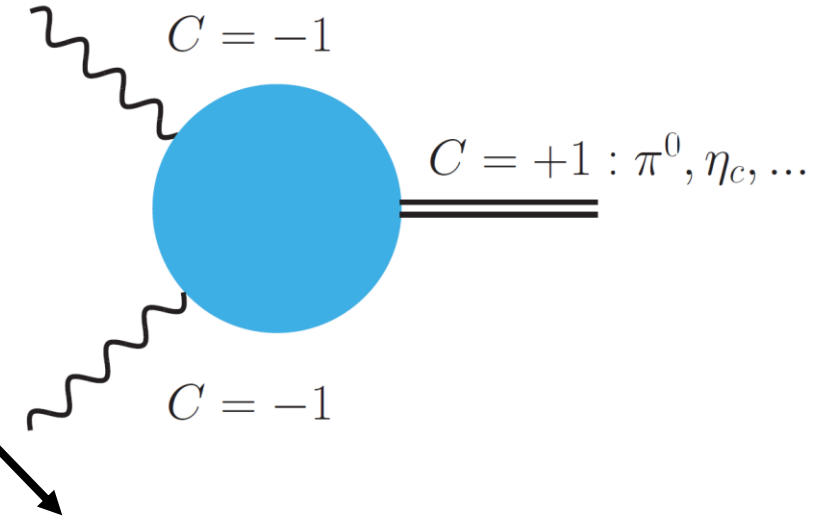
The Primakoff process

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

. replace odderon with photon exchange

$$\gamma^*(q)\gamma^*(\ell) \rightarrow \mathcal{H}(\Delta)$$

$$\mathcal{O}(\mathbf{r}_\perp, \mathbf{\Delta}_\perp) \rightarrow 8\pi i q_c \alpha \sin\left(\frac{\mathbf{\Delta}_\perp \cdot \mathbf{r}_\perp}{2}\right) \frac{F_1(\mathbf{\Delta}_\perp)}{\Delta_\perp^2}$$



charge

form factor

. usually we do not care about QED contributions to QCD process

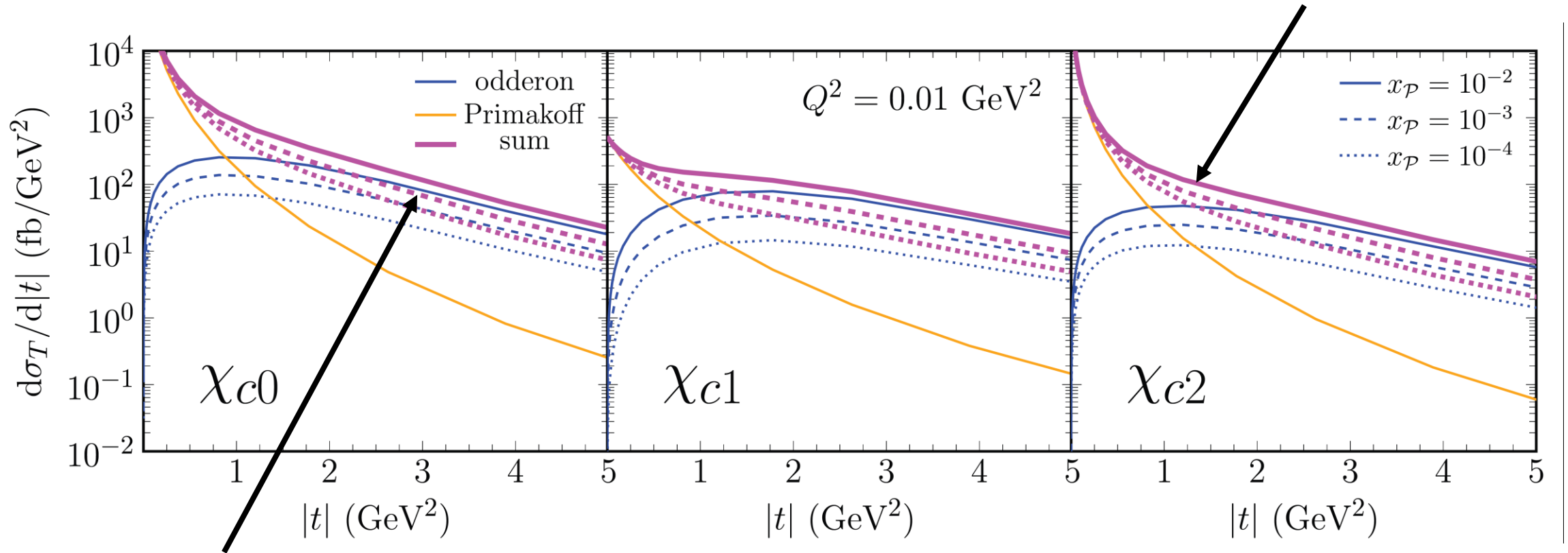
. but in case of odderon QCD cross section is small ($\sim \alpha_s^6$)

-> **Primakoff process becomes a serious background** to the odderon searches

Numerical results: t-distributions

. odderon important after $|t| \sim 1 \text{ GeV}^2$, low t-region dominated by Primakoff

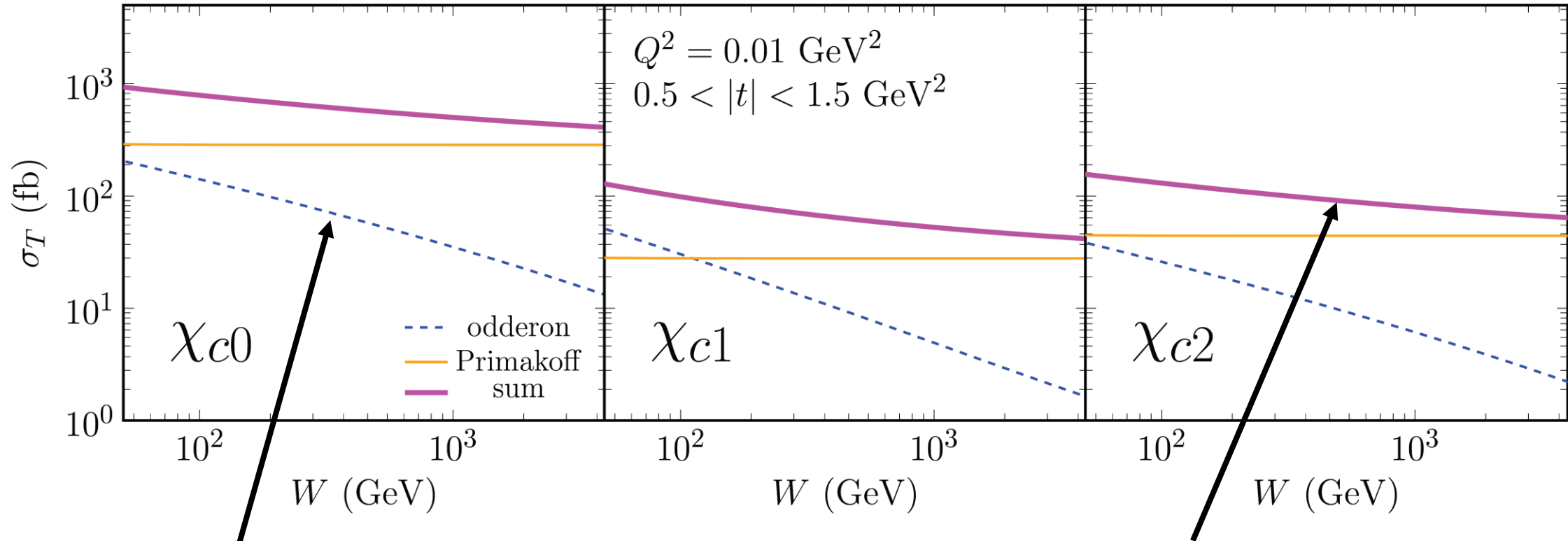
coherent sum of photon+odderon



Donnachie-Landshoff
mechanism

photon and odderon interfere constructively

Numerical results: W distributions

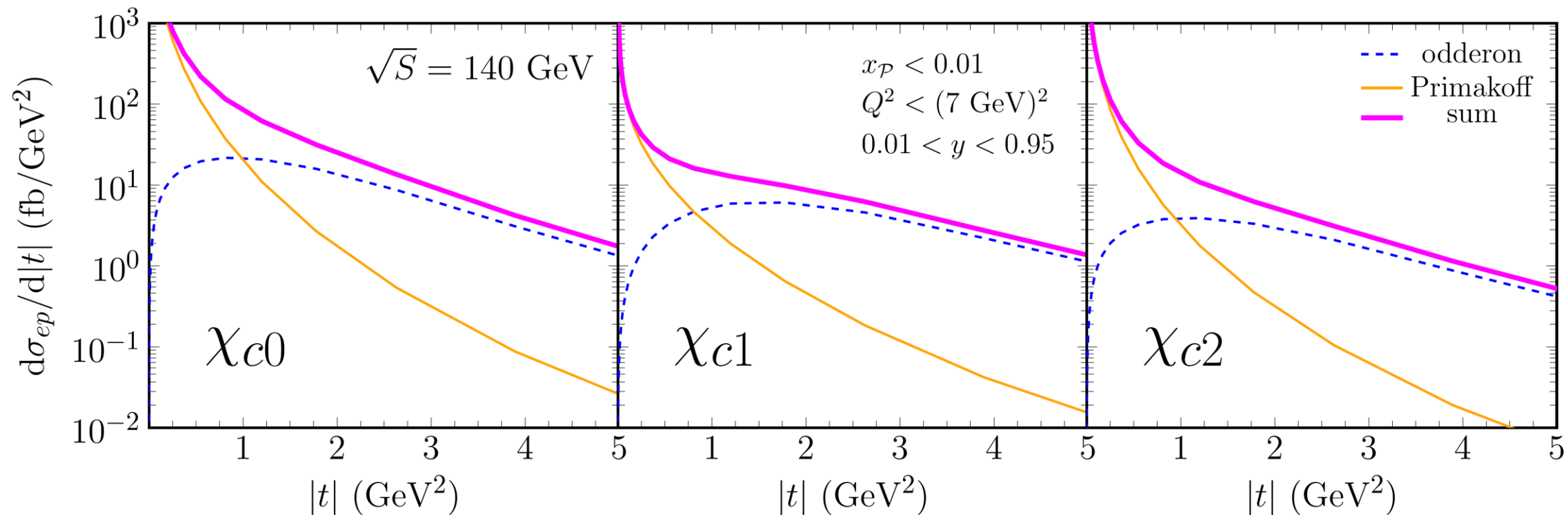


Odderon drops with evolution
(saturation corrections)

coherent sum deviates from the (constant)
Primakoff contribution: **few times higher in
magnitude** and with a **negative slope**

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

Numerical results: t-distributions in electroproduction for EIC kinematics

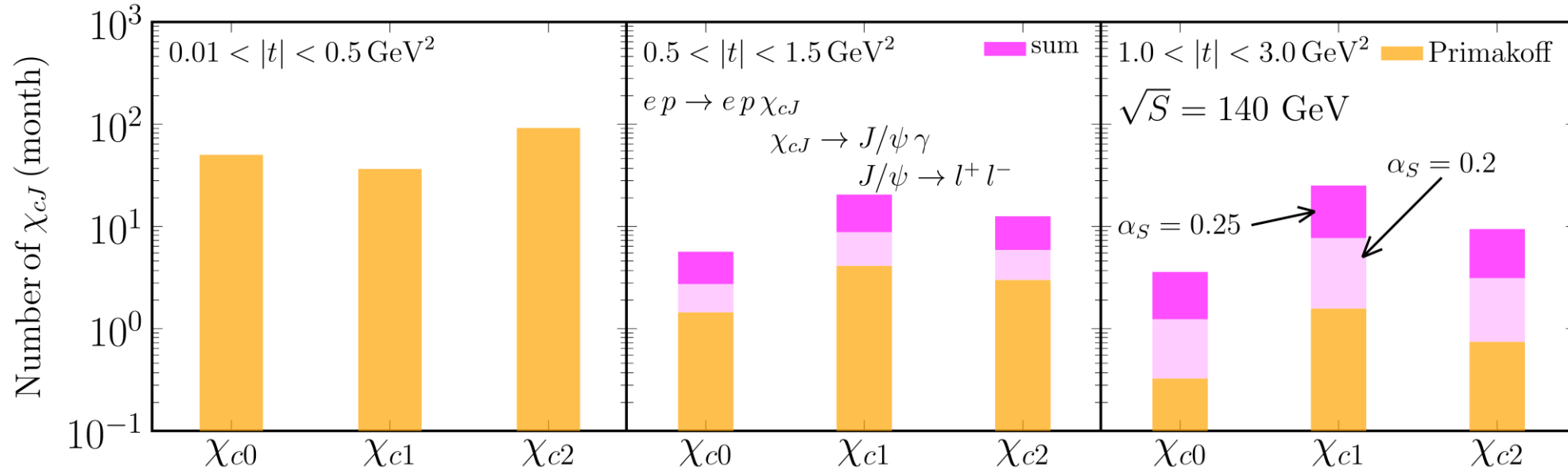


. excess **above the Primakoff contribution** after about $|t| \sim 0.5 \text{ GeV}^2$

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

Expected number of events at the EIC

SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)



- detection channel: $\chi_{cJ} \rightarrow J/\psi + \gamma$
- we predict **excess** in odderon events over Primakoff background
- χ_{c1} most promising (30% BR to $J/\psi + \gamma$): with EIC luminosity $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ expect **~ 30 events/month** (only Primakoff ~ 3 events/month)
- note: at the EIC proton detection is up to $p_T < 1.3 \text{ GeV}$ EIC Yellow report

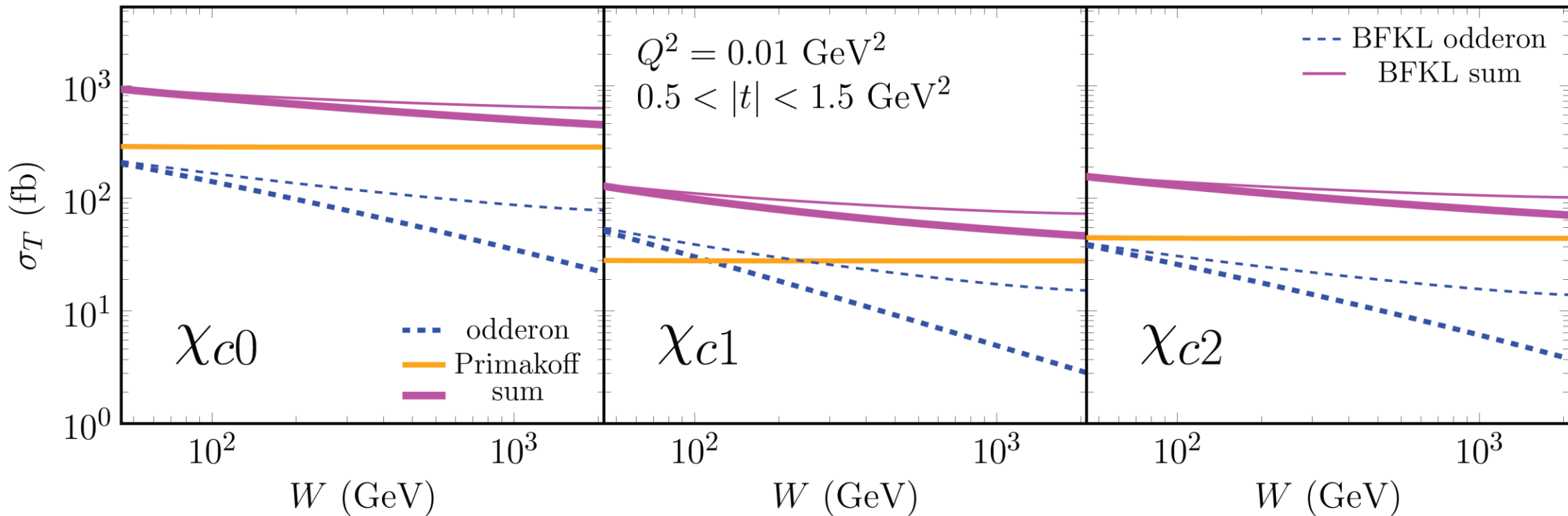
Concluding remarks

- . we suggest exclusive χ_c to detect the odderon at the EIC: a constructive interference with the Primakoff channel leads to an event excess – **we find about a few dozen events per month at the EIC**
- . was not possible at HERA.. (luminosity $\sim 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$)
- . theoretical uncertainties:
 1. χ_c wave functions -> constrain by first detecting the Primakoff channel at low t
 - > can use to calibrate the $\gamma\gamma$ form-factors
 2. value of α_s , QCD corrections..
 3. potential contribution from the gluon Sivers function (spin-dependent odderon)
Boussarie, Hatta, Szymanowski, Wallon (2020)
 - > finite at $t = 0$ -> a computation of the initial condition is required

Numerical results: linear vs nonlinear evolution

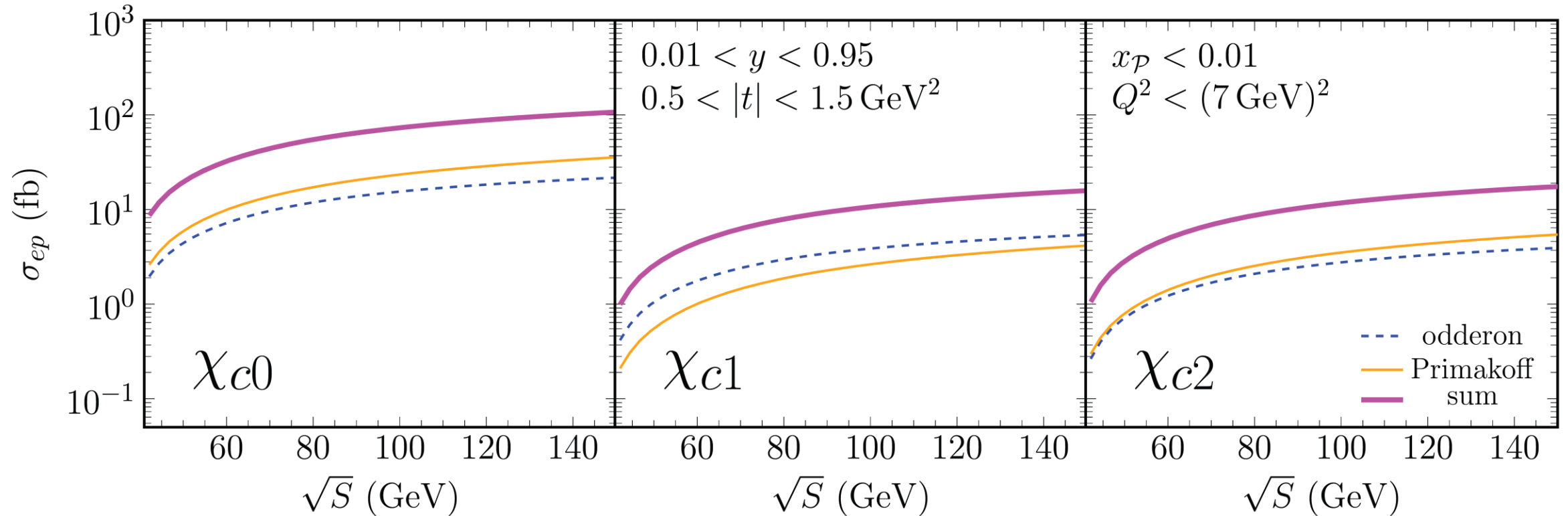
. with linear evolution the cross section flattens to a constant for asymptotically large W - agrees with the Bartels-Lipatov-Vacca odderon

Bartels, Lipatov, Vacca (2000)



SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

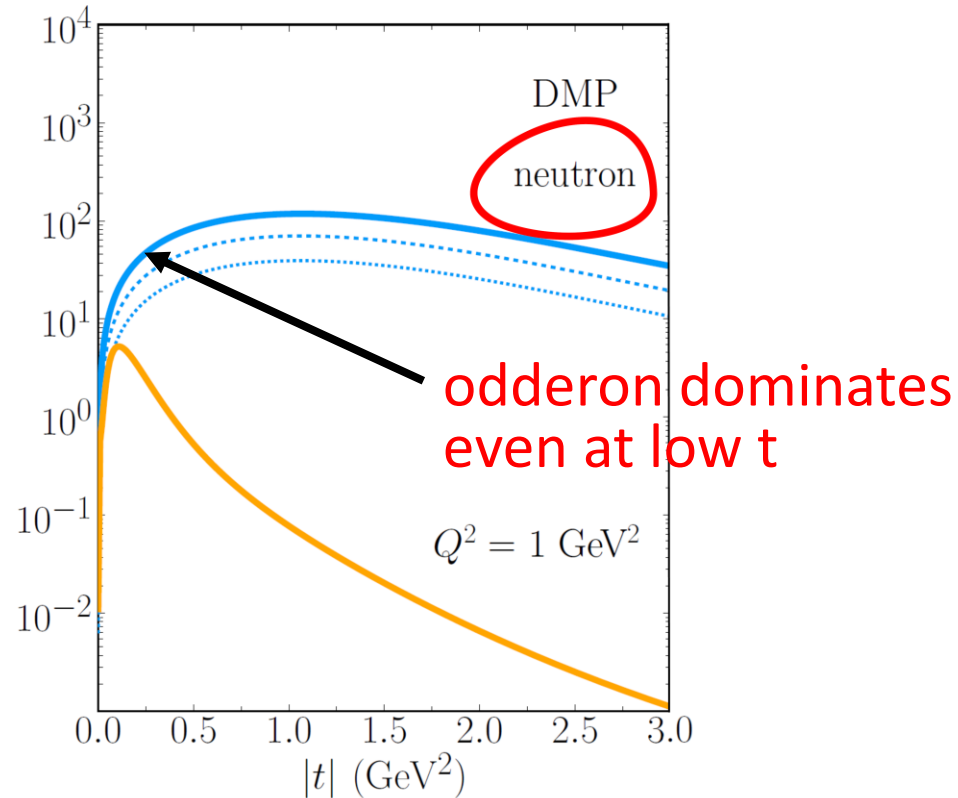
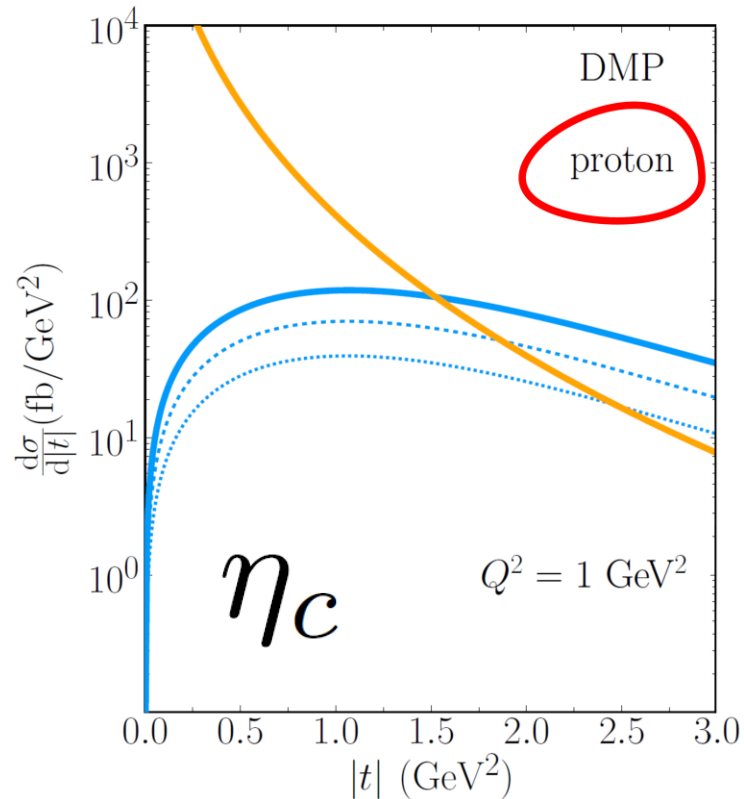
Numerical results: total electroproduction cross section



SB, Dumitru, Kaushik, Motyka, Stebel (in preparation)

Numerical results: neutron target

-> use **neutron** targets to **suppress Primakoff** background



. **measurement prospect**: d or ³He targets with spectator proton

tagging in the forward region

SB, Horvatic, Kaushik, Vivoda (2023)
CLAS (2012)
Friscic et al (2021)